

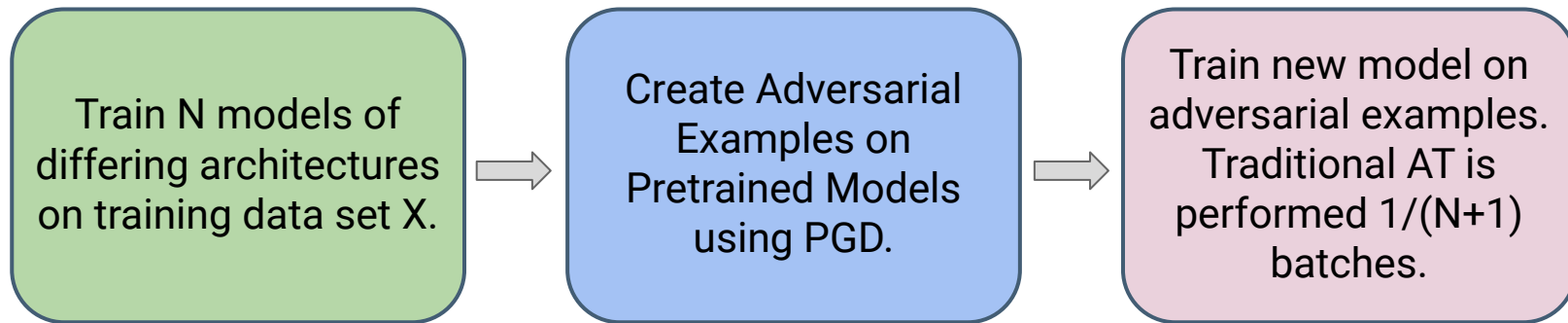
# **Inclusion-Exclusion Enhanced Ensemble Adversarial Training**

Group 6: Henry Shugart, Mikhal Ben-Joseph,  
Yesh Munagala, Judy Chao

STOR 566 Fall 2022

# Background: What is Ensemble Adversarial Training?

Ensemble AT is a training technique that utilizes several pre-trained models to produce transferable adversarial examples. These examples are then used to enrich training data for a new model.



# Understanding the Problem

## Ensemble Adversarial Training

### Advantages



- Improves robustness against black box transfer attacks
- Decouples adversarial attack generation from training (Faster than traditional AT)

Vs

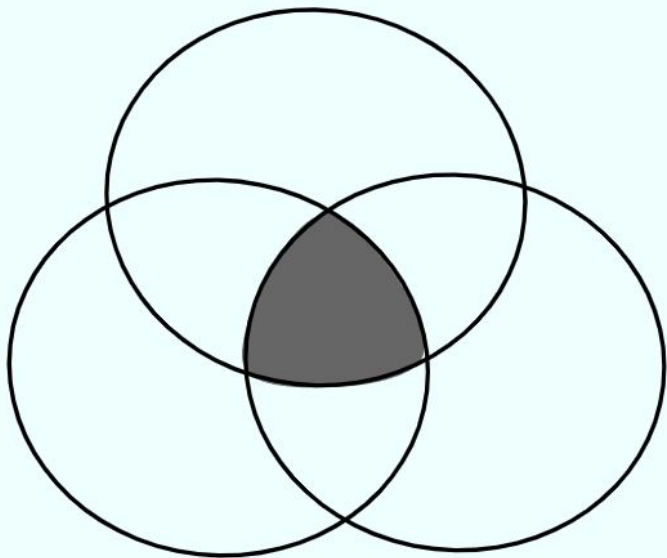
### Disadvantages



- Decreased robustness to white-box attacks like FGSM, PGD
- Lower accuracy on natural images

**GOAL:** Build on Ensemble AT with Inclusion-Exclusion and Min-Max Optimization

## Background: How Does Our Approach Differ?



### Adversarial Space:

$$A_n = \left\{ \hat{X} \in R^n \mid M(\hat{X}) \neq y, |\hat{X} - X| \leq \epsilon \right\}$$

**Original coverage of the adversarial space with ensemble AT:**

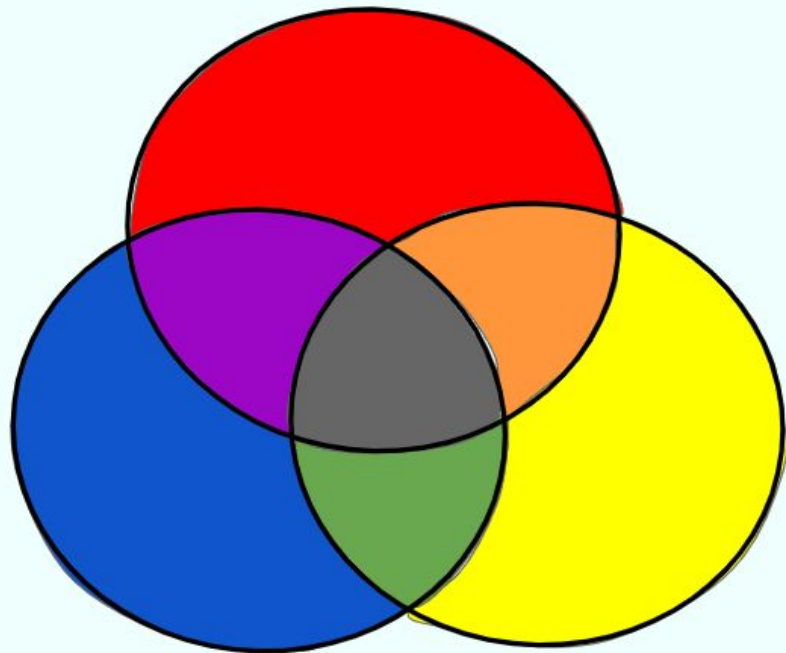
Each pre-trained model is fooled separately:

$$x_1 \in A_{M_1}, x_2 \in A_{M_2}, x_3 \in A_{M_3}$$

Because of the transferability of adversarial perturbations we expect the majority of these perturbations to exist in

$$x_1, x_2, x_3 \in A_{M_1} \cap A_{M_2} \cap A_{M_3}$$

## Background: How Does Our Approach Differ?



**Using Inclusion-Exclusion Idea:**

Fooling different subsets each time

$$\{A_{M_1} \cap A_{M_2} \cap A_{M_3}^C\}, \{A_{M_1}^C \cap A_{M_2} \cap A_{M_3}\}$$

We do this by using an APGDA method proposed in Wang et al.

# APGDA for Construction of Adversarial Examples

## APGDA

An alternating projected gradient ascent descent algorithm was proposed in Wang et al. to solve min-max optimization problems of the form and showed improved attack success rates against multiple models

$$\max_{\|\delta\|_\infty \leq \varepsilon} \min_{w \in \omega} \sum_{i=1}^N w_i \ell(M_i(X + \delta), Y)$$
$$\omega = \{w \mid \mathbf{1}^T w = 1, w \geq 0\}$$

## Inclusion Exclusion

For models being fooled we use

$$\hat{\ell}(\delta) = \ell(M_i(X + \delta), Y)$$

For models we do not intend to fool we use

$$\hat{\ell}(\delta) = \alpha - \beta \ell(M_i(X + \delta), Y)$$
$$\alpha, \beta \geq 0$$

We approximate the solution of the inner minimization with the sparsemax function proposed in Martins and Astudillo.

# Method

## 1 Generate adversarial examples for CIFAR-10

$2^3 - 1 = 7$  combinations of 50,000 perturbed images

## 2 Train a model with enriched training data

Finetune pre-trained VGG-11 model

## 3 Train the same model with traditional AT, regular EAT

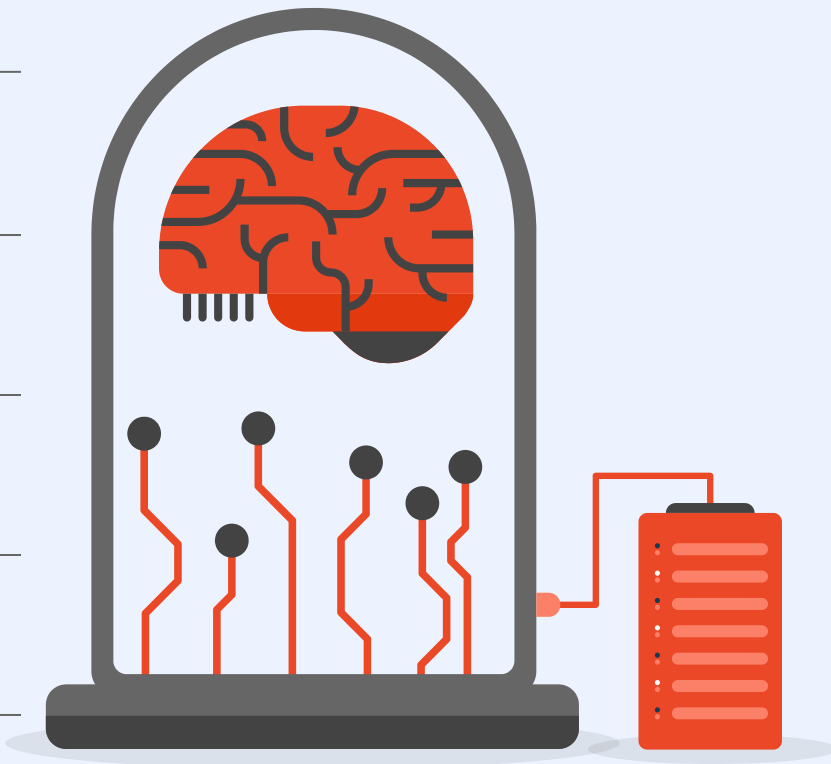
Produce baseline comparisons

## 4 Implement black and white box attacks

Transfer, FGSM, i-FGSM attacks from holdout models

## 5 Evaluate Performance

Compare attack performance on the four models



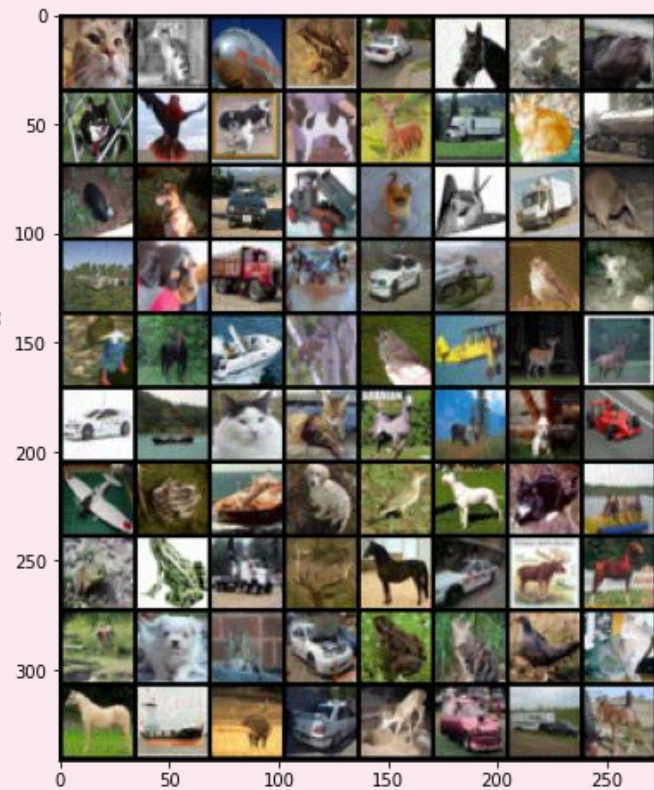
# Before/After Adversarial Perturbations



+ 0.0625 x



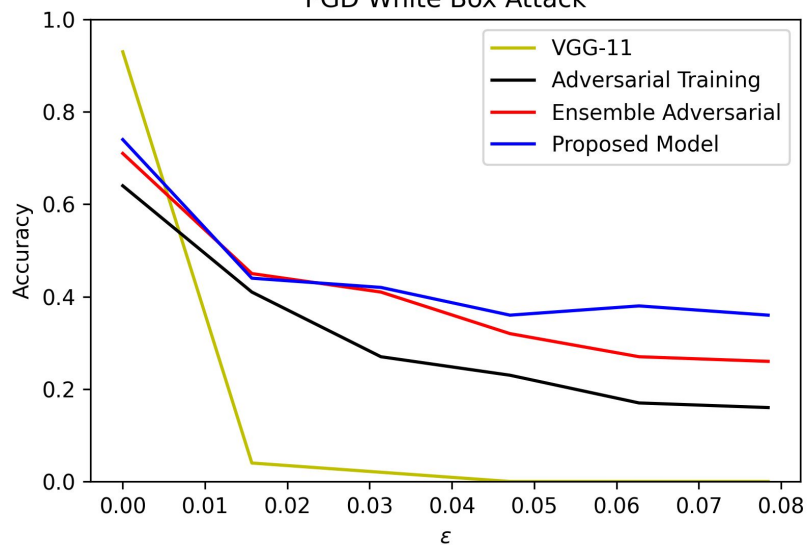
=



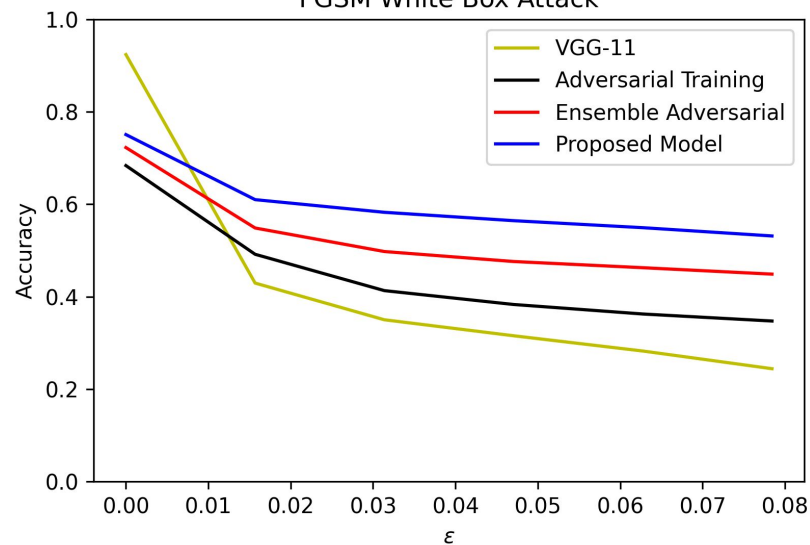


# Results - White Box Robustness

PGD White Box Attack

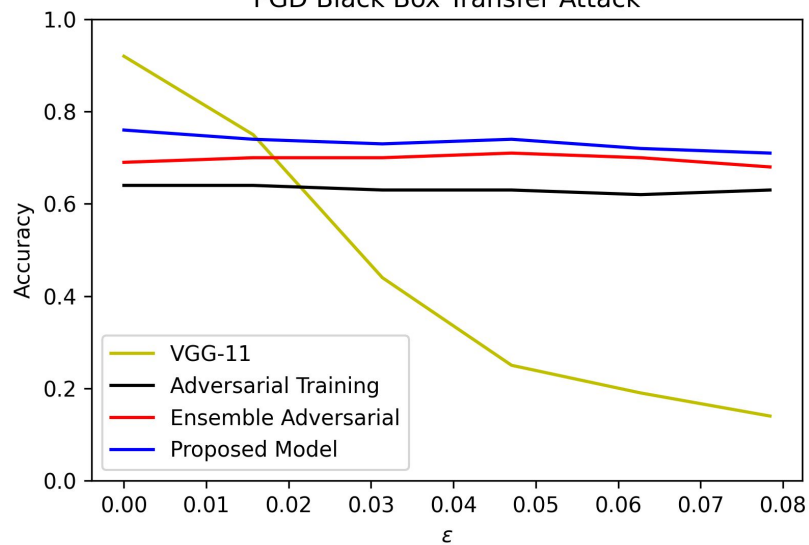


FGSM White Box Attack

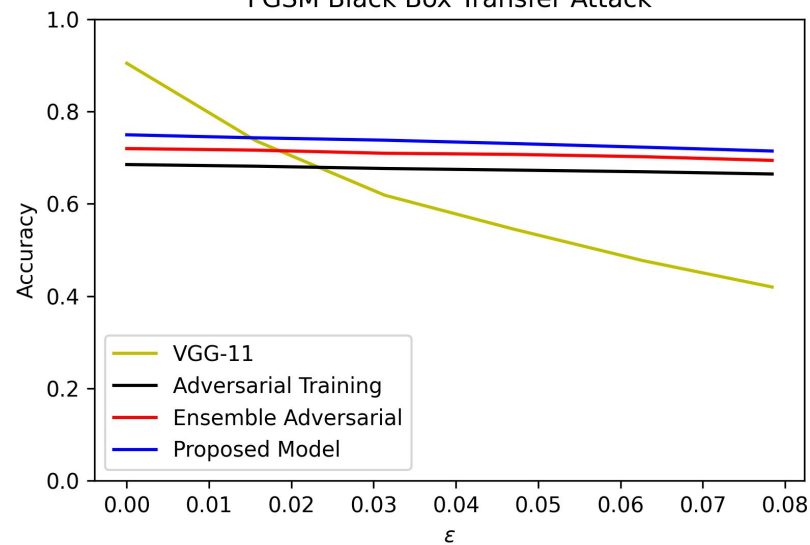


# Results - Black Box Robustness

PGD Black Box Transfer Attack



FGSM Black Box Transfer Attack



## Results - Training Time

Model	Training Time
<b>VGG-11 MM-EAT</b> (trained on our adversarial examples with ensemble AT)	1.8347 hours
<b>VGG-11 EAT</b> (regular ensemble AT)	2.4853 hours
<b>VGG-11 AT</b> (adversarially trained)	6.4425 hours

# Conclusion and Future Work

## Improved Defenses

Compared to both AT and EAT

## Improved Training Time

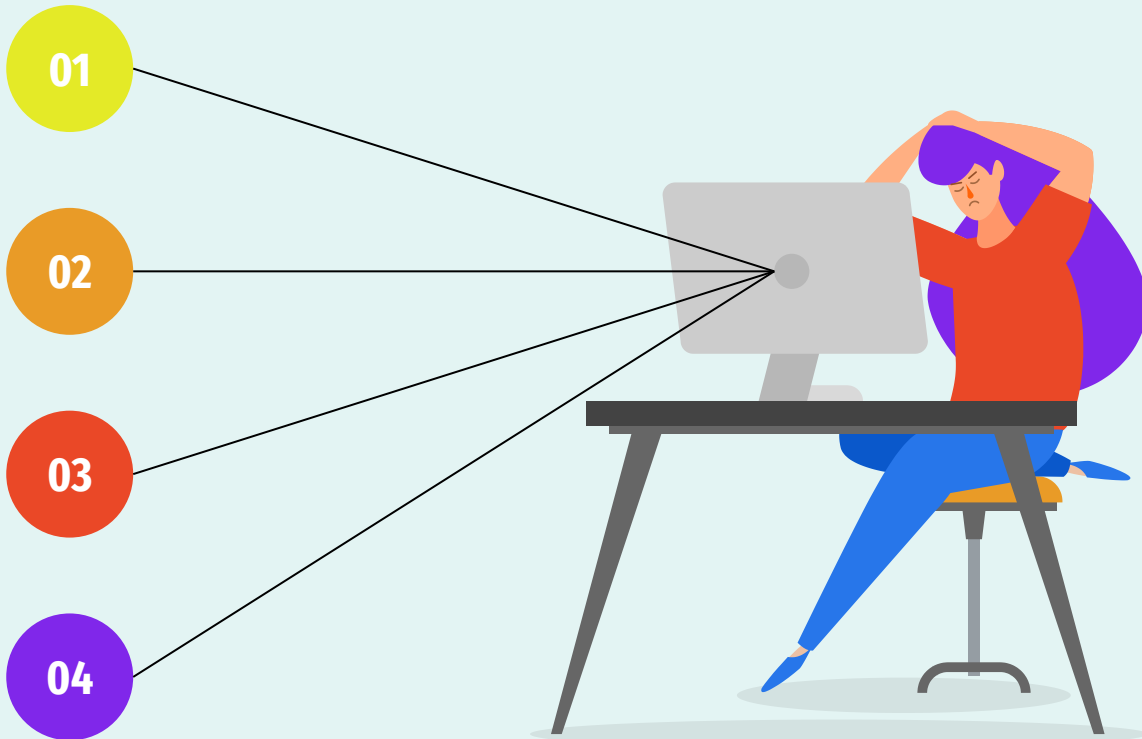
Compared to both AT and EAT

## Increase # of models used

More models = more robust?

## Apply to other datasets

MNIST, CIFAR-100, etc.



# References

- Martins, Andre, and Ramon Astudillo. "From softmax to sparsemax: A sparse model of attention and multi-label classification." International conference on machine learning. PMLR, 2016.
- Phan, Huy. "PyTorch Models Trained on CIFAR-10 Dataset." July 11, 2019. [https://github.com/huyvnphan/PyTorch\\_CIFAR10](https://github.com/huyvnphan/PyTorch_CIFAR10). <https://doi.org/10.5281/zenodo.4431043>.
- Tramèr, Florian, Alexey Kurakin, Nicolas Papernot, Ian Goodfellow, Dan Boneh, and Patrick McDaniel. "Ensemble Adversarial Training: Attacks and Defenses," May 19, 2017. <https://doi.org/10.48550/arXiv.1705.07204>.
- Wang, Jingkan, Tianyun Zhang, Sijia Liu, Pin-Yu Chen, Jiachen Xu, Makan Fardad, and Bo Li. "Adversarial Attack Generation Empowered by Min-Max Optimization," June 9, 2019. <https://doi.org/10.48550/arXiv.1906.03563>.

