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# Lab #1: Kinematics

Background: Isaac Newton compared movements with displacement, velocity, acceleration, and force. Isaac Newton described movement as kinematics. The British physicist provided multiple equations now in high school and college classrooms. Today, we describe acceleration from gravity by a linear equation.

**Goal**: The acceleration from gravity derived from an average, and actual vs expected error.

**Null Hypothesis:** Equations from Newton never predict an exact solution about displacement.

Alternative Hypothesis: Equations from Newton predict an exact solution about displacement.

### **Learning Outcomes:**

- 1. Problems evaluating frame of reference, displacement, velocity, and acceleration.
- 2. A relationship described between friction, air resistance, and other forces.
- 3. Experimental data tabulated from multiple measurements with one variable.
- **4.** A line graphed of force as a function of angle.
- 5. Percent errors validating acceleration from gravity.

#### **Equation #1: Velocity:**

$$\vec{v}_{avg} = \frac{\Delta \vec{d}}{\Delta \vec{t}} = \frac{d_f - d_0}{t_f - t_0}$$

### **Equation #2: Acceleration:**

$$\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta \vec{t}} = \frac{v_f - v_0}{t_f - t_0}$$

# **Equation #3: Newton's First Law:**

$$\vec{F}_g = m\vec{a}_g$$

Equation #4: Air Resistance: 
$$\vec{F}_{air} = \frac{1}{2} \rho A C \vec{v}$$

#### **Equation #5: Kinetic Friction:**

$$\vec{F}_{\!\mu} = \mu m a_g$$

# Equation #6: Force as a function of angle:

$$\vec{F} = ma = \vec{F}_g - \vec{F}_{air} - \vec{F}_{\mu} = m\vec{a}_g - \frac{1}{2}\rho AC\vec{v} - \mu ma_g = (1 - \mu)m\vec{a}_g - \frac{1}{2}\rho AC\vec{v} = "mx + b"$$

#### **Equation #7: Standard Deviation:**

$$\sigma = \sqrt{\frac{\sum_{i=1}^{N} |x_i - \bar{x}|^2}{N}}$$

#### **Equation #8: Percent Error:**

$$Percent\ error\ (\%) = \frac{|\textit{Measurable value} - \textit{Actual value}|}{|\textit{Actual value}|} * 100\%$$

- **1.** What are displacement, velocity, and acceleration?
- 2. What is a graph from experimental data about velocity?
- **3.** What is a graph from experimental data about acceleration?
- **4.** Why is percent error important?
- **5.** Newton was or was not correct about the equations?

Lab #2: Motion Graphing

**Background:** Free body diagrams apply to diagrams about movement by Newton's laws. Engineers sketch the system before the experiment via determination of total force. Gravity is a force in sketches, along the x-, y-, and z-axis, in addition to, friction, tension, or normal forces. Although, angles are difficult to new students, especially with cosine and sine. Today, students draw a free body diagram about a cart on a ramp.

**Goal:** The acceleration from gravity with derived error of the actual vs. expected physics.

**Null Hypothesis:** The velocity of the cart is not dependent on time throughout the experiment.

Alternative Hypothesis: The velocity of the cart is dependent on time throughout the experiment.

#### **Learning Outcomes:**

- 1. Problems involving frame of reference, displacement, velocity, and acceleration.
- **2.** Experimental data tabulating a record with one changing variable.
- **3.** A line of the tabulated data as a function of angle, then standard deviation.
- 4. Percent error to historically recorded values and constants

# Equation #1: Velocity:

$$\vec{v}_{avg} = \frac{\Delta \vec{d}}{\Delta t} = \frac{d_f - d_0}{t_f - t_0}$$

#### **Equation #2: Acceleration:**

$$\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t} = \frac{v_f - v_0}{t_f - t_0}$$

#### Equation #3: Newton's First Law:

$$\vec{F}_g = m\vec{a}_g$$

#### **Equation #7: Standard Deviation:**

$$\sigma = \sqrt{\frac{\sum_{i=1}^{N} |a_i - \bar{a}|^2}{N}}$$

Ring stand

#### **Equation #8: Percent Error:**

Percent Error (%) = 
$$\frac{|Measured\ value - Actual\ value|}{|Actual\ value|} * 100\%$$

#### **Tabular Data:**

Measurement [Full Distance]	Time (sec)
1	
2	
3	
4	
5	
6	

Tape

Track

7	
8	
9	
10	
Measurement [Half Distance]	Time (sec)
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

- 1. What are differences between displacement, velocity, and acceleration?
- 2. What is the free body diagram above? A label of gravity, and normal are requisite.
- 3. Why is half distance and full distance in the experiment?
- **4.** What is the acceleration?
- **5.** What is the force from movement?

# Lab #3: Repetitive Motion

<u>Background:</u> Automotive and robotic assembly is repetitive. Since the first vehicle by Henry Ford to Charlie Chaplin's initial films, motion is a childhood favorite. Prior in time, mechanical dolls repetitively wrote articles by Pierre Jaquet-Droz. Also, vintage watches from Swiss-manufacturing repetitively determined time. Today, in home devices generate simple motions, including printers and dishwashers. For class, we generate basic repetitive motion.

Goal: Discrete m

ovements measured by a series of photogates and a graph about a transient object.

**Null Hypothesis:** The independent and dependent variables in then graph below have no relationship.

Alternative Hypothesis: The independent and dependent variables in the graph have a relationship.

#### **Learning Outcomes:**

- 1. A car on a rail repeating movements back and forth along the rail.
- **2.** A graph about measured position vs. time of repetitive motions done by hand.
- 3. Velocity from moving the rail car in both positive and negative directions.
- **4.** The plot of acceleration from calculating velocity.

#### **Equation #1: Position:**

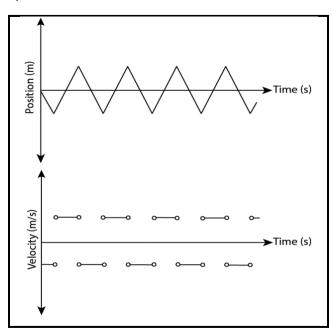
$$\Delta x = x_2 - x_1$$

### **Equation #2: Velocity:**

$$\vec{v} = \left(\frac{x_2 - x_1}{t_2 - t_1}\right)$$

#### **Equation #3: Acceleration**

$$\vec{a} = \left(\frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1}\right)$$



<u>Tabular Data:</u> Photogate 1-2 (cm): \_\_\_\_\_ Photogate 2-3 (cm): \_\_\_\_ Photogate 3-4 (cm): \_\_\_

									1	Photo	ogate	2								
	#1	#2	#3	#2	#1	#2	#3	#2	#1	#2	#3	#2	#1	#2	#3	#2	#1	#2	#3	#2
Time (ms)																				

- 1. What are the independent and dependent variables in the experiment?
- 2. A description about certainty in the experiment between time and position.
- **3.** What is velocity?
- **4.** Acceleration relates to velocity and position, why?
- **5.** A graph of time vs. position, time vs. velocity, and time vs. acceleration.

# Lab #4: Acceleration

<u>Background</u>: The construction, design, and purpose of machines is mechanical engineering. The field touches on virtually every motion, along with safety by failure, functionality, aesthetics, and durability. The failure process entails investigative preservation, visual inspection, electrical testing, reliability per use, and failure mechanism. For today's lab, students inhibit an approach of upward motion through mathematical calculation.

**Goal**: A prediction about mass and angle from trials stalling an upward motion.

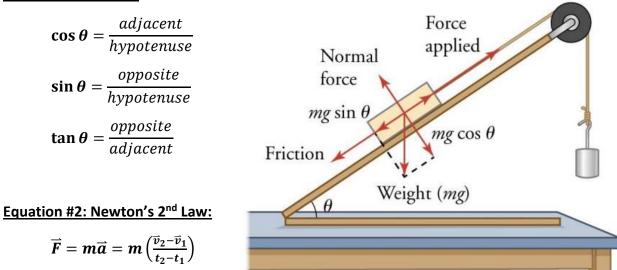
**Null Hypothesis:** The independent and dependent variables in the graph below have no relationship.

<u>Alternative Hypothesis:</u> The independent and dependent variables in the graph below have a relationship.

#### **Learning Outcomes:**

- 1. An incline angle before measuring linear motion on a ramp.
- 2. Communicate with others, what is the maximum limit of motion.
- **3.** For three attempts, the maximum mass to an exact stall.

# **Equation #1: Angles:**



Tabular Data: Ramp Length (cm): \_\_\_\_\_ Angle (°): \_\_\_\_\_ Mass of Cart (g): \_\_\_\_\_

Experiment	Mass (g)	Length of Travel (m)	Time of Travel (s)
Trial #1			
Trial #2			
Trial #3			

- 1. What are the independent and dependent variables in the experiment?
- 2. A description about certainty in the experiment between mass and length of travel.
- **3.** What is velocity in the experiment above?
- **4.** Why are trigonometric equations important to an incline or ramp?
- **5.** Were the trials accurate predictors to stall?

# Lab #5: Newton's Third Law of Motion

<u>Background</u>: Newton's third law relates equal forces of opposite direction. For the third law, balloons pronounce an upward rocket thrust. The equal and opposite corollary in a balloon is inertia. A balloon of ideal pressure and dimension simulates conditions of Newton's third law with little drag and friction. For this morning's lab, students produce different pressure systems to substantiate Newton's law.

**Goal**: Prior to lab, the pressure and distance of a balloon modelled on a string from mathematics.

**Null Hypothesis:** The independent and dependent variables in the graph below have no relationship.

Alternative Hypothesis: The independent and dependent variables in the graph below have a relationship.

# **Learning Outcomes:**

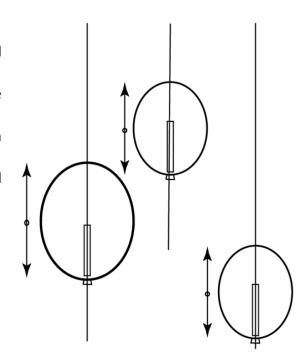
- **1.** A balloon-straw system predicts internal pressure
- **2.** The Ideal Gas Law for intermediate prediction of internal balloon pressure
- **3.** Average distance traveled by a balloon in an experiment
- **4.** Compare and contrast predicted vs. actual pressure in a written argument

**Equation #1 – Pressure:** 
$$P = \frac{Force}{Area}$$

**Equation #2 – Ideal Gas Law:** 
$$PV = nRT$$

**Equation #3 - Force:** 
$$F = ma = m \frac{\Delta v}{\Delta t}$$

**Equation #4 - Average:** 
$$\overline{x} = \frac{\sum_{i=1}^{n} x_i}{n}$$



#### **Tabular Setup:**

Total Mass (g):

rabaiai octup	<u></u>	10tal Mass (8).				
Experiment	Radius (m)	Predicted Pressure (atm)	Distance (m)	Travel Time (s)	Actual Pressure (atm)	
Trial #1						
Trial #2						
Trial #3						
Trial #4						
Trial #5						
Predicted Ave	erage (atm):		Actual Av	erage (atm)		
Standard Er	ror (atm):		Standard Error (atm):			

- 1. What are the independent and dependent variables in the experiment?
- 2. The Ideal Gas Law had what purpose?
- **3.** Five total trials were in the experiment. How many trials are necessary in a 95% confidence level? How does confidence level prove a hypothesis?
- **4.** What were clues about the actual pressure?
- **5.** Standard errors are not in the equations. Where is the standard error equation? Please, a citation.

Lab #6: Forces 1-D

<u>Background</u>: Gravity is a fundamental force of the natural universe. The effect upon mass is determinable to the accuracy and precision of the clock measurement. By a vertical ring stand, students delve into free fall, plotting data, calculating accuracy, along with determining precision of their methods.

**Goal**: Statistically determine the gravitational acceleration constant and experimental error.

Null Hypothesis: Position and time variables have no relationship in the experiment.

Alternative Hypothesis: Position and time variables have a relationship in the experiment.

### **Learning Outcomes:**

- 1. At Earth's Sea level, gravitational acceleration, a constant using photogates.
- **2.** A simple displacement, velocity, acceleration, and force plot from the data.
- **3.** The accuracy and precision of measured constants with many experimental trials.

#### **Equation #1: y-component:**

$$y = y_0 - v_x t - \frac{1}{2}gt^2$$

### **Equation #2: Standard Deviation:**

$$\sqrt{\frac{\sum_{i=1}^{N}(x_i-\overline{x}_i)^2}{N}}$$

# **Equation #3: Percent Error:**



$$Percent\ Error\ = \frac{|Measured-Actual|}{Actual}*100\%$$

Tabular Data: Height (cm): \_\_\_\_\_ Mass (g): \_\_\_

Measurement	Time (s)	Velocity (m/s)	Acceleration (m/s²)	Force (N)		
Photogate #1						
Photogate #2						
Photogate #3						
Photogate #4						
Photogate #5						

- 1. What are the independent and dependent variables in the experiment?
- **2.** What was purpose of Equation #1?
- **3.** Five total trials were in the experiment. What was the average time, velocity, acceleration, and force? A calculation individually or total average is applicable?
- **4.** What was percent error?
- **5.** Three plots prepared with position (m) vs. time (s), velocity (m) vs. time (s), and acceleration (m) vs. time(s).

Lab #7: Projectile Motion

**Background**: Documentation of projectiles existed from before the 12<sup>th</sup> century. The arcs of high-tensile bow and arrow represent a historic point in African and Eurasian history. Projectile motion led researchers to space, and beyond. For lab, students predict location and distance.

**Goal**: An equation about arcs from time, position, and velocity by using Newton's laws.

**Null Hypothesis:** The position and time variables have no dependent relationship.

Alternative Hypothesis: The position and time variables have a dependent relationship.

### **Learning Outcomes:**

- 1. Two equations having separable and dependent time components.
- 2. A position predicted by an angle via a model from Newton.
- **3.** The actual distance compared to a target already on the floor before experiment.

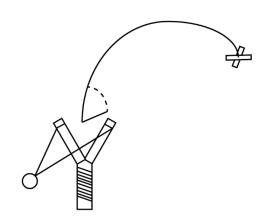
$$x = vt + x_0$$

#### **Equation #2 - Velocity:**

$$v = at + v_0$$

#### **Equation #3 - Acceleration:**

$$a_g = 9.8 \, m/s^2$$



<u>Derivation:</u>		

**Tabular Data:** Angle (°): \_ Force (N): **Predicted** Predicted Actual Actual **Experiment** x-Position (m) y-Position (m) x-Position (m) y-Position (m) Trial #1 Trial #2 Trial #3 Trial #4 Trial #5 Average

- 1. What are the independent and dependent variables in the experiment?
- 2. What was the purpose of Equation #1, #2, and #3?
- **3.** A paragraph written about the derivation, experiment, and trials.
- **4.** Which variable, x or y is dependent on gravity?
- **5.** How close was the target to prediction?

Lab #8: Forces 2-D

Background: Forces have separable components. Within the Cartesian coordinate system, individuals practice the F<sub>x</sub>, F<sub>y</sub>, and F<sub>z</sub> forces on a free body diagram. An example is an incline with 2-dimensional forces in both x-and-y directions from gravitational acceleration up the slope. Today, we apply Newton's 2<sup>nd</sup> Law to determine the free body diagram and individual components.

**Goal**: An object traveling by gravity up an incline, across a pulley, and down a ledge.

**Null Hypothesis:** The force in the x-direction never depends on the force in the y-direction.

<u>Alternative Hypothesis:</u> The force in the x-direction depends on force in the y-direction.

#### **Learning Outcomes:**

- 1. A free body diagram of a mass balanced on an incline by a block.
- **2.** The forces to movement  $(F_x, F_y)$  after mass releases.
- 3. Newton's 2<sup>nd</sup> Law demonstrating where forces equate.

#### **Equation #1: Angles:**

$$\cos \theta = \frac{adjacent}{hypotenuse}$$

$$\sin \theta = \frac{opposite}{hypotenuse}$$

$$\tan \theta = \frac{opposite}{adjacent}$$
Friction

Friction

Friction

Weight (mg)

$$\vec{F} = m\vec{a} = m\left(\frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1}\right)$$

Tabular Data: L	ength (cm):	: Angle (°): _	Mass of Cart (g): _	Mass	of Weight	: (g):
Measurement	Time (s)	Velocity (m/s)	Acceleration (m/s²)	$\overrightarrow{F}$ (N)	$\overrightarrow{F}_{x}$ (N)	$\overrightarrow{F}_y$ (N)
Photogate #1						
Photogate #2						
Photogate #3						
Photogate #4						
Photogate #5						

- 1. What are the independent and dependent variables in the experiment?
- **2.** What was purpose of Equation #1?
- **3.** What is the free body diagram from the incline?
- **4.** A plot about graphs showing time vs. x-position and time vs. y-position?
- **5.** What is the free body diagram where forces equate?

Lab #9: Pulleys and Tension

<u>Background:</u> A pulley system is historical. The framework transfers force in a circular motion and distributes tension across further connections. The first pulley operation was in 1500 BCE by Mesopotamians for resources. Archimedes used pulleys and Leonardo Da Vinci. For exposure to multi-pulley systems, students measure the force of gravity across three types of vertical hoists.

Goal: Newton's second law applied to force across multiple pulleys.

**Null Hypothesis:** Displacement is not dependent by mass with a number of pulleys.

Alternative Hypothesis: Displacement is not dependent by mass with a number of pulleys.

#### **Learning Outcomes:**

- 1. A pulley system using single, double, and triple wheels.
- 2. The distance during free fall by applying a body diagram with tensions.
- **3.** The error extracted from measurements in a one-, two-, three-, or tuple-wheel systems.

# **Displacement of Pulley System:**

Single Pulley System	
Mass A (g)	
Mass B (g)	
Predicted Displacement (m)	
Actual Displacement (m)	
Error (m)	

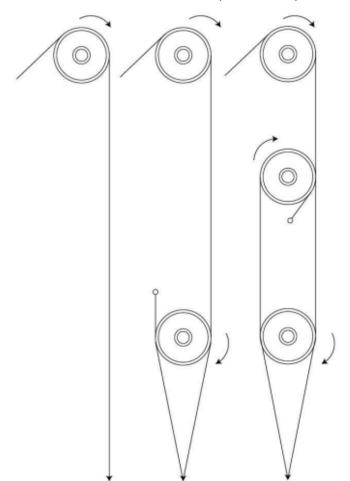
#### Calculations:

Double Pulley System	
Mass A (g)	
Mass B (g)	
Predicted Displacement (m)	
Actual Displacement (m)	
Error (m)	

#### Calculations:

Triple Pulley System	
Mass A (g)	
Mass B (g)	
Predicted Displacement (m)	
Actual Displacement (m)	
Error (m)	





- 1. What are the independent and dependent variables in the experiment?
- **2.** What happens from additional pulleys?
- **3.** What is the free body diagram about each system?
- **4.** Why is a triple pulley system helpful with lift?
- **5.** What is the error in each system?

Lab #10: Periodic Motion - 1D

<u>Background:</u> An occurrence at regular intervals is periodic. When about a circle, the direct motion is recurrent and cyclic. In a single dimension, amplitude distinguishes (co)sinusoidal model by extreme position. While, frequency describes periodic behavior. The solution to the model is unique and about natural motion. A circular ring represents a wave when perpendicular. For lab, students rotate a ring for periodic motion.

**Goal**: A continuous movement about unit circle by oscillating a wire loop.

**Null Hypothesis:** The motion around a unit circle never represents a wavey motion.

<u>Alternative Hypothesis:</u> The motion around a unit circle represents a wavey motion.

### **Learning Outcomes:**

- 1. Unit circle exposure by experimental periodic rotation around a circular object.
- 2. Angular rotation directly depends on wavey motion along a line in different dimensions.
- **3.** A model about error from rotational motion with a metal ring in two-dimensional space.

#### **Equation #1 & #2 - Periodic Motion in x-, and y-directions**

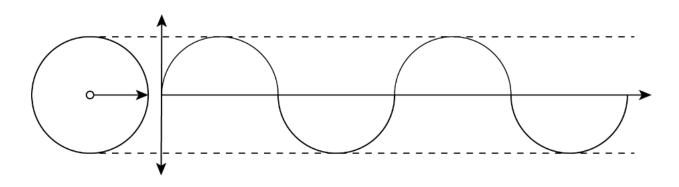
$$x(t) = A\cos(\omega t + \varphi)$$
  $y(t) = A\sin(\omega t + \varphi)$ 

**Tabular Data:** 

Rotation time (sec):

Rotation time	Unit Circle			Periodic Wave				
sec	Member Values A		Average	Member Values		Average		
Amplitude (cm)								
Frequency (1/s)								
Period (s)								
Phase (rad)								

Model Position (cm): \_\_\_\_\_ Model Position (cm): \_\_\_\_



- 1. The metal ring did what?
- 2. What is amplitude?
- **3.** What is frequency?
- **4.** Why was motion repetitive and periodic?
- **5.** What is phase?
- **6.** What was the error from rotation?

Lab #11: Simple Harmonic Motion

<u>Background</u>: Simple harmonic motion on a pendulum describes oscillatory motions. The sinusoidal behavior from position matches a sine (or cosine) function near equilibrium. With a weight and pivot point, students determine a model of frequency, displacement, and periodic motion.

**Goal**: A simple harmonic oscillator calculation from parameters in a pendulum near minimum.

**Null Hypothesis:** The angular frequency from a pendulum is never dependent on time.

Alternative Hypothesis: The angular frequency from a pendulum is dependent on time.

# **Learning Outcomes:**

- 1. A trigonometric model to harmonic motions from a pendulum.
- 2. Boundary conditions exposed through a sinusoidal function.
- 3. The frequency, position, and period of a sizeable multimeter pendulum.

# **Equation #1: Period:**

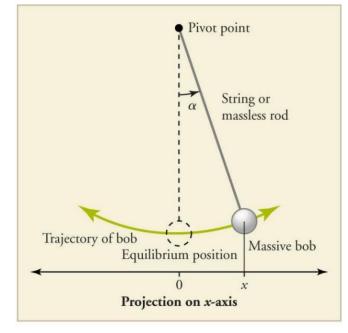
$$Period(s) = T = 2\pi \sqrt{\frac{L}{g}}$$

# **Equation #2: Angle:**

$$\alpha(t) = \omega t + \Phi$$

#### **Equation #2: Displacement:**

$$x = A \sin(\omega t + \phi)$$



**Tabular Data:** Length of String (cm): Mass of Weight (g):

taraiai Patai		2011,6411 01 041111,6 (0111,71)	''		(6)
Trials	Time (s)	Displacement (m)	Angle (°)	Period (s)	ω (rad/s)
Trial #1					
Trial #2					
Trial #3					
Trial #4					

- 1. What was the average period from the pendulum?
- **2.** What is the mathematics from period to angular frequency?
- **3.** A heavier mass has similar or different outcomes?
- **4.** What was the angular frequency?
- **5.** What is a boundary condition?

# Lab #12: Momentum

<u>Background</u>: Conservation of momentum symbolizes total object mass at a velocity. The momentum vector is the displacement by an object times mass per duration of travel. In a system without friction, drag, or other forces, momentum conserves during collision. Today's experiment transfers momentum before and after the collision. From photogates, the average and precise measuring about a perfectly elastic collision.

**Goal**: Quantitatively measure conservation and the total momentum of contact.

**Null Hypothesis:** Momentum of a car has no relationship before and after collision.

Alternative Hypothesis: Momentum of a car has a relationship before and after collision.

#### **Learning Outcomes:**

- 1. Collisions between frictionless physics cars at different marked lengths.
- 2. Quantitatively measure velocity with a series of photogates.
- **3.** Experimental practice measuring the mass of objects.
- **4.** A hypothesis before experiment about predicting the collision parameters.
- **5.** Momentum to kinetic energy for further calculating conservation of energy.

#### **Equation #1: Momentum:**

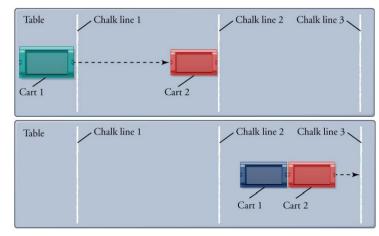
$$p = mv$$

### **Equation #2: Total Momentum:**

$$\left(\sum_{i=1}^n m_i v_i\right)_{initial} = \left(\sum_{i=1}^n m_i v_i\right)_{final}$$

#### **Equation #3: Kinetic Energy:**

$$K.E. = \frac{1}{2}mv^2$$



Tabular Data: Mass Car #1 (g): \_\_\_\_\_ Mass Car #2 (g):\_

Trial	Init	ial	Final		
	Velocity #1 (cm/s)	Velocity #2 (cm/s)	Velocity #1 (cm/s)	Velocity #2 (cm/s)	
1					
2					
3					
4					
5					
6					
7					
8					
9					

- 1. What was the average velocity of car #1 before collision?
- **2.** What was the average velocity of car #2 after collision?
- **3.** A paragraph about the momentum transfer.
- **4.** What was the kinetic energy of car #1 before collision?
- 5. What was the kinetic energy of car #2 after collision?

# **Lab #13: Potential Energy Storage**

<u>Background</u>: Across sciences, potential energy is the difference to ground. Count Rumford's studied thermodynamics, and also formulae about local heat and energy. Primary discoveries by Count Rumford (Benjamin Thompson) were plants correlation to rays from the sun, intensity in wax candles, conduction, convection, hot weights, and instrumentation thereof. Later scientists, Davy, Lavoisier, Mayer, Joule, Kelvin, and Carnot characterized their discoveries of thermo- and electrodynamics. Soon after, potential energy solidified. In the afternoon, students determine potential energies linear relationship.

Goal: A relationship between height and potential energy through a ramp with spherical mass.

**Null Hypothesis:** Potential energy has no correlation to height on a slope.

Alternative Hypothesis: Potential energy has a correlation to height on a slope.

## **Learning Outcomes:**

- 1. Conservation of energy through potential and kinetic energy transfer.
- 2. A graph incorporating height vs. potential energy or gravity, mass, and height.
- **3.** In words, how to increase experimental accuracy and precision.

## **Equation #1: Momentum:**

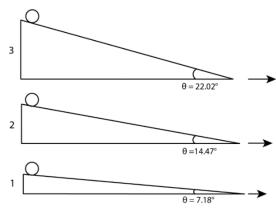
$$K.E. = \frac{1}{2}mv^2$$

#### **Equation #2: Total Momentum:**

$$a_g=9.8\,m/s^2$$

## **Equation #3: Kinetic Energy:**

$$\Delta E = KE + PE \cong 0$$



Mass Car #2 (g).

<u> I abular Data:</u>	Mass Car	#1 (g):	Mass Car #2 (g):				
	Ramp	#1	Ramp	#2	Ramp #3		
Experiment	Distance (m)	Time (sec)	Distance (m)	Time (sec)	Distance (m)	Time (sec)	
Mass #1							
Mass #1							
Mass #1							
Kinetic Energy (J)							
Potential Energy (J)							

- 1. What was the average kinetic energy in each trial?
- **2.** What was the average potential energy in each trial?
- **3.** How close were potential and kinetic energy?
- **4.** What height effected potential energy?
- 5. A plot about Height (m) vs Potential Energy (J).

# Lab #14: Mechanical Waves

<u>Background</u>: A mathematical representation of waves is foundational. Every day students hear terms about 'the speed of sound', 'light', 'p-wave', 's-wave', and 'earthquake!' Traditional calculations found in the medium of travel, but also less complexity. An incident wave reflects into an observable interference. For today's lab, thoughts explore incident phase, frequency, amplitude, and kinetic energy.

**Goal**: The kinetic energy of a transverse or longitudinal wave produced on a spring.

**Null Hypothesis:** The kinetic energy never depends on the wave function from the spring.

Alternative Hypothesis: Kinetic energy depends on the wave function from the spring.

### **Learning Outcomes:**

- 1. Observable waves on spring by oscillating frequency and/or phase of movement.
- 2. Quantitatively determine the amplitude of a wave with a standard ruler.
- 3. A multitude of wavelengths across varying frequencies.
- **4.** A functional relationship of simple waves using laboratory information.
- **5.** Separately, kinetic energy calculating a model to the experimental waves.

## **Equation #1: Wave Equation:**

$$y(t) = A\sin(\omega t + \varphi)$$

# **Equation #2: Velocity of Wave:**

$$v = \lambda f$$

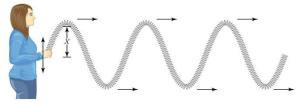
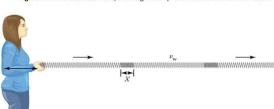


Figure 11.2: A transverse wave, showing the amplitude X and direction of motion.

## **Equation #3: Kinetic Energy:**

$$K.E. = \frac{1}{2}mv^2$$



#### **Tabular Data:**

Experiment	Phase	Frequency (1/s)	Amplitude (cm)	Wavelength (cm)	Function of Wave y(t)	Velocity (cm/s)	Kinetic Energy (J)
Trial #1							
Trial #2							
Trial #3							
Trial #4							
Trial #5							

- 1. What is phase?
- **2.** Why is frequency essential to Equation #1?
- **3.** Amplitude contributes to Equation #1? How?
- **4.** What was the wavelength from each trial?
- 5. Kinetic Energy was similar or dissimilar between each trial?

# **Lab #15: Pendulum Momentum**

Background: In China, Ganzhou, Jiangxi Province is a large pendulum. At 12.8-meters, Harmony Tower commissioned a pendulum in a clock by clockmakers - Smith of Derby. Prior to 2010's design, another pendulum existed for experimentation. With a length of 4,250 feet, two lengths of No. 24 steel piano wire, Professor Fred W. McNair of College of Mines, Michigan utilized Tamarack Mines with weighted bobs Down a shaft labelled No. 5 suspended an experiment about gravitational separation. Science Magazine published results of gravitational separation on Friday, June 20th, 1902. For examination, students' measure momentum from a pendulum.

**Goal**: Standardize momentum for a single pendulum then collide two pendulums

**Null Hypothesis:** Angular momentum never depends on time.

Alternative Hypothesis: Angular momentum depends on time.

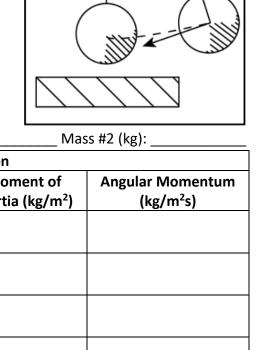
## **Learning Outcomes:**

- 1. A standard calibration for (later) measure of angular momentum.
- 2. Two pendulums as a momentum transfer experiment and observation of inelastic collision.
- 3. Momentum for single and double pendulum movements.

#### **Equation #1: Angular Velocity:**

$$\omega = \frac{v}{r}$$

## **Equation #2: Angular Momentum:**



	Second Pendulum Collision										
Experiment	Radians (rad)	Time (sec)	Angular Velocity (rad/s)	Moment of Inertia (kg/m²)	Angular Momentum (kg/m²s)						
Trial #1											
Trial #2											
Trial #3											
Average											

- **1.** What are radians?
- **2.** Calibration had what purpose? Why was a second pendulum important?
- **3.** What is momentum?
- **4.** What is the mathematical relationship between moment of inertia and angular momentum?
- **5.** Two pendulums generated error? What was the average error?

# **Lab #16: Electrostatics**

<u>Background</u>: Electrostatic forces relate to Coulomb's Law. An electron's charge act across distance by both direction and magnitude. The force is proportional through an inverse square law and during laboratory experiment. Two balloons charge by electrostatic electricity and exemplify Coulomb's Law. A coefficient describes the experiment (Equation #1) as a universal constant. Student's examine charges, a proportional constant, and a reciprocal square in Coulomb's law.

**Goal**: An experiment testing laws and equations, specifically Coulomb's.

**Null Hypothesis:** The distance from midline (center) is not proportional to Coulomb's constant.

<u>Alternative Hypothesis:</u> Distance from midline (center) is proportional to Coulomb's constant.

# **Learning Outcomes:**

- **1.** An apparatus using balloons and tangential forces.
- **2.** Experimental values accurately quantifying Coulomb's constant
- **3.** A precise determination by using uncertainty.

# **Equation #1: Coulomb's constant:**

$$k_e = 8.998 \, x \, 10^9 \ N \cdot m^2/C^2$$

# **Equation #2: Electron charge:**

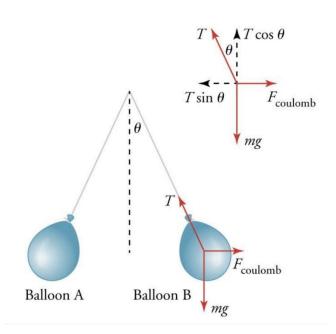
$$q = 1.602 \times 10^{-19} C$$

# **Equation #3: Coulomb's Law:**

$$\vec{F} = k_e \frac{q_1 q_2}{r^2}$$

## **Equation #4: Force of Coulomb:**

$$\vec{F} = m\vec{g} \tan \theta$$



<u>Tabular Data:</u>	Mass Balloon A (g):	Mass Balloon B (g):
Experiment	Distance from Center (cm)	Measured Coulomb Constant (N*m²/C²)
Trial #1		
Trial #2		
Trial #3		
Trial #4		
Trial #5		
Trial #6		
Trial #7		
Trial #8		
Trial #9		

Average Coulomb Constant (N*m <sup>2</sup> /C <sup>2</sup> )	:
Uncertainty of Measurement (%):	

- **1.** What is a tangent function?
- 2. What is a relationship between Equations #1 and #2?
- **3.** Any human errors arise from the experiment?
- **4.** What were experimental values about Coulomb's constant?
- **5.** How justifiable is error from actual Coulomb's constant?

Lab #17: Ohm's Law

<u>Background</u>: Ohm's Law describes a direct relationship between voltage, current, and resistance. Voltage (V) is potential difference from an energy source in an electric circuit. While current (C) is the flow of electrons in a conductive wire. Current flow is directly proportional to voltage by a coefficient, resistance (R). The linear relationship in the experiment was evidence to conductance. Students, today prepare a standard curve from a voltmeter across a circuit.

**Goal**: A standard curve (linear relationship) graphed between voltage and current.

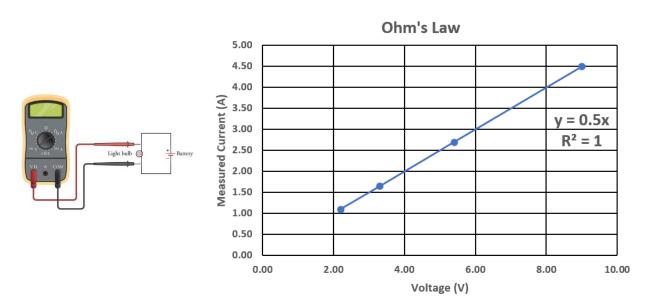
**Null Hypothesis:** Voltage is independent to current in electrical circuits.

Alternative Hypothesis: Voltage is dependent to current in electrical circuits.

## **Learning Outcomes:**

- 1. An electric circuit's current by using a voltmeter (ammeter).
- **2.** A light bulb contains resistance across positive and negative terminals.
- **3.** A linear curve collected at specific voltages onto a plot and graph.

## Equation #1: Ohm's Law: V = IR



**Tabular Data:** Instrument Model:

Experiment	Voltage (V)	Current (A)
Circuit #1		
Circuit #2		
Circuit #3		
Circuit #4		
Circuit #5		

- **1.** A 5-7 sentence paragraph about voltage, current, and resistance.
- **2.** What changed between each experiment?
- **3.** Voltage and current have units, any specific reason?
- **4.** Voltage (V) versus Current (I) plot.
- **5.** What was the light bulb's resistance?

**Lab #18: Resistor Circuits** 

**Background**: Circuits are conductive paths to positive and negative charges. Series circuits contain resistance across a single path, while parallel circuits resistance across multiple paths. Despite nearly infinite combinations, the simplest circuit involve wires, resistors, and batteries. A voltmeter or ammeter measure circuit voltage and amperage, respectively. A demonstration about Kirchhoff's law is the plan in the lab below.

**Goal**: Students examining series and parallel circuits through ammeter values.

**Null Hypothesis:** Current is not directly proportional to resistance in series and parallel circuits.

<u>Alternative Hypothesis:</u> Current is directly proportional to resistance in series and parallel circuits.

#### **Learning Outcomes:**

- 1. Ammeter or voltmeter usage for circuit information.
- **2.** Multiple circuits engineered as series and parallel circuits in a rigid test.
- **3.** Kirchhoff's law from collected electrical values as proof to the law.

### **Equation #1: Kirchhoff's Law for Currents:**

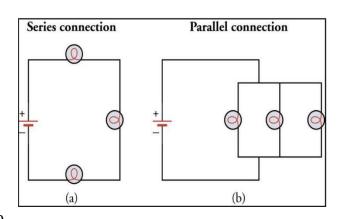
$$\sum_{i=1}^{n} I_i = I_1 + I_2 + I_3 + \dots + I_n = 0$$

# **Equation #2: Kirchhoff's Law for Voltage:**

$$\sum_{i=1}^{n} V_i = V_1 + V_2 + V_3 + \dots + V_n = 0$$

#### **Equation #3: Kirchhoff's Law for Resistance:**

$$\sum_{i=1}^{n} \frac{1}{R_i} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n} = 0$$



#### **Experimental Data:**

Series Circuit:			
Parallel Circuit:			

- **1.** What are series and parallel circuits?
- 2. Gustav Kirchhoff made laws for series and parallel circuits. Why?
- **3.** How many circuits are necessary as proof to Kirchhoff's law?
- **4.** What changed between each experiment?
- **5.** What is error from the experiment above?

# Lab #19: Torque

<u>Background</u>: Torque is an extension from kinematics. A tangential force upon a perpendicular axis is directly proportional to force-distance i.e., torque. A force applies across a length in a circular motion, as torque. The alternative perspective is angular momentum (L) and the relation to moment of inertia (I). By acceleration from gravity, the demonstration involves incremental mass onto a wrench and bolt.

**Goal**: Torque for a fastened bolt or nut and angular momentum from the same system.

**Null Hypothesis:** Torque is not dependent on mass in a linear equation.

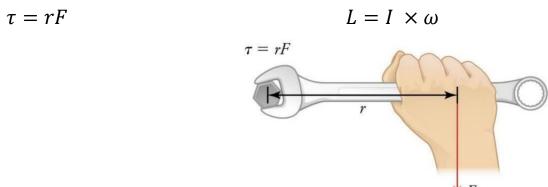
<u>Alternative Hypothesis:</u> Torque is dependent on mass in a linear equation.

## **Learning Outcomes:**

- 1. An apparatus to quantitatively measure the torque of a bolt.
- 2. Accurate torque from an arithmetic mean (or average) and multiple samples.
- **3.** Precise torque in the system by multiple experiments using standard deviation.

## **Equation #1: Torque:**

**Equation #2: Angular Momentum** 



#### **Tabular Data:**

Tool	Length (cm)	Trial	Total Mass (g)	Force (N)	Torque (N*m)	Average Torque (N*m)
Wrench		1				
#1		2				
#1		3				
Manah		4				
Wrench		5				
#2		6				
Muonob		7				
Wrench		8				
#3		9				

Sum Average Torque	N*m	):
--------------------	-----	----

Standard	Deviation	/N/*m/· +	

- 1. What is torque?
- **2.** What is angular momentum?
- **3.** What was the average torque?
- **4.** How precise was the experiment about torque?
- **5.** A paragraph (5-7 sentences) about torques relationship to a hand and wrench.

Lab #20: Angular Momentum

<u>Background</u>: Gyroscope applications model a stationary center of mass. In laboratory settings, gyroscopes rotate about a point with a rigid and symmetrical frame. The generated torque of gyroscope stabilizes or destabilizes the origin i.e., structural center of mass. A formula governs gyroscopes under Cartesian and spherical dimensions. Our experiment has two linear functions; center of mass and a rotation axis in a plane.

**Goal**: A gyroscopic torque and angular momentum from rotation, angle, and gravity.

**Null Hypothesis:** Angular momentum has no direct correlation to angular velocity.

Alternative Hypothesis: Angular momentum has a direct correlation to angular velocity.

### **Learning Outcomes:**

- 1. An object precesses about a rotational point the 'origin.'
- **2.** Torque from a gyroscope with the radius of rotation, mass, and gravitational force.
- **3.** Angular momentum around a disc from a verifiable experimental setup.

## **Equation #1: Torque:**

$$\tau = rF$$

## **Equation #2: Angular Momentum**

$$\vec{L} = I\vec{\omega} = \vec{r} \times \vec{p} = m \, (\vec{r} \times \vec{v})$$

# **Equation #3: Moment of Inertia (Disc)**

$$I_z = I_x + I_y = \frac{1}{2}MR^2$$

## **Experimental Data:**

Mass of Counterweight (g):\_\_\_\_\_\_

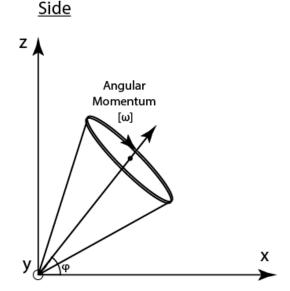
Length of Rope (m):\_\_\_\_\_

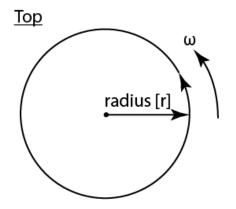
Angular Velocity (rad/s):\_\_\_\_\_

Radius of Gyroscope (m): \_\_\_\_\_

Angle of Gyroscope (°):\_\_\_\_\_

Torque of Gyroscope (kg m²):\_\_\_\_\_





- 1. What is torque?
- **2.** What is angular velocity?
- **3.** What is a gyroscope?
- **4.** What proves the alternative hypothesis?
- **5.** What data disproves the null hypothesis?

Lab #21: Conservation of Angular Momentum

**Background**: A system has conserved angular momentum under zero external torque. For a disc orthogonal to gravity, the law of conservation of angular momentum predicts accurate and precise data. To model angular motion, forces balance across a disc at a radial distance. In a proper model, students rotate a flywheel with specific properties, then solve for total angular momentum.

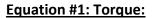
**Goal**: Masses on a rotational disc quantify the law of conservation of angular momentum.

**Null Hypothesis:** Angular momentum never conserves on a rotational disc.

Alternative Hypothesis: Angular momentum conserves on a rotational disc.

# **Learning Outcomes:**

- **1.** Average trials determining the accuracy of angular conservation.
- **2.** Qualitatively and quantitatively evaluate the standard error of experimental setup



$$\tau = rF$$

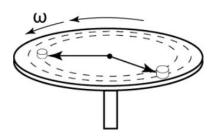
# **Equation #2: Angular Momentum**

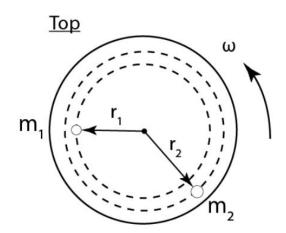
$$\vec{L} = I\vec{\omega} = \vec{r} \times \vec{p} = m (\vec{r} \times \vec{v})$$

## **Equation #3: Moment of Inertia**

$$I_z = I_x + I_y = \frac{1}{2}MR^2$$

# Side





## **Tabular Data:**

		Mass (kg)		Radius (m)		Predicted		Actual		
Experiment	Trial	A	В	A	В	Angular Momentum A (kg rad/s)	Angular Momentum B (kg rad/s)	Angular Velocity (rad/s)	Angular Momentum A (kg m²/s)	Angular Momentum B (kg m²/s)
	1a									
1	1b									
	1c									
	Average									
							Star	ndard Error		

	Mass (kg)		Radius (m)		Predicted		Actual			
Experiment	Trial	A	В	A	В	Angular Momentum A (kg rad/s)	Angular Momentum B (kg rad/s)	Angular Velocity (rad/s)	Angular Momentum A (kg m²/s)	Angular Momentum B (kg m²/s)
	2a									
2	2b									
	2c									
	Average									
		•	•		•	•	Star	ndard Error		

Experiment	Trial	Mass (kg)		Radius (m)		Predicted		Actual		
		A	В	A	В	Angular Momentum A (kg rad/s)	Angular Momentum B (kg rad/s)	Angular Velocity (rad/s)	Angular Momentum A (kg m²/s)	Angular Momentum B (kg m²/s)
	<b>3</b> a									
3	3b									
	3с									
Average										
Standard Error										

Model	Experiment	Model
Companyation of Diamontum	1	
Conservation of Momentum  Prediction	2	
Prediction	3	
Conservation of Momentum	1	
Actual	2	
Actual	3	
Standard Error of		
Conservation of Momentum		

- 1. What is moment of inertia?
- **2.** How conservative was angular momentum?
- **3.** What was the standard error?
- **4.** Why ever use a null or alternative hypothesis?
- 5. What equation modeled conservation of angular momentum from above?

#### **Glossary:**

**ABOUT** (preposition) – dealt; specific to; central; in apposition to ABOVE (adverb) – on top; greater coordinate; more; important ACCELERATION (noun) – a measure rating velocity differences ACCURATE (noun) - exact; average; agreeable or correct value ACROSS (adverb) - from both sides; the other side; opposite ACT (verb) -exercise; perform; operate; praxis practicing ACTUAL (adjective) - factual; true; exact amount; real quantity ADD (verb) – mathematical magic combining separate numbers ADJACENT (adjective) - nearby; neighbors; beside; next to AESTHETIC (noun, adjective) – artistic movement; beauty AFRICA (noun) - continent; etymology sources foreign phonetics outside the English language; a continent before English AFTER (preposition) - beyond; consecutively; typically, later AFTERNOON (noun) – after 12 o'clock and before 6 o'clock sharp AIR (noun) – gas mixture in the atmosphere around Earth ALONG (preposition) – beside; We walked 'next to' romantic castle walls: the curtain, earthwork, shield, and battlement. ALREADY (adverb) - earlier passage; prior; previously ALSO (adverb) - Furthermore; too ALTERNATIVE (adjective) – another; beside; not exact duplicate **ALTHOUGH** (conjunction) – rather; in spite; as though AMMETER (noun) - instrument measures current in Coulombs per second; Coulombs moving past instrument point per second AMPERAGE (noun) - strength in amperes within electrical circuit AMPLITUDE (noun) - greatest, maximum, or largest in range AN (determiner) – alternative to "a" for consonant or silent vowel AND (conjunction) – abstract list in communication and language ANGLE (noun) - degree; radian; ratio between sides; triangle ANOTHER (determiner) - additionally; and; an other ANSWER (noun, verb) – evaluation; solution; reply; react ANY (determiner, pronoun) – certainly not chosen in group APPARATUS (noun) - tool; equipment; gadget; not instrument APPLICABLE (adjective) - relatable; collateral; reasonable APPLICATION (noun) – particle; document; log; paper for records APPLY (verb) - use or push; spread forward; request; put APPROACH (noun, verb) – action; deal; converse; communicate **ARC** (noun, verb) – shape; story; movement around circular shape ARE (verb) – present tense word expressing state, space, or time **ARGUE** (verb) – conflict; debate; oppose by clear judgement ARISE (verb) - start; become; came into visibility; notice **ARITHMETIC** (noun) – maths with simple operations; real numbers added, subtracted, multiplied, or divided AROUND (adverb) - location nearby and surrounding something ARROW (noun) - long dart; stick with feathers and point ARTICLE (noun) – formal document in journals; legal agreement AS (adverb, preposition, conjunction) – like; similar to; because ASSEMBLE (verb) – group; gather; combine; bring; organize AT (preposition) - in the direction; exactly; about; show ATTEMPT (noun, verb) - initial act; effort; trial; try AUTOMOTIVE (adjective) – combustion engine; road vehicle AVERAGE (noun) - representation; total per number; typical AXIS (noun) - real or imaginary line; coordinate system BACK (adverb) - backward; previously; not forward; earlier **BACKGROUND** (noun, adjective) – scenery behind; lower sound; history in an individual life; profession; role; not nearer; far away BALANCE (noun, verb) - apparatus measuring mass; distribute **BALLOON** (noun, verb) – rubber or cloth bag; expand; increase BASIC (adjective) - simple; not complex; common **BATTERY** (noun) – storage converting chemical to electrical energy with both a cathode and anode for the circuit BEFORE (preposition, adverb, conjunction) – earlier; at a time **BEHAVIOR** (noun) – regular or irregular acts by living creatures **BELOW** (adverb, preposition) – not above; beneath; lower than

**BETWEEN** (preposition, adverb) – halfway; within; space along BEYOND (adverb) - farther than; greater than; outside **BLOCK** (noun, verb) – hard cube; square group; stop, prevent BOB (noun, verb) - quick object; move gently; up and down BODY (noun) -main portion; large part; whole group BOLT (noun, verb) - metal fastener; metallic lock; clamp BOTH (determiner, pronoun) - two things; together BOUNDARY (noun) - real or imaginary line; edge; limit; border BOW (noun, verb) - mid-range weapon; musical stick BRITISH (adjective) - reference to: Great Britain; an island next to Republic of Ireland; sovereign state with 2000+ years history; England, Scotland, and Whales; English people or language BULB (noun) – glass lit by electric arc, filament, gas, or junction BUT (conjunction) - rather; also; except; in addition BY (preposition) – with; proximity; near or next to something CALCULATE (verb) -prove; judge; number; deduce; deliberate CALIBRATE (verb) - mark in units; align; set; check CANDLE (noun) – wax cylinder for lighting space or room CAR (noun) - automotive vehicle; mobile; train; automobile CART (noun, verb) – wagon; small vehicle; push; pull; transport CARTESIAN (noun, adjective) – René Descartes; linear coordinates CENTER (noun, verb) - middle; central; align to point; balance **CENTURY** (noun) – 100 years; Middle English, cent (1/100th) CERTAIN (adjective) - without doubt; truly; factual; likely CHANGE (verb) - alter; make; take; improve; remove; adapt CHARACTER (noun) - particular personality; stereotype; quality CHARGE (noun) - Coulomb (C) unit; One ampere per second CHILDHOOD (noun) - time when humans live before adult CHINA (noun) - nation landmarked by Pacific Ocean, Amur River, Gobi Desert, Tien Shan mountains, and Himalayas CIRCLE (noun) - round shape with constant diameter and no vertex; ring; disc; onion or orange sectioned into planes CIRCUIT (noun, verb) – system fully closed; wire looped; travel CITE (verb) – reference; mention; official speaking or writing **CLASS** (noun, verb) – humans learning together in a room; abstract standard, degree, or ideal; physical attribute, taxon, relation, family, method, or variable; segment; divide **CLASSROOM** (noun) – room with students and teacher; school CLOCK (noun, verb) - instrument measuring time; time **CLOSE** (verb) – shut; not open; "Convenience and meat pie stores are often accessible. Commerce never closes" COEFFICIENT (noun) - multiple; factor; constant term multiplying COLLECT (verb) - gather; bring; receive; ask; accumulate **COLLEGE** (noun) – school after secondary education; university COLLIDE (verb) - hit; crash; jar; moment; violent shock **COMBINE** (verb) – group together; join into whole; organize **COMMISSION** (verb) – formal discovery; administrate **COMMUNICATE** (verb) – speaking, writing, or passing thought **COMPARE** (verb) – examine differences between multiple things **COMPLEX** (adjective) – not simple; difficult; multiple parts **COMPONENT** (noun) – piece in machine or equipment; essential **CONDITION** (noun, verb) – state; arrangement; clause; supposition CONDUCTION (noun) - heat or electricity transport in medium CONDUCTIVE (adjective) - substance passing heat or electricity CONFIDENCE (noun) - personal ability, emotion, skill; dogmatic CONNECT (verb) - link; join; combine; mutual relationship **CONSERVE** (verb) – less waste, damage, or change; sustain CONSTANT (noun, adjective) - value with no variance; value fixed to a number; regular; unambiguous definition; continuous **CONSTRUCT** (noun, verb) – idea or theory; prepare; build; prove CONTACT (noun, verb) – friend; person met; touch; connect CONTAIN (verb) - include; kept; retain; no spreading

**CONTINUOUS** (adjective) – without interruption; nonstop

**CONTRAST** (noun, verb) – clear distinction; discrepancy; mark CONTRIBUTE (verb) - kind effort; generously provide; achieve **CONVECTION** (noun) – heat or electricity flowing in medium **COORDINATE** (noun, verb) – exact point; arrange; align COROLLARY (noun) - theorem with proof; hypothesis from results CORRECT (verb, adjective) - agree; accept; normal; actual; right **CORRELATE** (verb) – affiliate; relate; justify; connect **COSINE** (noun) – function related to angle in a right triangle;  $\cos\theta$ COULOMB (noun) - unit about charge (C); 6.24x1018 electrons per coulomb; Charles-Agustin de Coulomb (R.I.P. 1806), father Henry Coulomb also with unit, electrical inductance (H - Henry) COUNT (verb) - total; sum; recite; combine; consider; discuss **COUNTERWEIGHT** (noun) – weight balancing another weight **CURRENT** (noun, adjective) – coulombs per second; present time CURVE (noun, verb) - continuous line; not straight object; form CYCLE (verb) - repeat; iterate; perform; movement **DATA** (noun) – numbers collected into a form; table; information DAY (noun) - full rotation on Earth; morning to night; 24 hours DELVE (verb) - scour; comb; investigate; examine; search **DEMONSTRATE** (verb) – present; prove; attest; public expressing **DEPEND** (verb) - rely; secondary cause; influence; base **DERBY** (noun) – tournament; competition; championship **DERIVE** (verb) – began; develop; originate source; obtain; get **DESCRIBE** (verb) – communicate; say; write; report; recognize DESIGN (verb) - prepare with style; decorate; make; draw **DESPITE** (preposition) – notice; prevent; without interaction **DESTABILIZE** (verb) – not stable; not settle; upsetting **DETERMINE** (verb) – evaluate; discover; direct; influence **DEVIATE** (verb) – depart; anomalous behavior; vary **DEVICE** (noun) – apparatus; invention; tool; gadget; appliance **DIAGRAM** (noun) – schematic; graphic; plan; operation **DIFFERENT** (adjective) – not similar; diverse; disparate DIFFICULT (adjective) - skill or effort; not easy; hard **DIMENSION** (noun) – measurement: caliber: factor: scale **DIRECT** (verb, adjective) – point; project; straight; associate DISC (noun) – flat object shaped into a circle; dinner plate, frisbee **DISCOVERY** (noun) – action or process founding information DISCRETE (adjective) - separable; divisible; alone; seclusive **DISHWASHER** (noun) – appliance for washing cutlery and flatware **DISPLACE** (verb) – force; take; expel; persecute; move **DISPROVE** (verb) – authenticate; attest; challenge; banter **DISSIMILAR** (adjective) – not exactly same; not identical; atypical DISTANCE (noun, verb) - space; length; scale; avoid **DISTINGUISH** (verb) – notice; recognize; scribe; politically identify **DISTRIBUTE** (verb) – give; provide; transport; sell; spread; supply **DOCUMENT** (noun, verb) – manuscript; note; archive; record **DO** (verb) – independent act; perform; exercise; operate **DOLL** (noun) – toy; puppet; effigy; dummy; mannequin; figure **DOUBLE** (noun, verb, adjective) – substitute; similar; twice **DOWN** (noun, verb, adverb, adjective) – feathers; lower; to; dole DRAG (verb) - pull; force; carry; move; transport; progress DRAW (verb) - sketch; act; make; express; classify; create; define **DURABLE** (adjective) – strong; without damage; persistent **DURATION** (noun) – time length; total period; span; length **DURING** (preposition) – over; through; amidst; by; circa; around EACH (pronoun, adverb) - individual; apiece; all; consider; per **EFFECT** (noun, verb) – consequence; aftermath; cause; condition ELASTIC (noun, adjective) - rubber; resistance to stress; plasticity ELECTRIC (adjective) - power from electricity; intense; 19th century invention during World's Fair; 20th century household commodities; 21st century utilities and central services **ELECTRODYNAMICS** (noun) – experiments about particles moving and properties during movement, such as mass, charge, and spin ELECTRON (noun) - atomic particle with negative charge and onehalf spin; fermion; elementary particle; Joke, "You positive? Not." **ELECTROSTATIC** (adjective) – electricity from stationary objects

**ENERGY** (noun) – potential; power; resource for work ENGINEER (noun, verb) - role building; arrange; design ENTAIL (verb) - involve; has; require; result EQUAL (verb, adjective) - match; equivalent; same amount **EQUATION** (noun) – function; statement; both independent and dependent relationships; representation; interpolate; extrapolate EQUILIBRIUM (noun) - chemical balance; accordance; harmony **ERROR** (noun) – distant; variation; accuracy; precision; mistake ESPECIAL (adjective) - more than; notable; unequivocal ESSENTIAL (adjective) - important; crucial; key; principle EURASIA (noun, adjective) - Europe plus Asia - Eurasia EVALUATE (verb) – consider; judge; calculate; conclude; gauge EVER (adverb) – constantly; continuously; eternally; again EVERY (adjective, determiner) – all members, things, or ideas; all EVIDENCE (noun) - historical, physical, or abstract fact deduction; witness or generalization; induction; corollary **EXACT** (adjective) – correct; definite; accurate; rational **EXAMINE** (verb) – observe; dissect; carefully interpret **EXAMPLE** (noun) – representation; specimen; piece from group **EXEMPLIFY** (verb) – summate; demonstrate; base; benchmark EXIST (verb) - live; reside; feature; actual or real being. **EXPECT** (verb) – predict; believe early; hope; stipulate **EXPERIMENT** (noun, verb) – scientific discovery from tests **EXPLORE** (verb) – search; discover; become familiar; venture EXPOSE (verb) - bring into observation; uncover; present **EXTEND** (verb) – move toward bigger or longer; increase EXTERNAL (adjective) - outside; beyond; exterior; outer EXTRACT (noun, verb) - essence; remove; separate; divide EXTREME (adjective) - maximum; dangerous; greater than regular FAILURE (noun) - not successful; with no standard; no agreement FASTEN (verb) - mantle; join by fixture; hardware affixing **FAVORITE** (adjective) – indefinite; without regret; in satisfaction; in fickle manner; by no fear; emotional; enjoyable; sensual FEET (noun) – unit about length; standard length; 12 inches; 5,280 to one mile; Customary unit measuring length in United States of America from fall of British empire in 1765 to 1783 FIELD (noun, verb) – agriculture; grassland for animals; location by husbandman e.g. farmer; turf; natural grass; mathematical region described by scalars, vectors, or tensors indirectly deal; divide FILM (noun, verb) – pictures moving; cinema; record; animate FINAL (noun, adjective) - terminal; last; end; furthest; eventual FIND (verb) - discover; build; base; bring into existence; FIRST (noun, adjective, adverb) – original; immediate; debut FIVE (noun) – total fingers on hand or edges around pentagon FLOOR (noun) - ground; surface for walking; lowest level FLOW (verb) -continuously moving; liquids or gases moving; FLYWHEEL (noun) – heavy wheel rotating on machinery FOR (preposition) - because; purpose of; as; in agreement with FORCE (noun, verb) – inertia; momentum changing; move FORD (noun) - Henry Ford friend to Thomas Edison; Influential vehicle in history because efficient motors; Ford company producing airplanes, boat, and cars from Detroit, Michigan FORMULA (noun) – standard relationship; acceptable expression FORTH (adverb) - from a point; forward; out; away; into visibility **FOUNDATION** (noun) – organization or state; idea or fact FRAME (noun, verb) - border; structure; outline; enclosure FRAMEWORK (noun) – structure supported by system; structure with ideas, rules, or beliefs for future advancement FREE (verb, adjective, adverb) - not kept; no limit; without cost FREQUENCY (noun) – count about how often; per second; Hertz FRICTION (noun) - force during static and dynamic interface FRIDAY (noun) - day in a week; special day in many religions, cultures, languages, nations, and divinities from celestial bodies **FROM** (preposition) – relationship between cause and effect, initial to final state, or points, such as distance; designate origin

FUNCTION (noun) – natural purpose; mathematical expression passing the vertical line test; official event with ceremony FUNDAMENTAL (adjective) – elementary; essential; important to FURTHER (adverb) - great distance in space, time, level, or degree GAS (noun, verb) - chemical phase; not liquid or solid; fill; empty **GENERATE** (verb) – cause; produce; bring into existence; make GOAL (noun) – aspiration; intention; purpose; aim; objective GOVERN (verb) - steer; authorize; kubernan; gubernare **GRAPH** (noun, verb) – picture about info; plan; chart; map; plot GRAVITY (noun) - physical force from mass; Gravity describes mechanics in tides, seasons, orbit, and growth in vegetation GROUND (noun) - floor; surface below feet; reason or argument GYROSCOPE (noun) - wheel inert to gravity; sensor rotating or vibrating for gravitational measurements by standard proportion HAND (noun, verb) - appendage of four fingers and thumb; move **HAPPEN** (verb, adverb) – occur; do; probably; perhaps; oddly HARMONIC (adjective) – fundamental; frequent; sinusoid in math HAVE (verb) - occur; act; own; verb related to an event or action HEAR (verb) - sense about sound in ear; receive; listen; know HEAT (noun, verb) - energy transferred between substances; first law in thermodynamics; a quality in-home about warmth; warm HEAVY (adjective) - high weight; a lot; strong; catastrophic **HEIGHT** (noun) – distance from ground; length; vertical dimension HELP (verb) - assist; care; improve; facilitate; guide; attend HIGH (adjective) - far from ground; above; aloft; scary distance **HISTORY** (noun) – past events or actions; important topics HOIST (verb) - lift; elevate; pick upward; raise by equipment for HOT (adjective) - high temperature above normal condition; spicy **HOW** (adverb) – what steps; way; critical steps toward outcome **HUMAN** (noun) – ape; surgent animal with vaulted skull; creature adorning stone in complex symbolic world; successful, adept, and resourceful with tools, but unpredictable nature in society; weird HYPOTHESIS (noun) - best guess; explanation; abstract idea IDEAL (noun, adjective) – principle; perfect outcome; immaculate IMPORTANT (adjective) - principle; critical; influential **IN** (preposition) – within; inside; into; part to; interior; segment **INCIDENT** (noun, adjective) – unhappy event; episode; next to INCLINE (noun, verb) - hill; bank; angle; slope; slant; pitch **INCLUDE** (verb) – by smaller parts; antonym to exclude; embody INCORPORATE (verb) – include; acquire; set organized INCREASE (verb) - become large; grow; rise up; big raising **INCREMENT** (noun, verb) – single step; smallest placement; ramp **INDEPENDENT** (noun, adjective) – it alone; not reliant; individual INDIVIDUAL (adjective) – separate; by itself; isolated; single thing INELASTIC (adjective) - not rubber; not plastic; In physics, a situation when kinetic energy decreases after collision by friction INERTIA (noun) – momentum; motion; movement after rest INFORMATION (noun) - tid bits about a situation, person, or event; not always truthful, but typically news or knowledge INHIBIT (verb) - stop; halt; avoid; prevent an action; limit HOME (noun) - residence; In foreign language, ham, heem, or heim. Many synonyms describe a home, such as the apartment, condo, townhouse, mobile, flat, farmhouse, log cabin, chalet, tent, bungalow, pad, dormitory, lodge, crib, penthouse, chamber, suite, tenement, studio, duplex, condominium, castle, and keep INITIAL (noun, adjective) – acronym to pronoun. from the start INSPECT (verb) - observe; look; check; investigate particulars **INSTRUMENT** (noun) – object prospecting character and insight INTENSE (adjective) – strong; potent; major; vigorous; incredible INTERFERE (verb) - interact; involve; connect; propagate; spread INTERMEDIATE (adjective) – between; middle; interim; middle INTERNAL (adjective) - inside; innate; inner; central; privates INTERVAL (noun) – short time; period; numbers between two endpoints; educators write intervals as closed [x1, x2] or open (x1, x<sub>2</sub>). Hominids prefer greater (<) or less (>) than. Also, educators write intervals by sets ( $\subset$ ) and subsets ( $\subseteq$ ).

INTO (preposition) – inside; aspect; enjoyable; inward INVERSE (noun, adjective) - opposite; reverse; contrary; an expression about a function for corresponding between INVESTIGATE (verb) – carefully inspect; examine well INVOLVE (verb) - participate; influence; mate; join IS (verb) – move; separate; indicate; cast an idea **JOULE** (noun) – unit; 1 Joule = 1 Newton-meter; potential; work; heat; energy in a system; James Prescott Joule founded a measure JUSTIFY (verb) - argue with reasonable doubts; reason; bet KELVIN (noun) - unit counting from absolute zero temperature (K) KINEMATICS (noun) – topic in general physics about motion KINETIC (adjective) - about inertia, collisions, rate, and motion LAB (noun) – environment were scientists test ideas for fun or fact LABEL (noun, verb) - information; cultural communication; tag LARGE (adjective) - big; more than average or typical; hefty LATER (adverb) - after; in future time; at the end; toward the end **LAW** (noun) – rules; action or fact about belief; standard opinion; process or argument in city, county, state, or nation; persuasion **LEAD** (noun, verb) – a controller, absent minded; cause, especially by bad events or influence; the first in a funny competition **LEARN** (verb) – increase ability; gain knowledge; practice LEDGE (noun) - flat surface for furniture; a cliffside; abrupt incline LENGTH (noun) - measurement in one-dimension; distance LESS (adverb) - small amount or degree; short; not as much LEVEL (noun, verb) - French invention balancing by gravity, air and water; tool; instrument; horizontally or vertically balance LIFT (verb) - raise; bring upward; hoist; move up; increase LIGHT (noun, verb) - sun; lamp; illumination; luminosity; lit **LIMIT** (noun, verb) – greatest amount; extremum; boundary; Instructors define limits by an argument 'near values'; allow LINE (noun, verb) – long or thin mark; Geometry characterized lines as straight, curve, parallel, perpendicular, or intersect; align LINEAR (adjective) – along a slope or incline; stepwise; straight LITTLE (adjective) - low; tiny; less than average, important, and essential, but greater than diminutive; emphasis about size LOCAL (adjective) – region; province; area; short distance; division LOCATION (noun) - site; exact coordinate; special place LONGITUDE (noun) - geographic lines describing earth; vertical **LOOP** (noun, verb) – circular object, but thin; turn; coil; curve. MACHINE (noun, verb) – equipment; appliance; tool; grind; turn MAGAZINE (noun) - booklet; publication; articles + photographs MAGNITUDE (noun) – scale; urgency; math – distance from zero MAKE (verb) – action with produce; cause; create; issue; model MANY (pronoun, adjective) - multiple things; large number; a lot MARK (noun, verb) - symbol as a clue; judge; correct. MASS (noun, adjective) – unit; kilograms, pounds; tons; large MATCH (noun, verb) - competition; agreement; equal; accord MATHEMATICS (noun) –quantitative and symbolic reasoning MAXIMUM (adjective) – extreme; upper limit; great amount MEAN (noun, verb) - representation; expectation; estimation; In statistics, an estimator without bias to true values MEASURE (noun, verb) – a value; standard; assess by increment MECHANICAL (adjective) - kinetic; automatic; operational MEDIUM (noun, adjective) - conveyance; middle; passage MEMBER (noun) - fellow; mate; compeer; associate MESOPOTAMIA (noun) - region in middle east from Mediterranean Sea to Iraq with stone, metal, water, and wood METAL (noun) – chemical elements described by Periodic Table of Elements up to semi-metals line; substance conducting heat and electricity; hard, ductile, shiny, or malleable, and solid substance METHOD (noun) – way for performing action; particular avenue mg (noun) - milligram; unit about mass; 1/1000 grams MICHIGAN (noun) – state in U.S.A from 1837; 10.14 million pop. MIDLINE (noun) - line dividing left and right or upper and lower MINE (noun, verb) - a hole for coal, metal, or salt in ground; dig MINIMUM (noun) – lowest output, smallest value in range

MODEL (noun, verb) – representation; duplicate; example; copy MOMENT (physics) – how many units over a specific distance MOMENTUM (noun) - inertia; mass multiplied by velocity MOTION (noun) – movement; action; formal agreement MOVE (verb) – displace; direct; force; change; carry; scoot **MULTIMETER** (noun) – originally an instrument from United Kingdom of Great Britain and Ireland measuring volts or amps MULTIPLE (adjective) - more than one; many; divisible number MULTITUDE (noun) - people; large body; crowd NATURAL (adjective) – nature; not artificial; effortless; authentic **NEAR** (verb, adjective, adverb) – close; not far; almost; proximate NECESSARY (adjective) - key; important; essential; particular NEGATIVE (adjective) - numbers less than zero; absence **NEVER** (adverb) – not any; no more; no way; absolutely not **NEW** (adjective) – novel; latest; current; never in the past NEWTON (noun) - unit for force; Isaac Newton derived ideas about inertia, gravity, color, and light with annotation NO (noun, adverb) - for nobody; not I; surely never; hardly NORMAL (adjective) – regular; ordinary; average; usually NOT (adverb) - suspect; doubt; denial and about an action NOTE (noun, verb) - formal post; piece; document; notice NOW (adverb) - currently; not in past or future; ergo NULL (adjective) - empty; in mathematics, empty; without NUMBER (noun, verb) - sign or symbol about amount; count NUT (noun) - the metal lock, jam, cap, or slot by internal thread **OBJECT** (noun, verb) – thing; item; intention; purpose; act OBSERVE (verb) - carefully examine; mark; describe; custom OCCUR (verb) - happen; pass; event; met; found; exist **OF** (preposition) – indicates an origin, expression, possession, position or location nearby; of translates to von in German **ON** (preposition) – above; along; upon; higher; on the top ONE (pronoun, noun) - individual; first natural number **ONTO** (preposition) – on now; action about future tense OPERATE (verb) - effect; work; cause; set; drive; use; go **OPPOSITE** (adjective) – not alike; no resemblance; not equal **OR** (conjunction) – connection between two or more ideas ORIGIN (noun) - initial action, event, or idea e.g. birthplace ORTHOGONAL (adjective) - perpendicular; right angle; square OSCILLATE (verb) – wave; rock; move; repeat; fluctuate; vibrate OTHER (pronoun) – another; in the group; not it, but next to it **OUR** (pronoun) – relationship to multiple people; themselves **OUTCOME** (noun, verb) – conclusion; consequent; result PAPER (noun) – material from wood in sheets for communication PARAGRAPH (noun) – sentences grouped into single statement PARALLEL (adjective) - same sloped lines or edges; not skew **PARAMETER** (noun) – variables measured by an instrument PATH (noun) – pathway; corridor; trail; hall; passage; walkway **PENDULUM** (noun) – device oscillating lower in height by gravity **PER** (preposition) – rate expressed by division in ratio or fraction PERCENT (adverb) - ratio into 100 or one per every 100 (%) PERFECT (adjective) - superb; best; done; fine; top; fair PERIOD (noun, adjective) – length in time; row; historical time PERPENDICULAR (adjective) – angle at 90° to horizontal surface **PERSPECTIVE** (noun) – interpretation; perception; physical angle PHASE (noun, verb) - In chemistry, solid, liquid, gas, or plasma; Physics describes phase by horizontal shift in sinusoids; introduce PHOTOGATE (noun) - light switch sensing movement by laser PHYSICIST (noun) – job with great knowledge in physical universe **PHYSICS** (noun) – in special terminology, thoughts about motion PIANO (noun) - instrument; Twinkle, Twinkle Little Star: G-G-D-D-E-E-D-C-C-B-B-A-A-G-D-D-C-C-B-B-A-D-D-C-C-B-B-A-G-G-D-D-E-E-D-C-C-B-B-A-A-G

PIVOT (noun, verb) – central point for balancing; turn or twist PLAN (noun, verb) – decision about future events; steps; stage PLANE (noun) – 20st century aeroplane first flown in North Carolina by the Wright Brothers in 1903; vehicle for flying

PLANT (noun, verb) - vegetation; garden; dug into the ground PLEASE (verb) - request; ask; beckon; solicit; demand; wish **PLOT** (noun, verb) – arc; diagram; image; chart; show; illustrate POINT (noun, verb) - explanation about ideas or facts; coordinate **POSITION** (noun, verb) – location in spaces, times, or roles; move **POSITIVE** (adjective) – natural numbers; positive integers; hopeful POTENTIAL (noun, adjective) - ability; successful skills or talent **PRACTICE** (noun, verb) – action toward ability; produce ability PRECESSION (noun) – rotation around a point or vertical axis PRECISE (adjective) – precision; variation; dispersion; exactness PREDICT (verb) - future acts with an outcome; future result PREPARE (verb) - brace; shelter; stock; made; equip; plan PRESERVE (verb) - store without fatigue PRESSURE (noun) – unit described by force per area; pounds per square inch; pascals; atmospheres; millimeters of mercury; torr PRIMARY (adjective) - essential; important; top; fundamental PRINT (noun) – transpose; copy; produce by ink on paper; publish PRIOR (adjective) - before; in the past; long ago; earlier; beside PROBLEM (noun) - question; a challenge; difficult situation PROCESS (noun, verb) - method; series; order; steps; perform **PRODUCE** (noun, verb) – end result; effect; generate; create PROFESSOR (noun) - role teaching in university or college PROJECTILE (noun) - object accurately flung or shot into air PRONOUNCE (verb) - specific saying in articulate accent PROOF (noun, verb) - evidence; show truths; declare facts PROPER (adjective) - right; good; official; just, fair; formal **PROPERTY** (noun) – natural relation; physical measure; chemist define properties into intensive and extensive quantities; intensive properties are a ratio between two extensive properties **PROPORTION** (noun) – comparable amount; whole relation PROVE (verb) - particular evidence; exact truth; true argue PROVIDE (verb) - assist; give to; offer; supply; prepare **PROVINCE** (noun) – populous city; busy area; active region PUBLISH (verb) – produce documents; prepare public paper PULLEY (noun) - mechanical equipment for moving objects by wheel and line; a mechanism for lift by rope and pivot PURPOSE (noun, verb) – goal or aim; an idea; construct; fashion QUALITY (noun) - observation; attribute; nature; property QUANTITY (noun) - amount; total; size; bulk; analysis RADIAN (noun) – angle; degree; gradian; steradian; arc; subtend RADIAL (adjective) - outward motion from midpoint; radiative **RADIUS** (noun) – half a diameter; circumference per  $2-\pi$ RAIL (noun) – infrastructure beside traffic direction; metal bar RAMP (noun, verb) - incline; slope; road; angle; path; route RAY (noun) – light; beam; column; source; sunlight; sunbeam **REASON** (noun, verb) – argument; explanation; compare **RECIPROCAL** (adjective) – help each other for advantage; inverse; RECORD (noun, verb) - account; table; list; store; write; note RECURRENT (adjective) - many times; regular; episodic REFERENCE (noun, verb) - quote; mention; cite; report; refer REFLECT (verb) - not transmit, absorb, or refract; bounce; send **REGULAR** (noun, adjective) – often; usual; ordinary; commonly **RELATE** (verb) – associate; agree; describe; reasonably connect **RELATIONSHIP** (noun) – kinship; relation; correspondence RELEASE (verb) - free; move; allow; leave; drop; distribute **RELIABLE** (adjective) - trustworthy; clear; dependable; countable **REPEAT** (verb) – circle; oscillate; revolve; spin; rotate; happen REPRESENT (verb) - write, speak, or listen in place for (an)other(s) REQUISITE (adjective) - important beforehand; necessary RESEARCH (noun, verb) - specific genre; discover; study; pervade RESIST (verb) - fight; refuse; deny; act against an attacker **RESISTOR** (noun) – passive component in electrical circuits measured by Ohms ( $\Omega$ ) for accurate current from source **RESOURCE** (noun, verb) – valuable object for either physical or abstract reason; organization or department specially aiding

RESPECT (noun, verb) - abstract qualities, features, details, events, or actions for admiring; accept; think; accustom **RESULT** (noun, verb) – outcome; effect; response; calculate RIGID (adjective) - not plastic; strong, stiff, or hard; solid RING (noun, verb) - metal looped in a circle; a bell sounding **ROBOT** (noun) – digital machine performing job; mechanical computer forced into eternal labor for servitude and drudgery **ROCKET** (noun, verb) – explosive cylinder burning fuel; quick rise ROPE (noun) - thread twisted into cord; tie; lasso; bind; bound ROTATE (verb) - turning around point or center line; move RULER (noun) – tool measuring length; length with increment SAFE (adjective) - not harmful; not injurious; not dangerous SAME (adjective) - similar; alike; equivalent; identical; next to **SAMPLE** (noun, verb) – small substance for test; test; example **SCHOOL** (noun, verb) – facility for teaching; assembly; educate **SCIENCE** (noun) – careful examination testing nature; measurements focused in systematic analysis and honest inquiry SCIENTIST (noun) – science career in hospital, college, or agency SEA (noun) - saltwater; pelagic water; larger waterbody than lake **SECOND** (noun, verb, adjective, adverb) – after the first instance **SENTENCE** (noun) – expressions combined into a statement SEPARATE (verb, adjective) - divide; bifurcate; not together SERIES (noun) – items ordered by a comparable relationship **SETTING** (noun) – background; environment; place and time SETUP (noun, adjective) - arrangement; association to assembly SHAFT (noun) – long rod or pole on tool, in wheel, or weapon **SHOW** (noun, verb) – theatre; program; display; demonstrate SIMILAR (adjective) - same; comparable; mostly alike; not distinct **SIMPLE** (adjective) – easy; not complex; not difficult; plain **SIMULATE** (verb) – computationally present; mock; create; model SINCE (adverb) – from a past occurrence; in time; at a later time SINE (noun) – ratio between opposite and hypotenuse; sinusoid SINGLE (verb, adjective) - choose; individual; solo; alone; only SINUSOID (noun) - sine wave: oscillatory function: periodic wave **SKETCH** (noun, verb) – simple example; draw; describe; illustrate **SLOPE** (noun, verb) – mountainside; incline; ramp; angle; slant; **SOLID** (noun) – chemical phase with definite volume and shape **SOLUTION** (noun) – aqueous mixture with solutes and solvents **SOLVE** (verb) – detail; explain; prepare; find; define; character **SOON** (adverb) – due time; before the finally; ahead; shortly **SOURCE** (noun, verb) – origin; from the cause; supply; get SPACE (noun, verb) - volume; empty area; make a region; arrange **SPECIFIC** (adjective) – one; particular; obvious; infallible SPEED (noun, verb) – absolute velocity; movement; rate; go SPHERE (noun) – shape like ball, sun, pebble, bubble, or marble **SPRING** (noun, verb) – metal coiled into helix; season; stretch **SQUARE** (noun, verb, adjective) – shape with four similar edges and four right angles; quadrilateral; multiply by itself; 90° angle **STABLE** (adjective) – firm; regular; successful; expectable STALL (noun, verb) – space kept; engine stall; sudden stop **STAND** (verb) – vertically align; make upright; base; pose STANDARD (noun, adjective) – basic criteria; not special; usual **STATIONARY** (noun, adjective) – office supply; not movable **STATISTICS** (noun) – heuristic about proving hypothesis; subject STEEL (noun) – iron composed with minor carbon (2.2% w/w) **STORAGE** (noun) – place holding personal collections; store; **STRING** (noun, adjective) – twine; thread; bind; harness; tie **STRUCTURE** (noun, verb) – arrangement; organization; plan; set **STUDENT** (noun) – person learning in classroom; pupil STUDY (verb) - practice; educate; learn; apply; interpret; parse **SUBMISSION** (noun) – documents given for responsibility SUBSTANTIATE (verb) - prove; dispel; attest; fight; support **SUM** (noun, verb) – calculation; add; total; found; decide SUN (noun) - warm star in sky with regular SUSPEND (verb) - inhibit; stop; prevent; end; limit; judge SYMBOL (noun) - sign, shape, or object, such as a national flag

SYMMETRICAL (adjective) - reflection about an axis **SYSTEM** (noun) – a set; a collection; interaction between pieces TABULATE (verb) – format into a table; arrange; show TAMARACK (noun) - larch; wooded tree; tamarack mine **TANGENT** (noun) – straight line perpendicular to normal; slope with zero-intercept; trigonometric function;  $tan(\theta)=opp/adj$ TARGET (noun, verb) – rings patterned for projectile; focus **TENSION** (noun) – force on a string; stiff and tight string; TERMINAL (adjective) - point toward; from central; final TERM (noun, verb) - values fixed; division in time; name TEST (noun, verb) - exam; discover; qualify; work; produce THE (determiner) – definite article; particular; clear; in context  $\textbf{THEIR} \ (\text{pronoun}) - \text{third-person possessive pronoun about them}$ THEN (adverb, adjective) – preposition to a clause; next; after **THEREOF** (adverb) – aforementioned; respectfully; hereof; allude THERMODYNAMICS (noun) – actions studying heat or work THIRD (noun, adjective, adverb) - not first and not second; 3rd THIS (pronoun) - a person, place, or thing; specifically **THOUGHT** (noun) – an idea; abstract action or event THREE (noun) – number; after two and before four; sum of one and two; prime; ostriches are herbivores with three stomachs THROUGH (adverb) - from one end; from beginning to end THROUGHOUT (adverb) - every piece; the whole time THRUST (noun, verb) - story arc; main point; push rapidly TIME (noun, verb) -minute; hour; day; year; measure duration **TO** (preposition) – an expression for agreeing, needing, or wanting TODAY (noun, adverb) – current day; this day; right now **TOOL** (noun) – equipment with specific purpose; device for repair TORQUE (noun, verb) – force times distance; angular force TOTAL (noun, adjective) - entire; everything; largest; all **TOUCH** (verb) – bring together; bring next to; lightly place **TOWER** (noun, verb) – spire; steeple; keep; donjon; raise above **TRADITION** (noun) – ceremony; heritage; principle or belief TRANSFER (verb) – move; transport; place; arrange; displace **TRANSIENT** (adjective) – temporary; ephemeral; momentary TRANSVERSE (adjective) – perpendicular; incident; normal TRAVEL (noun, verb) – journey; tour; explore; traverse; visit TRIAL (noun, verb) – at/to courtroom; test; assay; burden; judge TRIGONOMETRY (adjective) – math distinguished by triangles TRIPLE (verb, adjective) –multiply by three; three times; more than double, but less than quadruple; to three similar pieces TWO (noun) - one < two < three; an even prime number; number amounting to human eyes, ears, nostrils, legs, arms, and lungs TWO-DIMENSIONAL (adjective) - a space; x-and-y; dimensions for shapes including the triangle, circle, square, or rhombus TYPE (noun, verb) – particular category; a division; attribute UNCERTAIN (adjective) - without knowledge; not clear; unsure UNDER (preposition) - less than; below; not agreeable; lower UNIQUE (adjective) - special; only; uncommon; rare; unusual **UNIT** (noun) – exact quantity; standard measure; single item **UNIVERSAL** (adjective) – everywhere; everyone; without absence UNIVERSE (noun) - all physical matter, earth included UP (adverb) - higher; ascent; near; greater; improve; end **UPON** (preposition) – on; above; onto; atop; there; at; over UPWARD (adverb) -toward; uplift; vertical; upturn; erect **USE** (noun, verb) – purpose; apply; prepare; add; impose UTILIZE (verb) - use; make; purpose; effect; turn; got; give VALIDATE (verb) – authorize; accept; approve; ratify; sign VALUE (verb) – inspect; compare; rate; judge; estimate VARIABLE (noun, adjective) - symbol; letter; not constant; no set VARY (verb) - change; not according; disturb; alter; make VECTOR (noun) - expression with size and direction; carrier VEHICLE (noun) - transportation; car, bus, or truck VELOCITY (noun) - distance per second; movement; rate VERIFY (adjective) - provable; without false claim; unlikely VERSUS (preposition) – against; vs.; comparably; and second

VERTICAL (adjective) - higher; not horizontal; column VIA (preposition) - through; a way to; by; from **VINTAGE** (noun; adjective) – particular; original; official VIRTUAL (adjective) – almost; particular; not real; not done VISUAL (noun, adjective) - picture; image; descript **VOLT** (noun) – unit in electricity; unit (V) for potential per charge **VOLTMETER** (noun) – tool measuring volts by two terminals WAS (verb) – been; verb related to past action, event, or state WATCH (noun, verb) - clock; monitor; check; look; leer; peer **WAVE** (noun, verb) – oscillation; sinusoid; flag; jostle; sway WAVELENGTH (noun) – length unit about one full-period in wave WAX (noun) - hydrophobic organic compound with low melting point; bees prepare wax from glands; candles burn wax WE (pronoun) - nominative pronoun in 1st-person about plural WEIGHT (noun, verb) - mass on earth; scale; test; balance WERE (verb) - simple word about the past tense 'be' WHAT (pronoun) – people, place, thing, action, event, state that WHEEL (noun, verb) – a circle for moving objects on axel; direct WHEN (adverb) - at which time; to what extent; until; a fact that WHERE (adverb) - in what place; Dutch waar and German wo WHICH (determiner) – in the selection; what; before a clause WHILE (noun, conjunction) – the length; together; during; at least WHY (adverb) - for what; reasonably; duly; phonetically /wal/ WIRE (noun, verb) - metal braided or stranded; fasten; connect WITH (preposition) – together; along; additionally; in unison WITHIN (adverb) - inside; coincident; timely; possibly WITHOUT (adverb) – absent action; expression denying with WORD (noun, verb) - expression; collection; particular saying WRENCH (verb) – metal tool with head, profile, and handle; pull WRITE (verb) - communicate; transfer thought or ideas X-DIRECTION (noun) - number line; particular axes; x-coordinate X-POSITION (noun) – first value in coordinate pair; on x-axis Y-COMPONENT (noun) – projection in vector about size on y-axis Y-DIRECTION (noun) - position on y-axis in cartesian space; y-axis Y-POSITION (noun) – second value in coordinate pair; y-location **Z-AXIS** (noun) – axis in Cartesian space perpendicular to x and y