

# Exploration\_WFM1

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7/17/2021

## Packages used

The following packages were used:

```
library(R.matlab)
library(dplyr)
library(caret)
library(MASS)
```

## Reading information

The information is on **.mat** files, and so it must be transformed into a Data Frames via **R.matlab** and **dplyr** packages.

```
data <- readMat('Data/Raw/FeatureMatrices.mat')

unmin <- as.data.frame(data$WFM.1) # Using the first document of 1 minute

feature_names <- unlist(data$FMinfo) # Get column names
colnames(unmin) <- feature_names

unmin <- as.data.frame(unmin)
unmin <- mutate(unmin, Clas = as.factor(Clas)) # Transform the predicted variable to a factor

unmin <- unmin[,c(1:120,length(colnames(unmin)))] # Remove Empatica's variables (EDA TEMP HR HF)

print(head(unmin))
```

```
##   Delta (FP2) Delta (FP1)   Delta (C4)   Delta (C3)   Delta (P8)   Delta (P7)
## 1  0.11643540 -0.10807710 -0.0007967785 -0.021824544 -0.052001271 -0.052366123
## 2  0.08216888  0.09031544 -0.0685819650 -0.025703930 -0.032567698 -0.125933534
## 3  0.13396455  0.03674585  0.1240085263  0.090566646  0.008587199  0.273517209
## 4  0.08577410  0.04645360  0.0868305541  0.028435993  0.065335451  0.215342637
## 5  0.08974345  0.10104639  0.0002082496 -0.008906065  0.001834152  0.004868526
## 6  0.02974833 -0.12397229 -0.0798713713  0.032517547 -0.004881908  0.039584253
##   Delta (01) Delta (02) Theta (FP2) Theta (FP1)   Theta (C4)   Theta (C3)
## 1 -0.14262681 -0.06574524  0.06979229 -0.10023482  0.028478698 -0.092361944
## 2 -0.03696367 -0.03600595  0.07782443  0.02637755 -0.133740130 -0.023413436
## 3  0.19458963  0.16689514  0.13841042  0.05687610  0.143305425  0.113590601
## 4  0.17783968  0.02827166 -0.02372679  0.02989482  0.026600574 -0.001333520
```

```

## 5 -0.07280683 -0.08045784 0.09114603 0.07725917 -0.008292030 0.002163053
## 6 0.02801259 -0.01867924 -0.03278990 -0.24379312 -0.007344334 -0.027462357
##      Theta (P8)  Theta (P7)  Theta (O1)  Theta (O2)  Alpha (FP2)  Alpha (FP1)
## 1 -0.06544173 -0.07803322 -0.08154963 -0.042612373 0.064095119 -1.192098e-01
## 2 -0.05694315 -0.16648136 -0.06419076 -0.013380342 -0.017314926 -1.545495e-03
## 3 0.01735426 0.24849272 0.23423077 0.173923024 0.143913348 6.351154e-02
## 4 0.08405931 0.11828813 0.10736765 0.071394115 0.030066745 -1.902632e-05
## 5 -0.03675589 -0.00619311 -0.04312092 -0.115237194 0.041747758 2.902554e-02
## 6 0.02219570 0.05668009 0.04270302 0.007331088 -0.008774279 -8.920060e-02
##      Alpha (C4)  Alpha (C3)  Alpha (P8)  Alpha (P7)  Alpha (O1)  Alpha (O2)
## 1 0.004581389 -0.01000584 -0.035460413 -0.060126831 -0.09600703 -0.01363575
## 2 -0.045272500 -0.07419167 -0.004620613 -0.065084467 -0.06396609 -0.02152070
## 3 0.205249355 0.10303887 0.040745658 0.165030680 0.27547192 0.12999659
## 4 0.050404753 0.01224851 0.052043003 0.089883492 0.08762201 0.03695271
## 5 0.026771125 0.02443231 -0.021233805 -0.009411168 -0.06158332 -0.04199567
## 6 -0.036117189 -0.02386994 0.019305129 0.039668642 -0.07905597 -0.02377555
##      Beta (FP2)  Beta (FP1)  Beta (C4)  Beta (C3)  Beta (P8)  Beta (P7)
## 1 -0.006055553 -0.09151702 -0.006521960 -0.041936267 -0.02285706 -0.074626616
## 2 0.008422903 0.03103659 -0.069233398 -0.024787664 -0.02198951 -0.056246086
## 3 0.133964159 0.02572089 0.138657713 0.048892236 -0.02480671 0.098044607
## 4 -0.008250105 0.03366403 0.038406550 -0.008405902 0.05658794 0.086350493
## 5 -0.003041084 0.01483961 -0.005814856 -0.006915921 0.01369237 -0.022534921
## 6 -0.100519434 -0.08934101 -0.022341702 0.004814541 -0.01834323 0.001537814
##      Beta (O1)  Beta (O2)  Gamma (FP2)  Gamma (FP1)  Gamma (C4)  Gamma (C3)
## 1 -0.06195664 -0.016539408 0.032580386 -0.07589831 -0.000907479 -0.019117830
## 2 -0.06287619 -0.066806878 0.024391976 0.02794868 -0.042955610 -0.021346301
## 3 0.24008555 0.122599988 0.076839674 0.02380477 0.006026729 0.065713828
## 4 0.07967724 0.046137551 0.003852808 0.01239023 0.039379248 0.010437164
## 5 -0.02613204 -0.034037742 -0.004180727 -0.01069456 -0.026747773 -0.052203955
## 6 -0.05457313 -0.006554387 -0.061319071 -0.06863447 -0.032774287 -0.005948348
##      Gamma (P8)  Gamma (P7)  Gamma (O1)  Gamma (O2)  d/t (FP2)  d/t (FP1)
## 1 0.002288771 -0.022355512 -0.063759173 -0.072860482 1.094513 1.050034
## 2 -0.036451291 -0.075935705 -0.058142849 0.025417432 1.053013 1.125253
## 3 -0.022307056 0.144374762 0.186022865 0.097877342 1.044690 1.039091
## 4 0.001789249 0.097088453 0.113611042 0.020565270 1.166420 1.076298
## 5 -0.019672734 0.008026207 -0.025371014 -0.006619357 1.047438 1.082657
## 6 -0.052534621 0.017598768 -0.008216903 0.020651569 1.116598 1.227107
##      d/t (C4)  d/t (C3)  d/t (P8)  d/t (P7)  d/t (O1)  d/t (O2)  d/a (FP2)  d/a (FP1)
## 1 1.0441860 1.135998 1.073156 1.085699 0.9872727 1.036226 1.150863 1.132103
## 2 1.1556220 1.051608 1.085286 1.107678 1.0883742 1.037533 1.207956 1.220829
## 3 1.0566391 1.032286 1.048825 1.077465 1.0236354 1.055527 1.087368 1.089836
## 4 1.1378361 1.085501 1.039669 1.147967 1.1249086 1.019145 1.156231 1.169928
## 5 1.0839918 1.042437 1.100325 1.068050 1.0247928 1.103626 1.147446 1.196218
## 6 0.9962521 1.119089 1.029917 1.039203 1.0427032 1.034465 1.139538 1.075291
##      d/a (C4)  d/a (C3)  d/a (P8)  d/a (P7)  d/a (O1)  d/a (O2)  d/b (FP2)  d/b (FP1)
## 1 1.094563 1.109797 1.055851 1.111904 1.051007 1.029509 1.304028 1.154395
## 2 1.073587 1.182032 1.044111 1.031023 1.140123 1.070841 1.245856 1.243432
## 3 1.026277 1.110506 1.041079 1.205490 1.037883 1.122424 1.160955 1.188466
## 4 1.138616 1.141168 1.087847 1.229744 1.200076 1.077832 1.271021 1.190377
## 5 1.071985 1.086653 1.099592 1.118696 1.094902 1.043293 1.269002 1.275710
## 6 1.050501 1.188089 1.048782 1.102709 1.236989 1.092606 1.329091 1.131113
##      d/b (C4)  d/b (C3)  d/b (P8)  d/b (P7)  d/b (O1)  d/b (O2)  d/g (FP2)  d/g (FP1)
## 1 1.127422 1.172853 1.083099 1.186834 1.087593 1.085376 1.331941 1.176806
## 2 1.121747 1.147659 1.104322 1.073377 1.222827 1.180252 1.301380 1.293237

```

```

## 3 1.106541 1.194380 1.154626 1.344161 1.146269 1.187623 1.297250 1.234674
## 4 1.173236 1.191419 1.125640 1.296568 1.298110 1.123029 1.332431 1.260287
## 5 1.127753 1.146436 1.103337 1.191446 1.132895 1.087635 1.348090 1.356977
## 6 1.055000 1.180409 1.131706 1.202981 1.293868 1.128597 1.351414 1.146819
## d/g (C4) d/g (C3) d/g (P8) d/g (P7) d/g (O1) d/g (O2) t/a (FP2) t/a (FP1)
## 1 1.142469 1.173755 1.080409 1.160558 1.159745 1.228039 1.0514839 1.0781580
## 2 1.111754 1.171762 1.146886 1.132530 1.294905 1.145686 1.1471423 1.0849372
## 3 1.276311 1.204451 1.178377 1.332428 1.275575 1.295298 1.0408529 1.0488361
## 4 1.194494 1.197969 1.214740 1.326369 1.339470 1.227889 0.9912647 1.0869933
## 5 1.173982 1.230771 1.167342 1.193561 1.204790 1.128101 1.0954787 1.1048919
## 6 1.086718 1.222548 1.199733 1.223180 1.312690 1.171724 1.0205444 0.8762815
## t/a (C4) t/a (C3) t/a (P8) t/a (P7) t/a (O1) t/a (O2) t/b (FP2)
## 1 1.0482452 0.9769354 0.9838739 1.0241365 1.064556 0.9935175 1.191423
## 2 0.9290124 1.1240237 0.9620605 0.9307966 1.047547 1.0321033 1.183134
## 3 0.9712658 1.0757727 0.9926148 1.1188207 1.013919 1.0633776 1.111292
## 4 1.0006854 1.0512817 1.0463397 1.0712368 1.066821 1.0575851 1.089677
## 5 0.9889239 1.0424156 0.9993337 1.0474189 1.068413 0.9453321 1.211530
## 6 1.0544527 1.0616577 1.0183169 1.0611100 1.186329 1.0562035 1.190303
## t/b (FP1) t/b (C4) t/b (C3) t/b (P8) t/b (P7) t/b (O1) t/b (O2) t/g (FP2)
## 1 1.0993878 1.0797139 1.032443 1.009265 1.0931516 1.101614 1.0474312 1.216926
## 2 1.1050237 0.9706866 1.091338 1.017540 0.9690332 1.123536 1.1375563 1.235863
## 3 1.1437560 1.0472267 1.157024 1.100876 1.2475218 1.119802 1.1251470 1.241756
## 4 1.1059920 1.0311117 1.097575 1.082691 1.1294470 1.153970 1.1019329 1.142325
## 5 1.1783147 1.0403709 1.099765 1.002738 1.1155342 1.105487 0.9855108 1.287036
## 6 0.9217717 1.0589689 1.054795 1.098832 1.1575994 1.240878 1.0909951 1.210295
## t/g (FP1) t/g (C4) t/g (C3) t/g (P8) t/g (P7) t/g (O1) t/g (O2) a/b (FP2)
## 1 1.1207311 1.0941240 1.033237 1.006759 1.068950 1.174696 1.185107 1.133087
## 2 1.1492850 0.9620399 1.114258 1.056759 1.022436 1.189761 1.104241 1.031375
## 3 1.1882257 1.2078965 1.166780 1.123522 1.236633 1.246122 1.227158 1.067674
## 4 1.1709462 1.0497948 1.103609 1.168392 1.155407 1.190737 1.204823 1.099280
## 5 1.2533773 1.0830172 1.180667 1.060907 1.117514 1.175642 1.022176 1.105937
## 6 0.9345714 1.0908066 1.092450 1.164884 1.177037 1.258929 1.132686 1.166342
## a/b (FP1) a/b (C4) a/b (C3) a/b (P8) a/b (P7) a/b (O1) a/b (O2) a/g (FP2)
## 1 1.019691 1.030020 1.0568176 1.025808 1.067389 1.034810 1.054266 1.157341
## 2 1.018514 1.044859 0.9709205 1.057667 1.041080 1.072539 1.102173 1.077341
## 3 1.090500 1.078208 1.0755280 1.109067 1.115033 1.104429 1.058088 1.193018
## 4 1.017478 1.030406 1.0440349 1.034741 1.054339 1.081690 1.041933 1.152392
## 5 1.066452 1.052023 1.0550160 1.003406 1.065032 1.034700 1.042502 1.174862
## 6 1.051913 1.004283 0.9935359 1.079067 1.090933 1.045981 1.032940 1.185931
## a/g (FP1) a/g (C4) a/g (C3) a/g (P8) a/g (P7) a/g (O1) a/g (O2) b/g (FP2)
## 1 1.039487 1.043767 1.0576303 1.023260 1.043757 1.103461 1.192839 1.021405
## 2 1.059310 1.035551 0.9913115 1.098433 1.098453 1.135759 1.069894 1.044567
## 3 1.132899 1.243631 1.0845968 1.131881 1.105300 1.229016 1.154019 1.117399
## 4 1.077234 1.049076 1.0497743 1.116647 1.078573 1.116154 1.139221 1.048315
## 5 1.134389 1.095147 1.1326259 1.061614 1.066922 1.100363 1.081288 1.062323
## 6 1.066520 1.034477 1.0290035 1.143930 1.109250 1.061197 1.072412 1.016796
## b/g (FP1) b/g (C4) b/g (C3) b/g (P8) b/g (P7) b/g (O1) b/g (O2) Clas
## 1 1.019414 1.0133463 1.000769 0.9975163 0.9778605 1.066341 1.131441 2
## 2 1.040055 0.9910921 1.021002 1.0385433 1.0551093 1.058944 0.970713 2
## 3 1.038880 1.1534240 1.008432 1.0205704 0.9912714 1.112806 1.090665 2
## 4 1.058729 1.0181193 1.005497 1.0791555 1.0229848 1.031861 1.093372 2
## 5 1.063703 1.0409915 1.073563 1.0580102 1.0017752 1.063461 1.037205 2
## 6 1.013886 1.0300649 1.035698 1.0601103 1.0167909 1.014547 1.038213 2

```

## Information partitioning

We further use the **caret** package in order to divide the whole dataset into a separate training and testing dataset, a seed is used to test with the same division of data.

```
set.seed(1002)

trainIndex <- createDataPartition(unmin$Clas, p = 0.75, list = FALSE)
training <- unmin[trainIndex,]
testing <- unmin[-trainIndex,]
```

## ML models fitting

Data is already normalized, so it does not require pre-processing and can be directly used by ML algorithms. The following function tests a generated model on training and testing data, the parameters are: the ML algorithm and  $k$ , the number of cross-validations used.

A further for loop iterate three algorithms (rf, gmb, lda) with an incremental number of cross-validations, from 2 to **n\_max**.

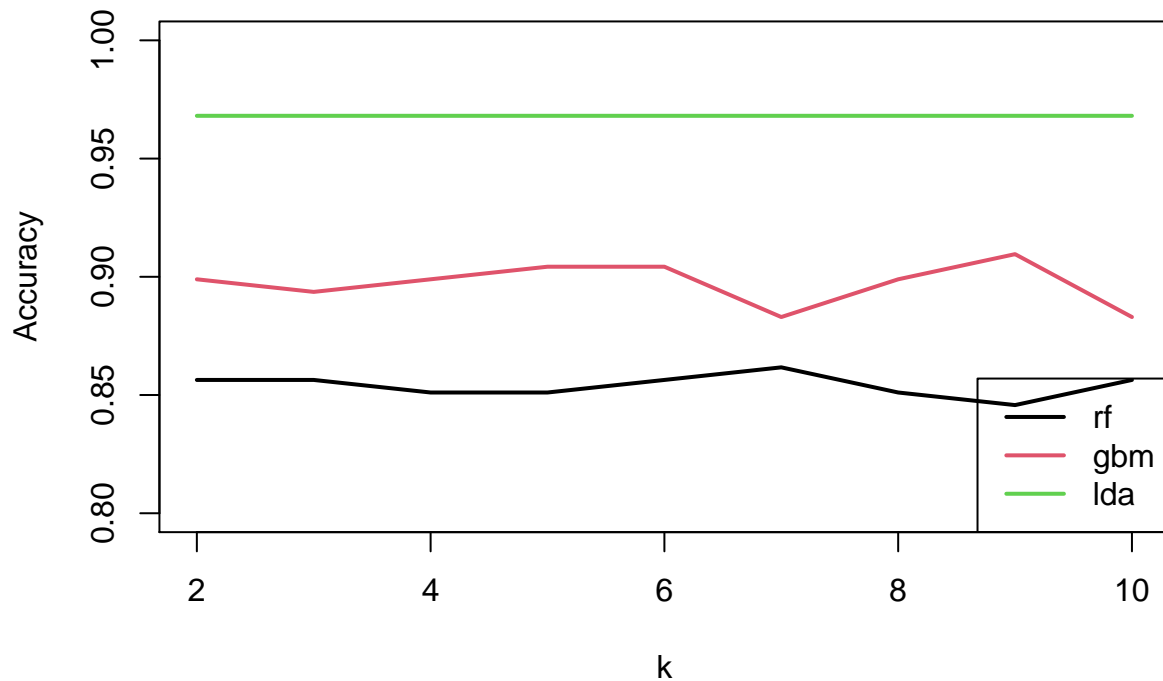
```
prob_modelo <- function(training, met, testing, control){
  if(met == 'gbm'){
    modelo <- train(Clas ~ ., data = training, method = met,
                    trControl = control, verbose = FALSE)
  } else{
    modelo <- train(Clas ~ ., data = training, method = met,
                    trControl = control)}
  Pred <- predict(modelo, testing)
  acc <- round(confusionMatrix(testing$Clas, Pred)$overall[1], 5)
  return(acc)
}

n_max <- 10 # Maximum number of cross-validations (CVs)
metodos <- c('rf', 'gbm', 'lda')
df <- data.frame('rf' = 2:n_max, 'gbm' = 2:n_max, 'lda' = 2:n_max)

for(metodo in metodos){
  acc_l <- c()
  for(num in 2:n_max){
    control <- trainControl(method = 'cv', number = num)
    acc <- prob_modelo(training, metodo, testing, control)
    acc_l <- c(acc_l, acc) }
  df[,metodo] <- acc_l
}

plot(y = df[,1], x = 2:n_max, ylim = c(0.8, 1), xlim = c(2,10), type = 'l', col = 1, lwd = 2,
     ylab = 'Accuracy', xlab = 'k',
     main = 'Accuracy of algorithms with respect to cross-validations')
lines(y = df[,2], x = 2:n_max, col = 2, lwd = 2)
lines(y = df[,3], x = 2:n_max, col = 3, lwd = 2)
legend('bottomright', legend = c('rf', 'gbm', 'lda'), col = 1:3, lty = 1, lwd = 2)
```

## Accuracy of algorithms with respect to cross-validations



As it can be seen on the plot, the LDA (Linear Discriminant Analysis) model outperformed *rf* and *gbm*, it is also not affected by the number of CVs, so it will be further analyzed.

```
modelo_lda <- lda(Clas ~ ., data = training)
```

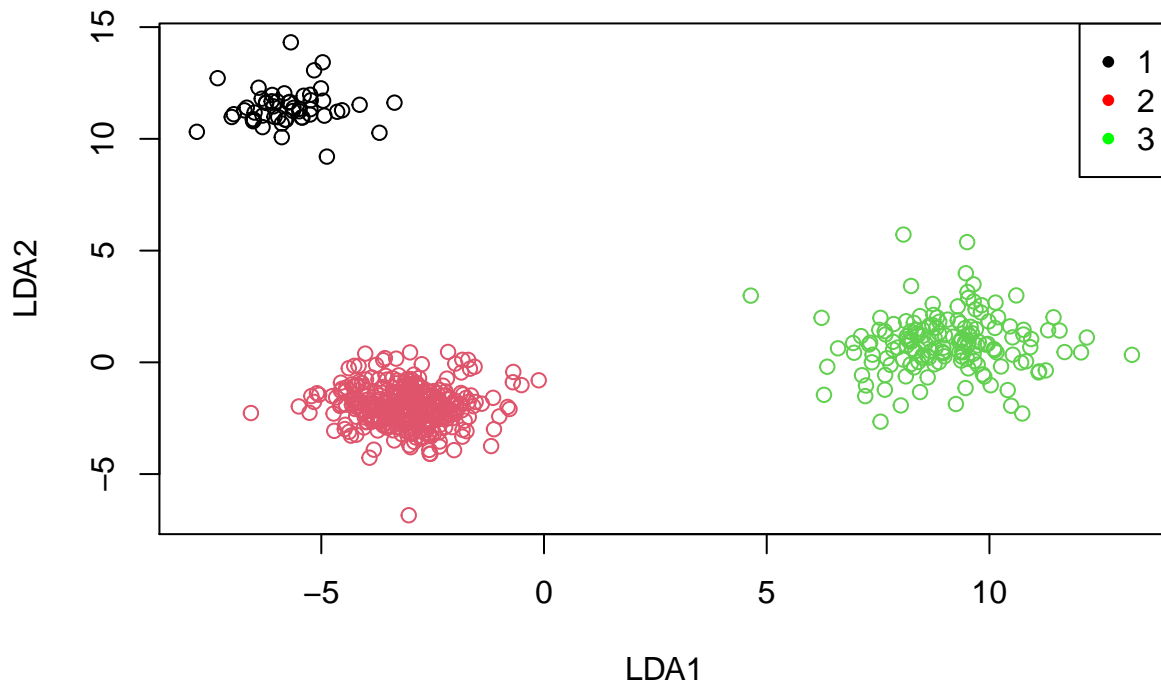
## Model evaluation

In order to visualize the LDAs predictions, we obtain the two most relevant components (LDA1 and LDA2), create a plot of the transformed values and its predicted class on training data.

```
valores <- predict(modelo_lda)

plot(valores$x[,1], valores$x[,2], col = training$Clas, xlab = 'LDA1', ylab = 'LDA2',
     main = 'Clusters of each class')
legend('topright', legend = c(1:3), col = c('black', 'red', 'green'), pch = 20)
```

## Clusters of each class



Using the current weights, the plot on testing data is affected due to an outlier, and thus we compute a confusion matrix on testing data:

```
pred <- predict(modelo_lda, testing)
print(confusionMatrix(testing$Clas, pred$class))
```

```
## Confusion Matrix and Statistics
```

```
##
```

```
##           Reference
```

```
## Prediction  1    2    3
```

```
##           1  17   0   0
```

```
##           2   0 120   0
```

```
##           3   1   5  45
```

```
##
```

```
## Overall Statistics
```

```
##
```

```
##           Accuracy : 0.9681
```

```
##           95% CI : (0.9318, 0.9882)
```

```
##           No Information Rate : 0.6649
```

```
##           P-Value [Acc > NIR] : < 2.2e-16
```

```
##
```

```
##           Kappa : 0.9364
```

```
##
```

```
##           McNemar's Test P-Value : NA
```

```
##
```

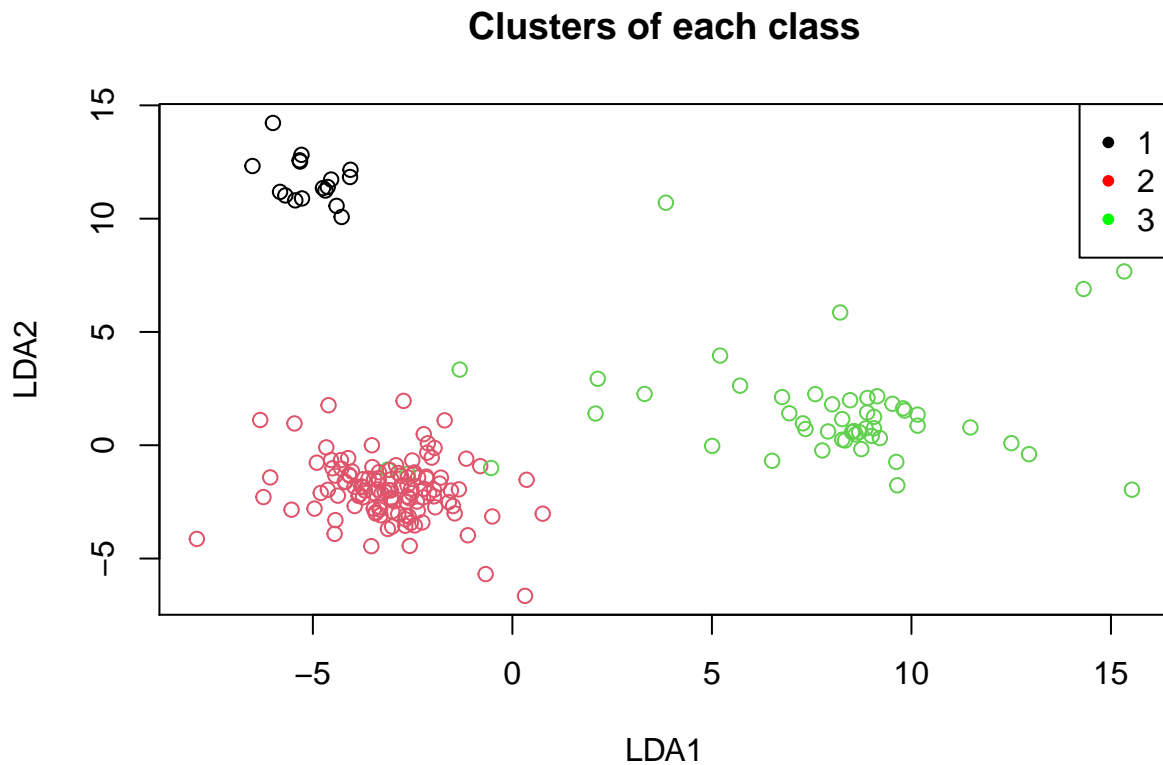
```
## Statistics by Class:
```

```
##
##          Class: 1 Class: 2 Class: 3
## Sensitivity      0.94444  0.9600  1.0000
## Specificity      1.00000  1.0000  0.9580
## Pos Pred Value   1.00000  1.0000  0.8824
## Neg Pred Value   0.99415  0.9265  1.0000
## Prevalence       0.09574  0.6649  0.2394
## Detection Rate   0.09043  0.6383  0.2394
## Detection Prevalence 0.09043  0.6383  0.2713
## Balanced Accuracy 0.97222  0.9800  0.9790
```

The outlier is then padded with the median of the predictions and thus the plot can be visualized.

```
outliers <- pred$x[,1] > 1000
pred$x[outliers,] <- c(median(pred$x[,1]), median(pred$x[,2]))

plot(pred$x[,1], pred$x[,2], col = testing$Clas, xlab = 'LDA1', ylab = 'LDA2',
      main = 'Clusters of each class')
legend('topright', legend = c(1:3), col = c('black', 'red', 'green'), pch = 20)
```



## Plotting the outlier

A visualization of the outlier is presented via an histogram of the value of its features.

```
out_df <- testing[outliers,]
barplot(as.matrix(out_df), las = 2, ylab = 'Standardized value', xlab = 'Feature name',
        cex.names = 0.5, main = paste('Value of row number', row.names(out_df)))
```

