

Chapter 10. Introduction to Artificial Neural Networks

Birds inspired us to fly, burdock plants inspired velcro, and nature has inspired many other inventions. It seems only logical, then, to look at the brain's architecture for inspiration on how to build an intelligent machine. This is the key idea that inspired artificial neural networks (ANNs). However, although planes were inspired by birds, they don't have to flap their wings. Similarly, ANNs have gradually become quite different from their biological cousins. Some researchers even argue that we should drop the biological analogy altogether (e.g., by saying "units" rather than "neurons"), lest we restrict our creativity to biologically plausible systems.\footnote{1}

ANNs are at the very core of Deep Learning. They are versatile, powerful, and scalable, making them ideal to tackle large and highly complex Machine Learning tasks, such as classifying billions of images (e.g., Google Images), powering speech recognition services (e.g., Apple's Siri), recommending the best videos to watch to bundreds of millions of users every day (e.g., YouTube), or learning to beat the world champion at the game of Go by examining millions of past games and then playing against itself (DeepMind's AlphAGO).

In this chapter, we will introduce artificial neural networks, starting with a quick tour of the very first ANN architectures. Then we will present Multi-Layer Perceptrons (MLPs) and implement one using TensorFlow to tackle the MNIST digit classification problem (introduced in Chapter 3).

From Biological to Artificial Neurons

Surprisingly, ANNs have been around for quite a while: they were first introduced back in 1943 by the neurophysiologist Warren McCulloch and the mathematician Walter Pitts. In their landmark paper https://docum.inde/to/2 "A Logical Calculus of Ideas Immanent in Nervous Activity." McCulloch and Pitts presented a simplified computational model of how biological neurons might work together in animal brains to perform complex computations using propositional logic. This was the first artificial neural network architecture. Since then many other architectures have been invented, as we will see.

The early successes of ANNs until the 1960s led to the widespread belief that we would soon be conversing with truly intelligent machines. When it became clear that this promise would go unfulfilled (at least for quite a while), funding flew elsewhere and ANNs entered a long dark era. In the early 1980s there was a revival of interest in ANNs as new network architectures were invented and better training techniques were developed. But by the 1990s, powerful alternative Machine Learning techniques such as Support Vector Machines (see Chapter 5) were favored by most researchers, as they seemed to offer better results and stronger theoretical foundations. Finally, we are now witnessing yet another wave of interest in ANNs. Will this wave die out like the previous ones did? There are a few good reasons to believe that this one is different and will have a much more profound impact on our lives:

- There is now a huge quantity of data available to train neural networks, and ANNs frequently outperform other ML techniques on very large and complex problems.
- The tremendous increase in computing power since the 1990s now makes it
 possible to train large neural networks in a reasonable amount of time. This
 is in part due to Moore's Law, but also thanks to the gaming industry, which
 has produced powerful GPU cards by the millions.
- The training algorithms have been improved. To be fair they are only slightly different from the ones used in the 1990s, but these relatively small tweaks have a huge positive impact.
- Some theoretical limitations of ANNs have turned out to be benign in practice. For example, many people thought that ANN training algorithms were doomed because they were likely to get stuck in local optima, but it turns out that this is rather rare in practice (or when it is the case, they are usually fairly close to the global optimum).

ANNs seem to have entered a virtuous circle of funding and progress.
 Amazing products based on ANNs regularly make the headline news, which pulls more and more attention and funding toward them, resulting in more and more progress, and even more amazing products.

Biological Neurons

Before we discuss artificial neurons, let's take a quick look at a biological neuron (represented in Figure 10-1). It is an unusual-looking cell mostly found in animal cerebral cortexes (e.g., your brain), composed of a cell hody containing the nucleus and most of the cell's complex components, and many branching extensions called dendrites, plus one very long extension called the axon. The axon's length may be just a few times longer than the cell body, or up to tens of thousands of times longer. Near its extremity the axon splits off into many branches called telodendria, and at the tip of these branches are minuscule structures called synaptic terminals (or simply synapses), which are connected to the dendrites (or directly to the cell body) of other neurons. Biological neurons receive short electrical impulses called signals from other neurons via these synapses. When a neuron receive a sufficient number of signals from other neurons within a few milliseconds, it fires its own signals.

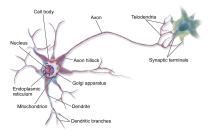


Figure 10-1. Biological neuron³

Thus, individual biological neurons seem to behave in a rather simple way, but they are organized in a vast network of billions of neurons, each neuron typically connected to thousands of other neurons. Highly complex computations can be performed by a vast network of fairly simple neurons, much like a complex anthill can emerge from the combined efforts of simple ants. The architecture of biological neural networks $(BNN)^{\delta}$ is still the subject of active research, but some parts of the brain have been mapped, and it seems that neurons are often organized in consecutive layers, as shown in Figure 10-2.

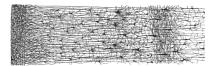


Figure 10-2. Multiple layers in a biological neural network (human cortex)⁵

Logical Computations with Neurons

Warren McCulloch and Walter Pitts proposed a very simple model of the biological neuron, which later became known as an artificial neuron: it has one or more binary (on/off) inputs and one binary output. The artificial neuron simply activates its output when more than a certain number of its inputs are active. McCulloch and Pitts showed that even with such a simplified model it is possible to build a network of artificial neurons that computes any logical proposition you want. For example, let's build a few ANNs that perform various logical computations (see Figure 10-3), assuming that a neuron is activated when at least two of its inputs are active.

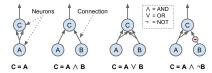


Figure 10-3. ANNs performing simple logical computations

- The first network on the left is simply the identity function: if neuron A is
 activated, then neuron C gets activated as well (since it receives two input
 signals from neuron A), but if neuron A is off, then neuron C is off as well.
- The second network performs a logical AND: neuron C is activated only
 when both neurons A and B are activated (a single input signal is not
 enough to activate neuron C).

- The third network performs a logical OR: neuron C gets activated if either neuron A or neuron B is activated (or both).
- Finally, if we suppose that an input connection can inhibit the neuron's activity (which is the case with biological neurons), then the fourth network computes a slightly more complex logical proposition: neuron C is activated only if neuron A is active and if neuron B is off. If neuron A is active all the time, then you get a logical NOT: neuron C is active when neuron B is off and vice versa.

You can easily imagine how these networks can be combined to compute complex logical expressions (see the exercises at the end of the chapter).

The Perceptron

The Perceptron is one of the simplest ANN architectures, invented in 1957 by Frank Rosenblatt. It is based on a slightly different artificial neuron (see Figure 19-4) called a threshold logic unit (TLU), or sometimes a linear threshold unit (TLU); the inputs and output are now numbers (instead of binary on/off values) and each input connection is associated with a weight. The TLU computes a weighted sum of its inputs $(c = w_1 x_1 + w_2 x_2 + \cdots + w_n x_n = \mathbf{w}^T \mathbf{x})$, then applies a step function to that sum and outputs the result: $h_{\mathbf{w}}(\mathbf{x}) = \text{step } (\mathbf{z}) = \text{step } (\mathbf{w}^T \mathbf{x})$.

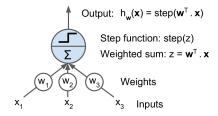


Figure 10-4. Threshold logic unit

The most common step function used in Perceptrons is the *Heaviside step func*tion (see Equation 10-1). Sometimes the sign function is used instead.

Equation 10-1. Common step functions used in Perceptron

heaviside
$$(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z \ge 0 \end{cases}$$
 $\operatorname{sgn}(z) = \begin{cases} -1 & \text{if } z < 0 \\ 0 & \text{if } z = 0 \\ +1 & \text{if } z > 0 \end{cases}$

A single TLU can be used for simple linear binary classification. It computes a linear combination of the inputs and if the result exceeds a threshold, it outputs the positive class or else outputs the negative class (just like a Logistic Regression classifier or a linear SVM). For example, you could use a single TLU to classify iris flowers based on the petal length and width (also adding an extra bias feature $x_0 = 1$, just like we did in previous chapters). Training a TLU means finding the right values for w_0 , w_1 , and w_2 (the training algorithm is discussed shortly).

A Perceptron is simply composed of a single layer of TLUs, 6 with each neuron connected to all the inputs. These connections are often represented using special passthrough neurons called *input neurons*: they just output whatever input they are fed. Moreover, an extra bias feature is generally added ($x_0 = 1$). This bias feature is typically represented using a special type of neuron called a *bias neuron*, which just outputs 1 all the time.

A Perceptron with two inputs and three outputs is represented in Figure 10-5. This Perceptron can classify instances simultaneously into three different binary classes, which makes it a multioutput classifier.

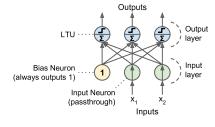


Figure 10-5. Perceptron diagram

So how is a Perceptron trained? The Perceptron training algorithm proposed by Frank Rosenblatt was largely inspired by Hebb's rule. In his book The Organization of Behavior, published in 1949, Donald Hebb suggested that when a biological neuron often triggers another neuron, the connection between these two neurons grows stronger. This idea was later summarized by Siegrid Löwel in this catchy phrase: "Cells that fire together, wire together." This rule later became known as Hebb's rule (or Hebbian learning); that is, the connection weight between two neurons is increased whenever they have the same output. Perceptrons are trained using a variant of this rule that takes into account the error made by the network; it does not reinforce connections that lead to the wrong output.

More specifically, the Perceptron is fed one training instance at a time, and for each instance it makes its predictions. For every output neuron that produced a wrong prediction, it reinforces the connection weights from the inputs that would have contributed to the correct prediction. The rule is shown in Equation 10-2.

Equation 10-2. Perceptron learning rule (weight update)

$$w_{i,j}^{\text{(next step)}} = w_{i,j} + \eta(y_j - \hat{y}_j)x_i$$

- $w_{i,j}$ is the connection weight between the i^{th} input neuron and the j^{th} output
- x_i is the ith input value of the current training instance.
- \$\mathcal{Y}_{j}\$ is the output of the jth output neuron for the current training instance.
- y_j is the target output of the jth output neuron for the current training instance.
- η is the learning rate.

The decision boundary of each output neuron is linear, so Perceptrons are incapable of learning complex patterns (just like Logistic Regression classifiers). However, if the training instances are linearly separable, Rosenblatt demonstrated that this algorithm would converge to a solution.⁷ This is called the *Perceptron* convergence theorem.

Scikit-Learn provides a Perceptron class that implements a single TLU network. It can be used pretty much as you would expect—for example, on the iris dataset (introduced in Chapter 4):

```
import numpy as np
from sklearn.datasets import load_iris
from sklearn.linear_model import Perceptron

iris = load_iris()
X = iris.data[:, (2, 3)]  # petal length, petal width
y = (iris.target == 0).astype(np.int)  # Iris Setosa?

per_olf = Perceptron(random_state=42)
per_olf.fit(X, y)
y_pred = per_olf.predict([[2, 0.5]])
```

You may have recognized that the Perceptron learning algorithm strongly resembles Stochastic Gradient Descent. In fact, Scikit-Learn's Perceptron class is equivalent to using an SGDClassifier with the following hyperparameters: loss="perceptron", learning_rate="constant", eta0=1 (the learning_rate), and penalty=None (no regularization).

Note that contrary to Logistic Regression classifiers, Perceptrons do not output a class probability; rather, they just make predictions based on a hard threshold. This is one of the good reasons to prefer Logistic Regression over Perceptrons.

In their 1969 monograph titled Perceptrons, Marvin Minsky and Seymour Papert highlighted a number of serious weaknesses of Perceptrons, in particular the fact that they are incapable of solving some trivial problems (e.g., the Exclusive OR (XOR) classification problem; see the left side of Figure 10-6). Of course this is true of any other linear classification model as well (such as Logistic Regression classifiers), but researchers had expected much more from Perceptrons, and their disappointment was great: as a result, many researchers dropped connectionism altogether (i.e., the study of neural networks) in favor of higher-level problems such as logic, problem solving, and search.

However, it turns out that some of the limitations of Perceptrons can be eliminated by stacking multiple Perceptrons. The resulting ANN is called a Multi-Luyer Perceptron (MLP). In particular, an MLP can solve the XOR problem, as you can verify by computing the output of the MLP represented on the right of Figure 10-6, for each combination of inputs: with inputs (0, 0) or (1, 1) the network outputs 0, and with inputs (0, 1) or (1, 0) it outputs 1. The numbers on the right part of the figure represent the connection weights (when a connection's weight is not shown, it is equal to 1).

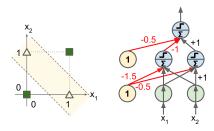


Figure 10-6. XOR classification problem and an MLP that solves it

Multi-Layer Perceptron and Backpropagation

An MLP is composed of one (passthrough) input layer, one or more layers of TLUs, called *hidden layers*, and one final layer of TLUs called the *output layer*

(see Figure 10-7). Every layer except the output layer includes a bias neuron and is fully connected to the next layer. When an ANN has two or more hidden layers, it is called a *deep neural network* (DNN).

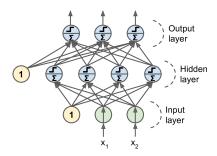


Figure 10-7. Multi-Layer Perceptron

For many years researchers struggled to find a way to train MLPs, without success. But in 1986, D. E. Rumelhart et al. published a groundbreaking article https://documents.org/linearia64448 introducing the backpropagation training algorithm. 9 Today we would describe it as Gradient Descent using reverse-mode autodiff (Gradient Descent was introduced in Chapter 4, and autodiff was discussed in Chapter 9).

For each training instance, the algorithm feeds it to the network and computes the output of every neuron in each consecutive layer (this is the forward pass, just like when making predictions). Then it measures the network's output error (i.e., the difference between the desired output and the actual output of the network), and it computes how much each neuron in the last hidden layer contributed to each output neuron's error. It then proceeds to measure how much of these error contributions came from each neuron in the previous hidden layer—and so on until the algorithm reaches the input layer. This reverse pass efficiently measures the error gradient across all the connection weights in the network by propagating the error gradient backward in the network (hence the name of the algorithm). If you check out the reverse-mode autodiff algorithm in Appendix D, you will find that the forward and reverse passes of backpropagation simply perform reverse-mode autodiff. The last step of the backpropagation algorithm is a Gradient Descent step on all the connection weights in the network, using the error gradients measured earlier.

Let's make this even shorter: for each training instance the backpropagation algorithm first makes a prediction (forward pass), measures the error, then goes through each layer in reverse to measure the error contribution from each connection (reverse pass), and finally slightly tweaks the connection weights to reduce the error (Gradient Descent step).

In order for this algorithm to work properly, the authors made a key change to the MLP's architecture: they replaced the step function with the logistic function, $\sigma(z) = 1/(1 + \exp(-z))$. This was essential because the step function contains only flat segments, so there is no gradient to work with (Gradient Descent cannot move on a flat surface), while the logistic function has a well-defined nonzero derivative everywhere, allowing Gradient Descent to make some progress at every step. The backpropagation algorithm may be used with other activation functions, instead of the logistic function. Two other popular activation functions are:

The *hyperbolic tangent* function $\tanh(z) = 2\sigma(2z) - 1$

Just like the logistic function it is S-shaped, continuous, and differentiable, but its output value ranges from -1 to 1 (instead of 0 to 1 in the case of the logistic function), which tends to make each layer's output more or less normalized (i.e., centered around 0) at the beginning of training. This often helps speed up convergence.

The ReLU function (introduced in Chapter 9)

ReLU (2) = max (0, z). It is continuous but unfortunately not differentiable at z=0 (the slope changes abruptly, which can make Gradient Descent bounce around). However, in practice it works very well and has the advantage of being fast to compute. Most importantly, the fact that it does not have a maximum output value also helps reduce some issues during Gradient Descent (we will come back to this in Chapter 11).

These popular activation functions and their derivatives are represented in \underline{Fig} ure 10-8.

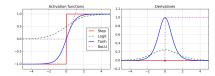


Figure 10-8. Activation functions and their derivatives

An MLP is often used for classification, with each output corresponding to a different binary class (e.g., spam/ham, urgent/not-urgent, and so on). When the

classes are exclusive (e.g., classes 0 through 9 for digit image classification), the output layer is typically modified by replacing the individual activation functions by a shared softmax function (see Figure 10-9). The softmax function was introduced in Chapter 4. The output of each neuron corresponds to the estimated probability of the corresponding class. Note that the signal flows only in one direction (from the inputs to the outputs), so this architecture is an example of a feedforward neural network (FNN).

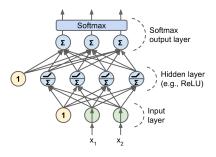


Figure 10-9. A modern MLP (including ReLU and softmax) for classification

NOTE

Biological neurons seem to implement a roughly sigmoid (S-shaped) activation function, so researchers stuck to sigmoid functions for a very long time. But it turns out that the ReLU activation function generally works better in ANNs. This is one of the cases where the biological analogy was misleading.

Training an MLP with TensorFlow's High-Level API

The simplest way to train an MLP with TensorFlow is to use the high-level API TFLeam, which offers a Scikit-Leam-compatible API. The DNNClassifier class makes if fairly easy to train a deep neural network with any number of hidden layers, and a softmax output layer to output estimated class probabilities. For example, the following code trains a DNN for classification with two hidden layers (one with 300 neurons, and the other with 100 neurons) and a softmax output layer with 10 neurons:

The code first creates a set of real valued columns from the training set (other types of columns, such as categorical columns, are available). Then we create the DNNClassifier, and we wrap it in a Scikit-Learn compatibility helper. Finally, we run 40,000 training iterations using batches of 50 instances.

If you run this code on the MNIST dataset (after scaling it, e.g., by using Scikit-Learn's StandardScaler), you will actually get a model that achieves around 98.2% accuracy on the test set! That's better than the best model we trained in Chapter 3:

```
>>> from sklearn.metrics import accuracy_score
>>> y_pred = dnn_clf.predict(X_test)
>>> accuracy_score(y_test, y_pred['classes'])
0.9825000000000000
```

WARNING

The tensorflow.contrib package contains many useful functions, but it is a place for experimental code that has not yet graduated to be part of the core TensorFlow API. So the DNNClassifier class (and any other contrib code) may change without notice in the future.

Under the hood, the DNNClassifier class creates all the neuron layers, based on the ReLU activation function (we can change this by setting the activation_fn hyperparameter). The output layer relies on the softmax function, and the cost function is cross entropy (introduced in Chapter 4).

Training a DNN Using Plain TensorFlow

If you want more control over the architecture of the network, you may prefer to use TensorFlow's lower-level Python API (introduced in Chapter 9). In this sec-

tion we will build the same model as before using this API, and we will implement Mini-batch Gradient Descent to train it on the MNIST dataset. The first step is the construction phase, building the TensorFlow graph. The second step is the execution phase, where you actually run the graph to train the model.

Construction Phase

Let's start. First we need to import the tensorflow library. Then we must specify the number of inputs and outputs, and set the number of hidden neurons in each layer:

```
import tensorflow as tf

n_inputs = 28*28 # MNIST
n_hidden1 = 300
n_hidden2 = 100
n_outputs = 10
```

Next, just like you did in Chapter 9, you can use placeholder nodes to represent the training data and targets. The shape of X is only partially defined. We know that it will be a 2D tensor (i.e., a matrix), with instances along the first dimension and features along the second dimension, and we know that the number of features is going to be 28 x 28 (one feature per pixel), but we don't know yet how many instances each training batch will contain. So the shape of X is (None, n_inputs). Similarly, we know that y will be a 1D tensor with one entry per instance, but again we don't know the size of the training batch at this point, so the shape is (None).

```
X = tf.placeholder(tf.float32, shape=(None, n_inputs), name="X")
y = tf.placeholder(tf.int64, shape=(None), name="y")
```

Now let's create the actual neural network. The placeholder X will act as the input layer, during the execution phase, it will be replaced with one training batch
at a time (note that all the instances in a training batch will be processed simultaneously by the neural network). Now you need to create the two hidden layers
and the output layer. The two hidden layers are almost identical: they differ only
by the inputs they are connected to and by the number of neurons they contain.
The output layer is also very similar, but it uses a softmax activation function instead of a ReLU activation function. So let's create a neuron_layer() function that we will use to create one layer at a time. It will need parameters to specify the inputs, the number of neurons, the activation function, and the name of the
layer:

```
def neuron_layer(X, n_neurons, name, activation=None):
    with tf.name_scope(name):
        n.inputs = int(X.ore_shape()[1])
        stddev = 2 / np.sqrt(n_inputs * n_neurons)
        init = tf.truncated_normal(n_inputs, n_neurons), stddev=
        W = tf.Variable(init, name="kernel")
        b = tf.Variable(tf.seros(n_neurons)), name="bias")
        Z = tf.natuml(X, W) + b
        if activation is not None:
            return activation(Z)
        else:
            return Z
```

Let's go through this code line by line:

- First we create a name scope using the name of the layer: it will contain all
 the computation nodes for this neuron layer. This is optional, but the graph
 will look much nicer in TensorBoard if its nodes are well organized.
- Next, we get the number of inputs by looking up the input matrix's shape and getting the size of the second dimension (the first dimension is for instances).
- 3. The next three lines create a W variable that will hold the weights matrix (often called the layer's kernef). It will be a 2D tensor containing all the connection weights between each input and each neuron; hence, its shape will be (n_inputs, n_neurons). It will be initialized randomly, using a truncated. O normal (Gaussian) distribution with a standard deviation

of $2/\sqrt{n_{inputs} + n_{neurons}}$. Using this specific standard deviation helps the algorithm converge much faster (we will discuss this further in Chapter 11; it is one of those small tweaks to neural networks that have had a tremendous impact on their efficiency). It is impor-

cuss this further in Chapter 11; it is one of those small tweaks to neural networks that have had a tremendous impact on their efficiency). It is important to initialize connection weights randomly for all hidden layers to avoid any symmetries that the Gradient Descent algorithm would be unable to break.¹¹

- 4. The next line creates a b variable for biases, initialized to 0 (no symmetry issue in this case), with one bias parameter per neuron.
- 5. Then we create a subgraph to compute $\mathbf{Z} = \mathbf{X} \ \mathbf{W} + \mathbf{b}$. This vectorized implementation will efficiently compute the weighted sums of the inputs plus the bias term for each and every neuron in the layer, for all the instances in the batch in just one shot. Note that adding a 1D array (b) to a 2D matrix with the same number of columns ($\mathbf{X} \cdot \mathbf{W}$) results in adding the 1D array to every row in the matrix: this is called broadcasting.
- 6. Finally, if an activation parameter is provided, such as f.n.relu (i.e., max (0, Z)), then the code returns activation (z), or else it just returns z.

Okay, so now you have a nice function to create a neuron layer. Let's use it to create the deep neural network! The first hidden layer takes X as its input. The

second takes the output of the first hidden layer as its input. And finally, the output layer takes the output of the second hidden layer as its input.

```
with tf.name_scope("dnn"):
hidden1 = neuron_layer(X, n_hidden1, name="hidden1",
activation=tf.nn.relu)
hidden2 = neuron_layer(hidden1, n_hidden2, name="hidden2",
activation=tf.nn.relu)
logits = neuron_layer(hidden2, n_outputs, name="outputs")
```

Notice that once again we used a name scope for clarity. Also note that logits is the output of the neural network before going through the softmax activation function: for optimization reasons, we will handle the softmax computation later.

As you might expect, TensorFlow comes with many handy functions to create

standard neural network layers, so there's often no need to define your own neuron_layer() function like we just did. For example, TensorFlow's tf.layers.dense() function (previously called tf.contrib.layers.fully_connected()) creates a fully connected layer, where all the inputs are connected to all the neurons in the layer. It takes care of creating the weights and biases variables, named kernel and bias respectively, using the appropriate initialization strategy, and you can set the activation function using the activation argument. As we will see in Chapter 11, it also supports regularization parameters. Let's tweak the preceding code to use the dense() function instead of our neuron_layer() function. Simply replace

```
with tf.name_scope("dnn"):
hidden1 = tf.layers.dense(X, n_hidden1, name="hidden1",
activation=tf.nn.relu)
hidden2 = tf.layers.dense(hidden1, n_hidden2, name="hidden2",
activation=tf.nn.relu)
logits = tf.layers.dense(hidden2, n_outputs, name="outputs")
```

the dnn construction section with the following code:

Now that we have the neural network model ready to go, we need to define the cost function that we will use to train it. Just as we did for Softmax Regression in Chapter 4, we will use cross entropy. As we discussed earlier, cross entropy will penalize models that estimate a low probability for the target class. TensorFlow provides several functions to compute cross entropy. We will use sparse_softmax_cross_entropy_with_logits(): it computes the cross entropy based on the "logits" (i.e., the output of the network before going through the softmax activation function), and it expects labels in the form of integers ranging from 0 to the number of classes minus 1 (in our case, from 0 to 9). This will give us a 1D tensor containing the cross entropy for each instance. We can then use TensorFlow's reduce_mean() function to compute the mean cross entropy over all instances.

NOTE

The

sparse_softmax_cross_entropy_with_logits () function is equivalent to applying the softmax activation function and then computing the cross entropy, but it is more efficient, and it properly takes care of corner cases: when logits are large, floating-point rounding errors may cause the softmax output to be exactly equal to 0 or 1, and in this case the cross entropy equation would contain a log(0) term, equal to negative infinity. The sparse_softmax_cross_ entropy_with_logits() function solves this problem by computing $log(\epsilon)$ instead, where ϵ is a tiny positive number. This is why we did not apply the softmax activation function earlier. There is also another function called softmax_cross_entropy_with_logits(), which takes labels in the form of one-hot vectors (instead of ints from 0 to the number of classes minus 1).

We have the neural network model, we have the cost function, and now we need to define a GradientDescentOptimizer that will tweak the model parameters to minimize the cost function. Nothing new; it's just like we did in Chapter?

```
learning_rate = 0.01

with tf.name_scope("train"):
    optimizer = tf.train.GradientDescentOptimizer(learning_rate)
    training_op = optimizer.minimize(loss)
```

The last important step in the construction phase is to specify how to evaluate the model. We will simply use accuracy as our performance measure. First, for each instance, determine if the neural network's prediction is correct by checking whether or not the highest logit corresponds to the target class. For this you can use the in_top_k() function. This returns a ID tensor full of boolean values, so we need to cast these booleans to floats and then compute the average. This will give us the network's overall accuracy.

```
with tf.name_scope('eval'):
    correct = tf.nn.in_top_k(logits, y, 1)
    accuracy = tf.reduce_mean(tf.cast(correct, tf.float32))
```

And, as usual, we need to create a node to initialize all variables, and we will also create a Saver to save our trained model parameters to disk:

```
init = tf.global_variables_initializer()
saver = tf.train.Saver()
```

Phew! This concludes the construction phase. This was fewer than 40 lines of code, but it was pretty intense: we created placeholders for the inputs and the targets, we created a function to build a neuron layer, we used it to create the DNN, we defined the cost function, we created an optimizer, and finally we defined the performance measure. Now on to the execution phase.

Execution Phase

This part is much shorter and simpler. First, let's load MNIST. We could use Scikit-Learn for that as we did in previous chapters, but TensorFlow offers its own helper that fetches the data, scales it (between 0 and 1), shuffles it, and provides a simple function to load one mini-batch a time. Moreover, the data is already split into a training set (55,000 instances), a validation set (5,000 instances), and a test set (10,000 instances). So let's use this helper:

```
from tensorflow.examples.tutorials.mnist import input_data
mnist = input_data.read_data_sets("/tmp/data/")
```

Now we define the number of epochs that we want to run, as well as the size of the mini-batches:

```
n_epochs = 40
batch_size = 50
```

And now we can train the model:

This code opens a TensorFlow session, and it runs the init node that initializes all the variables. Then it runs the main training loop: at each epoch, the code iter attes through a number of mini-batches that corresponds to the training set size. Each mini-batch is fetched via the next_batch() method, and then the code simply runs the training operation, feeding it the current mini-batch input data and targets. Next, at the end of each epoch, the code evaluates the model on the last mini-batch and on the full validation set, and it prints out the result. Finally, the model parameters are saved to disk.

Using the Neural Network

Now that the neural network is trained, you can use it to make predictions. To do that, you can reuse the same construction phase, but change the execution phase like this:

```
with tf.Session() as sess:
saver.restore(sess, "./my_model_final.ckpt")
X_new_scaled = [...] # some new images !scaled from 0 to 1)
Z = logits.eval(feed_dict=(Xx X_new_scaled))
y_pred = np.argmax(Z, axis=1)
```

First the code loads the model parameters from disk. Then it loads some new images that you want to classify. Remember to apply the same feature scaling as for the training data (in this case, scale it from 0 to 1). Then the code evaluates the logits node. If you wanted to know all the estimated class probabilities, you would need to apply the softmax() function to the logits, but if you just want to predict a class, you can simply pick the class that has the highest logit value (using the argmax() function does the trick).

Fine-Tuning Neural Network Hyperparameters

The flexibility of neural networks is also one of their main drawbacks: there are many hyperparameters to tweak. Not only can you use any imaginable network topology (how neurons are interconnected), but even in a simple MLP you can change the number of layers, the number of neurons per layer, the type of activation function to use in each layer, the weight initialization logic, and much more. How do you know what combination of hyperparameters is the best for your task?

Of course, you can use grid search with cross-validation to find the right hyperparameters, like you did in previous chapters, but since there are many hyperparameters to tune, and since training a neural network on a large dataset takes a lot of time, you will only be able to explore a finy part of the hyperparameter space in a reasonable amount of time. It is much better to use randomized search (https://doi.org/10.1001/j.com/10.1

such as Oscar (https://oscar.calldesk.ai/), which implements more complex algorithms to help you find a good set of hyperparameters quickly.

It helps to have an idea of what values are reasonable for each hyperparameter, so you can restrict the search space. Let's start with the number of hidden layers.

Number of Hidden Layers

For many problems, you can just begin with a single hidden layer and you will get reasonable results. It has actually been shown that an MLP with just one hidden layer can model even the most complex functions provided it has enough neurons. For a long time, these facts convinced researchers that there was no need to investigate any deeper neural networks. But they overlooked the fact that deep networks have a much higher parameter efficiency than shallow ones: they can model complex functions using exponentially fewer neurons than shallow nets, making them much faster to train.

To understand why, suppose you are asked to draw a forest using some drawing software, but you are forbidden to use copy/paste. You would have to draw each tree individually, branch per branch, leaf per leaf. If you could instead draw one leaf, copy/paste it to draw a branch, then copy/paste that branch to create a tree, and finally copy/paste this tree to make a forest, you would be finished in no time. Real-world data is often structured in such a hierarchical way and DNNs automatically take advantage of this fact: lower hidden layers model low-level structures (e.g., line segments of various shapes and orientations), intermediate hidden layers combine these low-level structures to model intermediate-level structures (e.g., squares, circles), and the highest hidden layers and the output layer combine these intermediate structures to model high-level structures (e.g., floors).

Not only does this hierarchical architecture help DNNs converge faster to a good solution, it also improves their ability to generalize to new datasets. For example, if you have already trained a model to recognize faces in pictures, and you now want to train a new neural network to recognize hairstyles, then you can kickstart training by reusing the lower layers of the first network. Instead of randomly initializing the weights and biases of the first few layers of the new neural network, you can initialize them to the value of the weights and biases of the lower layers of the first network. This way the network will not have to learn from scratch all the low-level structures that occur in most pictures; it will only have to learn the higher-level structures (e.g., hairstyles).

In summary, for many problems you can start with just one or two hidden layers and it will work just fine (e.g., you can easily reach above 97% accuracy on the MNIST dataset using just one hidden layer with a few hundred neurons, and above 98% accuracy using two hidden layers with the same total amount of neurons, in roughly the same amount of training time). For more complex problems, you can gradually ramp up the number of hidden layers, until you start overfitting the training set. Very complex tasks, such as large image classification or speech recognition, typically require networks with dozens of layers (or even hundreds, but not fully connected ones, as we will see in Chapter 13), and they need a huge amount of training data. However, you will rarely have to train such networks from scratch: it is much more common to reuse parts of a pretrained state-of-theart network that performs a similar task. Training will be a lot faster and require much less data (we will discuss this in Chapter 11).

Number of Neurons per Hidden Layer

Obviously the number of neurons in the input and output layers is determined by the type of input and output your task requires. For example, the MNIST task requires 28 x 28 = 784 input neurons and 10 output neurons. As for the hidden layers, a common practice is to size them to form a funnel, with fewer and fewer neurons at each layer—the rationale being that many low-level features can coalesce into far fewer high-level features. For example, a typical neural network for MNIST may have two hidden layers, the first with 300 neurons and the second with 100. However, this practice is not as common now, and you may simply use the same size for all hidden layers—for example, all hidden layers with 150 neurons: that's just one hyperparameter to tune instead of one per layer. Just like for the number of layers, you can try increasing the number of neurons gradually until the network starts overfitting. In general you will get more bang for the buck by increasing the number of layers than the number of neurons per layer. Unfortunately, as you can see, finding the perfect amount of neurons is still somewhat of a black art.

A simpler approach is to pick a model with more layers and neurons than you actually need, then use early stopping to prevent it from overfitting (and other regu larization techniques, especially dropout, as we will see in Chapter 11). This has been dubbed the "stretch pants" approach: 12 instead of wasting time looking for pants that perfectly match your size, just use large stretch pants that will shrink down to the right size.

Activation Functions

In most cases you can use the ReLU activation function in the hidden layers (or one of its variants, as we will see in Chapter11). It is a bit faster to compute than other activation functions, and Gradient Descent does not get stuck as much on plateaus, thanks to the fact that it does not saturate for large input values (as opposed to the logistic function or the hyperbolic tangent function, which saturate at 1).

For the output layer, the softmax activation function is generally a good choice for classification tasks when the classes are mutually exclusive. When they are not mutually exclusive (or when there are just two classes), you generally want to use the logistic function. For regression tasks, you can simply use no activation function at all for the output layer.

This concludes this introduction to artificial neural networks. In the following chapters, we will discuss techniques to train very deep nets, and distribute training across multiple servers and GPUs. Then we will explore a few other popular neural network architectures: convolutional neural networks, recurrent neural networks, and autoencoders.

Exercises

- Draw an ANN using the original artificial neurons (like the ones in Figure 10-3) that computes A ⊕ B (where ⊕ represents the XOR operation). Hint: A ⊕ B = (A ∧ ¬B) ∨ (¬A ∧ B).
- 2. Why is it generally preferable to use a Logistic Regression classifier rather than a classical Perceptron (i.e., a single layer of threshold logic units trained using the Perceptron training algorithm)? How can you tweak a Perceptron to make it equivalent to a Logistic Regression classifier?
- 3. Why was the logistic activation function a key ingredient in training the first MLPs?
- 4. Name three popular activation functions. Can you draw them?
- 5. Suppose you have an MLP composed of one input layer with 10 passthrough neurons, followed by one hidden layer with 50 artificial neurons, and finally one output layer with 3 artificial neurons use the ReLU activation function.
 - $\bullet \quad \text{What is the shape of the input matrix X?}$
 - What about the shape of the hidden layer's weight vector W_h, and the shape of its bias vector b_h?
 - What is the shape of the output layer's weight vector W_o, and its bias vector b_o?
 - What is the shape of the network's output matrix Y?
 - Write the equation that computes the network's output matrix Y as a function of X, W_b, b_b, W_a and b_a.
- 6. How many neurons do you need in the output layer if you want to classify email into spam or ham? What activation function should you use in the output layer? If instead you want to tackle MNIST, how many neurons do you need in the output layer, using what activation function? Answer the same questions for getting your network to predict housing prices as in Chapter 2.
- 7. What is backpropagation and how does it work? What is the difference between backpropagation and reverse-mode autodiff?
- 8. Can you list all the hyperparameters you can tweak in an MLP? If the MLP overfits the training data, how could you tweak these hyperparameters to try to solve the problem?
- 9. Train a deep MLP on the MNIST dataset and see if you can get over 98% precision. Just like in the last exercise of <u>Chapter 9</u>, try adding all the bells and whistles (i.e., save checkpoints, restore the last checkpoint in case of an interruption, add summaries, plot learning curves using TensorBoard, and so on).

Solutions to these exercises are available in Appendix A.

- 1 You can get the best of both worlds by being open to biological inspirations without being afraid to create biologically unrealistic models, as long as they
- 2 "A Logical Calculus of Ideas Immanent in Nervous Activity," W. McCulloch and W. Pitts (1943)
- 3 Image by Bruce Blaus (Creative Commons 3.0). Reproduced from https://en.wikipedia.org/wiki/Neuron.
- 4 In the context of Machine Learning, the phrase "neural networks" generally refers to ANNs, not BNNs.
- 5 Drawing of a cortical lamination by S. Ramon y Cajal (public domain). Reproduced from https://en.wikipedia.org/wiki/Cerebral_cortex.
- $_{\rm 6}$ The name Perceptron is sometimes used to mean a tiny network with a single TLU.
- 7 Note that this solution is generally not unique: in general when the data are linearly separable, there is an infinity of hyperplanes that can separate them.
- 8 "Learning Internal Representations by Error Propagation," D. Rumelhart, G. Hinton R. Williams (1986).
- $_{\rm 9}$ This algorithm was actually invented several times by various researchers in different fields, starting with P. Werbos in 1974.
- 10 Using a truncated normal distribution rather than a regular normal distribution ensures that there won't be any large weights, which could slow down training.

- For example, if you set all the weights to 0, then all neurons will output 0, and the error gradient will be the same for all neurons in a given hidden layer. The Gradient Descent step will then update all the weights in exactly the same way in each layer, so they will all remain equal. In other words, despite having hundreds of neurons per layer, your model will act as if there were only one neuron per layer. It is not going to fly.
- By Vincent Vanhoucke in his Deep Learning class (http://homl.info/46) on Udacity.com
- $^{\rm 13}~$ A few extra ANN architectures are presented in $\underline{Appendix\,E}.$

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9. Up and Running with TensorFlow

NEXT 11. Training Deep Neural Nets