C4W3_Assignment

April 5, 2023

1 Week 3: Using RNNs to predict time series

Welcome! In the previous assignment you used a vanilla deep neural network to create forecasts for generated time series. This time you will be using Tensorflow's layers for processing sequence data such as Recurrent layers or LSTMs to see how these two approaches compare.

Let's get started!

```
[1]: import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt
from dataclasses import dataclass
```

1.1 Generating the data

The next cell includes a bunch of helper functions to generate and plot the time series:

```
[2]: def plot_series(time, series, format="-", start=0, end=None):
         plt.plot(time[start:end], series[start:end], format)
         plt.xlabel("Time")
         plt.ylabel("Value")
         plt.grid(False)
     def trend(time, slope=0):
         return slope * time
     def seasonal_pattern(season_time):
         """Just an arbitrary pattern, you can change it if you wish"""
         return np.where(season_time < 0.1,</pre>
                         np.cos(season_time * 6 * np.pi),
                         2 / np.exp(9 * season_time))
     def seasonality(time, period, amplitude=1, phase=0):
         """Repeats the same pattern at each period"""
         season_time = ((time + phase) % period) / period
         return amplitude * seasonal_pattern(season_time)
     def noise(time, noise_level=1, seed=None):
         rnd = np.random.RandomState(seed)
```

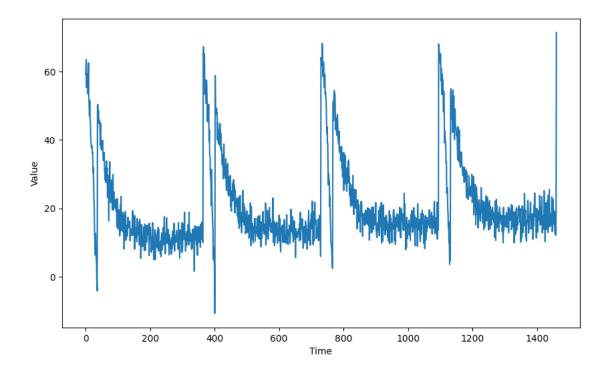
```
return rnd.randn(len(time)) * noise_level
```

You will be generating the same time series data as in last week's assignment.

Notice that this time all the generation is done within a function and global variables are saved within a dataclass. This is done to avoid using global scope as it was done in during the first week of the course.

If you haven't used dataclasses before, they are just Python classes that provide a convenient syntax for storing data. You can read more about them in the docs.

```
[3]: def generate_time_series():
         # The time dimension or the x-coordinate of the time series
         time = np.arange(4 * 365 + 1, dtype="float32")
         # Initial series is just a straight line with a y-intercept
         y_intercept = 10
         slope = 0.005
         series = trend(time, slope) + y_intercept
         # Adding seasonality
         amplitude = 50
         series += seasonality(time, period=365, amplitude=amplitude)
         # Adding some noise
         noise_level = 3
         series += noise(time, noise_level, seed=51)
         return time, series
     # Save all "global" variables within the G class (G stands for global)
     @dataclass
     class G:
         TIME, SERIES = generate_time_series()
         SPLIT_TIME = 1100
         WINDOW SIZE = 20
         BATCH SIZE = 32
         SHUFFLE_BUFFER_SIZE = 1000
     # Plot the generated series
     plt.figure(figsize=(10, 6))
     plot_series(G.TIME, G.SERIES)
     plt.show()
```



1.2 Processing the data

Since you already coded the train_val_split and windowed_dataset functions during past week's assignments, this time they are provided for you:

```
[5]: def windowed_dataset(series, window_size=G.WINDOW_SIZE, batch_size=G.

BATCH_SIZE, shuffle_buffer=G.SHUFFLE_BUFFER_SIZE):
    dataset = tf.data.Dataset.from_tensor_slices(series)
    dataset = dataset.window(window_size + 1, shift=1, drop_remainder=True)
    dataset = dataset.flat_map(lambda window: window.batch(window_size + 1))
    dataset = dataset.shuffle(shuffle_buffer)
```

```
dataset = dataset.map(lambda window: (window[:-1], window[-1]))
  dataset = dataset.batch(batch_size).prefetch(1)
  return dataset

# Apply the transformation to the training set
dataset = windowed_dataset(series_train)
```

```
Metal device set to: Apple M1 Pro

2023-04-05 13:08:07.786452: I

tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:305]

Could not identify NUMA node of platform GPU ID 0, defaulting to 0. Your kernel

may not have been built with NUMA support.

2023-04-05 13:08:07.787288: I

tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:271]

Created TensorFlow device (/job:localhost/replica:0/task:0/device:GPU:0 with 0

MB memory) -> physical PluggableDevice (device: 0, name: METAL, pci bus id:

<undefined>)
```

1.3 Defining the model architecture

Now that you have a function that will process the data before it is fed into your neural network for training, it is time to define you layer architecture. Unlike previous weeks or courses in which you define your layers and compile the model in the same function, here you will first need to complete the create_uncompiled_model function below.

This is done so you can reuse your model's layers for the learning rate adjusting and the actual training.

Hint: - Fill in the Lambda layers at the beginning and end of the network with the correct lamda functions. - You should use SimpleRNN or Bidirectional(LSTM) as intermediate layers. - The last layer of the network (before the last Lambda) should be a Dense layer.

```
[9]: # Test your uncompiled model
uncompiled_model = create_uncompiled_model()

try:
    uncompiled_model.predict(dataset)
except:
    print("Your current architecture is incompatible with the windowed dataset, use try adjusting it.")
else:
    print("Your current architecture is compatible with the windowed dataset!:
    print("Your current architecture is compatible with the windowed dataset!:
    print("Your current architecture is compatible with the windowed dataset!:
```

1.4 Adjusting the learning rate - (Optional Exercise)

As you saw in the lecture you can leverage Tensorflow's callbacks to dinamically vary the learning rate during training. This can be helpful to get a better sense of which learning rate better acommodates to the problem at hand.

Notice that this is only changing the learning rate during the training process to give you an idea of what a reasonable learning rate is and should not be confused with selecting the best learning rate, this is known as hyperparameter optimization and it is outside the scope of this course.

For the optimizers you can try out: - tf.keras.optimizers.Adam - tf.keras.optimizers.SGD with a momentum of 0.9

```
model.compile(loss=tf.keras.losses.Huber(),
           optimizer=optimizer,
           metrics=["mae"])
     ### END CODE HERE
    history = model.fit(dataset, epochs=100, callbacks=[lr_schedule])
    return history
[12]: # Run the training with dynamic LR
  lr_history = adjust_learning_rate()
  Epoch 1/100
  2023-04-05 13:11:36.664883: I
  tensorflow/core/grappler/optimizers/custom_graph_optimizer_registry.cc:113]
  Plugin optimizer for device_type GPU is enabled.
  53.3393 - lr: 1.0000e-06
  Epoch 2/100
  9.9924 - lr: 1.1220e-06
  Epoch 3/100
  7.6574 - lr: 1.2589e-06
  Epoch 4/100
  6.7612 - lr: 1.4125e-06
  Epoch 5/100
  6.0493 - lr: 1.5849e-06
  Epoch 6/100
  5.3585 - lr: 1.7783e-06
  Epoch 7/100
  4.9570 - lr: 1.9953e-06
  Epoch 8/100
  4.7071 - lr: 2.2387e-06
  Epoch 9/100
  4.5065 - lr: 2.5119e-06
  Epoch 10/100
```

4.3383 - lr: 2.8184e-06

```
Epoch 11/100
4.3923 - lr: 3.1623e-06
Epoch 12/100
4.7053 - lr: 3.5481e-06
Epoch 13/100
4.3123 - lr: 3.9811e-06
Epoch 14/100
4.1857 - lr: 4.4668e-06
Epoch 15/100
4.2569 - lr: 5.0119e-06
Epoch 16/100
4.0750 - lr: 5.6234e-06
Epoch 17/100
4.2209 - lr: 6.3096e-06
Epoch 18/100
3.7645 - lr: 7.0795e-06
Epoch 19/100
3.9169 - lr: 7.9433e-06
Epoch 20/100
4.0058 - lr: 8.9125e-06
Epoch 21/100
3.7227 - lr: 1.0000e-05
Epoch 22/100
4.1799 - lr: 1.1220e-05
Epoch 23/100
4.5222 - lr: 1.2589e-05
Epoch 24/100
34/34 [=============== ] - 11s 333ms/step - loss: 3.4625 - mae:
3.9320 - lr: 1.4125e-05
Epoch 25/100
4.3392 - lr: 1.5849e-05
Epoch 26/100
3.9500 - lr: 1.7783e-05
```

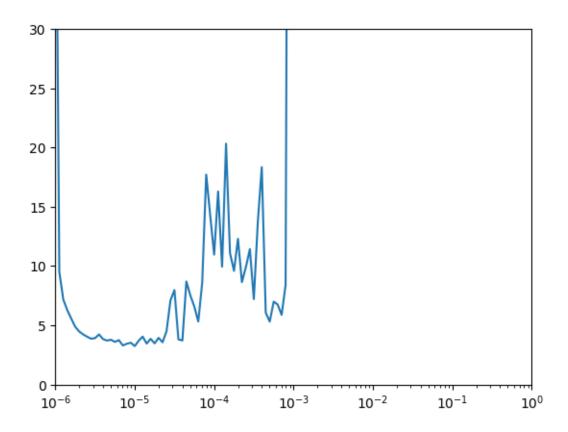
```
Epoch 27/100
4.4152 - lr: 1.9953e-05
Epoch 28/100
4.0463 - lr: 2.2387e-05
Epoch 29/100
4.9733 - lr: 2.5119e-05
Epoch 30/100
7.5976 - lr: 2.8184e-05
Epoch 31/100
8.4703 - lr: 3.1623e-05
Epoch 32/100
4.2947 - lr: 3.5481e-05
Epoch 33/100
4.1911 - lr: 3.9811e-05
Epoch 34/100
9.1849 - lr: 4.4668e-05
Epoch 35/100
8.0200 - lr: 5.0119e-05
Epoch 36/100
7.0733 - lr: 5.6234e-05
Epoch 37/100
5.7944 - lr: 6.3096e-05
Epoch 38/100
9.1072 - lr: 7.0795e-05
Epoch 39/100
18.2155 - lr: 7.9433e-05
Epoch 40/100
14.7976 - lr: 8.9125e-05
Epoch 41/100
11.4587 - lr: 1.0000e-04
Epoch 42/100
16.7833 - lr: 1.1220e-04
```

```
Epoch 43/100
10.4377 - lr: 1.2589e-04
Epoch 44/100
20.8206 - lr: 1.4125e-04
Epoch 45/100
11.5769 - lr: 1.5849e-04
Epoch 46/100
10.0851 - lr: 1.7783e-04
Epoch 47/100
12.7939 - lr: 1.9953e-04
Epoch 48/100
9.1255 - lr: 2.2387e-04
Epoch 49/100
10.4130 - lr: 2.5119e-04
Epoch 50/100
11.9265 - lr: 2.8184e-04
Epoch 51/100
7.6970 - lr: 3.1623e-04
Epoch 52/100
14.2264 - lr: 3.5481e-04
Epoch 53/100
18.8438 - lr: 3.9811e-04
Epoch 54/100
6.5555 - lr: 4.4668e-04
Epoch 55/100
5.7969 - lr: 5.0119e-04
Epoch 56/100
34/34 [=============== ] - 12s 338ms/step - loss: 7.0013 - mae:
7.4862 - lr: 5.6234e-04
Epoch 57/100
7.2437 - lr: 6.3096e-04
Epoch 58/100
6.3590 - lr: 7.0795e-04
```

```
Epoch 59/100
8.8856 - lr: 7.9433e-04
Epoch 60/100
99.9819 - lr: 8.9125e-04
Epoch 61/100
117.5362 - lr: 0.0010
Epoch 62/100
358.6143 - lr: 0.0011
Epoch 63/100
498.7973 - lr: 0.0013
Epoch 64/100
449.7979 - lr: 0.0014
Epoch 65/100
333.9644 - lr: 0.0016
Epoch 66/100
682.2157 - lr: 0.0018
Epoch 67/100
1202.6833 - lr: 0.0020
Epoch 68/100
488.9872 - lr: 0.0022
Epoch 69/100
751.5267 - lr: 0.0025
Epoch 70/100
1102.5394 - lr: 0.0028
Epoch 71/100
1608.7765 - lr: 0.0032
Epoch 72/100
743.3171 - lr: 0.0035
Epoch 73/100
845.1494 - lr: 0.0040
Epoch 74/100
2254.4783 - lr: 0.0045
```

```
Epoch 75/100
1072.5190 - lr: 0.0050
Epoch 76/100
2605.1980 - lr: 0.0056
Epoch 77/100
4015.3606 - lr: 0.0063
Epoch 78/100
2435.2856 - lr: 0.0071
Epoch 79/100
4764.0381 - lr: 0.0079
Epoch 80/100
2926.9180 - lr: 0.0089
Epoch 81/100
4431.5117 - lr: 0.0100
Epoch 82/100
6161.8115 - lr: 0.0112
Epoch 83/100
3865.4109 - lr: 0.0126
Epoch 84/100
7332.2271 - lr: 0.0141
Epoch 85/100
mae: 10481.0166 - lr: 0.0158
Epoch 86/100
mae: 10118.3037 - lr: 0.0178
Epoch 87/100
8478.8203 - lr: 0.0200
Epoch 88/100
mae: 11397.4414 - lr: 0.0224
Epoch 89/100
mae: 10399.5469 - lr: 0.0251
Epoch 90/100
mae: 18172.4297 - lr: 0.0282
```

```
Epoch 91/100
  mae: 19768.1562 - lr: 0.0316
  Epoch 92/100
  mae: 17535.7734 - lr: 0.0355
  Epoch 93/100
  8418.4053 - lr: 0.0398
  Epoch 94/100
  9509.5312 - lr: 0.0447
  Epoch 95/100
  mae: 30229.4941 - lr: 0.0501
  Epoch 96/100
  mae: 36539.4492 - lr: 0.0562
  Epoch 97/100
  mae: 36878.5508 - lr: 0.0631
  Epoch 98/100
  mae: 38701.0039 - lr: 0.0708
  Epoch 99/100
  mae: 51588.9805 - lr: 0.0794
  Epoch 100/100
  34/34 [============= ] - 13s 370ms/step - loss: 56037.8203 -
  mae: 56038.3203 - lr: 0.0891
[13]: # Plot the loss for every LR
  plt.semilogx(lr_history.history["lr"], lr_history.history["loss"])
  plt.axis([1e-6, 1, 0, 30])
[13]: (1e-06, 1.0, 0.0, 30.0)
```



1.5 Compiling the model

Now that you have trained the model while varying the learning rate, it is time to do the actual training that will be used to forecast the time series. For this complete the create_model function below.

Notice that you are reusing the architecture you defined in the create_uncompiled_model earlier. Now you only need to compile this model using the appropriate loss, optimizer (and learning rate).

Hint: - The training should be really quick so if you notice that each epoch is taking more than a few seconds, consider trying a different architecture.

• If after the first epoch you get an output like this: loss: nan - mae: nan it is very likely that your network is suffering from exploding gradients. This is a common problem if you used SGD as optimizer and set a learning rate that is too high. If you encounter this problem consider lowering the learning rate or using Adam with the default learning rate.

```
[14]: def create_model():
    tf.random.set_seed(51)
    model = create_uncompiled_model()
```

```
### START CODE HERE
    model.compile(loss=tf.keras.losses.Huber(),
           optimizer=tf.keras.optimizers.SGD(learning_rate=1e-5,__
   \rightarrowmomentum=0.9),
           metrics=["mae"])
    ### END CODE HERE
    return model
[15]: # Save an instance of the model
  model = create_model()
  # Train it
  history = model.fit(dataset, epochs=50)
  Epoch 1/50
  2023-04-05 13:31:10.081963: I
  tensorflow/core/grappler/optimizers/custom_graph_optimizer_registry.cc:113]
  Plugin optimizer for device_type GPU is enabled.
  14.4950
  Epoch 2/50
  Epoch 3/50
  5.5000
  Epoch 4/50
  5.8862
  Epoch 5/50
  4.2969
  Epoch 6/50
  4.1587
  Epoch 7/50
  4.1037
  Epoch 8/50
  5.3158
  Epoch 9/50
```

```
4.3463
Epoch 10/50
3.8830
Epoch 11/50
Epoch 12/50
3.8155
Epoch 13/50
4.6797
Epoch 14/50
4.1400
Epoch 15/50
3.8165
Epoch 16/50
3.5806
Epoch 17/50
4.2569
Epoch 18/50
3.9468
Epoch 19/50
3.4853
Epoch 20/50
5.0497
Epoch 21/50
3.6316
Epoch 22/50
3.9215
Epoch 23/50
3.8909
Epoch 24/50
4.2335
Epoch 25/50
```

```
3.3613
Epoch 26/50
3.5085
Epoch 27/50
3.4866
Epoch 28/50
3.6330
Epoch 29/50
4.0004
Epoch 30/50
3.5668
Epoch 31/50
3.9260
Epoch 32/50
3.4659
Epoch 33/50
3.7303
Epoch 34/50
3.4394
Epoch 35/50
3.5482
Epoch 36/50
3.9317
Epoch 37/50
4.1454
Epoch 38/50
3.2524
Epoch 39/50
3.6343
Epoch 40/50
3.4122
Epoch 41/50
```

```
3.7503
Epoch 42/50
Epoch 43/50
3.3733
Epoch 44/50
34/34 [=======
         =========] - 11s 329ms/step - loss: 2.9403 - mae:
3.4039
Epoch 45/50
34/34 [=============== ] - 11s 334ms/step - loss: 2.9266 - mae:
3.3929
Epoch 46/50
3.2794
Epoch 47/50
34/34 [============== ] - 11s 332ms/step - loss: 2.9003 - mae:
3.3609
Epoch 48/50
3.8901
Epoch 49/50
3.3901
Epoch 50/50
3.4828
```

1.6 Evaluating the forecast

Now it is time to evaluate the performance of the forecast. For this you can use the compute metrics function that you coded in a previous assignment:

```
[16]: def compute_metrics(true_series, forecast):
    mse = tf.keras.metrics.mean_squared_error(true_series, forecast).numpy()
    mae = tf.keras.metrics.mean_absolute_error(true_series, forecast).numpy()
    return mse, mae
```

At this point only the model that will perform the forecast is ready but you still need to compute the actual forecast.

1.7 Faster model forecasts

In the previous week you used a for loop to compute the forecasts for every point in the sequence. This approach is valid but there is a more efficient way of doing the same thing by using batches of data. The code to implement this is provided in the model_forecast below. Notice that the code is very similar to the one in the windowed_dataset function with the differences that:

- The dataset is windowed using window_size rather than window_size + 1
- No shuffle should be used
- No need to split the data into features and labels
- A model is used to predict batches of the dataset

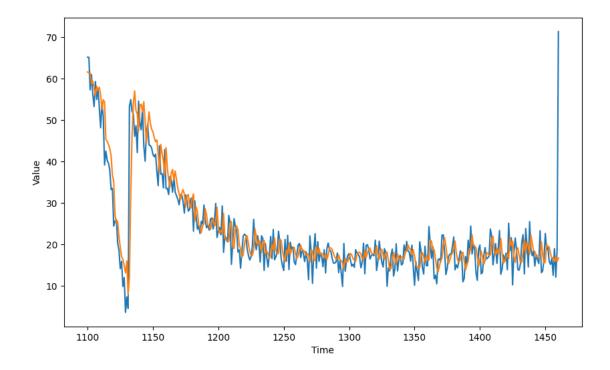
```
[17]: def model_forecast(model, series, window_size):
    ds = tf.data.Dataset.from_tensor_slices(series)
    ds = ds.window(window_size, shift=1, drop_remainder=True)
    ds = ds.flat_map(lambda w: w.batch(window_size))
    ds = ds.batch(32).prefetch(1)
    forecast = model.predict(ds)
    return forecast
```

```
[18]: # Compute the forecast for all the series
rnn_forecast = model_forecast(model, G.SERIES, G.WINDOW_SIZE).squeeze()

# Slice the forecast to get only the predictions for the validation set
rnn_forecast = rnn_forecast[G.SPLIT_TIME - G.WINDOW_SIZE:-1]

# Plot it
plt.figure(figsize=(10, 6))

plot_series(time_valid, series_valid)
plot_series(time_valid, rnn_forecast)
```



Expected Output:

A series similar to this one:

```
[19]: mse, mae = compute_metrics(series_valid, rnn_forecast)
print(f"mse: {mse:.2f}, mae: {mae:.2f} for forecast")
```

mse: 31.85, mae: 3.64 for forecast

To pass this assignment your forecast should achieve an MAE of 4.5 or less.

- If your forecast didn't achieve this threshold try re-training your model with a different architecture (you will need to re-run both create_uncompiled_model and create_model functions) or tweaking the optimizer's parameters.
- If your forecast did achieve this threshold run the following cell to save your model in a tar file which will be used for grading and after doing so, submit your assignment for grading.
- This environment includes a dummy SavedModel directory which contains a dummy model trained for one epoch. To replace this file with your actual model you need to run the next cell before submitting for grading.
- Unlike last week, this time the model is saved using the SavedModel format. This is done because the HDF5 format does not fully support Lambda layers.

```
[20]: # Save your model in the SavedModel format model.save('saved_model/my_model')
```

```
# Compress the directory using tar
! tar -czvf saved_model.tar.gz saved_model/
```

```
INFO:tensorflow:Assets written to: saved_model/my_model/assets
a saved_model
a saved_model/my_model
a saved_model/my_model/keras_metadata.pb
a saved_model/my_model/variables
a saved_model/my_model/saved_model.pb
a saved_model/my_model/assets
a saved_model/my_model/variables/variables.data-00000-of-00001
a saved_model/my_model/variables/variables.index
```

Congratulations on finishing this week's assignment!

You have successfully implemented a neural network capable of forecasting time series leveraging Tensorflow's layers for sequence modelling such as RNNs and LSTMs! This resulted in a forecast that matches (or even surpasses) the one from last week while training for half of the epochs.

Keep it up!