

Subject Name Solutions

4300005 – Winter 2024

Semester 1 Study Material

Detailed Solutions and Explanations

Question 1(a) [3 marks]

Define accuracy and precision.

Solution

- **Accuracy:** Closeness of a measured value to the true value
- **Precision:** Consistency or repeatability of measurement values

Mnemonic

“Accuracy Aims at Truth, Precision Produces Repeatability”

Question 1(b) [4 marks]

Derive SI unit of work and Velocity using fundamental physical units.

Solution

Table 1: Derivation of Work and Velocity Units

| Physical Quantity | Formula | SI Unit Derivation | SI Unit |
|-------------------|------------------|--|-----------|
| Work (W) | $W = F \times d$ | $W = [\text{Force}]$ $\times [\text{Distance}] = [kgm/s^2]$ $\times [m] = [kgm^2/s^2]$ | Joule (J) |
| Velocity (v) | $v = d/t$ | $v = [\text{Distance}]/[\text{Time}] = [m]/[s]$ | m/s |

- **Work:** When a force ($kg \cdot m/s^2$) acts through a distance (m), we get $kg \cdot m^2/s^2 = \text{Joule}$
- **Velocity:** When an object covers distance (m) in time (s), we get m/s

Mnemonic

“Work Forces Distance, Velocity Distances Time”

Question 1(c) [7 marks]

What is Least Count of instrument. State equation of Least count of Vernier calipers. Explain measurement by vernier calipers with neat and clean diagram.

Solution

Least Count: Smallest measurement that can be directly measured using a measuring instrument.

Equation for Least Count of Vernier Caliper: Least Count = 1 Main Scale Division - 1 Vernier Scale Division or Least Count = Value of 1 MSD / Number of VSD

Diagram: Vernier Caliper

0 1 2 3 4 5 6 7 8 9 10

0 5 10 15 20 25 30 35 40 45

Vernier Scale

Measurement Process:

- **Step 1:** Close the jaws of caliper around the object
- **Step 2:** Note the main scale reading just before the zero of vernier scale
- **Step 3:** Find which vernier division exactly coincides with a main scale division
- **Step 4:** Add the vernier reading to the main scale reading: $\text{Total} = \text{MSR} + (\text{VC} \times \text{LC})$
- **Main Scale Reading (MSR):** Value on main scale just before vernier zero
- **Vernier Coincidence (VC):** Division number where vernier line aligns with main scale line
- **Least Count (LC):** Usually 0.02 mm or 0.001 inch

Mnemonic

“Main plus Matched makes Measurement”

Question 1(c) OR [7 marks]

What is Least Count of instrument. State equation of Least count of micrometer screw. Explain the positive and negative error in micrometer screw with neat and clean diagram.

Solution

Least Count: Smallest measurement that can be directly measured using a measuring instrument.

Equation for Least Count of Micrometer Screw: $\text{Least Count} = \text{Pitch of screw} / \text{Number of divisions on circular scale}$

Diagram: Micrometer Screw Gauge

0 5 10 15 20 25

V

0 5 Circular Scale

Positive Error: When zero of circular scale is above the reference line. The measured reading will be more than the actual value.

Negative Error: When zero of circular scale is below the reference line. The measured reading will be less than the actual value.

Error Correction:

- For positive error: $\text{Actual Reading} = \text{Observed Reading} - \text{Zero Error}$
- For negative error: $\text{Actual Reading} = \text{Observed Reading} + \text{Zero Error}$

Mnemonic

“Positive Produces Plus, Negative Needs Addition”

Question 2(a) [3 marks]

Write characteristics of electric lines of force.

Solution

Table 3: Characteristics of Electric Field Lines

| Characteristic | Description |
|----------------|--|
| Direction | Always from positive to negative charge |
| Shape | Straight lines for uniform fields, curved for non-uniform fields |
| Density | Proportional to field strength |
| Path | Never intersect each other |
| Nature | Start from positive and end at negative charges |

Mnemonic

“Direction, Density, Never Cross, Start-End”

Question 2(b) [4 marks]

Calculate the equivalent capacitance for both series and parallel connection of capacitors having capacitance of values 9 F, 12 F & 15 F.

Solution

For Series Connection: $1/C_{eq} = 1/C_1 + 1/C_2 + 1/C_3$
 $1/C_{eq} = 1/9 + 1/12 + 1/15$
 $1/C_{eq} = 5/36 + 3/36 + 2.4/36 = 10.4/36$
 $C_{eq} = 36/10.4 = 3.46F$

For Parallel Connection: $C_{eq} = C_1 + C_2 + C_3$
 $C_{eq} = 9 + 12 + 15 = 36F$

Mnemonic

“Series Sums Reciprocals, Parallel Puts Together”

Question 2(c) [7 marks]

$K = 9 \times 10^9 Nm^2C^{-2}$ Explain coulomb's inverse square law and derive its equation. Calculate coulomb force between two electrons.
 $1.66 \times 10^{-19}C$,

$K = 9 \times 10^9 Nm^2C^{-2}$

Solution

Coulomb's Law: The electrostatic force between two point charges is directly proportional to the product of the charges and inversely proportional to the square of the distance between them.

Equation Derivation: $F \propto q_1 q_2 / r^2$ Combining : $F \propto q_1 q_2 / r^2$ With constant : $F = k(q_1 q_2 / r^2)$

Where

$k = 1/(4\pi\epsilon_0) = 9 \times 10^9 Nm^2/C^2$

Diagram: Coulomb's Law

q_1 q_2

r
 F_{12} F_{21}

Calculation: $F = k(q_1 q_2 / r^2)$
 $F = 9 \times 10^9 \times (1.66 \times 10^{-19}) \times (1.66 \times 10^{-19}) / (10)^2$

$F = 9 \times 10^9 \times 2.76 \times 10^{-38} / 100$

$F = 9 \times 2.76$

$\times 10^{-38-2} \times 10^9 F = 2.48 \times 10^{-31} N$

Mnemonic

“Charges Multiply, Distance Squares, Force Declines”

Question 2(a) OR [3 marks]

Explain electric field and derive its unit.

Solution

Electric Field: The region around a charge where another charge experiences a force.

Definition: Electric field at a point is the force experienced by a unit positive charge placed at that point.

$$E = F/q$$

Unit Derivation: $E = F/q = [N]/[C] = [kg \cdot m/s^2]/[As] = [kgm/(As^3)]$ SI unit : N/C or V/m

Mnemonic

“Electric field Equals Force per Charge”

Question 2(b) OR [4 marks]

Explain electric flux with neat figure and derive its unit.

Solution

Electric Flux: Measure of the electric field passing through a given area.

Equation: $\phi_e = EA \cos \theta$

Where:

- E is the electric field
- A is the area
- θ is the angle between E and the normal to the area

Diagram: Electric Flux

↑ n (normal)

/

E (electric field)

Surface Area A

Unit Derivation: $\phi_e = EA \cos \theta = [N/C][m^2][dimensionless] = [Nm^2/C]$ Since $1N/C = 1V/m$, flux unit = $Vm = Nm^2/C$

SI unit: $N \cdot m^2/C$ or Vm

Mnemonic

“Flux Flows through Fields and Areas”

Question 2(c) OR [7 marks]

Define capacitor and derive its unit. Give the formula of parallel plate capacitor and explain each term. Calculate the capacitance of a parallel plate capacitor having 20 cm x 20 cm square plates separated by a distance of 1.0 mm.

Solution

Capacitor: A device that stores electric charge.

Definition: Capacitance is the ratio of charge stored to the potential difference applied. $C = Q/V$

Unit Derivation: $C = Q/V = [C]/[V] = [A \cdot s]/[J/C] = [A \cdot s]/[N \cdot m/C] = [A^2 s^4/(kgm^2)] = Farad(F)$

Parallel Plate Capacitor Formula: $C = \epsilon_0 A/d$

Where:

- C is the capacitance
- ϵ_0 is the permittivity of free space ($8.85 \times 10^{-12} F/m$)
- ϵ_r is the relative permittivity of dielectric
- A is the area of overlap of plates
- d is the distance between plates

Diagram: Parallel Plate Capacitor

+ + + + + + +
d

{- {-} {-} {-} {-} {-} {-} }

Area A

Calculation: $A = 20 \text{ cm} \times 20 \text{ cm} = 0.2 \text{ m} \times 0.2 \text{ m} = 0.04 \text{ m}^2$
 $d = 1.0 \text{ mm} = 0.001 \text{ m}$
 $C = \epsilon_0 A/d = 8.85 \times 10^{-12} \times 1 \times 0.04/0.001 = 354 \times 10^{-12}$
 $F = 354 \text{ pF}$

Mnemonic

“Capacitance Collects Charge between Closer Plates”

Question 3(a) [3 marks]

Explain heat conduction in solid with example.

Solution

Heat Conduction: Transfer of heat through a solid material without the movement of the material itself.

Process: Heat energy transfers from high temperature region to low temperature region through molecular vibrations.

Diagram: Heat Conduction

Hot Cold
↓ ↓

{ }

Heat flow

Example: Metal spoon in hot tea gets heated up at the handle end through conduction.

Mnemonic

“Hot Energizes, Atoms Transfer, Conducts Outward”

Question 3(b) [4 marks]

A person has fever 102. What is the temperature scale here? Convert the temperature in remaining two scales.

Solution

Temperature Scale: 102 (Fahrenheit)

Conversion Formulas:

- $F = (C \times 9/5) + 32$
- $C = (F - 32) \times 5/9$

Calculation: $C = (102 - 32) \times 5/9 = 70 \times 5/9 = 38.89^\circ C = 38.89 + 273.15 = 312.04 K$

Table 5: Temperature Conversion

| Fahrenheit | Celsius | Kelvin |
|------------|---------|----------|
| 102 | 38.89 | 312.04 K |

Mnemonic

“Fahrenheit First, Convert Celsius, Kelvin Comes last”

Question 3(c) [7 marks]

Explain the principle of platinum resistance thermometer and list out its uses.

Solution

Principle: The electrical resistance of platinum changes predictably and consistently with temperature, allowing for precise temperature measurement.

Working: Based on the relationship $R = R_0[1 + \alpha(T - T_0)]$, where R is resistance at temperature T , R_0 is resistance at reference temperature T_0 .

Diagram: Platinum Resistance Thermometer

Indicator

Wheatstone
Bridge

Platinum
Resistance
Coil

Uses:

- **Industrial process:** Temperature monitoring in manufacturing
- **Scientific research:** Laboratory measurements requiring high precision
- **Calibration:** Standard for calibrating other thermometers
- **Medical applications:** Temperature monitoring in medical equipment

Mnemonic

“Platinum Provides Precise Proportional Resistance”

Question 3(a) OR [3 marks]

Define specific heat and heat capacity. And write its units.

Solution

Specific Heat: Amount of heat energy required to raise the temperature of 1 kg of substance by 1 K.

Heat Capacity: Amount of heat energy required to raise the temperature of an entire object by 1 K.

Table 7: Heat Capacity Terms

| Term | Formula | SI Unit |
|-------------------|-------------------|------------|
| Specific Heat (c) | $Q = mc \Delta T$ | J/(kg · K) |
| Heat Capacity (C) | $Q = C \Delta T$ | J/K |

Mnemonic

“Specific for Substance, Capacity for Complete Object”

Question 3(b) OR [4 marks]

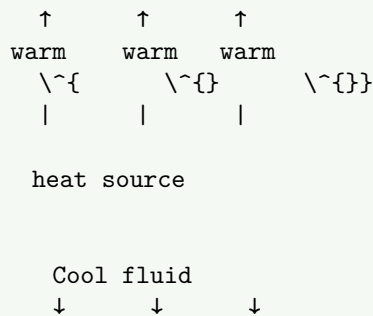
Explain heat convection in fluid with example.

Solution

Heat Convection: Transfer of heat through a fluid (liquid or gas) by the movement of the fluid itself.

Process: Hot fluid expands, becomes less dense, rises; cooler fluid descends, creating a continuous circulation pattern called convection current.

Diagram: Convection Current



Example: Boiling water in a pot - heated water rises to the top while cooler water sinks to the bottom.

Mnemonic

“Heat Rises, Cool Descends, Currents Circulate”

Question 3(c) OR [7 marks]

Define coefficient of thermal conductivity. Derive its equation of coefficient of thermal conductivity for heat transfer in solids.

Solution

Coefficient of Thermal Conductivity: The amount of heat transferred per unit time per unit area per unit temperature gradient.

Definition: The quantity of heat flowing per second through unit area when temperature gradient is unity.

Derivation:

- Consider a rod with cross-sectional area A and length L
- Temperature difference between ends is T
- Heat flow Q in time t

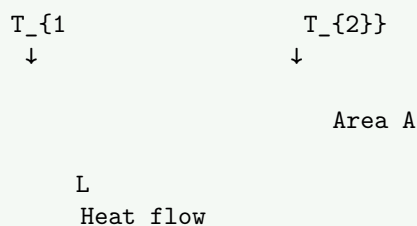
Heat current = Q/t Temperature gradient = T/L Area = A

According to Fourier's law: $Q/t = k \cdot A \cdot (T/L)$

Rearranging: $k = (Q \cdot L)/(t \cdot A \cdot T)$

Where k is the coefficient of thermal conductivity.

Diagram: Thermal Conductivity



Unit: $W/(m \cdot K)$

Mnemonic

“Heat Quantity Transfers Along Length Divided by Area and Temperature”

Question 4(a) [3 marks]

Write the difference between transverse waves and longitudinal waves.

Solution

Table 9: Transverse vs Longitudinal Waves

| Property | Transverse Waves | Longitudinal Waves |
|---------------------|---------------------------------|---|
| Particle motion | Perpendicular to wave direction | Parallel to wave direction |
| Medium displacement | Crests and troughs | Compressions and rarefactions |
| Examples | Light waves, water waves | Sound waves, seismic P-waves |
| Medium requirements | Can travel through solids | Can travel through solids, liquids, gases |
| Polarization | Can be polarized | Cannot be polarized |

Mnemonic

“Transverse Takes Perpendicular Path, Longitudinal Likes Linear Lanes”

Question 4(b) [4 marks]

Calculate the wavelength of a wave having velocity 350 m/s and frequency 10 Hz.

Solution

Wave Equation: $v = f\lambda$

Where:

- v is wave velocity (350 m/s)
- f is frequency (10 Hz)
- λ is wavelength (to be calculated)

Calculation: $\lambda = v/f = 350/10 = 35 \text{ m}$

Mnemonic

“Velocity Values frequency times wavelength”

Question 4(c) [7 marks]

Define Ultrasonic waves and write its characteristics. Write its four major applications of Ultrasonic wave.

Solution

Ultrasonic Waves: Sound waves with frequencies higher than the upper audible limit of human hearing (above 20 kHz).

Characteristics:

- **High frequency:** Above 20 kHz
- **Short wavelength:** Enables detection of small objects
- **Directional:** Can be focused in a specific direction
- **Non-ionizing:** Safe for biological tissues
- **Penetration:** Can travel through various media

Diagram: Ultrasonic Wave

Amplitude

↑

/ { / / }
/ { / / }

/ { / / Time}
/ {/ / }

Period { 50 s (f 20 kHz)}

Applications:

- **Medical:** Diagnostic imaging, therapeutic procedures
- **Industrial:** Non-destructive testing, flaw detection
- **Cleaning:** Ultrasonic cleaning baths for precision parts
- **Distance measurement:** Sonar, parking sensors, level indicators

Mnemonic

“Ultrasonic Uses Sound to Sense, Scan, Sanitize”

Question 4(a) OR [3 marks]

Explain the polarization of light with neat diagram.

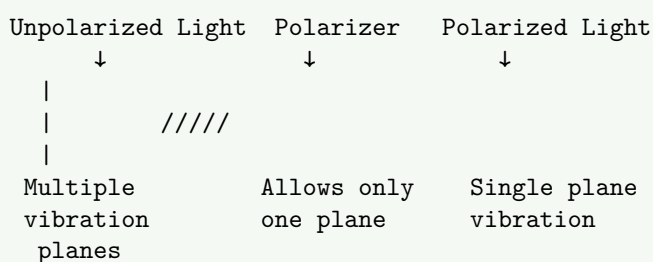
Solution

Polarization: The process of restricting the vibrations of light waves to a single plane.

Types:

- Linear polarization
- Circular polarization
- Elliptical polarization

Diagram: Light Polarization



Mnemonic

“Polarizers Pick Particular Planes”

Question 4(b) OR [4 marks]

If velocity of light in air is $3 \times 10^8 \text{ m/s}$ and velocity of light in water is $2.25 \times 10^8 \text{ m/s}$. Calculate refractive index of water.

Solution

Refractive Index Formula: $n = c/v$

Where:

- **n** is the refractive index
- **c** is the speed of light in vacuum (or air)
- **v** is the speed of light in medium

Calculation: $n = 3 \times 10^8 / 2.25 \times 10^8 = 3/2.25 = 4/3 = 1.33$

Mnemonic

“Slower Speeds Show higher index”

Question 4(c)(i) OR [4 marks]

Define: velocity, wavelength and frequency of wave. And derive the relationship between wave velocity, wavelength and frequency.

Solution

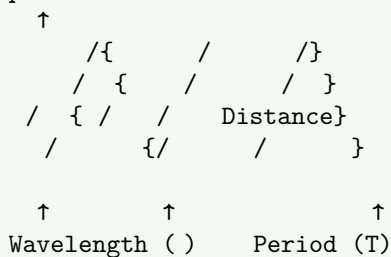
Wave Velocity (v): The speed at which a wave travels through a medium.

Wavelength (λ): The distance between two consecutive similar points on a wave.

Frequency (f): Number of complete wave cycles passing a point per unit time.

Diagram: Wave Parameters

Amplitude



Derivation:

- In time T (period), the wave travels a distance of one wavelength
- So, $v = \lambda / T$
- Since $f = 1/T$ (frequency is inverse of period)
- Therefore, $v = \lambda f$

Mnemonic

“Velocity Values frequency times wavelength”

Question 4(c)(ii) OR [3 marks]

Write properties of light.

Solution

Table 11: Properties of Light

| Property | Description |
|--------------|---|
| Propagation | Travels in straight lines in homogeneous medium |
| Speed | $3 \times 10^8 \text{ m/s}$ in vacuum |
| Reflection | Bounces off surfaces following law of reflection |
| Refraction | Changes direction when passing between media |
| Dispersion | White light splits into component colors |
| Interference | Waves can superimpose to create patterns |
| Diffraction | Bends around obstacles and through small openings |
| Polarization | Can be restricted to vibrate in one plane |
| Dual nature | Exhibits both wave and particle properties |

Mnemonic

“Light Reflects, Refracts, Disperses, Interferes, Polarizes”

Question 5(a) [3 marks]

Explain law of refraction of light for plane surface. And explain Snell's law.

Solution

Law of Refraction: When light passes from one medium to another, it changes direction at the boundary.

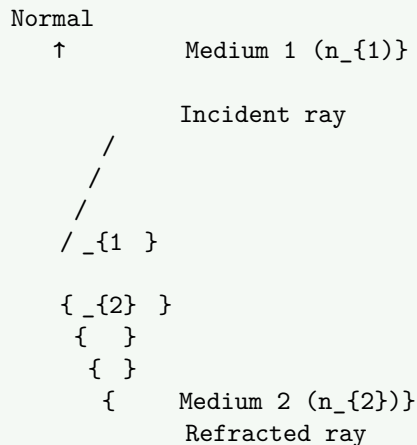
Snell's Law: The ratio of the sine of the angle of incidence to the sine of the angle of refraction is constant for a given pair of media.

$$n_1 \sin(i_1) = n_2 \sin(i_2)$$

Where:

- n_1 is the refractive index of first medium
- n_2 is the refractive index of second medium
- i_1 is the angle of incidence
- i_2 is the angle of refraction

Diagram: Refraction



Mnemonic

“Sines Show Speeds in Separate Substances”

Question 5(b) [4 marks]

A step index fiber has core refractive index of 1.30 and relative refractive index difference is $\Delta=0.02$. Find numerical aperture.

Solution

Numerical Aperture Formula: $NA = \sqrt{n_1^2 - n_2^2}$

For step index fiber: $NA = n_1 \sqrt{2\Delta}$

Where:

- n_1 is the core refractive index
- Δ is the relative refractive index difference

Calculation: $NA = 1.30 \times \sqrt{2 \times 0.02}$
 $NA = 1.30 \times \sqrt{0.04}$
 $NA = 1.30 \times 0.2$
 $NA = 0.26$

Mnemonic

“Numerical Aperture Needs core And Delta”

Question 5(c) [7 marks]

Explain Total internal reflection of light. And derive the equation of critical angle.

Solution

Total Internal Reflection (TIR): The complete reflection of light at the boundary between two media when light travels from a denser medium to a rarer medium at an angle greater than the critical angle.

Conditions for TIR:

1. Light must travel from denser to rarer medium
2. Angle of incidence must exceed critical angle

Critical Angle: The angle of incidence in the denser medium for which the angle of refraction in the rarer medium is 90° .

Derivation: Using Snell's law: $n_1 \sin(i_1) = n_2 \sin(i_2)$

At critical angle (c):

- $i_1 = c$
- $i_2 = 90^\circ$
- $\sin(90^\circ) = 1$

Therefore: $n_1 \sin(c) = n_2 \sin(90^\circ) = n_2 \times 1 = n_2$

Rearranging: $\sin(c) = n_2/n_1$

Diagram: Total Internal Reflection

Medium 1 (n_1)
(Denser)

```

      {      /}
      { c  /}
      {   /}
      {  /}
      { /}
      {/}
      / {}
     /  {}
    /   {}

```

Medium 2 (n_2)
(Rarer)

Mnemonic

“Critical Comes when Dense to Rare with Sine at Ratio”

Question 5(a) OR [3 marks]

Explain numerical aperture and acceptance angle for fiber optic cable.

Solution

Numerical Aperture (NA): Measure of the light-gathering ability of an optical fiber.

Acceptance Angle (θ_a): Maximum angle at which light can enter the fiber and still experience total internal reflection.

Relationship: $NA = \sin(\theta_a)$

Diagram: Numerical Aperture and Acceptance Angle

```

      _{a}
      / {}
Cladding /a {   Cladding}

Core           Core

Cladding       Cladding

```

Mnemonic

“Acceptance Angle Allows light, Numerical Aperture Names its Sine”

Question 5(b) OR [4 marks]

Write full form LASER. Write its characteristics.

Solution

LASER: Light Amplification by Stimulated Emission of Radiation

Table 13: Characteristics of LASER

| Characteristic | Description |
|--------------------|--|
| Monochromatic | Single wavelength or color |
| Coherent | All waves in same phase |
| Highly directional | Travels in straight line with minimal divergence |
| High intensity | Concentrated energy in narrow beam |
| Collimated | Parallel rays with minimal spreading |

Mnemonic

“LASER Light: Mono, Coherent, Direct, Intense”

Question 5(c) OR [7 marks]

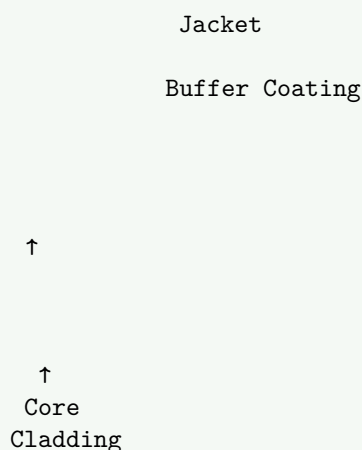
Explain the construction of optical fiber cable in details. And Explain Step index and Graded index optical fiber.

Solution

Optical Fiber Construction:

1. **Core:** Central light-transmitting portion (glass or plastic)
2. **Cladding:** Surrounds core, with lower refractive index than core
3. **Buffer Coating:** Protective plastic coating
4. **Jacket:** Outer protective covering

Diagram: Optical Fiber Structure



Step Index Fiber:

- Abrupt change in refractive index between core and cladding
- Light travels in zigzag path by total internal reflection
- Higher modal dispersion (signal spreading)
- Simpler construction

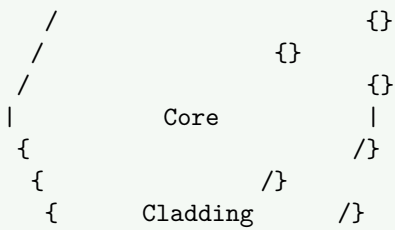
Graded Index Fiber:

- Gradual change in refractive index from center of core to cladding

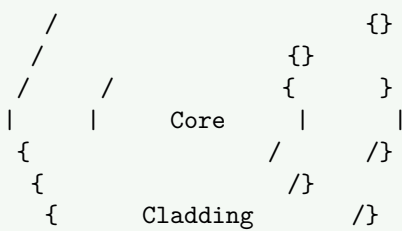
- Light travels in helical path due to continuous refraction
- Lower modal dispersion
- More complex construction

Diagram: Step Index vs Graded Index Fiber

Step Index:



Graded Index:



Refractive Index Profile:

Step Index: Graded Index:

$n_{\{1$ $\}$

$n_{\{2$ $\}$

r

r

Mnemonic

“Step Shows Sharp Shift, Graded Gradually Goes down”