

Subject Name Solutions

4300005 – Summer 2023

Semester 1 Study Material

Detailed Solutions and Explanations

Question 1(a) [3 marks]

Write base units with their symbols in SI.

Solution

Physical Quantity	Base Unit	Symbol
Length	meter	m
Mass	kilogram	kg
Time	second	s
Electric current	ampere	A
Temperature	kelvin	K
Amount of substance	mole	mol
Luminous intensity	candela	cd

Mnemonic

“Learn Measurements Through Accurate Techniques Like Modern Scientists”

Question 1(b) [4 marks]

Explain construction and working of a vernier caliper. Explain its least count and zero error.

Solution

Construction of Vernier Caliper:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Main Scale] --- B[Fixed Jaw]
    A --- C[Vernier Scale]
    C --- D[Movable Jaw]
    C --- E[Depth Rod]
    A --- F[Locking Screw]
{Highlighting}
{Shaded}
```

- **Main scale:** Fixed scale with millimeter divisions
- **Vernier scale:** Sliding scale with divisions slightly smaller than main scale
- **Fixed jaw:** Connected to main scale
- **Movable jaw:** Attached to vernier scale
- **Depth rod:** For measuring depths
- **Locking screw:** To fix position during measurement

Working: Object is placed between jaws, movable jaw is adjusted to hold object firmly. Reading is taken by noting main scale reading and adding vernier coincidence value.

Least Count: Smallest measurement possible with vernier caliper. $LC = 1 \text{ division on main scale} \div \text{Number of divisions on vernier scale}$

Zero Error: Error when caliper shows non-zero reading with jaws closed.

- **Positive error:** Subtract from reading
- **Negative error:** Add to reading

Mnemonic

“Very Careful Measurements Leave Count Errors Zero”

Question 1(c)(i) [4 marks]

Distinguish between accuracy and precision.

Solution

Accuracy	Precision
Closeness of measurement to true value	Repeatability of measurement
Affected by systematic errors	Affected by random errors
Represented by mean of measurements	Represented by standard deviation
Improved by calibration	Improved by using better instruments
Example: If true value is 10 cm, measurements of 9.9, 10.1, and 10.0 cm are accurate	Example: Measurements of 9.8, 9.8, 9.8 cm are precise but not accurate if true value is 10 cm

Mnemonic

“Accurate measurements Are Always At true value, Precise measurements Produce Perfect repeatability”

Question 1(c)(ii) [2 marks]

Pitch of a micrometer screw gauge is 0.5 mm and there are 50 divisions on its circular scale. Find its least count.

Solution

Formula: Least Count = Pitch \div Number of divisions on circular scale

Calculation: LC = 0.5 mm \div 50 = 0.01 mm

Least Count of micrometer screw gauge = 0.01 mm

Question 1(c)(iii) [1 mark]

What is SI unit of heat?

Solution

SI unit of heat is **Joule (J)**

Question 1(c)(i) [4 marks] (OR)

How are absolute and relative errors calculated?

Solution

Absolute Error (Δa): Difference between measured value and true value

- For multiple measurements, it's difference between measured value and mean value

Calculation of Absolute Error:

- Single measurement:** $\Delta a = |\text{Measured value} - \text{True value}|$
- Multiple measurements:**
 - Calculate mean (a_m)
 - For each measurement: $\Delta a_i = |a_i - a_m|$
 - Mean absolute error: $\Delta a = (\Delta a_1 + \Delta a_2 + \dots + \Delta a_n) \div n$

Relative Error (r): Ratio of absolute error to true value

- $r = \text{Absolute error} \div \text{True value} = \Delta a \div \text{True value}$

Percentage Error (p): Relative error expressed as percentage

- $p = \text{Relative error} \times 100 = (\Delta a \div \text{True value}) \times 100\%$

Mnemonic

“Absolute Always measures Actual deviation; Relative References the total value”

Question 1(c)(ii) [2 marks] (OR)

Main scale of a vernier caliper is calibrated in mm and there are 50 divisions on its vernier scale. Find its least count.

Solution

Formula: Least Count = 1 division on main scale \div Number of divisions on vernier scale

Calculation: 1 division on main scale = 1 mm LC = 1 mm \div 50 = 0.02 mm

Least Count of vernier caliper = 0.02 mm

Question 1(c)(iii) [1 mark] (OR)

In which of the mode of heat transfer, medium is not required?

Solution

Radiation does not require a medium for heat transfer.

Question 2(a) [3 marks]

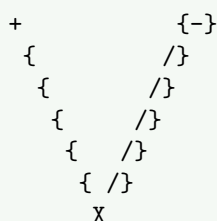
Write characteristics of electric field lines.

Solution

Characteristics of Electric Field Lines:

1. Electric field lines start from positive charge and end on negative charge
2. Field lines never cross each other
3. Field lines are always perpendicular to the surface of conductor
4. Number of field lines is proportional to magnitude of charge
5. Closer field lines indicate stronger electric field
6. Field lines are continuous curves
7. Field lines contract longitudinally and expand laterally

Diagram:



Mnemonic

“Electric Field Lines: Start Positive, End Negative, Cross Never”

Question 2(b) [4 marks]

Explain Coulomb’s inverse square law for electrostatic forces.

Solution

Coulomb's Inverse Square Law: The electrostatic force between two point charges is directly proportional to the product of magnitudes of charges and inversely proportional to the square of distance between them.

Mathematical Form: $F = k(q_1 q_2)/r^2$

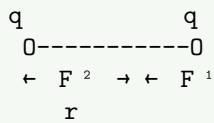
Where:

- F = electrostatic force (in Newtons)
- k = electrostatic constant ($9 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$)
- q_1, q_2 = magnitudes of charges (in Coulombs)
- r = distance between charges (in meters)

Properties:

- **Vector Quantity:** Force acts along the line joining the two charges
- **Attractive/Repulsive:** Like charges repel, unlike charges attract
- **Central Force:** Follows Newton's third law
- **Medium Dependence:** Depends on the medium between charges (k changes)

Diagram:



Mnemonic

“Charges Attract/Repel Leveraging Distance Squared”

Question 2(c)(i) [4 marks]

Derive formula for equivalent capacitance of capacitors connected in series and parallel combination.

Solution

For Series Combination:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A["{+}"] --- B["{C}"]
    B --- C["{C}"]
    C --- D["{C}"]
    D --- E["{-}"]
{Highlighting}
{Shaded}
```

When capacitors are connected in series:

- Same charge Q appears on each capacitor
- Potential difference distributes across capacitors
- $V = V_1 + V_2 + V_3$

For each capacitor: $V_1 = Q/C_1, V_2 = Q/C_2, V_3 = Q/C_3$

Total voltage: $V = Q/C_1 + Q/C_2 + Q/C_3 = Q(1/C_1 + 1/C_2 + 1/C_3)$

For equivalent capacitance: $V = Q/C_{eq}$

Therefore: $1/C_{eq} = 1/C_1 + 1/C_2 + 1/C_3$

For Parallel Combination:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A["{+}"] --- B["{C}"]
    A --- C["{C}"]
    A --- D["{C}"]
{Highlighting}
{Shaded}
```

B $\{-\{-\}\{-\}\ E["\{\}\{-\}"]\}$
 C $\{-\{-\}\{-\}\ E\}$
 D $\{-\{-\}\{-\}\ E\}$
 {Highlighting}
 {Shaded}

When capacitors are connected in parallel:

- Same potential difference V across each capacitor
- Total charge distributes among capacitors
- $Q = Q + Q + Q$

For each capacitor: $Q = C V$, $Q = C V$, $Q = C V$

Total charge: $Q = C V + C V + C V = (C + C + C) V$

For equivalent capacitance: $Q = C_{eq} V$

Therefore: $C_{eq} = C + C + C$

Mnemonic

“Series Sums Reciprocals, Parallel Puts Capacitance Together”

Question 2(c)(ii) [2 marks]

Two capacitors of capacitances 8 F and 9 F are connected in parallel combination. Find equivalent capacitance.

Solution

Formula for parallel combination: $C_{eq} = C + C$

Given:

- $C = 8\text{ F}$
- $C = 9\text{ F}$

Calculation: $C_{eq} = 8\text{ F} + 9\text{ F} = 17\text{ F}$

Therefore, equivalent capacitance = 17 F

Question 2(c)(iii) [1 mark]

Write full name of “LASER”.

Solution

LASER: Light Amplification by Stimulated Emission of Radiation

Question 2(a) [3 marks] (OR)

What is a capacitor? Define capacitance and write its unit.

Solution

Capacitor: A device that stores electric charge and electrical energy in the form of electric field.

Capacitance: The ability of a capacitor to store electric charge. It is defined as the ratio of charge stored to the potential difference applied.

Mathematical Form: $C = Q/V$

Where:

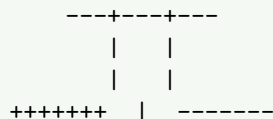
- C = capacitance
- Q = charge stored on capacitor
- V = potential difference across capacitor

Unit of Capacitance: Farad (F)

Diagram:

```

+++++++ | -----
        | |
        | |
  
```



Mnemonic

“Capacitors Collect Charge, Volts Vary Fastidiously”

Question 2(b) [4 marks] (OR)

Explain intensity of electric field and electric potential.

Solution

Electric Field Intensity:

- **Definition:** Force experienced by unit positive charge placed at that point
- **Formula:** $E = F/q$
- **Unit:** Newton/Coulomb (N/C) or Volt/meter (V/m)
- **Vector Quantity:** Has both magnitude and direction
- **Direction:** Same as force on positive charge

Electric Potential:

- **Definition:** Work done to bring unit positive charge from infinity to that point
- **Formula:** $V = W/q$
- **Unit:** Volt (V) or Joule/Coulomb (J/C)
- **Scalar Quantity:** Has only magnitude
- **Relation with field:** $E = -dV/dr$ (field is negative gradient of potential)

Comparison Table:

Property	Electric Field	Electric Potential
Definition	Force per unit charge	Work done per unit charge
Nature	Vector	Scalar
Unit	N/C or V/m	V or J/C
Dependence	Varies as $1/r^2$	Varies as $1/r$
Direction	Away from +ve charge	No direction

Mnemonic

“Electric Field Forces charges; Potential Provides energy”

Question 2(c)(i) [4 marks] (OR)

Using formula of capacitance of a parallel plate capacitor, explain effect of plate area, separation between plates and presence of dielectric material between the plates on its capacitance.

Solution

Formula for capacitance of parallel plate capacitor: $C = \frac{\epsilon_0 \epsilon_r A}{d}$

Where:

- C = capacitance
- ϵ_0 = permittivity of free space (8.85×10^{-12} F/m)
- ϵ_r = relative permittivity of dielectric
- A = area of overlap between plates
- d = distance between plates

Effect of Plate Area (A):

- Capacitance is directly proportional to area of plates
- Increasing area \rightarrow Increases capacitance
- Doubling area \rightarrow Doubles capacitance

Effect of Separation (d):

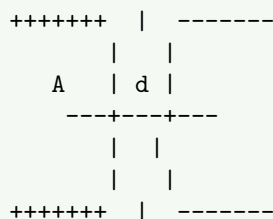
- Capacitance is inversely proportional to distance between plates

- Increasing separation → Decreases capacitance
- Doubling separation → Halves capacitance

Effect of Dielectric Material (ϵ_r):

- Capacitance is directly proportional to relative permittivity of dielectric
- Inserting dielectric → Increases capacitance
- Dielectric constant measures this increase: $C(\text{with dielectric}) = \epsilon_r \times C(\text{without dielectric})$

Diagram:



Mnemonic

“Area Amplifies, Distance Diminishes, Dielectrics Double”

Question 2(c)(ii) [2 marks] (OR)

Voltage between plates of a capacitor of capacitance 0.5 F is 150 V . Find magnitude of electric charge on plates.

Solution

Formula: $Q = CV$

Given:

- Capacitance (C) = $0.5 \text{ F} = 0.5 \times 10^{-6} \text{ F}$
- Voltage (V) = 150 V

Calculation: $Q = CV = 0.5 \times 10^{-6} \times 150 = 75 \times 10^{-6} \text{ C} = 75 \text{ } \mu\text{C}$

Therefore, charge on plates = **$75 \text{ } \mu\text{C}$**

Question 2(c)(iii) [1 mark] (OR)

Of the two parts of an optical fiber, the core and the cladding, which one has larger refractive index?

Solution

The **core** has a larger refractive index than the cladding.

Question 3(a) [3 marks]

Define conduction and convection of heat.

Solution

Heat Conduction:

- Transfer of heat through matter without actual movement of particles
- Occurs due to direct molecular collisions
- Heat flows from higher to lower temperature region
- Metals are good conductors of heat
- Examples: Heat transfer through metal rod, cooking pot

Heat Convection:

- Transfer of heat through actual movement of matter
- Occurs in fluids (liquids and gases)
- Involves formation of convection currents
- Examples: Room heater, sea breeze, boiling water

Diagram:

Conduction:
 Hot Cold
 |->->->->|

Convection:
 ↑
 ← →
 ↓
 Heat

Mnemonic

“Conduction Connects molecules; Convection Carries material”

Question 3(b) [4 marks]

Explain construction and working of mercury thermometer.

Solution

Construction of Mercury Thermometer:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Glass Bulb] --{-}{-} B[Capillary Tube]
    B --{-}{-} C[Scale]
    C --{-}{-} D[Protective Glass Cover]
{Highlighting}
{Shaded}
```

- **Glass bulb:** Contains mercury, acts as reservoir
- **Capillary tube:** Thin glass tube connected to bulb
- **Scale:** Calibrated with temperature markings
- **Protective glass cover:** Protects capillary tube and scale

Working Principle:

1. Based on thermal expansion of mercury
2. When temperature increases, mercury expands and rises in capillary
3. When temperature decreases, mercury contracts and level falls
4. Temperature is read from scale at mercury level

Temperature Range: -38.83°C to 356.73°C (mercury's freezing to boiling point)

Advantages:

- High accuracy
- Linear expansion
- Clearly visible in capillary

Limitations:

- Cannot measure very low temperatures
- Mercury is toxic
- Cannot be used for remote sensing

Mnemonic

“Mercury Moves Through Capillary, Showing Temperature”

Question 3(c)(i) [4 marks]

State laws of thermal conductivity and derive formula of coefficient of thermal conductivity.

Solution

Laws of Thermal Conductivity:

1. Heat flow is directly proportional to temperature difference (ΔT)
2. Heat flow is directly proportional to cross-sectional area (A)
3. Heat flow is inversely proportional to length (L)
4. Heat flow is directly proportional to time (t)

Derivation of Coefficient of Thermal Conductivity:

According to Fourier's law: $Q = A \times t \times \Delta T / L$

Converting to equation with proportionality constant K: $Q = K \times A \times t \times \Delta T / L$

Rearranging: $K = (Q \times L) / (A \times t \times \Delta T)$

Where:

- Q = Heat conducted (in Joules)
- L = Length of conductor (in meters)
- A = Cross-sectional area (in m^2)
- t = Time (in seconds)
- ΔT = Temperature difference (in Kelvin)
- K = Coefficient of thermal conductivity (in $W/m \cdot K$)

Diagram:

Hot Cold
T -----T
Length L
Area A
Heat Q

Mnemonic

“Heat Transfers Faster when Area Larger, Temperature higher, Length shorter”

Question 3(c)(ii) [2 marks]

The total area of glass window pane is $0.5m^2$. Calculate amount of heat conducted per hour through the pane if thickness of glass is $0.6cm$, the inside temperature is $30^\circ C$ and outside temperature is $20^\circ C$. Coefficient of thermal conductivity of glass is $1.0 Wm^{-1}K^{-1}$.

Solution

Formula: $Q = (K \times A \times t \times \Delta T) / L$

Given:

- Area (A) = $0.5 m^2$
- Thickness (L) = $0.6 cm = 0.006 m$
- Inside temperature (T) = $30^\circ C$
- Outside temperature (T) = $20^\circ C$
- Temperature difference (ΔT) = $10^\circ C = 10 K$
- Coefficient of thermal conductivity (K) = $1.0 W/m \cdot K$
- Time (t) = 1 hour = 3600 seconds

Calculation: $Q = (1.0 \times 0.5 \times 3600 \times 10) / 0.006$ $Q = (18000) / 0.006$ $Q = 3,000,000 J = 3000 kJ$

Therefore, heat conducted = 3000 kJ per hour

Question 3(c)(iii) [1 mark]

Which property of light is responsible for transmission of light through optical fibre?

Solution

Total Internal Reflection (TIR) is responsible for transmission of light through optical fiber.

Question 3(a) [3 marks] (OR)

Define heat capacity and specific heat.

Solution

Heat Capacity:

- Amount of heat energy required to raise temperature of an object by 1°C or 1K
- Depends on mass and material of object
- Formula: $C = Q/\Delta T$
- Unit: Joule/Kelvin (J/K)

Specific Heat:

- Amount of heat energy required to raise temperature of 1 kg of substance by 1°C or 1K
- Property of material, independent of mass
- Formula: $c = Q/(m \times \Delta T)$
- Unit: Joule/kg \cdot K ($\text{J/kg} \cdot \text{K}$)

Relation: Heat capacity (C) = mass (m) \times specific heat (c)

Comparison Table:

Property	Heat Capacity	Specific Heat
Definition	Heat per degree for object	Heat per degree per unit mass
Symbol	C	c
Unit	J/K	$\text{J/kg} \cdot \text{K}$
Depends on	Mass and material	Only material
Formula	$Q/\Delta T$	$Q/(m \times \Delta T)$

Mnemonic

“Heat Capacity for Complete object, Specific heat for Single kilogram”

Question 3(b) [4 marks] (OR)

Explain construction and working of optical pyrometer.

Solution

Construction of Optical Pyrometer:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Telescope] --- B[Filament Lamp]
    B --- C[Ammeter]
    C --- D[Battery]
    D --- B
    A --- E[Color Filter]
    E --- F[Eyepiece]
{Highlighting}
{Shaded}
```

- **Telescope:** To view hot object
- **Filament lamp:** Calibrated tungsten filament
- **Rheostat:** To adjust current through filament
- **Ammeter:** To measure current
- **Red filter:** To match wavelengths
- **Eyepiece:** For viewing

Working Principle:

1. Based on comparing brightness of hot object with standard lamp filament
2. Object is viewed through telescope
3. Current adjusted until filament brightness matches object brightness
4. At match point, filament “disappears” against object background
5. Temperature determined from calibrated scale or ammeter reading

Temperature Range: 700°C to 3000°C

Advantages:

- Non-contact measurement
- High temperature measurement
- Suitable for moving objects

Mnemonic

“Pyrometer Produces Perfect Temperature by Brightness Comparison”

Question 3(c)(i) [4 marks] (OR)

Define linear thermal expansion of solids and derive formula of coefficient linear thermal expansion.

Solution

Linear Thermal Expansion: Increase in length of a solid material when its temperature increases

Coefficient of Linear Thermal Expansion (α): Fractional change in length per unit change in temperature

Derivation:

For small temperature changes:

- Change in length (ΔL) is directly proportional to original length (L)
- ΔL is directly proportional to change in temperature (ΔT)

Therefore: $\Delta L \propto L \times \Delta T$

Converting to equation with proportionality constant : $\Delta L = \alpha \times L \times \Delta T$

Rearranging: $\alpha = \Delta L / (L \times \Delta T)$

Where:

- ΔL = Change in length (in meters)
- L = Original length (in meters)
- ΔT = Change in temperature (in Kelvin or Celsius)
- α = Coefficient of linear thermal expansion (per $^{\circ}\text{C}$ or per K)

Final length: $L = L (1 + \alpha \Delta T)$

Diagram:

Before heating:

|----L----|

After heating:

|-----L-----|

Mnemonic

“Linear Expansion Numerically Gives Total Length Increase”

Question 3(c)(ii) [2 marks] (OR)

Length of a steel rod at 0°C is 150 cm. What will be its length at 200°C , if its coefficient of linear thermal expansion is 12×10^{-6} per $^{\circ}\text{C}$.

Solution

Formula: $L = L (1 + \alpha \Delta T)$

Given:

- Original length (L) = 150 cm
- Original temperature = 0°C
- Final temperature = 200°C
- Temperature change (ΔT) = 200°C
- Coefficient of linear expansion (α) = 12×10^{-6} per $^{\circ}\text{C}$

Calculation: $L = 150(1 + 12 \times 10^{-6} \times 200)$ $L = 150(1 + 24 \times 10^{-6})$ $L = 150(1 + 0.0024)$ $L = 150 \times 1.0024$

$L = 150.36$ cm

Therefore, final length of steel rod = 150.36 cm

Question 3(c)(iii) [1 mark] (OR)

Which type of emission of radiation is responsible for emission of ordinary light?

Solution

Spontaneous emission is responsible for emission of ordinary light.

Question 4(a) [3 marks]

Define amplitude, frequency and time period of a wave.

Solution

Amplitude:

- Maximum displacement of medium particles from equilibrium position
- Represents energy of wave
- Denoted by 'A'
- Measured in meters (m)

Frequency:

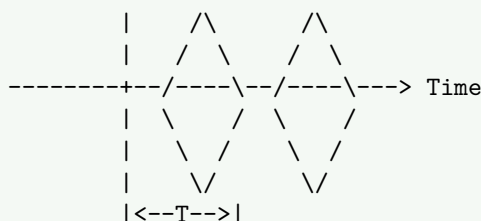
- Number of complete oscillations per unit time
- Denoted by 'f' or ' ν '
- Measured in hertz (Hz) or cycles per second
- Related to wavelength (λ) and velocity (v): $f = v/\lambda$

Time Period:

- Time taken to complete one oscillation
- Denoted by 'T'
- Measured in seconds (s)
- Related to frequency: $T = 1/f$

Diagram:

Amplitude



Mnemonic

“Amplitude Adjusts energy, Frequency Finds cycles, Time-period Tracks one cycle”

Question 4(b) [4 marks]

Write difference between transverse and longitudinal waves.

Solution

Property	Transverse Waves	Longitudinal Waves
Direction of particle motion	Perpendicular to wave propagation	Parallel to wave propagation
Formation of	Crests and troughs	Compressions and rarefactions
Examples	Light waves, water waves, electromagnetic waves	Sound waves, seismic P-waves
Medium requirement	Can travel through vacuum (e.g., light)	Requires material medium
Polarization	Can be polarized	Cannot be polarized
Speed	Generally faster in solids	Generally slower in solids

Mathematical representation

$$y = A \sin(kx - t)$$

$$s = A \sin(kx - t)$$

Diagram:

Transverse:



Direction of propagation

Longitudinal:



Direction of propagation

Mnemonic

“Transverse Travels perpendicular, Longitudinal Lies along length”

Question 4(c)(i) [5 marks]

How is ultrasonic wave produced using piezoelectric method?

Solution

Piezoelectric Method for Ultrasonic Wave Production:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Oscillator] --> B[Amplifier]
    B --> C[Piezoelectric Crystal]
    C --> D[Ultrasonic Waves]
{Highlighting}
{Shaded}
```

Working Principle:

1. Based on piezoelectric effect - generating electric charge in response to mechanical stress and vice versa
2. High-frequency AC voltage applied across piezoelectric crystal (quartz, tourmaline, Rochelle salt)
3. Crystal vibrates at same frequency as applied voltage
4. When frequency matches natural frequency of crystal, resonance occurs
5. Maximum amplitude vibrations generate ultrasonic waves

Components:

- **Oscillator:** Generates high-frequency electrical oscillations
- **Amplifier:** Increases amplitude of oscillations
- **Piezoelectric crystal:** Converts electrical energy to mechanical vibrations
- **Mounting:** Supports crystal properly

Frequency Range: 20 kHz to several MHz

Advantages:

- High efficiency
- Precise frequency control
- Compact size
- No moving parts

Mnemonic

“Piezo Produces waves when Properly Pulsed with electricity”

Question 4(c)(ii) [2 marks]

Explain any two properties of sound wave.

Solution

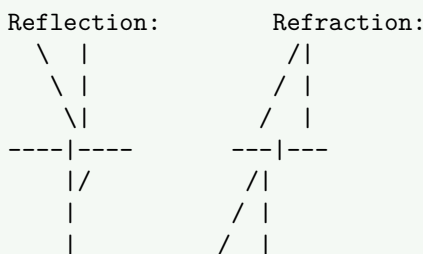
1. Reflection of Sound:

- Sound waves bounce back from obstacles
- Follows law of reflection: angle of incidence = angle of reflection
- Creates echo when reflected from distant objects
- Applications: Sonar, echo location, acoustic design

2. Refraction of Sound:

- Bending of sound waves when passing from one medium to another
- Caused by change in speed of sound in different media
- Examples: Sound focusing in domes, sound heard better at night
- Applications: Acoustic lenses, medical ultrasound

Diagram:



Mnemonic

“Sound Shows Remarkable Refractions During travel”

Question 4(a) [3 marks] (OR)

Define wavelength, phase and velocity of a wave.

Solution

Wavelength:

- Distance between two consecutive points in phase
- Distance traveled during one complete oscillation
- Denoted by ' λ ' (lambda)
- Measured in meters (m)
- Related to frequency (f) and velocity (v): $\lambda = v/f$

Phase:

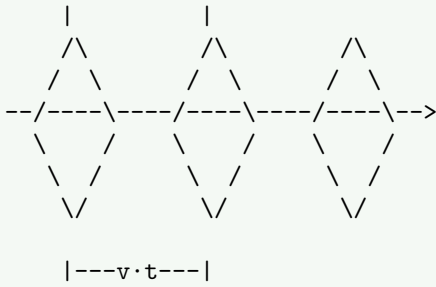
- State of oscillation at a specific point and time
- Measured in radians or degrees
- Full cycle = 2π radians or 360°
- Points having same phase are in phase
- Points differing by π radians (180°) are in opposite phase

Velocity:

- Rate at which wave propagates through medium
- Denoted by ' v '
- Measured in meters per second (m/s)
- Related to wavelength and frequency: $v = \lambda f$
- Depends on properties of medium, not on wave characteristics

Diagram for wavelength, phase and velocity:

|<--- --->|



Mnemonic

“Wavelength Wraps one cycle, Phase Portrays position, Velocity Values propagation speed”

Question 4(b) [4 marks] (OR)

Explain constructive and destructive interference of waves.

Solution

Interference: Superposition of two or more waves at same point in space resulting in a new wave pattern

Constructive Interference:

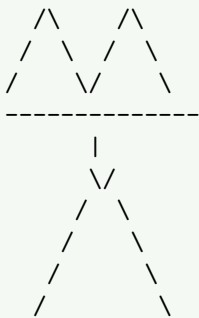
- Occurs when waves meet in phase (crest meets crest)
- Phase difference = $0, 2, 4, \dots$ ($0^\circ, 360^\circ, 720^\circ, \dots$)
- Path difference = n ($n = 0, 1, 2, \dots$)
- Results in amplitude larger than individual waves
- Resultant amplitude = sum of individual amplitudes

Destructive Interference:

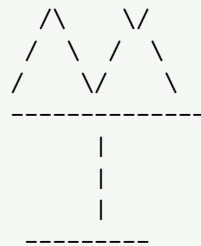
- Occurs when waves meet in opposite phase (crest meets trough)
- Phase difference = $\pi, 3\pi, 5\pi, \dots$ ($180^\circ, 540^\circ, 900^\circ, \dots$)
- Path difference = $(n+1/2)$ ($n = 0, 1, 2, \dots$)
- Results in amplitude smaller than individual waves
- Complete cancellation if amplitudes are equal

Diagram:

Constructive:



Destructive:



Mnemonic

“Constructive Creates Larger waves; Destructive Diminishes wave height”

Question 4(c)(i) [5 marks] (OR)

How is ultrasonic wave produced using magnetostriction method?

Solution

Magnetostriction Method for Ultrasonic Wave Production:

Mermaid Diagram (Code)

{Shaded}

```
{Highlighting}[]
graph LR
    A[Oscillator] --> B[Amplifier]
    B --> C[Coil around Ferromagnetic Rod]
    C --> D[Magnetostrictive Rod Vibrations]
    D --> E[Ultrasonic Waves]
{Highlighting}
{Shaded}
```

Working Principle:

1. Based on magnetostriction effect - dimensional change in ferromagnetic materials when placed in magnetic field
2. When magnetic field is applied, rod contracts
3. When field is removed, rod expands back to original size
4. Alternating current creates alternating magnetic field
5. Rod vibrates at frequency of applied current
6. These vibrations generate ultrasonic waves

Components:

- **Oscillator:** Generates high-frequency electrical oscillations
- **Amplifier:** Increases amplitude of oscillations
- **Coil:** Creates magnetic field when current passes
- **Ferromagnetic rod:** Nickel, iron-nickel alloy, or ferrites
- **Mounting:** Supports rod properly

Frequency Range: 20 kHz to 100 kHz (lower than piezoelectric method)

Advantages:

- Handles high power
- Suitable for high-intensity applications
- Rugged construction
- Works well at lower frequencies

Limitations:

- Limited to lower frequencies
- Lower efficiency than piezoelectric method
- Heating of rod at high frequencies

Mnemonic

“Magnetic Materials Move Minutely Making ultrasonic waves”

Question 4(c)(ii) [2 marks] (OR)

Explain any two properties of light wave.

Solution

1. Reflection of Light:

- Light bounces back when it strikes a surface
- Follows law of reflection: angle of incidence = angle of reflection
- Specular reflection from smooth surfaces
- Diffuse reflection from rough surfaces
- Applications: Mirrors, reflectors, optical instruments

2. Refraction of Light:

- Bending of light when passing from one medium to another
- Follows Snell's law: $n \sin(i) = n \sin(r)$
- Caused by change in speed of light in different media
- Examples: Bent appearance of stick in water
- Applications: Lenses, prisms, fiber optics

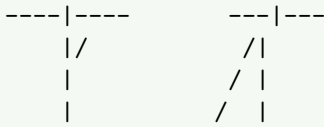
Diagram:

Reflection:

```
\ |
 \ |
  \|
```

Refraction:

```
/ |
 / |
 / |
```

Mnemonic

“Light Likes to Reflect from mirrors and Refract through media”

Question 5(a) [3 marks]

Write characteristics of LASER.

Solution

Characteristics of LASER:

Characteristic	Description
Monochromatic	Single wavelength/color (very narrow frequency range)
Coherent	All waves in same phase, creating high interference
Directional	Highly collimated, minimal divergence over long distances
High intensity	Concentrated energy in narrow beam
High purity	Extremely pure color compared to ordinary light

Diagram:

Ordinary Light:



Different wavelengths & directions

LASER:



Single wavelength, single direction

Mnemonic

“LASER Light: Monochromatic, Coherent, Directional, Intense”

Question 5(b) [4 marks]

Discuss importance of LASER in engineering and medical field.

Solution

Importance of LASER in Engineering:

1. Manufacturing:

- Precision cutting and welding of metals
- 3D printing and rapid prototyping
- Engraving and marking materials

2. Measurement and Testing:

- Distance measurement (LIDAR)
- Alignment and leveling
- Non-destructive testing
- Holography for stress analysis

3. Communications:

- Fiber optic communications
- Free-space optical communication
- Data storage (CD/DVD/Blu-ray)

4. Material Processing:

- Heat treatment
- Surface hardening
- Micromachining

Importance of LASER in Medical Field:

1. Surgery:

- Bloodless cutting (laser scalpel)
- Ophthalmic surgery (LASIK)
- Dermatological procedures
- Tumor removal

2. Diagnostics:

- Laser imaging
- Spectroscopy
- Flow cytometry
- Optical coherence tomography

3. Therapy:

- Photodynamic therapy for cancer
- Low-level laser therapy
- Pain management
- Cosmetic procedures (hair removal, skin rejuvenation)

4. Dentistry:

- Cavity detection
- Teeth whitening
- Gum surgery

Mnemonic

“LASER Enhances Manufacturing, Measures precisely, Communicates data, Heals patients”

Question 5(c)(i) [5 marks]

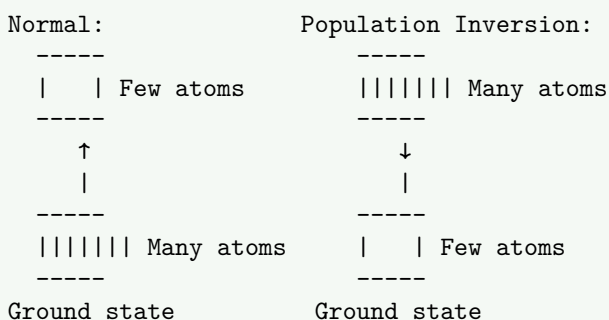
What is importance of population inversion and metastable state for production of LASER?

Solution

Population Inversion:

- **Definition:** State where more atoms are in excited state than in ground state (reverse of normal equilibrium)
- **Importance:**
 1. Essential condition for laser action to occur
 2. Creates environment for stimulated emission to dominate over absorption
 3. Enables amplification of light (negative absorption)
 4. Without it, emitted photons would be absorbed, preventing laser action
 5. Required for chain reaction of stimulated emission

Diagram:



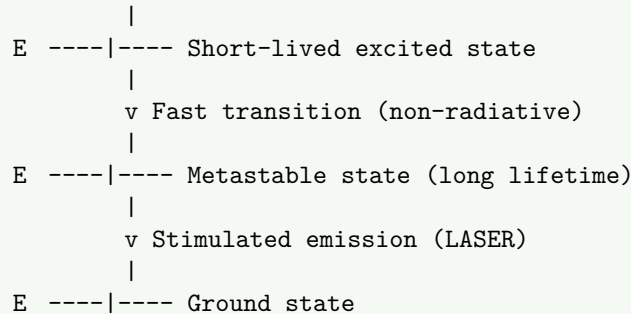
Metastable State:

- **Definition:** Excited energy state with relatively long lifetime (10^{-3} to 10^{-2} seconds)

- **Importance:**

1. Allows accumulation of excited atoms (temporary energy reservoir)
2. Provides time for population inversion to establish
3. Long lifetime prevents rapid spontaneous emission
4. Ensures stimulated emission dominates over spontaneous emission
5. Essential for continuous laser operation

Energy Level Diagram:



Mnemonic

“Population Inversion Makes Electrons Stay high; Metastable maintains this Situation Longer”

Question 5(c)(ii) [2 marks]

Explain graded index optical fibre.

Solution

Graded Index Optical Fiber:

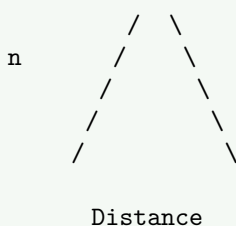
- **Structure:** Core with gradually decreasing refractive index from center to periphery
- **Refractive Index Profile:** Follows parabolic pattern: $n(r) = n(1 - r^2)$
- **Light Propagation:** Light travels in curved paths rather than zigzag pattern
- **Mechanism:** Light near periphery travels faster than at center, compensating for longer path
- **Advantages:**
 1. Reduced modal dispersion compared to step index fiber
 2. Higher bandwidth
 3. Less signal distortion
 4. Suitable for medium-distance communication

Cross-sectional Diagram:

Cladding

Core

Refractive Index Profile:



Mnemonic

“Graded Index Gradually Improves transmission by Smoothing dispersion”

Question 5(a) [3 marks] (OR)

Define refraction of light and write Snell’s law.

Solution

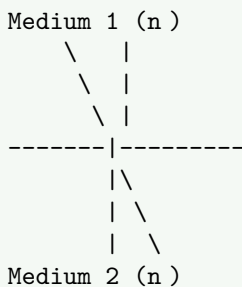
Refraction of Light:

- Bending of light when it passes from one transparent medium to another
- Occurs due to change in speed of light in different media
- Direction changes but frequency remains same
- Wavelength changes with speed

Snell’s Law:

- Mathematical relationship governing refraction
- States that ratio of sines of angles of incidence and refraction equals ratio of refractive indices
- Formula: $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$
- Where:
 - n_1 = Refractive index of first medium
 - n_2 = Refractive index of second medium
 - θ_1 = Angle of incidence
 - θ_2 = Angle of refraction

Diagram:



Mnemonic

“Sine ratios Equal Index ratios” or “ $n_1 \sin \theta_1 = n_2 \sin \theta_2$ ”

Question 5(b) [4 marks] (OR)

Discuss importance of optical fibre in engineering and medical field.

Solution

Importance of Optical Fiber in Engineering:

1. Communications:

- High-speed internet transmission
- Long-distance telecommunications
- Secure data transmission (difficult to tap)
- Higher bandwidth than copper cables

2. Sensors and Instrumentation:

- Temperature, pressure, strain measurement
- Structural health monitoring
- Chemical and biological sensing
- Seismic detection

3. Industrial Applications:

- Remote inspection of hazardous areas
- Industrial process control
- Power system monitoring
- Mining and petroleum exploration

4. Computing:

- High-speed data transfer between components
- Optical interconnects
- Quantum computing connections

Importance of Optical Fiber in Medical Field:

1. Diagnostics:

- Endoscopy for internal organ examination
- Laparoscopy for minimally invasive surgery
- Angioscopy for blood vessel examination
- Bronchoscopy for respiratory tract examination

2. Surgery:

- Laser light delivery for precise operations
- Photodynamic therapy
- Microsurgery guidance
- Remote surgery monitoring

3. Imaging:

- Optical coherence tomography
- Confocal microscopy
- Optogenetics
- Medical spectroscopy

4. Treatment:

- Phototherapy for skin conditions
- Laser treatment delivery
- Biosensing for real-time monitoring
- Targeted drug delivery

Mnemonic

“Optical Fibers Connect, Sense, Visualize, and Treat”

Question 5(c)(i) [5 marks] (OR)

Derive formula for numerical aperture and angle of acceptance of optical fibre.

Solution

Numerical Aperture (NA) Derivation:

Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Consider Critical Angle at Core-Cladding Interface] --> B[Apply Snell's Law]
    B --> C[Relate to Angle of Acceptance]
    C --> D[Derive NA Formula]
{Highlighting}
{Shaded}
```

Step 1: Consider critical angle (θ_c) at core-cladding interface

- At critical angle, refracted ray grazes along interface
- $\sin(\theta_c) = n_2 / n_1$ (where n_1 = core index, n_2 = cladding index)

Step 2: For a ray traveling in core, apply condition for total internal reflection

- Ray must strike at angle greater than critical angle
- Maximum angle in core: $90^\circ - \theta_c$

Step 3: For ray entering from air ($n = 1$), apply Snell's law

- $n \sin(\theta_a) = n_1 \sin(\theta_c)$
- $\sin(\theta_a) = n \sin(\theta_c)$
- Where θ_a is acceptance angle

Step 4: Use maximum value of θ_c ($90^\circ - \theta_c$)

- $\sin(\theta_a) = n \sin(90^\circ - \theta_c) = n \cos(\theta_c)$

Step 5: Substitute $\sin(\theta_c) = n_2 / n_1$

- $\cos(\theta_c) = \sqrt{1 - \sin^2(\theta_c)} = \sqrt{1 - (n_2/n_1)^2}$

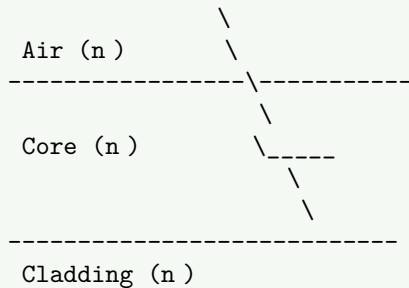
Step 6: Therefore:

- $\sin(\theta_c) = n_2 \sqrt{1 - (n_2/n_1)^2} = \sqrt{n_1^2 - n_2^2}$

Final Formula:

- Numerical Aperture (NA) = $\sin(\theta_c) = \sqrt{n_1^2 - n_2^2}$
- Where θ_c is angle of acceptance

Diagram:



Mnemonic

“NA Notes Acceptance angle; $\sqrt{n_1^2 - n_2^2}$ Shows maximum sine”

Question 5(c)(ii) [2 marks] (OR)

Explain step index optical fibre.

Solution

Step Index Optical Fiber:

- **Structure:** Core with uniform refractive index surrounded by cladding with lower uniform refractive index
- **Refractive Index Profile:** Sharp transition (step) between core and cladding
- **Light Propagation:** Light travels in zigzag path by total internal reflection
- **Types:**
 1. Single-mode: Small core (8-10 μm), carries one mode of light
 2. Multi-mode: Large core (50-100 μm), carries multiple modes

Characteristics:

- Simple construction
- Lower bandwidth than graded index
- Suffers from modal dispersion in multi-mode
- Longer path for some rays causes pulse spreading

Cross-sectional Diagram:

Cladding (n₂)

Core
(n₁)

Refractive Index Profile:

n

Distance

Mnemonic

“Step Index Shows Two distinct Indices with Perfect boundary”