

# Structured CPDs + Week 1 Review

[Help](#)

**Warning:** The hard deadline has passed. You can attempt it, but **you will not get credit for it**. You are welcome to try it as a learning exercise.

☐ In accordance with the Coursera Honor Code, I (Mike Ryan) certify that the answers here are my own work.

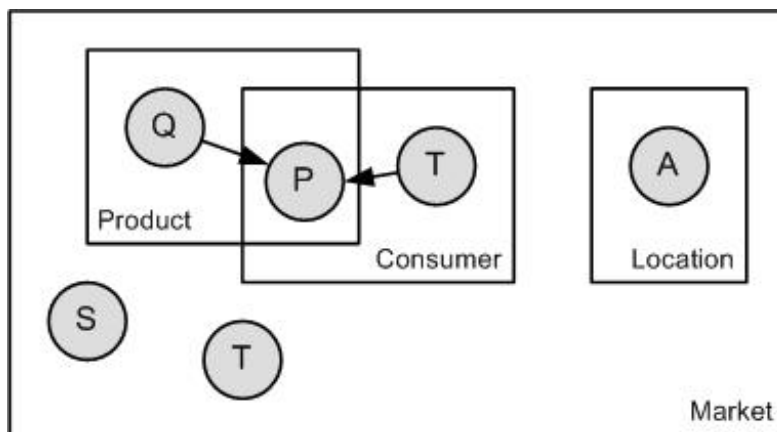
## Question 1

**I-maps.** Suppose  $(A \perp B) \in \mathcal{I}(P)$ , and  $G$  is an I-map of  $P$ . Is it necessarily true that  $(A \perp B) \in \mathcal{I}(G)$ ?

- ☐ No
- ☐ Yes

## Question 2

**Template Models.** Consider the plate model shown below. Assume we are given  $K$  Markets,  $L$  Products,  $M$  Consumers and  $N$  Locations. What is the total number of instances of the variable  $P$  in the grounded BN?



- ☐  $(L \cdot M)^K$

- ☐  $K \cdot (N + (L \cdot M))$
- ☐  $K \cdot L \cdot M \cdot N$
- ☐  $K \cdot L \cdot M$

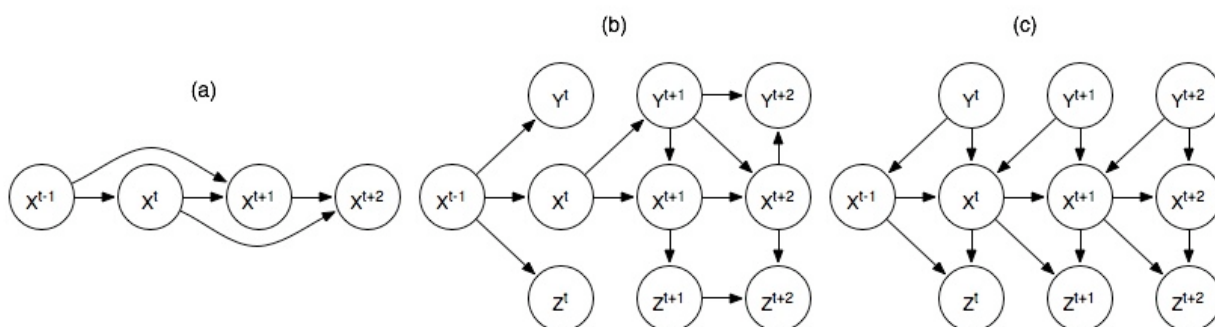
## Question 3

**Template Models.** Consider the plate model from the previous question. What might P represent?

- ☐ Whether a specific product PROD was consumed by consumer C in market M
- ☐ Whether a specific product of brand q was consumed by a consumer with age t in a market of type m that is in location a
- ☐ Whether a specific product PROD was consumed by consumer C in market M that is supervised by supervisor S (assuming that there is exactly 1 unique supervisor per market) and has target audience T (assuming that there is exactly 1 unique target audience per market)
- ☐ Whether a specific product of brand q was consumed by a consumer with age t in a market of type m

## Question 4

**Time-Series Graphs.** Which of the time-series graphs satisfies the Markov assumption? You may select 1 or more options (or none of them, if you think none apply).



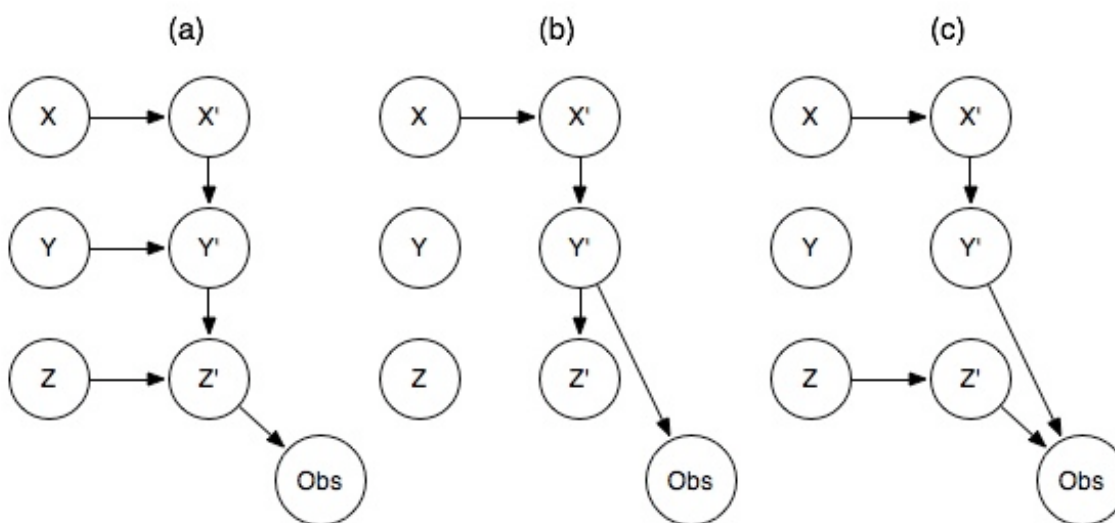
- ☐ (b)
- ☐ (a)

☐ (c)

## Question 5

**\*Unrolling DBNs.** Below are 2-TBNs that could be unrolled into DBNs. Consider these unrolled DBNs (note that there are no edges within the first time-point). In which of them will  $(X^{(t)} \perp Z^{(t)} \mid Y^{(t)})$  hold for all  $t$ , assuming  $Obs^{(t)}$  is observed for all  $t$  and  $X^{(t)}$  and  $Z^{(t)}$  are never observed? You may select 1 or more options (or none of them, if you think none apply).

Hint: Unroll these 2-TBNs into DBNs that are at least 3 time steps long (i.e., involving variables from  $t - 1, t, t + 1$ ).


☐ (b)

☐ (a)

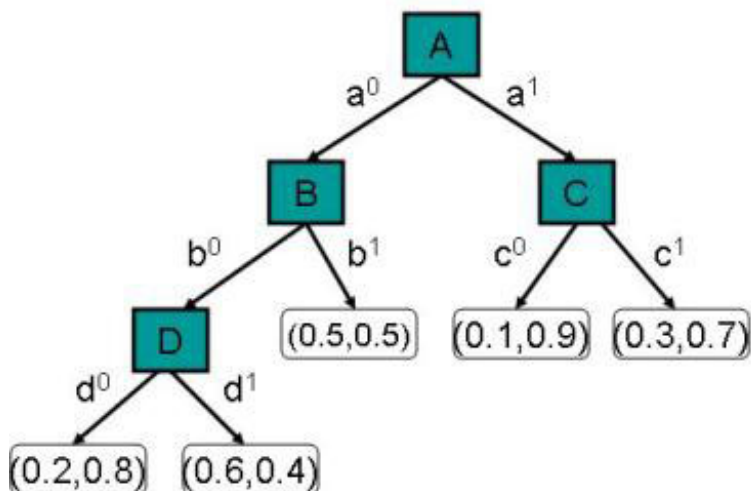
☐ (c)

## Question 6

**Causal Influence.** Consider the CPD below. What is the probability that  $E = e_1$  in the following graph, given an observation  $A = a_0, B = b_0, C = c_1, D = d_1$ ? Note that for the pairs of probabilities that make up the leaves, the probability on the left is the probability of  $e_0$ , and the

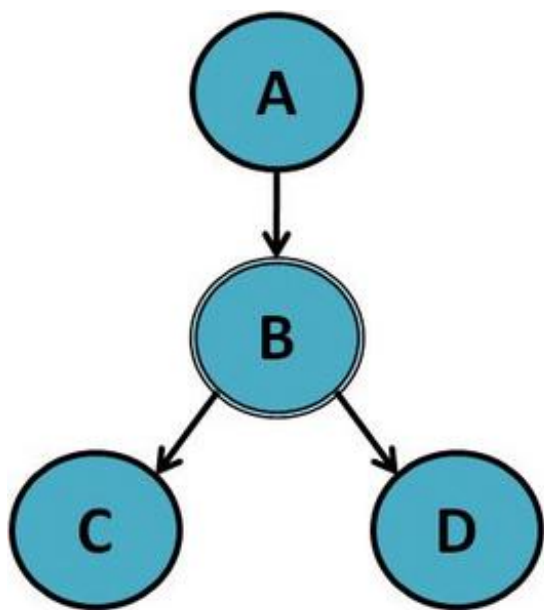
probability on the right is the probability of  $e_1$ .

Tree CPD for  $P(E | A, B, C, D)$




## Question 7

**Independencies with Deterministic Functions.** In the following Bayesian network, the node B is a deterministic function of its parent A. Which of the following is an independence statement that holds in the network? You may select 1 or more options (or none of them, if you think none apply).



- ☐  $(B \perp D \mid C)$
- ☐  $(C \perp D \mid A)$
- ☐  $(A \perp D \mid C)$
- ☐  $(C \perp D \mid B)$

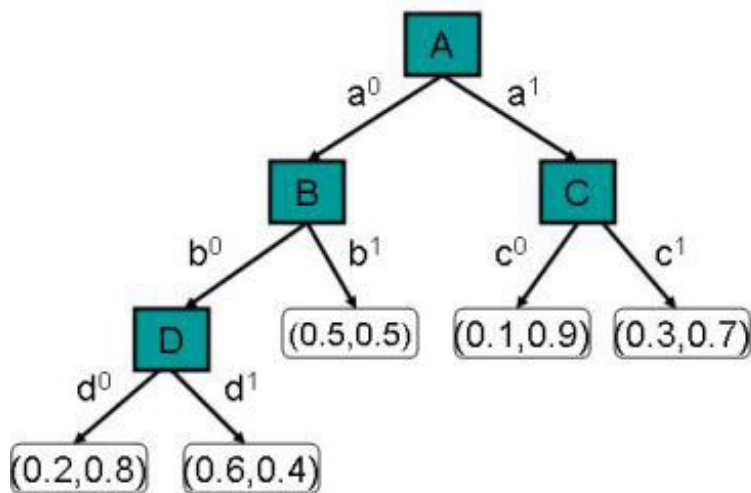
## Question 8

**Independencies in Bayesian Networks.** For the network in the previous question, let B no longer be a deterministic function of its parent A. Which of the following is an independence statement that holds in the modified Bayesian network? You may select 1 or more options (or none of them, if you think none apply).

- ☐  $(A \perp D \mid C)$
- ☐  $(A \perp D \mid B)$
- ☐  $(A \perp B \mid C, D)$
- ☐  $(C \perp D \mid A)$

## Question 9

**Context-Specific Independencies in Bayesian Networks.** Which of the following are context-specific independencies that **do** exist in the tree CPD below? (Note: Only consider independencies in this CPD, ignoring other possible paths in the network that are not shown here. You may select 1 or more options (or none of them, if you think none apply).

Tree CPD for  $P(E \mid A, B, C, D)$ 

- ☐  $(E \perp_c D \mid b^1)$
- ☐  $(E \perp_c C \mid a^0, b^0)$
- ☐  $(E \perp_c D \mid a^0)$
- ☐  $(E \perp_c C \mid b^0, d^0)$

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