

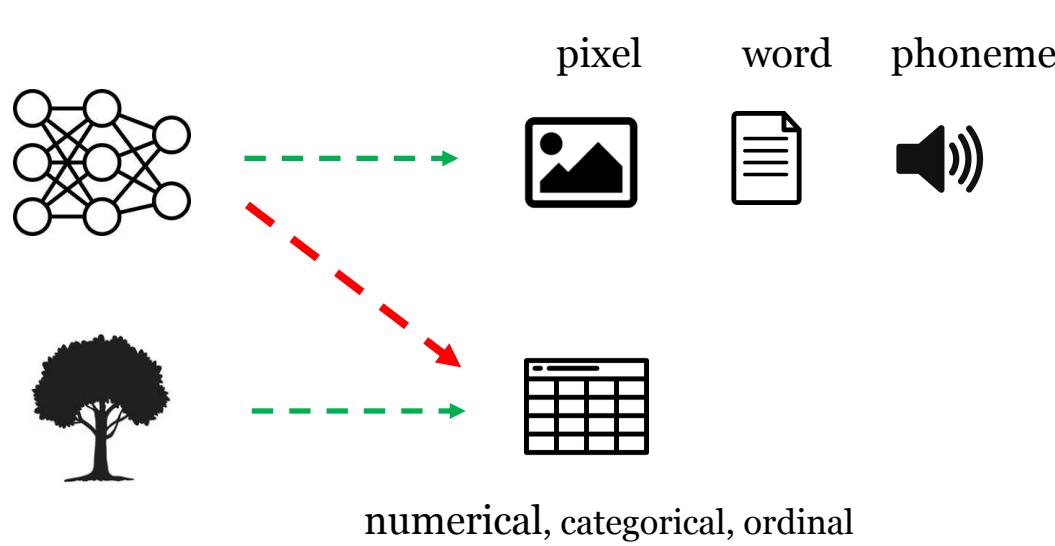
# Tree-Regularized Tabular Embeddings



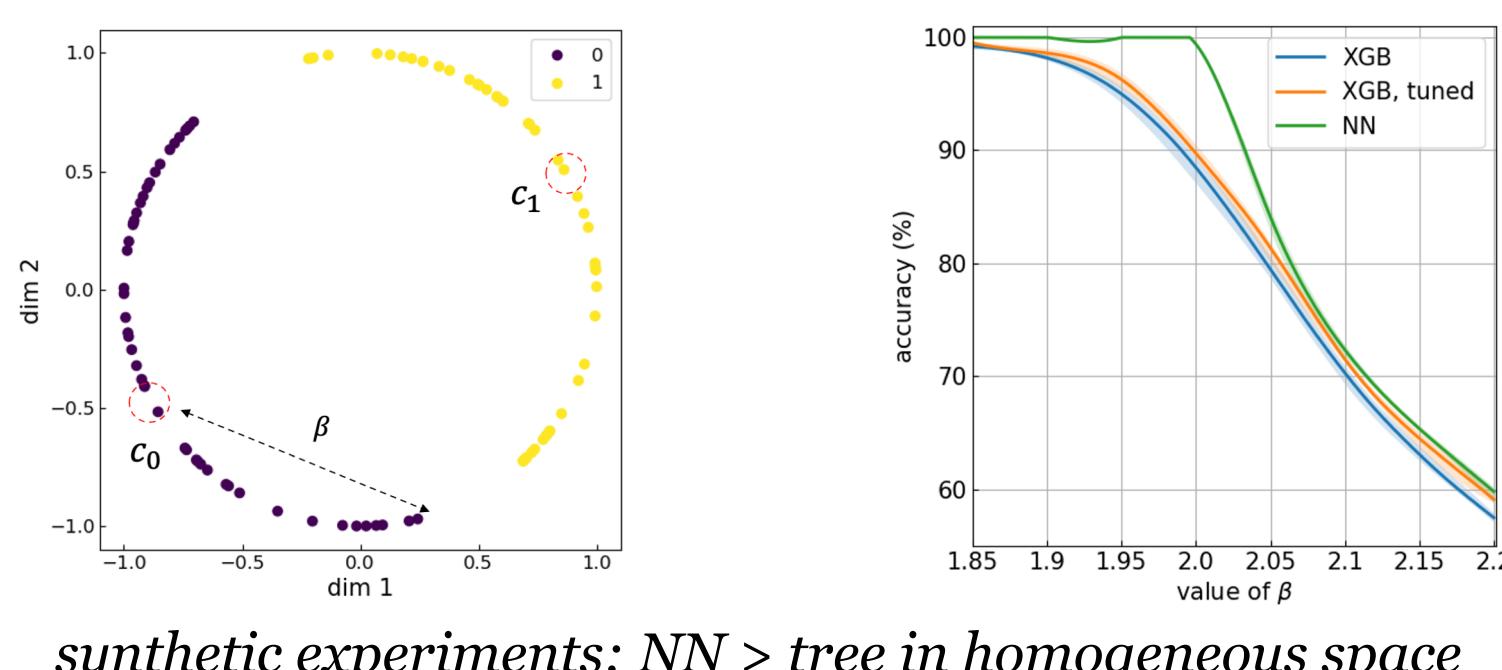
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## Data-Centric Tabular Learning

**Goal:** taper the performance gap between tree-based and NN models on tabular data.

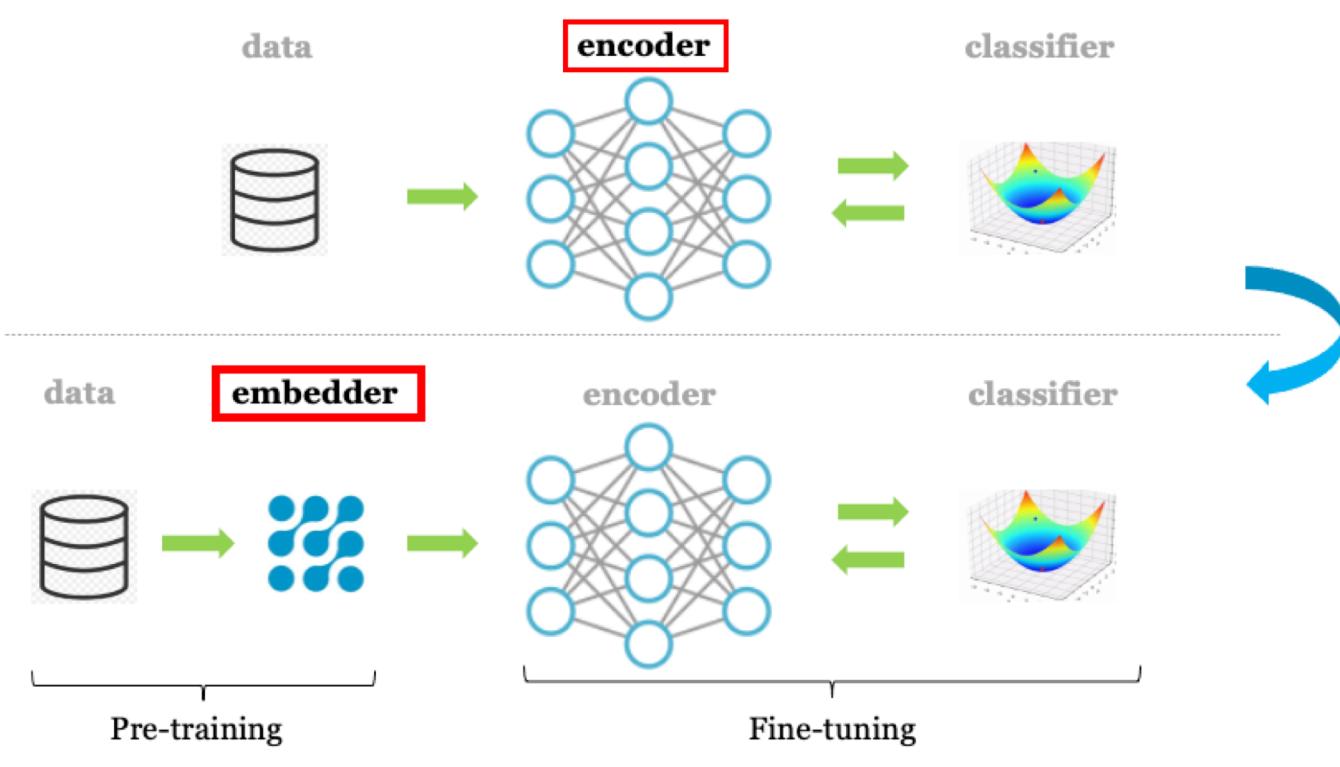


**Limitation:** tabular data are heterogeneous in nature, and an underemphasis on feature alignment could overshadow the efficacy of NN.



synthetic experiments: NN > tree in homogeneous space

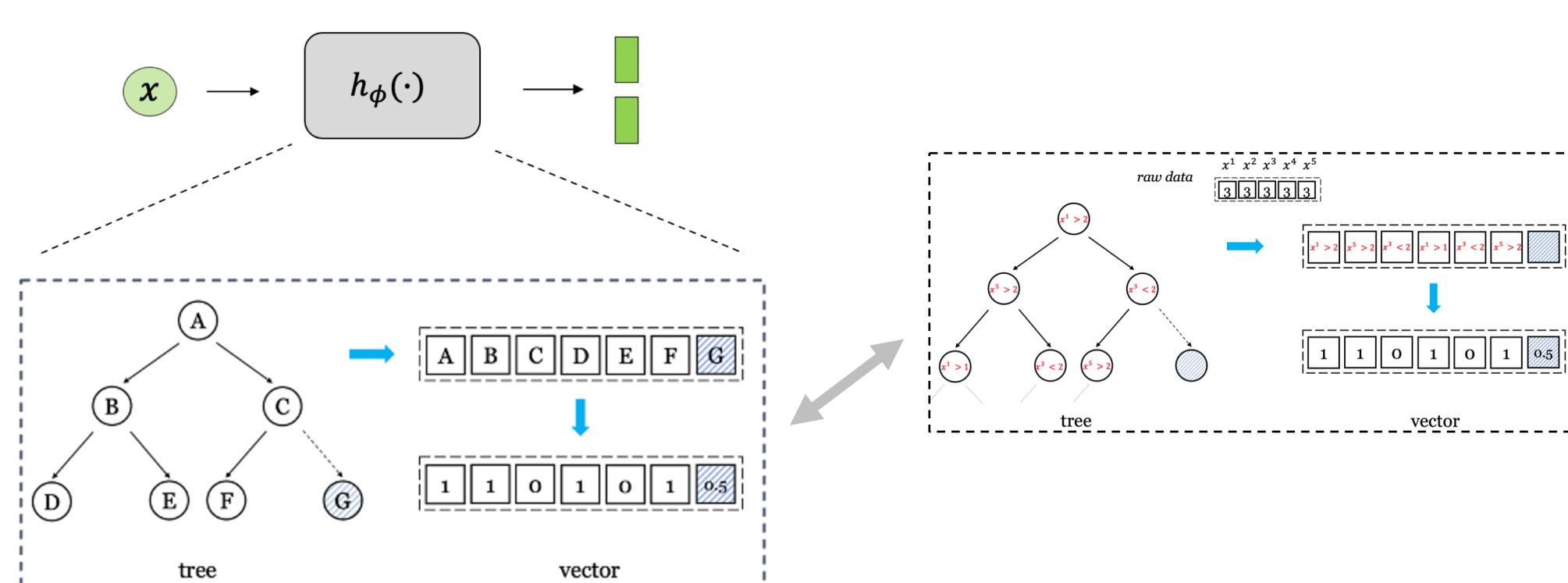
**Proposal:** calibrate tabular data to fit NN from a data-centric perspective.



## In-Batch Tree-Regularized Embeddings

### Overview:

- binarize representations through pairwise comparison between variable values and thresholds in tree nodes.
- reformulated as a single vector (T2V) [1] or an array of tokens (T2T) for MLP and transformer blocks.



T2T tokens: generated through level-order traversal with padding

**Implementation:** in-batch transformation, supporting industrial use cases with hundreds of columns and millions of rows.

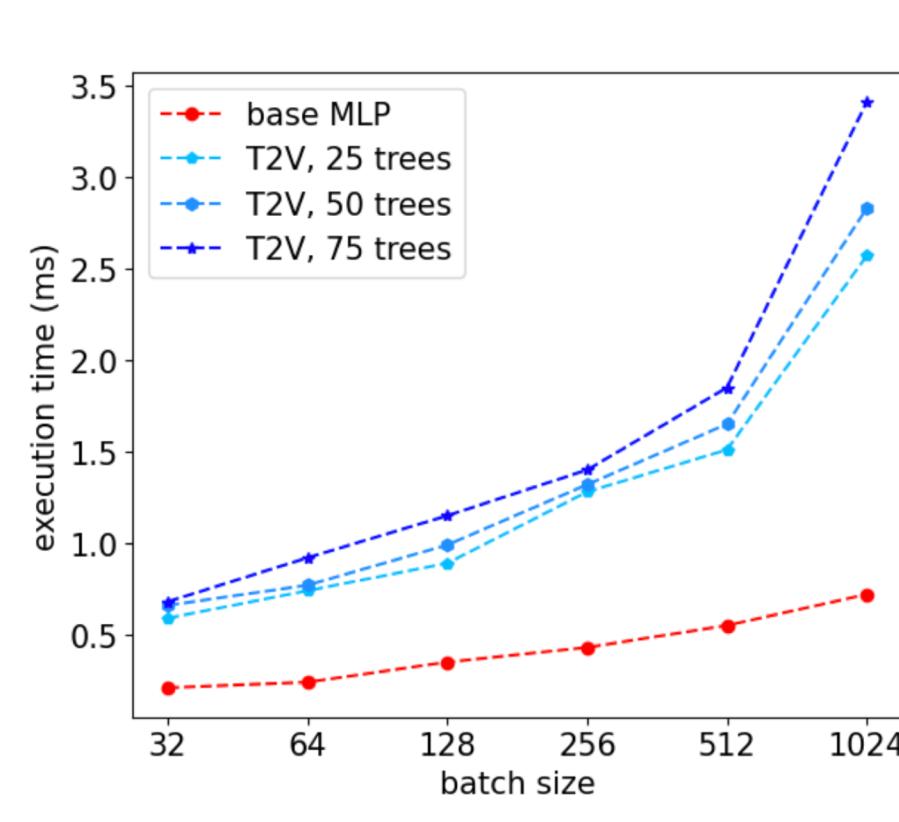
```
class TreeToVectorSimple:
    def __init__(self, xgbTree, dtype=torch.float, device='cpu'):
        self.xgbTree = xgbTree
        self.dtype = dtype
        self.device = device

    def __call__(self, tensor):
        output = self.tree_encoder(tensor)
        return output

    def tree_encoder(self, tensor):
        # fill nan with -1
        tensor = torch.nan_to_num(tensor, nan=-1.0)
        output = self.preprocessing(
            tensor,
            self.xgbTree.multiply_matrix,
            self.xgbTree.offset_vector)
        return output

    def postprocessing(self, x, multiply_matrix, offset_vector):
        x = torch.matmul(x, multiply_matrix.to(self.device))
        x -= offset_vector.to(self.device)
        x[x > 0] = 1.0
        x[x < 0] = 0.0
        return x

transform_batch = transforms.Compose([TreeToVectorSimple(xgbTree)])
# within each batch
X_train_batch = transform_batch(X_train_batch)
```



left: pseudocode of in-batch transformation with matrix manipulation  
right: time complexity between T2V and vanilla features with MLP

## Evaluations

Experiment results on 91 OpenML benchmark datasets [2] with binary classification task. Reported in percentaged AUC.

### Robustness

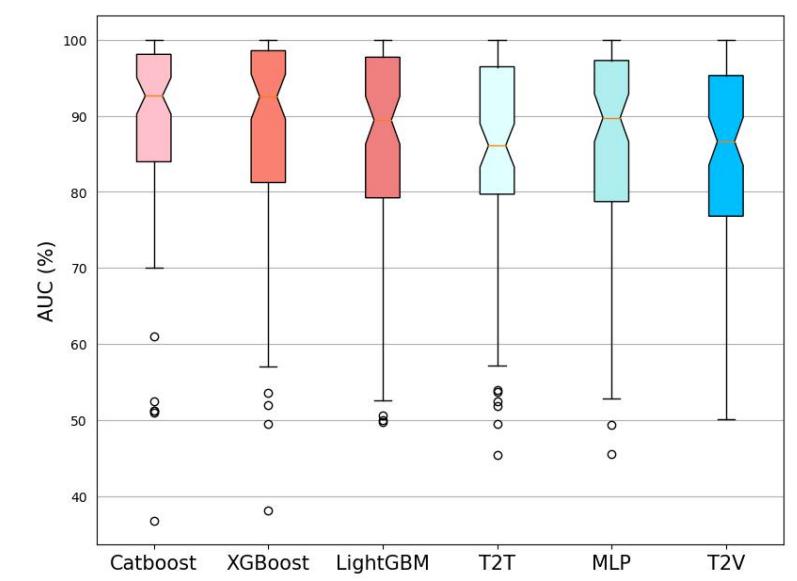
CatBoost	XGBoost	LightGBM	T2V	T2T	MLP	SAINT	ResNet
91	91	91	88	88	88	59	73

# datasets can be evaluated

### Comparison w.r.t. tree-based models

Algorithm	Rank ↓			AUC (%) ↑	
	min	max	mean	median	mean
CatBoost	1	6	2.38	2	88.06
XGBoost	1	6	2.83	2	87.70
LightGBM	1	6	3.16	3	86.37
T2T	1	6	4.07	4	84.63
MLP	1	6	4.22	4	84.42
T2V	1	6	4.45	5	83.15

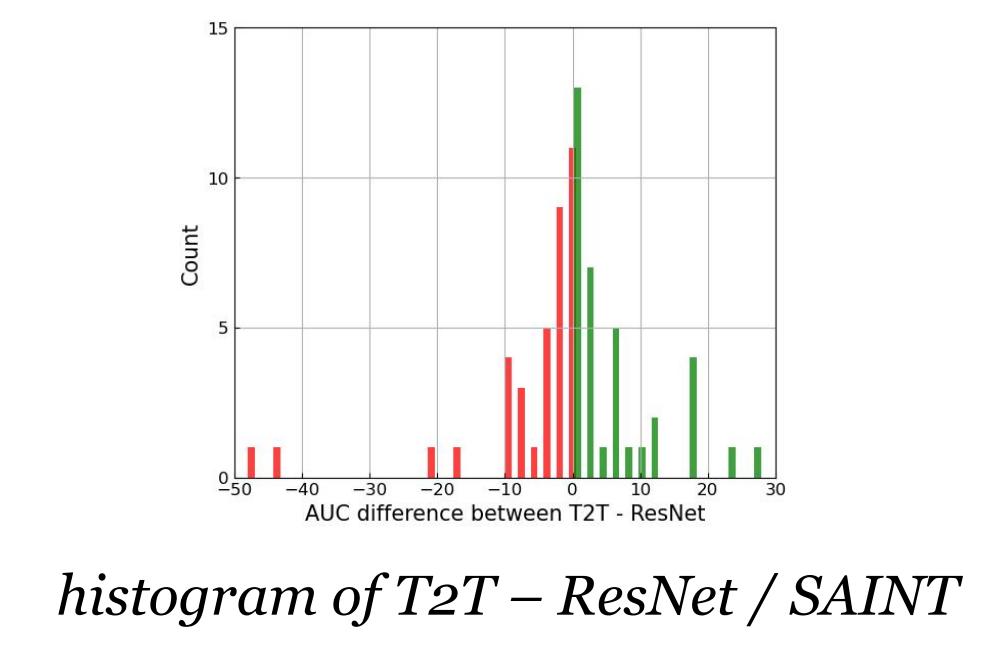
ranked by average AUC



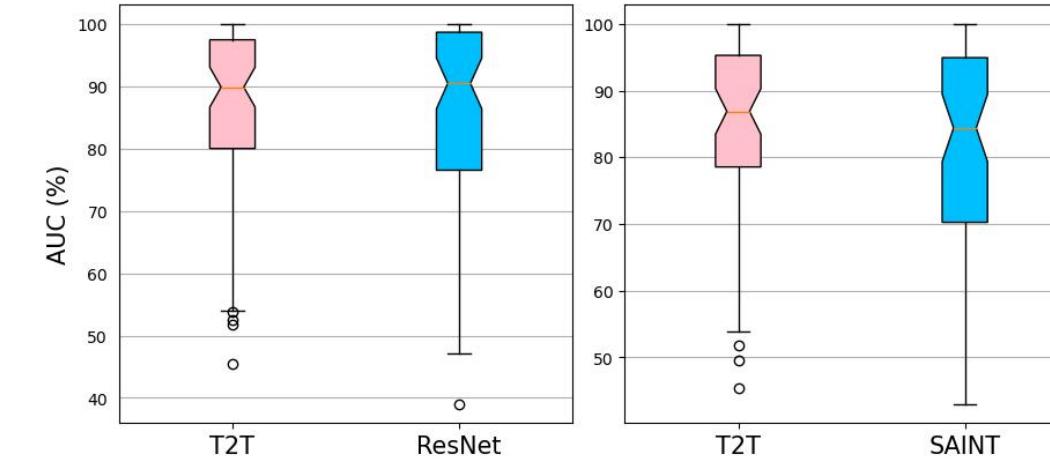
distribution of AUC

### Comparison w.r.t. NN models

Algorithm	Rank ↓			AUC (%) ↑	
	min	max	mean	median	mean
ResNet	1	4	2.15	2	84.87
T2T	1	4	2.29	2	84.72
T2V	1	4	2.61	3	83.92
SAINT	1	4	3.01	3	81.46



histogram of T2T - ResNet / SAINT



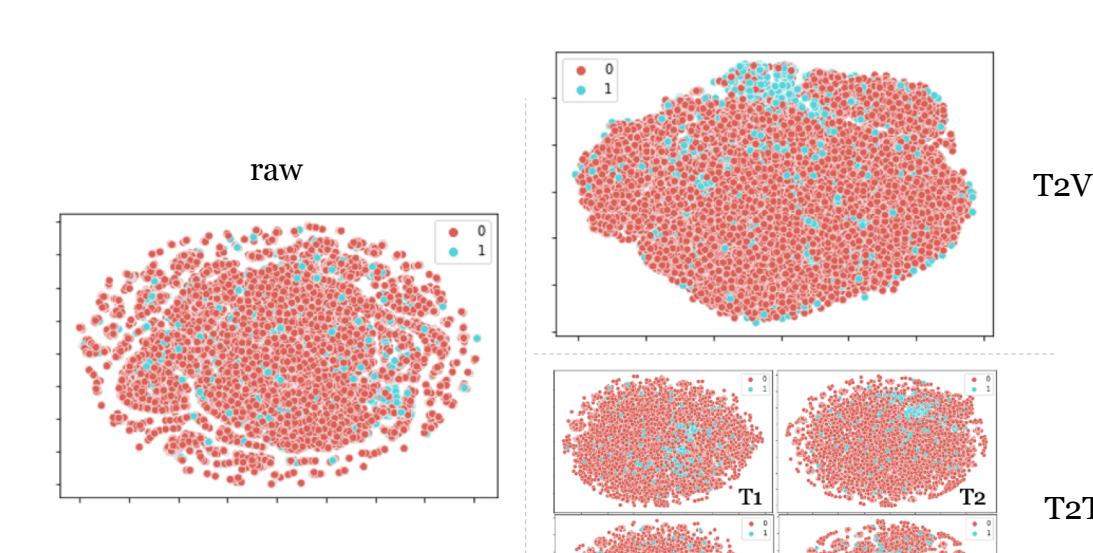
## Main Takeaways

1. Implemented scalable algorithms to obtain tree-regularized embeddings T2V and T2T. The latter is more performant and can serve as tabular tokenizer for multimodal learning with transformer-based framework.
2. Although not reported in the paper, T2V with 4-layered transformer scales and outperforms tree-based models on production binary classification tasks. Interestingly, similar results are also observed in [3].
3. Future works: generalize to regression and multi-class classification tasks; explore consistent encoding of numerical and categorical features; call for industrial-scale benchmark datasets.

## Appendix

```
Algorithm 1: Tree to Vector (T2V)
Input: xgb_trees, ε
Output: emb_vec
Init: emb_map = {}
for tree ∈ xgb_trees do
    for node ∈ tree do
        var_key = node;
        var_val.round(ε);
        if {var_key, var_val} ∈ emb_map then
            emb_map[var_key].append(var_val);
        end
    end
end

Algorithm 2: Tree to Tokens (T2T)
Input: xgb_trees, τ, η
Output: emb_vec
Init: vec_len, emb_vec = []
for tree ∈ xgb_trees do
    l = tree.count_node();
    vec_len = max(vec_len, l)
end
for tree ∈ xgb_trees do
    vec = tree.to_vec(τ);
    vec.pad(vec_len, η);
    emb_vec.append(vec);
end
```



left: pseudocode of T2V and T2T algorithm  
right: t-SNE plot of raw, T2V and T2T embedding on internal dataset

## References

- [1] Vadim Borisov et al. "DeepTLF: robust deep neural networks for heterogeneous tabular data"
- [2] Duncan McElfresh et al. "When Do Neural Nets Outperform Boosted Trees on Tabular Data?"
- [3] Hu, X., et al. "Deepeta: How uber predicts arrival times using deep learning."