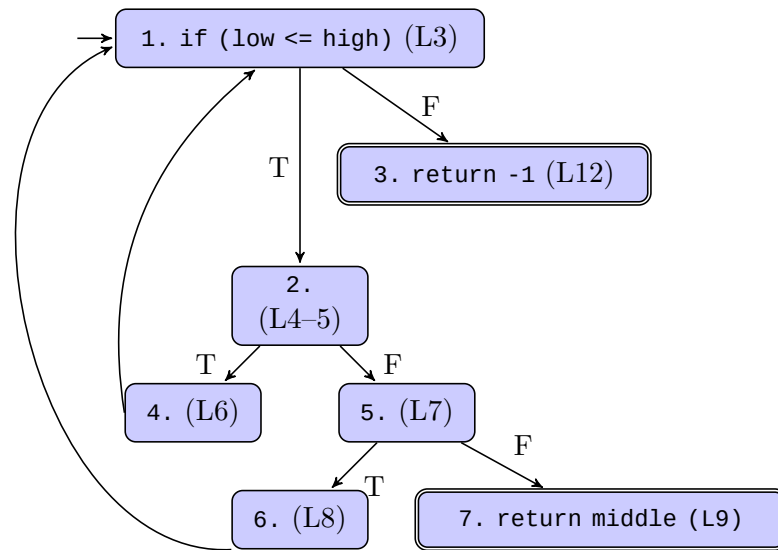


**Larger CFG example.** You can draw a 7-node CFG for this program:

```

1  /** Binary search for target in sorted subarray a[low..high] */
2  int binary_search(int[] a, int low, int high, int target) {
3      while (low <= high) {
4          int middle = low + (high-low)/2;
5          if (target < a[middle])
6              high = middle - 1;
7          else if (target > a[middle])
8              low = middle + 1;
9          else
10             return middle;
11     }
12     return -1; /* not found in a[low..high] */
13 }

```



Here are more exercise programs that you can draw CFGs for.

```

1  /* effects: if x==null, throw NullPointerException
2             otherwise, return number of elements in x that are odd, positive or both. */
3  int oddOrPos(int[] x) {
4      int count = 0;
5      for (int i = 0; i < x.length; i++) {
6          if (x[i]%2 == 1 || x[i] > 0) {
7              count++;
8          }
9      }
10     return count;
11 }
12
13 // example test case: input: x=[-3, -2, 0, 1, 4]; output: 3

```

Finally, we have a really poorly-designed API (I'd give it a D at most, maybe an F) because it's impossible to succinctly describe what it does. **Do not design functions with interfaces like this.** But we can still draw a CFG, no matter how bad the code is.

```

1  /** Returns the mean of the first maxSize numbers in the array,
2      if they are between min and max. Otherwise, skip the numbers. */
3  double computeMean(int[] value, int maxSize, int min, int max) {
4      int i, ti, tv, sum;
5
6      i = 0; ti = 0; tv = 0; sum = 0;
7      while (ti < maxSize) {
8          ti++;
9          if (value[i] >= min && value[i] <= max) {
10             tv++;
11             sum += value[i];
12         }
13         i++;
14     }
15     if (tv > 0)
16         return (double)sum/tv;
17     else
18         throw new IllegalArgumentException();
19 }

```

## Statement and Branch Coverage

We defined Control-Flow Graphs so that we can give principled definitions of statement and branch coverage. We can start with the definition of a test path:

**Definition 1** A test path is a path  $p$  (possibly of length 0) that starts at some initial node (i.e. in  $N_0$ ) and ends at some final node (i.e. in  $N_f$ ).

Here's a definition of coverage for graphs:

**Definition 2** Given a set of test requirements  $TR$  for a graph criterion  $C$ , a test set  $T$  satisfies  $C$  on graph  $G$  iff for every test requirement  $tr$  in  $TR$ , at least one test path  $p$  in  $path(T)$  exists such that  $p$  satisfies  $tr$ .

We'll use this notion to define a number of standard testing coverage criteria. But first, what are test paths?

**Test cases and test paths.** We connect test cases and test paths with a mapping  $path_G$  from test cases to test paths; e.g.  $path_G(t)$  is the set of test paths corresponding to test case  $t$ .

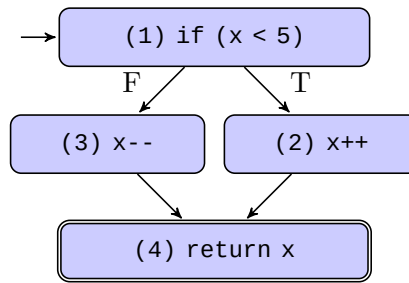
- usually we just write  $path$  since  $G$  is obvious from the context.
- we can lift the definition of  $path$  to test sets  $T$  by defining  $path(T) = \{path(t) | t \in T\}$ .
- each test case gives at least one test path. If the software is deterministic, then each test case gives exactly one test path; otherwise, multiple test cases may arise from one test path.

**Example.** Here is a short method, the associated control-flow graph, and some test cases and test paths.

```

1  int foo(int x) {
2    if (x < 5) {
3      x ++;
4    } else {
5      x --;
6    }
7    return x;
8  }

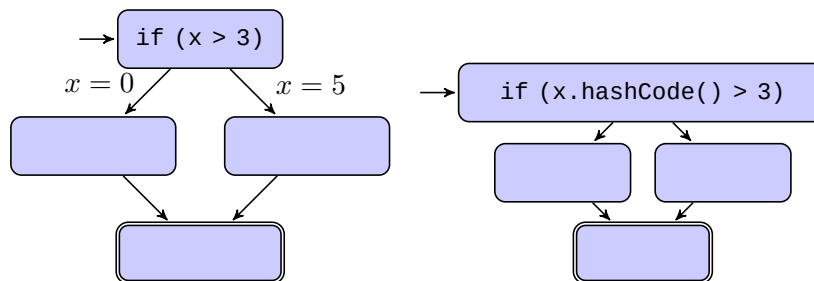
```



- Test case:  $x = 5$ ; test path:  $[(1), (3), (4)]$ .
- Test case:  $x = 2$ ; test path:  $[(1), (2), (4)]$ .

Note that (1) we can deduce properties of the test case from the test path; and (2) in this example, since our method is deterministic, the test case determines the test path.

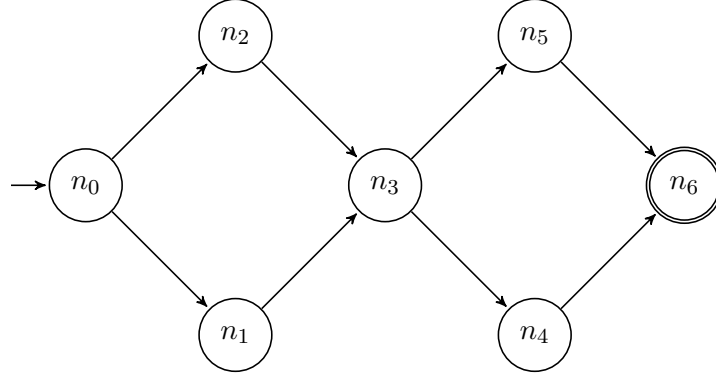
**Nondeterminism.** I mentioned the mapping between test cases and test paths above. The mapping is not one-to-one for nondeterministic code. Here's an example of deterministic and non-deterministic control-flow graphs:



Causes of nondeterminism include dependence on inputs; on the thread scheduler; and on memory addresses, for instance as seen in calls to the default Java `hashCode()` implementation.

Nondeterminism makes it hard to check test case output, since more than one output might be a valid result of a single test input.

As another (more abstract) example, consider the double-diamond graph  $D$ .



Here are the four test paths in  $D$ :

$$\begin{aligned} &[n_0, n_1, n_3, n_4, n_6] \\ &[n_0, n_1, n_3, n_5, n_6] \\ &[n_0, n_2, n_3, n_4, n_6] \\ &[n_0, n_2, n_3, n_5, n_6] \end{aligned}$$

For the *statement coverage* criterion, we get the following test requirements:

$$\{n_0, n_1, n_2, n_3, n_4, n_5, n_6\}$$

That is, any test set  $T$  which satisfies statement coverage on  $D$  must include test cases  $t$ ; the cases  $t$  give rise to test paths  $\text{path}(t)$ , and some path must include each node from  $n_0$  to  $n_6$ . (No single path must include all of these nodes; the requirement applies to the set of test paths.)

Let's formally define statement coverage.

**Definition 3** *Statement coverage:* For each node  $n \in \text{reach}_G(N_0)$ , TR contains a requirement to visit node  $n$ .

For our example,

$$TR = \{n_0, n_1, n_2, n_3, n_4, n_5, n_6\}.$$

Let's consider an example of a test set which satisfies statement coverage on  $D$ .

Start with a test case  $t_1$ ; assume that executing  $t_1$  gives the test path

$$\text{path}(t_1) = p_1 = [n_0, n_1, n_3, n_4, n_6].$$

Then test set  $\{t_1\}$  does not give statement coverage on  $D$ , because no test case covers node  $n_2$  or  $n_5$ . If we can find a test case  $t_2$  with test path

$$\text{path}(t_2) = p_2 = [n_0, n_2, n_3, n_5, n_6],$$

then the test set  $T = \{t_1, t_2\}$  satisfies statement coverage on  $D$ .

What is another test set which satisfies statement coverage on  $D$ ?

Here is a more verbose definition of statement coverage.

**Definition 4** *Test set  $T$  satisfies statement coverage on graph  $G$  if and only if for every syntactically reachable node  $n \in N$ , there is some path  $p$  in  $\text{path}(T)$  such that  $p$  visits  $n$ .*

A second standard criterion is that of branch coverage.

**Criterion 1 Branch Coverage.** *TR contains each reachable path of length up to 1, inclusive, in  $G$ .*

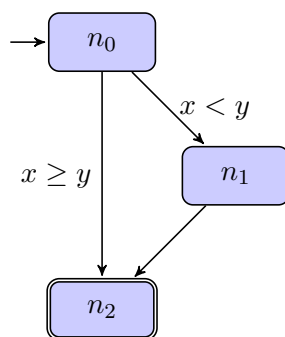
Here are some examples of paths of length  $\leq 1$ :

Note that since we're not talking about *test paths*, these reachable paths need not start in  $N_0$ .

In general, paths of length  $\leq 1$  consist of nodes and edges. (Why not just say edges?)

Saying “edges” on the above graph would not be the same as saying “paths of length  $\leq 1$ ”.

**Another example.** Here is a more involved example:



Let's define

$$\begin{aligned} \text{path}(t_1) &= [n_0, n_1, n_2] \\ \text{path}(t_2) &= [n_0, n_2] \end{aligned}$$

Then

$$\begin{aligned} T_1 &= \langle ? \rangle \{t_1\} && \text{satisfies statement coverage} && \text{but not branch coverage} \\ T_2 &= \langle ? \rangle \{t_1, t_2\} && \text{satisfies branch coverage} \end{aligned}$$

# Web Applications

Frontends  
HTML, CSS, JS  
(client-side)

vs

Backends  
Web server, Database, PHP, Node.js  
(server-side)

Testing Frontend:

- rendering
- cross-browser (frontend)
- wrong value errors
- malware
- performance
- cache issues

Testing Backend:

- Dev Ops  
(simulations of failures)
- responsiveness to requests
- data persistence
- security (SQL injection prevention)
- race conditions
- performance testing

About coverage:

- often 80% statement coverage is good enough
- statement coverage is not sufficient for being a good test suite. need good asserts and other coverage
- complete path coverage: cover paths of all lengths