

EE247 Lecture 24

Pipelined ADCs (continued)

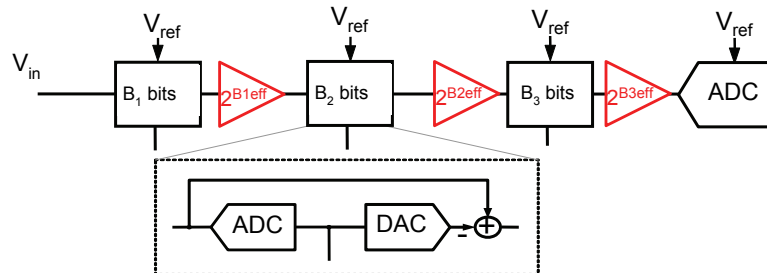
- Effect gain stage, sub-DAC non-idealities on overall ADC performance
 - Digital calibration (continued)
 - Correction for inter-stage gain nonlinearity
- Implementation
 - Practical circuits
 - Stage scaling
 - Combining the bits
 - Stage implementation
 - Circuits
 - Noise budgeting
 - How many bits per stage?

Summary Last Lecture

ADC Converters

- Techniques to reduce flash ADC complexity (continued)
 - Interleaved ADCs
 - Multi-Step ADCs
 - Two-Step flash
 - Pipelined ADCs
 - Effect of sub-ADC non-idealities on overall ADC performance
 - Error correction by adding redundancy (additional decision levels)

Summary So Far Pipelined A/D Converters

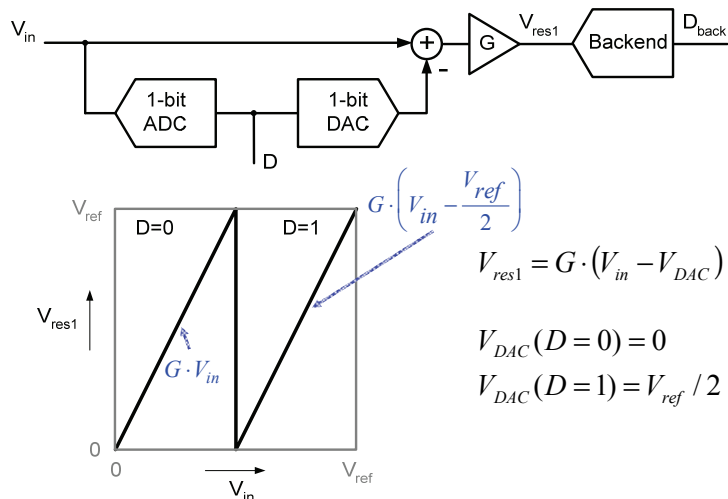


- Cascade of low resolution stages
 - Stages operate concurrently- trades latency resolution
 - Throughput limited by speed of one stage → Fast
- Errors and correction
 - Built-in redundancy compensate for sub-ADC inaccuracies (interstage gain: $G=2^{B_{\text{neff}}}$, $B_{\text{neff}} < B_n$)

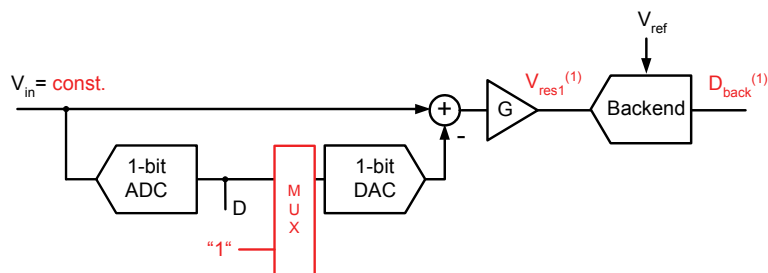
Gain Stage Gain Inaccuracy

- Gain error can be compensated in digital domain – "Digital Calibration"
- Problem: Need to measure/calibrate digital correction coefficient
- Example: Calibrate 1-bit first stage
- Objective: Measure G in digital domain

ADC Model



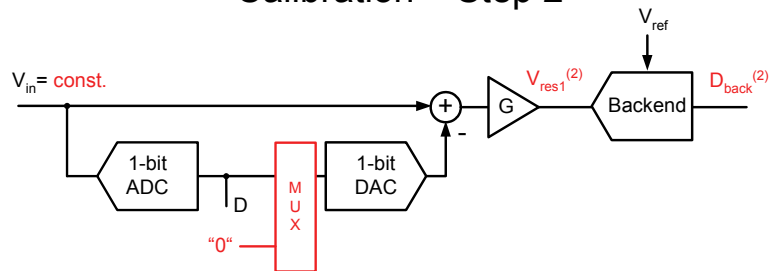
Gain Stage Inaccuracy Calibration – Step 1



$$V_{res1}^{(1)} = G \cdot (V_{in} - V_{ref} / 2)$$

$$D_{back}^{(1)} = G \cdot \frac{(V_{in} - V_{ref} / 2)}{V_{ref}} \rightarrow \text{store}$$

Gain Stage Inaccuracy Calibration – Step 2



$$V_{res1}^{(2)} = G \cdot (V_{in} - 0)$$

$$D_{back}^{(2)} = G \cdot \frac{(V_{in} - 0)}{V_{ref}} \rightarrow \text{store}$$

Gain Stage Inaccuracy Calibration – Evaluate

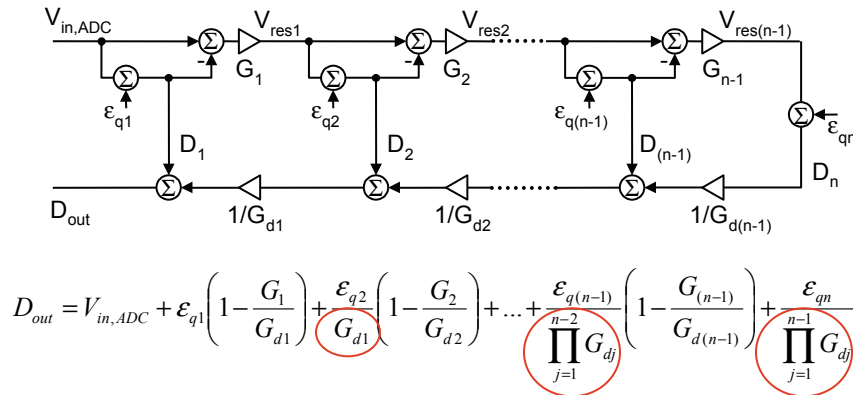
$$D_{back}^{(1)} = G \cdot \frac{(V_{in} - V_{ref}/2)}{V_{ref}}$$

$$-D_{back}^{(2)} = G \cdot \frac{(V_{in} - 0)}{V_{ref}}$$

$$D_{back}^{(1)} - D_{back}^{(2)} = \frac{1}{2} \cdot G$$

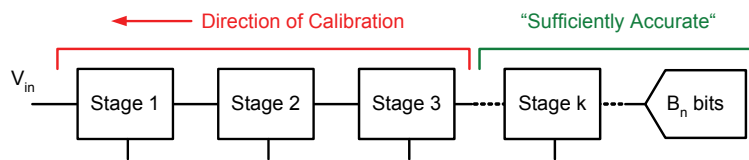
- To minimize the effect of backend ADC noise → perform measurement several times and take the average

Accuracy Bootstrapping



- Highest sensitivity to gain errors in front-end stages

"Accuracy Bootstrapping"




Ref:

A. N. Karanicolas et al. "A 15-b 1-Msample/s digitally self-calibrated pipeline ADC," *IEEE J. Of Solid-State Circuits*, pp. 1207-15, Dec. 1993

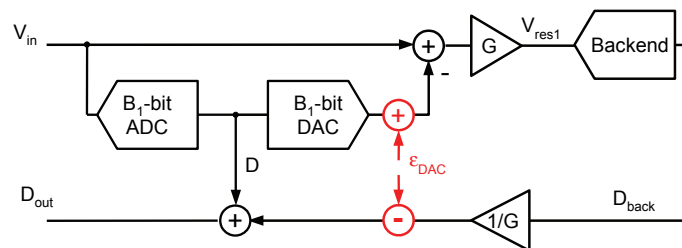
E. G. Soenen et al., "An architecture and an algorithm for fully digital correction of monolithic pipelined ADCs," *TCAS II*, pp. 143-153, March 1995

L. Singer et al., "A 12 b 65 MSample/s CMOS ADC with 82 dB SFDR at 120 MHz," *ISSCC 2000, Digest of Tech. Papers.*, pp. 38-9 (calibration in opposite direction!)

Pipeline ADC Errors

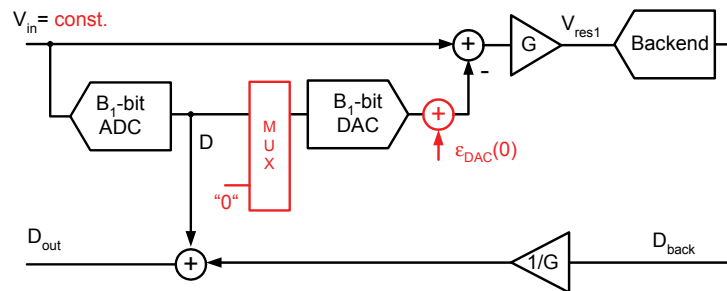
- Non-idealities associated with sub-ADCs, sub-DACs and gain stages \rightarrow error in overall pipeline ADC performance
- Need to find means to tolerate/correct errors
- Important sources of error
 - Sub-ADC errors- comparator offset
 - Gain stage offset
 - Gain stage error
 -  Sub-DAC error

DAC Errors



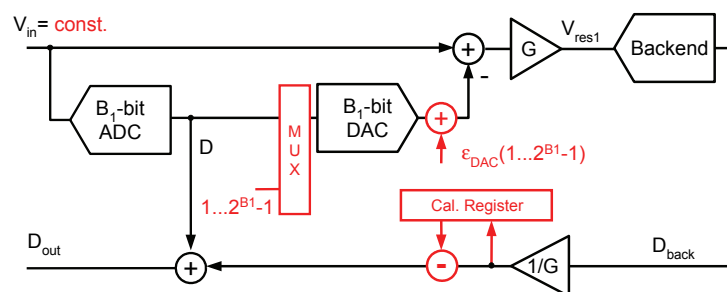
- Can be corrected digitally as well
- Same calibration concept as gain errors
 - \rightarrow Vary DAC codes & measure errors via backend ADC

DAC Calibration – Step 1



- $\epsilon_{DAC}(0)$ equivalent to offset - ignore

DAC Calibration – Step 2...2^{B1}



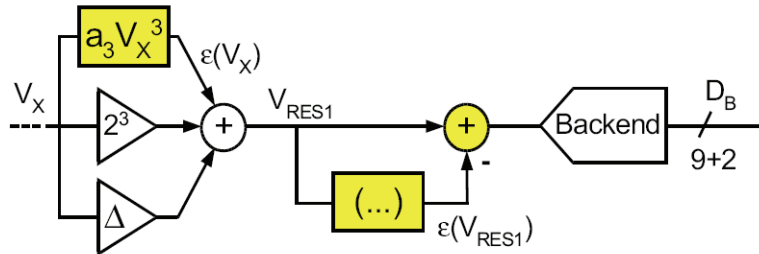
- Stepping through DAC codes $1...2^{B1}-1$ yields all incremental correction values
- Measurements repeated and averages to account for variance associated with noise

[illegible]

- Ref: E. G. Soenen et al., "An architecture and an algorithm for fully digital correction of monolithic pipelined ADCs," TCAS II, pp. 143-153, March 1995

Error	Correction/Calibration
$\epsilon_{\text{ADC}}, V_{\text{os}}$	Redundancy either same stage or next stage
ϵ_{gain}	Digital adjustment
ϵ_{DAC}	Either sufficient component matching or digital calibration
Inter-stage amplifier non-linearity	?

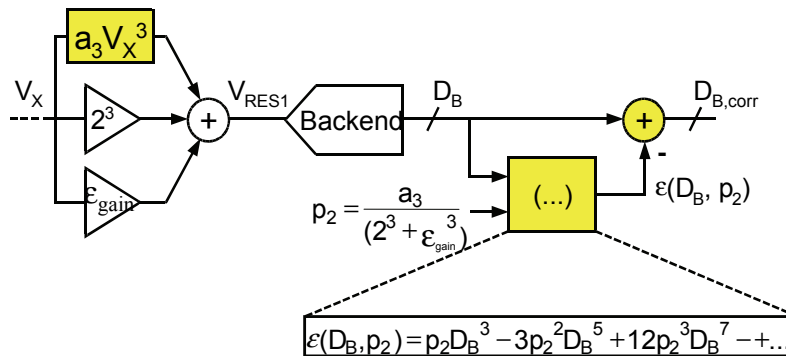
Inter-stage Gain Nonlinearity



- Invert gain stage non-linear polynomial
- Express error as function of V_{RES1}
- Push error into digital domain through backend

Ref: B. Murmann and B. E. Boser, "A 12-b, 75MS/s Pipelined ADC using Open-Loop Residue Amplification," *ISSCC Dig. Techn. Papers*, pp. 328-329, 2003

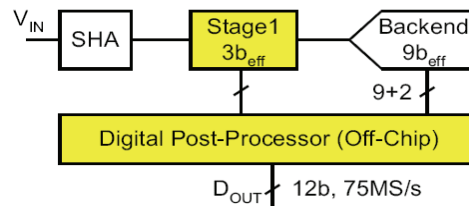
Inter-stage Gain Nonlinearity



- Pre-computed table look-up
- p_2 continuously estimated & updated (account for temp. & other variations)

Ref: B. Murmann and B. E. Boser, "A 12-b, 75MS/s Pipelined ADC using Open-Loop Residue Amplification," *ISSCC Dig. Techn. Papers*, pp. 328-329, 2003

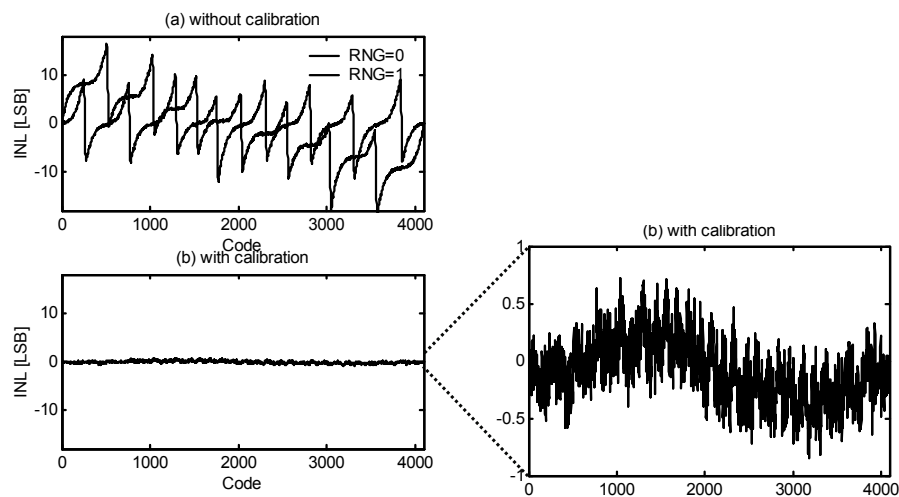
Inter-stage Gain Nonlinearity Compensation Proof of Concept Evaluation Prototype



- Re-used 14-bit ADC in 0.35 μ m from Analog Devices [Kelly, ISSCC 2001]
- Modified only 1st stage with 3- b_{eff} \rightarrow open-loop amplifier built with simple diff-pair + resistive load instead of the conventional feedback around high-gain amp
- Conventional 9- b_{eff} backend, 2-bit redundancy in 1st stage
- Real-time post-processor off-chip (FPGA)

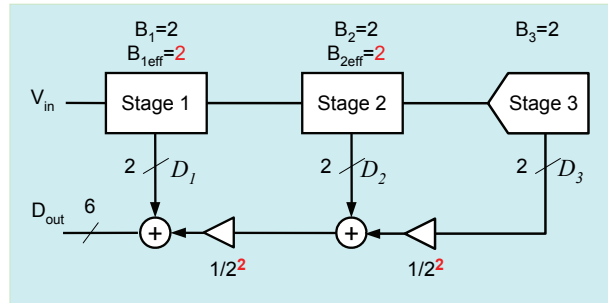
Ref: B. Murmann and B. E. Boser, "A 12-b, 75MS/s Pipelined ADC using Open-Loop Residue Amplification," *ISSCC Dig. Techn. Papers*, pp. 328-329, 2003

Measurement Results 12-bit ADC w Extra 2-bits for Calibration



Combining the Bits

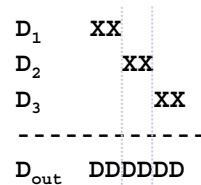
- Example: Three 2-bit stages, no redundancy



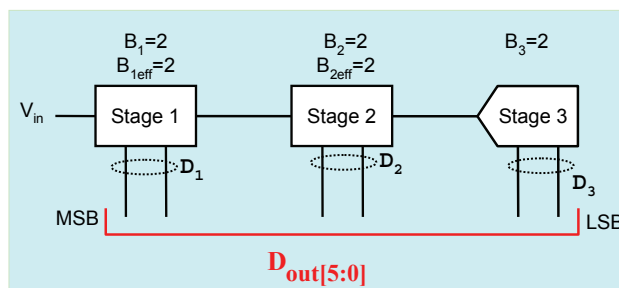
$$D_{out} = D_1 + \frac{1}{2^{B1_{eff}}} D_2 + \frac{1}{2^{B1_{eff}} \cdot 2^{B2_{eff}}} D_3$$

$$D_{out} = D_1 + \frac{1}{4} D_2 + \frac{1}{16} D_3$$

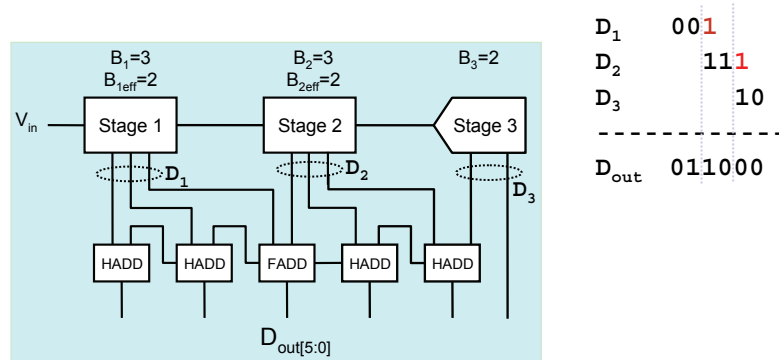
Combining the Bits



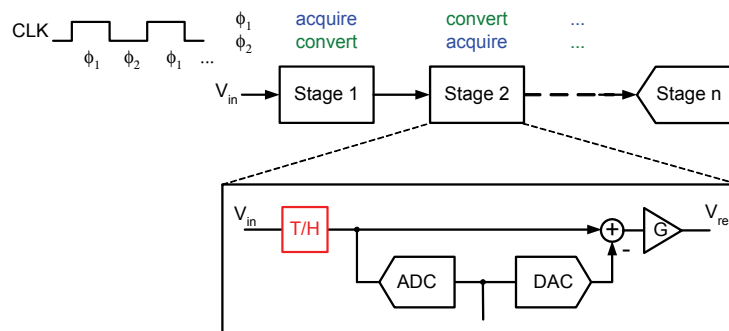
- Only bit shifts
- No arithmetic circuits needed



Combining the Bits Example

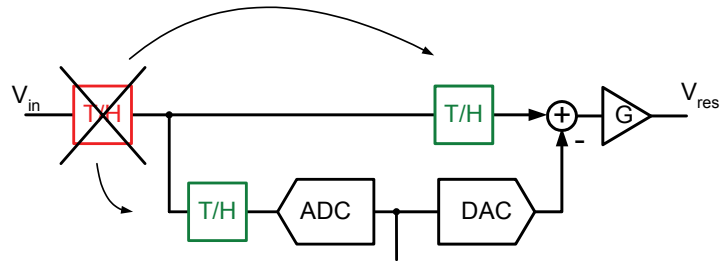


Stage Implementation



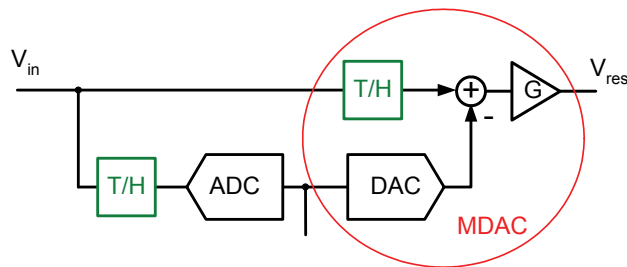
- Each stage needs T/H hold function
- Track phase: Acquire input/residue from previous stage
- Hold phase: sub-ADC decision, compute residue

Stage Implementation



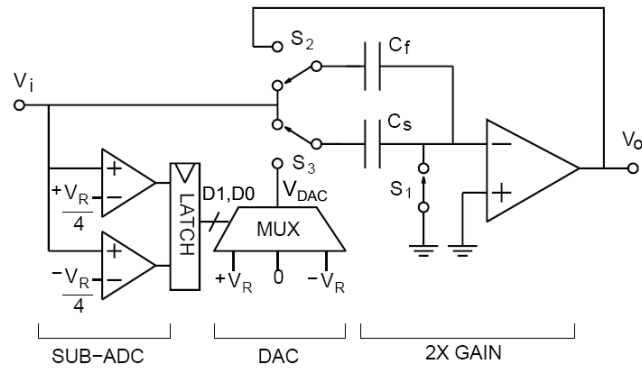
- Usually no dedicated T/H amplifier in each stage (Except first stage in some cases – why?)
- T/H implicitly contained in stage building blocks

Stage Implementation



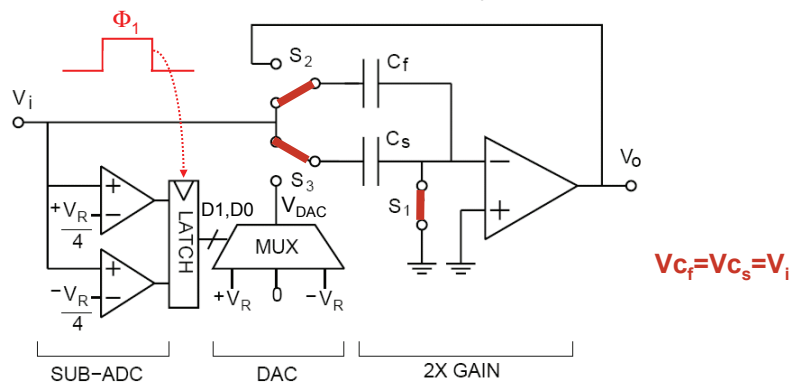
- DAC-subtract-gain function can be lumped into a single switched capacitor circuit
- "MDAC"

1.5-Bit Stage Implementation Example



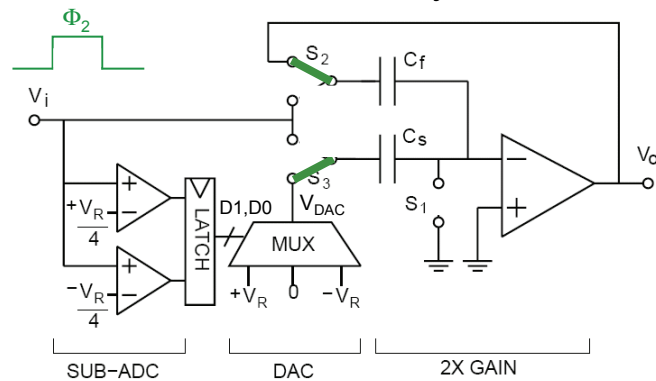
Ref: A. Abo, "Design for Reliability of Low-voltage, Switched-capacitor Circuits," UCB PhD Thesis, 1999

1.5-Bit Stage Implementation Acquisition Cycle



Ref: A. Abo, "Design for Reliability of Low-voltage, Switched-capacitor Circuits," UCB PhD Thesis, 1999

1.5-Bit Stage Implementation Conversion Cycle

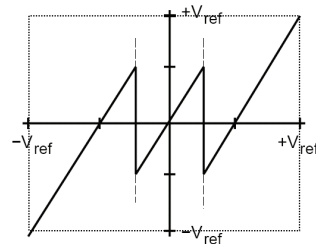


Ref: A. Abo, "Design for Reliability of Low- voltage, Switched-capacitor Circuits," UCB PhD Thesis, 1999

1.5 Bit Stage Implementation Example

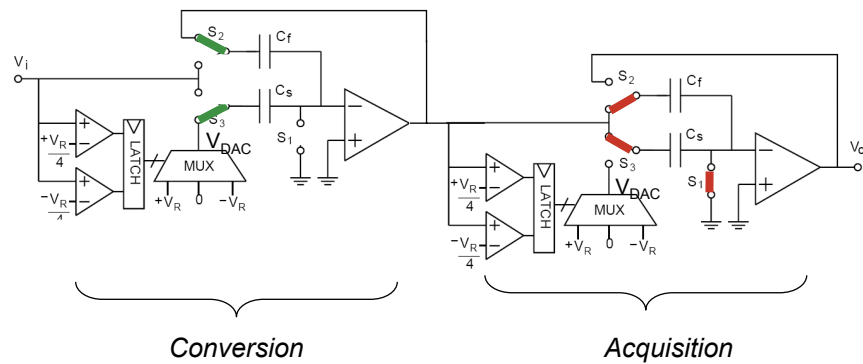
$$V_o = \begin{cases} \left(1 + \frac{C_s}{C_f}\right) V_i - \frac{C_s}{C_f} V_{ref} & \text{if } V_i > V_{ref}/4 \\ \left(1 + \frac{C_s}{C_f}\right) V_i & \text{if } -V_{ref}/4 \leq V_i \leq +V_{ref}/4 \\ \left(1 + \frac{C_s}{C_f}\right) V_i + \frac{C_s}{C_f} V_{ref} & \text{if } V_i < -V_{ref}/4 \end{cases}$$

Note: Interstage gain set by C ratios
 → Accuracy better than 0.1%
 → Up to 10bit level no need for gain calibration



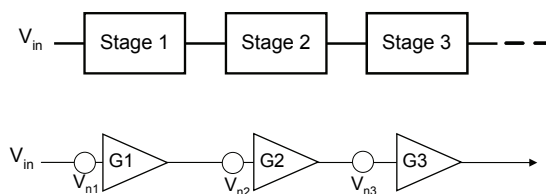
Ref: A. Abo, "Design for Reliability of Low- voltage, Switched-capacitor Circuits," UCB PhD Thesis, 1999

1.5-Bit Stage Implementation Timing of Stages



Pipelined ADC Stage Power Dissipation & Noise

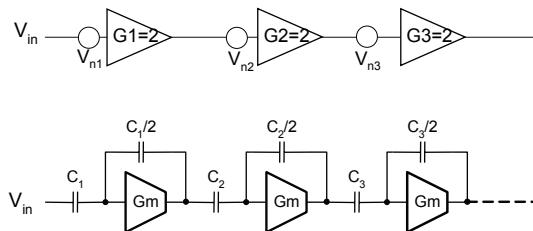
- Typically pipeline ADC noise dominated by inter-stage gain blocks
- Sub-ADC comparator noise translates into comparator threshold uncertainty and is compensated for by redundancy



$$V_{noise}^{in} = \sqrt{V_{n1}^2 + \frac{V_{n2}^2}{G1^2} + \frac{V_{n3}^2}{G1^2 G2^2} + \dots}$$

Pipelined ADC Stage Scaling

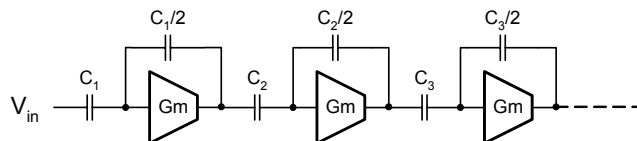
- Example: Pipeline using 1-bit_{eff} stages



- Total input referred noise power:
$$N_{tot} \propto kT \left[\frac{1}{C_1} + \frac{1}{G_1^2 C_2} + \frac{1}{G_1^2 G_2^2 C_3} + \dots \right]$$

$$N_{tot} \propto kT \left[\frac{1}{C_1} + \frac{1}{4C_2} + \frac{1}{16C_3} + \dots \right]$$

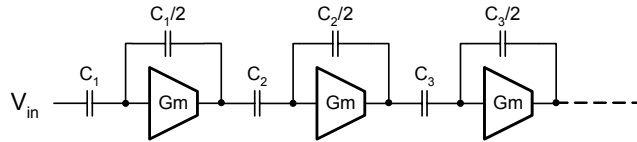
Pipelined ADC Stage Scaling



$$N_{tot} \propto kT \left[\frac{1}{C_1} + \frac{1}{4C_2} + \frac{1}{16C_3} + \dots \right]$$

- If all caps made the same size, backend stages contribute very little noise
- Wasteful power-wise, because:
 - Power $\sim G_m$
 - Speed $\sim G_m/C$
 - Power $\sim C$

Pipelined ADC Stage Scaling

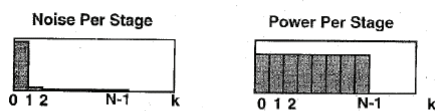


$$N_{tot} \propto kT \left[\frac{1}{C_1} + \frac{1}{4C_2} + \frac{1}{16C_3} + \dots \right]$$

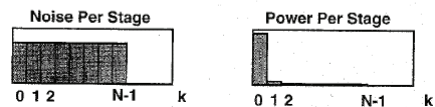
- How about scaling caps down by $G^2=2^2=4x$ per stage?
 - Same amount of noise from every stage
 - All stages contribute significant noise
 - Noise from first few stages must be reduced
 - Power $\sim Gm \sim C$ goes up!

Stage Scaling Example: 2-bit_{eff}/stage

Extreme 1: All Stages the Same Size



Extreme 2: All Stages Contribute the Same Noise

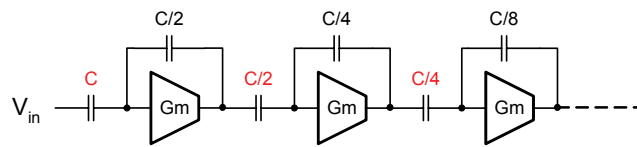


- Optimum capacitor scaling lies approximately midway between these two extremes

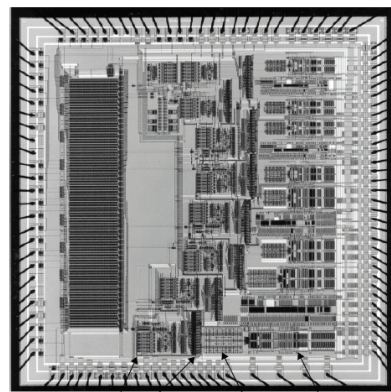
Ref: D. W. Cline, P.R Gray "A power optimized 13-b 5 MSamples/s pipelined analog-to-digital converter in 1.2um CMOS," JSSC 3/1996

Pipeline ADC Stage Scaling

- Power minimum is "shallow"
- Near optimum solution in practice: Scale capacitors by stage gain
- E.g. for effective stage resolution of 1bit (Gain=2):

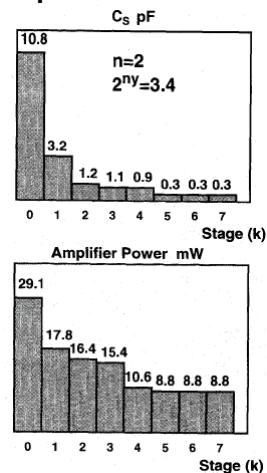


Stage Scaling Example



stage 0 comparators
stage 0 sampling capacitors
stage 0 opamp

Note:
Resolution
per stage:
→ 2bits
→ $A=4$



Ref: D. W. Cline, P.R Gray "A power optimized 13-b 5 MSamples/s pipelined analog-to-digital converter in 1.2um CMOS," JSSC 3/1996

How Many Bits Per Stage?

- Many possible architectures
 - E.g. $B_{1\text{eff}}=3, B_{2\text{eff}}=1, \dots$
Vs. $B_{1\text{eff}}=1, B_{2\text{eff}}=1, B_{3\text{eff}}=1, \dots$
- Complex optimization problem, fortunately optimum tends to be shallow...
- Qualitative answer:
 - Maximum speed for given technology
 - Use small resolution-per-stage (large feedback factor)
 - Maximum power efficiency for fixed, "low" speed
 - Try higher resolution stages
 - Can help alleviate matching requirements in front-end

Ref: Singer VLSI 96, Yang, JSSC 12/01

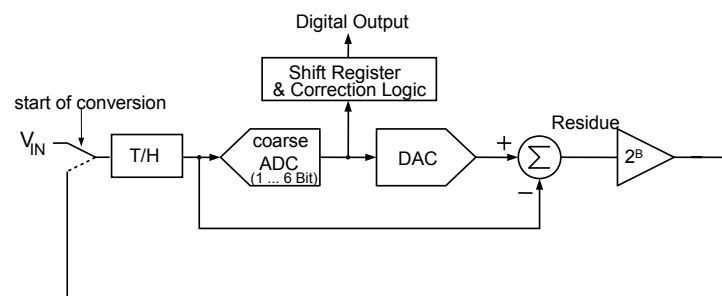
14 & 12-Bit State-of-the-Art Implementations

Reference	Yang (JSSC 12/2001) 0.35 μ /3V	Loloee (ESSIRC 2002) 0.18 μ /3V
Bits	14	12
Architecture	3-1-1-1-1-1-1-1-3	1-1-1-1-1-1-1-1-1-2
SNR/SFDR	~73dB/88dB	~66dB/75dB
Speed	75MS/s	80MS/s
Power	340mW	260mW

10 & 8-Bit State-of-the-Art Implementations

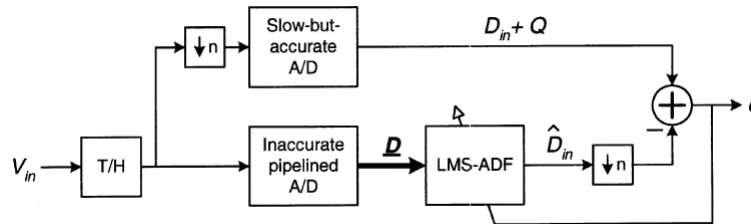
Reference	Yoshioko et al (ISSCC 2005) 0.18 μ /1.8V	Kim et al (ISSCC 2005) 0.18 μ /1.8V
Bits	10	8
Architecture	1.5bit/stage	2.8 -2.8 - 4
SNR/SFDR	~55dB/66dB	~48dB/56dB
Speed	125MS/s	200MS/s
Power	40mW	30mW

Algorithmic ADC



- Essentially same as pipeline, but a single stage is reused for all partial conversions
- For overall B_{overall} bits \rightarrow need $B_{\text{overall}}/B_{\text{stage}}$ clock cycles per conversion
 \rightarrow Small area, slow

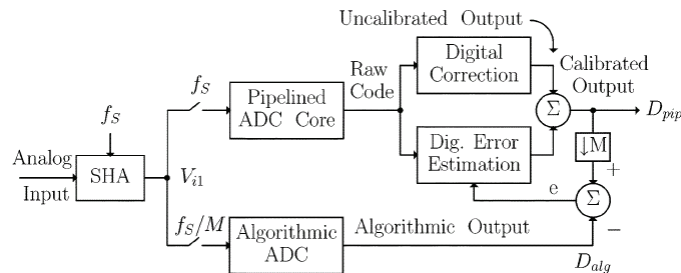
Least Mean Square Adaptive Digital Background Calibration of Pipelined Analog-to-Digital Converters



- Slow, but accurate ADC operates in parallel with pipelined (main) ADC
- Slow ADC samples input signal at a lower sampling rate (f_s/n)
- Difference between corresponding samples for two ADCs (e) used to correct fast ADC digital output via an adaptive digital filter (ADF) based on minimizing the Least-Mean-Squared error

Ref: Y. Chiu, *et al*, "Least Mean Square Adaptive Digital Background Calibration of Pipelined Analog-to-Digital Converters," IEEE TRANS. CAS, VOL. 51, NO. 1, JANUARY 2004

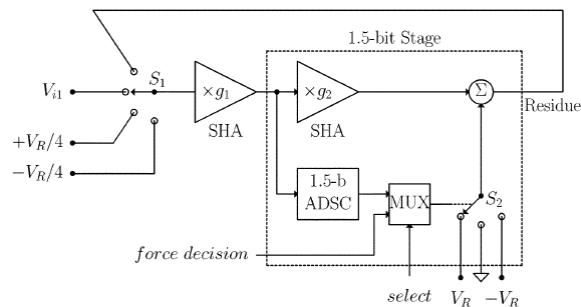
Example: "A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration"



- Pipelined ADC operates at 20Ms/s @ has 1.5bit/stage
- Slow ADC → Algorithmic type operating at 20Ms/32=625ks/s
- Digital correction accounts for bit redundancy
- Digital error estimator → minimizes the mean-squared-error

Ref: X. Wang, P. J. Hurst, S. H. Lewis, "A 12-bit 20-Msample/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004

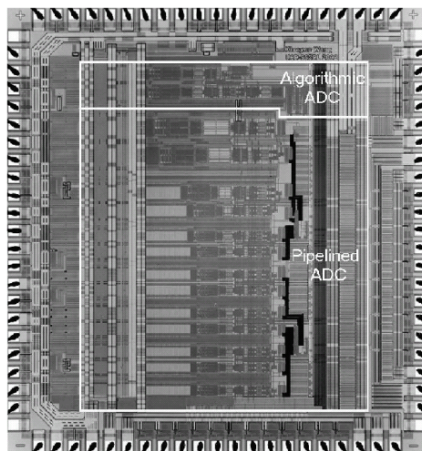
Algorithmic ADC Used for Calibration of Pipelined ADC (continued from previous page)



- Uses replica of pipelined ADC stage
- Requires extra SHA in front to hold residue
- Undergoes a calibration cycle periodically prior to being used to calibrate pipelined ADC

Ref: X. Wang, P. J. Hurst, S. H. Lewis, "A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004

12-bit 20-MS/s Pipelined ADC with Digital Background Calibration



Sampling capacitors scaled:

- Input SHA: 6pF
- Pipelined ADC: 2pF, 0.9, 0.4, 0.2, 0.1, 0.1...
- Algorithmic ADC: 0.2pF

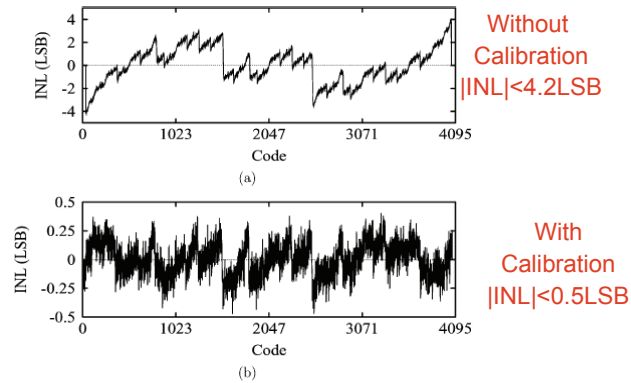
Chip area: 13.2mm²

- Area of Algorithmic ADC <20%
- Does not include digital calibration circuitry estimated ~1.7mm²

Ref: X. Wang, P. J. Hurst, S. H. Lewis, "A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004

Measurement Results

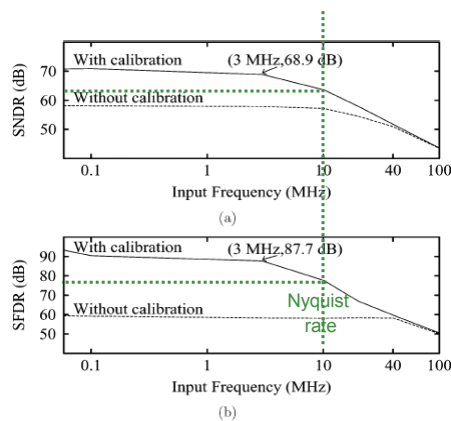
12-bit 20-MS/s Pipelined ADC with Digital Background Calibration



Ref: X. Wang, P. J. Hurst, S. H. Lewis, "A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004

Measurement Results

12-bit 20-MS/s Pipelined ADC with Digital Background Calibration



Ref: X. Wang, P. J. Hurst, S. H. Lewis, "A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004

Measurement Results

12-bit 20-MS/s Pipelined ADC with Digital Background Calibration

PERFORMANCE SUMMARY (3.3 V, 25 °C)

Process	0.35 μ m 2P4M CMOS	
Sampling rate	20 Msample/s	
Active area	7.5 mm ²	
Full-Scale Input	1.6 V _{p-p}	
	Without Cal.	With Cal.
Analog Power Diss.	190 mW	226 mW
Total Power Diss.	217 mW	254 mW
Max. INL (Pip. ADC)*	4.21 LSB	0.47 LSB
Max. DNL (Pip. ADC)*	0.60 LSB	0.41 LSB
SNDR (Alg. ADC)*	49.6 dB	59.6 dB
SNDR (Pip. ADC)*	58.2 dB	70.8 dB
SFDR (Pip. ADC)*	59.4 dB	93.3 dB
THD (Pip. ADC)*	-59.4 dB	-92.9 dB
PSRR*	65.0 dB	64.8 dB
CMRR*	73.6 dB	73.4 dB

Does not include
digital calibration
circuitry estimated
~1.7mm²

Alg. ADC SNDR
dominated by noise

* f_{in} = 58 kHz

Ref: X. Wang, P. J. Hurst, S. H. Lewis, " A 12-bit 20-MS/s pipelined analog-to-digital converter with nested digital background calibration", IEEE JSSC, vol. 39, pp. 1799 - 1808, Nov. 2004