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Assignment 13: Further Logic Programming

Mathematics is concerned only with the enumeration and comparison of relations.

Preliminaries

This week's assignment is a continuation of our work with miniKanren. So you should need to (require C311/mk) and (require C311/numbers), as these files contain miniKanren and the relational arithmetic system. You should be able to test your solutions with the attached a13-student-tests.rkt

Submit your results to OnCourse in a file named a13.rkt.

Make sure they pass the included tests, but as usual you should also write your own.

NOTE: Remember that, in general, the order of answers in a miniKanren program is irrelevant. Its not mandatory that your answers appear in the same order as below, but do try and check that your relations don't produce incorrect answers when run with fresh logic variables.

NOTE: Also recall that, while generally you want your recursions last, if some of your calls are serious, non-tail calls you might have to change the ordering.

Assignment

1. listo

As a warm-up, first, write the listo miniKanren relation. This is intended to operate similarly to Racket's list?

```
> (run 1 (q) (listo '(a b c d e)))
(_.0)
> (run 1 (q) (listo '(a b c d . e)))
()
> (run 4 (q) (listo q))
(() (_.0) (_.0 _.1) (_.0 _.1 _.2))
> (run 4 (q) (listo `(a b ,q)))
(_.0)
```

For the next two questions, we get a chance to play with the miniKanren relational arithmetic system.

2. facto Build a relation that holds between two backward-binary numbers whenever the second is the factorial of the first. Use the backwards-binary arithmetic primitives found in C311/numbers, and described in chapters 7 & 8 of *The Reasoned Schemer*.

```
> (run 1 (q) (facto q '(0 0 0 1 1 1 1)))
((1 0 1))
> (run 1 (q) (facto (build-num 5) q))
((0 0 0 1 1 1 1))
> (run 6 (q) (fresh (n1 n2) (facto n1 n2) (== `(,n1 ,n2) q)))
((() (1))
((1) (1))
```

```
((0 1) (0 1))

((1 1) (0 1 1))

((0 0 1) (0 0 0 1 1))

((1 0 1) (0 0 0 1 1 1 1)))
```

3. fibs Plain old fibonacci has had its day. Let's do something more fun. And in the process, learn a technique sometimes of use when building miniKanren relations. Here, we're going to take a function fibs which takes one input and returns two values, and make a three-place relation fibso. Check out the definition of fibs:

```
> (define fibs
    (lambda (n)
      (cond
        ((eqv? n 0) (values 1 1))
        (else
          (let ((n- (- n 1)))
            (let-values (((u v) (fibs n-)))
              (let ((u+v (+ u v)))
                (values v u+v))))))))
> (fibs 0)
1
1
  (fibs 1)
  (fibs 2)
  (fibs 3)
3
```

We use values, which allows a Racket function to return multiple output values. This function returns the nth and n+1th fibonacci number. Since fibs returns two values, we need to use let-values when let binding the recursive call. Here, the first answer is bound to u and the second is bound to v. When writing fibso you will need to use two "output variables" in your relation, rather than just one like we usually do.

```
> (run 4 (q)
    (fresh (n o1 o2)
      ((02, 10, n (,o2)) (== q
      (fibso n o1 o2)))
((() (1) (1))
 ((1) (1) (0 1))
 ((0\ 1)\ (0\ 1)\ (1\ 1))
 ((1 1) (1 1) (1 0 1)))
> (run 1 (q)
    (fresh (n o1)
      (== q `(,n ,o1))
      (fibso n o1 (build-num 5))))
(((1\ 1)\ (1\ 1)))
> (run 1 (q)
    (fresh (n o2)
      (== q `(,n ,o2))
      (fibso n (build-num 5) o2)))
(((0 0 1) (0 0 0 1)))
```

4. fo-lavo

In class, Dan demonstrated a relational interpreter written in miniKanren which generates quines. What we have here is a whole different way of making it "run backwards". You might have seen the interpreter fo-lav on Assignment 3. Drop 1bus, ?orez, fi, and *, and instead add etouq and tsil. Your job is to write a relation fo-lavo, which is the transformation of this provided interpreter into miniKanren. You should be able to use your Racket implementation of fo-lav and the val-ofo from class to guide you a good deal of the way. Your relation should be able to produce fo-lav quines.

```
;; fo-lav quines
> (run 1 (q) (fo-lavo q '() '() q))
(((((((_.0 (etouq etouq) tsil) _.0 tsil) (_.0) adbmal)
        etouq)
        (((_.0 (etouq etouq) tsil) _.0 tsil) (_.0) adbmal))
        (=/= ((_.0 closure)) ((_.0 etouq)) ((_.0 tsil)))
        (sym _.0)))
```

Together with the val-ofo code from class, you should be able to build programs in one language which, on given input, generate programs in the other language. Be sure to include the val-ofo code from class and its helpers, so we can watch it work.

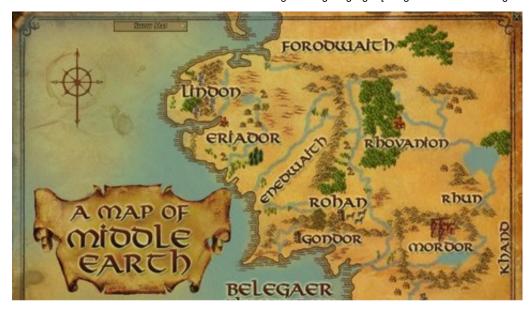
```
> (run 3 (q) (fresh (a c d)
                  (val-ofo `(,a ,d) '() '() c)
(fo-lavo `(,c ,d) '() '() a)
                  (== `(,a ,c ,d) q)))
(((quote ('etouq (_.0) adbmal) ('etouq (_.0) adbmal))
    (=/= ((_.0 closure)) ((_.0 etouq)))
    (sym _.0))
  ((quote
      (((\_.0 \ \mathsf{etouq}) \ ('\mathsf{etouq} \ (\_.1) \ \mathsf{adbmal})) \ (\_.2) \ \mathsf{adbmal})
      (((_.0 etouq) ('etouq (_.1) adbmal)) (_.2) adbmal))
     (=/= ((_.1 closure)) ((_.1 etouq)) ((_.2 adbmal))
          ((_.2 closure)) ((_.2 etouq)))
     (sym _.1 _.2)
     (absento (closure _.0)))
  ((quote
      ((\_.0 \ \mathsf{etouq}) \ (('\mathsf{etouq} \ (\_.1) \ \mathsf{adbmal}) \ (\_.2) \ \mathsf{adbmal}))
      ((_.0 etouq) (('etouq (_.1) adbmal) (_.2) adbmal)))
     (=/= ((_.1 closure))
           ((_.1 etouq))
           ((_.2 adbmal))
           ((_.2 closure)))
     (sym _.1 _.2)
     (absento (closure _.0))))
```

And you can also generate a handful of expressions valid in both languages.

5. Color Middle Earth

If you take a look at a world map, it's colored in by countries. Notice, too that no two adjacent countries are given the same color. The four-color theorem [http://en.wikipedia.org/wiki/Four_color_theorem], that four distinct colors suffice to color any planar graph, was first conjectured in 1852. It stood as an open problem for more than 100 years, until it was proven with the aid of a computer in 1976. The initial proof, by contradiction and by cases for 1,936 cases, raised philosophical questions into what it means to be a proof.

Here, we're not asking you to prove the theorem. We're simply asking you to color a particular graph. Consider the following map of Tolkien's Middle Earth.



As the map is somewhat ambiguous, consider the simplified list representation below, which makes clear which realms (nodes) are adjacent (connected via an edge) to which. For each list, the car of the list is considered to be adjacent to all the realms in the cdr.

```
> (define middle-earth
  '((lindon eriador forodwaith)
    (forodwaith lindon rhovanion eriador)
    (eriador lindon forodwaith rhovanion enedwaith)
    (rhovanion forodwaith eriador enedwaith rohan rhun)
    (enedwaith eriador rhovanion rohan gondor)
    (rohan enedwaith rhovanion rhun gondor mordor)
    (gondor enedwaith rohan mordor)
    (rhun rohan rhovanion khand mordor)
    (mordor gondor rohan rhun khand harad)
    (khand mordor khand)))
```

You may find you don't need this list middle-earth per se, just the information it contains. Write a program color-middle-earth, that takes a list of colors, and uses that as a part of a miniKanren relation to associate a list of colors with an alist containing pairs (node . color). Notice that we aren't asking you to solve the general case, merely this particular graph. Also notice we only ask for one answer. Also, its not necessary to generate this exact coloring: valid coloring will suffice. Moreover, your solution isn't required to "run backwards". The trick to this problem is to just tell miniKanren what needs to be the case. Declare what you want, and miniKanren will color your graph.

```
> (color-middle-earth '(red orange purple black))
(((lindon . red) (forodwaith . orange) (eriador . purple) (rhovanion . red)
      (enedwaith . orange) (rohan . purple) (gondor . red)
      (rhun . orange) (mordor . black) (khand . red)
      (harad . orange)))
```

Just Dessert

In our opinion, we've gotten to do some pretty cool stuff this semester, and we've been able to introduce a whole host of neat ideas and things to play with. The intrepid student this semester has probably been messing around with a couple of these ideas on his or her own. Did something neat with streams? Did you write your own monad transformers? Finally finish that automatic

CPSer? Or perhaps treat lambda calculus as an equational theory viz. miniKanren? Or something else cool?

The point is, if you've done something neat you wanted to show off, now's the time. Toss it in, and explain it to us in a comment. Just be sure it doesn't mess up your autograder submission when you do — if you're messing with modules or additional imports, you might want to comment all that jazz out and then just tell us about it.

But now's the time to strut your stuff!

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