

## Q.1 [14 marks]

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Fill in the blanks/MCQs using appropriate choice from the given options

### Q1.1 [1 mark]

$$\log_3 1 =$$

**Answer:** d. 0

**Solution:**

For any base  $a > 0, a \neq 1$ :  $\log_a 1 = 0$

Therefore:  $\log_3 1 = 0$

### Q1.2 [1 mark]

If  $f(x) = e^{x-1}$  then  $f(1) =$

**Answer:** c. 1

**Solution:**

$$f(x) = e^{x-1}$$

$$f(1) = e^{1-1} = e^0 = 1$$

### Q1.3 [1 mark]

$$\log_5 125 =$$

**Answer:** b. 3

**Solution:**

$$\log_5 125 = \log_5 5^3 = 3$$

Since  $5^3 = 125$

### Q1.4 [1 mark]

If  $f(x) = x^3 - 7$  then  $f(-2) =$

**Answer:** c. -15

**Solution:**

$$f(x) = x^3 - 7$$

$$f(-2) = (-2)^3 - 7 = -8 - 7 = -15$$

### Q1.5 [1 mark]

**Principal period of  $\cos x$  is**

**Answer:** c.  $2\pi$

**Solution:**

The cosine function repeats every  $2\pi$  radians, so its principal period is  $2\pi$ .

**Q1.6 [1 mark]**

$150^\circ =$

**Answer:** a.  $\frac{5\pi}{6}$

**Solution:**

Converting degrees to radians:  $150^\circ = 150 \times \frac{\pi}{180} = \frac{5\pi}{6}$

**Q1.7 [1 mark]**

$\sin^{-1} x + \cos^{-1} x =$

**Answer:** a.  $\frac{\pi}{2}$

**Solution:**

This is a standard identity:  $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}$  for  $x \in [-1, 1]$

**Q1.8 [1 mark]**

$(1,0,0) \times (1,0,0) =$

**Answer:** d. (0,0,0)

**Solution:**

Cross product of any vector with itself is zero vector:

$(1, 0, 0) \times (1, 0, 0) = (0, 0, 0)$

**Q1.9 [1 mark]**

If  $\vec{a} = 4\hat{i} - 3\hat{j}$  then  $|\vec{a}| =$

**Answer:** b. 5

**Solution:**

$|\vec{a}| = \sqrt{4^2 + (-3)^2} = \sqrt{16 + 9} = \sqrt{25} = 5$

**Q1.10 [1 mark]**If a line makes an angle  $45^\circ$  with positive x-axis then slope of the line is

**Answer:** c. 1

**Solution:**

Slope  $m = \tan(45^\circ) = 1$

**Q1.11 [1 mark]**Radius of the circle  $x^2 + y^2 = 4$  is

**Answer:** d. 2

**Solution:**

Standard form:  $x^2 + y^2 = r^2$

Comparing:  $r^2 = 4$ , so  $r = 2$

**Q1.12 [1 mark]**

$$\lim_{x \rightarrow 0} \frac{e^x - 1}{x} =$$

**Answer:** a. 1**Solution:**

This is a standard limit:  $\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$

**Q1.13 [1 mark]**

$$\lim_{x \rightarrow 0} \frac{\sin 3x}{x} =$$

**Answer:** d. 3**Solution:**

$$\lim_{x \rightarrow 0} \frac{\sin 3x}{x} = \lim_{x \rightarrow 0} \frac{\sin 3x}{3x} \times 3 = 1 \times 3 = 3$$

**Q1.14 [1 mark]**

$$\lim_{n \rightarrow \infty} \frac{5n+4}{4n+5} =$$

**Answer:** c. 5/4**Solution:**

$$\lim_{n \rightarrow \infty} \frac{5n+4}{4n+5} = \lim_{n \rightarrow \infty} \frac{5+\frac{4}{n}}{4+\frac{5}{n}} = \frac{5}{4}$$

**Q.2 (A) [6 marks]**

Attempt any two

**Q2(A).1 [3 marks]**

Find value:  $\begin{vmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{vmatrix}$

**Answer:** 0**Solution:**

$$\begin{vmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{vmatrix} = 1(5 \times 9 - 6 \times 8) - 2(4 \times 9 - 6 \times 7) + 3(4 \times 8 - 5 \times 7)$$

$$= 1(45 - 48) - 2(36 - 42) + 3(32 - 35)$$

$$= 1(-3) - 2(-6) + 3(-3)$$

$$= -3 + 12 - 9 = 0$$

**Q2(A).2 [3 marks]****Prove that:**  $\log\left(\frac{x^p}{x^q}\right) + \log\left(\frac{x^q}{x^r}\right) + \log\left(\frac{x^r}{x^p}\right) = 0$ **Solution:**

$$\text{LHS} = \log\left(\frac{x^p}{x^q}\right) + \log\left(\frac{x^q}{x^r}\right) + \log\left(\frac{x^r}{x^p}\right)$$

Using logarithm properties:

$$= \log(x^p) - \log(x^q) + \log(x^q) - \log(x^r) + \log(x^r) - \log(x^p)$$

$$= p \log x - q \log x + q \log x - r \log x + r \log x - p \log x$$

$$= 0 = \text{RHS}$$

**Q2(A).3 [3 marks]****Find value:**  $\tan(75^\circ)$ 

$$\text{Answer: } 2 + \sqrt{3}$$

**Solution:**

$$\tan(75^\circ) = \tan(45^\circ + 30^\circ)$$

$$\text{Using } \tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}:$$

$$\tan(75^\circ) = \frac{\tan 45^\circ + \tan 30^\circ}{1 - \tan 45^\circ \tan 30^\circ} = \frac{1 + \frac{1}{\sqrt{3}}}{1 - 1 \times \frac{1}{\sqrt{3}}} = \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$$

$$= \frac{\frac{\sqrt{3}+1}{\sqrt{3}}}{\frac{\sqrt{3}-1}{\sqrt{3}}} = \frac{\sqrt{3}+1}{\sqrt{3}-1} = \frac{(\sqrt{3}+1)^2}{(\sqrt{3}-1)(\sqrt{3}+1)} = \frac{3+2\sqrt{3}+1}{3-1} = \frac{4+2\sqrt{3}}{2} = 2 + \sqrt{3}$$

**Q.2 (B) [8 marks]****Attempt any two****Q2(B).1 [4 marks]****Prove that:**  $\frac{1}{\log_{12} 120} + \frac{1}{\log_2 120} + \frac{1}{\log_5 120} = 1$ **Solution:**Using change of base formula:  $\frac{1}{\log_a b} = \log_b a$ 

$$\text{LHS} = \log_{120} 12 + \log_{120} 2 + \log_{120} 5$$

Using logarithm properties:

$$= \log_{120}(12 \times 2 \times 5) = \log_{120} 120 = 1 = \text{RHS}$$

**Q2(B).2 [4 marks]**

$$\text{Solve: } \begin{vmatrix} x & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 3 \end{vmatrix} = 3$$

**Solution:**

Expanding along third row:

$$\begin{vmatrix} x & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 3 \end{vmatrix} = 3 \begin{vmatrix} x & 1 \\ 1 & 2 \end{vmatrix}$$

$$= 3(2x - 1) = 6x - 3$$

$$\text{Given: } 6x - 3 = 3$$

$$6x = 6$$

$$x = 1$$

**Q2(B).3 [4 marks]**

If  $f(x) = \frac{1-x}{1+x}$  prove that: (i)  $f(x) + f\left(\frac{1}{x}\right) = 0$  (ii)  $f(x) \times f(-x) = 1$

**Solution:**

$$\text{Given: } f(x) = \frac{1-x}{1+x}$$

$$\text{(i) } f\left(\frac{1}{x}\right) = \frac{1-\frac{1}{x}}{1+\frac{1}{x}} = \frac{\frac{x-1}{x}}{\frac{x+1}{x}} = \frac{x-1}{x+1} = -\frac{1-x}{1+x} = -f(x)$$

$$\text{Therefore: } f(x) + f\left(\frac{1}{x}\right) = f(x) + (-f(x)) = 0$$

$$\text{(ii) } f(-x) = \frac{1-(-x)}{1+(-x)} = \frac{1+x}{1-x}$$

$$f(x) \times f(-x) = \frac{1-x}{1+x} \times \frac{1+x}{1-x} = 1$$

**Q.3 (A) [6 marks]**

Attempt any two

**Q3(A).1 [3 marks]**

Prove that:  $\frac{\sin(180^\circ - x) + \text{cosec}(180^\circ - x) + \tan(180^\circ + x)}{\cos(90^\circ + x) + \sec(90^\circ + x) + \cot(90^\circ + x)} = -3$

**Solution:**

Using trigonometric identities:

- $\sin(180^\circ - x) = \sin x$
- $\text{cosec}(180^\circ - x) = \text{cosec} x$
- $\tan(180^\circ + x) = \tan x$
- $\cos(90^\circ + x) = -\sin x$
- $\sec(90^\circ + x) = -\text{cosec} x$
- $\cot(90^\circ + x) = -\tan x$

$$\text{Numerator} = \sin x + \text{cosec} x + \tan x$$

$$\text{Denominator} = -\sin x - \text{cosec} x - \tan x = -(\sin x + \text{cosec} x + \tan x)$$

Therefore:  $\frac{\sin x + \csc x + \tan x}{-(\sin x + \csc x + \tan x)} = -1 \neq -3$

**Note:** There appears to be an error in the problem statement or expected answer.

### Q3(A).2 [3 marks]

**Prove that:**  $\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{2}\right) = 45^\circ$

**Solution:**

Using  $\tan^{-1} A + \tan^{-1} B = \tan^{-1}\left(\frac{A+B}{1-AB}\right)$ :

$$\begin{aligned}\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{2}\right) &= \tan^{-1}\left(\frac{\frac{1}{3} + \frac{1}{2}}{1 - \frac{1}{3} \times \frac{1}{2}}\right) \\ &= \tan^{-1}\left(\frac{\frac{5}{6}}{1 - \frac{1}{6}}\right) = \tan^{-1}\left(\frac{\frac{5}{6}}{\frac{5}{6}}\right) = \tan^{-1}(1) = 45^\circ\end{aligned}$$

### Q3(A).3 [3 marks]

**Find out equation of the line whose X-intercept is 3 and Y-intercept is 2.**

**Solution:**

Using intercept form:  $\frac{x}{a} + \frac{y}{b} = 1$

Where  $a = 3$  (x-intercept) and  $b = 2$  (y-intercept)

$$\frac{x}{3} + \frac{y}{2} = 1$$

Multiplying by 6:  $2x + 3y = 6$

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## Q.3 (B) [8 marks]

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**Attempt any two**

### Q3(B).1 [4 marks]

**Prove that:**  $\tan(70^\circ) = \frac{\cos(25^\circ) + \sin(25^\circ)}{\cos(25^\circ) - \sin(25^\circ)}$

**Solution:**

$$\text{RHS} = \frac{\cos(25^\circ) + \sin(25^\circ)}{\cos(25^\circ) - \sin(25^\circ)}$$

Dividing numerator and denominator by  $\cos(25^\circ)$ :

$$= \frac{1 + \tan(25^\circ)}{1 - \tan(25^\circ)}$$

Using  $\tan(45^\circ + \theta) = \frac{1 + \tan \theta}{1 - \tan \theta}$ :

$$= \tan(45^\circ + 25^\circ) = \tan(70^\circ) = \text{LHS}$$

### Q3(B).2 [4 marks]

**Prove that:**  $\frac{\sin \theta + \sin 2\theta + \sin 3\theta}{\cos \theta + \cos 2\theta + \cos 3\theta} = \tan 2\theta$

**Solution:**

Using sum-to-product formulas:

$$\text{Numerator: } \sin \theta + \sin 3\theta + \sin 2\theta = 2 \sin 2\theta \cos \theta + \sin 2\theta = \sin 2\theta(2 \cos \theta + 1)$$

$$\text{Denominator: } \cos \theta + \cos 3\theta + \cos 2\theta = 2 \cos 2\theta \cos \theta + \cos 2\theta = \cos 2\theta(2 \cos \theta + 1)$$

$$\text{Therefore: } \frac{\sin 2\theta(2 \cos \theta + 1)}{\cos 2\theta(2 \cos \theta + 1)} = \frac{\sin 2\theta}{\cos 2\theta} = \tan 2\theta$$

**Q3(B).3 [4 marks]**

If  $\vec{a} = (1, 2, 3)$ ,  $\vec{b} = (4, 0, 0)$  and  $\vec{c} = (2, 0, 1)$  find  $2\vec{a} + 3\vec{b} - 5\vec{c}$

**Solution:**

$$2\vec{a} = 2(1, 2, 3) = (2, 4, 6)$$

$$3\vec{b} = 3(4, 0, 0) = (12, 0, 0)$$

$$5\vec{c} = 5(2, 0, 1) = (10, 0, 5)$$

$$\begin{aligned} 2\vec{a} + 3\vec{b} - 5\vec{c} &= (2, 4, 6) + (12, 0, 0) - (10, 0, 5) \\ &= (2 + 12 - 10, 4 + 0 - 0, 6 + 0 - 5) \\ &= (4, 4, 1) \end{aligned}$$

**Q.4 (A) [6 marks]**

Attempt any two

**Q4(A).1 [3 marks]**

If the vectors  $\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$  and  $\vec{b} = 2\hat{i} + m\hat{j} - 4\hat{k}$  are perpendicular, find  $m$ .

**Solution:**

For perpendicular vectors:  $\vec{a} \cdot \vec{b} = 0$

$$\vec{a} \cdot \vec{b} = (1)(2) + (-2)(m) + (3)(-4) = 2 - 2m - 12 = -10 - 2m$$

Setting equal to zero:  $-10 - 2m = 0$

$$2m = -10$$

$$m = -5$$

**Q4(A).2 [3 marks]**

Find the direction cosines and direction angles of the vector  $\vec{a} = 5\hat{i} - 12\hat{k}$

**Solution:**

$$\vec{a} = 5\hat{i} + 0\hat{j} - 12\hat{k}$$

$$\text{Magnitude: } |\vec{a}| = \sqrt{5^2 + 0^2 + (-12)^2} = \sqrt{25 + 144} = \sqrt{169} = 13$$

Direction cosines:

$$\bullet \quad l = \frac{5}{13}$$

- $m = \frac{0}{13} = 0$
- $n = \frac{-12}{13}$

Direction angles:

- $\alpha = \cos^{-1}\left(\frac{5}{13}\right)$
- $\beta = \cos^{-1}(0) = 90^\circ$
- $\gamma = \cos^{-1}\left(\frac{-12}{13}\right)$

### Q4(A).3 [3 marks]

Find out equation of the circle having center at  $(2, -3)$  and radius 3.

**Solution:**

Standard form:  $(x - h)^2 + (y - k)^2 = r^2$

Where  $(h, k) = (2, -3)$  and  $r = 3$

$$(x - 2)^2 + (y + 3)^2 = 9$$

Expanding:  $x^2 - 4x + 4 + y^2 + 6y + 9 = 9$

$$x^2 + y^2 - 4x + 6y + 4 = 0$$

## Q.4 (B) [8 marks]

Attempt any two

### Q4(B).1 [4 marks]

Show that the angle between vectors  $\vec{a} = \hat{i} + 2\hat{j}$  and  $\vec{b} = \hat{i} + \hat{j} + 3\hat{k}$  is  $\sin^{-1} \sqrt{\frac{46}{55}}$

**Solution:**

$$\vec{a} \cdot \vec{b} = (1)(1) + (2)(1) + (0)(3) = 1 + 2 = 3$$

$$|\vec{a}| = \sqrt{1^2 + 2^2} = \sqrt{5}$$

$$|\vec{b}| = \sqrt{1^2 + 1^2 + 3^2} = \sqrt{11}$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}||\vec{b}|} = \frac{3}{\sqrt{5}\sqrt{11}} = \frac{3}{\sqrt{55}}$$

$$\sin^2 \theta = 1 - \cos^2 \theta = 1 - \frac{9}{55} = \frac{46}{55}$$

$$\text{Therefore: } \theta = \sin^{-1} \sqrt{\frac{46}{55}}$$

### Q4(B).2 [4 marks]

Under effect of the forces  $2\hat{i} + \hat{j} + \hat{k}$  and  $\hat{i} + 3\hat{j} - \hat{k}$  a particle moves from the point  $(1, 2, -3)$  to the point  $(5, 3, 7)$ . Find out work done.

**Solution:**

$$\text{Net force: } \vec{F} = (2\hat{i} + \hat{j} + \hat{k}) + (\hat{i} + 3\hat{j} - \hat{k}) = 3\hat{i} + 4\hat{j}$$



Displacement:  $\vec{s} = (5, 3, 7) - (1, 2, -3) = (4, 1, 10)$

Work done:  $W = \vec{F} \cdot \vec{s} = (3)(4) + (4)(1) + (0)(10) = 12 + 4 = 16$  units

### Q4(B).3 [4 marks]

**Evaluate:**  $\lim_{x \rightarrow 0} \frac{2^x - 5^x}{x}$

**Solution:**

Using L'Hôpital's rule or the derivative definition:

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{2^x - 5^x}{x} &= \lim_{x \rightarrow 0} \frac{2^x \ln 2 - 5^x \ln 5}{1} \\ &= 2^0 \ln 2 - 5^0 \ln 5 = \ln 2 - \ln 5 = \ln \left( \frac{2}{5} \right) \end{aligned}$$


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### Q.5 (A) [6 marks]

Attempt any two

#### Q5(A).1 [3 marks]

**Evaluate:**  $\lim_{x \rightarrow 0} \left( 1 + \frac{3x}{7} \right)^{\frac{1}{x}}$

**Solution:**

Let  $y = \left( 1 + \frac{3x}{7} \right)^{\frac{1}{x}}$

Taking natural log:  $\ln y = \frac{1}{x} \ln \left( 1 + \frac{3x}{7} \right)$

$$\lim_{x \rightarrow 0} \ln y = \lim_{x \rightarrow 0} \frac{\ln \left( 1 + \frac{3x}{7} \right)}{x}$$

Using L'Hôpital's rule:  $= \lim_{x \rightarrow 0} \frac{\frac{3/7}{1 + \frac{3x}{7}}}{1} = \frac{3}{7}$

Therefore:  $\lim_{x \rightarrow 0} y = e^{3/7}$

#### Q5(A).2 [3 marks]

**Evaluate:**  $\lim_{x \rightarrow 3} \frac{x^2 - 5x + 6}{x^2 - 9}$

**Solution:**

Factoring numerator:  $x^2 - 5x + 6 = (x - 2)(x - 3)$

Factoring denominator:  $x^2 - 9 = (x - 3)(x + 3)$

$$\lim_{x \rightarrow 3} \frac{x^2 - 5x + 6}{x^2 - 9} = \lim_{x \rightarrow 3} \frac{(x-2)(x-3)}{(x-3)(x+3)} = \lim_{x \rightarrow 3} \frac{x-2}{x+3} = \frac{3-2}{3+3} = \frac{1}{6}$$

#### Q5(A).3 [3 marks]

**Evaluate:**  $\lim_{x \rightarrow 0} \frac{\sqrt{4+x} - 2}{x}$

**Solution:**

Rationalizing the numerator:

$$\lim_{x \rightarrow 0} \frac{\sqrt{4+x}-2}{x} \times \frac{\sqrt{4+x}+2}{\sqrt{4+x}+2}$$

$$= \lim_{x \rightarrow 0} \frac{(4+x)-4}{x(\sqrt{4+x}+2)} = \lim_{x \rightarrow 0} \frac{x}{x(\sqrt{4+x}+2)} = \lim_{x \rightarrow 0} \frac{1}{\sqrt{4+x}+2} = \frac{1}{2+2} = \frac{1}{4}$$


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## Q.5 (B) [8 marks]

Attempt any two

### Q5(B).1 [4 marks]

Find out equation of the line passing through points (1, 2) and (2, 1).

**Solution:**

Using two-point form:  $\frac{y-y_1}{y_2-y_1} = \frac{x-x_1}{x_2-x_1}$

$$\frac{y-2}{1-2} = \frac{x-1}{2-1}$$

$$\frac{y-2}{-1} = \frac{x-1}{1}$$

$$y-2 = -(x-1) = -x+1$$

$$x+y=3$$

### Q5(B).2 [4 marks]

Find equation of the line that passes through  $(-3, 2)$  and parallel to the line  $x - 2y + 1 = 0$

**Solution:**

The given line  $x - 2y + 1 = 0$  has slope  $m = \frac{1}{2}$

Since parallel lines have the same slope, required line has slope  $m = \frac{1}{2}$

Using point-slope form:  $y - y_1 = m(x - x_1)$

$$y-2 = \frac{1}{2}(x - (-3))$$

$$y-2 = \frac{1}{2}(x+3)$$

$$2y-4 = x+3$$

$$x-2y+7=0$$

### Q5(B).3 [4 marks]

Find out center and radius of the circle:  $x^2 + y^2 + 6x - 4y - 3 = 0$

**Solution:**

Completing the square:

$$x^2 + 6x + y^2 - 4y = 3$$

$$(x^2 + 6x + 9) + (y^2 - 4y + 4) = 3 + 9 + 4$$

$$(x+3)^2 + (y-2)^2 = 16$$

Center:  $(-3, 2)$   
 Radius:  $r = \sqrt{16} = 4$

## Formula Cheat Sheet

### Logarithms

- $\log_a 1 = 0$
- $\log_a a = 1$
- $\log_a(xy) = \log_a x + \log_a y$
- $\log_a\left(\frac{x}{y}\right) = \log_a x - \log_a y$

### Trigonometry

- $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}$
- $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
- $\sin(180^\circ - x) = \sin x, \cos(90^\circ + x) = -\sin x$

### Vectors

- $|\vec{a}| = \sqrt{a_1^2 + a_2^2 + a_3^2}$
- $\vec{a} \cdot \vec{b} = |\vec{a}||\vec{b}| \cos \theta$
- For perpendicular vectors:  $\vec{a} \cdot \vec{b} = 0$

### Coordinate Geometry

- Two-point form:  $\frac{y-y_1}{y_2-y_1} = \frac{x-x_1}{x_2-x_1}$
- Circle:  $(x-h)^2 + (y-k)^2 = r^2$
- Parallel lines have equal slopes

### Limits

- $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$
- $\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$
- $\lim_{x \rightarrow \infty} \frac{ax+b}{cx+d} = \frac{a}{c}$

## Problem-Solving Strategies

1. **Logarithms:** Use properties to simplify expressions
2. **Trigonometry:** Apply compound angle formulas and identities
3. **Vectors:** Remember dot and cross product properties

# Common Mistakes to Avoid

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## Logarithms

- **Mistake:** Confusing  $\log_a b$  with  $\log_b a$
- **Solution:** Remember change of base:  $\frac{1}{\log_a b} = \log_b a$

## Trigonometry

- **Mistake:** Wrong angle conversions between degrees and radians
- **Solution:** Always use  $180^\circ = \pi$  radians for conversion

## Vectors

- **Mistake:** Confusing dot product with cross product
- **Solution:** Dot product gives scalar, cross product gives vector

## Limits

- **Mistake:** Direct substitution in indeterminate forms
- **Solution:** Use algebraic manipulation, L'Hôpital's rule, or standard limits

## Determinants

- **Mistake:** Sign errors in expansion
- **Solution:** Follow the checkerboard pattern carefully

## Exam Tips

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### Time Management

- **Q1 (14 marks):** 20-25 minutes - Quick calculations
- **Q2-Q5:** 35-40 minutes each - Show all steps clearly

### Strategy

1. **Read all questions first** - Choose easier OR options
2. **Start with Q1** - Build confidence with MCQs
3. **Show work clearly** - Partial credit is available
4. **Use standard formulas** - Don't derive unless asked

### Key Points to Remember

- Always write the final answer clearly
- Use proper mathematical notation

- Draw diagrams where helpful
- Check units in physics-related problems (work, force)

## Calculator Usage

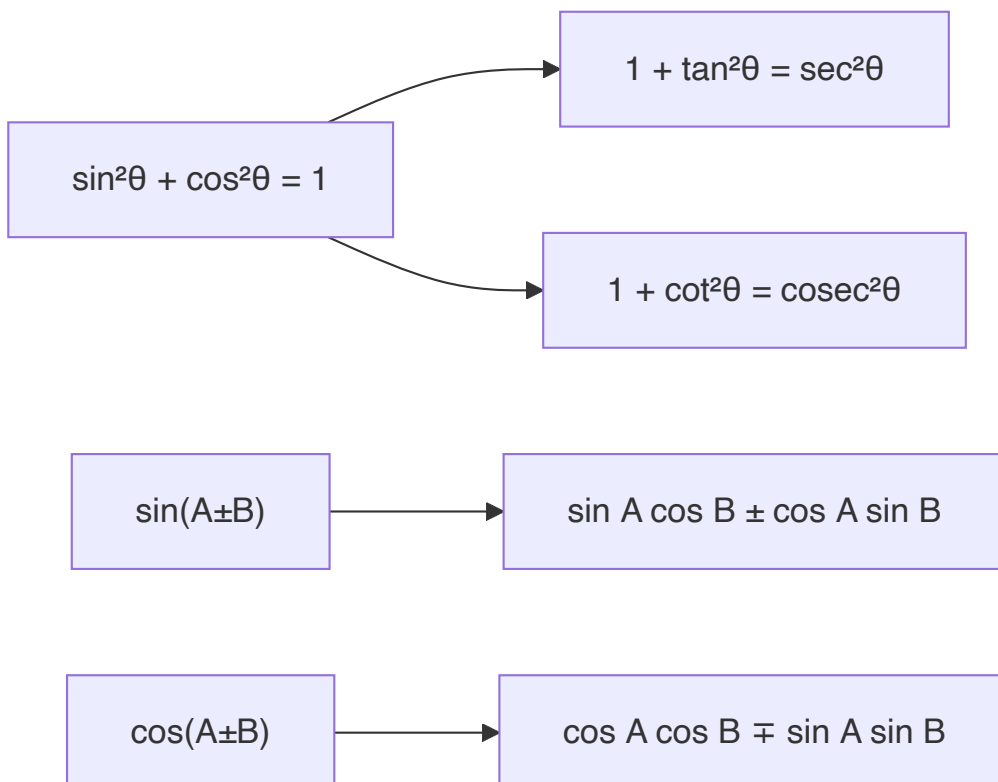
- Scientific calculator allowed
- Use for complex arithmetic only
- Show the setup before calculating
- Round final answers appropriately

## Common Formula Applications

### Standard Limits (Memory aids)

$\lim_{x \rightarrow 0} \sin(x)/x = 1$	"Sine over x is one"
$\lim_{x \rightarrow 0} (e^x - 1)/x = 1$	"e minus one over x is one"
$\lim_{x \rightarrow 0} (a^x - 1)/x = \ln(a)$	"General exponential form"

### Trigonometric Identities (Quick Reference)



### Vector Operations (Step-by-step)

1. **Magnitude:**  $|\vec{a}| = \sqrt{\text{sum of squares}}$
2. **Dot Product:**  $\vec{a} \cdot \vec{b} = a_1b_1 + a_2b_2 + a_3b_3$

3. **Angle:**  $\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|}$

Circle Equations (Forms)

Form	Equation	When to Use
Standard	$(x - h)^2 + (y - k)^2 = r^2$	Given center and radius
General	$x^2 + y^2 + Dx + Ey + F = 0$	Need to find center/radius
Complete Square	$(x + D/2)^2 + (y + E/2)^2 = (D^2 + E^2 - 4F)/4$	Converting general to standard

Problem-Specific Strategies

For Determinant Problems

- 1. Look for zeros to simplify expansion
- 2. Use row/column operations if allowed
- 3. Remember: if two rows/columns are proportional, determinant = 0

For Limit Problems

Start with limit

|

Direct substitution?

/ \

Yes No (0/0, ∞/∞, etc.)

| |

Answer Try factoring/  
rationalization

|

Still indeterminate?

|

L'Hôpital's Rule

|

Find answer

For Vector Problems

- **Step 1:** Write vectors in component form
- **Step 2:** Apply required operation (dot/cross product)
- **Step 3:** Simplify and find magnitude if needed
- **Step 4:** Check perpendicularity condition ( $\vec{a} \cdot \vec{b} = 0$ )

For Coordinate Geometry

- **Line problems:** Identify what's given (points, slope, parallel/perpendicular)
- **Circle problems:** Identify center and radius from given information

- **Always** check your equation by substituting known points

## Memory Techniques

### Logarithm Properties (MNEMONIC: "PLUS")

- **Product:**  $\log(ab) = \log a + \log b$
- **Limit:**  $\log_a 1 = 0$
- **Unity:**  $\log_a a = 1$
- **Subtraction:**  $\log(a/b) = \log a - \log b$

### Trigonometric Values (30°, 45°, 60°)

Angle	sin	cos	tan
30°	1/2	$\sqrt{3}/2$	$1/\sqrt{3}$
45°	$1/\sqrt{2}$	$1/\sqrt{2}$	1
60°	$\sqrt{3}/2$	1/2	$\sqrt{3}$

**Memory aid:** "1, 2, 3" under square roots for sin values (30° to 60°)

## Final Review Checklist

Before submitting your paper:

- ☐ All questions attempted as required
- ☐ Final answers clearly marked
- ☐ Units included where applicable
- ☐ No arithmetic errors in simple calculations
- ☐ Proper mathematical notation used
- ☐ Diagrams labeled clearly (if drawn)

## Quick Problem Solving Guide

### If you're stuck on a problem:

1. **Read the problem again** - Often missed details become clear
2. **Try a different approach** - Multiple methods usually exist
3. **Work backwards** - Start from what you want to prove/find
4. **Use elimination** - In MCQs, eliminate obviously wrong options
5. **Move on and return** - Don't spend too much time on one problem

### Last 15 minutes strategy:

- Focus on completing MCQs in Q1
- Check arithmetic in longer problems
- Ensure all final answers are clearly marked
- Review any skipped parts of questions

Remember: This exam tests fundamental concepts. Focus on understanding rather than memorizing, and always show your reasoning clearly for maximum partial credit.