

# Homework 1

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## I. ASSIGNMENT 1

### A. Q1

They should fall at the same speed as all the external forces on them are the same.

Simulation proved it.

### B. Q2

For implicit method,  $\Delta t$  from  $10e-2$  to  $10e-5$  all works well But for explicit method,  $\Delta t$  cannot be too large, testing results shows that even  $10e-4$  still results into disaster (singular value).

## II. ASSIGNMENT 2

### A. Q1

$5.83472e-3$  m/s

#### ■ Velocity vs. time

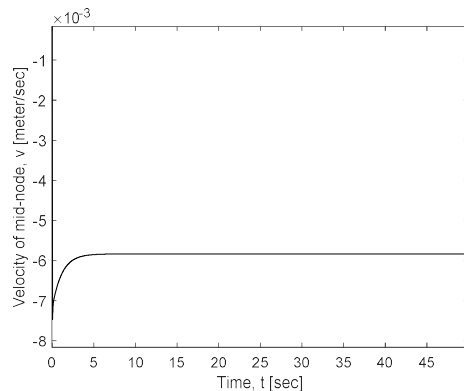


Figure 1. Velocity vs. time

#### ■ Position vs. time

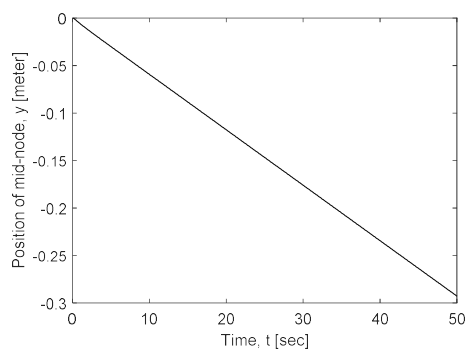


Figure 2. Y position vs. time

### B. Q2

#### ■ Deformed shape

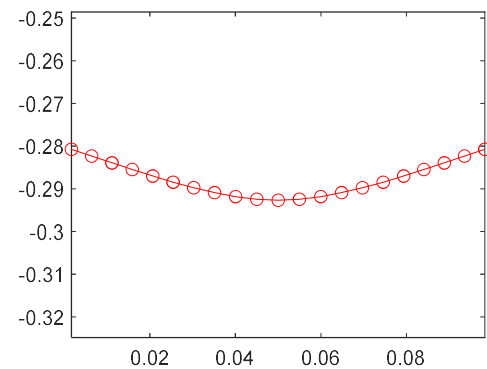


Figure 3. Final deformed shape of beam

### C. Q3

Larger  $dt$  discretization makes more inaccurate velocity error while more nodes make simulation more accurate. It fits intuition, but not should choose appropriate value as the trade-off between accuracy and computation time.

#### ■ Velocity variation vs. dt discretization

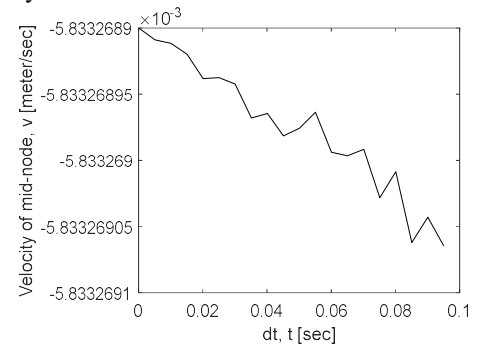


Figure 4. Velocity variation vs. dt discretization

#### ■ Velocity variation vs. nodes number

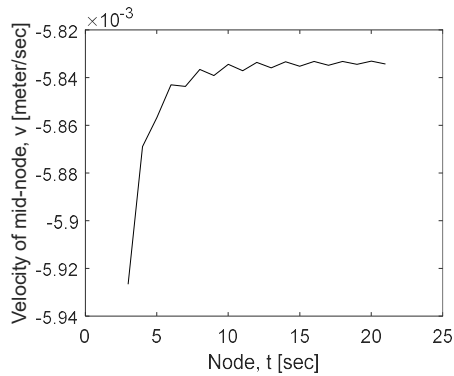


Figure 5. Velocity variation vs. nodes number

### III. ASSIGNMENT 3

#### A. Q1

- If  $P = 2000N$

Theory prediction:

0.038m

Simulation:

0.039m

- If  $P = 20000N$

Theory prediction:

0.3804m

Simulation:

0.2456m

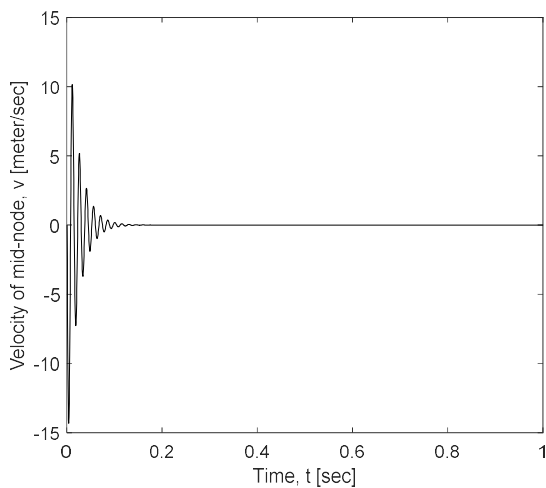


Figure 6. Displacement vs. time

#### B. Q2

The gap between simulation and theory results is going up along with larger and larger  $P$ .

The intersection of  $P$  is less than 500N, but the error bound of  $P=500$  is less than  $10e-4$ .

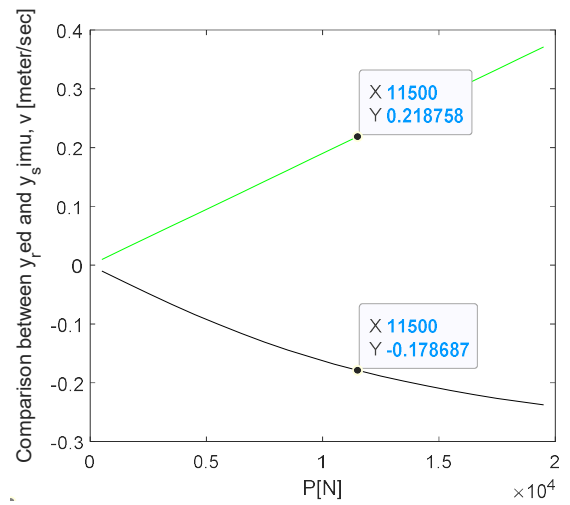


Figure 7. Gap between theory and simulation along with  $P$