# GCLC Prover Output for conjecture "konstrukcija-trougla"

Groebner bases method used
April 28, 2022

## 1 Construction and prover internal state

#### **Construction commands:**

- Point O
- Point  $M_b$
- Point  $M_c$
- Line  $m_b$ :  $O M_b$
- Line  $m_c$ :  $O\ M_c$
- Perpendicular, b:  $M_b m_b$
- Perpendicular, c:  $M_c$   $m_c$
- Intersection of lines, A: c b
- $\bullet$  Towards C A A  $M_b$  2
- Towards  $B\ M_c\ M_c\ A\ -1$
- Line c': A B
- Line b': A C
- Midpoint,  $M_b'$ : A C
- Midpoint,  $M'_c$ : A B
- $\bullet$  Perpendicular,  $m_c' \colon M_c' \ c$
- Perpendicular,  $m_b'$ :  $M_b'$  b
- Intersection of lines, O':  $m'_b \ m'_c$

#### Coordinates assigned to the points:

- O = (0,0)
- $M_b = (u_1, 0)$
- $\bullet \ M_c = (u_2, u_3)$
- $A = (u_1, x_1)$
- $C = (u_1, x_3)$
- $B = (x_6, x_5)$
- $M_b' = (u_1, x_7)$
- $M'_c = (x_{10}, x_9)$
- $O' = (x_{12}, x_7)$

#### Conjecture(s):

- 1. Given conjecture
  - GCLC code:

identical 0 0'

• Expression:

 $P_{OO'O} = 0$ 

## 2 Resolving constructed lines

- $m_b \ni O, M_b$ ; line is horizontal (i.e.,  $y(O) = y(M_b)$ )
- $m_c \ni O, M_c$
- $b \ni M_b, A, C, M_b'$ ; line is vertical (i.e.,  $x(M_b) = x(A)$ )
- $c \ni M_c, A, B, M'_c$
- $c' \ni A, B$
- $b' \ni A, C$
- $m'_c \ni M'_c, O'$
- $m_b' \ni M_b', O'$ ; line is horizontal (i.e.,  $y(M_b') = y(O')$ )

## 3 Creating polynomials from hypotheses

- Point O no condition
- Point  $M_b$  no condition
- Point  $M_c$  no condition
- Line  $m_b$ :  $O M_b$ 
  - point O is on the line  $(O, M_b)$  no condition
  - point  $M_b$  is on the line  $(O, M_b)$  no condition
- Line  $m_c$ :  $O M_c$ 
  - point O is on the line  $(O, M_c)$ no condition
  - point  $M_c$  is on the line  $(O, M_c)$ no condition
- Perpendicular, b:  $M_b m_b$ 
  - Line  $(M_b, A)$  perpendicular with line  $(O, M_b)$ - true by the construction
- Perpendicular, c:  $M_c$   $m_c$ 
  - Line  $(M_c, A)$  perpendicular with line  $(O, M_c)$

$$p_1 = u_3 x_1 + \left(-u_3^2 - u_2^2 + u_2 u_1\right)$$

- Intersection of lines, A: c b
  - point A is on the line  $(M_c, A)$ no condition
  - point A is on the line  $(M_b, A)$ no condition
- Towards  $C A A M_b 2$ 
  - Line (A, C) parallel with line  $(A, M_b)$ - true by the construction
  - Ratio of projections of the segments (A, C) and  $(A, M_b)$  on axis y equal to 2.000

$$p_2 = -x_3 - x_1$$

- Towards  $B M_c M_c A -1$ 
  - Line  $(M_c, B)$  parallel with line  $(M_c, A)$

$$p_3 = x_6x_1 - u_3x_6 + (u_2 - u_1)x_5 - u_2x_1 + u_3u_1$$

– Ratio of projections of the segments  $(M_c, B)$  and  $(M_c, A)$  on axis x equal to -1.000

$$p_4 = -x_6 + (2u_2 - u_1)$$

- Line c': A B
  - point A is on the line (A, B) no condition
  - point B is on the line (A, B) no condition
- Line b': A C
  - point A is on the line (A, C) no condition
  - point C is on the line (A, C) no condition
- Midpoint,  $M'_b$ : A C
  - point  $M'_b$  is on the line (A, C) true by the construction no condition
  - Segment  $[M'_b, A]$  equal size as segment  $[M'_b, C]$

$$p_5 = 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2$$

- Midpoint,  $M'_c$ : A B
  - point  $M'_c$  is on the line (A, B)

$$p_6 = -x_{10}x_5 + x_{10}x_1 + x_9x_6 - u_1x_9 - x_6x_1 + u_1x_5$$

– Segment  $[M_c',\,A]$  equal size as segment  $[M_c',\,B]$ 

$$p_7 = 2x_{10}x_6 - 2u_1x_{10} + 2x_9x_5 - 2x_9x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2$$

- Perpendicular,  $m'_c$ :  $M'_c$  c
  - Line  $(M'_c, O')$  perpendicular with line  $(M_c, A)$

$$p_8 = (-u_2 + u_1)x_{12} + (u_2 - u_1)x_{10} - x_9x_1 + u_3x_9 + x_7x_1 - u_3x_7$$

• Perpendicular,  $m_b'$ :  $M_b'$  b

- Line  $(M'_b, O')$  perpendicular with line  $(M_b, A)$ — true by the construction
- Intersection of lines, O':  $m'_b m'_c$ 
  - point O' is on the line  $(M'_b, O')$ no condition
  - point O' is on the line  $(M'_c, O')$ no condition

## 4 Creating polynomial from the conjecture

• Processing given conjecture(s).

#### Conjecture 1:

$$p_9 = 2x_{12}^2 + 2x_7^2$$

## 5 Invoking the theorem prover

The used proving method is Buchberger's method. Input polynomial system is:

$$\begin{array}{rcl} p_0 & = & u_3x_1 + \left(-u_3^2 - u_2^2 + u_2u_1\right) \\ p_1 & = & -x_3 - x_1 \\ p_2 & = & x_6x_1 - u_3x_6 + \left(u_2 - u_1\right)x_5 - u_2x_1 + u_3u_1 \\ p_3 & = & -x_6 + \left(2u_2 - u_1\right) \\ p_4 & = & 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2 \\ p_5 & = & -x_{10}x_5 + x_{10}x_1 + x_9x_6 - u_1x_9 - x_6x_1 + u_1x_5 \\ p_6 & = & 2x_{10}x_6 - 2u_1x_{10} + 2x_9x_5 - 2x_9x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2 \\ p_7 & = & \left(-u_2 + u_1\right)x_{12} + \left(u_2 - u_1\right)x_{10} - x_9x_1 + u_3x_9 + x_7x_1 - u_3x_7 \\ \end{array}$$

#### 5.1 Iteration 1

Current set is  $S_1 =$ 

$$\begin{array}{rcl} p_0 & = & u_3x_1 + \left(-u_3^2 - u_2^2 + u_2u_1\right) \\ p_1 & = & -x_3 - x_1 \\ p_2 & = & x_6x_1 - u_3x_6 + \left(u_2 - u_1\right)x_5 - u_2x_1 + u_3u_1 \\ p_3 & = & -x_6 + \left(2u_2 - u_1\right) \\ p_4 & = & 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2 \\ p_5 & = & -x_{10}x_5 + x_{10}x_1 + x_9x_6 - u_1x_9 - x_6x_1 + u_1x_5 \\ p_6 & = & 2x_{10}x_6 - 2u_1x_{10} + 2x_9x_5 - 2x_9x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2 \\ p_7 & = & \left(-u_2 + u_1\right)x_{12} + \left(u_2 - u_1\right)x_{10} - x_9x_1 + u_3x_9 + x_7x_1 - u_3x_7 \end{array}$$

- 1. Creating S-polynomial from the pair  $(p_0, p_1)$ . Skipping pair  $p_0$  and  $p_1$  because gcd of their leading monoms is zero.
- 2. Creating S-polynomial from the pair  $(p_0, p_2)$ .

Forming S-pol of  $p_0$  and  $p_2$ :

$$p_{26} = (-u_2^2 + u_2 u_1)x_6 + (-u_3 u_2 + u_3 u_1)x_5 + u_3 u_2 x_1 - u_3^2 u_1$$

S-pol added.

- 3. Creating S-polynomial from the pair  $(p_0, p_3)$ . Skipping pair  $p_0$  and  $p_3$  because gcd of their leading monoms is zero.
- 4. Creating S-polynomial from the pair  $(p_0, p_4)$ . Skipping pair  $p_0$  and  $p_4$  because gcd of their leading monoms is zero.
- 5. Creating S-polynomial from the pair  $(p_0, p_5)$ . Skipping pair  $p_0$  and  $p_5$  because gcd of their leading monoms is zero.
- 6. Creating S-polynomial from the pair  $(p_0, p_6)$ . Skipping pair  $p_0$  and  $p_6$  because gcd of their leading monoms is zero.
- 7. Creating S-polynomial from the pair  $(p_0, p_7)$ . Skipping pair  $p_0$  and  $p_7$  because gcd of their leading monoms is zero.
- 8. Creating S-polynomial from the pair  $(p_1, p_2)$ . Skipping pair  $p_1$  and  $p_2$  because gcd of their leading monoms is zero.
- 9. Creating S-polynomial from the pair  $(p_1, p_3)$ . Skipping pair  $p_1$  and  $p_3$  because gcd of their leading monoms is zero.
- 10. Creating S-polynomial from the pair  $(p_1, p_4)$ . Forming S-pol of  $p_1$  and  $p_4$ :

$$p_{27} = -4x_7x_1 - x_3^2 + x_1^2$$

S-pol added.

- 11. Creating S-polynomial from the pair  $(p_1, p_5)$ . Skipping pair  $p_1$  and  $p_5$  because gcd of their leading monoms is zero.
- 12. Creating S-polynomial from the pair  $(p_1, p_6)$ . Skipping pair  $p_1$  and  $p_6$  because gcd of their leading monoms is zero.
- 13. Creating S-polynomial from the pair  $(p_1, p_7)$ . Skipping pair  $p_1$  and  $p_7$  because gcd of their leading monoms is zero.
- 14. Creating S-polynomial from the pair  $(p_2, p_3)$ .

Forming S-pol of  $p_2$  and  $p_3$ :

$$p_{28} = u_3x_6 + (-u_2 + u_1)x_5 + (-u_2 + u_1)x_1 - u_3u_1$$

S-pol added.

- 15. Creating S-polynomial from the pair  $(p_2, p_4)$ . Skipping pair  $p_2$  and  $p_4$  because gcd of their leading monoms is zero.
- 16. Creating S-polynomial from the pair  $(p_2, p_5)$ . Skipping pair  $p_2$  and  $p_5$  because gcd of their leading monoms is zero.
- 17. Creating S-polynomial from the pair  $(p_2, p_6)$ . Forming S-pol of  $p_2$  and  $p_6$ :

$$p_{29} = -2u_3x_{10}x_6 + (2u_2 - 2u_1)x_{10}x_5 +$$

$$(-2u_2 + 2u_1)x_{10}x_1 + 2u_3u_1x_{10} - 2x_9x_5x_1 + 2x_9x_1^2 + x_6^2x_1 + x_5^2x_1 -$$

$$x_1^3 - u_1^2x_1$$

S-pol added.

- 18. Creating S-polynomial from the pair  $(p_2, p_7)$ . Skipping pair  $p_2$  and  $p_7$  because gcd of their leading monoms is zero.
- 19. Creating S-polynomial from the pair  $(p_3, p_4)$ . Skipping pair  $p_3$  and  $p_4$  because gcd of their leading monoms is zero.
- 20. Creating S-polynomial from the pair  $(p_3, p_5)$ . Skipping pair  $p_3$  and  $p_5$  because gcd of their leading monoms is zero.
- 21. Creating S-polynomial from the pair  $(p_3, p_6)$ . Forming S-pol of  $p_3$  and  $p_6$ :

$$p_{30} = (4u_2 - 4u_1)x_{10} + 2x_9x_5 - 2x_9x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2$$

S-pol added.

- 22. Creating S-polynomial from the pair  $(p_3, p_7)$ . Skipping pair  $p_3$  and  $p_7$  because gcd of their leading monoms is zero.
- 23. Creating S-polynomial from the pair  $(p_4, p_5)$ . Skipping pair  $p_4$  and  $p_5$  because gcd of their leading monoms is zero.
- 24. Creating S-polynomial from the pair  $(p_4, p_6)$ . Skipping pair  $p_4$  and  $p_6$  because gcd of their leading monoms is zero.
- 25. Creating S-polynomial from the pair  $(p_4, p_7)$ . Skipping pair  $p_4$  and  $p_7$  because gcd of their leading monoms is zero.
- 26. Creating S-polynomial from the pair  $(p_5, p_6)$ . Forming S-pol of  $p_5$  and  $p_6$ :

$$p_{31} = 2x_{10}x_6x_1 - 2u_1x_{10}x_5 + 2x_9x_6^2 - 2u_1x_9x_6 + 2x_9x_5^2 - 2x_9x_5x_1 - x_6^2x_5 - 2x_6^2x_1 + 2u_1x_6x_5 - x_5^3 + x_5x_1^2 + u_1^2x_5$$

S-pol added.

- 27. Creating S-polynomial from the pair  $(p_5, p_7)$ . Skipping pair  $p_5$  and  $p_7$  because gcd of their leading monoms is zero.
- 28. Creating S-polynomial from the pair  $(p_6, p_7)$ . Skipping pair  $p_6$  and  $p_7$  because gcd of their leading monoms is zero.

#### 5.2 Iteration 2

Current set is  $S_2 =$ 

$$\begin{array}{lll} p_0 &=& u_3x_1 + (-u_3^2 - u_2^2 + u_2u_1) \\ p_1 &=& -x_3 - x_1 \\ p_2 &=& x_6x_1 - u_3x_6 + (u_2 - u_1)x_5 - u_2x_1 + u_3u_1 \\ p_3 &=& -x_6 + (2u_2 - u_1) \\ p_4 &=& 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2 \\ p_5 &=& -x_{10}x_5 + x_{10}x_1 + x_{9}x_6 - u_1x_9 - x_6x_1 + u_1x_5 \\ p_6 &=& 2x_{10}x_6 - 2u_1x_{10} + 2x_{9}x_5 - 2x_{9}x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2 \\ p_7 &=& (-u_2 + u_1)x_{12} + (u_2 - u_1)x_{10} - x_{9}x_1 + u_3x_9 + x_{7}x_1 - u_3x_7 \\ p_8 &=& (u_3^2u_2 - u_3^2u_1)x_5 + \\ & (-u_3^3u_2 + u_3^3u_1 + u_3u_2^3 - 2u_3u_2^2u_1 + u_3u_2u_1^2) \\ p_9 &=& (-4u_3^4 - 4u_3^2u_2^2 + 4u_3^2u_2u_1)x_7 \\ p_{10} &=& (u_3u_2 - u_3u_1)x_5 + (-u_3^2u_2 + u_3^2u_1 + u_2^3 - 2u_2^2u_1 + u_2u_1^2) \\ p_{11} &=& (4u_3^{10}u_2 - 4u_3^{10}u_1)x_{10} + (2u_3^{10} + 2u_3^8u_2^2 - 2u_3^8u_2u_1)x_{9}x_5 + \\ & (-2u_3^{11} - 8u_3^9u_2^2 + 12u_3^9u_2u_1 - 4u_3^9u_1^2 - 2u_3^7u_2^4 + 4u_3^7u_2^3u_1 - \\ & 2u_3^7u_2^2u_1^2)x_9 + (-u_3^{10} - u_3^8u_2^2 + u_3^8u_2u_1)x_5^2 + \\ & (-2u_3^9u_2u_1 + 2u_3^9u_1^2)x_5 + \\ & (u_1^2 + 3u_3^{10}u_2^2 - 5u_3^{10}u_2u_1 + 2u_3^{10}u_1^2 + 3u_3^8u_2^4 - 8u_3^8u_2^3u_1 + \\ & x_3u_2^2u_1^2 - 2u_3^8u_2u_1^3 + u_3^6u_2^6 - 3u_3^6u_2^5u_1 + \\ & 3u_3^6u_2^4u_1^2 - u_3^6u_2^3u_1^3) \\ p_{12} &=& (4u_3^3u_2 - 4u_3^3u_1)x_{10} + 2u_3^3x_9x_5 + \\ & (-2u_3^4 - 2u_3^2u_2^2 + 2u_3^3u_2u_1 + u_3u_2^4 - 2u_3u_2^2u_1 + u_3u_2^2u_1^2) \\ p_{13} &=& (\\ & 4u_3^8u_2 - 4u_3^8u_1 + 4u_3^6u_2^3 - 8u_3^6u_2^2u_1 + 4u_3^6u_2u_1^2)x_{10} + \\ & 2u_3^7x_9x_5^2 + (-2u_3^8 - 2u_3^6u_2^2 + 2u_3^6u_2u_1)x_9x_5 + \\ & (8u_3^7u_2^2 - 16u_3^7u_2u_1 + 8u_3^7u_1^2)x_9 - u_3^7x_5^3 + \\ & (u_9^3 - 2u_3^7u_2^2 + 6u_3^7u_2u_1 - 4u_3^7u_1^2 + u_3^5u_2^4 - 2u_3^5u_2^3u_1 + \\ & u_3^5u_2^2u_1^2)x_5 + \\ & (-8u_3^8u_2^2 + 12u_3^8u_2u_1 - 4u_3^8u_1^2 - 8u_3^6u_2^4 + 20u_3^6u_2^3u_1 - \\ & 16u_3^9u_2^2u_1^2 + 4u_3^6u_2u_1^3) \end{array}$$

1. Creating S-polynomial from the pair  $(p_0, p_8)$ .

- Skipping pair  $p_0$  and  $p_8$  because gcd of their leading monoms is zero.
- 2. Creating S-polynomial from the pair  $(p_0, p_9)$ . Skipping pair  $p_0$  and  $p_9$  because gcd of their leading monoms is zero.
- 3. Creating S-polynomial from the pair  $(p_0, p_{10})$ . Skipping pair  $p_0$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 4. Creating S-polynomial from the pair  $(p_0, p_{11})$ . Skipping pair  $p_0$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 5. Creating S-polynomial from the pair  $(p_0, p_{12})$ . Skipping pair  $p_0$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 6. Creating S-polynomial from the pair  $(p_0, p_{13})$ . Skipping pair  $p_0$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 7. Creating S-polynomial from the pair  $(p_1, p_8)$ . Skipping pair  $p_1$  and  $p_8$  because gcd of their leading monoms is zero.
- 8. Creating S-polynomial from the pair  $(p_1, p_9)$ . Skipping pair  $p_1$  and  $p_9$  because gcd of their leading monoms is zero.
- 9. Creating S-polynomial from the pair  $(p_1, p_{10})$ . Skipping pair  $p_1$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 10. Creating S-polynomial from the pair  $(p_1, p_{11})$ . Skipping pair  $p_1$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 11. Creating S-polynomial from the pair  $(p_1, p_{12})$ . Skipping pair  $p_1$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 12. Creating S-polynomial from the pair  $(p_1, p_{13})$ . Skipping pair  $p_1$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 13. Creating S-polynomial from the pair  $(p_2, p_8)$ . Skipping pair  $p_2$  and  $p_8$  because gcd of their leading monoms is zero.
- 14. Creating S-polynomial from the pair  $(p_2, p_9)$ . Skipping pair  $p_2$  and  $p_9$  because gcd of their leading monoms is zero.
- 15. Creating S-polynomial from the pair  $(p_2, p_{10})$ . Skipping pair  $p_2$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 16. Creating S-polynomial from the pair  $(p_2, p_{11})$ . Skipping pair  $p_2$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 17. Creating S-polynomial from the pair  $(p_2, p_{12})$ . Skipping pair  $p_2$  and  $p_{12}$  because gcd of their leading monoms is zero.

- 18. Creating S-polynomial from the pair  $(p_2, p_{13})$ . Skipping pair  $p_2$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 19. Creating S-polynomial from the pair  $(p_3, p_8)$ . Skipping pair  $p_3$  and  $p_8$  because gcd of their leading monoms is zero.
- 20. Creating S-polynomial from the pair  $(p_3, p_9)$ . Skipping pair  $p_3$  and  $p_9$  because gcd of their leading monoms is zero.
- 21. Creating S-polynomial from the pair  $(p_3, p_{10})$ . Skipping pair  $p_3$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 22. Creating S-polynomial from the pair  $(p_3, p_{11})$ . Skipping pair  $p_3$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 23. Creating S-polynomial from the pair  $(p_3, p_{12})$ . Skipping pair  $p_3$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 24. Creating S-polynomial from the pair  $(p_3, p_{13})$ . Skipping pair  $p_3$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 25. Creating S-polynomial from the pair  $(p_4, p_8)$ . Skipping pair  $p_4$  and  $p_8$  because gcd of their leading monoms is zero.
- 26. Creating S-polynomial from the pair  $(p_4, p_9)$ . Forming S-pol of  $p_4$  and  $p_9$ :

$$p_{46} = (8u_3^4 + 8u_3^2u_2^2 - 8u_3^2u_2u_1)x_7x_1 +$$

$$(4u_3^4 + 4u_3^2u_2^2 - 4u_3^2u_2u_1)x_3^2 +$$

$$(-4u_3^4 - 4u_3^2u_2^2 + 4u_3^2u_2u_1)x_1^2$$

- 27. Creating S-polynomial from the pair  $(p_4, p_{10})$ . Skipping pair  $p_4$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 28. Creating S-polynomial from the pair  $(p_4, p_{11})$ . Skipping pair  $p_4$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 29. Creating S-polynomial from the pair  $(p_4, p_{12})$ . Skipping pair  $p_4$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 30. Creating S-polynomial from the pair  $(p_4, p_{13})$ . Skipping pair  $p_4$  and  $p_{13}$  because gcd of their leading monoms is zero.

31. Creating S-polynomial from the pair  $(p_5, p_8)$ . Forming S-pol of  $p_5$  and  $p_8$ :

$$p_{47} = (u_3^2 u_2 - u_3^2 u_1)x_{10}x_1 +$$

$$(-u_3^3 u_2 + u_3^3 u_1 + u_3 u_2^3 - 2u_3 u_2^2 u_1 + u_3 u_2 u_1^2)x_{10} +$$

$$(u_3^2 u_2 - u_3^2 u_1)x_9 x_6 + (-u_3^2 u_2 u_1 + u_3^2 u_1^2)x_9 +$$

$$(-u_3^2 u_2 + u_3^2 u_1)x_6 x_1 + (u_3^2 u_2 u_1 - u_3^2 u_1^2)x_5$$

S-pol added.

- 32. Creating S-polynomial from the pair  $(p_5, p_9)$ . Skipping pair  $p_5$  and  $p_9$  because gcd of their leading monoms is zero.
- 33. Creating S-polynomial from the pair  $(p_5, p_{10})$ . Forming S-pol of  $p_5$  and  $p_{10}$ :

$$p_{48} = (u_3u_2 - u_3u_1)x_{10}x_1 + (-u_3^2u_2 + u_3^2u_1 + u_2^3 - 2u_2^2u_1 + u_2u_1^2)x_{10} +$$

$$(u_3u_2 - u_3u_1)x_9x_6 + (-u_3u_2u_1 + u_3u_1^2)x_9 + (-u_3u_2 + u_3u_1)x_6x_1 +$$

$$(u_3u_2u_1 - u_3u_1^2)x_5$$

S-pol added.

34. Creating S-polynomial from the pair  $(p_5, p_{11})$ . Forming S-pol of  $p_5$  and  $p_{11}$ :

$$\begin{split} p_{49} &= (4u_3^{10}u_2 - 4u_3^{10}u_1)x_{10}x_1 + (4u_3^{10}u_2 - 4u_3^{10}u_1)x_9x_6 + \\ &\qquad (2u_3^{10} + 2u_3^8u_2^2 - 2u_3^8u_2u_1)x_9x_5^2 + \\ &(-2u_3^{11} - 8u_3^9u_2^2 + 12u_3^9u_2u_1 - 4u_3^9u_1^2 - 2u_3^7u_2^4 + 4u_3^7u_2^3u_1 - \\ &\qquad 2u_3^7u_2^2u_1^2)x_9x_5 + (-4u_3^{10}u_2u_1 + 4u_3^{10}u_1^2)x_9 + \\ &(-4u_3^{10}u_2 + 4u_3^{10}u_1)x_6x_1 + (-u_3^{10} - u_3^8u_2^2 + u_3^8u_2u_1)x_5^3 + \\ &\qquad (-2u_3^9u_2u_1 + 2u_3^9u_1^2)x_5^2 + \\ &(u_3^{12} + 3u_3^{10}u_2^2 - u_3^{10}u_2u_1 - 2u_3^{10}u_1^2 + 3u_3^8u_2^4 - 8u_3^8u_2^3u_1 + \\ &\qquad 7u_3^8u_2^2u_1^2 - 2u_3^8u_2u_1^3 + u_2^6u_0^6 - 3u_3^6u_2^5u_1 + \end{split}$$

 $3u_3^6u_2^4u_1^2 - u_3^6u_2^3u_1^3)x_5$ 

S-pol added.

35. Creating S-polynomial from the pair  $(p_5, p_{12})$ . Forming S-pol of  $p_5$  and  $p_{12}$ :

$$\begin{split} p_{50} &= (4u_3^3u_2 - 4u_3^3u_1)x_{10}x_1 + (4u_3^3u_2 - 4u_3^3u_1)x_9x_6 + 2u_3^3x_9x_5^2 + \\ & (-2u_3^4 - 2u_3^2u_2^2 + 2u_3^2u_2u_1)x_9x_5 + (-4u_3^3u_2u_1 + 4u_3^3u_1^2)x_9 + \\ & (-4u_3^3u_2 + 4u_3^3u_1)x_6x_1 - u_3^3x_5^3 + \\ & (u_3^5 - 2u_3^3u_2^2 + 6u_3^3u_2u_1 - 4u_3^3u_1^2 + u_3u_2^4 - 2u_3u_2^3u_1 + \\ & u_3u_2^2u_1^2)x_5 \end{split}$$

S-pol added.

36. Creating S-polynomial from the pair  $(p_5, p_{13})$ . Forming S-pol of  $p_5$  and  $p_{13}$ :

$$\begin{split} p_{51} &= (4u_3^8u_2 - 4u_3^8u_1 + 4u_3^6u_2^3 - 8u_3^6u_2^2u_1 + 4u_3^6u_2u_1^2)x_{10}x_1 + \\ & (4u_3^8u_2 - 4u_3^8u_1 + 4u_3^6u_2^3 - 8u_3^6u_2^2u_1 + 4u_3^6u_2u_1^2)x_9x_6 + \\ & 2u_3^7x_9x_5^3 + (-2u_3^8 - 2u_3^6u_2^2 + 2u_3^6u_2u_1)x_9x_5^2 + \\ & (8u_3^7u_2^2 - 16u_3^7u_2u_1 + 8u_3^7u_1^2)x_9x_5 + \\ & (-4u_3^8u_2u_1 + 4u_3^8u_1^2 - 4u_3^6u_2^3u_1 + 8u_3^6u_2^2u_1^2 - \\ & 4u_3^6u_2u_1^3)x_9 + \\ & (-4u_3^8u_2 + 4u_3^8u_1 - 4u_3^6u_2^3 + 8u_3^6u_2^2u_1 - 4u_3^6u_2u_1^2)x_6x_1 - \\ & u_3^7x_5^4 + \\ & (u_3^9 - 2u_3^7u_2^2 + 6u_3^7u_2u_1 - 4u_3^7u_1^2 + u_3^5u_2^4 - 2u_3^5u_2^3u_1 + \\ & u_3^5u_2^2u_1^2)x_5^2 + \\ & (-8u_3^8u_2^2 + 16u_3^8u_2u_1 - 8u_3^8u_1^2 - 8u_3^6u_2^4 + 24u_3^6u_2^3u_1 - \\ & 24u_3^6u_2^2u_1^2 + 8u_3^6u_2u_1^3)x_5 \end{split}$$

S-pol added.

- 37. Creating S-polynomial from the pair  $(p_6, p_8)$ . Skipping pair  $p_6$  and  $p_8$  because gcd of their leading monoms is zero.
- 38. Creating S-polynomial from the pair  $(p_6, p_9)$ . Skipping pair  $p_6$  and  $p_9$  because gcd of their leading monoms is zero.
- 39. Creating S-polynomial from the pair  $(p_6, p_{10})$ . Skipping pair  $p_6$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 40. Creating S-polynomial from the pair  $(p_6, p_{11})$ . Forming S-pol of  $p_6$  and  $p_{11}$ :

$$\begin{split} p_{52} &= (-8u_3^{10}u_2u_1 + 8u_3^{10}u_1^2)x_{10} + \\ & (-4u_3^{10} - 4u_3^8u_2^2 + 4u_3^8u_2u_1)x_9x_6x_5 + \\ & (4u_3^{11} + 16u_3^9u_2^2 - 24u_3^9u_2u_1 + 8u_3^9u_1^2 + 4u_3^7u_2^4 - 8u_3^7u_2^3u_1 + \\ & 4u_3^7u_2^2u_1^2)x_9x_6 + (8u_3^{10}u_2 - 8u_3^{10}u_1)x_9x_5 + \\ & (-8u_3^{10}u_2 + 8u_3^{10}u_1)x_9x_1 + (-4u_3^{10}u_2 + 4u_3^{10}u_1)x_6^2 + \\ & (2u_3^{10} + 2u_3^8u_2^2 - 2u_3^8u_2u_1)x_6x_5^2 + \\ & (4u_3^9u_2u_1 - 4u_3^9u_1^2)x_6x_5 + \\ & (-2u_3^{12} - 6u_3^{10}u_2^2 + 10u_3^{10}u_2u_1 - 4u_3^{10}u_1^2 - 6u_3^8u_2^4 + \\ & 16u_3^8u_2^3u_1 - 14u_3^8u_2^2u_1^2 + 4u_3^8u_2u_1^3 - 2u_3^6u_2^6 + \\ & 6u_3^6u_2^5u_1 - 6u_3^6u_2^4u_1^2 + 2u_3^6u_2^3u_1^3)x_6 + \\ & (-4u_3^{10}u_2 + 4u_3^{10}u_1)x_5^2 + (4u_3^{10}u_2 - 4u_3^{10}u_1)x_1^2 + \\ & (4u_3^{10}u_2u_1^2 - 4u_3^{10}u_1^3) \end{split}$$

S-pol added.

41. Creating S-polynomial from the pair  $(p_6, p_{12})$ . Forming S-pol of  $p_6$  and  $p_{12}$ :

$$p_{53} = (-8u_3^3u_2u_1 + 8u_3^3u_1^2)x_{10} - 4u_3^3x_9x_6x_5 +$$

$$(4u_3^4 + 4u_3^2u_2^2 - 4u_3^2u_2u_1)x_9x_6 + (8u_3^3u_2 - 8u_3^3u_1)x_9x_5 +$$

$$(-8u_3^3u_2 + 8u_3^3u_1)x_9x_1 + (-4u_3^3u_2 + 4u_3^3u_1)x_6^2 + 2u_3^3x_6x_5^2 +$$

$$(-2u_3^5 + 4u_3^3u_2^2 - 4u_3^3u_2u_1 - 2u_3u_2^4 + 4u_3u_2^3u_1 - 2u_3u_2^2u_1^2)x_6 +$$

$$(-4u_3^3u_2 + 4u_3^3u_1)x_5^2 + (4u_3^3u_2 - 4u_3^3u_1)x_1^2 +$$

$$(4u_3^3u_2u_1^2 - 4u_3^3u_1^3)$$

S-pol added.

42. Creating S-polynomial from the pair  $(p_6, p_{13})$ .

Forming S-pol of  $p_6$  and  $p_{13}$ : Polynomial too big for output (text size is 1364 characters, number of terms is 13)

S-pol added.

- 43. Creating S-polynomial from the pair  $(p_7, p_8)$ . Skipping pair  $p_7$  and  $p_8$  because gcd of their leading monoms is zero.
- 44. Creating S-polynomial from the pair  $(p_7, p_9)$ . Skipping pair  $p_7$  and  $p_9$  because gcd of their leading monoms is zero.
- 45. Creating S-polynomial from the pair  $(p_7, p_{10})$ . Skipping pair  $p_7$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 46. Creating S-polynomial from the pair  $(p_7, p_{11})$ . Skipping pair  $p_7$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 47. Creating S-polynomial from the pair  $(p_7, p_{12})$ . Skipping pair  $p_7$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 48. Creating S-polynomial from the pair  $(p_7, p_{13})$ . Skipping pair  $p_7$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 49. Creating S-polynomial from the pair  $(p_8, p_9)$ . Skipping pair  $p_8$  and  $p_9$  because gcd of their leading monoms is zero.
- 50. Creating S-polynomial from the pair  $(p_8, p_{10})$ . Forming S-pol of  $p_8$  and  $p_{10}$ :

$$p_{54} = 0$$

Reduced to zero.

51. Creating S-polynomial from the pair  $(p_8, p_{11})$ . Skipping pair  $p_8$  and  $p_{11}$  because gcd of their leading monoms is zero.

- 52. Creating S-polynomial from the pair  $(p_8, p_{12})$ . Skipping pair  $p_8$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 53. Creating S-polynomial from the pair  $(p_8, p_{13})$ . Skipping pair  $p_8$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 54. Creating S-polynomial from the pair  $(p_9, p_{10})$ . Skipping pair  $p_9$  and  $p_{10}$  because gcd of their leading monoms is zero.
- 55. Creating S-polynomial from the pair  $(p_9, p_{11})$ . Skipping pair  $p_9$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 56. Creating S-polynomial from the pair  $(p_9, p_{12})$ . Skipping pair  $p_9$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 57. Creating S-polynomial from the pair  $(p_9, p_{13})$ . Skipping pair  $p_9$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 58. Creating S-polynomial from the pair  $(p_{10}, p_{11})$ . Skipping pair  $p_{10}$  and  $p_{11}$  because gcd of their leading monoms is zero.
- 59. Creating S-polynomial from the pair  $(p_{10}, p_{12})$ . Skipping pair  $p_{10}$  and  $p_{12}$  because gcd of their leading monoms is zero.
- 60. Creating S-polynomial from the pair  $(p_{10}, p_{13})$ . Skipping pair  $p_{10}$  and  $p_{13}$  because gcd of their leading monoms is zero.
- 61. Creating S-polynomial from the pair  $(p_{11}, p_{12})$ . Forming S-pol of  $p_{11}$  and  $p_{12}$ :

$$\begin{split} p_{55} &= (8u_3^{11}u_2^3 - 16u_3^{11}u_2^2u_1 + 8u_3^{11}u_2u_1^2)x_9x_5 + \\ &(-24u_3^{12}u_2^3 + 64u_3^{12}u_2^2u_1 - 56u_3^{12}u_2u_1^2 + 16u_3^{12}u_1^3 - 8u_3^{10}u_2^5 + \\ &24u_3^{10}u_2^4u_1 - 24u_3^{10}u_2^3u_1^2 + 8u_3^{10}u_2^2u_1^3)x_9 + \\ &(-4u_3^{11}u_2^3 + 8u_3^{11}u_2^2u_1 - 4u_3^{11}u_2u_1^2)x_5^2 + \\ &(-8u_3^{12}u_2^2u_1 + 16u_3^{12}u_2u_1^2 - 8u_3^{12}u_1^3)x_5 + \\ &(20u_3^{13}u_2^3 - 48u_3^{13}u_2^2u_1 + 36u_3^{13}u_2u_1^2 - 8u_3^{13}u_1^3 + 8u_3^{11}u_2^5 - \\ &32u_3^{11}u_2^4u_1 + 48u_3^{11}u_2^3u_1^2 - 32u_3^{11}u_2^2u_1^3 + 8u_3^{11}u_2u_1^4 + \\ &4u_3^9u_2^7 - 16u_3^9u_2^6u_1 + 24u_3^9u_2^5u_1^2 - 16u_3^9u_2^4u_1^3 + \\ &4u_3^9u_2^3u_1^4) \end{split}$$

S-pol added.

62. Creating S-polynomial from the pair  $(p_{11}, p_{13})$ .

Forming S-pol of  $p_{11}$  and  $p_{13}$ : Polynomial too big for output (text size is 1874 characters, number of terms is 7)

S-pol added.

63. Creating S-polynomial from the pair  $(p_{12}, p_{13})$ .

Forming S-pol of  $p_{12}$  and  $p_{13}$ : Polynomial too big for output (text size is 1227 characters, number of terms is 7)

S-pol added.

#### 5.3 Iteration 3

Current set is  $S_3 =$ 

$$\begin{array}{lll} p_0 &=& u_3x_1 + (-u_3^2 - u_2^2 + u_2u_1) \\ p_1 &=& -x_3 - x_1 \\ p_2 &=& x_6x_1 - u_3x_6 + (u_2 - u_1)x_5 - u_2x_1 + u_3u_1 \\ p_3 &=& -x_6 + (2u_2 - u_1) \\ p_4 &=& 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2 \\ p_5 &=& -x_{10}x_5 + x_{10}x_1 + x_{9}x_6 - u_1x_9 - x_6x_1 + u_1x_5 \\ p_6 &=& 2x_{10}x_6 - 2u_1x_{10} + 2x_{9}x_5 - 2x_{9}x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2 \\ p_7 &=& (-u_2 + u_1)x_{12} + (u_2 - u_1)x_{10} - x_{9}x_1 + u_3x_9 + x_7x_1 - u_3x_7 \\ p_8 &=& (u_3^2u_2 - u_3^2u_1)x_5 + \\ & & (-u_3^3u_2 + u_3^3u_1 + u_3u_2^3 - 2u_3u_2^2u_1 + u_3u_2u_1^2) \\ p_9 &=& (-4u_4^4 - 4u_3^2u_2^2 + 4u_3^2u_2u_1)x_7 \\ p_{10} &=& (u_3u_2 - u_3u_1)x_5 + (-u_3^2u_2 + u_3^2u_1 + u_2^3 - 2u_3^2u_2u_1 + u_2u_1^2) \\ p_{11} &=& (4u_3^{10}u_2 - 4u_3^{10}u_1)x_{10} + (2u_3^{10} + 2u_3^3u_2^2 - 2u_3^3u_2u_1)x_{9}x_5 + \\ & & (-2u_1^{11} - 8u_3^3u_2^2 + 12u_3^9u_2u_1 - 4u_3^9u_1^2 - 2u_3^7u_2^4 + 4u_3^7u_2^3u_1 - \\ & 2u_3^7u_2^2u_1^2)x_9 + (-u_1^{10} - u_3^8u_2^2 + u_3^8u_2u_1)x_5^2 + \\ & & (-2u_3^9u_2u_1 + 2u_3^9u_1^2)x_5 + \\ & & (u_1^3 + 3u_3^{10}u_2^2 - 5u_3^{10}u_2u_1 + 2u_3^{10}u_1^2 + 3u_3^8u_2^4 - 8u_3^8u_2^3u_1 + \\ & & x_0^8u_2^2u_1^2 - 2u_3^8u_2u_1^3 + u_3^6u_2^6 - 3u_3^6u_2^5u_1 + \\ & & 3u_3^6u_2^4u_1^2 - u_3^6u_2^3u_1^3) \\ p_{12} &=& (4u_3^3u_2 - 4u_3^3u_1)x_{10} + 2u_3^3x_{9}x_5 + \\ & & (-2u_3^4 - 2u_3^3u_2^2 + 2u_3^3u_2u_1 + u_3u_2^4 - 2u_3u_2^3u_1 + u_3u_2^2u_1^2) \\ p_{13} &=& (\\ & 4u_3^8u_2 - 4u_3^8u_1 + 4u_3^6u_2^3 - 8u_3^6u_2^2u_1 + 4u_3^6u_2u_1^2)x_{10} + \\ & 2u_3^7x_9x_5^2 + (-2u_3^8 - 2u_3^6u_2^2 + 2u_3^6u_2u_1)x_{9}x_5 + \\ & (8u_3^8u_2 - 16u_3^7u_2u_1 + 8u_3^7u_1^2 + u_3^5u_2^4 - 2u_3^5u_2^3u_1 + \\ & u_3^5u_2^2u_1^2)x_5 + \\ & (u_3^9 - 2u_3^7u_2^2 + 6u_3^7u_2u_1 - 4u_3^7u_1^2 + u_3^5u_2^4 + 2u_3^5u_2^3u_1 + \\ & u_3^5u_2^2u_1^2)x_5 + \\ & (-8u_3^8u_2^2 + 12u_3^8u_2u_1 - 4u_3^8u_1^2 - 8u_3^6u_2^4 + 20u_3^6u_2^3u_1 - \\ & 16u_3^6u_2^2u_1^2 + 4u_3^6u_2u_1^3) \\ p_{14} &= & \dots \\ p_{15} &= & \dots \end{array}$$

```
p_{18}
p_{19}
                              64u_3^{28}u_2^7 - 448u_3^{28}u_2^6u_1 + 1344u_3^{28}u_2^5u_1^2 - 2240u_3^{28}u_2^4u_1^3 +
                              2240u_3^{28}u_2^3u_1^4 - 1344u_3^{28}u_2^2u_1^5 + 448u_3^{28}u_2u_1^6 - 64u_3^{28}u_1^7 +
                              64u_3^{26}u_2^9 - 448u_3^{26}u_2^8u_1 + 1344u_3^{26}u_2^7u_1^2 - 2240u_3^{26}u_2^6u_1^3 +
                              2240u_3^{26}u_2^5u_1^4 - 1344u_3^{26}u_2^4u_1^5 + 448u_3^{26}u_2^3u_1^6 -
                              64u_3^{26}u_2^2u_1^7)x_9 +
                              (-64u_3^{29}u_2^7 + 448u_3^{29}u_2^6u_1 - 1344u_3^{29}u_2^5u_1^2 + 2240u_3^{29}u_2^4u_1^3 -
                              2240u_3^{29}u_2^3u_1^4 + 1344u_3^{29}u_2^2u_1^5 - 448u_3^{29}u_2u_1^6 + 64u_3^{29}u_1^7 - 448u_3^{29}u_1^7 + 64u_3^{29}u_1^7 - 448u_3^{29}u_2^7 + 64u_3^{29}u_1^7 - 448u_3^{29}u_2^7 + 64u_3^{29}u_2^7 - 448u_3^{29}u_2^7 - 448u_3^7 
                              64u_3^{27}u_2^9 + 448u_3^{27}u_2^8u_1 - 1344u_3^{27}u_2^7u_1^2 + 2240u_3^{27}u_2^6u_1^3 -
                              2240u_3^{27}u_2^5u_1^4 + 1344u_3^{27}u_2^4u_1^5 - 448u_3^{27}u_2^3u_1^6 +
                              64u_3^{27}u_2^2u_1^7
p_{20} =
                              32u_3^{21}u_2^6u_1 - 192u_3^{21}u_2^5u_1^2 + 480u_3^{21}u_2^4u_1^3 -
                              640u_3^{21}u_2^3u_1^4 + 480u_3^{21}u_2^2u_1^5 - 192u_3^{21}u_2u_1^6 + 32u_3^{21}u_1^7 +
                              32u_3^{19}u_2^8u_1 - 192u_3^{19}u_2^7u_1^2 + 480u_3^{19}u_2^6u_1^3 -
                              640u_3^{19}u_2^5u_1^4 + 480u_3^{19}u_2^4u_1^5 - 192u_3^{19}u_2^3u_1^6 +
                              32u_3^{19}u_2^2u_1^7)x_9 +
                              (-32u_3^{22}u_2^6u_1+192u_3^{22}u_2^5u_1^2-480u_3^{22}u_2^4u_1^3+
                              640u_3^{22}u_2^3u_1^4 - 480u_3^{22}u_2^2u_1^5 + 192u_3^{22}u_2u_1^6 - 32u_3^{22}u_1^7 - \\
                              32u_3^{20}u_2^8u_1 + 192u_3^{20}u_2^7u_1^2 - 480u_3^{20}u_2^6u_1^3 +
                              640u_3^{20}u_2^5u_1^4 - 480u_3^{20}u_2^4u_1^5 + 192u_3^{20}u_2^3u_1^6 -
                              32u_3^{20}u_2^2u_1^7
p_{21}
p_{22}
                               -16u_3^{18}u_2^6 + 96u_3^{18}u_2^5u_1 - 240u_3^{18}u_2^4u_1^2 + 320u_3^{18}u_2^3u_1^3 -
                              240u_3^{18}u_2^2u_1^4 + 96u_3^{18}u_2u_1^5 - 16u_3^{18}u_1^6 - 16u_3^{16}u_2^8 +
                              96u_3^{16}u_2^7u_1 - 240u_3^{16}u_2^6u_1^2 + 320u_3^{16}u_2^5u_1^3 -
                              240u_3^{16}u_2^4u_1^4 + 96u_3^{16}u_2^3u_1^5 - 16u_3^{16}u_2^2u_1^6)x_9 +
                               (16u_3^{19}u_2^6 - 96u_3^{19}u_2^5u_1 + 240u_3^{19}u_2^4u_1^2 - 320u_3^{19}u_2^3u_1^3 +
                              240u_3^{19}u_2^2u_1^4 - 96u_3^{19}u_2u_1^5 + 16u_3^{19}u_1^6 + 16u_3^{17}u_2^8 -
                              96u_3^{17}u_2^7u_1 + 240u_3^{17}u_2^6u_1^2 - 320u_3^{17}u_2^5u_1^3 +
                              240u_3^{17}u_2^4u_1^4 - 96u_3^{17}u_2^3u_1^5 + 16u_3^{17}u_2^2u_1^6
p_{23}
p_{24}
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1. Creating S-polynomial from the pair  $(p_0, p_{14})$ . Skipping pair  $p_0$  and  $p_{14}$  because gcd of their leading monoms is zero.

- 2. Creating S-polynomial from the pair  $(p_0, p_{15})$ . Skipping pair  $p_0$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 3. Creating S-polynomial from the pair  $(p_0, p_{16})$ . Skipping pair  $p_0$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 4. Creating S-polynomial from the pair  $(p_0, p_{17})$ . Skipping pair  $p_0$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 5. Creating S-polynomial from the pair  $(p_0, p_{18})$ . Skipping pair  $p_0$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 6. Creating S-polynomial from the pair  $(p_0, p_{19})$ . Skipping pair  $p_0$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 7. Creating S-polynomial from the pair  $(p_0, p_{20})$ . Skipping pair  $p_0$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 8. Creating S-polynomial from the pair  $(p_0, p_{21})$ . Skipping pair  $p_0$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 9. Creating S-polynomial from the pair  $(p_0, p_{22})$ . Skipping pair  $p_0$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 10. Creating S-polynomial from the pair  $(p_0, p_{23})$ . Skipping pair  $p_0$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 11. Creating S-polynomial from the pair  $(p_0, p_{24})$ . Skipping pair  $p_0$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 12. Creating S-polynomial from the pair  $(p_1, p_{14})$ . Skipping pair  $p_1$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 13. Creating S-polynomial from the pair  $(p_1, p_{15})$ . Skipping pair  $p_1$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 14. Creating S-polynomial from the pair  $(p_1, p_{16})$ . Skipping pair  $p_1$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 15. Creating S-polynomial from the pair  $(p_1, p_{17})$ . Skipping pair  $p_1$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 16. Creating S-polynomial from the pair  $(p_1, p_{18})$ . Skipping pair  $p_1$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 17. Creating S-polynomial from the pair  $(p_1, p_{19})$ . Skipping pair  $p_1$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 18. Creating S-polynomial from the pair  $(p_1, p_{20})$ . Skipping pair  $p_1$  and  $p_{20}$  because gcd of their leading monoms is zero.

- 19. Creating S-polynomial from the pair  $(p_1, p_{21})$ . Skipping pair  $p_1$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 20. Creating S-polynomial from the pair  $(p_1, p_{22})$ . Skipping pair  $p_1$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 21. Creating S-polynomial from the pair  $(p_1, p_{23})$ . Skipping pair  $p_1$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 22. Creating S-polynomial from the pair  $(p_1, p_{24})$ . Skipping pair  $p_1$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 23. Creating S-polynomial from the pair  $(p_2, p_{14})$ . Skipping pair  $p_2$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 24. Creating S-polynomial from the pair  $(p_2, p_{15})$ . Skipping pair  $p_2$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 25. Creating S-polynomial from the pair  $(p_2, p_{16})$ . Skipping pair  $p_2$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 26. Creating S-polynomial from the pair  $(p_2, p_{17})$ . Skipping pair  $p_2$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 27. Creating S-polynomial from the pair  $(p_2, p_{18})$ . Skipping pair  $p_2$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 28. Creating S-polynomial from the pair  $(p_2, p_{19})$ . Skipping pair  $p_2$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 29. Creating S-polynomial from the pair  $(p_2, p_{20})$ . Skipping pair  $p_2$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 30. Creating S-polynomial from the pair  $(p_2, p_{21})$ . Skipping pair  $p_2$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 31. Creating S-polynomial from the pair  $(p_2, p_{22})$ . Skipping pair  $p_2$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 32. Creating S-polynomial from the pair  $(p_2, p_{23})$ . Skipping pair  $p_2$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 33. Creating S-polynomial from the pair  $(p_2, p_{24})$ . Skipping pair  $p_2$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 34. Creating S-polynomial from the pair  $(p_3, p_{14})$ . Skipping pair  $p_3$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 35. Creating S-polynomial from the pair  $(p_3, p_{15})$ . Skipping pair  $p_3$  and  $p_{15}$  because gcd of their leading monoms is zero.

- 36. Creating S-polynomial from the pair  $(p_3, p_{16})$ . Skipping pair  $p_3$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 37. Creating S-polynomial from the pair  $(p_3, p_{17})$ . Skipping pair  $p_3$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 38. Creating S-polynomial from the pair  $(p_3, p_{18})$ . Skipping pair  $p_3$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 39. Creating S-polynomial from the pair  $(p_3, p_{19})$ . Skipping pair  $p_3$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 40. Creating S-polynomial from the pair  $(p_3, p_{20})$ . Skipping pair  $p_3$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 41. Creating S-polynomial from the pair  $(p_3, p_{21})$ . Skipping pair  $p_3$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 42. Creating S-polynomial from the pair  $(p_3, p_{22})$ . Skipping pair  $p_3$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 43. Creating S-polynomial from the pair  $(p_3, p_{23})$ . Skipping pair  $p_3$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 44. Creating S-polynomial from the pair  $(p_3, p_{24})$ . Skipping pair  $p_3$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 45. Creating S-polynomial from the pair  $(p_4, p_{14})$ . Skipping pair  $p_4$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 46. Creating S-polynomial from the pair  $(p_4, p_{15})$ . Skipping pair  $p_4$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 47. Creating S-polynomial from the pair  $(p_4, p_{16})$ . Skipping pair  $p_4$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 48. Creating S-polynomial from the pair  $(p_4, p_{17})$ . Skipping pair  $p_4$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 49. Creating S-polynomial from the pair  $(p_4, p_{18})$ . Skipping pair  $p_4$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 50. Creating S-polynomial from the pair  $(p_4, p_{19})$ . Skipping pair  $p_4$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 51. Creating S-polynomial from the pair  $(p_4, p_{20})$ . Skipping pair  $p_4$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 52. Creating S-polynomial from the pair  $(p_4, p_{21})$ . Skipping pair  $p_4$  and  $p_{21}$  because gcd of their leading monoms is zero.

- 53. Creating S-polynomial from the pair  $(p_4, p_{22})$ . Skipping pair  $p_4$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 54. Creating S-polynomial from the pair  $(p_4, p_{23})$ . Skipping pair  $p_4$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 55. Creating S-polynomial from the pair  $(p_4, p_{24})$ . Skipping pair  $p_4$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 56. Creating S-polynomial from the pair  $(p_5, p_{14})$ . Skipping pair  $p_5$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 57. Creating S-polynomial from the pair  $(p_5, p_{15})$ . Skipping pair  $p_5$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 58. Creating S-polynomial from the pair  $(p_5, p_{16})$ . Skipping pair  $p_5$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 59. Creating S-polynomial from the pair  $(p_5, p_{17})$ . Skipping pair  $p_5$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 60. Creating S-polynomial from the pair  $(p_5, p_{18})$ . Skipping pair  $p_5$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 61. Creating S-polynomial from the pair  $(p_5, p_{19})$ . Skipping pair  $p_5$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 62. Creating S-polynomial from the pair  $(p_5, p_{20})$ . Skipping pair  $p_5$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 63. Creating S-polynomial from the pair  $(p_5, p_{21})$ . Skipping pair  $p_5$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 64. Creating S-polynomial from the pair  $(p_5, p_{22})$ . Skipping pair  $p_5$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 65. Creating S-polynomial from the pair  $(p_5, p_{23})$ . Skipping pair  $p_5$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 66. Creating S-polynomial from the pair  $(p_5, p_{24})$ . Skipping pair  $p_5$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 67. Creating S-polynomial from the pair  $(p_6, p_{14})$ . Skipping pair  $p_6$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 68. Creating S-polynomial from the pair  $(p_6, p_{15})$ . Skipping pair  $p_6$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 69. Creating S-polynomial from the pair  $(p_6, p_{16})$ . Skipping pair  $p_6$  and  $p_{16}$  because gcd of their leading monoms is zero.

- 70. Creating S-polynomial from the pair  $(p_6, p_{17})$ . Skipping pair  $p_6$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 71. Creating S-polynomial from the pair  $(p_6, p_{18})$ . Skipping pair  $p_6$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 72. Creating S-polynomial from the pair  $(p_6, p_{19})$ . Skipping pair  $p_6$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 73. Creating S-polynomial from the pair  $(p_6, p_{20})$ . Skipping pair  $p_6$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 74. Creating S-polynomial from the pair  $(p_6, p_{21})$ . Skipping pair  $p_6$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 75. Creating S-polynomial from the pair  $(p_6, p_{22})$ . Skipping pair  $p_6$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 76. Creating S-polynomial from the pair  $(p_6, p_{23})$ . Skipping pair  $p_6$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 77. Creating S-polynomial from the pair  $(p_6, p_{24})$ . Skipping pair  $p_6$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 78. Creating S-polynomial from the pair  $(p_7, p_{14})$ . Skipping pair  $p_7$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 79. Creating S-polynomial from the pair  $(p_7, p_{15})$ . Skipping pair  $p_7$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 80. Creating S-polynomial from the pair  $(p_7, p_{16})$ . Skipping pair  $p_7$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 81. Creating S-polynomial from the pair  $(p_7, p_{17})$ . Skipping pair  $p_7$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 82. Creating S-polynomial from the pair  $(p_7, p_{18})$ . Skipping pair  $p_7$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 83. Creating S-polynomial from the pair  $(p_7, p_{19})$ . Skipping pair  $p_7$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 84. Creating S-polynomial from the pair  $(p_7, p_{20})$ . Skipping pair  $p_7$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 85. Creating S-polynomial from the pair  $(p_7, p_{21})$ . Skipping pair  $p_7$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 86. Creating S-polynomial from the pair  $(p_7, p_{22})$ . Skipping pair  $p_7$  and  $p_{22}$  because gcd of their leading monoms is zero.

- 87. Creating S-polynomial from the pair  $(p_7, p_{23})$ . Skipping pair  $p_7$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 88. Creating S-polynomial from the pair  $(p_7, p_{24})$ . Skipping pair  $p_7$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 89. Creating S-polynomial from the pair  $(p_8, p_{14})$ . Skipping pair  $p_8$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 90. Creating S-polynomial from the pair  $(p_8, p_{15})$ . Skipping pair  $p_8$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 91. Creating S-polynomial from the pair  $(p_8, p_{16})$ . Skipping pair  $p_8$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 92. Creating S-polynomial from the pair  $(p_8, p_{17})$ . Skipping pair  $p_8$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 93. Creating S-polynomial from the pair  $(p_8, p_{18})$ . Skipping pair  $p_8$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 94. Creating S-polynomial from the pair  $(p_8, p_{19})$ . Skipping pair  $p_8$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 95. Creating S-polynomial from the pair  $(p_8, p_{20})$ . Skipping pair  $p_8$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 96. Creating S-polynomial from the pair  $(p_8, p_{21})$ . Skipping pair  $p_8$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 97. Creating S-polynomial from the pair  $(p_8, p_{22})$ . Skipping pair  $p_8$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 98. Creating S-polynomial from the pair  $(p_8, p_{23})$ . Skipping pair  $p_8$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 99. Creating S-polynomial from the pair  $(p_8, p_{24})$ . Skipping pair  $p_8$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 100. Creating S-polynomial from the pair  $(p_9, p_{14})$ . Skipping pair  $p_9$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 101. Creating S-polynomial from the pair  $(p_9, p_{15})$ . Skipping pair  $p_9$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 102. Creating S-polynomial from the pair  $(p_9, p_{16})$ . Skipping pair  $p_9$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 103. Creating S-polynomial from the pair  $(p_9, p_{17})$ . Skipping pair  $p_9$  and  $p_{17}$  because gcd of their leading monoms is zero.

- 104. Creating S-polynomial from the pair  $(p_9, p_{18})$ . Skipping pair  $p_9$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 105. Creating S-polynomial from the pair  $(p_9, p_{19})$ . Skipping pair  $p_9$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 106. Creating S-polynomial from the pair  $(p_9, p_{20})$ . Skipping pair  $p_9$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 107. Creating S-polynomial from the pair  $(p_9, p_{21})$ . Skipping pair  $p_9$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 108. Creating S-polynomial from the pair  $(p_9, p_{22})$ . Skipping pair  $p_9$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 109. Creating S-polynomial from the pair  $(p_9, p_{23})$ . Skipping pair  $p_9$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 110. Creating S-polynomial from the pair  $(p_9, p_{24})$ . Skipping pair  $p_9$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 111. Creating S-polynomial from the pair  $(p_{10}, p_{14})$ . Skipping pair  $p_{10}$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 112. Creating S-polynomial from the pair  $(p_{10}, p_{15})$ . Skipping pair  $p_{10}$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 113. Creating S-polynomial from the pair  $(p_{10}, p_{16})$ . Skipping pair  $p_{10}$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 114. Creating S-polynomial from the pair  $(p_{10}, p_{17})$ . Skipping pair  $p_{10}$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 115. Creating S-polynomial from the pair  $(p_{10}, p_{18})$ . Skipping pair  $p_{10}$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 116. Creating S-polynomial from the pair  $(p_{10}, p_{19})$ . Skipping pair  $p_{10}$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 117. Creating S-polynomial from the pair  $(p_{10}, p_{20})$ . Skipping pair  $p_{10}$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 118. Creating S-polynomial from the pair  $(p_{10}, p_{21})$ . Skipping pair  $p_{10}$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 119. Creating S-polynomial from the pair  $(p_{10}, p_{22})$ . Skipping pair  $p_{10}$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 120. Creating S-polynomial from the pair  $(p_{10}, p_{23})$ . Skipping pair  $p_{10}$  and  $p_{23}$  because gcd of their leading monoms is zero.

- 121. Creating S-polynomial from the pair  $(p_{10}, p_{24})$ . Skipping pair  $p_{10}$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 122. Creating S-polynomial from the pair  $(p_{11}, p_{14})$ . Skipping pair  $p_{11}$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 123. Creating S-polynomial from the pair  $(p_{11}, p_{15})$ . Skipping pair  $p_{11}$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 124. Creating S-polynomial from the pair  $(p_{11}, p_{16})$ . Skipping pair  $p_{11}$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 125. Creating S-polynomial from the pair  $(p_{11}, p_{17})$ . Skipping pair  $p_{11}$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 126. Creating S-polynomial from the pair  $(p_{11}, p_{18})$ . Skipping pair  $p_{11}$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 127. Creating S-polynomial from the pair  $(p_{11}, p_{19})$ . Skipping pair  $p_{11}$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 128. Creating S-polynomial from the pair  $(p_{11}, p_{20})$ . Skipping pair  $p_{11}$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 129. Creating S-polynomial from the pair  $(p_{11}, p_{21})$ . Skipping pair  $p_{11}$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 130. Creating S-polynomial from the pair  $(p_{11}, p_{22})$ . Skipping pair  $p_{11}$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 131. Creating S-polynomial from the pair  $(p_{11}, p_{23})$ . Skipping pair  $p_{11}$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 132. Creating S-polynomial from the pair  $(p_{11}, p_{24})$ . Skipping pair  $p_{11}$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 133. Creating S-polynomial from the pair  $(p_{12}, p_{14})$ . Skipping pair  $p_{12}$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 134. Creating S-polynomial from the pair  $(p_{12}, p_{15})$ . Skipping pair  $p_{12}$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 135. Creating S-polynomial from the pair  $(p_{12}, p_{16})$ . Skipping pair  $p_{12}$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 136. Creating S-polynomial from the pair  $(p_{12}, p_{17})$ . Skipping pair  $p_{12}$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 137. Creating S-polynomial from the pair  $(p_{12}, p_{18})$ . Skipping pair  $p_{12}$  and  $p_{18}$  because gcd of their leading monoms is zero.

- 138. Creating S-polynomial from the pair  $(p_{12}, p_{19})$ . Skipping pair  $p_{12}$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 139. Creating S-polynomial from the pair  $(p_{12}, p_{20})$ . Skipping pair  $p_{12}$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 140. Creating S-polynomial from the pair  $(p_{12}, p_{21})$ . Skipping pair  $p_{12}$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 141. Creating S-polynomial from the pair  $(p_{12}, p_{22})$ . Skipping pair  $p_{12}$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 142. Creating S-polynomial from the pair  $(p_{12}, p_{23})$ . Skipping pair  $p_{12}$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 143. Creating S-polynomial from the pair  $(p_{12}, p_{24})$ . Skipping pair  $p_{12}$  and  $p_{24}$  because gcd of their leading monoms is zero.
- 144. Creating S-polynomial from the pair  $(p_{13}, p_{14})$ . Skipping pair  $p_{13}$  and  $p_{14}$  because gcd of their leading monoms is zero.
- 145. Creating S-polynomial from the pair  $(p_{13}, p_{15})$ . Skipping pair  $p_{13}$  and  $p_{15}$  because gcd of their leading monoms is zero.
- 146. Creating S-polynomial from the pair  $(p_{13}, p_{16})$ . Skipping pair  $p_{13}$  and  $p_{16}$  because gcd of their leading monoms is zero.
- 147. Creating S-polynomial from the pair  $(p_{13}, p_{17})$ . Skipping pair  $p_{13}$  and  $p_{17}$  because gcd of their leading monoms is zero.
- 148. Creating S-polynomial from the pair  $(p_{13}, p_{18})$ . Skipping pair  $p_{13}$  and  $p_{18}$  because gcd of their leading monoms is zero.
- 149. Creating S-polynomial from the pair  $(p_{13}, p_{19})$ . Skipping pair  $p_{13}$  and  $p_{19}$  because gcd of their leading monoms is zero.
- 150. Creating S-polynomial from the pair  $(p_{13}, p_{20})$ . Skipping pair  $p_{13}$  and  $p_{20}$  because gcd of their leading monoms is zero.
- 151. Creating S-polynomial from the pair  $(p_{13}, p_{21})$ . Skipping pair  $p_{13}$  and  $p_{21}$  because gcd of their leading monoms is zero.
- 152. Creating S-polynomial from the pair  $(p_{13}, p_{22})$ . Skipping pair  $p_{13}$  and  $p_{22}$  because gcd of their leading monoms is zero.
- 153. Creating S-polynomial from the pair  $(p_{13}, p_{23})$ . Skipping pair  $p_{13}$  and  $p_{23}$  because gcd of their leading monoms is zero.
- 154. Creating S-polynomial from the pair  $(p_{13}, p_{24})$ . Skipping pair  $p_{13}$  and  $p_{24}$  because gcd of their leading monoms is zero.

155. Creating S-polynomial from the pair  $(p_{14}, p_{15})$ . Forming S-pol of  $p_{14}$  and  $p_{15}$ :

$$p_{73} = 0$$

Reduced to zero.

156. Creating S-polynomial from the pair  $(p_{14}, p_{16})$ . Forming S-pol of  $p_{14}$  and  $p_{16}$ :

$$p_{74} = 0$$

Reduced to zero.

157. Creating S-polynomial from the pair  $(p_{14}, p_{17})$ . Forming S-pol of  $p_{14}$  and  $p_{17}$ :

$$p_{75} = 0$$

Reduced to zero.

158. Creating S-polynomial from the pair  $(p_{14}, p_{18})$ . Forming S-pol of  $p_{14}$  and  $p_{18}$ :

$$p_{76} = 0$$

Reduced to zero.

159. Creating S-polynomial from the pair  $(p_{14}, p_{19})$ . Forming S-pol of  $p_{14}$  and  $p_{19}$ :

$$p_{77} = 0$$

Reduced to zero.

160. Creating S-polynomial from the pair  $(p_{14}, p_{20})$ . Forming S-pol of  $p_{14}$  and  $p_{20}$ :

$$p_{78} = 0$$

Reduced to zero.

161. Creating S-polynomial from the pair  $(p_{14}, p_{21})$ . Forming S-pol of  $p_{14}$  and  $p_{21}$ :

$$p_{79} = 0$$

Reduced to zero.

162. Creating S-polynomial from the pair  $(p_{14}, p_{22})$ . Forming S-pol of  $p_{14}$  and  $p_{22}$ :

$$p_{80} = 0$$

163.	Creating S-polynomial from the pair	$(p_{14}, p_{23})$
	Forming S-pol of $p_{14}$ and $p_{23}$ :	

$$p_{81} = 0$$

Reduced to zero.

164. Creating S-polynomial from the pair  $(p_{14}, p_{24})$ . Forming S-pol of  $p_{14}$  and  $p_{24}$ :

$$p_{82}=0$$

Reduced to zero.

165. Creating S-polynomial from the pair  $(p_{15}, p_{16})$ . Forming S-pol of  $p_{15}$  and  $p_{16}$ :

$$p_{83} = 0$$

Reduced to zero.

166. Creating S-polynomial from the pair  $(p_{15}, p_{17})$ . Forming S-pol of  $p_{15}$  and  $p_{17}$ :

$$p_{84} = 0$$

Reduced to zero.

167. Creating S-polynomial from the pair  $(p_{15}, p_{18})$ . Forming S-pol of  $p_{15}$  and  $p_{18}$ :

$$p_{85} = 0$$

Reduced to zero.

168. Creating S-polynomial from the pair  $(p_{15}, p_{19})$ . Forming S-pol of  $p_{15}$  and  $p_{19}$ :

$$p_{86} = 0$$

Reduced to zero.

169. Creating S-polynomial from the pair  $(p_{15}, p_{20})$ . Forming S-pol of  $p_{15}$  and  $p_{20}$ :

$$p_{87} = 0$$

Reduced to zero.

170. Creating S-polynomial from the pair  $(p_{15}, p_{21})$ . Forming S-pol of  $p_{15}$  and  $p_{21}$ :

$$p_{88} = 0$$

171. Creating S-polynomial from the pair  $(p_{15}, p_{22})$ . Forming S-pol of  $p_{15}$  and  $p_{22}$ :

$$p_{89} = 0$$

Reduced to zero.

172. Creating S-polynomial from the pair  $(p_{15}, p_{23})$ . Forming S-pol of  $p_{15}$  and  $p_{23}$ :

$$p_{90} = 0$$

Reduced to zero.

173. Creating S-polynomial from the pair  $(p_{15}, p_{24})$ . Forming S-pol of  $p_{15}$  and  $p_{24}$ :

$$p_{91} = 0$$

Reduced to zero.

174. Creating S-polynomial from the pair  $(p_{16}, p_{17})$ . Forming S-pol of  $p_{16}$  and  $p_{17}$ :

$$p_{92} = 0$$

Reduced to zero.

175. Creating S-polynomial from the pair  $(p_{16}, p_{18})$ . Forming S-pol of  $p_{16}$  and  $p_{18}$ :

$$p_{93} = 0$$

Reduced to zero.

176. Creating S-polynomial from the pair  $(p_{16}, p_{19})$ . Forming S-pol of  $p_{16}$  and  $p_{19}$ :

$$p_{94} = 0$$

Reduced to zero.

177. Creating S-polynomial from the pair  $(p_{16}, p_{20})$ . Forming S-pol of  $p_{16}$  and  $p_{20}$ :

$$p_{95} = 0$$

Reduced to zero.

178. Creating S-polynomial from the pair  $(p_{16}, p_{21})$ . Forming S-pol of  $p_{16}$  and  $p_{21}$ :

$$p_{96} = 0$$

179.	Creating S-polynomial from the pair	$(p_{16}, p_{22})$
	Forming S-pol of $p_{16}$ and $p_{22}$ :	

$$p_{97} = 0$$

Reduced to zero.

180. Creating S-polynomial from the pair  $(p_{16}, p_{23})$ . Forming S-pol of  $p_{16}$  and  $p_{23}$ :

$$p_{98} = 0$$

Reduced to zero.

181. Creating S-polynomial from the pair  $(p_{16}, p_{24})$ . Forming S-pol of  $p_{16}$  and  $p_{24}$ :

$$p_{99} = 0$$

Reduced to zero.

182. Creating S-polynomial from the pair  $(p_{17}, p_{18})$ . Forming S-pol of  $p_{17}$  and  $p_{18}$ :

$$p_{100} = 0$$

Reduced to zero.

183. Creating S-polynomial from the pair  $(p_{17}, p_{19})$ . Forming S-pol of  $p_{17}$  and  $p_{19}$ :

$$p_{101} = 0$$

Reduced to zero.

184. Creating S-polynomial from the pair  $(p_{17}, p_{20})$ . Forming S-pol of  $p_{17}$  and  $p_{20}$ :

$$p_{102} = 0$$

Reduced to zero.

185. Creating S-polynomial from the pair  $(p_{17}, p_{21})$ . Forming S-pol of  $p_{17}$  and  $p_{21}$ :

$$p_{103} = 0$$

Reduced to zero.

186. Creating S-polynomial from the pair  $(p_{17}, p_{22})$ . Forming S-pol of  $p_{17}$  and  $p_{22}$ :

$$p_{104} = 0$$

187.	Creating S-polynomial from the pair (	$(p_{17}, p_{23})$
	Forming S-pol of $p_{17}$ and $p_{23}$ :	

$$p_{105} = 0$$

Reduced to zero.

188. Creating S-polynomial from the pair  $(p_{17}, p_{24})$ . Forming S-pol of  $p_{17}$  and  $p_{24}$ :

$$p_{106}=0$$

Reduced to zero.

189. Creating S-polynomial from the pair  $(p_{18}, p_{19})$ . Forming S-pol of  $p_{18}$  and  $p_{19}$ :

$$p_{107} = 0$$

Reduced to zero.

190. Creating S-polynomial from the pair  $(p_{18}, p_{20})$ . Forming S-pol of  $p_{18}$  and  $p_{20}$ :

$$p_{108} = 0$$

Reduced to zero.

191. Creating S-polynomial from the pair  $(p_{18}, p_{21})$ . Forming S-pol of  $p_{18}$  and  $p_{21}$ :

$$p_{109} = 0$$

Reduced to zero.

192. Creating S-polynomial from the pair  $(p_{18}, p_{22})$ . Forming S-pol of  $p_{18}$  and  $p_{22}$ :

$$p_{110}=0$$

Reduced to zero.

193. Creating S-polynomial from the pair  $(p_{18}, p_{23})$ . Forming S-pol of  $p_{18}$  and  $p_{23}$ :

$$p_{111}=0$$

Reduced to zero.

194. Creating S-polynomial from the pair  $(p_{18}, p_{24})$ . Forming S-pol of  $p_{18}$  and  $p_{24}$ :

$$p_{112} = 0$$

195. Creating S-polynomial from the pair  $(p_{19}, p_{20})$ . Forming S-pol of  $p_{19}$  and  $p_{20}$ :

$$p_{113}=0$$

Reduced to zero.

196. Creating S-polynomial from the pair  $(p_{19}, p_{21})$ . Forming S-pol of  $p_{19}$  and  $p_{21}$ :

$$p_{114}=0$$

Reduced to zero.

197. Creating S-polynomial from the pair  $(p_{19}, p_{22})$ . Forming S-pol of  $p_{19}$  and  $p_{22}$ :

$$p_{115} = 0$$

Reduced to zero.

198. Creating S-polynomial from the pair  $(p_{19}, p_{23})$ . Forming S-pol of  $p_{19}$  and  $p_{23}$ :

$$p_{116} = 0$$

Reduced to zero.

199. Creating S-polynomial from the pair  $(p_{19}, p_{24})$ . Forming S-pol of  $p_{19}$  and  $p_{24}$ :

$$p_{117} = 0$$

Reduced to zero.

200. Creating S-polynomial from the pair  $(p_{20}, p_{21})$ . Forming S-pol of  $p_{20}$  and  $p_{21}$ :

$$p_{118} = 0$$

Reduced to zero.

201. Creating S-polynomial from the pair  $(p_{20}, p_{22})$ . Forming S-pol of  $p_{20}$  and  $p_{22}$ :

$$p_{119} = 0$$

Reduced to zero.

202. Creating S-polynomial from the pair  $(p_{20}, p_{23})$ . Forming S-pol of  $p_{20}$  and  $p_{23}$ :

$$p_{120} = 0$$

203. Creating S-polynomial from the pair  $(p_{20}, p_{24})$ . Forming S-pol of  $p_{20}$  and  $p_{24}$ :

$$p_{121} = 0$$

Reduced to zero.

204. Creating S-polynomial from the pair  $(p_{21}, p_{22})$ . Forming S-pol of  $p_{21}$  and  $p_{22}$ :

$$p_{122} = 0$$

Reduced to zero.

205. Creating S-polynomial from the pair  $(p_{21}, p_{23})$ . Forming S-pol of  $p_{21}$  and  $p_{23}$ :

$$p_{123} = 0$$

Reduced to zero.

206. Creating S-polynomial from the pair  $(p_{21}, p_{24})$ . Forming S-pol of  $p_{21}$  and  $p_{24}$ :

$$p_{124} = 0$$

Reduced to zero.

207. Creating S-polynomial from the pair  $(p_{22}, p_{23})$ . Forming S-pol of  $p_{22}$  and  $p_{23}$ :

$$p_{125} = 0$$

Reduced to zero.

208. Creating S-polynomial from the pair  $(p_{22}, p_{24})$ . Forming S-pol of  $p_{22}$  and  $p_{24}$ :

$$p_{126} = 0$$

Reduced to zero.

209. Creating S-polynomial from the pair  $(p_{23}, p_{24})$ . Forming S-pol of  $p_{23}$  and  $p_{24}$ :

$$p_{127} = 0$$

#### 5.4 Groebner Basis

Groebner basis has 25 polynomials:

```
= u_3x_1 + (-u_3^2 - u_2^2 + u_2u_1)
      = x_6x_1 - u_3x_6 + (u_2 - u_1)x_5 - u_2x_1 + u_3u_1
      = -x_6 + (2u_2 - u_1)
      = 2x_7x_3 - 2x_7x_1 - x_3^2 + x_1^2
       = -x_{10}x_5 + x_{10}x_1 + x_9x_6 - u_1x_9 - x_6x_1 + u_1x_5
       = 2x_{10}x_6 - 2u_1x_{10} + 2x_9x_5 - 2x_9x_1 - x_6^2 - x_5^2 + x_1^2 + u_1^2
      = (-u_2 + u_1)x_{12} + (u_2 - u_1)x_{10} - x_9x_1 + u_3x_9 + x_7x_1 - u_3x_7
      = (u_3^2 u_2 - u_3^2 u_1) x_5 +
 p_8
             (-u_3^3u_2 + u_3^3u_1 + u_3u_2^3 - 2u_3u_2^2u_1 + u_3u_2u_1^2)
      = (-4u_3^4 - 4u_3^2u_2^2 + 4u_3^2u_2u_1)x_7
     = (u_3u_2 - u_3u_1)x_5 + (-u_3^2u_2 + u_3^2u_1 + u_2^3 - 2u_2^2u_1 + u_2u_1^2)
p_{11} = (4u_3^{10}u_2 - 4u_3^{10}u_1)x_{10} + (2u_3^{10} + 2u_3^8u_2^2 - 2u_3^8u_2u_1)x_9x_5 +
             (-2u_3^{11} - 8u_3^9u_2^2 + 12u_3^9u_2u_1 - 4u_3^9u_1^2 - 2u_3^7u_2^4 + 4u_3^7u_2^3u_1 -
             2u_3^7u_2^2u_1^2)x_9 + (-u_3^{10} - u_3^8u_2^2 + u_3^8u_2u_1)x_5^2 +
             (-2u_3^9u_2u_1+2u_3^9u_1^2)x_5+
             (u_3^{12} + 3u_3^{10}u_2^2 - 5u_3^{10}u_2u_1 + 2u_3^{10}u_1^2 + 3u_3^8u_2^4 - 8u_3^8u_2^3u_1 +
             7u_3^8u_2^2u_1^2 - 2u_3^8u_2u_1^3 + u_3^6u_2^6 - 3u_3^6u_2^5u_1 +
             3u_3^6u_2^4u_1^2 - u_3^6u_2^3u_1^3
p_{12} = (4u_3^3u_2 - 4u_3^3u_1)x_{10} + 2u_3^3x_9x_5 +
             (-2u_3^4 - 2u_3^2u_2^2 + 2u_3^2u_2u_1)x_9 - u_3^3x_5^2 +
             (u_3^5 - 2u_3^3u_2^2 + 2u_3^3u_2u_1 + u_3u_2^4 - 2u_3u_2^3u_1 + u_3u_2^2u_1^2)
     = (
p_{13}
             4u_3^8u_2 - 4u_3^8u_1 + 4u_3^6u_2^3 - 8u_3^6u_2^2u_1 + 4u_3^6u_2u_1^2)x_{10} +
             2u_3^7x_9x_5^2 + (-2u_3^8 - 2u_3^6u_2^2 + 2u_3^6u_2u_1)x_9x_5 +
             (8u_3^7u_2^2 - 16u_3^7u_2u_1 + 8u_3^7u_1^2)x_9 - u_3^7x_5^3 +
             (u_3^9 - 2u_3^7u_2^2 + 6u_3^7u_2u_1 - 4u_3^7u_1^2 + u_3^5u_2^4 - 2u_3^5u_2^3u_1 +
             u_2^5u_2^2u_1^2)x_5 +
             (-8u_3^8u_2^2 + 12u_3^8u_2u_1 - 4u_3^8u_1^2 - 8u_3^6u_2^4 + 20u_3^6u_2^3u_1 -
             16u_3^6u_2^2u_1^2 + 4u_3^6u_2u_1^3
p_{14}
p_{15}
p_{16}
p_{17}
p_{18}
p_{19}
             64u_3^{28}u_2^7 - 448u_3^{28}u_2^6u_1 + 1344u_3^{28}u_2^5u_1^2 - 2240u_3^{28}u_2^4u_1^3 +
```

```
2240u_{3}^{28}u_{2}^{3}u_{1}^{4} - 1344u_{3}^{28}u_{2}^{2}u_{1}^{5} + 448u_{3}^{28}u_{2}u_{1}^{6} - 64u_{3}^{28}u_{1}^{7} +
               64u_3^{26}u_2^9 - 448u_3^{26}u_2^8u_1 + 1344u_3^{26}u_1^7u_1^2 - 2240u_3^{26}u_2^6u_1^3 +
               2240u_3^{26}u_2^5u_1^4 - 1344u_3^{26}u_2^4u_1^5 + 448u_3^{26}u_2^3u_1^6 -
               64u_3^{26}u_2^2u_1^7)x_9 +
               (-64u_3^{29}u_2^7 + 448u_3^{29}u_2^6u_1 - 1344u_3^{29}u_2^5u_1^2 + 2240u_3^{29}u_2^4u_1^3 -
               64u_3^{27}u_2^9 + 448u_3^{27}u_2^8u_1 - 1344u_3^{27}u_2^7u_1^2 + 2240u_3^{27}u_2^6u_1^3 -
               2240u_3^{27}u_2^5u_1^4 + 1344u_3^{27}u_2^4u_1^5 - 448u_3^{27}u_2^3u_1^6 +
               64u_3^{27}u_2^2u_1^7
p_{20} = (
               32u_3^{21}u_2^6u_1 - 192u_3^{21}u_2^5u_1^2 + 480u_3^{21}u_2^4u_1^3 -
               640u_3^{21}u_2^3u_1^4 + 480u_3^{21}u_2^2u_1^5 - 192u_3^{21}u_2u_1^6 + 32u_3^{21}u_1^7 +
               32u_3^{19}u_2^8u_1 - 192u_3^{19}u_2^7u_1^2 + 480u_3^{19}u_2^6u_1^3 -
               640u_3^{19}u_2^5u_1^4 + 480u_3^{19}u_2^4u_1^5 - 192u_3^{19}u_2^3u_1^6 +
               32u_3^{19}u_2^2u_1^7)x_9 +
               (-32u_3^{22}u_2^6u_1+192u_3^{22}u_2^5u_1^2-480u_3^{22}u_2^4u_1^3+
               640u_3^{22}u_2^3u_1^4 - 480u_3^{22}u_2^2u_1^5 + 192u_3^{22}u_2u_1^6 - 32u_3^{22}u_1^7 - \\
               32u_3^{20}u_2^8u_1 + 192u_3^{20}u_2^7u_1^2 - 480u_3^{20}u_2^6u_1^3 +
               640u_3^{20}u_2^5u_1^4 - 480u_3^{20}u_2^4u_1^5 + 192u_3^{20}u_2^3u_1^6 -
               32u_3^{20}u_2^2u_1^7
p_{21} = \dots
p_{22} = (
                -16u_3^{18}u_2^6 + 96u_3^{18}u_2^5u_1 - 240u_3^{18}u_2^4u_1^2 + 320u_3^{18}u_2^3u_1^3 -
               240u_3^{18}u_2^2u_1^4 + 96u_3^{18}u_2u_1^5 - 16u_3^{18}u_1^6 - 16u_3^{16}u_2^8 +
               96u_3^{16}u_2^7u_1 - 240u_3^{16}u_2^6u_1^2 + 320u_3^{16}u_2^5u_1^3 -
               240u_3^{16}u_2^4u_1^4 + 96u_3^{16}u_2^3u_1^5 - 16u_3^{16}u_2^2u_1^6)x_9 +
               (16u_3^{19}u_2^6 - 96u_3^{19}u_2^5u_1 + 240u_3^{19}u_2^4u_1^2 - 320u_3^{19}u_2^3u_1^3 +
               240u_{1}^{19}u_{2}^{2}u_{1}^{4} - 96u_{1}^{19}u_{2}u_{1}^{5} + 16u_{1}^{19}u_{1}^{6} + 16u_{1}^{17}u_{2}^{8} -
               96u_3^{17}u_2^7u_1 + 240u_3^{17}u_2^6u_1^2 - 320u_3^{17}u_2^5u_1^3 +
               240u_3^{17}u_2^4u_1^4 - 96u_3^{17}u_2^3u_1^5 + 16u_3^{17}u_2^2u_1^6
p_{23}
p_{24}
```

Groebner basis succesfully computed.

# 6 Reducing Polynomial Conjecture

Reducing with polynomial  $p_7$ , the result is:

$$p_{145} = (-2u_2 + 2u_1)x_{12}x_{10} + 2x_{12}x_9x_1 - 2u_3x_{12}x_9 - 2x_{12}x_7x_1 + 2u_3x_{12}x_7 + 2u_3x_7 + 2u_3x$$

$$(-2u_2+2u_1)x_7^2$$

Reducing with polynomial  $p_7$ , the result is:

$$p_{146} = (-2u_2 + 2u_1)x_{12}x_9x_1 + (2u_3u_2 - 2u_3u_1)x_{12}x_9 + (2u_2 - 2u_1)x_{12}x_7x_1 + (-2u_3u_2 + 2u_3u_1)x_{12}x_7 + (2u_2^2 - 4u_2u_1 + 2u_1^2)x_{10}^2 + (-2u_2 + 2u_1)x_{10}x_9x_1 + (2u_3u_2 - 2u_3u_1)x_{10}x_9 + (2u_2 - 2u_1)x_{10}x_7x_1 + (-2u_3u_2 + 2u_3u_1)x_{10}x_7 + (2u_2^2 - 4u_2u_1 + 2u_1^2)x_7^2$$

Reducing with polynomial  $p_0$ , the result is:

$$\begin{aligned} p_{147} &= (-2u_2^3 + 4u_2^2u_1 - 2u_2u_1^2)x_{12}x_9 + (2u_3u_2 - 2u_3u_1)x_{12}x_7x_1 + \\ & (-2u_3^2u_2 + 2u_3^2u_1)x_{12}x_7 + (2u_3u_2^2 - 4u_3u_2u_1 + 2u_3u_1^2)x_{10}^2 + \\ & (-2u_3u_2 + 2u_3u_1)x_{10}x_9x_1 + (2u_3^2u_2 - 2u_3^2u_1)x_{10}x_9 + \\ & (2u_3u_2 - 2u_3u_1)x_{10}x_7x_1 + (-2u_3^2u_2 + 2u_3^2u_1)x_{10}x_7 + \\ & (2u_3u_2^2 - 4u_3u_2u_1 + 2u_3u_1^2)x_7^2 \end{aligned}$$

Reducing with polynomial  $p_7$ , the result is:

$$p_{148} = (-2u_3u_2^2 + 4u_3u_2u_1 - 2u_3u_1^2)x_{12}x_7x_1 + (2u_3^2u_2^2 - 4u_3^2u_2u_1 + 2u_3^2u_1^2)x_{12}x_7 + (-2u_3u_2^3 + 6u_3u_2^2u_1 - 6u_3u_2u_1^2 + 2u_3u_1^3)x_{10}^2 + (2u_3u_2^2 - 4u_3u_2u_1 + 2u_3u_1^2)x_{10}x_9x_1 + (-2u_3^2u_2^2 + 4u_3^2u_2u_1 - 2u_3^2u_1^2 + 2u_2^4 - 6u_2^3u_1 + 6u_2^2u_1^2 - 2u_2u_1^3)x_{10}x_9 + (-2u_3u_2^2 + 4u_3u_2u_1 - 2u_3u_1^2)x_{10}x_7x_1 + (2u_3^2u_2^2 - 4u_3^2u_2u_1 + 2u_3^2u_1^2)x_{10}x_7 + (-2u_3^3 + 4u_2^2u_1 - 2u_2u_1^2)x_9^2x_1 + (2u_3u_2^3 - 4u_3u_2^2u_1 + 2u_3u_2u_1^2)x_9^2 + (2u_3^3 - 4u_2^2u_1 + 2u_2u_1^2)x_9x_7x_1 + (-2u_3u_2^3 + 4u_3u_2^2u_1 - 2u_3u_2u_1^2)x_9x_7 + (-2u_3u_2^3 + 6u_3u_2^2u_1 - 6u_3u_2u_1^2 + 2u_3u_1^3)x_7^2$$

Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (text size is 1006 characters, number of terms is 11)

Reducing with polynomial  $p_7$ , the result is:

Polynomial too big for output (text size is 1409 characters, number of terms is 11)

Reducing with polynomial  $p_{11}$ , the result is:

Polynomial too big for output (text size is 3617 characters, number of terms is 14)

Reducing with polynomial  $p_5$ , the result is:

Polynomial too big for output (text size is 4618 characters, number of terms is 16)

Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (text size is 3945 characters, number of terms is 15)

Reducing with polynomial  $p_{11}$ , the result is:

Polynomial too big for output (text size is 6745 characters, number of terms is 17)

Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (text size is 6400 characters, number of terms is 16)

Reducing with polynomial  $p_9$ , the result is:

Polynomial too big for output (number of terms is 15) Reducing with polynomial  $p_5$ , the result is:

Polynomial too big for output (number of terms is 18) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 17) Reducing with polynomial  $p_5$ , the result is:

Polynomial too big for output (number of terms is 20) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 19) Reducing with polynomial  $p_{11}$ , the result is:

Polynomial too big for output (number of terms is 19) Reducing with polynomial  $p_3$ , the result is:

Polynomial too big for output (number of terms is 18) Reducing with polynomial  $p_8$ , the result is:

Polynomial too big for output (number of terms is 17) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 16) Reducing with polynomial  $p_{14}$ , the result is:

Polynomial too big for output (number of terms is 15) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 14) Reducing with polynomial  $p_9$ , the result is:

Polynomial too big for output (number of terms is 13) Reducing with polynomial  $p_3$ , the result is:

Polynomial too big for output (number of terms is 12) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 11) Reducing with polynomial  $p_3$ , the result is:

Polynomial too big for output (number of terms is 10) Reducing with polynomial  $p_8$ , the result is:

Polynomial too big for output (number of terms is 9) Reducing with polynomial  $p_8$ , the result is:

Polynomial too big for output (number of terms is 8) Reducing with polynomial  $p_{14}$ , the result is:

Polynomial too big for output (number of terms is 7) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 6) Reducing with polynomial  $p_9$ , the result is:

Polynomial too big for output (number of terms is 5) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 5) Reducing with polynomial  $p_3$ , the result is:

Polynomial too big for output (number of terms is 4) Reducing with polynomial  $p_0$ , the result is:

Polynomial too big for output (number of terms is 4) Reducing with polynomial  $p_3$ , the result is:

Polynomial too big for output (number of terms is 3) Reducing with polynomial  $p_8$ , the result is:

Polynomial too big for output (number of terms is 2) Reducing with polynomial  $p_8$ , the result is:

$$p_{149} = 0$$

Conclusion is reduced to zero.

## 7 Prover report

Status: The conjecture has been proved.

**Space Complexity:** The biggest polynomial obtained during proof process contained 1560 terms.

**Time Complexity:** Time spent by the prover: 1.536 seconds. There are no ndg conditions.