Synthesizing Indirect Effects in Mediation Models with Meta-Analytic Methods: Supplementary Materials 1

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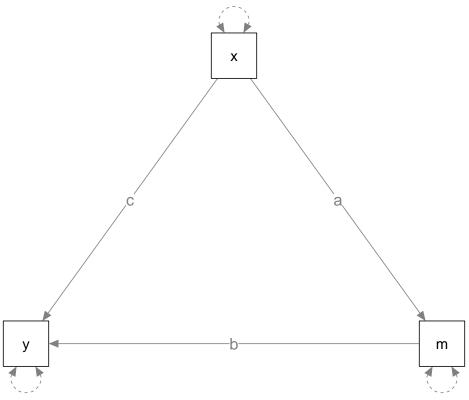
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• This file demonstrates how to compute effect sizes and their sampling covariance matrix with two approaches using the delta method. The first one uses a numeric approach with the structural equation modeling (SEM) framework. The second approach computes the sampling covariance matrix with the symbolic calculations.

Numeric calculations with the SEM approach

One mediator

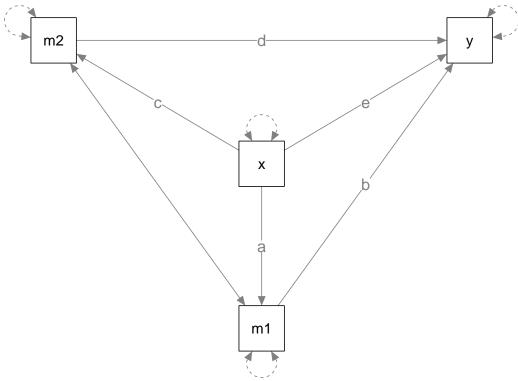


```
## y 1.0 0.5 0.3
## m 0.5 1.0 0.4
## x 0.3 0.4 1.0
```

Calculate the indirect and direct effects and their sampling covariance matrix
calEffSizes(model=model1, n=300, Cov=my.cor)

```
## $ES
## Indirect Direct
## 0.1809524 0.1190476
##
## $VCOV
## Indirect Direct
## Indirect 0.0010416478 -0.0004686319
## Direct -0.0004686319 0.0029289494
```

Two parallel mediators



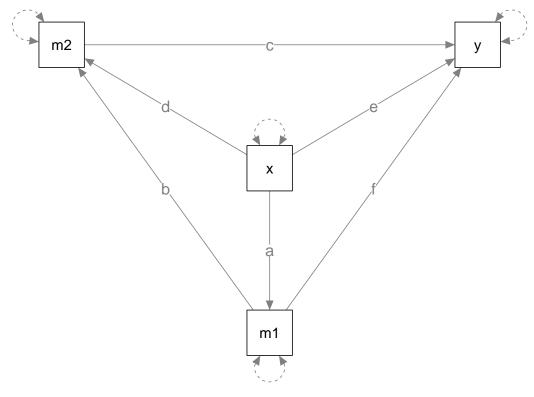
```
## y 1.0 0.5 0.6 0.3
## m1 0.5 1.0 0.4 0.2
## m2 0.6 0.4 1.0 0.3
```

```
## x 0.3 0.2 0.3 1.0
```

Calculate the indirect and direct effects and their sampling covariance matrix
calEffSizes(model=model2, n=300, Cov=my.cor)

```
## $ES
## Ind_m1 Ind_m2 Direct
## 0.05989446 0.13456464 0.10554090
##
## $VCOV
## Ind_m1 Ind_m2 Direct
## Ind_m1 0.0003749419 0.0001029453 -0.0000386612
## Ind_m2 0.0001029453 0.0008190651 -0.0001594774
## Direct -0.0000386612 -0.0001594774 0.0020297130
```

Two serial mediators



```
## Calculate the indirect and direct effects and their sampling covariance matrix
calEffSizes(model=model3, n=300, Cov=my.cor)
## $ES
     Ind m1m2
                 Ind m1
                            Ind m2
                                       Direct
## 0.03177221 0.05989446 0.10279244 0.10554090
## $VCOV
##
                Ind_m1m2
                                Ind_m1
                                              Ind_m2
                                                            Direct
## Ind_m1m2 1.144605e-04 0.0001405997 1.559037e-05 -0.0000376544
           1.405997e-04 0.0003749419 -3.765440e-05 -0.0000386612
## Ind m1
            1.559037e-05 -0.0000376544 6.734239e-04 -0.0001218231
## Ind_m2
```

Direct -3.765440e-05 -0.0000386612 -1.218231e-04 0.0020297130

Symbolic calculations

One mediator

```
library(symSEM)
## fn: The effect sizes
## Covfn: Sampling covariance matrix of fn: "b^2*Va+2*b*a*Cba+a^2*Vb"
## Va: Sampling variance of a
## Vb: Sampling variance of b
## Cba: Sampling covariance of a and b
deltamethod(fn="a*b")
## $fn
##
       [,1]
## fn1 "a*b"
##
## $Covfn
##
       fn1
## fn1 "b^2*Va+2*b*a*Cba+a^2*Vb"
##
## $vars
## [1] "a" "b"
##
## $Covvars
## a
## a "Va" "Cba"
## b "Cba" "Vb"
##
## $Jmatrix
       a
## fn1 "b" "a"
```

Two parallel mediators

```
deltamethod(fn=c("a*b", "c*d"))
## $fn
## [,1]
```

```
## fn1 "a*b"
## fn2 "c*d"
##
## $Covfn
## fn1 "b^2*Va+2*b*a*Cba+a^2*Vb"
                                      "b*Cca*d+b*Cda*c+a*Ccb*d+a*Cdb*c"
## fn2 "d*Cca*b+d*Ccb*a+c*Cda*b+c*Cdb*a" "d^2*Vc+2*d*c*Cdc+c^2*Vd"
## $vars
## [1] "a" "b" "c" "d"
## $Covvars
## a b c d
## a "Va" "Cba" "Cca" "Cda"
## b "Cba" "Vb" "Ccb" "Cdb"
## c "Cca" "Ccb" "Vc" "Cdc"
## d "Cda" "Cdb" "Cdc" "Vd"
##
## $Jmatrix
## a b c d
## fn1 "b" "a" "0" "0"
## fn2 "0" "0" "d" "c"
```

Two serial mediators

```
deltamethod(fn="a*b*c")
```

Matrix products: default

```
## $fn
## [,1]
## fn1 "a*b*c"
##
## $Covfn
## fn1 "b^2*c^2*Va+2*b^2*c*a*Cca+b^2*a^2*Vc+2*b*c^2*a*Cba+2*b*c*a^2*Ccb+c^2*a^2*Vb"
## $vars
## [1] "a" "b" "c"
##
## $Covvars
## a b
## a "Va" "Cba" "Cca"
## b "Cba" "Vb" "Ccb"
## c "Cca" "Ccb" "Vc"
##
## $Jmatrix
## a b
## fn1 "b*c" "a*c" "a*b"
sessionInfo()
## R version 4.0.3 (2020-10-10)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Ubuntu 20.04.2 LTS
```

```
/usr/lib/x86_64-linux-gnu/blas/libblas.so.3.9.0
## LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.9.0
##
## locale:
##
   [1] LC_CTYPE=en_SG.UTF-8
                                   LC NUMERIC=C
                                   LC COLLATE=en SG.UTF-8
##
  [3] LC TIME=en SG.UTF-8
                                    LC MESSAGES=en SG.UTF-8
  [5] LC MONETARY=en SG.UTF-8
##
   [7] LC_PAPER=en_SG.UTF-8
                                   LC NAME=C
##
  [9] LC_ADDRESS=C
                                   LC TELEPHONE=C
## [11] LC_MEASUREMENT=en_SG.UTF-8 LC_IDENTIFICATION=C
## attached base packages:
## [1] stats
                 graphics
                          grDevices utils
                                                                    base
                                                datasets methods
##
## other attached packages:
## [1] symSEM_0.1.1
                       metaSEM_1.2.5.1 OpenMx_2.19.5
##
## loaded via a namespace (and not attached):
##
     [1] nlme_3.1-152
                             RColorBrewer_1.1-2
                                                  rprojroot_1.3-2
##
     [4] mi 1.0
                             tools 4.0.3
                                                  backports_1.2.1
##
     [7] R6_2.5.0
                             rpart_4.1-15
                                                  Hmisc_4.4-1
                             nnet_7.3-14
                                                  withr 2.3.0
   [10] colorspace_1.4-1
                                                  mnormt_2.0.2
##
   [13] tidyselect 1.1.0
                             gridExtra 2.3
                             fdrtool 1.2.15
##
   [16] compiler 4.0.3
                                                  qgraph_1.6.9
##
  [19] htmlTable 2.1.0
                             regsem_1.6.2
                                                  desc_1.2.0
  [22] scales_1.1.1
                             checkmate_2.0.0
                                                  psych_2.0.9
##
   [25] mvtnorm_1.1-1
                             pbapply_1.4-3
                                                  sem_3.1-11
##
   [28] stringr_1.4.0
                             digest_0.6.27
                                                  pbivnorm_0.6.0
##
                                                  rmarkdown_2.7
  [31] foreign_0.8-80
                             minqa_1.2.4
  [34] base64enc_0.1-3
                             jpeg_0.1-8.1
                                                  pkgconfig_2.0.3
##
   [37] htmltools_0.5.0
                             lme4_1.1-26
                                                  lisrelToR_0.1.4
##
   [40] htmlwidgets_1.5.2
                             rlang_0.4.10
                                                  rstudioapi_0.11
##
   [43] generics_0.0.2
                             gtools_3.8.2
                                                  dplyr_1.0.2
##
   [46] zip_2.1.1
                                                  Formula_1.2-3
                             magrittr_1.5
##
    [49] Matrix 1.2-18
                                                  munsell 0.5.0
                             Rcpp_1.0.5
##
                             rockchalk_1.8.144
  [52] abind_1.4-5
                                                  lifecycle_0.2.0
## [55] stringi 1.5.3
                             yaml 2.2.1
                                                  carData 3.0-4
##
  [58] MASS_7.3-53
                                                  matrixcalc_1.0-3
                             plyr_1.8.6
   [61] lavaan_0.6-8
                                                  parallel_4.0.3
##
                             grid_4.0.3
##
  [64] crayon_1.3.4
                             lattice_0.20-41
                                                  semPlot_1.1.2
  [67] kutils 1.70
                             splines_4.0.3
                                                  Ryacas 1.1.3.1
##
   [70] tmvnsim 1.0-2
                             knitr_1.30
                                                  pillar_1.4.6
##
   [73] igraph_1.2.6
                             boot_1.3-25
                                                  corpcor_1.6.9
##
                                                  stats4_4.0.3
  [76] pkgload_1.1.0
                             reshape2_1.4.4
  [79] XML_3.99-0.5
                             glue_1.4.2
                                                  evaluate_0.14
##
   [82] latticeExtra_0.6-29 data.table_1.13.2
                                                  png_0.1-7
##
   [85] vctrs_0.3.4
                             nloptr_1.2.2.2
                                                  testthat_3.0.2
##
   [88] gtable_0.3.0
                             purrr_0.3.4
                                                  assertthat_0.2.1
                                                  openxlsx_4.2.2
   [91] ggplot2_3.3.2
                             xfun_0.19
   [94] xtable_1.8-4
                             coda_0.19-4
                                                  Rsolnp_1.16
## [97] glasso_1.11
                             survival_3.2-7
                                                  truncnorm_1.0-8
## [100] tibble_3.0.4
                             arm_1.11-2
                                                  ellipse_0.4.2
## [103] cluster_2.1.0
                             statmod_1.4.35
                                                  ellipsis_0.3.1
```