

# Electronic Circuits & Networks (4331101) - Winter 2022 Solution

Milav Dabgar

February 23, 2023

## Question 1(a) [3 marks]

### Question Question 1(a) [3 marks]

marks

Define: 1) Branch 2) Junction 3) Mesh

#### Solution

- **Branch:** A branch is a single circuit element or a combination of elements connected between two nodes of a network.
- **Junction:** A junction (or node) is a point in a circuit where two or more circuit elements are connected together.
- **Mesh:** A mesh is a closed path in a network where no other closed path exists inside it.

#### Mnemonic

"BJM: Branches Join at junctions to Make meshes"

## Question 1(b) [4 marks]

### Question Question 1(b) [4 marks]

marks

Write voltage division and current division rule with necessary circuit diagram

#### Solution

**Voltage Division Rule:** In a series circuit, voltage across any component is proportional to its resistance.

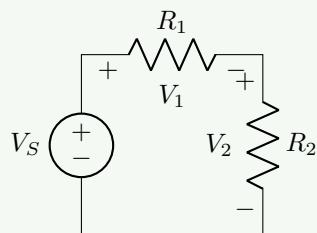
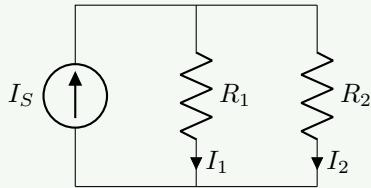


Figure 1. Voltage Division Circuit

- **Formula:**  $V_1 = V_S \times \frac{R_1}{R_1 + R_2}$

- **Application:** Used to find individual voltage drops across series components

**Current Division Rule:** In a parallel circuit, current through any branch is inversely proportional to its resistance.

**Figure 2.** Current Division Circuit

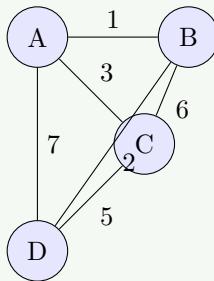
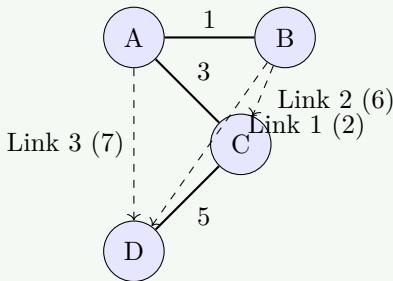
- Formula:**  $I_1 = I_S \times \frac{R_2}{R_1 + R_2}$
- Key concept:** Current takes path of least resistance

**Mnemonic**

"VoSe CuPa: Voltage divides in Series, Current divides in Parallel"

**Question 1(c) [7 marks]****Question Question 1(c) [7 marks]****marks**

Draw Graph and Tree for a network shown in fig(1). Show link currents on a graph. Also write Tie-set schedule for a tree of network shown in fig. (1)

**Solution****Graph of the Network:****Figure 3.** Graph of the Network**Tree of the Network** (Twigs in solid, Links in dashed):**Figure 4.** Tree and Links**Tie-set Schedule:**

| Link/Tree Branch | Br 1 (AB) | Br 3 (AC) | Br 4 (CD) | Br 2 (BD) | Br 6 (BC) | Br 7 (AD) | Br 5 (CD) |
|------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Link 1 (BD)      | 1         | 0         | 0         | 1         | 0         | 0         | 0         |
| Link 2 (BC)      | 1         | 1         | 0         | 0         | 1         | 0         | 0         |
| Link 3 (AD)      | 0         | 0         | 1         | 0         | 0         | 1         | 0         |
| Link 4 (CD)      | 0         | 0         | 1         | 0         | 0         | 0         | 1         |

**Mnemonic**

"TGLT: Trees Generate Link-current Tie-sets"

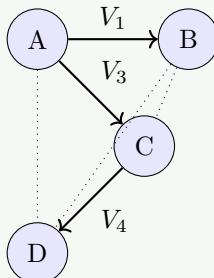
**Question 1(c) OR [7 marks]****Question Question 1(c) OR [7 marks]****marks**

Draw Graph and Tree for a network shown in fig(1). Show branch voltages on tree. Also write cut-set schedule for a tree of network shown on fig.(1)

**Solution**

**Graph of the Network:** Same as above.

**Tree of the Network:**



**Figure 5.** Tree with Branch Voltages

**Cut-set Schedule:**

| Cut-set/Branch | Br 1 (AB) | Br 3 (AC) | Br 4 (CD) | Br 2 (BD) | Br 6 (BC) | Br 7 (AD) | Br 5 (CD) |
|----------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Cut-set 1 (AB) | 1         | 0         | 0         | -1        | -1        | 0         | 0         |
| Cut-set 2 (AC) | 0         | 1         | 0         | 0         | 1         | -1        | 0         |
| Cut-set 3 (CD) | 0         | 0         | 1         | 1         | 0         | 1         | 1         |

**Mnemonic**

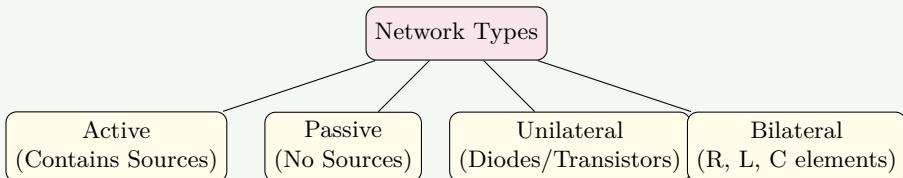
"CGVS: Cut-sets Generate Voltage Sources"

**Question 2(a) [3 marks]****Question Question 2(a) [3 marks]****marks**

**Define:** 1) Active and passive network 2) Unilateral and Bilateral network.

### Solution

- **Active Network:** A network containing one or more sources of EMF (voltage/current sources) that supply energy to the circuit.
- **Passive Network:** A network containing only passive elements like resistors, capacitors, and inductors with no energy sources.
- **Unilateral Network:** A network in which the properties and performance change when input and output terminals are interchanged (e.g., diode circuits).
- **Bilateral Network:** A network in which the properties and performance remain unchanged when input and output terminals are interchanged (e.g., resistor circuits).



**Figure 6.** Network Classification

### Mnemonic

"APUB: Active Provides energy, Unilateral Blocks reversal"

## Question 2(b) [4 marks]

### Question Question 2(b) [4 marks]

marks

Write equation for Z parameter and derive  $Z_{11}$ ,  $Z_{12}$ ,  $Z_{21}$ ,  $Z_{22}$  from that equation.

### Solution

Z-parameters define the relationship between port voltages and currents in a two-port network:

**Equations:**

$$\begin{aligned} V_1 &= Z_{11}I_1 + Z_{12}I_2 \\ V_2 &= Z_{21}I_1 + Z_{22}I_2 \end{aligned}$$

**Derivation:**

- $Z_{11} = \left. \frac{V_1}{I_1} \right|_{I_2=0}$  : Input impedance with output port open-circuited.
- $Z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$  : Reverse transfer impedance with input port open-circuited.
- $Z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$  : Forward transfer impedance with output port open-circuited.
- $Z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$  : Output impedance with input port open-circuited.

### Mnemonic

"Z Impedance: Open circuit gives correct Parameters"

## Question 2(c) [7 marks]

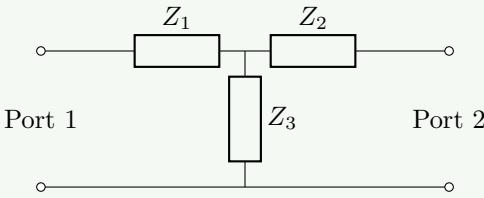
### Question Question 2(c) [7 marks]

marks

Derive equation of characteristic impedance(ZOT) for a standard T network.

#### Solution

For a standard T-network:



**Figure 7.** T-Network

#### Derivation Steps:

1. For a symmetric T-network,  $Z_1 = Z_2$ .
  2. Under matched condition, input impedance equals characteristic impedance.
  3.  $Z_{0T} = Z_1 + \frac{Z_1 \times Z_3}{Z_1 + Z_3}$
  4. For balanced T-network where series arms are  $Z/2$  and shunt arm is  $Z$ :
  5.  $Z_{0T} = \frac{Z}{2} + \frac{\frac{Z}{2} \times Z}{\frac{Z}{2} + Z}$
  6.  $Z_{0T} = \frac{Z}{2} + \frac{Z^2/2}{3Z/2}$
  7.  $Z_{0T} = \frac{Z}{2} + \frac{Z}{3}$
  8.  $Z_{0T} = \frac{3Z+2Z}{6}$
  9.  $Z_{0T} = \sqrt{Z_1(Z_1 + 2Z_3)}$
- Final Equation:**  $Z_{0T} = \sqrt{Z_1(Z_1 + 2Z_3)}$

#### Mnemonic

"TO Impedance: Two arms Over middle branch"

## Question 2(a) OR [3 marks]

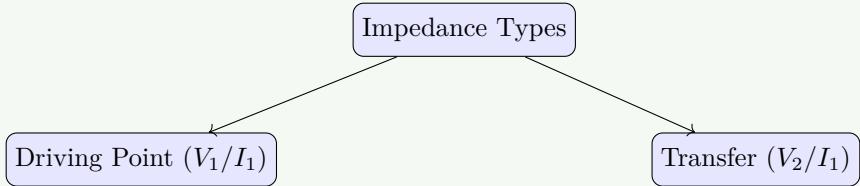
### Question Question 2(a) OR [3 marks]

marks

Define: 1)Driving point impedance 2) Transfer impedance

#### Solution

- **Driving Point Impedance:** The ratio of voltage to current at the same port/pair of terminals when all other independent sources are set to zero ( $Z_{11} = V_1/I_1$ ).
- **Transfer Impedance:** The ratio of voltage at one port to the current at another port when all other independent sources are set to zero ( $Z_{21} = V_2/I_1$ ).

**Mnemonic**

"DTSS: Driving at Terminal Same, Transfer at Separate"

**Question 2(b) OR [4 marks]****Question Question 2(b) OR [4 marks]**

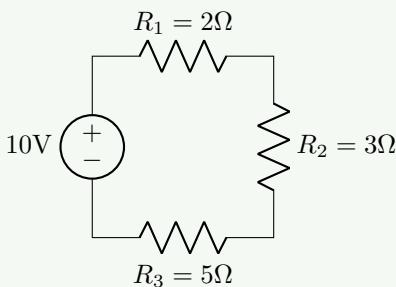
**marks**

Explain Kirchhoff's voltage law with example.

**Solution**

**Kirchhoff's Voltage Law (KVL):** The algebraic sum of all voltages around any closed loop in a circuit is zero.  
**Mathematically:**  $\sum V = 0$  (around a closed loop)

**Circuit Example:**



**Figure 8.** KVL Example Circuit

If  $I = 1A$ , then:

- $V_1 = 1A \times 2\Omega = 2V$
- $V_2 = 1A \times 3\Omega = 3V$
- $V_3 = 1A \times 5\Omega = 5V$

Applying KVL:  $10V - 2V - 3V - 5V = 0 \checkmark$

**Mnemonic**

"VACZ: Voltages Around Closed loop are Zero"

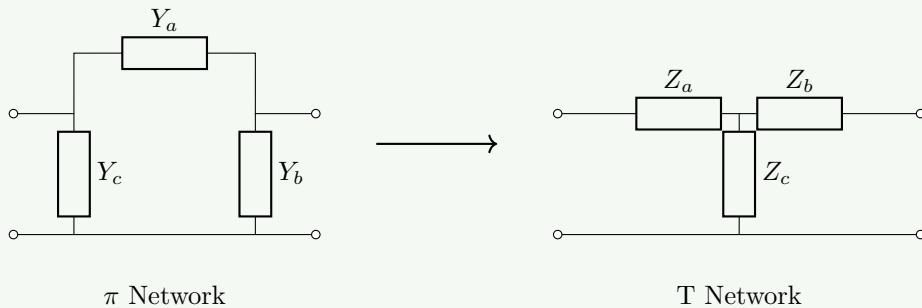
**Question 2(c) OR [7 marks]****Question Question 2(c) OR [7 marks]**

**marks**

Derive equation to convert  $\pi$  network into T network.

## Solution

### $\pi$ Network to T Network Conversion:



**Figure 9.** Conversion Diagram

## Conversion Equations:

- $Z_a = \frac{Y_a \times Y_c}{Y_\Delta}$
  - $Z_b = \frac{Y_b \times Y_c}{Y_\Delta}$
  - $Z_c = \frac{Y_a \times Y_b}{Y_\Delta}$

Where  $Y_{\Delta} = Y_a + Y_b + Y_c$

## Derivation:

1. Start with Y-parameters of  $\pi$ -network
  2. Express Y-parameters in terms of branch admittances
  3. Convert to Z-parameters using matrix inversion
  4. Express T-network impedances in terms of Z-parameters
  5. Simplify to get the conversion formulas above

## Mnemonic

"PIE to TEA: Product over sum for opposite branch"

### Question 3(a) [3 marks]

### Question Question 3(a) [3 marks]

marks

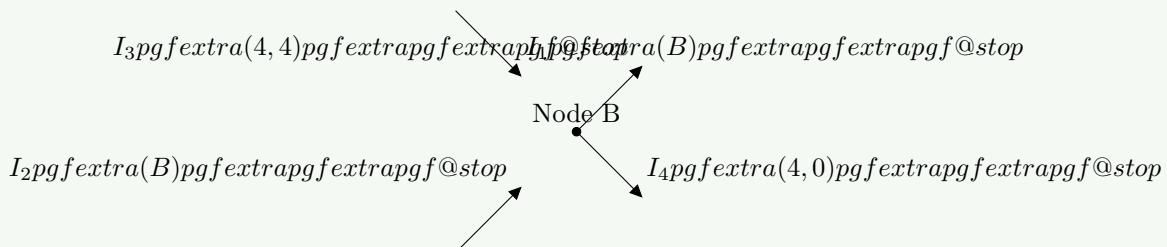
Explain Kirchhoff's current law with example.

## Solution

**Kirchhoff's Current Law (KCL):** The algebraic sum of all currents entering and leaving a node must equal zero.

**Mathematically:**  $\sum I = 0$  (at any node)

### Circuit Example:



Applying KCL at node B:

- Currents entering:  $I_1 + I_2 = 5A + 2A = 7A$

- Currents leaving:  $I_3 + I_4 = 3A + 4A = 7A$
- Therefore:  $I_1 + I_2 - I_3 - I_4 = 5 + 2 - 3 - 4 = 0 \checkmark$

**Mnemonic**

"CuNoZ: Currents at Node are Zero"

**Question 3(b) [4 marks]****Question Question 3(b) [4 marks]**

**marks**

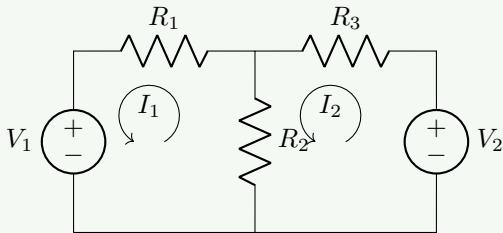
Explain mesh analysis with required equations.

**Solution**

**Mesh Analysis:** A circuit analysis technique that uses mesh currents as variables to solve a circuit with multiple loops.

**Steps:**

1. Identify all meshes (closed loops) in the circuit
2. Assign a mesh current to each mesh
3. Apply KVL to each mesh
4. Solve the resulting system of equations

**Example Circuit:**

**Figure 10.** Mesh Analysis Example

**Equations:**

- Mesh 1:  $V_1 = I_1 R_1 + (I_1 - I_2) R_2$
- Mesh 2:  $V_2 = I_2 R_3 + (I_2 - I_1) R_2$

**Mnemonic**

"MILK: Mesh Is Loop with KVL"

**Question 3(c) [7 marks]****Question Question 3(c) [7 marks]**

**marks**

State and explain Thevenin's theorem.

**Solution**

**Thevenin's Theorem:** Any linear network with voltage and current sources can be replaced by an equivalent circuit consisting of a voltage source ( $V_{TH}$ ) in series with a resistance ( $R_{TH}$ ).

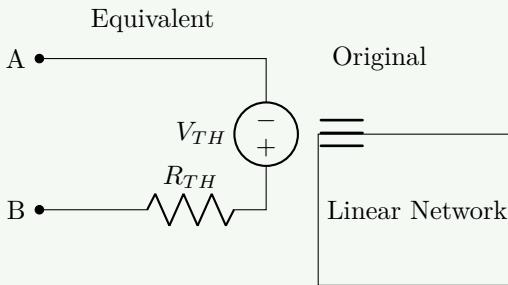


Figure 11. Thevenin Equivalent

**Steps to Find Thevenin Equivalent:**

1. Remove the load from the terminals of interest
2. Calculate the open-circuit voltage ( $V_{OC}$ ) across these terminals ( $= V_{TH}$ )
3. Calculate the resistance looking back into the circuit with all sources replaced by their internal resistances ( $= R_{TH}$ )
4. The Thevenin equivalent consists of  $V_{TH}$  in series with  $R_{TH}$

**Mnemonic**

"TORV: Thevenin's Open-circuit Resistance and Voltage"

## Question 3(a) OR [3 marks]

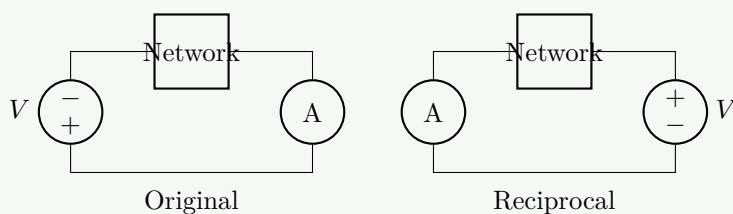
## Question Question 3(a) OR [3 marks]

marks

State and explain reciprocity theorem.

**Solution**

**Reciprocity Theorem:** In a linear, bilateral network, if a voltage source in one branch produces a current in another branch, then the same voltage source, if placed in the second branch, will produce the same current in the first branch.



**Mathematically:** If a voltage  $V_1$  in branch 1 produces current  $I_2$  in branch 2, then voltage  $V_1$  in branch 2 will produce current  $I_2$  in branch 1.

**Limitations:** Applies only to networks with:

- Linear elements
- Bilateral elements (no diodes, transistors)
- Single independent source

**Mnemonic**

"RESWAP: REciprocity SWAPs Position with identical results"

**Question 3(b) OR [4 marks]****Question Question 3(b) OR [4 marks]**

**marks**

Explain nodal analysis with required equations.

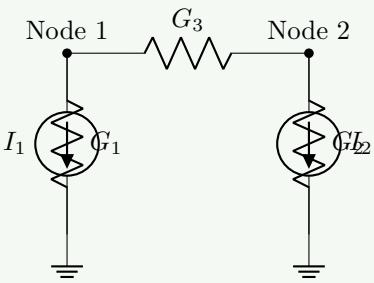
**Solution**

**Nodal Analysis:** A circuit analysis technique that uses node voltages as variables to solve a circuit.

**Steps:**

1. Choose a reference node (ground)
2. Assign voltage variables to remaining nodes
3. Apply KCL at each non-reference node
4. Solve the resulting system of equations

**Example Circuit:**



**Figure 12.** Nodal Analysis

**Equations:**

- Node 1:  $I_1 = V_1G_1 + (V_1 - V_2)G_3$
- Node 2:  $I_2 = V_2G_{L2} + (V_2 - V_1)G_3$

**Mnemonic**

"NKCV: Nodal uses KCL with Voltage variables"

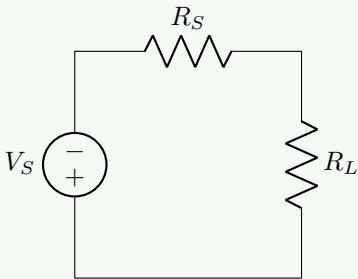
**Question 3(c) OR [7 marks]****Question Question 3(c) OR [7 marks]**

**marks**

State and prove maximum power transfer theorem.

**Solution**

**Maximum Power Transfer Theorem:** A load connected to a source will extract maximum power when its resistance equals the internal resistance of the source.

**Proof:**

1. Current in the circuit:  $I = \frac{V_S}{R_S + R_L}$
2. Power delivered to load:  $P = I^2 R_L = \frac{V_S^2 R_L}{(R_S + R_L)^2}$
3. For maximum power,  $\frac{dP}{dR_L} = 0$
4. Solving:  $\frac{V_S^2 (R_S + R_L)^2 - V_S^2 R_L \cdot 2(R_S + R_L)}{(R_S + R_L)^4} = 0$
5. Simplifying:  $(R_S + R_L)^2 = 2R_L(R_S + R_L)$
6. Further simplifying:  $R_S + R_L = 2R_L$
7. Therefore:  $R_S = R_L$

**Maximum Power:**  $P_{max} = \frac{V_S^2}{4R_S}$

**Mnemonic**

"MaRLRS: Maximum power when load Resistance equals Source Resistance"

**Question 4(a) [3 marks]****Question Question 4(a) [3 marks]**

marks

Why series resonance circuit act as voltage amplifier and parallel resonance circuit act as current amplifier?

**Solution****Series Resonance as Voltage Amplifier:**

- At resonance, series circuit impedance is minimum (just R)
- Voltage across L or C can be much larger than source voltage
- Voltage magnification factor =  $Q = \frac{X_L}{R} = \frac{1}{R} \sqrt{\frac{L}{C}}$
- Voltage across L or C =  $Q \times$  Source voltage

**Parallel Resonance as Current Amplifier:**

- At resonance, parallel circuit impedance is maximum
- Current in L or C can be much larger than source current
- Current magnification factor =  $Q = \frac{R}{X_L} = R \sqrt{\frac{C}{L}}$
- Current through L or C =  $Q \times$  Source current

| Circuit Type | Impedance at Resonance | Amplification                             |
|--------------|------------------------|---|
| Series       | Minimum ( $R$ only)    | Voltage ( $V_L$ or $V_C = Q \times V_S$ ) |
| Parallel     | Maximum ( $R^2/r$ )    | Current ( $I_L$ or $I_C = Q \times I_S$ ) |

**Mnemonic**

"SeVoPa: Series Voltage, Parallel current amplification"

## Question 4(b) [4 marks]

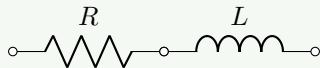
### Question Question 4(b) [4 marks]

marks

Derive equation of Q of coil.

#### Solution

**Q-factor of a Coil:**



**Derivation:**

1. Q-factor is defined as:  $Q = \frac{\text{Energy stored}}{\text{Energy dissipated per cycle}}$
  2. Energy stored in inductor =  $\frac{1}{2}LI^2$
  3. Power dissipated in resistor =  $I^2R$
  4. Energy dissipated per cycle = Power × Time period =  $I^2R \times \frac{1}{f}$
  5. Therefore:  $Q = \frac{\frac{1}{2}LI^2}{I^2R \times \frac{1}{f}}$
  6. Simplifying:  $Q = \frac{2\pi \times \frac{1}{2}LI^2 \times f}{I^2R}$
  7.  $Q = \frac{2\pi f \times L}{R} = \frac{\omega L}{R}$
- Final Equation:**  $Q = \frac{\omega L}{R} = \frac{2\pi f L}{R} = \frac{X_L}{R}$

#### Mnemonic

"QualityEDR: Quality equals Energy stored Divided by energy lost per Radian"

## Question 4(c) [7 marks]

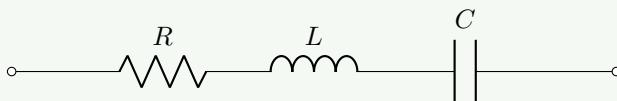
### Question Question 4(c) [7 marks]

marks

Derive equation of series resonance frequency for series R-L-C circuit.

#### Solution

**Series R-L-C Circuit:**



**Figure 13.** Series RLC Circuit

**Derivation:**

1. Impedance of series RLC circuit:  $Z = R + j(X_L - X_C)$
  2. Where:  $X_L = \omega L$  and  $X_C = \frac{1}{\omega C}$
  3. At resonance,  $X_L = X_C$  (inductive and capacitive reactances are equal)
  4. Therefore:  $\omega L = \frac{1}{\omega C}$
  5. Solving for  $\omega$ :  $\omega^2 = \frac{1}{LC}$
  6. Resonant frequency:  $\omega_0 = \frac{1}{\sqrt{LC}}$
  7. In terms of frequency f:  $f_0 = \frac{1}{2\pi\sqrt{LC}}$
- Characteristics at Resonance:**

- Impedance is minimum (purely resistive:  $Z = R$ )
- Current is maximum ( $I = V/R$ )
- Power factor is unity (circuit appears resistive)
- Voltages across L and C are equal and opposite

**Mnemonic**

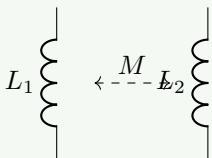
"RES: Reactances Equal at Series resonance"

**Question 4(a) OR [3 marks]****Question Question 4(a) OR [3 marks]****marks**

**What is coupled circuits? Define self-inductance and mutual inductance.**

**Solution**

**Coupled Circuits:** Two or more circuits that are magnetically linked such that energy can be transferred between them through their mutual magnetic field.



**Figure 14.** Coupled Coils

**Self-inductance (L):** The property of a circuit whereby a change in current produces a self-induced EMF in the same circuit.  $L = \Phi/I$  (ratio of magnetic flux to the current producing it)

**Mutual inductance (M):** The property of a circuit whereby a change in current in one circuit induces an EMF in another circuit.  $M = \Phi_{21}/I_1$  (ratio of flux in circuit 2 due to current in circuit 1)

**Mnemonic**

"SiMu: Self in Mine, Mutual in Yours"

**Question 4(b) OR [4 marks]****Question Question 4(b) OR [4 marks]****marks**

**Derive equation for co-efficient of coupling (K).**

**Solution****Coefficient of Coupling (k):****Derivation:**

1. The mutual inductance (M) between two coils depends on:
  - Self-inductances of the coils ( $L_1$  and  $L_2$ )
  - Physical arrangement (proximity and orientation)
2. Maximum possible mutual inductance:  $M_{max} = \sqrt{L_1 L_2}$

3. Coefficient of coupling is defined as:  $k = \frac{M}{M_{max}}$

4. Therefore:  $k = \frac{M}{\sqrt{L_1 L_2}}$

**Characteristics:**

- $k$  ranges from 0 (no coupling) to 1 (perfect coupling)
- $k$  depends on geometry, orientation, and medium
- Typical transformers:  $k = 0.95$  to  $0.99$
- Air-core coils:  $k = 0.01$  to  $0.5$

**Mnemonic**

"KMutual: K Measures Mutual linkage proportion"

## Question 4(c) OR [7 marks]

### Question Question 4(c) OR [7 marks]

marks

A series RLC circuit has  $R=30\Omega$ ,  $L = 0.5H$ , and  $C = 5\mu F$ . Calculate (i) series resonance frequency (2) Q Factor (3)BW

**Solution**

**Given:**

- Resistance,  $R = 30\Omega$
- Inductance,  $L = 0.5H$
- Capacitance,  $C = 5\mu F = 5 \times 10^{-6}F$

**Calculations:**

(i) Series Resonance Frequency:

- $f_0 = \frac{1}{2\pi\sqrt{LC}}$
- $f_0 = \frac{1}{2\pi\sqrt{0.5 \times 5 \times 10^{-6}}}$
- $f_0 = 100.76 \text{ Hz} \approx 100 \text{ Hz}$

(ii) Q Factor:

- $Q = \frac{1}{R} \sqrt{\frac{L}{C}}$
- $Q = \frac{1}{30} \sqrt{\frac{0.5}{5 \times 10^{-6}}}$
- $Q = 10.54$

(iii) Bandwidth (BW):

- $BW = \frac{f_0}{Q}$
- $BW = \frac{100.76}{10.54} = 9.56 \text{ Hz}$

Table:  
Parameter

| Parameter                    | Formula                          | Value   |
|------------------------------|----------------------------------|---------|
| Resonant Frequency ( $f_0$ ) | $\frac{1}{2\pi\sqrt{LC}}$        | 100 Hz  |
| Quality Factor ( $Q$ )       | $\frac{1}{R} \sqrt{\frac{L}{C}}$ | 10.54   |
| Bandwidth (BW)               | $f_0/Q$                          | 9.56 Hz |

**Mnemonic**

"RQB: Resonance Quality determines Bandwidth"

## Question 5(a) [3 marks]

## Question Question 5(a) [3 marks]

marks

Classify various types of attenuators.

### Solution

**Attenuators:** Network of resistors designed to reduce (attenuate) signal level without distortion.

**Types of Attenuators:**

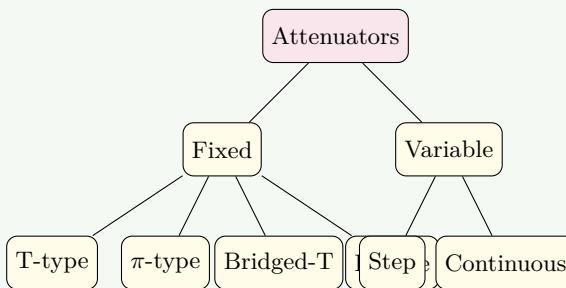


Figure 15. Classification of Attenuators

- **Based on configuration:** T-type, π-type, Bridged-T, Lattice
- **Based on symmetry:** Symmetrical (equal Z in/out), Asymmetrical

### Mnemonic

"ATP Fixed: Attenuator Types include Pad, Tee, Lattice"

## Question 5(b) [4 marks]

## Question Question 5(b) [4 marks]

marks

Derive relation between attenuator and neper.

### Solution

**Relationship between Attenuation and Neper:**

- **Attenuation ( $\alpha$ ):** Ratio of input voltage (or current) to output voltage (or current).
- **Neper (Np):** Natural logarithmic unit of ratios.

**Derivation:**

1. For a voltage ratio  $V_1/V_2$ :
  - Attenuation in Nepers =  $\ln(V_1/V_2)$
  - Attenuation in Decibels =  $20 \log_{10}(V_1/V_2)$
2. For a power ratio  $P_1/P_2$ :
  - Attenuation in Nepers =  $\frac{1}{2} \ln(P_1/P_2)$
  - Attenuation in Decibels =  $10 \log_{10}(P_1/P_2)$
3. Relationship between dB and Neper:
  - 1 Neper = 8.686 dB
  - 1 dB = 0.115 Neper

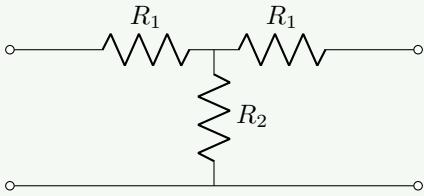
| Unit         | Voltage Ratio           | Power Ratio                |
|--------------|-------------------------|----------------------------|
| Neper (Np)   | $\ln(V_1/V_2)$          | $\frac{1}{2} \ln(P_1/P_2)$ |
| Decibel (dB) | $20 \log_{10}(V_1/V_2)$ | $10 \log_{10}(P_1/P_2)$    |

**Mnemonic**

"NED: Neper Equals Decibel divided by 8.686"

**Question 5(c) [7 marks]****Question Question 5(c) [7 marks]****marks**

Derive equations of R1 and R2 for symmetrical T attenuator.

**Solution****Symmetrical T Attenuator:**

**Figure 16.** Symmetrical T Attenuator

**Derivation:**

- For a symmetrical T-attenuator with characteristic impedance  $Z_0$ :
  - Input and output impedance must both equal  $Z_0$
  - Attenuation ratio  $N = V_1/V_2 = I_2/I_1$
- From circuit analysis:
  - $R_1 = Z_0 \frac{N-1}{N+1}$
  - $R_2 = \frac{2Z_0 N}{N^2 - 1}$
- For attenuation in dB ( $\alpha$ ):
  - $N = 10^{\alpha/20}$
  - $R_1 = Z_0 \tanh(\alpha/2)$
  - $R_2 = Z_0 / \sinh(\alpha)$

**Final Equations:**

- $R_1 = Z_0 \frac{N-1}{N+1}$
- $R_2 = \frac{2Z_0 N}{N^2 - 1}$

**Mnemonic**

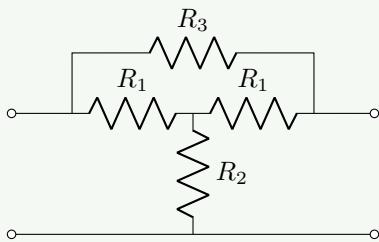
"TSR: T-attenuator Symmetry Requires equal R1 values"

**Question 5(a) OR [3 marks]****Question Question 5(a) OR [3 marks]****marks**

Draw circuit diagram of symmetrical Bridge T and symmetrical Lattice attenuator.

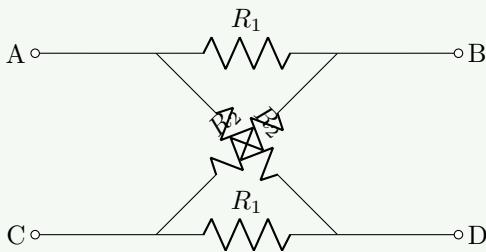
**Solution**

**Symmetrical Bridge-T Attenuator:**



**Figure 17.** Bridge-T Attenuator

**Symmetrical Lattice Attenuator:**



**Figure 18.** Lattice Attenuator

**Characteristics:**

- **Bridge-T:** Combines features of T and  $\pi$  attenuators.
- **Lattice:** Balanced configuration with excellent phase/frequency response.

**Mnemonic**

"BL-BA: Bridge Ladder, Balanced Attenuators"

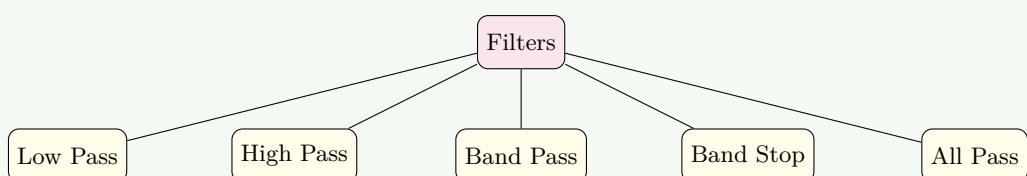
**Question 5(b) OR [4 marks]****Question Question 5(b) OR [4 marks]**

marks

Write classification of filter based on frequency with their frequency responses showing pass band and stop band.

**Solution**

**Classification of Filters Based on Frequency:**



**Frequency Responses:**

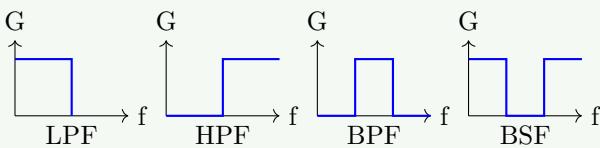


Figure 19. Ideal Frequency Responses

**Mnemonic**

"LHBBA: Low High Band-pass Band-stop All-pass"

**Question 5(c) OR [7 marks]****Question Question 5(c) OR [7 marks]**

marks

Draw the circuit for T-section and  $\pi$ -section constant-K low pass filter and Derive equation of cut-off frequency.

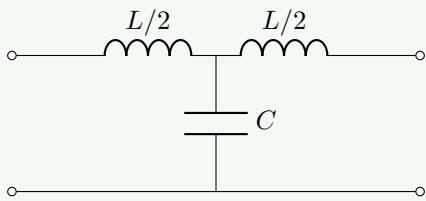
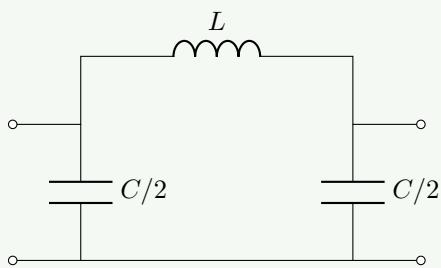
**Solution****T-section Constant-K Low Pass Filter:**

Figure 20. T-section LPF

 **$\pi$ -section Constant-K Low Pass Filter:**Figure 21.  $\pi$ -section LPF**Derivation of Cutoff Frequency:**

1. For a constant-K filter:

- $Z_1 \times Z_2 = R_0^2$  (characteristic impedance squared)
- $Z_1 = j\omega L$  (series impedance)
- $Z_2 = \frac{1}{j\omega C}$  (shunt impedance)

$$2. R_0^2 = j\omega L \times \frac{1}{j\omega C} = \frac{L}{C} \implies R_0 = \sqrt{L/C}$$

3. Pass band condition:  $-1 < \frac{Z_1}{4Z_2} < 0$

4. At cutoff frequency:  $\frac{\omega^2 LC}{4} = 1$

$$5. \omega_c = \frac{2}{\sqrt{LC}}$$

$$6. f_c = \frac{1}{\pi\sqrt{LC}}$$

**Final Equation:**  $f_c = \frac{1}{\pi\sqrt{LC}}$

**Mnemonic**

"KCLP: Konstant-k Cutoff in Low Pass depends on L and C product"