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# FEW-SHOT LEARNING

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TOWARD DEEP LEARNING AND  
CONVOLUTIONAL NEURAL NETWORK

## BACHELOR THESIS

by

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*» It has been a long journey to this moment. «*

Sidney Poitier, 1964

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# 1 MOTIVATION

Nowadays machine learning and deep learning have become a distinguished approach for visual recognition tasks and has achieved great success in this process. However, they seek a large amount of labeled data to learn. Providing this amount of labeled data not only will bring much effort along but also will occupy a huge size of storage and seek large storage. In contrast, humans are very good in visual recognition so that, they can learn with one <sup>1</sup> or few <sup>2</sup> examples. Imagine one kid who can recognize a lion in a picture after looking a few pictures of lions as an example. We want to simulate and apply this human's ability to the deep learning and make them learn with few examples, with desirable accuracy. In this bachelor thesis, we concern ourselves with few-shot learning in deep learning. We aim to learn and train a model when there are few labeled examples obtainable. We approach to generate artificial examples from a few available labeled examples and enlarge our dataset artificially. This technique known as data augmentation. These artificial labeled examples aid us to learn better with more accuracy and prevent overfitting. Data augmentation is our focus in this work to achieve few-shot learning and prevent overfitting. In this thesis, we will introduce different well-known methods of data augmentation. The first purpose will be to discover if and how far data augmentation can improve the learning process and accuracy. The second step will be to compare their accuracy. In the end, we aim to discover the potential possibility of combining the different methods of data augmentation to increase accuracy and reduce error-rate and improve the learning process. We will focus on visual recognition tasks and their classification. Additionally, we will concentrate on the implementation of various methods of data augmentation for convolutional neural networks

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<sup>1</sup>This is known as one-shot learning in deep learning and represents the scenario when there is one instance of each class in training-set to learn.

<sup>2</sup>This is known as few-shot learning in deep learning and represents the scenario when there are just few instances of each class in training-set to learn.

## 2 INTRODUCTION

Neural networks can possibly contain multiple non-linear layers and this makes them very expressive models that can learn very complicated relationships between their inputs and outputs. With even limited input data, neural networks can discover and learn many relations from the data, however, sometimes the discovered and learned relations do not exist or just consist of redundant information and relations. Redundant relation can potentially arise of data-noise or lack of data-generalization. Non exist relations can potentially emerge from lack of enough data. These phenomena known as *overffiting* in deep learning. In other words, learning with few labeled examples or noisy data causes overfitting. Overffiting cause low accuracy and high error-rate. Hence, we approach to propagation of artificial labeled examples from a few given examples to prevent overfitting and reduce the error rate and increase the accuracy.

As we mentioned acquiring a huge labeled dataset is expensive and seeks much effort and time. Therefore we aim to generate artificial example from few obtainable labeled examples. In other words, we augment our data and this strategy is known as data augmentation. There are a few well-known methods for data augmentation. We aim to introduce them in this thesis. Besides we will implement these methods to compare their efficiency and capability. These methods are as follow:

- **Label Preserving Transformation** 5.1
- **Elastic Distrotion** 5.2
- **Stroke Warping** 5.3
- **Bayesian Approach** 5.4
- **Manifold Approach** 5.5

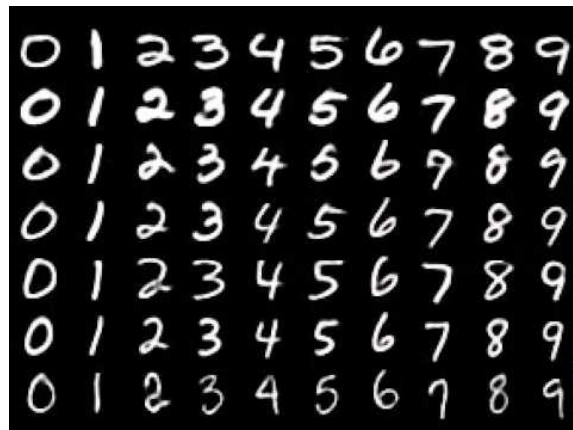
## 3 DATA REPRESENTATION

Here should be an Introduction of chapter and introduce the data

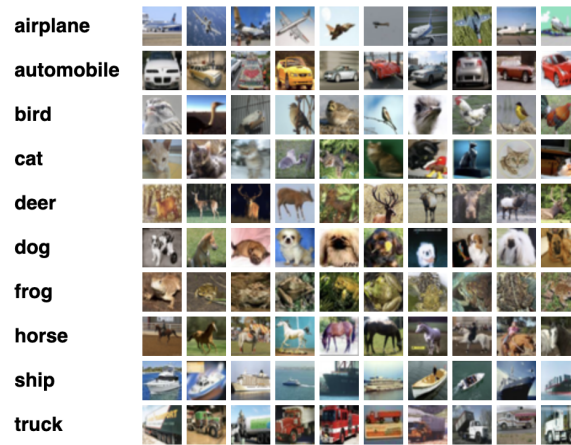
### 3.1 MNIST

The MNIST dataset (Modified National Institute of Standards and Technology) is a large handwritten digits dataset, provided by Yann Le Cun, derived from NIST Special Database 19 [STA].

The MSNIT dataset consists of 60,000 train- and 10,000 test-images and each image is grayscale with  $28 \times 28$  pixels. It has 10 classes that represent 0 – 9 digits and data is fairly splitted between classes [LeC]. MNIST is one of the most popular datasets for deep learning because of the not too high complexity and compatibility with almost all deep learning models. Hence many papers attempted to reach a low error-rate on this dataset. One of them manages to reduce the error-rate on the MNIST by up to 0.23% [CMS12]. You can find the information about the dataset at table 1 and figure 1 shows an example of the dataset.



**FIGURE 1:** 7 examples per class of MNIST dataset, merged in one image [Ath]



**FIGURE 2:** 10 examples per class of CIFAR-10 dataset, merged in one image [Kri]

**TABLE 1:** Structure and organization of the datasets.

| Dataset  | NO. Classes | NO. Train | NO. Test | Size (pixel)   | NO. Channel   |
|----------|-------------|-----------|----------|----------------|---------------|
| MNIST    | 10          | 60,000    | 10,000   | $28 \times 28$ | 1 (Grayscale) |
| EMNIST   | 26          |           |          |                |               |
| CIFAR-10 | 10          | 50,000    | 10,000   | $28 \times 28$ | 3 (RGB)       |
| CIFAR100 | 100         |           |          |                |               |

### 3.2 EMNIST

blablabla

### 3.3 CIFAR-10

The CIFAR-10 (Canadian Institute for Advanced Research) , collected by Alex Krizhevsky, Vinod Nair, and Geoffrey Hinton is a subset from 80 million tiny images dataset [Uni].

The dataset consists of 60,000 RGB with  $32 \times 32$  pixels images, which are divided to the 50,000 train and 10,000 test datasets. As the name makes it clear the CIFAR-10 contains 10 classes ([plane, car, bird, cat, deer, dog, frog, horse, ship, truck]) [Kri]. One of the lowest reported error-rate with a convolutional neural network managed to achieve 2.56% [DT17]. You can find the information about the dataset at table 1 and figure 2 shows an example of the dataset.

### 3.4 CIFAR100

blablabla

## 4 NEURAL NETWORK

### 4.1 INTRODUCTION

### 4.2 CONVOLUTIONAL NEURAL NETWORK

### 4.3 OVERFITTING



## 5 DATA AUGMENTATION

Here should be Introduction for data augmentation

### 5.1 LABEL PRESERVING TRANSFORMATION

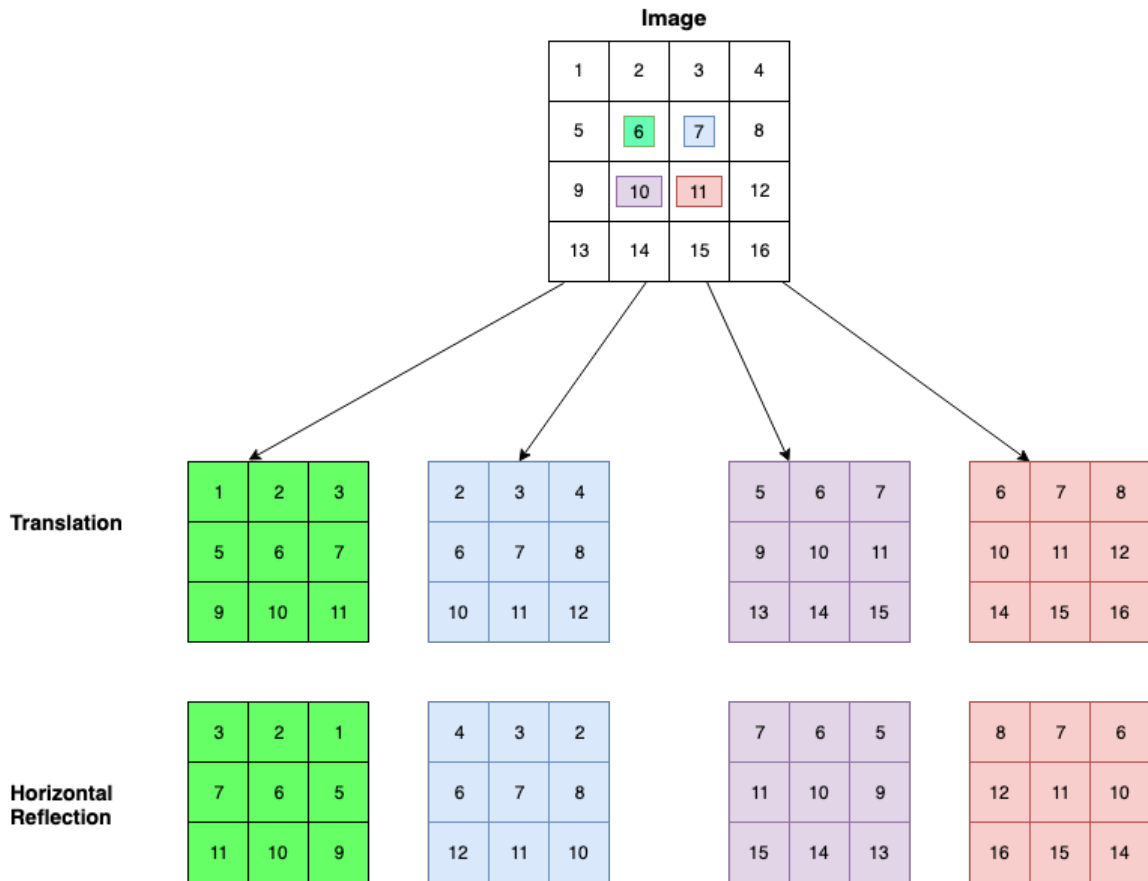
One of the most in common method to enlarge the dataset artificially is the label preserving transformation. This method provides the possibility to generate artificial data with non-heavy computation. The advantage of a very little computation aids us to save storage. In other words, it wouldn't be required to save the generated data on a storage and the data can always be enlarged artificially in a short time and with a little computation. As the method's name makes it clear, this method aims to generate new data from a single data with the same label. We explain the method and its approach for image datasets because as we mentioned our focus is image datasets.

This method consists of generating image translations and horizontal reflections. Image translations mean, random patches from the original images. The size of the patches are smaller than the size of the original images. We will extract all possible translations (all possible patches which fit in the image) from our image. These extracted translations (extracted random patches) and their horizontal reflection will be used for training our network. Given a single channel (gray)  $n \times n$  image and the translation patch with size of  $m \times m$  and  $n > m$  then the training dataset will increase by a factor:

$$2 \times (n - m + 1) \times (n - m + 1)$$

In the figure 3 is the process of the translations and reflections of a small image presented.

At test time, the method extracts the patches with the same size. This time the patches will be extracted from 4 corners and center of the original image.



**FIGURE 3:** An example of single channel image with size of  $4 \times 4$  with its translations with size of  $3 \times 3$  patches and their horizontal reflections. The numbers determinate the pixels intensity

The network predicts on these five patches and their horizontal reflections (10 patches altogether). In the end, the average of the predictions will be our network's prediction.

## 5.2 ELASTIC DISTORTION

Another well-known method for data augmentation is elastic distortion. This method as the same as label preserving transformation generates artificial data (images) from a single data (image) but with this difference that this time instead of resizing the image (translation) the pixels inside of the image will be moved and displaced. The intensity of pixels also will be changed with respect to their new places and their neighbors' intensity and their old places and their origin intensity.

As it cleared elastic distortions concerns itself with a displacement of the pixels and an adjustment of the pixels intensity. This approach is known as interpolation.

There are a few schemes like (nearest neighbor-, bicubic-, spline- and bilinear interpolation) to reach the goal. Bilinear interpolation is one of the simplest with a desirable result. Hence we use bilinear interpolation. We will explain the process below.

We will start with pixels displacement. For instance if  $\Delta x(x, y) = \alpha x$  and  $\Delta y(x, y) = \alpha y$ , this means that each pixels will be moved  $\alpha x$  in the direction of x-axis and  $\alpha y$  in the direction of y-axis.  $\alpha$  would be our scale parameter and since  $\alpha$  can be a non-integer value, interpolation is necessary and as we mentioned we use the bilinear interpolation. In the next step after pixels displacement, the intensity of the pixels in the new locations should be adjusted concerning the intensity of the neighbors' pixels in the original image (origin square). Hence bilinear interpolation aids us to reach this target. The bilinear interpolation interpolates the moved pixel horizontally. Then it interpolates the pixel vertically with respect to yielded values from horizontal interpolations. We will show and summarize the process formally in below.

**DEFINITION 1:** Given  $p'$  the pixel which we want to displacement it with  $\Delta x(x, y) = \alpha x$  and  $\Delta y(x, y) = \alpha y$  and  $p_{(x,y)}, p_{(x+1,y)}, p_{(x,y-1)}, p_{(x+1,y-1)}$  are the neighbors (on origin square) of  $p'$  in the new location after displacement and  $I(p)$  shows the intensity of pixel  $p$ . Then the vertical interpolation yields:

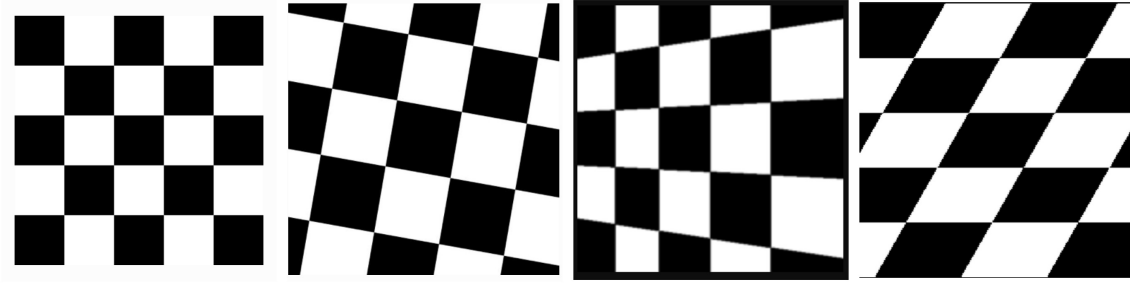
$$V_1 = I(p_{(x,y)}) + (\Delta x(p', p_{(x,y)}) \times I(p_{(x+1,y)}))$$

$$V_2 = I(p_{(x,y-1)}) + (\Delta x(p', p_{(x,y-1)}) \times I(p_{(x+1,y-1)}))$$

And then the horizontal interpolation yields a new intensity for pixel  $p'$  after displacement:

$$I(p') = V_1 + (\Delta y(p', p_{(x,y-1)}) \times V_2)$$

To reach elastic deformation or elastic distortion we approach to generate  $\Delta x(x, y) = \alpha x$  and  $\Delta y(x, y) = \alpha y$  with  $\alpha \times rand(-1, +1)$  since  $\alpha$  is image-scale parameter and  $rand(-1, +1)$  generate a number between  $-1$  and  $+1$  with uniform distribution. After all, the fields  $\Delta x$  and  $\Delta y$  are convolved with a Gaussian filter with standard deviation of  $\sigma$ . The values of  $\sigma$  and  $\alpha$  depends on the image size and the image entropy. This process will generate elastic deformed image from original image which called elastic distortion.



**FIGURE 4:** An exmaple of rotation, skew, shear, and scale translations for stroke warping respectively from left to right. The first image from left is the original image [TODO-Augmentaion]

### 5.3 STROKE WARPING

This method as same as previously introduced methods uses predetermined families of transformations. In other words, we enlarge our dataset artificially with the aid of well-known classical computer vision transformations. This method notwithstanding of non-heavy complexity accomplished desirable results even on medical purposes [Bai+19]. The ideas of this Methode raised from Tangent Dist and Tangent Prop [Sim+92] and [SLD93] works.

In this method, we perform small changes in images to augment our data. That means we augment our images with skewing, rotating and shearing them [YLW97]. As same as the label preserving transformation and elastic distortion the augmentation will be started before the training phase and the training will be performed on enlarged data. In figure 4 represents each mentioned translation to make them visually understandable.

### 5.4 BAYESIAN APPROACH

As you may until now realized, all introduced classes of techniques in this work for data augmentation were pre-defined families of statistical transformations. In other words, we generated synthetic images with computer vision techniques statistically before the training phase and we didn't change our augmented data until the end of the learning. In fact, the basic idea of each of them is known as "poor man's" data augmentation (PMDA) [Tan91]. The point is if neural networks, in general, can learn such complex relations and patterns in images, therefore they should be able to learn latent variables to improve data augmentation dynamically. Put the matter another way, in this method, we focus not only on the classification task and learning patterns of images but also on learning how to improve our image augmentation dynamically and iteratively during the training and classification.

## 5.5 MANIFOLD APPROACH

## 6 COMPREHENSIVE COMPARISON

## **7 MTHODES COMBINATION AND NEW METHOD**

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## STATEMENT OF AUTHORSHIP

I hereby confirm that the work presented in this bachelor thesis has been performed and interpreted solely by myself except where explicitly identified to the contrary. I declare that I have used no other sources and aids other than those indicated. This work has not been submitted elsewhere in any other form for the fulfilment of any other degree or qualification.

Bonn, January 4, 2020

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Milad Navidizadeh