Modeling King County House Sales

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Final Project Submission

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1 Introduction (DONE)

In this note, we are trying to help homeowners to buy or sell homes by predicting the price of the property in **King County**, **WA**. We use some available data from the housing prices in this county to present a model to predict the price of a house.

In order to do so, we use regression methods to find an appropriate model to fit housing price data so that we can predict the price of different houses with different features.

This notebook is organized as follows:

- 2. Importing data. In this part we import the data and we will introduce which columns it contains.
- **3. Functions.** This section contains the functions we defined to perform special computations for us. These functions are:
 - 3.1 corr
 - 3.2 summary_of_results
 - 3.3 concatenate
- 4. Some Insight Into Data. In this section we are trying to identify the categorical and numerical features. By plotting some graphs, we will find the outliers and how to clean the data. This section has the following subsections:
 - 4.1 Scatter Plots for Categorical Features
 - 4.2 Scatter Plots for Numerical data
 - 4.3 Cleaning data
- **5.** Categorical. In this section, we are converting the categorical data into numerical values to be able to use them in the model. This section contains the following subsections:
 - 5.1 Dealing with Null Values
 - 5.2 Converting multi categorical columns to numerical values

- **6. Preprocessing.** In this section, we are going to see the effects of containing different categorical and numerical variables on R2 score to see which features we need to keep. This section contains:
 - 6.1 Putting `grade`, `condition` and `zipcode` into the model.
 - 6.2 Putting only `condition` into the model.
 - 6.3 Putting only `grade` into the model.
 - 6.4 Putting `grade` and `condition` into the model.
 - 6.5 Considering only `grade` into the modeling.
- 7. Features Selection. In this section, based on the dataframe that we found in the previous section, we will try to find the features that we have more information but low collinearity and high R2 score. We use different approaches to decide which features we need to keep. These approaches are used in different subsections which are:
 - 7.1 First Approach By using p-values, R2 scores and Condition number.
- **8. Final Model.** In this section, we find the baseline model to compare the model we found in the previous section with. This section contains the following subsections:
 - 8.1 Baseline Model
 - 8.2 Final Model
 - 8.3 Interpretation
- **9. Prediction.** We will use the model introduced in the section 9 to predict some data.
- 10. Assumption Checking. In this section, we are going to check the regression model's assumptions to see if they are satisfied or not. This section contains the following subsections:
 - 11.1 Normality of Residuals
 - 11.2 Investigating Multicollinearity (Independence Assumption)
 - 11.3 Investigating Homoscedasticity
 - 11.4 Investigating Linearity
- 11. Model's Shortcomings. In this section we mention the limitation of the model and how we can improve it.
- 12. Business Suggestion. In this section we will give some suggestions as an answer to our business question.

2 Importing Data (DONE)

First we are going to import the data and save them into a dataframe called data_initial. After that we select some columns as the features of our model. The dataframe that we are using in the rest of the work contains the following type of variables:

- 1. Numerical Columns
 - price
 - bedrooms
 - bathrooms

- sqft_living
- sqft_lot
- floors
- yr_built
- lat
- long

2. Categorical Columns

- waterfront
- condition
- grade
- zipcode

However, we may not use all of these columns in our model and we need to choose among them as features of our final model.

3 Functions we use (DONE)

In this section, the functions we used to get some information about data (corr function) or create a final dataframe to use (concatenate function) or will return the R2score and condition number (summary_of_results function). These functions are:

- 1. corr
- 2. summary_of_results
- 3. concatenate

Each of these functions is introduced below.

3.1 corr

In order to get the correlation coefficients, we define a function that takes two inputs which are data and then the minimum value of the correlation. This minimum value will be used to find features with correlation more than or equal to this minimum value.

3.2 summary_of_results

In order to update the text automatically and get R2 score and collinearity, we are going to convert results_summary obtained from statsmodels library into Pandas DataFrame to find R2-scores, coefficients and P-values for different models.

```
[4]: def summary_of_results(data, to_drop, pval):
    import statsmodels.api as sm

    features = df_final.drop(columns = to_drop, axis = 1)
    X = sm.add_constant(features)
    model = sm.OLS(df_final["price"], X)
    results = model.fit()
    results_summary = results.summary()

### Converting results_summary to pandas dataframe
    results_R2 = results_summary.tables[0].as_html()
    R2_df = pd.read_html(results_R2, header=0, index_col=0)[0]
    R2_df.reset_index(inplace = True)
    R2_df = R2_df.columns.to_frame().T.append(R2_df, ignore_index=True)
    R2_df.columns = range(len(R2_df.columns))
```

```
results_coeff = results_summary.tables[1].as_html()
coeff_df = pd.read_html(results_coeff, header=0, index_col=0)[0]
coeff_df.reset_index(inplace = True)
coeff_df = coeff_df.columns.to_frame().T.append(coeff_df,
                                                 ignore_index=True)
coeff_df.columns = range(len(coeff_df.columns))
results_collin = results_summary.tables[2].as_html()
collin_df = pd.read_html(results_collin, header=0, index_col=0)[0]
collin_df.reset_index(inplace = True)
collin_df = collin_df.columns.to_frame().T.append(collin_df,
                                                   ignore_index=True)
collin_df.columns = range(len(collin_df.columns))
R2 = R2_df.iloc[0, 3]
collinearity_num = collin_df.iloc[3, 3]
coeff = coeff_df.iloc[1:,[0,4, 1]]
coeff.columns = ["feature", "P-value", "coefficient"]
coeff["coefficient_absolute_value"] = np.abs(coeff["coefficient"])
coeff.sort_values(by = "coefficient_absolute_value",
                        ascending = True, inplace = True)
critical_pval = coeff.loc[coeff["P-value"]>= pval]
return [R2, collinearity_num, critical_pval, coeff]
```

3.3 concatenate

This functions will return the final dataframe that we use for our analysis.

```
data = df_no_outliers
sub_df1 = grade_num_df
sub_df2 = zipcode_num_df
sub_df3 = condition_num_df
include_sub_df1 = include_grade
include_sub_df2 = include_zipcode
include_sub_df3 = include_condition
if (include_sub_df1 == True
    and include_sub_df2 == False
   and include_sub_df3 == False):
    df_final = pd.concat([data, sub_df1], axis = 1)
elif (include_sub_df1 == False
    and include_sub_df2 == True
    and include_sub_df3 == False):
    df_final = pd.concat([data, sub_df2], axis = 1)
elif (include_sub_df1 == False
    and include_sub_df2 == False
    and include_sub_df3 == True):
    df_final = pd.concat([data, sub_df3], axis = 1)
elif include_sub_df1 == True and include_sub_df2 == True:
    df_final = pd.concat([data, sub_df1, sub_df2], axis = 1)
elif include_sub_df1 == True and include_sub_df3 == True:
    df_final = pd.concat([data, sub_df1, sub_df3], axis = 1)
elif include_sub_df2 == True and include_sub_df3 == True:
    df_final = pd.concat([data, sub_df2, sub_df3], axis = 1)
else:
    df_final = pd.concat([data, sub_df1, sub_df2, sub_df3], axis = 1)
return df_final
```

4 Some Insight Into Data (DONE)

In order to find the outliers and how the data looks like, we will check the scatter plots of both categorical and numerical data as well as histogram for numerical data. In order to do so, first we need to find categorical and numerical data. To do this we use select_dtypes method as shown below:

```
[6]: y = df["price"]
numerical = df.drop(columns = ["price", "zipcode"], axis = 1).select_dtypes(
        include=["float64", "int64"])
1 = list(numerical.columns)
1.append("price")
categorical = df.drop(columns = 1, axis = 1)
```

4.1 Scatter Plots for Categorical Features

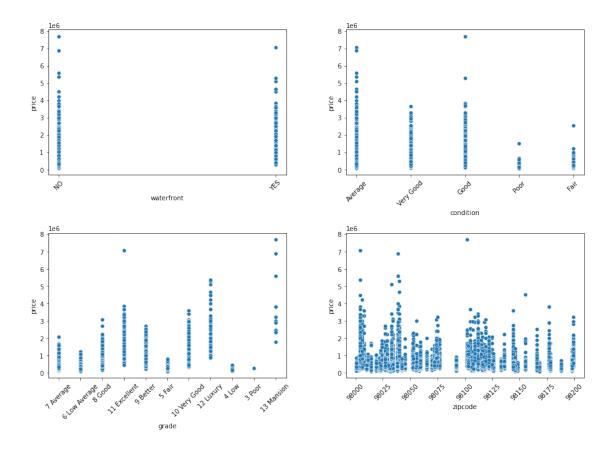
By studying the scatter plots of different categorical variable vs. price, we may find some points that can be considered not that much useful. For example, we see that we only have one data point for 3 Poor in grade column, so we may drop this because we cannot use it.

```
[7]: fig, axes = plt.subplots(nrows = 2, ncols = 2, figsize = (15,10))

fig.subplots_adjust(hspace=0.4, wspace=0.25)

to_pick = list(categorical.columns)

for i,col in enumerate(to_pick):
    ax = axes[i//2][i%2]
    sns.scatterplot(x = df[col], y = df["price"], ax = ax)#, label = col)
    ax.tick_params(axis='x', labelrotation = 45)
```



```
[8]: len(df.loc[df["grade"] == "3 Poor"])
```

[8]: 1

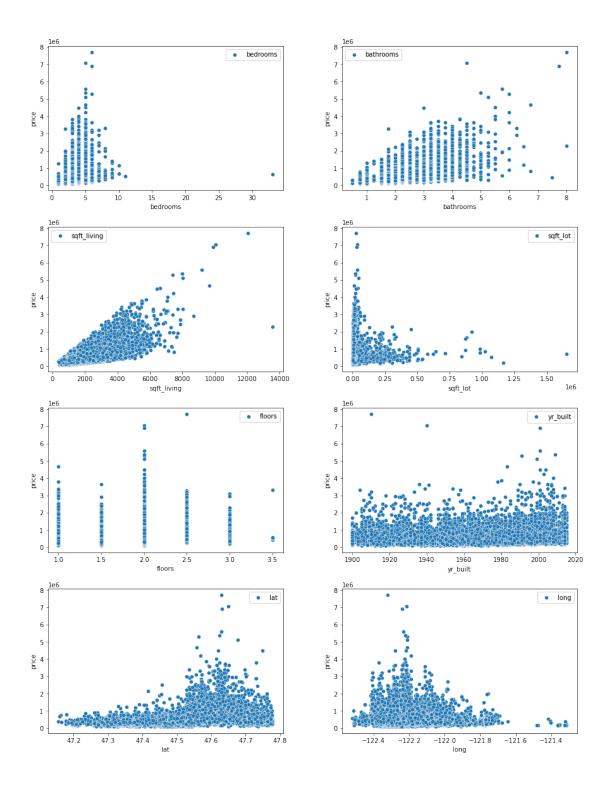
4.2 Scatter Plots for Numerical data

In this section, by checking the scatter plot of numerical data vs. price, we may be able to find some outliers. For example we see that there is a point with more than 30 rooms. Also, we see that there are houses with less than a bathroom. So, checking these scatter plots will help us with finding some outliers and not that useful data points.

```
[9]: fig, axes = plt.subplots(nrows = 4, ncols = 2, figsize = (15,20))
fig.subplots_adjust(hspace=0.25, wspace=0.25)

to_pick = list(numerical.columns)

for i,col in enumerate(to_pick):
    ax = axes[i//2][i%2]
    sns.scatterplot(x = df[col], y = df["price"], ax = ax, label = col)
```



[10]: len(df.loc[df["floors"] == 3.5])

[10]: 7

4.3 Cleaning data

First we are going to drop the outliers for highest and lowest prices. In order to do so, we are going to drop the row in price column that are more/less than 3 standard deviations from average price. In order to do that, we are going to use the function stats.zscore from scipy.stats library.

```
import scipy.stats as stats
import warnings
warnings.filterwarnings("ignore")

z = stats.zscore(df["price"], ddof=0)
df["z_score"] = stats.zscore(df["price"], ddof=0)
df_no_outliers = df.loc[(df["z_score"] < 3) & (df["z_score"] > -3)]
df_no_outliers.drop(columns = "z_score", axis = 1, inplace = True)
```

As we can see there are some outliers in the bedrooms, sqft_lot and sqft_living. So, we are going to drop houses with more than NameError: name 'max_b' is not defined bedrooms, NameError: name 'max_bath' is not defined bathrooms, and NameError: name 'max_floors' is not defined floors as well as houses with less than NameError: name 'min_bath' is not defined bathrooms. Moreover, we are going to drop the houses with the highest values of sqft_lot and sqft_living and the only data whose grade is 3 Poor.

```
categorical = df_no_outliers.drop(columns = 1, axis = 1)
```

Now we are going to convert (scaling and normalizing) the data in the columns price, lat, long, yr_built, sqft_living and sqft_lot to make the data more normal. However, if we check we realize that the values of the column long are all negative and we need to first multiply them with a minus sign to be able to convert them by a logarithmic function.

```
[14]: sum(df_no_outliers["long"] > 0)
    df_no_outliers["long"] = -1 * df_no_outliers["long"]
    to_convert = ["price", "long", "lat", 'sqft_living', 'sqft_lot', "yr_built" ]
    for item in to_convert:
        if item == "price":
            df_no_outliers[item] = np.log(df_no_outliers[item])
        else:
            df_no_outliers[item] = np.log(df_no_outliers[item])
            numerical[item] = np.log(numerical[item])
```

After cleaning, we are going to check the histogram and scatter plots of the data that are recently converted.

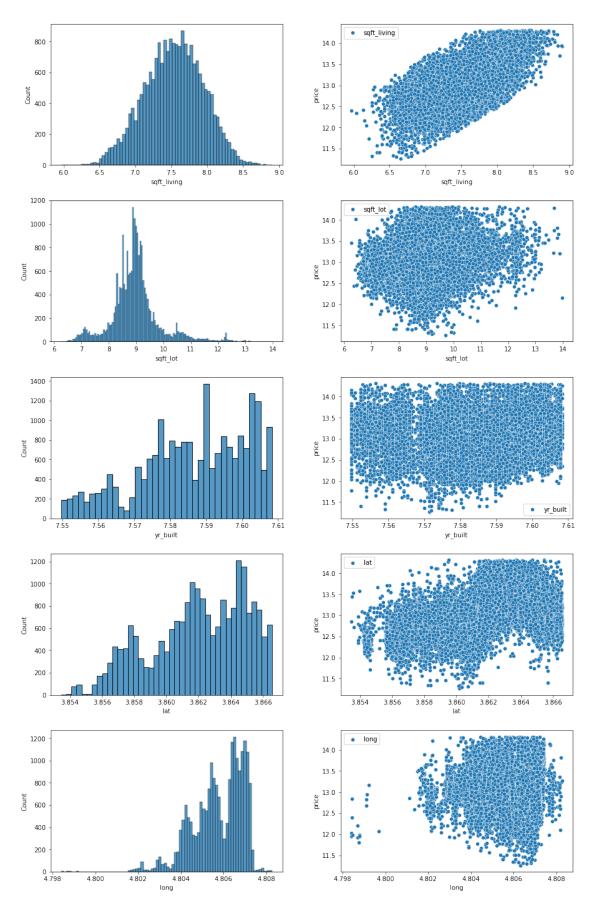
```
[15]: to_pick = list(numerical.columns)

to_pick.remove("bedrooms")
to_pick.remove("bathrooms")

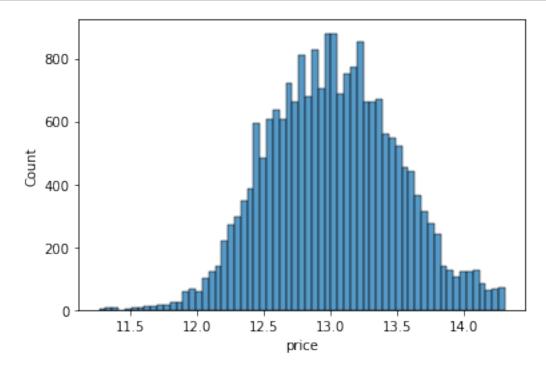
to_pick.remove("floors")

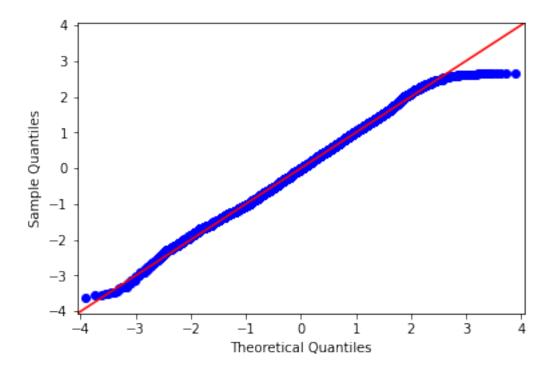
r = len(to_pick)
c = 2
fig, axes = plt.subplots(nrows = r, ncols = c, figsize = (15,25))
fig.subplots_adjust(hspace=0.25, wspace=0.25)

for i,col in enumerate(to_pick):
    axh = axes[i%r][0]
    axs = axes[i%r][1]
    sns.histplot(x = df_no_outliers[col], ax = axh, label = col)
    sns.scatterplot(x = df_no_outliers[col], y = df_no_outliers["price"]
    , ax = axs, label = col)
```



Let's also check the histogram and Q-Q plot of price to see if price is normal or not.





5 Categorical (DONE)

We need to convert the categorical data to numerical values so that we can use them in our model. First we are going to find the columns that have missing data.

```
[17]: a = categorical.isna().sum().to_frame().reset_index()
```

We can see that only waterfront has missing values and the total number of values that are missed is 2325.

5.1 Dealing with Null Values

First we are going to create a new column for missing values. We know that the column waterfront has 2325 missing values. Therefore, we are going to create a column called waterfront_null to indicate where data is missing. In order to do so, we take the following steps.

First we use MissingIndicator from sklearn.impute to create a column in df called waterfront_null as shown below:

```
[18]: ### Missing Indicator for waterfront
import warnings
from sklearn.impute import MissingIndicator
warnings.filterwarnings("ignore")
missing_indicator = MissingIndicator()
```

```
null_val = df_no_outliers[["waterfront"]]
missing_indicator.fit(null_val)

df_no_outliers["waterfront_null"] = missing_indicator.transform(null_val)
```

After creating a new column for the missing values, we are going to to impute the missing values in the column waterfront by using SimpleImputer from sklearn.impute as done below

At the end, we will use OrdinalEncoder from from sklearn.preprocessing to convert the binary values into numerical values. To do so, first we need to convert the Column waterfront_impute to numerical value as:

```
[20]: ### Converting the Column waterfront_impute to numerical value
import warnings
warnings.filterwarnings("ignore")

from sklearn.preprocessing import OrdinalEncoder
encoder_waterfront = OrdinalEncoder()
encoder_waterfront.fit(df_no_outliers[["waterfront_impute"]])

encoder_waterfront_transform = encoder_waterfront.transform(
    df_no_outliers[["waterfront_impute"]]).flatten()

df_no_outliers["waterfront_impute"] = encoder_waterfront_transform

df_no_outliers.drop(columns = ['waterfront'], inplace = True, axis = 1)
```

Now we are going to convert the column waterfront_null to Numerical value.

```
[21]: ### Converting the Column waterfront_null to Numerical value import warnings
```

```
warnings.filterwarnings("ignore")
from sklearn.preprocessing import OrdinalEncoder
encoder_waterfront_null = OrdinalEncoder()
encoder_waterfront_null.fit(df_no_outliers[["waterfront_null"]])
encoder_waterfront_null_transform = encoder_waterfront_null.transform(
    df_no_outliers[["waterfront_null"]]).flatten()

df_no_outliers["waterfront_null"] = encoder_waterfront_null_transform
```

5.2 Converting multi-categorical columns to numerical values

The categorical multiple values are stored in columns condition, grade and zipcode. In order to convert them to numerical values we should use OneHotEncoder from sklearn.preprocessing.

First we are going to convert the categorical variable condition to numerical values in the following cell

In the following cell, we are going to do the same thing to convert grade to numerical values

```
[23]: import warnings
warnings.filterwarnings("ignore")

from sklearn.preprocessing import OneHotEncoder

grade_cat = df_no_outliers[["grade"]]

ohe = OneHotEncoder(categories='auto', sparse=False, handle_unknown='ignore')
```

And finally, we are going to converting zipcode to numerical values in the following cell

6 Preprocessing (DONE)

In order to create a model, first we need to decide what features we want to consider in our model. Initially, we will try to calculate R2 score and Cond. No. for different combinations of categorical features to decide which combination we want to choose.

6.1 Putting grade, condition and zipcode into the model.

First we want to see how different features affect the data. If we include grade_num_df, zipcode_num_df and condition_num_df, we get R2-score and collinearity as:

R2 : 0.854

 the R2 score which is 0.854 is really good but Cond. No. which is 2380000000000000.0. If we calculate the variance-inflation factors we will notice that including zipcode_num_df into the final dataframe will cause a lot of collinearities as shown below

We can see that the number of coefficients with Variance Inflation Factor more than 5 is around

```
[33]: print(sum(variance_inf_fact>5))
```

49

Therefore, we just exclude zipcode from rest of the work and we can use lat and long as a method to check the location of different houses.

6.2 Putting only condition into the model.

If we only consider condition in the model, we find R2 and Cond. No. as

R2 : 0.659 Cond. No. : 1.44e+16

Therefore, considering only condition in the model will result in R2 score equals to 0.659 and Cond. No. equals 1.44e+16 which are ,respectively, lower and higher than previous cases. We will

check the collinearity by using Variance Inflation Factor as:

```
[37]: from statsmodels.stats.outliers_influence import variance_inflation_factor
      import statsmodels.api as sm
      df_final = concatenate(include grade = False, include_zipcode = False,
                             include_condition = True)
      to_drop = ["price"]
      XX = df_final.drop(columns = to_drop, axis = 1)
      XX_constant_added = sm.add_constant(XX)
      vif = \Gamma
          variance_inflation_factor(XX_constant_added.values, i)
             range(XX_constant_added.shape[1])
      variance_inf_fact = pd.Series(vif, index=XX_constant_added.columns,
                                    name="Variance Inflation Factor")
```

```
[38]: variance_inf_fact
```

```
[38]: const
                            0.000000
                            1.669104
      bedrooms
      bathrooms
                            3.036816
      sqft_living
                            3.257208
      sqft_lot
                            1.642007
      floors
                            1.757113
                            2.065253
      yr_built
      lat
                            1.092286
      long
                            1.476550
      waterfront_null
                            1.000601
                            1.016638
      waterfront_impute
      Average
                                 inf
      Fair
                                 inf
      Good
                                 inf
      Poor
                                 inf
      Very Good
                                 inf
```

Name: Variance Inflation Factor, dtype: float64

From this we realize that there are a lot of collinearities in the model and it is because we considered conditions as a part of the model.

6.3 Putting only grade into the model.

Now, finally if we only consider grade as the only categorical variable in the model, we find

R2 : 0.724 Cond. No. : 3.08e+16

Relative to the case where we only considered condition, we see that R2 score has increased from 0.659 to 0.724 while Cond. No. has changed from 1.44e+16 to 3.08e+16 and the collinearity can be found as:

[41]: variance_inf_fact

```
[41]: const
                            0.000000
      bedrooms
                            1.727743
      bathrooms
                            3.063405
      sqft_living
                            4.282652
      sqft_lot
                            1.676991
      floors
                            1.807908
      yr_built
                            2.039266
      lat
                            1.117938
```

```
long
                       1.491353
waterfront_null
                       1.000842
waterfront_impute
                      1.016886
10 Very Good
                            inf
11 Excellent
                            inf
12 Luxury
                            inf
4 Low
                            inf
5 Fair
                            inf
6 Low Average
                            inf
7 Average
                            inf
8 Good
                            inf
9 Better
                            inf
```

Name: Variance Inflation Factor, dtype: float64

In this case we have a lot of collinearity but we have a higher R2 score. So, we may be able to make some changes in this combination and get a better results. So, this combination is one of the candidate to be used for making a model.

6.4 Putting grade and condition into the model.

Now let's check how grade_num_df and condition_num_df affect the modeling. Therefore, we only consider these two features and we will get R2-score and collinearity as:

R2 : 0.729 Cond. No. : 1.19e+17

Again, we see that the R2 score which is 0.729 is really good but Cond. No. which is 1.19e+17 is really high. Compare to the previous case that we found R2 to be 0.724 and Cond. No. to be 3.08e+16, we see that R2 is slightly better but Cond. No. has increased a lot.

However, both condition and grade might be responsible for the quality of the house and we can just exclude one of them and use the other one. Before deciding which one to drop, let's check the coefficients with p-values greater than 0.05.

```
[43]: gc[2]
```

```
[43]: feature P-value coefficient coefficient_absolute_value
10 waterfront_null 0.445 -0.0042 0.0042
```

We can see that waterfront_null has p-values more than the critical value of 0.05. Therefore, we are going to drop this columns. On the other hand, if a house has a view to a water fall, they would not miss the data and they will state that the property has that view. So, waterfall_null

might be just those houses that they do not have the view which they are already in the model. Therefore, we are going to include these categorical variables in the model and we will try to find the best features which will reduce the collinearity of the model's features.

```
[44]: df_final.drop(columns = ["waterfront_null", "long"], axis = 1, inplace = True)
```

First we are going to drop waterfront_null and long from the dataframe and will check the R2 and Cond. No.. At the same time we are going to calculate the correlation table to find the highly correlated features as

R2 : 0.729 Cond. No. : 1.13e+17

Also we may check the correlation coefficients as:

```
[56]: print(corr(df_final, value = 0.8))
```

```
0 pairs 0 0.814728 (Good, Average)
```

As we can see, Average and Good are highly correlated so we are going to drop Average and will keep only Good.

```
[57]: df_final.drop(columns = ["Average"], axis = 1, inplace = True)
```

By checking the coefficients, we notice that there are several groups of features that almost have similar coefficients which can we group them to reduce the number of features. In order to do so, we define new columns that contains linear combination of these features. These columns are:

```
1. df_final["MLE"] = df_final["13 Mansion"] + df_final["12 Luxury"] +
    df_final["11 Excellent"]
```

- 2. df_final["BV"] = df_final["10 Very Good"] + df_final["9 Better"]
- 3. df_final["LF"] = df_final["4 Low"] + df_final["5 Fair"]
- 4. df_final["LA"] = df_final["7 Average"] + df_final["6 Low Average"]

Moreover, we notice that by ignoring the following features, we can significantly reduce the collinearity from 1.13e+17 to 24200.0

3 Poor, 8 Good, floors, bedrooms, Good, Very Good, floors, bedrooms, bathrooms.

R2 : 0.708 Cond. No. : 24200.0

However, we could not reduce the collinearity more than what we obtained. The reason might be because of including both categorical variables condition and grade. Therefore, we are jut going to pick one of them and we will drop the other one. For now we will not include conditions and we only include grade as a metric to determine the quality and condition of a house.

```
gc = summary_of_results(data = df_final, to_drop = to_drop, pval = 0.05)
print("R2 : ", gc[0])
print("Cond. No.: ", gc[1])
# gc[3]
```

R2 : 0.708 Cond. No. : 24200.0

Now to check the collinearity we will use variance inflation factor to see which coefficient has a value more than 5.

[61]: variance_inf_fact

```
[61]: const
                           2.658851e+06
      sqft_living
                           2.053800e+00
      sqft_lot
                           1.213567e+00
     yr_built
                           1.361740e+00
                           1.103982e+00
      lat
      waterfront_impute
                           1.006970e+00
     Fair
                           1.014862e+00
     Poor
                           1.013944e+00
     EL
                           1.124267e+00
     BV
                           1.518348e+00
     LF
                           1.169037e+00
```

```
LA 1.815533e+00
Name: Variance Inflation Factor, dtype: float64
```

We can see that all of the coefficients are under 5 which is a good sign because it shows that the collinearity is minimized in this model. However, the issue is that the coefficients of the features EL, BV, LF, and LA are not clear and it is hard to interpret them. Therefore, we may ignore this model and move forward to find another model.

6.5 Considering only grade into the modeling.

As we saw, including both conditions and grades will result in a high collinearity. Therefore, we are going to only include grade in our data sets. By doing so, we get R2 equals to 0.724 and Cond. No. equals to 3.08e+16 as shown below

R2 : 0.724 Cond. No. : 3.08e+16

However, we notice that waterfront_null has P-Values more than 0.05. Therefore, we are going to drop this feature, as a result we find R2 and Cond. No. to be equal to 0.724 and 2.95e+16, respectively, as shown below:

R2 : 0.724 Cond. No. : 2.95e+16

Now, we notice that there are some features whose coefficients are close to each other. Therefore, we can group them and create new columns (as we did in the previous section) to reduce these features. Moreover, we see that if we drop some features we can reduce the collinearity significantly as shown below

```
, "5 Fair", "4 Low"
, "9 Better"
, "12 Luxury", "11 Excellent"
, "6 Low Average", "7 Average", "8 Good"
, "sqft_lot", "bedrooms", "floors", "bathrooms"]

df_final["LF"] = df_final["4 Low"] + df_final["5 Fair"]

df_final["MLE"] = df_final["11 Excellent"] + df_final["12 Luxury"]

df_final["LAG"] = (df_final["6 Low Average"] + df_final["7 Average"] + df_final["8 Good"])

g4 = summary_of_results(data = df_final, to_drop = to_drop, pval = 0.05)
print("R2 : ", g4[0])
print("Cond. No.: ", g4[1])
# g4[3]
```

R2 : 0.678 Cond. No. : 18200.0

The problem is that we almost lost all the numerical features and we have a much lower R2. Therefore, we need to drop some categorical features and not combine them so that we can keep some of the numerical features. However, before that, let's check the variance_inflation_factor

```
[70]: const 2.420026e+06
sqft_living 1.603750e+00
```

Name: Variance Inflation Factor, dtype: float64

These numbers are below 5 and we can conclude that collinearity between features is low. However, because we combined several variables, it is hard to interpret the coefficients.

7 Features Selection (DONE)

In this section, we are going to find the features we want in the model, by checking R2 score, Cond. No. and variance inflation factor of each model that we find by trial and error. At the end, we will present the final model.

Now we will try to drop categorical features to improve R2 and Cond. No.. This process is shown below:

- 1. First we drop waterfront_null, long because the p-values for them are more than 0.05. After dropping these columns, we find R2 and Cond. No. as 0.752 and 2.58e+16, respectively. Now we go to the next step.
- 2. We see that the coefficients of the features 12 Luxury, 11 Excellent and 10 Very Good are close to each other, so we may be able to drop two of them and keep one of them. We see if we drop one of them and keep the others, we find that R2 score and Cond. No. will become 0.752 and 26200. This is an improvement in the collinearity. Also, we tried and notice that if we drop two of them and keep one of them, these numbers do not change. So, we are going to keep 10 Very Good and drop the others. Now we go to the next step.
- 3. Now we are checking the p-value and we see that 3 Poor has a high p value. So, we are going to drop this feature. This will not change the desired scores. Now we go to the next step.
- 4. We can see that sqft_lot has the lowest coefficient compares to the rest of the features. Therefore, we are going to drop this feature. By doing so, we get R2 equals to 0.751 and Cond. No. equals to 20900.0. However, we notice that after dropping this feature, the other coefficients changed significantly and they got closer to each other.

R2 : 0.724 Cond. No. : 20900.0

[73]: const

Now, to make a better judgment, we are going to calculate the variance_inflation_factor of each feature and we will drop the features with variance_inflation_factor more than 5

```
bedrooms
                     1.726551e+00
bathrooms
                     3.010845e+00
sqft_living
                     3.806831e+00
floors
                     1.579189e+00
yr built
                     1.757285e+00
                     1.089267e+00
lat
waterfront_impute
                     1.008661e+00
10 Very Good
                     4.018333e+00
4 Low
                     1.076849e+00
5 Fair
                     2.106338e+00
6 Low Average
                     9.240997e+00
7 Average
                     2.084637e+01
8 Good
                     1.596404e+01
9 Better
                     8.340610e+00
Name: Variance Inflation Factor, dtype: float64
```

2.817982e+06

From this calculation, we are going to drop either 9 Better or 6 Low Average or both and we see how R2 changes. After than we again will check the variance_inflation_factors of coefficients to make sure that all the values are below 5.

We notice that if we drop both 9 Better and 6 Low Average, we will get R2 as 0.670 and if we only drop 9 Better while keeping 6 Low Average in the model we find R2 to be 0.716 and if we drop 9 Better and keep 6 Low Average, we find R2 as 0.689. Therefore, we will drop 9 Better and keep 6 Low Average in the model. Moreover, we noticed that if we keep 12 Luxury and 11 Excellent in the model, the R2 will change to 0.720 which is an improvement.

R2 : 0.720 Cond. No. : 20300.0

We see that R2 decreased significantly and Cond. No. also has increased. So, we are going to check the variance inflation factor method of each feature as:

```
[75]: const 2.749223e+06
bedrooms 1.685800e+00
sqft_living 3.095564e+00
floors 1.492513e+00
```

```
1.610135e+00
yr_built
                      1.088157e+00
lat
waterfront_impute
                      1.008530e+00
10 Very Good
                      2.377908e+00
11 Excellent
                      1.497874e+00
12 Luxury
                      1.064289e+00
4 Low
                      1.008810e+00
5 Fair
                      1.108188e+00
7 Average
                      3.729220e+00
8 Good
                      4.462613e+00
9 Better
                      3.604696e+00
Name: Variance Inflation Factor, dtype: float64
```

We see that the values are below 5 so we should accept these values. So, we fill define a function to give us the final dataframe as defined below:

```
[76]: def final dataframe():
          df_final = concatenate(include_grade = True, include_zipcode = False,
                             include_condition = False)
          to_drop = ["waterfront_null", "long"
                , "6 Low Average", "sqft_lot", "bathrooms"]
          df_final.drop(columns = to_drop, axis = 1, inplace = True)
          return df_final
```

Final Model (almost DONE)

In this section we are going to introduce baseline model and the final model and we will compare the results of the final model with the base line model. We will use split our data to train and test sets one for modeling and the other for checking the results.

Baseline Model 8.1

We will introduce a baseline model to compare the results of the model we propose with the result of the baseline model. In order to find the baseline model, we will find a variable that has the highest correlation with the price.

```
[80]: numerical_II = df_no_outliers.drop(columns = "price", axis = 1).select_dtypes(
          include=["float64", "int64"])
      corr column = list(numerical II.columns)
      corr_dict = {}
      for item in corr_column:
          corr_dict[df_no_outliers["price"].corr(df_no_outliers[item])] = item
      high_corr = corr_dict[max(corr_dict)]
      high_corr
```

[80]: 'sqft_living'

Now, we are going to find the R2 of the base line model for different test train sets

Train score: 0.4080095230264854 Validation score: 0.4147140046119352

8.2 Final Model

Now we are going to make the final model and will split the data into train and test sets so that we can compare the R2 score of the final model with that of the baseline model.

```
[87]: from sklearn.model_selection import train_test_split
    df_final = final_dataframe()
    X = df_final.drop(columns = "price", axis = 1)
    y = df_final["price"]
    X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42)

# X_train = sm.add_constant(X_train)
# X_test = sm.add_constant(X_test)
```

```
[88]: from sklearn.linear_model import LinearRegression from sklearn.model_selection import cross_validate, ShuffleSplit second_model = LinearRegression()
```

Train score(mean): 0.7204077469223853 Validation score(mean): 0.7196751357685064

Train score: 0.4080095230264854 Validation score: 0.4147140046119352

As we can see, the final model has higher R2 score compared to the baseline model. The features we will consider in our model and their coefficients are:

```
[113]: coeffs=final[3][["feature", "P-value", "coefficient"]].reset_index(drop = True) coeffs
```

```
[113]:
                     feature P-value coefficient
                                        -0.0208
      0
                   bedrooms
                                  0
      1
                     floors
                                  0
                                          0.054
      2
                     5 Fair
                                        -0.1196
                                  0
      3
                  7 Average
                                  0
                                         0.1789
      4
                      4 Low 0.002
                                        -0.2152
      5
                     8 Good
                                  0
                                         0.3805
      6
                sqft_living
                                  0
                                         0.4858
      7
          waterfront_impute
                                  0
                                         0.5539
                   9 Better
      8
                                  0
                                         0.5932
      9
               10 Very Good
                                  0
                                         0.7328
               11 Excellent
                                  0
      10
                                         0.861
                  12 Luxury
                                  0
                                         1.0057
      11
      12
                                  0
                   yr_built
                                        -7.6526
      13
                                  0
                                         62.5153
                        lat
                                  0
                                       -174.335
      14
                       const
```

8.3 Interpretation

In order to interpret the model, we know that there are two types of features in the model. One of these features is numerical features and the others are categorical variables. It is easy to interpret the numerical features. For example, consider sqft_living which has the coefficient

feature

P-value

coefficient

6

sqft living

0

0.4858

this coefficient is positive meaning that by increasing sqft_living the price of the property goes up. On the other hand, we calculate the logarithm of both price and this variable. Therefore, if we ignore all other variables and we just consider price and sqft_living we have

$$\ln(p) = c_l \ln(l) \tag{1}$$

in which, p and l denote price and sqft_living, respectively and c_l is the coefficient of sqft_living in our model which is equal to 0.4858.

Now if sqft_living is increased from l_0 to $l_1 = 2.72 \times l_0$, the price will change from p_0 to p_1 as:

$$\begin{split} \ln(p_1) &= c_l \ln(2.72 \times l_0) \\ &= c_l + c_l \ln(l_0) \\ &= c_l + \ln(p_0) \end{split}$$

as a result

$$\ln(\frac{p_1}{p_0}) = c_l \Longrightarrow p_1 = p_0 e^{c_l} \tag{2}$$

in which \$e = \$ 2.718281828459045 is called Neper number. Therefore, if we increase sqft_living from one value l_0 to $l_1 = 2.72 \times l_0$, the price will change from p_0 to 1.6254748687259315 $\times p_0$.

Interpreting the coefficient of categorical variables is more complicated than the numerical variables. In order to interpret these coefficients, first we need to choose a base coefficient to compare all other categorical coefficients with. In order to do so, we are going to first create another dataframe in which we only have categorical features and their coefficients.

```
to_drop_index.append(ind)
cat_coeff = coeffs.drop(index = to_drop_index, axis = 0)
cat_coeff
```

```
[137]:
                       feature P-value coefficient
                        5 Fair
                                      0
                                             -0.1196
       2
       3
                    7 Average
                                      0
                                              0.1789
       4
                         4 Low
                                  0.002
                                             -0.2152
                        8 Good
       5
                                      0
                                              0.3805
       7
           waterfront_impute
                                      0
                                              0.5539
       8
                     9 Better
                                      0
                                              0.5932
                 10 Very Good
       9
                                      0
                                              0.7328
       10
                 11 Excellent
                                      0
                                               0.861
                                      0
       11
                    12 Luxury
                                              1.0057
```

Let's pick 7 Average as the base coefficient and then we divide all other coefficients with the coefficient of 7 Average

[146]:		feature	P-value	coefficient	divided by	7 Average
	2	5 Fair	0	-0.1196		-0.66853
	3	7 Average	0	0.1789		1
	4	4 Low	0.002	-0.2152		-1.20291
	5	8 Good	0	0.3805		2.12689
	7	waterfront_impute	0	0.5539		3.09614
	8	9 Better	0	0.5932		3.31582
	9	10 Very Good	0	0.7328		4.09614
	10	11 Excellent	0	0.861		4.81274
	11	12 Luxury	0	1.0057		5.62158

From this dataframe we can realize that 5 Fair and 4 Low as negative effect on the price of the property since they have negative coefficients. In addition to that, we realize that if we improve/change the grade from 7 Average to 12 Luxury we should expect high change in the logarithm of the price since the coefficient of 12 Luxury is 5.62157629960872 times of that of 7 Average.

9 Prediction (almost DONE)

We want to use the model we presented in the previous sections to predict the price of properties with the data saved in X_test and then we want to compare the real values with the predicted ones. In order to do so, we do the following:

```
[151]: from sklearn.model_selection import train_test_split
       from sklearn.linear_model import LinearRegression
       from sklearn.metrics import mean_squared_error
       ## Test-Train Split
       df final = final dataframe()
       X = df_final.drop(columns = "price", axis = 1)
       y = df final["price"]
       X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42)
       ## Fitting to the Model
       final_model = LinearRegression()
       final_model.fit(X_train, y_train)
       final_model.score(X_test, y_test)
       prediction = final_model.predict(X_test)
       ## Calculating Mean Squared Error
       MSE = mean_squared_error(np.exp(y_test),
                          np.exp(final_model.predict(X_test)),
                          squared = False)
       MSE
```

[151]: 143922.6971401071

10 Assumption Checking

In order to be able to use regression model, we need to check if the following assumptions are satisfied.

- 1. Normality of Residuals
- 2. Multicollinearity (Independence Assumption)
- 3. Homoscedasticity
- 4. Linearity

In the following subsections, we will check each of these assumptions.

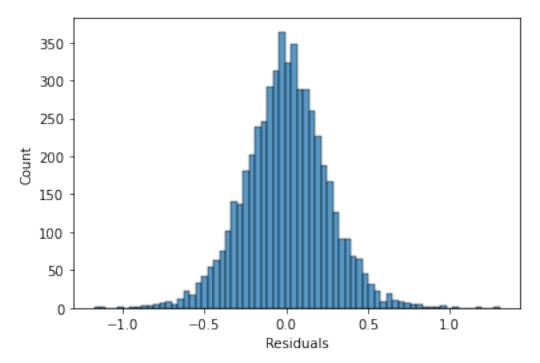
10.1 Normality of Residuals

We will check if the residuals are normal buy visually checking histogram and QQ-Plot of the residuals.

```
[159]: import scipy.stats as stats

residuals = (y_test - prediction)
sns.histplot(residuals)
```

```
plt.xlabel('Residuals');
# sm.graphics.qqplot(residuals, dist=stats.norm, line='45', fit=True);
```



It seems that the histogram of residuals follows the normal distribution so, we might accept that the residuals are normally distributed.

10.2 Investigating Multicollinearity (Independence Assumption)

In order to check if the features are independent or not, we will check the variance_inflation_factor and see if the values of each coefficient is below 5 or not. If the values are below 5, we may accept that the features are independent.

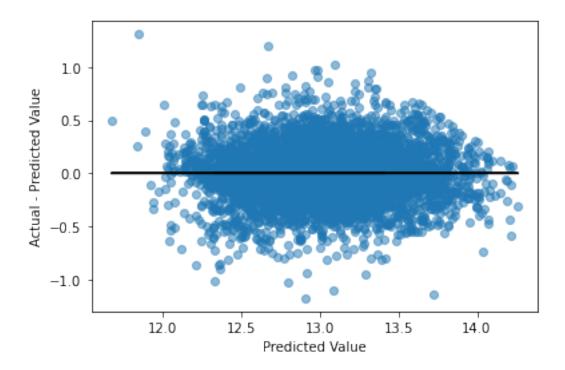
```
[160]: const
                             2.759625e+06
       bedrooms
                             1.680581e+00
       sqft_living
                             3.069384e+00
       floors
                             1.495836e+00
       yr built
                             1.619488e+00
       lat
                             1.090620e+00
       waterfront_impute
                             1.010457e+00
       10 Very Good
                             2.374400e+00
       11 Excellent
                             1.520302e+00
       12 Luxury
                             1.058862e+00
       4 Low
                             1.010572e+00
       5 Fair
                             1.103537e+00
                             3.757455e+00
       7 Average
       8 Good
                             4.474132e+00
       9 Better
                             3.622918e+00
       Name: Variance Inflation Factor, dtype: float64
```

We can see that all the values are below 5 so we may conclude that the features are independent from one another and we do not have collinearity in our model.

10.3 Investigating Homoscedasticity

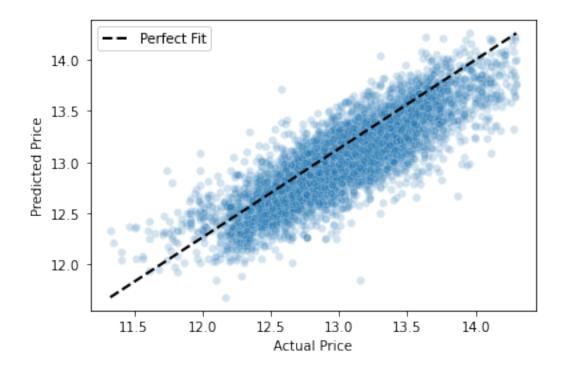
```
[127]: fig, ax = plt.subplots()

ax.scatter(prediction, residuals, alpha=0.5)
ax.plot(prediction, [0 for i in range(len(X_test))], color = "black")
ax.set_xlabel("Predicted Value")
ax.set_ylabel("Actual - Predicted Value");
```



10.4 Investigating Linearity

- 11.326595886778735 14.297936707208567
- 11.67919343736753 14.259572840391826



11 Model's Shortcomings

12 Business Suggestion