Modeling Magnetorheological Fluids

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Abstract

The purpose of this project was to create a simple model of a magnetorheological fluid in order to examine the structural trends as a function of magnetic to non-magnetic particle ratio and external field strength. The rheological properties were examined by testing the ability of a massive projectile to penetrate the fluid.

Introduction

Magnetorheological fluids, similar to their ferrofluid cousins, have the ability to be controlled by magnetic fields. Composed of a micrometer sized magnetic particles suspended in a non-magnetic medium, the application of an external magnetic field induces two conformational changes. A magnetic particle experiences an interaction force with those surrounding it, but the random alignment of the magnetic poles prevents this force from creating a global structure amongst them. With the application of an external magnetic field, the torsion aligns the magnetic along the field. This uniformity causes the magnetic pole interactions to create chain-like structures amongst the magnetic particles. These chain structures increase the apparent magnitude of the fluid and may cause the fluid to become a viscoelastic solid. This property gives MR fluids applications in vehicle shock absorbers, prosthetics, and impact resistant materials. The goal of creating a model of MR fluids was to look at trends in its rheological properties by examining the viscosity under varying magnetic field strengths as well as varying magnetic to non-magnetic particle ratios.

The simulation was written in C and is available at github.com/millerjs/MagRheol. There is a preprocessor definition that relies on GNU_SOURCE and therefore the code has only been tested on a GNU linux machine.

Fluid Model

The model presented on this paper is based on the work of Y. Ido, T. Inagaki, and T. Yamaguchi[1]. For simplicity, the model fluid is composed of uniform, hard, spherical particles suspended in a carrier fluid. The magnetic particles are approximated to be dipoles. Particle parameters used in this simulation mirror those in the Ido simulation. The magnetic material is approximated to be ${\rm ZnFe_2O_4}$ in particles of radius $1.5\mu{\rm m}$ with a density of $\rho=2.5\times10^{-4}$ kg m⁻³. The non-magnetic particles maintain the same properties aside from the lack of magnetic dipole moment.

Domain and Magnetic Field

This simulation ignores the effect of the fluid on the magnetic field, and the field strength and direction is considered constant throughout the domain. The domain was constructed by selecting the number of particles used in the simulation, a cubic number for convenience, and using this to determine the domain size. For example, for a simulation with 343 particles, the domain volume was approximated as

$$V = \frac{\text{no. of particles}}{\text{particle dens}}$$

$$\text{particle dens} = \frac{\rho}{m_{\text{particle}}}$$

$$m_{\text{particle}} = m_{\text{molecule}} \times \frac{\text{molecules}}{\text{particle}}$$

$$m_{\text{molecule}} = \frac{m_{ZnFe_2O_4}}{N_A}$$

$$\frac{\text{molecules}}{\text{particle}} \approx \frac{r_{particle}^3}{r_{molecule}^3}$$

This calculation provided for a cubic domain on the order of $40\mu m$ in length. The external magnetic field was $-H\hat{z}$ across the domain. During the initial creation of the model the boundary condition PERIODIC was applied to all faces of the domain. All distances calculated for directions with periodic faces used the minimum image convention. I found that the periodic boundary condition was especially important for the faces perpendicular to magnetic field. This not only allowed the fluid to behave as if it were in a larger domain but also prevented the truncation of particle chains near the boundaries that would be seen in a non-physically small domain from a lack of dipole attraction across the border. This condition is necessary because the dipole interaction force was not mirrored across a reflecting boundary condition in this simulation. The REFLECTING boundary condition was created simply by reflecting the velocity of particles crossing the face.

The code reads in a parameter config file to avoid compilation for every new initial setup. Included below REFERENCES Joshua Miller

is a sample config file:

magrheol config file # maxt in 1e-4 seconds 12. checkpoint_interval= 50 dt= .001 # Particle counts/ratio 343 ratio= . 5 # dimensions in micrometers X= 4.223095e+01 Y= 4.223095e+01 Z= 4.223095e+01 # Magnetic field and dipole 70 MU= .01

Forces/Torques

Due to the reduction of the magnetic particles to spheres with dipole moments, the forces needed to simulate the fluid included $F_{\rm rep}$, the physical repulsion force, $F_{\rm Dipole-Dipole}$, the dipole interaction between magnetic particles, and $F_{\rm drag}$. Because the particles are on the micrometer scale, the random force due to Brownian motion was considered negligible. The forces used were as derived in the Ido paper[1]. The repulsion force was based on the DLVO theory which is derived from the van der Waal's attraction and the Double Layer force caused by charge dissociation at particle surfaces.

$$F_{rep} = \frac{3\mu_s^2}{64\pi\mu_0 R^4} e^{(-\kappa S)} \frac{\vec{r}}{||\vec{r}||}$$

where S is the distance between the surfaces of the two particles 1 . The Dipole-Dipole interaction force was

$$F_{Dipole} = \frac{3}{4\pi\mu_0 ||\vec{r}||^4} \left[(\mu_i \cdot \mu_j) \frac{\vec{r}}{||\vec{r}||} - 5(\mu_i \cdot \vec{r})(\mu_j \cdot \vec{r}) \frac{\vec{r}}{||\vec{r}||} + ((\mu_i \cdot \vec{r})\mu_j + (\mu_j \cdot \vec{r}\mu_i)) \frac{1}{||\vec{r}||} \right].$$

The drag force was applied with Stokes' drag,

$$F_{drag} = -6\pi \eta r \vec{v},$$

where the particle radius was used for the Stokes radius. In order for the particles to align to the magnetic field, the must experience a torque. The torque on a magnetic dipole in an external field is

$$T_H = \vec{\mu} \times \vec{H}$$
.

Furthermore each magnetic particle experiences a torsion force from the dipoles around it,

$$T_{Dipole} = \frac{1}{4\pi\mu_0||\vec{r}||^3} \left(\mu_i \times \mu_j - \frac{3}{||\vec{r}||^2} (\mu_j \cdot \vec{r}) \mu_i \times \vec{r}\right).$$

Both the positions and the orientation of the dipole moment were evolved using Verlet integration. Because

long evolution and the small time step that were necessary, I decided to parallelize the verlet algorithm in order to utilize any available cores. I created a pool of pthreads. Each thread performs $\frac{1}{N}$ th of the forces and verlet integration where N is the number of threads set to be used. The inclusion of this scheme necessitated an update in the integration. Due to the race condition introduced by the threading, the data belonging to thread was not guaranteed to be at the right time step when viewed by another thread. To handle this, the data was stored in pre-allocated temporary arrays. Each thread utilized a thread barrier to wait until all threads had updated their positions to a temporary memory location before the master thread performed calculations involving projectile position and performed output writes to checkpoints. After the thread barrier was reached, the variables pointing to the (old and new) position and dipole vectors were rotated. Using 16 cores I was able to achieve approximately a 1200% speedup. Even with this parallelization, simulations were relatively costly, making it difficult to verify parameters such as the time step and gather quantitative data on the rheological properties of the fluid.

References

- [1] Y. Ido, T. Inagaki, and T. Yamaguchi. Numerical simulation of microstructure formation of suspended particles in magnetorheological fluids. Journal of Physics: Condensed Matter. IOP Publishing. 15 July 2010.
- [2] Spinks, Joseph Michael. Dynamic simulation of particles in a magnetorheological fluid. PhD diss., Monterey California. Naval Postgraduate School, 2008.
- [3] ViSit Visualization, animation and analysis tool. https://wci.llnl.gov/codes/visit/

¹This repulsion convention was novel to me. I found it extremely interesting because of its generality to varied surface topologies.