

Problem 2:

For 10,000 randomly generated numbers:

K	Number of Recursion Calls	Number of Move Operations
2	19997	25010130
3	19997	25005287
4	19993	12509747
5	19991	10029321
6	19989	8357090
7	19987	7161699
8	19985	6269081
9	19983	5596105
10	19981	5027870

Pseudocode:

Partition(A, lo, hi):

For j from lo to hi:

$l = (lo - 1) + 1$

 If $A[j] \leq A[hi]$

 Swap $\rightarrow A[hi]$ with $A[l]$

 Swap $\rightarrow A[l + 1]$ with $A[hi]$

 Return $l + 1$

QuickSort(A, lo, hi):

 If $\text{len}(\text{inputArray}) \leq 1$:

 Return inputArray

 If $lo < hi$:

 Pivot = Partition(A, lo, hi)

 Quicksort(A, pivot + 1, hi)

 Quicksort(A, lo, pivot - 1)

InsertionSort(A)

For j from 1 to A.length:

 I = j - 1

 While I >= 0 and A[I] > A[j]

 A[I + 1] = A[I]

 I -= 1

 A[I + 1] = A[j]

QuickInsertionSort(A, n, k):

 If n > k:

 QuickSort()

 InsertionSort()

Analysis:

QuickSort():

This is a recursive function that takes in a list to sort, a starting index, and an ending index. It then calls a second function Partition() that takes an element, and sorts the array by placing all the larger elements before it in the array, and the larger elements after it. Once the partition is finished, QuickSort() recursively calls itself to sort the left and right halves of the array. The complexity of Partition() is linear, it is $O(n)$ as it only goes through the array once. The complexity of QuickSort() as a result of this is $O(n \log n)$.

InsertionSort():

This is an iterative algorithm that sorts in place. It iterates through the input list and compares each of the items to its neighbor. If the value is less than its neighbor, it iterates backwards through the list and comparing the item to the sorted list so far. When it encounters another item that is less than the current item, it inserts that value before it in the list. The time complexity of this is $O(n^2)$ as it must traverse the list multiple times.