## **GLM1** reference table

|                       | Notation       | Definition   | Formula   |  |
|-----------------------|----------------|--|---|--|
| Mean                  | $\overline{Y}$ | The average of the numbers   | $\frac{\sum x}{n} = \frac{Sum}{sample \ size}$  |  |
| Individual value      | $y_i$          |  |   |  |
| Deviation             |                | A measure of<br>difference between<br>the observed value<br>of a variable and the<br>mean                              | $(x_i - \bar{x})^2$ = the difference between the individual value and the mean                                      |  |
| Degree of freedom     | df             | The maximum number of logically independent values, which are values that have the freedom to vary, in the data sample | n - 1   |  |
| Variance              | $\sigma^2/S^2$ | A measure of how spread-out numbers are  | $\frac{\sum (x_i - \bar{x})^2}{n - 1} = \frac{square \ of \ deviation}{degree \ of \ freedom}$                      |  |
| Total Sum of Squares  | SSET,<br>SST   | Squared differences<br>between the<br>observed dependent<br>variables and its<br>mean                                  | $\sum (Y_i - \overline{Y})^2 =$ sum of squared deviation  |  |
| Standard<br>Deviation | σ/S            | A measure of the amount of variation or dispersion of a set of values  | $\sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{variance} = \frac{total\ sum\ of\ squares}{degree\ of\ freedom}$ |  |
| Standard<br>Error     | SE             | The standard deviation of its sampling distribution or an estimate of that standard deviation                          | $rac{\sigma}{\sqrt{n}} = rac{	ext{Standard deviation}}{	ext{sample size}}$  |  |
| Predicted value       | Ŷ              |  |   |  |

| Sum of squares error                | SSEA,<br>SSE          | Difference between<br>the observed value<br>and the predicted<br>value                        | $\sum (y_i - \hat{y})^2$  |
|-------------------------------------|-----------------------|---|---|
| Reduced<br>error                    | SSER,<br>SSR          | The sum of the differences between the predicted value and the mean of the dependent variable | SST-SSE <sub>A</sub>  |
| Proportional reduction in Error     | PRE or R <sup>2</sup> | The ratio of reduced<br>error (SSR) to initial<br>total error (SST)                           | SSR/SST   |
|                                     | $b_1$                 |   | 1. Conceptual formula   |
| Regression coefficient              |                       |   | $\frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}$  |
|                                     |                       |   | $= \frac{sum \ of \ (x \ deviation*ydeviation)}{sum \ of \ squared \ x \ deviation}$  |
|                                     |                       |   | 2. Computational formula  |
|                                     |                       |   | $\frac{\sum XY - \frac{(\sum X)(\sum Y)}{n}}{(\sum X)^2}$   |
|                                     |                       |   | $\sum X^2 - \frac{(\sum x)^2}{n}$   |
| Regression intercept                | $b_0$                 |   | $\overline{Y} - b_1 \overline{X}$   |
| Pearson's r correlation coefficient | r                     |   | $\frac{\sum (X-\bar{X})(Y-\bar{Y})}{\sqrt{((X-\bar{X})^2\sqrt{(Y-\bar{Y})^2}}} =$   |
|                                     |                       |   | $\frac{\sum XY - \frac{\sum X \sum Y}{n}}{\sqrt{\sum X^2 - \frac{(\sum X)^2}{N}} \sqrt{\sum Y^2 - \frac{(\sum Y)^2}{N}}} =$ |
|                                     |                       |   | $\frac{SS_{XY}}{\sqrt{SS_XSS_Y}}$   |

|   |            | $\overline{Y_1} - \overline{Y_2}$  |                                 |
|---|------------|--|---------------------------------|
| T-Test statistics                               | t          | $\frac{\overline{Y_1} - \overline{Y_2}}{S^2_{pooled}} \text{ where}$   |                                 |
|   |            | $S^2_{pooled}$   |                                 |
|   |            | $=\sqrt{\frac{(N_1-1)S_1^2+(N_1-1)S_1^2}{N_1+N_2-2}}$  |                                 |
| F test statistics                               | $F_{obt}$  | $\frac{\textit{Between-groups variability}}{\textit{Within-groups variability}} = \frac{1}{2}$                         | $\frac{MS_{BG}}{MS_E} =$        |
|   |            | $\frac{SSB/df}{SSW/df}$  |                                 |
| Degrees of freedom between groups               | $df_{BG}$  | k-1 where $k = number of$  |                                 |
|   |            | levels/groups/conditions   |                                 |
| Degrees of freedom within groups                | $df_E$     | N-k  |                                 |
| Sum of<br>degrees of<br>freedom                 | $df_{Tot}$ | N-1  |                                 |
| Proportion of variability in Y explained by X   | SSB        | $\left[\frac{(\sum Y_{Group1})^{2}}{N_{Group1}}\right] + \left[\frac{(\sum Y_{Group2})^{2}}{N_{Group2}}\right] - $     | $-\frac{(\sum Y)^2}{N_{Total}}$ |
| Proportion of variability in Y unexplained by X | SSW        | $\sum Y^2 - \left[\frac{(\sum Y_{Group1})^2}{N_{Group1}}\right] + \left[\frac{(\sum Y_{Group1})^2}{N_{Group1}}\right]$ | oup2) <sup>2</sup> ]            |