Data Science Methods - Homework Assignment 2

Group 20: Steffie van Poppel (2031218), Robbie Reyerse (2039047), Mike Weltevrede (1257560)

March 28, 2020

Question 1: Forecasting financial crises

In this exercise, we are asked to apply two methods (we choose to apply a LASSO and a ridge regression) to a dataset on many macroeconomic variables to forecast financial crises. The dataset that we will use was also used by Ward (2017, Journal of Applied Econometrics) where they contrast the performance of one tree with bagging and a random forest against the logit benchmark. We wish to compare our results to those as presented in Table 1.

| | Results | | | | | |
| | **Restricted Selection** | | | **Many Predictors** | | |
Model	AUC	95%-CI	N	AUC	95%-CI	N
Single Tree	0.55	[0.49,0.6]	1816	0.63	[0.56,0.69]	1742
Bagging	**0.77**	[0.73,0.81]	1816	**0.87**	[0.84,0.9]	1742
Random Forest	**0.79**	[0.75,0.83]	1816	**0.88**	[0.86,0.91]	1742
	Specification					
	Restricted Selection			**Many Predictors**		
Parameter	Single	Bagging	RF	Single	Bagging	RF
B	1	5000	5000	1	5000	5000
J_{try}	10	10	3	76	76	9
J		10			76	
# of crises		72			70	

Table 1: Results from Ward (2017).

We first need to do data preparation. We follow the same data preparation procedure as Ward. We are,

however, only interested in the case where "many predictors" are used.

```r
data_path = "data"
df_data   = read.table(paste0(data_path, "/R_class.csv"), sep=",", dec=".",
                         header=TRUE)

ca = grep("ca", names(df_data), value=T)
df_data = df_data[!(names(df_data) %in% c(ca))]

# drop vars not used
stocks = grep("stocks", names(df_data), value=T)
money = grep("money", names(df_data), value=T)
stir = grep("stir", names(df_data), value=T)
assets = grep("assets", names(df_data), value=T)
i = grep("i_", names(df_data), value=T)
ri = grep("ri", names(df_data), value=T)
glo = grep("a_", names(df_data), value=T)

drops = names(df_data) %in% c("year", "ccode", stocks, money, stir, assets, i,
                               ri, glo)
full_om = na.omit(cbind(df_data[glo], df_data[!drops]))
```

Next, we run a LASSO and a ridge regression model. The function that we use for this is `lasso_ridge_sim`. Using the parameter `alpha`, we can specify whether we want a LASSO regression (`alpha=1`) or a Ridge regression (`alpha=0`).

```r
lasso_ridge_sim = function(data, grid_lambda = 10^seq(2, -3, length=100),
                            alpha=1, num_runs=100){

  lambdas = vector("numeric", num_runs)

  if (alpha==1){
    nzeros = vector("numeric", num_runs)
  }

  auc = vector("numeric", num_runs)
  ci95_auc_lo = vector("numeric", num_runs)
  ci95_auc_up = vector("numeric", num_runs)
  precisions = vector("numeric", num_runs)
  recalls = vector("numeric", num_runs)
  f_measures = vector("numeric", num_runs)

  for(j in 1:num_runs) {

    set.seed(j)

    # Select training and test data
    train_labels = sample(1:nrow(data), floor(nrow(data)*0.5))
    train = data[train_labels, ]
    test = data[-train_labels, ]
    train_matrix = model.matrix(b2 ~ ., data=train)
    test_matrix = model.matrix(b2 ~ ., data=test)

    # Train the LASSO/Ridge model
    model = glmnet::cv.glmnet(train_matrix, train[, "b2"], alpha=alpha,
```

```r
                                 lambda=grid_lambda, thresh=1e-12,
                                 family="binomial")

    lambdas[j] = model$lambda.1se

    if (alpha==1){
      nzeros[j] = model$nzero[[which(model$lambda == model$lambda.1se)]]
    }

    # Test the LASSO/Ridge model
    prediction = predict(model, newx=test_matrix, s=model$lambda.1se,
                         type ="class")

    # ROC analysis
    r = pROC::roc(test[, "b2"], as.numeric(prediction), ci=T, quiet=T)
    auc[j] = as.numeric(r$auc)

    ci95_auc_lo[j] = as.numeric(ci.auc(r, conf.level = r$ci[2]))[1]
    ci95_auc_up[j] = as.numeric(ci.auc(r, conf.level = r$ci[2]))[3]

    # Classification evaluation methods
    precisions[j] = caret::precision(factor(prediction, levels=c(0,1)),
                                     factor(test$b2, levels=c(0,1)))
    recalls[j] = caret::recall(factor(prediction, levels=c(0,1)),
                               factor(test$b2, levels=c(0,1)))
    f_measures[j] = caret::F_meas(factor(prediction, levels=c(0,1)),
                                  factor(test$b2, levels=c(0,1)))
}

results = list(auc = mean(auc),
               ci95_auc_lo = mean(ci95_auc_lo),
               ci95_auc_up = mean(ci95_auc_up),
               precision = mean(precisions),
               ci95_precision_lo = mean(precisions) - qnorm(0.975)*
                 sd(precisions) / sqrt(nrow(test_matrix)),
               ci95_precision_up = mean(precisions) + qnorm(0.975)*
                 sd(precisions) / sqrt(nrow(test_matrix)),
               recall = mean(recalls),
               ci95_recall_lo = mean(recalls) - qnorm(0.975)*sd(recalls) /
                 sqrt(nrow(test_matrix)),
               ci95_recall_up = mean(recalls) + qnorm(0.975)*sd(recalls) /
                 sqrt(nrow(test_matrix)),
               f_measure = mean(f_measures),
               ci95_f_measure_lo = mean(f_measures) - qnorm(0.975)*
                 sd(f_measures) / sqrt(nrow(test_matrix)),
               ci95_f_measure_up = mean(f_measures) + qnorm(0.975)*
                 sd(f_measures) / sqrt(nrow(test_matrix)),
               lambda = mean(lambdas),
               ci95_lambdas_lo = mean(lambdas) - qnorm(0.975)*sd(lambdas) /
                 sqrt(nrow(test_matrix)),
               ci95_lambdas_up = mean(lambdas) + qnorm(0.975)*sd(lambdas) /
                 sqrt(nrow(test_matrix))
               )
```

```
  if (alpha == 1){
    results[["nzeros"]] = mean(nzeros)
    results[["ci95_nzeros_lo"]] = mean(nzeros) - qnorm(0.975)*sd(nzeros) /
      sqrt(nrow(test_matrix))
    results[["ci95_nzeros_up"]] = mean(nzeros) + qnorm(0.975)*sd(nzeros) /
      sqrt(nrow(test_matrix))
  }

  return(results)
}


lasso_results = lasso_ridge_sim(full_om)
ridge_results = lasso_ridge_sim(full_om, alpha=0)
```

In addition to the AUC used by Ward, we have also added the precision, recall, and F-measure (AKA the F-Score or the F1-Score) to our analysis. These are commonly used evaluation metrics for categorical response variables. Since our variable is binary, these are applicable. We did not use accuracy as a measure since we have only 140 observations where our variable has value 1 compared to 1602 observations with value 0. As such, the majority class of zeros will overpower the minority class with value 1.

For completeness sake, these are the definitions of the three metrics:

- $Precision = \frac{\#True\ Positives}{\#True\ Positives\ +\ \#False\ Positives}$, i.e. if we predict a crisis, how often is this true?
- $Recall = \frac{\#True\ Positives}{\#True\ Positives\ +\ \#False\ Negatives}$, i.e. out of the total number of crises, how many do we correctly identify?
- $F\text{-}measure = \frac{2 \times Precision \times Recall}{Precision + Recall}$, i.e. the harmonic mean of the precision and recall scores. This balances the precision and recall measures. It is often used to provide an additional check to values of precision and recall.

Given these definitions, we want a high precision if we want to minimise the number of false positives and a high recall when we want to minimise false negatives. In this case, our intuition would be that we would be most interested in the former. That is, we want to minimise the amount of times that a crisis is coming but that we do not identify this rather than minimising the amount of times where we say that a crisis is coming while this is not true. This is because a crisis can have a grave impact on many people in society and we would rather take too many precautions than too few. However, the other case is also not desirable; therefore, the F-measure is also important to consider.

The results from our analysis using the LASSO and ridge regression models can be found in Table 2.

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	Results			
Model	AUC	Precision	Recall	F-measure
LASSO	0.8421	0.9739	0.9823	0.9777
	[0.8143, 0.8699]	[0.9726, 0.9752]	[0.9809, 0.9836]	[0.9775, 0.9779]
Ridge	0.8112	0.9681	0.9922	0.9799
	[0.7736, 0.8489]	[0.9675, 0.9687]	[0.9918, 0.9926]	[0.9797, 0.9801]

	Specification	
Parameter	LASSO	Ridge
λ	0.0162	0.0318
	[0.0158, 0.0166]	[0.031, 0.0325]
Mean # nonzero parameters	3.55	-
	[3.3633, 3.7367]	-

Table 2: Our results (Ranges indicate 95% confidence intervals)

Firstly, we will compare our results to that of Ward using the AUC for the ROC curve (hereafter referred to only as the AUC). After this, we will look into the measures of precision, recall, and the F-measure. We weigh these off to the AUC measure that Ward uses. Lastly, we look into whether these models actually are applicable to the specific data that we are analysing.

To first compare our results with those of Ward, we can only look at the AUC as a quantitative measure since Ward reports no other measures. Ward achieves AUC values of 0.63, 0.87, and 0.88 for the Single Tree, Bagging, and Random Forest methods, respectively. Our analyses using LASSO and ridge regression achieve AUC values of 0.8421 and 0.8112. Because we want to achieve an AUC value as close to 1 as possible, we can see that the LASSO and ridge regressions perform a bit worse than the Bagging and Random Forest methods used by Ward. However, note that AUC is deemed to not be a good metric in case of imbalance in the response as we have explained before. This is because one can achieve a high AUC when the model can identify the majority class well even though it may be very bad at identifying the minority class. Therefore, we think that it would be better to consider precision, recall, and the F-measure.

In that case, we see that the LASSO model achieves the values 0.9739, 0.9823, and 0.9777 for the precision, recall, and F-measure, respectively. The ridge model achieves the values 0.9681, 0.9922, and 0.9799 for the precision, recall, and F-measure, respectively. One can see that the LASSO model has a higher precision while the ridge model achieves a higher recall and F-measure. Following our arguments of before, we should value recall a bit more than precision, though this is not set in stone. Therefore, we can also consider the F-measure as a balance between the two measures. In that case, the ridge model achieves a slightly higher value for the F-measure though not by much. Since the confidence interval of the F-measure for the ridge regression does not include the mean F-measure for the LASSO regression, it is significantly higher for the ridge regression.

We would then say that the choice comes to the final part of our analysis: do these models actually fit the data type? It is important to recognise that the LASSO model sets certain parameters to zero and that the ridge model shrinks them to zero. Although we cannot say that the LASSO model sets all parameters to zero that are truly zero (in exercise 2 we discuss that another model called adaptive LASSO is able to do this for estimation putposes), it seems intuitive that 82 variables are likely too many to describe whether a crisis would occur. The problem comes when we look at how many nonzero parameters LASSO selects, namely only 3.55 (on average). It seems unintuitive that only 3 to 4 parameters can accurately predict whether a crisis will occur. Nonetheless, apparently the LASSO model still does well on the basis of our evaluation metrics so it is not that bad. For the ridge model, some parameters are shrunk towards zero but none are set

equal to zero (with probability 1). As such, all 82 variables are kept in the model but some will have lower coefficients. This makes the model in itself less intuitive to interpret but we are more interested in prediction than estimation so this is not a problem.

All in all, this means that we prefer the ridge model over the LASSO model. Comparing to the models by Ward, we can only use the AUC and our intuition on the applicability of the model to the specific data. On the AUC side, we saw that the AUC values for Ward's models were a bit higher than the LASSO and ridge models. However, also recall that this is not that applicable since the data is imbalanced in the response variable. Therefore, our final conclusion comes to the applicability of the models. Here, we unfortunately do not see a clear reason why we choose one model over the other purely on a theoretical level. As such, we make our conclusion based on the fact that the precision, recall, and F-measure values for the ridge regression model are quite high (also considering the lower bound of its confidence interval); high enough to choose this model over Ward's Random Forest, for example, as we do not have any information on this method's precision, recall, and F-measure.