

# Subject Name Solutions

1333203 – Winter 2023

Semester 1 Study Material

*Detailed Solutions and Explanations*

## Question 1(a) [3 marks]

Define linked list. List different types of linked list.

### Solution

#### Definition

A linked list is a linear data structure where elements are stored in nodes, and each node points to the next node in the sequence

#### Types of Linked List

1. Singly Linked List
2. Doubly Linked List
3. Circular Linked List
4. Circular Doubly Linked List

#### Diagram:

Singly: [Data|Next] [Data|Next] [Data|Next] NULL  
Doubly: [Prev|Data|Next] [Prev|Data|Next] [Prev|Data|Next] NULL  
Circular: [Data|Next] [Data|Next] [Data|Next]

### Mnemonic

“Single, Double, Circle, Double-Circle”

## Question 1(b) [4 marks]

Explain Linear and Non Linear Data structure in Python with examples.

### Solution

#### Data Structure

Linear

#### Description

Elements arranged in sequential order where each element has exactly one predecessor and successor (except first and last)

#### Python Examples

Lists: [1, 2, 3] Tuples: (1, 2, 3)  
Strings: "abc" Queue: `queue.Queue()`

Non-Linear

Elements not arranged sequentially; an element can connect to multiple elements

Dictionary: {"a": 1, "b": 2} Set: {1, 2, 3} Tree: Custom implementation Graph: Custom implementation

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[Data Structures]
    A --{-}{-}{ B[Linear]}
    A --{-}{-}{ C[Non{-}Linear]}
    B --{-}{-}{ D[Arrays]}
    B --{-}{-}{ E[Linked Lists]}
    B --{-}{-}{ F[Stacks]}
    B --{-}{-}{ G[Queues]}
    C --{-}{-}{ H[Trees]}
    C --{-}{-}{ I[Graphs]}
    C --{-}{-}{ J[Hash Tables]}
{Highlighting}
{Shaded}
```

### Mnemonic

“Linear Listens In Sequence, Non-linear Navigates Various Paths”

### Question 1(c) [7 marks]

Explain class, attributes, object and class method in python with suitable example.

### Solution

#### Diagram:

```
classDiagram
    class Student \{
        {-roll\_no}
        {-name}
        +\_\_init\_\_()
        +display()
    \}
```

Term	Description
Class	Blueprint for creating objects with shared attributes and methods
Attributes	Variables that store data inside a class
Object	Instance of a class with specific attribute values
Class Method	Functions defined within a class that can access and modify class states

**Code:**

```
class Student:
    \# Class attribute
    school = "GTU"

    \# Constructor
    def \_\_init\_\_(self, roll\_no, name):
        \# Instance attributes
        self.roll\_no = roll\_no
        self.name = name

    \# Instance method
    def display(self):
        print(f"Roll No: \{self.roll\_no\}, Name: \{self.name\}")

    \# Class method
    @classmethod
    def change\_school(cls, new\_school):
        cls.school = new\_school

\# Creating object
student1 = Student(101, "Raj")
student1.display() \# Output: Roll No: 101, Name: Raj
```

**Mnemonic**

“Class Creates, Attributes Store, Objects Use, Methods Operate”

**Question 1(c) OR [7 marks]**

Define Data Encapsulation & Polymorphism. Develop a Python code to explain Polymorphism.

**Solution**

Concept	Definition
Data Encapsulation	Bundling data and methods into a single unit (class) and restricting direct access to some components
Polymorphism	Ability of different classes to provide their own implementation of methods with the same name

## Diagram:

### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[Polymorphism]
    A --{} B[Method Overriding]
    A --{} C[Method Overloading]
    A --{} D[Duck Typing]
{Highlighting}
{Shaded}
```

## Code:

```
\# Polymorphism example
class Animal:
    def speak(self):
        pass

class Dog(Animal):
    def speak(self):
        return "Woof!"

class Cat(Animal):
    def speak(self):
        return "Meow!"

class Duck(Animal):
    def speak(self):
        return "Quack!"

\# Function demonstrating polymorphism
def animal\_sound(animal):
    return animal.speak()

\# Creating objects
dog = Dog()
cat = Cat()
duck = Duck()

\# Same function works for different animal objects
print(animal\_sound(dog))    \# Output: Woof!
print(animal\_sound(cat))    \# Output: Meow!
print(animal\_sound(duck))    \# Output: Quack!
```

## Mnemonic

“Encapsulate to Protect, Polymorphism for Flexibility”

## Question 2(a) [3 marks]

Differentiate between Stack and Queue.

### Solution

Feature	Stack	Queue
Principle	LIFO (Last In First Out)	FIFO (First In First Out)
Operations	Push, Pop	Enqueue, Dequeue

Access

Elements can only be added/removed from one end (top)

Elements are added at rear end and removed from front end

**Diagram:**

Stack:            [3]            Queue:   [1]   [2]   [3]  
                  [2]                        Front        Rear  
                  [1]  
                  {-}{-}{-}

**Mnemonic**

“Stack Piles Up, Queue Lines Up”

## Question 2(b) [4 marks]

Write an algorithm for PUSH and POP operation of stack in python.

**Solution**

**PUSH Algorithm:**

Start

1. Check if stack is full
2. If not full, increment top by 1
3. Add element at position {top}

End

**POP Algorithm:**

Start

1. Check if stack is empty
2. If not empty, retrieve element at {top}
3. Decrement top by 1
4. Return retrieved element

End

**Code:**

```
class Stack:
    def __init__(self, size):
        self.stack = []
        self.size = size
        self.top = -1

    def push(self, element):
        if self.top == self.size - 1:
            return "Stack Overflow"
        else:
            self.top += 1
            self.stack.append(element)
            return "Pushed " + str(element)

    def pop(self):
        if self.top < 0:
            return "Stack Underflow"
        else:
            element = self.stack.pop()
            self.top -= 1
            return element
```

### Mnemonic

“Push to Top, Pop from Top”

### Question 2(c) [7 marks]

Convert following equation from infix to postfix using Stack.  $A * (B + C) - D / (E + F)$

#### Solution

##### Diagram:

Infix:  $A * (B + C) \{- D / (E + F)\}$

Postfix:  $A B C + * D E F + / \{-\}$

Step	Symbol	Stack	Output
1	A		A
2	*	*	A
3	(	* (	A
4	B	* (	A B
5	+	* ( +	A B
6	C	* ( +	A B C
7	)	*	A B C +
8	-	-	A B C + *
9	D	-	A B C + * D
10	/	- /	A B C + * D
11	(	- / (	A B C + * D
12	E	- / (	A B C + * D E
13	+	- / ( +	A B C + * D E
14	F	- / ( +	A B C + * D E F
15	)	- /	A B C + * D E F +
16	end		A B C + * D E F + / -

#### Solution

$A B C + * D E F + / -$

### Mnemonic

“Operators Stack, Operands Print”

### Question 2(a) OR [3 marks]

Differentiate between simple Queue and circular Queue.

#### Solution

Feature	Simple Queue	Circular Queue
Structure	Linear data structure	Linear data structure with connected ends
Memory	Inefficient memory usage due to unused space after dequeue	Efficient memory usage by reusing empty spaces
Implementation	Front always at index 0, rear increases	Front and rear move in circular fashion using modulo

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Simple Queue] --{} B[Front]
    B --{} C[...]
    C --{} D[Rear]

    E[Circular Queue] --{} F[Front]
    F --{} G[...]
    G --{} H[Rear]
    H --{} F
{Highlighting}
{Shaded}
```

### Mnemonic

“Simple Wastes, Circular Reuses”

### Question 2(b) OR [4 marks]

Explain concept of recursive function with suitable example.

#### Solution

Key Aspects	Description
Definition	A function that calls itself to solve a smaller instance of the same problem
Base Case	The condition where the function stops calling itself
Recursive Case	The condition where the function calls itself with a simpler version of the problem

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A["factorial(3)"] --{-}{-} B["3 * factorial(2)"]
    B --{-}{-} C["3 * 2 * factorial(1)"]
    C --{-}{-} D["3 * 2 * 1 * factorial(0)"]
    D --{-}{-} E["3 * 2 * 1 * 1"]
    E --{-}{-} F["3 * 2 * 1"]
    F --{-}{-} G["3 * 2"]
    G --{-}{-} H["6"]
{Highlighting}
{Shaded}
```

### Code:

```
def factorial(n):
    \# Base case
    if
n == 0:

        return 1
    \# Recursive case
    else:
        return n * factorial(n{-}1)

\# Example
result = factorial(5) \# 5! = 120
```

### Mnemonic

“Base Breaks, Recursion Returns”

## Question 2(c) OR [7 marks]

Develop a python code to implement Enqueue and Dequeue operation in Queue.

### Solution

#### Diagram:

Enqueue:

[1] [2] [3]    [1] [2] [3] [4]

Dequeue:

[1] [2] [3] [4]    [2] [3] [4]

#### Code:

```
class Queue:
    def __init__(self, size):
        self.queue = []
        self.size = size
        self.front = 0
        self.rear = {-}1
        self.count = 0

    def enqueue(self, item):
        if self.count {=} self.size:
```



```

        return "Queue is full"
    else:
        self.rear += 1
        self.queue.append(item)
        self.count += 1
        return "Enqueued " + str(item)

    def dequeue(self):
        if self.count {=} 0:
            return "Queue is empty"
        else:
            item = self.queue.pop(0)
            self.count {-=} 1
            return item

    def display(self):
        return self.queue

\# Test
q = Queue(5)
q.enqueue(10)
q.enqueue(20)
q.enqueue(30)
print(q.display()) \# [10, 20, 30]
print(q.dequeue()) \# 10
print(q.display()) \# [20, 30]

```

#### Mnemonic

“Enqueue at End, Dequeue from Start”

### Question 3(a) [3 marks]

Give Difference between Singly linked list and Circular linked list.

#### Solution

Feature	Singly Linked List	Circular Linked List
Last Node	Points to NULL	Points back to the first node
Traversal	Has a definite end	Can be traversed continuously
Memory	Each node needs one pointer	Each node needs one pointer

#### Diagram:

Singly: [1] [2] [3] NULL  
 Circular: [1] [2] [3]

#### Mnemonic

“Singly Stops, Circular Cycles”

### Question 3(b) [4 marks]

Explain concept of Doubly linked list.

#### Solution

#### Diagram:

NULL [Prev|1|Next] [Prev|2|Next] [Prev|3|Next] NULL

Feature	Description
Node Structure	Each node contains data and two pointers (previous and next)
Navigation	Can traverse in both forward and backward directions
Operations	Insertion and deletion can be performed from both ends
Memory Usage	Requires more memory than singly linked list due to extra pointer

#### Code:

```
class Node:
    def __init__(self, data):
        self.data = data
        self.prev = None
        self.next = None
```

#### Mnemonic

“Double Pointers, Double Directions”

### Question 3(c) [7 marks]

Write an algorithm for following operation on singly linked list: 1. To insert a node at the beginning of the list. 2. To insert the node at the end of the list.

#### Solution

##### Insert at Beginning:

##### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[Create new node]
    B --> C[Set new node's data]
    C --> D[Set new node's next to head]
    D --> E[Set head to new node]
    E --> F[End]
{Highlighting}
{Shaded}
```

##### Insert at End:

##### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[Create new node]
    B --> C[Set new node's data]
    C --> D[Set new node's next to NULL]
    D --> E{Is head NULL?}
    E -- Yes --> F[Set head to new node]
    E -- No --> G[Traverse to last node]
    G --> H[Set last node's next to new node]
    H --> I[End]
    I --> J[I]
{Highlighting}
{Shaded}
```

#### Code:

```
def insert\_at\_beginning(head, data):
    new\_node = Node(data)
    new\_node.next = head
    return new\_node  \# New head

def insert\_at\_end(head, data):
    new\_node = Node(data)
    new\_node.next = None

    \# If linked list is empty
    if head is None:
        return new\_node

    \# Traverse to the last node
    temp = head
    while temp.next:
        temp = temp.next

    \# Link the last node to new node
    temp.next = new\_node
    return head
```

### Mnemonic

“Begin: New Leads Old, End: Old Leads New”

## Question 3(a) OR [3 marks]

List different operations performed on singly linked list.

### Solution

#### Operations on Singly Linked List

1. Insertion (at beginning, middle, end)
2. Deletion (from beginning, middle, end)
3. Traversal (visiting each node)
4. Searching (finding a specific node)
5. Updating (modifying node data)

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[Linked List Operations]
    A --> B[Insertion]
    A --> C[Deletion]
    A --> D[Traversal]
    A --> E[Searching]
    A --> F[Updating]
{Highlighting}
{Shaded}
```

### Mnemonic

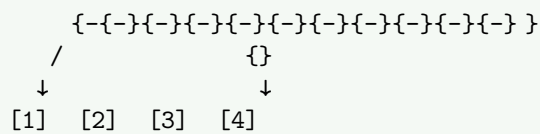
“Insert Delete Traversal Search Update”

### Question 3(b) OR [4 marks]

Explain concept of Circular linked list.

#### Solution

##### Diagram:



Feature	Description
Structure	Last node points to the first node instead of NULL
Advantage	Allows continuous traversal through all nodes
Applications	Round robin scheduling, circular buffer implementation
Operations	Insertion and deletion similar to singly linked list with special handling for the last node

##### Code:

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None

\# Creating a circular linked list with 3 nodes
head = Node(1)
node2 = Node(2)
node3 = Node(3)

head.next = node2
node2.next = node3
node3.next = head \# Makes it circular
```

#### Mnemonic

“Last Links to First”

### Question 3(c) OR [7 marks]

List application of linked list. Write an algorithm to count the number of nodes in singly linked list.

#### Solution

##### Applications of Linked List

1. Implementation of stacks and queues
2. Dynamic memory allocation
3. Undo functionality in applications
4. Hash tables (chaining)
5. Adjacency lists for graphs

### Algorithm to Count Nodes:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[Initialize count = 0]
    B --> C[Initialize temp = head]
    C --> D{temp != NULL?}
    D -- Yes --> E[increment count]
    D -- No --> F[Return count]
    E --> G[temp = temp.next]
    G --> D
{Highlighting}
{Shaded}
```

#### Code:

```
def count\_nodes(head):
    count = 0
    temp = head

    while temp:
        count += 1
        temp = temp.next

    return count

\# Example usage
\# Assuming head points to the first node of a linked list
total\_nodes = count\_nodes(head)
print(f"Total nodes: \{total\_nodes\}")
```

#### Mnemonic

“Count While Moving”

### Question 4(a) [3 marks]

Compare Linear search with Binary search.

#### Solution

Feature	Linear Search	Binary Search
Data Arrangement	Works on both sorted and unsorted data	Works only on sorted data
Time Complexity	$O(n)$	$O(\log n)$
Implementation	Simpler	More complex
Best For	Small datasets or unsorted data	Large sorted datasets

**Diagram:**

Linear: [1] [2] [3] [4] [5] [6] [7] [8]  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 Sequential checking

Binary: [1] [2] [3] [4] [5] [6] [7] [8]  
 ↓  
 Check middle  
 / {}  
 / {}  
 Lower half Upper half

**Mnemonic**

“Linear Looks at All, Binary Breaks in Half”

**Question 4(b) [4 marks]**

Write an algorithm for selection sort method.

**Solution****Diagram:**

Initial: [5, 3, 8, 1, 2]  
 Pass 1: [1, 3, 8, 5, 2] (Find min = 1, swap with 5)  
 Pass 2: [1, 2, 8, 5, 3] (Find min = 2, swap with 3)  
 Pass 3: [1, 2, 3, 5, 8] (Find min = 3, swap with 8)  
 Pass 4: [1, 2, 3, 5, 8] (Find min = 5, already in place)

**Algorithm:****Mermaid Diagram (Code)**

```
{Shaded}
{Highlighting}[]
graph LR
  A[Start] --> B[For i = 0 to n-1]
  B --> C[Find minimum element in unsorted portion]
  C --> D[Swap minimum with first element of unsorted portion]
  D --> E[End]
{Highlighting}
{Shaded}
```

**Code Outline:**

```
def selection_sort(arr):
    n = len(arr)

    for i in range(n):
        min_idx = i

        # Find the minimum element in unsorted array
        for j in range(i+1, n):
            if arr[j] < arr[min_idx]:
                min_idx = j

        # Swap the found minimum element with the first element
        arr[i], arr[min_idx] = arr[min_idx], arr[i]
```

### Mnemonic

“Find Minimum, Swap Position”

### Question 4(c) [7 marks]

Develop a python code to sort following list in ascending order using Bubble sort method. list1=[5,4,3,2,1,0]

#### Solution

##### Diagram:

Initial: [5, 4, 3, 2, 1, 0]  
Pass 1: [4, 3, 2, 1, 0, 5]  
Pass 2: [3, 2, 1, 0, 4, 5]  
Pass 3: [2, 1, 0, 3, 4, 5]  
Pass 4: [1, 0, 2, 3, 4, 5]  
Pass 5: [0, 1, 2, 3, 4, 5]

##### Code:

```
def bubble\_sort(arr):  
    n = len(arr)  
  
    \# Traverse through all array elements  
    for i in range(n):  
        \# Last i elements are already in place  
        for j in range(0, n{-}i{-}1):  
            \# Swap if current element is greater than next element  
            if arr[j] > arr[j+1]:  
                arr[j], arr[j+1] = arr[j+1], arr[j]  
  
    return arr  
  
\# Input list  
list1 = [5, 4, 3, 2, 1, 0]  
  
\# Sorting the list  
sorted\_list = bubble\_sort(list1)  
  
\# Displaying the result  
print("Sorted list:", sorted\_list)  
\# Output: Sorted list: [0, 1, 2, 3, 4, 5]
```

### Mnemonic

“Bubble Biggest Upward”

### Question 4(a) OR [3 marks]

Define sorting. List different sorting methods.

#### Solution

Definition	Sorting Methods
Sorting is the process of arranging data in a specified order (ascending or descending)	1. Bubble Sort 2. Selection Sort 3. Insertion Sort 4. Merge Sort 5. Quick Sort 6. Heap Sort 7. Radix Sort

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[Sorting Algorithms]
    A --> B[Comparison-based]
    A --> C[Non-comparison]
    B --> D[Bubble Sort]
    B --> E[Selection Sort]
    B --> F[Insertion Sort]
    B --> G[Merge Sort]
    B --> H[Quick Sort]
    C --> I[Counting Sort]
    C --> J[Radix Sort]
    C --> K[Bucket Sort]
{Highlighting}
{Shaded}
```

### Mnemonic

“Better Sort Improves Many Query Results”

## Question 4(b) OR [4 marks]

Write an algorithm for Insertion sort method.

### Solution

#### Diagram:

Initial: [5, 2, 4, 6, 1, 3]  
Pass 1: [2, 5, 4, 6, 1, 3] (Insert 2 before 5)  
Pass 2: [2, 4, 5, 6, 1, 3] (Insert 4 before 5)  
Pass 3: [2, 4, 5, 6, 1, 3] (6 is already in place)  
Pass 4: [1, 2, 4, 5, 6, 3] (Insert 1 at beginning)  
Pass 5: [1, 2, 3, 4, 5, 6] (Insert 3 after 2)

#### Algorithm:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[For i = 1 to n-1]
    B --> C["Set key = arr[i]"]
    C --> D["Set j = i-1"]
    D --> E["j >= 0 and arr[j] > key?"]
    E -- Yes --> F[Move element right]
    F --> G[Decrement j]
    G --> E
    E -- No --> H[Place key at correct position]
    H --> I[End]
{Highlighting}
{Shaded}
```

#### Code Outline:

```
def insertion_sort(arr):
    for i in range(1, len(arr)):
```



```

key = arr[i]
j = i {-} 1

\# Move elements that are greater than key
\# to one position ahead of their current position
while j {=} 0 and arr[j] {>} key:
    arr[j + 1] = arr[j]
    j {-=} 1

arr[j + 1] = key

```

### Mnemonic

“Take Card, Insert In Order”

### Question 4(c) OR [7 marks]

Develop a python code to sort following list in ascending order using selection sort method. list1=[6,3,25,8,-1,55,0]

### Solution

#### Diagram:

```

Initial: [6, 3, 25, 8, {-1, 55, 0}]
Pass 1:  [{-1, 3, 25, 8, 6, 55, 0}] (Find min = {-}1, swap with 6)}
Pass 2:  [{-1, 0, 25, 8, 6, 55, 3}] (Find min = 0, swap with 3)}
Pass 3:  [{-1, 0, 3, 8, 6, 55, 25}] (Find min = 3, swap with 25)}
Pass 4:  [{-1, 0, 3, 6, 8, 55, 25}] (Find min = 6, swap with 8)}
Pass 5:  [{-1, 0, 3, 6, 8, 55, 25}] (Find min = 8, already in place)}
Pass 6:  [{-1, 0, 3, 6, 8, 25, 55}] (Find min = 25, swap with 55)}

```

#### Code:

```

def selection\_sort(arr):
    n = len(arr)

    for i in range(n):
        \# Find the minimum element in remaining unsorted array
        min\_idx = i
        for j in range(i+1, n):
            if arr[j] {<} arr[min\_idx]:
                min\_idx = j

        \# Swap the found minimum element with the first element
        arr[i], arr[min\_idx] = arr[min\_idx], arr[i]

    return arr

\# Input list
list1 = [6, 3, 25, 8, {-}1, 55, 0]

\# Sorting the list
sorted\_list = selection\_sort(list1)

\# Displaying the result
print("Sorted list:", sorted\_list)
\# Output: Sorted list: [{-1, 0, 3, 6, 8, 25, 55]}

```

### Mnemonic

“Select Smallest, Shift to Start”

### Question 5(a) [3 marks]

Define following terms regarding Tree data structure: 1. Forest 2. Root node 3. Leaf node

#### Solution

Term	Definition
Forest	Collection of disjoint trees (multiple trees without connections between them)
Root Node	Topmost node of a tree with no parent, from which all other nodes are descended
Leaf Node	Node with no children (terminal node at the bottom of the tree)

#### Diagram:

Forest:      Tree1      Tree2      Tree3  
              / {        /        |}  
              / {        /        |}

Root:        [R]  
              / {}  
              / {}

Leaf:    [A]    [B]    [L]    [L]  
                              No children

### Mnemonic

“Forest has Many Roots, Roots Lead All, Leaves End All”

### Question 5(b) [4 marks]

Draw Binary search tree for 78,58,82,15,66,80,99 and write In-order traversal for the tree.

#### Solution

#### Binary Search Tree:

```
      78
     / {}
    / {}
   58  82
  / {} / {}
15 66 80 99
```

#### In-order Traversal:

Step	Visit Order
1	Visit left subtree of 78
2	Visit left subtree of 58
3	Visit 15
4	Visit 58
5	Visit 66
6	Visit 78
7	Visit left subtree of 82
8	Visit 80

9	Visit 82
10	Visit 99

In-order Traversal Result: 15, 58, 66, 78, 80, 82, 99

### Mnemonic

“Left, Root, Right”

## Question 5(c) [7 marks]

Write an algorithm for following operation: 1. Insertion of Node in Binary Tree 2. Deletion of Node in Binary Tree

### Solution

#### Insertion Algorithm:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[Create new node with given data]
    B --> C[Is root NULL?]
    C -- Yes --> D[Set root to new node]
    C -- No --> E[Find position using level order traversal]
    E --> F[Insert node at first vacant position]
    F --> G[End]
    G --> H[ ]
    style H fill:none,stroke:none
{Highlighting}
{Shaded}
```

#### Deletion Algorithm:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Start] --> B[Is tree empty?]
    B -- Yes --> C[Return]
    B -- No --> D[Find node to delete]
    D --> E[Find deepest rightmost node]
    E --> F[Replace node to delete with deepest rightmost node]
    F --> G[Delete deepest rightmost node]
    G --> H[End]
    H --> I[ ]
    style I fill:none,stroke:none
{Highlighting}
{Shaded}
```

#### Code:

```
class Node:
    def __init__(self, data):
        self.data = data
        self.left = None
        self.right = None

\# Insertion in Binary Tree
def insert(root, data):
    if root is None:
        return Node(data)
```

```

\# Level order traversal to find vacant position
queue = []
queue.append(root)

while queue:
    temp = queue.pop(0)

    if temp.left is None:
        temp.left = Node(data)
        break
    else:
        queue.append(temp.left)

    if temp.right is None:
        temp.right = Node(data)
        break
    else:
        queue.append(temp.right)

return root

\# Deletion in Binary Tree
def delete\_node(root, key):
    if root is None:
        return None

    if root.left is None and root.right is None:
        if root.data == key:
            return None
        else:
            return root

    \# Find the node to delete
    key\_node = None
    \# Find the deepest node
    last = None
    parent = None

    \# Level order traversal
    queue = []
    queue.append(root)

    while queue:
        temp = queue.pop(0)

        if temp.data == key:
            key\_node = temp

        if temp.left:
            parent = temp
            queue.append(temp.left)
            last = temp.left

        if temp.right:
            parent = temp
            queue.append(temp.right)
            last = temp.right

    if key\_node:
        \# Replace with deepest node's data
        key\_node.data = last.data

```

```

    \# Delete the deepest node
    if parent.right == last:
        parent.right = None
    else:
        parent.left = None

return root

```

### Mnemonic

“Insert at Empty, Delete by Swap and Remove”

### Question 5(a) OR [3 marks]

Define following terms regarding Tree data structure: 1. In-degree 2. Out-degree 3. Depth

### Solution

Term	Definition
In-degree	Number of edges coming into a node (always 1 for each node except root node in a tree)
Out-degree	Number of edges going out from a node (number of children)
Depth	Length of the path from root to the node (number of edges in path)

### Diagram:

```

      A (Root, Depth 0)
     / {}
    /  {}
   B   C (Depth 1)
  / {}   {}
 D  E   F (Depth 2)

```

Node	In-degree	Out-degree
A	0	2
B	1	2
C	1	1
D	1	0
E	1	0
F	1	0

### Mnemonic

“In Counts Parents, Out Counts Children, Depth Counts Edges from Root”

### Question 5(b) OR [4 marks]

Write Preorder and postorder traversal of following Binary tree.

Binary Tree:

```

      100
     / {}
    /  {}
   20  200
  / {} / {}
10 30 150 300

```

## Solution

Traversal	Order	Result
Preorder	Root, Left, Right	100, 20, 10, 30, 200, 150, 300
Postorder	Left, Right, Root	10, 30, 20, 150, 300, 200, 100

### Preorder Visualization:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[100] --{-}{-}{ B[Visit 100]}
    B --{-}{-}{ C[Visit left subtree]}
    C --{-}{-}{ D[Visit 20]}
    D --{-}{-}{ E[Visit 10]}
    E --{-}{-}{ F[Visit 30]}
    F --{-}{-}{ G[Visit right subtree]}
    G --{-}{-}{ H[Visit 200]}
    H --{-}{-}{ I[Visit 150]}
    I --{-}{-}{ J[Visit 300]}
{Highlighting}
{Shaded}
```

### Postorder Visualization:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph TD
    A[100] --{-}{-}{ B[Visit left subtree]}
    B --{-}{-}{ C[Visit 10]}
    C --{-}{-}{ D[Visit 30]}
    D --{-}{-}{ E[Visit 20]}
    E --{-}{-}{ F[Visit right subtree]}
    F --{-}{-}{ G[Visit 150]}
    G --{-}{-}{ H[Visit 300]}
    H --{-}{-}{ I[Visit 200]}
    I --{-}{-}{ J[Visit 100]}
{Highlighting}
{Shaded}
```

## Mnemonic

- Preorder: “Root First, Then Children”
- Postorder: “Children First, Then Root”

## Question 5(c) OR [7 marks]

Develop a program to implement construction of Binary Search Tree.

## Solution

### Diagram:

#### Mermaid Diagram (Code)

```
{Shaded}
{Highlighting}[]
graph LR
    A[Root] --{-}{-}{|Insert 50| B[50]}
```

```

B {-{-}{}|Insert 30| C[50]}
C {-.{-}{| D[30]}
C {-{-}{}|Insert 70| E[50]}
E {-.{-}{| F[30]}
E {-{-}{| G[70]}
G {-{-}{|Insert 20| H[50]}
H {-.{-}{| I[30]}
I {-.{-}{| J[20]}
H {-{-}{| K[70]}

```

{Highlighting}  
{Shaded}

**Code:**

```

class Node:
    def \_\_init\_\_(self, key):
        self.key = key
        self.left = None
        self.right = None

def insert(root, key):
    \# If the tree is empty, return a new node
    if root is None:
        return Node(key)

    \# Otherwise, recur down the tree
    if key < root.key:
        root.left = insert(root.left, key)
    else:
        root.right = insert(root.right, key)

    \# Return the unchanged node pointer
    return root

def inorder(root):
    if root:
        inorder(root.left)
        print(root.key, end=" ")
        inorder(root.right)

def preorder(root):
    if root:
        print(root.key, end=" ")
        preorder(root.left)
        preorder(root.right)

def postorder(root):
    if root:
        postorder(root.left)
        postorder(root.right)
        print(root.key, end=" ")

\# Driver program to test the above functions
def main():
    \# Create BST with these elements: 50, 30, 20, 40, 70, 60, 80
    root = None
    elements = [50, 30, 20, 40, 70, 60, 80]

    for element in elements:
        root = insert(root, element)

    \# Print traversals

```

```
print("Inorder traversal: ", end="")
inorder(root)
print("\nPreorder traversal: ", end="")
preorder(root)
print("\nPostorder traversal: ", end="")
postorder(root)
```

```
\# Run the program
main()
```

#### Example Output:

```
Inorder traversal: 20 30 40 50 60 70 80
Preorder traversal: 50 30 20 40 70 60 80
Postorder traversal: 20 40 30 60 80 70 50
```

#### Mnemonic

“Insert Smaller Left, Larger Right”