

Exercise 1 Consider the vector $\vec{\mathbf{u}} = \langle a, a - 1 \rangle$.

For how many values of a does the vector $\vec{\mathbf{u}} = \langle a, a - 1 \rangle$ have magnitude $\sqrt{5}$?

Multiple Choice:

- (a) 0
- (b) 1
- (c) 2 ✓
- (d) 3
- (e) more than three, but finitely many
- (f) infinitely many

The values of a for which $|\vec{\mathbf{u}}| = \sqrt{5}$ are $a = \boxed{-1}$ and $a = \boxed{2}$. (type the smaller of the values first)

Hint: The magnitude of $\vec{\mathbf{u}}$ in terms of a is:

$$|\vec{\mathbf{u}}| = \sqrt{\boxed{a^2 + (a - 1)^2}}$$

Setting $|\vec{\mathbf{u}}| = \sqrt{5}$ and squaring both sides gives:

$$\boxed{5} = \boxed{a^2 + (a - 1)^2}$$

After a little algebra, this gives a quadratic equation:

$$\boxed{2}a^2 + (\boxed{-2})a + (\boxed{-4}) = 0$$

This can be factored, and the roots are $a = \boxed{-1}$ and $a = \boxed{2}$. (type the smaller root first)