

Object Initialization in X10

Abstract

X10 is an object oriented programming language with a sophisticated type system (constraints, class invariants, non-erased generics, closures) and concurrency constructs (asynchronous activities, multiple places). Object initialization is a cross-cutting concern that interacts with all of these features in delicate ways that may cause type, runtime, and security errors. This paper discusses possible designs for object initialization, and the “hardhat” design chosen and implemented in X10 version 2.2. Our implementation includes a fixed-point inter-procedural (intra-class) data-flow analysis that infers, for each method called during initialization, the set of fields that are read, and those that are asynchronously and synchronously assigned. Finally, we formalize the essence of initialization checking with an effect system intended to complement a standard FJ style formalization of the type system for X10. This system is substantially simpler than the masked types of [9]. To our knowledge, this is the first formalization of a type and (flow-sensitive) effect system for safe initialization in the presence of concurrency constructs. This formalization can be extended to cover all the features discussed in the first part of the paper.

1. Introduction

Constructing an object in a safe way is not easy: it is well known that dynamic dispatch or leaking `this` during object construction is error-prone [1, 5, 10], and various type systems and verifiers have been proposed to handle safe object initialization [3, 6, 9, 11]. As languages become more and more complex, new pitfalls are created due to the interactions between language features.

X10 is an object oriented programming language with a sophisticated type system (constraints, class invariants, non-erased generics, closures) and concurrency constructs (asynchronous activities, multiple places). This paper shows that object initialization is a cross-cutting concern that interacts with other features in the language. We discuss several language designs that restrict these interactions, and explain why we chose the *hardhat* design for X10.

Hardhat was termed in [5] and it describes a design that prohibits dynamic dispatch or leaking `this` (e.g., storing `this` in the heap) during construction. A hardhat design limits the user but also protects her from future bugs (see Fig. 1 below for two such bugs). X10’s hardhat design is even stricter due to additional language features such as concurrency, places, and closures.

On the other end of the spectrum, Java and C# allow dynamic dispatch and leaking `this`. However, they still maintain type and runtime safety by relying on the fact that every type has a default

value (also called zero value, which is either 0, `false`, or `null`), and all fields are zero-initialized before the constructor begins. As a consequence, a half-baked object can leak before all its fields are set. Phrased differently, when reading a final field, one can read the default value initially and later read a different value. Another source of subtle bugs is due to the synchronization barrier at the end of a constructor [8] after which all assignments to final fields are guaranteed to be written. The programmer is warned (in the documentation only!) that immutable objects (using final fields) are thread-safe only if `this` does not escape its constructor. Finally, if the type-system is augmented, for example, with non-null types, then a default value no longer exists, which leads to complicated type-systems for initialization [3, 9].

C++ sacrifices type-safety on the altar of performance: fields are not zero-initialized. (X10 has both type-safety and the performance for not zero-initializing fields.) Therefore if `this` leaks in C++, one can read an uninitialized field resulting in an arbitrary value. Moreover, method calls are statically bound during construction, which may result in an exception at runtime if one tries to invoke a virtual method of an abstract class (see Fig. 4 below). (Determining whether this happens is intractable [4].) We believe a design for object initialization should have these desirable properties:

Cannot read uninitialized fields One should not be able to read uninitialized fields. In C++ it is possible to read uninitialized fields, returning an unspecified value which can lead to unpredictable behavior. In Java, fields are zero initialized before the constructor begins to execute, so it is possible to read the default or zero value, but never an unspecified value.

Single value for final fields Final fields can be assigned exactly once, and should be read only after assigned. In Java it is possible to read a final field before it was assigned, therefore returning its default value.

Immutable objects are thread-safe Immutable classes are a common pattern where fields are `final/const` and instances have no mutable state, e.g., `String` in Java. Immutable objects are often shared between threads without any explicit synchronization, because programmers assume that if another thread gets a handle to an object that that thread should see all assignments done during initialization. However, weak memory models today do not necessarily have this guarantee and immutable objects could be thread-unsafe! Fig. 1 below will show that this can happen in Java if `this` escapes from the constructor [8].

Simple The order of initialization should be clear from the syntax, and should not surprise the user. Dynamic dispatch during construction disrupts the order of initialization by executing a subclass’s method before the superclass finished its initialization. This is error-prone and often surprises the user.

Flexible The user should be able to express the common idioms found in other languages with minor variations.

Type safe The language should continue to be statically type-safe even if it has rich types that do not have a default or zero value, such as non-null types (`T{self!=null}` in X10’s syntax). Type-

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```

class A {
    static HashSet INSTANCES = new HashSet();
    final int a;
    A() {
        a = initA(); // dynamic dispatch!
        System.out.println(toString()); //again!
        INSTANCES.add(this); // leakage!
    }
    int initA() { return 1; }
    public String toString() { return "a="+a; }
}
class B extends A {
    int b = 2;
    int initA() { return b+42; }
    public String toString() {
        return super.toString()+"b="+b; }
    public static void main(String[] args) {
        new B(); // prints: a=42,b=0
    }
}

```

Figure 1. Two initialization pitfalls in Java: leaking `this` and dynamic dispatch during construction.

safety implies that reading from a non-null type should never return null. Adding non-null types to Java [2, 3, 9] has been a challenge precisely due to Java’s relaxed initialization rules.

We took the ideas of prohibiting dynamic dispatch or leaking `this` during construction from [5], and materialized them into a set of rules that cover all aspects of X10 (type-system, closures, generics, properties, and concurrent and distributed constructs). This hardhat design in X10 (version 2.2) has the above desirable properties, however they come at a cost of limiting flexibility: it is not possible to express cyclic immutable structures in X10. We chose simplicity over flexibility in our design choices, e.g., X10 prohibits creating an alias of `this` during object construction (whereas a more flexible design could track aliases via alias-analysis, at the cost of sacrificing simplicity). Alternative designs for initialization are described in Sec. 3, such as the `proto` design (which was part of X10 version 2.0) that allows cyclic immutable structures at the cost of a more complicated design. To our knowledge, X10 is the first object-oriented (OO) language to adopt the strict hardhat initialization design.

The *contributions of this paper* are: (i) presenting a complete and strict hardhat design in a full-blown advanced OO language with many cross-cutting concerns (especially the concurrent and distributed aspects), (ii) discussing alternative designs, such as the `proto` design, (iii) implementation inside the X10 open-source compiler and converting the entire X10 code-base (+200K lines of code) to conform to the hardhat principles, (vi) FX10 formalism which is the first to present a flow-sensitive effect system with concurrency constructs and a soundness theorem stating that one can never read an uninitialized field in a statically correct program.

The remainder of this introduction presents error-prone sequential initialization idioms in Sec. 1.1, thread-unsafe immutable objects and serialization in Sec. 1.2, and common initialization pitfalls in parallel X10 programs in Sec. 1.3.

1.1 Initialization pitfalls in sequential code

Fig. 1 demonstrates the two most common initialization pitfalls in Java: leaking `this` and dynamic dispatch. We will first explain the surprising output due to dynamic dispatch, and then the less known possible bug due to leaking `this`.

Running this code prints `a=42,b=0`, which is surprising to most Java users. One would expect `b` to be 2, and `a` to be either 1 or 44. However, due to initialization order and dynamic dispatch, the user sees the default value for `b` which is 0, and therefore the value of

`a` is 42. We will trace the initialization order for `new B()`: we first allocate a new object with zero-initialized fields, and then invoke the constructor of `B`. The constructor of `B` first calls `super()`, and only afterward it will run the field initializer which sets `b` to 2. This is the cause of surprise, because *syntactically* the field initializer comes before `super()`, however it is executed after. (And writing `b=2;super();` is illegal in Java because calling `super` must be the first statement). During the `super()` call we perform two dynamic dispatches: the two calls (`initA()` and `toString()`) execute the implementation in `B` (and recall that `b` is still 0). Therefore, `initA()` returns 42, and `toString()` returns `a=42,b=0`. This bug might seem pretty harmless, however if we change the type of `b` from `int` to `Integer`, then this code will throw a `NullPointerException`, which is more severe.

The second pitfall is leaking `this` before the object is fully-initialized, e.g., `INSTANCES.add(this)`. Note that we leak a partially-initialized object, i.e., the fields of `B` have not yet been assigned and they contain their default values. Suppose that some other thread iterates over `INSTANCES` and prints them. Then that thread might read `b=0`. In fact, it might even read `a=0`, even though we just assigned 42 to `a` two statements ago! The reason is that this write is guaranteed to be seen by other threads only after an implicit synchronization barrier that is executed after the constructor ends. Sec. 1.2 further explains final fields in Java and the implicit synchronization barrier.

The hardhat design in X10 (described in Sec. 2) prevents both pitfalls, because its rules prohibit leaking `this`, and they only allow calling private or final methods (which cannot be overridden). It is possible to annotate a method with `@NoThisAccess`, which allows overriding but prohibits any access to `this`. This can be useful, e.g., if you want to subclass and override a factory method to change the concrete type of the object constructed, when the original class uses the factory method in its constructor. It is possible to fix the bugs in this example by following the hardhat initialization rules in the following way: (i) Instead of leaking `this` in the constructor, we should add factory methods to create instances of `A` and `B`, and add the new fully-initialized instance to `INSTANCES` in the factory methods. (ii) We should mark `initA` as `@NoThisAccess`, and so it can be overridden in `B`, but cannot access field `b`. (iii) We need to define a private or final method `toStringOnlyA`; this method cannot be overridden so it can be called during construction; the public non-final method `toString` could delegate to `toStringOnlyA`.

The hardhat design of X10 guarantees that a field can be read only after it was written. Therefore, there is no need to zero-initialize all fields before executing the constructor (as done in Java).

1.2 Final fields, Concurrency, and Serialization

We will start with an anecdote: suppose you have a friend that playfully removed all the occurrences of the `final` keyword from your legal Java program. Would your program still *run* the same? On the face of it, `final` is used only to make the *compiler* more strict, i.e., to catch more errors at compile time (to make sure a method is not overridden, a class is not extended, and a field or local is assigned exactly once). After *compilation* is done, `final` should not change the *runtime* behavior of the program. However, this is not the case due to interaction between initialization and concurrency: a synchronization barrier is implicitly added at the end of a constructor [8] ensuring that assignments to *final* fields are visible to all other threads. (Assignments to non-final fields might not be visible to other threads!)

The synchronization barrier was added to the memory model of Java 5 to ensure that the common pattern of immutable objects is thread-safe. Without this barrier another thread might see the default value of a field instead of its final value. For example, it is well-known that `String` is immutable in Java, and its implementation uses three final fields: `char[]` `value`, and two `int` fields named

offset and count. The following code `"AB".substring(1)` will return a new string "B" that shares the same value array as "AB", but with offset and count equal to 1. Without the barrier, another thread might see the default values for these three fields, i.e., null for value and 0 for offset and count. For instance, if one removes the final keyword from all three fields in String, then the following code might print B (the expected answer), or it might print A or an empty string, or might even throw a NullPointerException:

```
final String name = "AB".substring(1);
new Thread() { public void run() {
    System.out.println(name); } }.start();
```

A similar bug might happen in Fig. 1 because this was leaked into INSTANCES before the barrier was executed. Consider another thread that iterates over INSTANCES and reads field a. It might read 0, because the assignment of 42 to a is guaranteed to be visible to other threads only after the barrier was reached.

Therefore, when creating an immutable class, Java's documentation recommends using final fields and avoid leaking this in the constructor. However, javac does not even give a warning if that recommendation is violated. X10 rules prevent any leakage of this, thus making it safe and easy to create immutable classes.

To summarize, final fields in Java enable thread-safe immutable objects, but the user must be careful to avoid the pitfall of leaking this.

Moreover, there are two other features in Java that are incompatible with final fields: *custom serialization* and *clone*. (These two features are conceptually connected, because a clone can be made by serializing and then de-serializing.) For example, below we will explain why adding custom serialization to String would have forced us to remove final from all its fields, thus making it thread-unsafe! Similarly, these two features prevent us from adding final to the header field in LinkedList (even though this field is never re-assigned).

1.2.1 Custom serialization and immutability

Default serialization in Java of an object *o* will serialize the entire object graph reachable from *o*. Default serialization is not always efficient, e.g., for a LinkedList, we only need to serialize the elements in the list, without serializing the nodes with their next and prev pointers. (It is possible to mark a field with transient to exclude it from serialization. However, marking next and prev as transient would simply create nodes that are disconnected upon deserialization).

Custom serialization is done by defining a pair of methods called `writeObject` and `readObject` that handle serializing and de-serializing, respectively. For example, `readObject` in LinkedList de-serializes the list's elements and rebuilds a new list; in the process, it assigns to field `header`. This field could have been final because it points to the same dummy header node during the entire lifetime of the list. However, it is re-assigned in two *methods*: `readObject` and `clone` (see Sec. 1.2.2), and final fields can only be assigned in *constructors*. It is possible to use reflection in Java to set a final field, and the new memory model (Java's spec, Section 17.5.3) even considers this:

"In some cases, such as *deserialization*, the system will need to change the final fields of an object after construction."

"Freezes of a final field occur both at the end of the constructor in which the final field is set, and immediately after each modification of a final field via reflection or other special mechanism."

(The "other special mechanism" is default serialization that has the privilege of assigning to final fields.)

As another example, consider serializing the empty string `aVeryLongString.substring(0,0)`. The default serialization in Java will serialize the very long `char[]` with a zero offset and count. If one would have wanted to write a custom serializer for String, then she would have to remove the final keyword (making it thread-

unsafe!), or use reflection to set final fields (making it inefficient). To summarize, custom serialization in Java is incompatible with final fields.

On the other hand, X10 de-serializes an object by calling a *constructor* with a `SerialData` argument (as opposed to `readObject` in Java which is a *method*). Therefore, de-serialization in X10 can assign to final fields, without using reflection and without special cases in the memory model (i.e., a freeze only happens at the end of a constructor).

Currently, the CustomSerialization interfaces only specify the serializer method:

```
def serialize():SerialData; // for serialization
```

There is an RFC (for a future version of X10) for adding static method and constructor signatures to interfaces; with that feature, the CustomSerialization interface would not be (partly) magical, because it will also contain the de-serializer signature:

```
def this(data:SerialData); // for de-serialization
```

The X10 compiler currently auto-generates these two entities (method and constructor) for every class (all classes are serializable by default in X10), unless the user implemented CustomSerialization and wrote these two methods herself.

1.2.2 Cloning and immutability

Cloning in Java has the same incompatibility with final fields as serialization: `clone` is a method and therefore it cannot assign to final fields. However, *immutable* objects (such as strings) have no use for cloning, because you only need to clone an object if you plan to *mutate* the object or the clone. Therefore, cloning is less problematic than serialization with respect to immutability.

Unlike Java, X10 has no magic clone method. Instead, the user can (deeply) clone an object using the serialization mechanism, which is invoked when a final variable is copied to another place (Sec. 1.3 talks about *at* and *places* in X10). So, currently clone can be defined as:

```
def clone[T](o:T) { return at (here) o; }
```

Using serialization is less efficient than directly cloning an object, and future work is planned to add cloning support to X10 that would be compatible with final fields (in a way similar to serialization) by defining an interface `Cloneable` with:

```
def this(cloneFrom:CloneSource);
```

where `CloneSource` is a struct that references the target object we wish to clone.

1.3 Parallelism and Initialization in X10

X10 supports parallelism in the form of both concurrent and distributed code. Next we describe parallelism in X10 and its interaction with object initialization.

Concurrent code uses asynchronous un-named activities that are created with the `async` construct, and it is possible to wait for activities to complete with the `finish` construct. Informally, statement `async S` executes statement *S* asynchronously; we say that the newly created activity *locally terminated* when it finished executing *S*, and that it *globally terminated* when it locally terminated and any activity spawned by *S* also globally terminated. Statement `finish S` blocks until all the activities created by *S* globally terminated.

Distributed code is run over multiple *places* that do not share memory, therefore objects are (deeply) copied from one place to another. The expression `at(p) E` evaluates *p* to a place, then copies all captured references in *E* to place *p*, then evaluates *E* in place *p*, and finally copies the result back to the original place. Note that `at` is a synchronous construct, meaning that the current activity is blocked until the `at` finishes. This construct can also be used as a statement, in which case there is no copy back (but there is still a notification that is sent back when the `at` finishes, in order to release the blocked activity in the original place).


```

class Fib {
  val fib2: Int, fib1: Int, fib: Int;
  def this(n: Int) {
    finish {
      async {
        val p = here.next();
        fib2 = at(p) n <= 1? 0 : new Fib(n-2).fib;
      }
      fib1 = n <= 0? 0 : n <= 1? 1 : new Fib(n-1).fib;
    }
    at(p) this.fib2 = ...;
    fib = fib2 + fib1;
  }
}

```

Figure 2. Concurrent and distributed Fibonacci example. Concurrent code is expressed using `async` and `finish`: `async` starts an asynchronous activity, and `finish` waits for all spawned activities to finish. Distributed code uses `at` to shift between *places*; `here` denotes the current place. `at(p) E` evaluates expression `E` in place `p`, and finally copies the result back; any final variables captured in `E` from the outer environment (e.g., `n`) are first copied to place `p`. Possible initialization pitfalls: (i) forget to use `finish`, and read from `fib2` before its write finished, (ii) write to field `fib2` in another place, i.e., `at(p) this.fib2 = ...`, which causes `this` to be copied to `p` so one writes to a copy of `this`.

Fig. 2 shows how to calculate the Fibonacci number `fib(n)` in X10 using concurrent and distributed code. The keywords `val` and `var` are modifiers that correspond to final and non-final variables, respectively. Note how `fib(n-2)` is calculated asynchronously at the next place (`next()` returns the next place in a cyclic ordering of all places), while simultaneously recursively calculating `fib(n-1)` in the current place (that will recursively spawn a new activity, and so on). Therefore, the computation will recursively continue to spawn activities at the next place until `n` is 1. When both calculations globally terminate, the `finish` unblocks, and we sum their result into the final field `fib`.

We note that using *final local variables* for `fib2` and `fib1` instead of fields would have made this example more elegant, however we chose the later because this paper focuses on *object* initialization. X10 has similar initialization rules for final locals and final fields, but it is outside the scope of this paper to present all forms of initialization in X10 (including local variables and static fields). Details of those can be found in X10’s language specification at x10-lang.org.

There are two possible pitfalls in this example. The first is a concurrency pitfall, where we forget to use `finish`, and therefore we might read from a field before its assignment was definitely executed. Java has definite-assignment rules (using an intra-procedural data-flow analysis) to ensure that a read can only happen after a write; The hardhat design in X10 adopted those rules and extended them in the face of concurrency to support the pattern of *asynchronous initialization* where an `async` must have an enclosing `finish` (using an intra-class inter-procedural analysis, see Sec. 2.11).

The second is a distributed pitfall, where one assigns to a field of a copy of `this` in another place (instead of assigning in the original place). Leaking `this` to another place before it is fully initialized might also cause bugs in custom serialization code (see Sec. 2.10).

The rest of this paper is organized as follows. Sec. 2 presents the hardhat initialization rules of X10 version 2.1 using examples, by slowly adding language features and describing their interaction with object initialization. Sec. 3 describes alternative designs for object initialization (one was implemented in X10 version 2.0 and another was under consideration for 2.1), weighing the pros and cons of each. Sec. 4 presents Featherweight X10 (FX10), which is a formalization of core X10 that includes `finish`, `async`, and flow-

```

class A {
  val a: Int;
  def this() {
    LeakIt.foo(this); //err
    this.a = 1;
    val me = this; //err
    LeakIt.foo(me);
    this.m2(); // so m2 is implicitly non-escaping
  }
  // permitted to escape
  final def m1() {
    LeakIt.foo(this);
  }
  // implicitly non-escaping because of this.m2()
  final def m2() {
    LeakIt.foo(this); //err
  }
  // explicitly non-escaping
  @NonEscaping final def m3() {
    LeakIt.foo(this); //err
  }
}

class B extends A {
  val b: Int;
  def this() {
    super(); this.b = 2; super.m3();
  }
}

```

Figure 3. Escaping `this` example. **Definition of *raw*:** `this` and `super` are *raw* in non-escaping methods and in field initializers. **Definition of *non-escaping*: A method is *non-escaping* if it is a constructor, or annotated with `@NonEscaping` or `@NoThisAccess`, or a method that is called on a raw `this` receiver. **Rule 1:** A raw `this` or `super` cannot escape or be aliased. **Rule 2:** A call on a raw `super` is allowed only for a `@NonEscaping` method. (**final** and `@NoThisAccess` are related to dynamic dispatch as shown in Fig. 4.)**

sensitive type-checking rules. Sec. 5 summarizes previous work in the field of object initialization. Finally, Sec. 6 concludes.

2. X10 Initialization Rules

X10 is an advanced object-oriented language with a complex type-system and concurrency constructs. This section describes how object initialization interacts with X10 features. We begin with object-oriented features found in mainstream languages, such as constructors, inheritance, dynamic dispatch, exceptions, and inner classes. We then proceed to X10’s type-system features, such as constraints, properties, class invariants, closures, (non-erased) generics, and structs, followed by the parallel features of X10 for writing concurrent code (`finish` and `async`), and distributed code (`at`). Next we describe the inter-procedural data-flow analysis that ensures that a field is read only after it has been assigned. Finally, we summarize the virtues and attributes of initialization in X10.

2.1 Constructors and inheritance

Inheritance is the first feature that interacts with initialization: when class `B` inherits from `A` then every instance of `B` has a sub-object that is like an instance of `A`. When we initialize an instance of `B`, we must first initialize its `A` sub-object. We do this in X10 by forcing the constructors of `B` to make a `super` call, i.e., call a constructor of `A` (either explicitly or implicitly).

Fig. 3 shows X10 code that demonstrates the interaction between inheritance and initialization, and explains by example why leaking `this` during construction can cause bugs. In all the examples, all errors issued by the X10 compiler are marked with `//err` (and if there is no such mark then the code is correct).

We say that an object is *raw* (also called partially initialized) before its constructor ends, and afterward it is *cooked* (also called

```

abstract class A {
  val a1:Int, a2:Int;
  def this() {
    this.a1 = m1(); //err1
    this.a2 = m2();
  }
  abstract def m1():Int;
  @NoThisAccess abstract def m2():Int;
}
class B extends A {
  var b:Int = 3; // non-final field
  def m1() {
    val x = super.a1;
    val y = this.b;
    return 1;
  }
  @NoThisAccess def m2() {
    val x = super.a1; //err2
    val y = this.b; //err3
    return 2;
  }
}

```

Figure 4. Dynamic dispatch example. **Rule 3:** A non-escaping method must be private or final, unless it has `@NoThisAccess`. **Rule 4:** A method with `@NoThisAccess` cannot access `this` or `super` (neither read nor write its fields).

fully initialized). Note that when an object is cooked, all its sub-objects must be cooked as well. X10 prohibits any aliasing or leaking of `this` during construction, therefore only `this` or `super` can be raw (any other variable is definitely cooked).

Object initialization begins by invoking a constructor, denoted by the method definition `def this()`. The first leak would cause a problem because field `a` was not assigned yet. However, even after all the fields of `A` have been assigned, leaking is still a problem because fields in a subclass (field `b`) have not yet been initialized. Note that leaking is not a problem if `this` is not raw, e.g., in `m1()`.

We begin with two definitions: (i) when an object is *raw*, and (ii) when a method is *non-escaping*. (i) Variables `this` and `super` are raw during the object’s construction, i.e., in field initializers and in non-escaping methods (methods that cannot escape or leak `this`). (ii) Obviously constructors are non-escaping, but you can also annotate methods *explicitly* as `@NonEscaping`, or they can be inferred to be *implicitly* non-escaping if they are called on a raw `this` receiver.

For example, `m2` is *implicitly* non-escaping (and therefore cannot leak `this`) because of the call to `m2` in the constructor. The user could also mark `m2` *explicitly* as non-escaping by using the annotation `@NonEscaping`. (Like in Java, `@` is used for annotations in X10.) We recommend explicitly marking public methods as `@NonEscaping` to show intent, as done on method `m3`. Without this annotation the call `super.m3()` in `B` would be illegal, due to rule 2. (We could infer that `m3` must be non-escaping, but that would cause a dependency from a subclass to a superclass, which is not natural for people used to separate compilation.) Finally, we note that all errors in this example are due to rule 1 that prevents leaking a raw `this` or `super`.

2.2 Dynamic dispatch

Dynamic dispatch interacts with initialization by transferring control to the subclass before the superclass completed its initialization. Fig. 4 demonstrates why dynamic dispatch is error-prone during construction: calling `m1` in `A` would dynamically dispatch to the implementation in `B` that would read the default value.

X10 prevents dynamic dispatch by requiring that non-escaping methods must be private or final (so overriding is impossible). For example, `err1` is caused by rule 3 because `m1` is neither private nor final nor `@NoThisAccess`.

```

class B extends A {
  def this() {
    try { super(); } catch(e:Throwable){} //err
  }
}

```

Figure 5. Exceptions example: if a constructor ends normally (without throwing an exception), then all preceding constructor calls ended normally as well. **Rule 5:** If a constructor does not call `super(...)` or `this(...)`, then an implicit `super()` is added at the beginning of the constructor; the first statement in a constructor is a constructor call (either `super(...)` or `this(...)`); a constructor call may only appear as the first statement in a constructor.

However, sometimes dynamic dispatch is required during construction. For example, if a subclass needs to refine initialization of the superclass’s fields. Such refinement cannot have any access to `this`, and therefore such methods must be marked with `@NoThisAccess`. For example, `err2` and `err3` are caused by rule 4 that prohibits access `this` or `super` when using `@NoThisAccess`. `@NoThisAccess` prohibits any access to `this`, however, one could still access the method parameters. (If the subclass needs to read a certain field of the superclass that was previously assigned, then that field can be passed as an argument.)

In C++, the call to `m1` is legal, but at runtime methods are statically bound, so you will get a crash trying to call a pure virtual function. In Java, the call to `m1` is also legal, but at runtime methods are dynamically bound, so the implementation of `m1` in `B` will read the default values of `a1` and `b`.

2.3 Exceptions

Constructing an object may not always end normally, e.g., building a date object from an illegal date string should throw an exception. Exceptions combined with inheritance interact with initialization in the following way: a cooked object must have cooked sub-objects, therefore if a constructor ends normally (thus returning a cooked object) then all preceding constructor calls (either `super(...)` or `this(...)`) must end normally as well. Phrased differently, in a constructor it should not be possible to recover from an exception thrown by a `this` or `super` constructor call. This is one of the reason why a constructor call must be the first statement in Java; failure to verify this led to a famous security attack [1].

Fig. 5 shows that it is an error to try to recover from an exception thrown by a constructor call; the reason for the error is rule 5 that requires the first statement to be `super()`.

2.4 Inner classes

Inner classes usually read the outer instance’s fields during construction, e.g., a list iterator would read the list’s header node. Therefore, X10 requires that the outer instance is cooked, and prohibits creating an inner instance when the receiver is a raw `this`.

Fig. 6 shows it is an error in X10 to create an inner instance if the outer is raw (from rule 6), but it is ok to create an instance of a static nested class, because it has no outer instance.

In fact, it is possible to view this rule as a special case to the rule that prohibits leaking a raw `this` (because when you create an inner instance on a raw `this` receiver, you created an alias, and now you have two raw objects: `Inner.this` and `Outer.this`). We wish to keep the invariant that only one `this` can be raw.

In our rules, we assume that there is a single `this` reference, because we can convert all inner, anonymous and local classes into static nested classes by passing the outer instance and all other captured variables explicitly as arguments to the constructor.

We now turn our attention to X10’s sophisticated type-system features not found in main-stream languages: constraints, properties, class invariants, closures, (non-erased) generics, and structs.

```

class Outer {
  val a: Int;
  def this() {
    // Outer.this is raw
    Outer.this.new Inner(); //err
    new Nested(); // ok
    a = 3;
  }
  class Inner {
    def this() {
      // Inner.this is raw, but
      // Outer.this is cooked
      val x = Outer.this.a;
    }
  }
  static class Nested {}
}

```

Figure 6. Inner class example: the outer instance is always cooked.
Rule 6: a raw `this` cannot be the receiver of `new`.

```

class A {
  val i0: Int; //err
  var i1: Int;
  var i2: Int{self!=0}; //err
  var i3: Int{self!=0} = 3;
  var i4: Int{self==42}; //err
  var s1: String;
  var s2: String{self!=null}; //err
  var b1: Boolean;
  var b2: Boolean{self==true}; //err
}

```

Figure 7. Default value example. **Definition of *has-zero*:** A type *has-zero* if it contains the zero value (which is either null, false, 0, or zero in all fields for user-defined structs) or if it is a type parameter guarded with *haszero* (see Sec. 2.8). **Rule 7:** A `var` field that lacks a field initializer and whose type *has-zero*, is implicitly given a zero initializer.

2.5 Constraints and default/zero values

X10 supports constrained types using the syntax $T\{c\}$, where c is a boolean expression that can use final variables in scope, literals, properties (described below), the special keyword `self` that denotes the type itself, field access, equality (`==`) and disequality (`!=`). There are plans to add arithmetic inequality (`<`, `<=`) to X10 in the future, and one can plug in any constraint solver into the X10 compiler.

As a consequence of constrained types, some types do not have a default value, e.g., `Int{self!=0}`. Therefore, in X10, the fields of an object cannot be zero-initialized as done in Java. Furthermore, in Java, a non-final field does not have to be assigned in a constructor because it is assumed to have an implicit zero initializer. X10 follows the same principle, and a non-final field is implicitly given a zero initializer *if its type has-zero*. Fig. 7 defines when a type *has-zero*, and gives examples of types without zero. Note that `i0` has to be assigned because it is a final field (`val`), as opposed to `i1` which is non-final (`var`).

2.6 Properties and the class invariant

Properties are final fields that can be used in constraints, e.g., `Array` has a `size` property, so an array of size 2 can be expressed as: `Array{self.size==2}`. The differences between a property and a final field are both syntactic and semantic, as seen in class `A` of Fig. 8. Syntactically, properties are defined after the class name, must have a type and cannot have an initializer, and must be initialized in a constructor using a property call statement written as `property(...)`. Semantically, properties are initialized before all other fields, and they can be used in constraints with the prefix `self`.

```

class A(a: Int) {
  def this(x: Int) {
    property(x);
  }
}
class B(b: Int) {b==a} extends A {
  val f1 = a+b, f2: Int, f3: A{this.a==self.a};
  def this(x: Int) {
    super(x);
    val i1 = super.a;
    val i2 = this.b; //err
    val i3 = this.f1; //err
    f2 = 2; //err
    property(x);
    f3 = new A(this.a);
  }
}

```

Figure 8. Properties and class invariant example: properties (`a` and `b`) are final fields that are initialized before all other fields using a property call (`property(...); statement`). If a class does not define any properties, then an implicit `property()` is added after the (implicit or explicit) `super(...)`. Field initializers are executed in their declaration order after the (implicit or explicit) property call. **Rule 8:** If a constructor does not call `this(...)`, then it must have exactly one property call, and it must be unconditionally executed (unless the constructor throws an exception). **Rule 9:** The class invariant must be satisfied after the property call. **Rule 10:** The super fields can only be accessed after `super(...)`, and the fields of `this` can only be accessed after `property(...)`.

```

class A {
  var a: Int = 3;
  def this() {
    val closure1 = ()=>this.a; //err
    at(here.next()) closure1();
    val local_a = this.a;
    val closure2 = ()=>local_a;
  }
}

```

Figure 9. Closures example. **Rule 11:** A closure cannot capture a raw `this`.

When using the prefix `this`, you can access both properties and other final fields. The difference between `this` and `self` is shown in field `f3` in Fig. 8: `this.a` refers to the property `a` stored in `this`, whereas `self.a` refers to a stored in the object to which `f3` refers. (In the constructor, we indeed see that we assign to `f3` a new instance of `A` whose `a` property is equal to `this.a`.)

Properties must be initialized before other fields because field initializers and field types can refer to properties (see initializer for `f1` and the type of `f3`). The superclass's fields can be accessed after the super call, and the other fields after the property call; field initializers are executed after the property call.

The *class invariant* (`{b==a}` in Fig. 8) may refer only to properties, and it must be satisfied after the property call (rule 9).

2.7 Closures

Closures are functions that can refer to final variables in the enclosing scope, e.g., they can refer to final method parameters, locals, and `this`. When a closure refers to a variable, we say that the variable is *captured* by the closure, and the variable is thus stored in the closure object. Closures interact with initialization when they capture `this` during construction.

Fig. 9 shows why it is prohibited to capture a raw `this` in a closure: that closure can later escape to another place which will serialize all captured variables (including the raw `this`, which

```

class B[T] {T haszero} {
  var f1:T;
  val f2 = Zero.get[T]();
}
struct WithZeroValue(x:Int,y:Int) {}
struct WithoutZeroValue(x:Int{self!=0}) {}
class Usage {
  var b1:B[Int];
  var b2:B[Int{self!=0}]; //err
  var b3:B[WithZeroValue];
  var b4:B[WithoutZeroValue]; //err
}

```

Figure 10. haszero type predicate example. **Rule 12:** A type must be consistent, i.e., it cannot contradict the environment; the environment includes final variables in scope, method guards, and class invariants..

should not be serialized, see Sec. 2.10). The work-around for using a field in a closure is to define a local that will refer only to the field (which is definitely cooked) and capture the local instead of the field as done in closure2.

2.8 Generics and Structs

Structs in X10 are header-less inlinable objects that cannot inherit code (i.e., they can *implement* interfaces, but cannot *extend* anything). Therefore an instance of a struct type has a known size and can be inlined in a containing object. Java’s primitive types (int, byte, etc) are represented as structs in X10. Structs, as opposed to classes, do not contain the value null.

Generics in X10 are reified, i.e., not erased as in Java. For example, instances of Box[Byte] and Box[Double] would have the same size in Java but different sizes in X10. Although generics are not a new concept, the combination of generics and the lack of default values leads to new pitfalls. For example, in Java and C#, it is possible to define an equivalent to

```
class A[T] { var a:T; }
```

However, this is illegal in X10 because we cannot be sure that T has-zero (see Fig. 7), e.g., if the user instantiates A[Int{self!=0}] then field a cannot be assigned a zero value without violating type-safety. Therefore X10 has a type predicate written x haszero that evaluates to true if type x has-zero. Using haszero in a constraint (e.g., in a class invariant or a method guard), makes it possible to guarantee that a type-parameter will be instantiated with a type that has-zero.

Fig. 10 shows an example of a generic class B[T] that constrains the type-parameter T to always have a zero value. According to rule 7, field f1 has an implicit zero field initializer. It is also possible to write the initializer explicitly (as done in field f2) by using the static method Zero.get[X]() (that is guarded by X haszero). Next we see two struct definitions: the first has two properties that has-zero, and the second has a property that does not have zero. According to the definition of has-zero in Fig. 7, a struct has-zero if all its fields has-zero, therefore WithZeroValue haszero is true, but WithoutZeroValue haszero is false. Finally, we see an example of usages of B[T], where two usages are legal and two are illegal (see rule 12).

We now turn our attention to the parallel features of X10 for concurrent programming (finish and async) and distributed programming (at). Sec. 1.3 already explained how parallel code is written in X10, and what are the common pitfalls of initialization in parallel code. Next we present the rules that prevent these pitfalls.

2.9 Concurrent programming and Initialization

Fig. 11 shows how to asynchronously assign to fields. Recall that we wish to guarantee that one can never read an uninitialized field, therefore rule 13 ensures that all fields are assigned at least once.

```

class A {
  var f1:Int; // note: var field
  val f2:Int; // note: val field
  val f3:Int;
  def this() { //err: f2 was not definitely assigned
    async f1 = 1; async f2 = 2;
    finish { async f3 = 3; }
  }
}

```

Figure 11. Concurrency in initialization example: asynchronously assign to a field. **Rule 13:** A constructor must finish assigning to all fields at least once. **Rule 14:** A final field can be assigned at most once.

```

class A {
  val f:Int;
  def this() { //err: f was not definitely assigned
    // Execute at another place
    at (here.next())
      this.f = 1; //err: this escaped
  }
}

```

Figure 12. Distributed initialization example. **Rule 15:** a raw this cannot be captured by an at.

All three fields in A are asynchronously assigned, however, only f2 is not definitely assigned at the end of the constructor. Assigning to f3 has an enclosing finish, so it is definitely assigned. Field f1 is also definitely assigned, because it is non-final so from rule 7 it has an implicit zero field initializer. However, field f2 is final so it does not have an implicit field initializer. Moreover, f2 is only asynchronously assigned, and the constructor does not have to wait for this assignment to finish, thus violating rule 13. (The exact data-flow analysis to enforce rule 13 is described in Sec. 2.11.) Rule 14 is the same as in Java: a final field is assigned *at most* once (and, combined with rule 13, we know it is assigned *exactly* once).

2.10 Distributed programming and Initialization

X10 programs can be executed on a distributed system with multiple places that have no shared memory. Objects are copied from one place to another when captured by an at. Copying is done by first serializing the object into a buffer, sending the buffer to the other place, and then de-serializing the buffer at the other place. As in Java, one can write custom serialization code in X10 by implementing the CustomSerialization interface, and defining the method serialize():SerialData and the constructor this(data:SerialData).

Fig. 12 shows a common pitfall where a raw this escapes to another place, and the field assignment would have been done on a copy of this. We wish to de-serialize only cooked objects, and therefore rule 15 prohibits this to be captured by an at. Consequently, we also report that field f was not definitely assigned.

2.11 Read and write of fields

We now present a data-flow analysis for guaranteeing that a field is read only after it was written, and that a final field is assigned exactly once. Java performs an *intra*-procedural data-flow analysis in *constructors* to calculate when a *final* field is definitely-assigned and definitely-unassigned. In contrast, X10 performs an *inter*-procedural (fixed-point) data-flow analysis in all *non-escaping methods* (and constructors) to calculate when a field (*both final and non-final*) is definitely-assigned, *definitely-asynchronously-assigned*, and definitely-unassigned. The details are explained using examples (Fig. 13) by comparison with Java; the full analysis is described in X10’s language specification.


```

class A {
  val a: Int;
  def this() {
    readA(); //err1
    finish {
      async {
        a = 1; // assigned={a}
        readA();
      } // asyncAssigned={a}
      readA(); //err2
    } // assigned={a}
    readA();
  }
  private def readA() { // reads={a}
    val x = a;
  }
}
class B {
  var i: Int {self != 0}, j: Int {self != 0};
  def this() {
    finish {
      asyncWriteI(); // asyncAssigned={i}
    } // assigned={i}
    writeJ(); // assigned={i, j}
    readIJ();
  }
  private def asyncWriteI() { // asyncAssigned={i}
    async i = 1;
  }
  private def writeJ() { // reads={i} assigned={j}
    if (i == 1) writeJ(); else this.j = 1;
  }
  private def readIJ() { // reads={i, j}
    val x = this.i + this.j;
  }
}

```

Figure 13. Read-Write order for fields. We infer for each method three sets: (i) fields it reads (i.e., these fields must be assigned before the method is called), (ii) fields it assigns, (iii) fields it assigns asynchronously. The data-flow maintains these three sets before and after each statement; *assigned* becomes *asyncAssigned* after an *async*, and *asyncAssigned* becomes *assigned* after a *finish*. In this example, we omitted empty sets. **Rule 16:** A field may be read only if it is definitely-assigned. **Rule 17:** A final field may be written only if it is definitely-unassigned.

X10, like Java, allows *writing* to a final field only when it is definitely-unassigned, and it allows *reading* from a final field only when it is definitely-assigned. X10 also has the same read restriction on non-final fields (recall that rule 7 adds a field initializer if the field's type has-zero).

Consider first only final fields. They are easier to type-check because they can only be assigned in constructors. X10 extends Java rules, by calculating for each non-escaping method *m* the set of final fields it reads, and calling *m* is legal only if these fields have been definitely assigned. For example, in class *A*, method *readA* reads field *a* and therefore cannot be called before *a* is assigned (e.g., *err1*). Note that Java does not perform this check, and it is legal to call *readA* which will return the zero value of *a*. X10 also adds the notion of *definitely-asynchronously-assigned* which means a field was definitely-assigned within an *async* (so it cannot be read, e.g., *err2*), but after an enclosing *finish* it will become definitely-assigned (so it can be read). The flow maintains three sets: *reads*, *assigned*, and *asyncAssigned*. If a method reads an uninitialized field, then we add it to its *reads* set; however, if a constructor reads an uninitialized field, then it is an error. Phrased differently, the *reads* set of a constructor must be empty.

Now consider non-final fields. They can be assigned and read in methods, thus requiring a fixed-point algorithm. For example, consider method *writeJ*. Initially, *reads* is empty, while *assigned* and *asyncAssigned* are the entire set of fields. In the first iteration, we add *i* to *reads*, and when we join the two branches of the *if*, *assigned* is decreased to only *j*. The fixed-point calculation, in every iteration, increases *reads* and decreases *assigned* and *asyncAssigned*, until a fixed-point is reached.

2.12 Static initialization

Unlike Java, X10 does not support dynamic class loading, and all static fields in X10 are final. Thus, initialization of static fields is a one-time phase that is done before the *main* method is executed. Reading a static field in this phase *waits* until the field is initialized, which may lead to dead-lock. However, in practice, deadlock is rare, and usually found quickly the first time a program is executed.

2.13 Virtues and attributes of initialization in X10

We assume there is a single *this* variable, because all nested classes can be converted to static, as described in Sec. 2.4. Therefore, initialization in X10 has the following attributes: (i) *this* (and its alias *super*) is the only accessible raw object in scope (rule 1), (ii) only cooked objects cross places (rule 15), (iii) only *@NoThisAccess* methods can be dynamically dispatched during construction (rule 3), (iv) all final field assignments finish by the time the constructor ends (rule 13), (v) it is not possible to read an uninitialized field (rule 16), and (vi) reading a final field always results in the same value (rule 17 combined with attribute (v)).

3. Alternative Initialization Designs

3.1 Default values design

Java first initializes fields with either 0, false, or null (depending on the field type) and then runs the constructor to initialize the fields according to the programmer's wishes. If every X10 type had a default value that was statically known, then Java's object initialization scheme could be used in X10. This would have the advantage of familiarity for Java programmers that are learning X10. The disadvantages are that that observing final fields changing value is nonintuitive, and that reading the field before initialization is prone to undetectable errors.

Unfortunately, it is hard to reconcile the notion of a default value with X10's type system, because a programmer can define a type which does not contain a default value. In the X10 type system, one can define a type with no values at all, by using a constraint that yields a contradiction.

This could be addressed by extending the X10 types to require that the programmer define a new constant value for any type that has been constrained enough that the original default value is no longer a member of the type. This means that every field can be initialized to the value defined in its type. The disadvantage of this approach is that the type system becomes more complex and more type annotations are required. We decided that this, in combination with the disadvantages given above, was too problematic to justify the advantages of Java-style object initialization.

For example, consider a field *birthday* that cannot be null, i.e., it does not have a default value:

```

class Person { val birthday: Date {self != null}; ... }

```

Then in this design the programmer would have to specify a default value for this field, e.g., *Date.MIN_DATE*. The field would be initialized with this default value, and its final value would be assigned only later. Specifying default values seems like a cumbersome design.


```

class C {
  val next : C {self!=null};
  var fld : C;
  def this(n : proto C{self!=null}) {
    //Console.OUT.println(n.next); //err1
    //n.fld(); //err2
    this.next = n;
  }
  def this() {
    //Console.OUT.println(this.next); //err3
    //this.fld(); //err4
    val c = new C(this);
    //Console.OUT.println(c.next.next); //err5
    this.next = c;
  }
  def f() {
    Console.OUT.println(this.next);
  }
  def this(c : C, Int) {
    //c.m(this); //err6
    Console.OUT.println(c.fld.next);
    this.next = c;
  }
  void m (n : proto C) proto {
    this.fld = n;
  }
  static def test() {
    val c:C{self!=null} = new C();
    assert c.next.next==c;
  }
}

```

Figure 14. An immutable cycle of heap references, using proto.

3.2 Proto Design

If we want to allow some of the programs that the Hardhat design rejects, such as immutable cycles in the object graph, but we do not want to burden the type system with default value annotations, then one solution is to allow `this` to escape in certain cases while still preventing reads from uninitialized fields. This can be achieved by annotating reference types with a keyword `proto` to indicate that the referenced object is partially constructed. Reads of fields where the target object is `proto` are not allowed because a partially constructed object may not have initialized its fields yet. The advantage of this approach is that it allows a set of partially constructed objects to establish themselves as a mutually referential cycle of objects in the heap, which would not otherwise be possible. The disadvantage is that it requires an additional type annotation, although this annotation is only required in code that creates immutable cyclic heap structures. Also note that there are no additional space or runtime overheads since these extra type system mechanisms are for static checking only.

An example of an immutable cycle of two nodes is given in Fig. 14. A more practical but less concise example would be an immutable doubly-linked list. Let us assume that we would like to optimize away any null reference checks, so we constrain all references to exclude the null value. The commented out lines indicate code that would be rejected by the type system.

In all constructors, `this` is a reference to a partially constructed object. If the type of `this` were to be explicit, it would be `proto C{self!=null}`. The `proto` element of the type forbids any field reads. It also prevents the reference being leaked (e.g. into `f()`), except into variables of `proto` type where it follows that there is protection from uninitialized field reads.

The first constructor's `n` parameter takes a `proto` reference to the original `C` instance. It is limited in what it can do with `n`, e.g. it cannot read `n.next`, but it can initialize its own `next` field with the passed-in value. When the second constructor returns, both objects

are fully constructed with all fields initialized. Thus, the type of the variable `c` does not have a `proto` annotation and the field read `c.next` is allowed.

If a type has the `proto` keyword, then its fields (both `var` and `val`) may have partially constructed objects assigned to them, but fields may not be read. Conversely, the absence of `proto` means that the fields may be read but `var` fields may not have partially constructed objects assigned to them. This means that `proto C` and `C` are not related by sub-typing. In other words, `proto C` means definitely partially constructed and `C` means definitely fully constructed. Consequently it makes no sense to allow casting between the two types, and one may not extend or implement a `proto` type. The only sources of `proto` typed objects are via the `this` keyword in a constructor and via method parameters of `proto` type. The only way a type can lose its `proto` is by becoming fully constructed.

Consider `err5` in Fig. 14. If we had inferred the type of `c` to be non-`proto`, then we could have read the uninitialized field `this.next`. To solve this problem, we must ensure that the whole cycle becomes fully constructed together. This can be arranged by changing the type of `new C(...)` to be `proto C` if one of its arguments is of `proto` type. This does not affect the assignment `this.next = c` because this is `proto`.

We do not allow fields to have `proto` type. This is because the referenced object will eventually be fully constructed and then there would be a variable of `proto` type pointing to a fully constructed instance. This admits the possibility of someone assigning a partially constructed object to a field of the fully constructed object, just as was done in the first constructor in Fig. 14. Then, one could accidentally read an uninitialized field from the partially constructed object by going through the fully constructed object. Disallowing `proto` in fields avoids this problem. However local variables are safe because of lexical scoping, since they will go out of scope before the constructor returns and the object becomes fully constructed.

There would be an issue calling other instance methods on `this` from a constructor, because the type of `this` in those methods would need to be `proto` since the target is still partially constructed. We support this by allowing the `proto` keyword to also be used on a method as an effect annotation, i.e. it must be preserved by inheritance. Such methods are called `proto` methods and can be called on partially constructed targets. The type of `this` then subjects the body of the method to the same restrictions as we have already seen in constructor bodies.

However in some cases we would like to avoid code duplication by allowing some methods to be callable on both `proto` and non-`proto` targets. This violates our principle that the two kinds of objects enjoy different privileges and are completely distinct. The error `err6` in Fig. 14 shows how we could potentially read an uninitialized field if we allowed this relaxation.

To address this, we only allow the method to be called on non-`proto` targets if there are no `proto` parameters to the method. No such parameters means the only partially constructed object in scope is `this`. In the case where the method is called on a non-`proto` target there is therefore no partially constructed object in scope, and no harm can be done.

While we believe this type system is correct and usable for writing real programs in the X10 language, we had to decide whether the additional type system complexity and annotations were a reasonable price to pay for the additional expressiveness (i.e. the ability to construct immutable heap cycles). We ultimately decided that immutable heap cycles are too rare in practice to justify including these extra mechanisms in the language.

4. Formalism: FX10

Featherweight X10 (FX10) is a formal calculus for X10 intended to complement Featherweight Java (FJ). It models imperative aspects

of X10 including the concurrency constructs `finish` and `async`. FX10 models the heart of the field initialization problem: a field can be read only after it is definitely assigned.

The basic idea behind the formalization is very straightforward. We break up the formalization into two distinct but interacting subsystems, a *type system* (Sec. 4.2) and an *effect system* (Sec. 4.3). The type system is completely standard – think the system of FJ, adapted to the richer constructs of FX10.

The effect system is built on a very simple *logic of initialization assertions*. The primitive formula $+x$ ($+p.f$) asserts that the variable x (the field f of p) is definitely initialized with a cooked object, and the formula $-x$ ($-p.f$) asserts that it is being initialized by a concurrent activity (and hence it will be definitely initialized once an enclosing `finish` is crossed). An *initialization formula* ϕ or ψ is simply a conjunction of such formulas $\phi \wedge \psi$. An *effects assertion* $\phi \vdash \psi$ (for a statement S) is read as a partial correctness assertion: when executed in a heap H that satisfies the constraint ϕ , S will on termination result in a heap H' that satisfies ψ . Since we do not model `null`, our formalization can be particularly simple: variables, once initialized, stay initialized, hence H' will also satisfy ϕ (see Sec. 4.4 for a definition of heaps and when a heap satisfy ϕ).

Another feature of our approach is that, unlike Masked Types [9], the source program syntax does not permit the specification of initialization assertions. Instead we use a standard least fixed point computation to automatically decorate each method $\text{def } m(\bar{x}:\bar{C})\{S\}$ with pairs (ϕ, ψ) (in the free variables `this`, \bar{x}) such that under the assumption that all methods satisfy their corresponding assertion we can show that $\phi \vdash \psi$.¹ This computation must be sensitive to the semantics of method overriding, that is a method with decoration (ϕ, ψ) can only be overridden by a method with decoration (ϕ', ψ') that is “at least as strong as” (ϕ, ψ) (viz, it must be the case that $(\phi \vdash \phi'$ and $\psi' \vdash \psi)$). Further, if the method is not marked `@NonEscaping`, then ϕ is required to entail $+this$ (that is, `this` is cooked), and if it marked `@NoThisAccess` then ϕ, ψ cannot have `this` free.

By not permitting the user to specify initialization assertions we make the source language much simpler than [9] and usable by most programmers. The down side is that some initialization idioms, such as cyclic initialization, are not expressible.

For reasons of space we do not include the (standard) details behind the decoration of methods with initialization assertions. We also omit many extensions (such as generics, interfaces, constraints, casting, inner classes, overloading, co-variant return types, private/final locals, field initializers etc.) necessary to establish the soundness of initialization for the full language discussed in the first half of the paper. FX10 also does not model places because the language design decision to only permit cooked objects to cross places means that the rules for `at` are routine.

We use the usual notation of \bar{x} to represent a vector or set of x_1, \dots, x_n . A program P is a pair of class declarations \bar{L} (that is assumed to be global information) and a statement S .

Overview of formalism Sec. 4.1 presents the syntax of FX10. Sec. 4.2 briefly describes the type system. Sec. 4.3 defines the flow-sensitive rules for $(\phi \vdash \psi)$, while Sec. 4.4 gives the reduction rules for statements and expressions $(S, H \rightsquigarrow S', H' \mid H'$ and $e, H \rightsquigarrow v, H')$. Finally Sec. 4.5 presents the main formal result (soundness theorem).

¹ Note that this approach permits a formal x to a method to be completely raw (ϕ does not entail $+x$ or $+x.f$ for any field f) or partially raw (ϕ does not entail $+x$ but may entail $+x.f$ for some fields f). As a result of the method invocation the formal may become more cooked. In X10, in order for the inference to be intra-class, we require that all method parameters \bar{x} (except `this`) are cooked, i.e., $+x_i$. In FX10 we are more relaxed and allow methods to receive and initialize raw parameters.

4.1 Syntax

$P ::= \bar{L}, S$	Program.
$L ::= \text{class } C \text{ extends } D \{ \bar{F}; \bar{M} \}$	cClass declaration.
$F ::= \text{var } f : C$	Field declaration.
$M ::= G \text{ def } m(\bar{x}:\bar{C}) : C\{S\}$	Method declaration.
$G ::= @\text{NonEscaping} \mid @\text{NoThisAccess}$	Method modifier.
$p ::= l \mid x$	Path.
$e ::= p.f \mid \text{new } C$	Expressions.
$S ::= p.f = p; \mid p.m(\bar{p}); \mid \text{val } x = e; S$ $\mid \text{finish } \{S\} \mid \text{async } \{S\} \mid S S$	Statements.

Figure 15. FX10 Syntax. The terminals are locations (l), parameters and `this` (x), field name (f), method name (m), class name (B, C, D, Object), and keywords (`new`, `finish`, `async`, `val`). The program source code cannot contain locations (l), because locations are only created during execution/reduction in R-NEW of Fig. 17.

Fig. 15 shows the syntax of FX10. Expression `val x = e; S` evaluates e , assigns it to a new variable x , and then evaluates S . The scope of x is S .

The syntax is similar to the real X10 syntax with the following difference: FX10 does not have constructors; instead, an object is initialized by assigning to its fields or by calling non-escaping methods.

4.2 Type system

The type system for FX10 checks that every parameter and variable has a type (a type is the name of a class), and that a variable of type C can be assigned only expressions whose type is a subclass of C , and can only be the receiver of invocations of methods defined in C . The type system is formalized along the lines of FJ. No complications are introduced by the extra features of FX10 – assignable fields, local variable declarations, `finish` and `async`. We omit details for lack of space and because they are completely routine.

In the rest of this section we shall assume that the program being considered \bar{L}, S is well-typed.

4.3 Effect system

We use a simple logic of initialization for our basic assertions. This is an intuitionistic logic over the primitive formulas $+p$ (the variable or parameter p is initialized), $+p.f$ (the field $p.f$ is initialized), and $-p$, $-p.f$ (it is being *concurrently* initialized). We are only concerned with conjunctions and existential quantifications over these formulas: $\phi, \psi ::= \text{true} \mid +x \mid +p.f \mid -p.f \mid \phi \wedge \psi$

The notion of substitution on formulas $\phi[\bar{x}/\bar{z}]$ is specified in a standard fashion.

The inference relation is the usual intuitionistic implication over these formulas, and the following additional proof rules: (1) if $\phi \vdash +p$ then $\phi \vdash -p$; (2) if $\phi \vdash +p.f$ then $\phi \vdash -p.f$; (3) if $\phi \vdash +p$ ($\phi \vdash -p$) then $\phi \vdash +p.f$ ($\phi \vdash -p.f$); and (4) if the *exact* class of x is C , and C has the fields \bar{f} , then $\phi \vdash +p$ ($\phi \vdash -p$) if $\phi \vdash +p.f_i$ ($\phi \vdash -p.f_i$), for each i . (We only know the *exact* class for a local x when `val x = new C; S`.)

The proof rules for the judgement $\phi \vdash \psi$ are given in Figure 16. They use two syntactic operations on initialization formulas defined as follows. $+ \psi$ is defined inductively as follows: $+ \text{true} = \text{true}$, $+ \pm x = \pm x$, $+ \pm p.f = \pm p.f$, $+ (\phi \wedge \psi) = (+\phi) \wedge (+\psi)$. $- \psi$ is defined similarly: $- \text{true} = \text{true}$, $- \pm x = -x$, $- \pm p.f = -p.f$, $- (\phi \wedge \psi) = (-\phi) \wedge (-\psi)$.

The rule (T-ACCESS) can be read as asserting: if ϕ entails the field $p.f$ is initialized (together with $+x$ which states that x is initialized to a cooked object), we can establish that execution of S satisfies the assertion ψ then we can establish that execution

$\frac{\phi \vdash +p.f \quad \phi, +x.S \Psi}{\phi \text{ val } x = p.f; S \Psi} \text{ (T-ACCESS)}$	$\frac{\phi.S \Psi}{\phi \text{ val } x = \text{new } C; S \Psi} \text{ (T-NEW)}$	$\frac{\phi \vdash +q}{\phi.p.f = q + p.f} \text{ (T-ASSIGN)}$
$\frac{\phi.S \Psi}{\phi \text{ finish } \{S\} + \Psi} \text{ (T-FINISH, ASYNC)}$	$\frac{\phi.S_1 \Psi_1 \quad \phi, \Psi_1.S_2 \Psi_2}{\phi.S_1.S_2 \Psi_1, \Psi_2} \text{ (T-SEQ)}$	$\frac{m(\bar{x}) :: \phi' \Rightarrow \Psi' \quad \phi \vdash \phi' [p/\text{this}, \bar{p}/\bar{x}]}{\phi.p.m(\bar{p}) \Psi' [p/\text{this}, \bar{p}/\bar{x}]} \text{ (T-INVOKE)}$
$\phi \text{ async } \{S\} - \Psi$		

Figure 16. FX10 Effect System ($\phi \vdash S \Psi$)

of $\text{val } x = p.f; S$ in (a heap satisfying) ϕ establishes Ψ . Here we must take care to project x out of Ψ since x is not accessible outside its scope S ; similarly we must take care to project x out of ϕ when checking S . The rule (T-NEW) can be read in a similar way except that when executing S we can make no assumption that x is initialized, since it has been initialized with a raw object (none of its fields are initialized). Subsequent assignments to the fields of x will introduce effects recording that those fields have been initialized. The rule (T-ASSIGN) checks that q is initialized to a cooked object and then asserts that $p.f$ is initialized to a cooked object. The rule (T-FINISH) can be understood as recording that after a `finish` has been “crossed” all asynchronous initializations Ψ can be considered to have been performed ϕ . Conversely, the rule (T-ASYNC) states that any initializations must be considered asynchronous to the surrounding context. The rule (T-SEQ) is a slight variation of the standard rule for sequential composition that permits ϕ to be used in the antecedent of S_2 , exploiting monotonicity of effects. Note the effects recorded for $S_1.S_2$ are a conjunction of the effects recorded for S_1 and S_2 . The rule (T-INVOKE) is routine.

As an example, consider the following classes. Assertions are provided in-line.

```

class A extends Object {
  var f:Object; var g:Object; var h:Object;
  @NonEscaping def build(a:Object) {
    // inferred decoration: phi => psi
    // phi= +this.g, +a
    // psi= -this.h, +this.f
    // checks phi implies +this.g
    val x = this.g;
    async { this.h = x; } // psi= -this.h
    finish {
      // checks phi implies +a
      async { this.f = a; } // psi= -this.h, -this.f
    } // psi= -this.h, +this.f
  }
}
class B extends A { e:Object; }
Method build synchronously (asynchronously) initializes fields
this.f (this.h), and it assumes that this.g and a are cooked. The
following statement completely initializes b:
val b = new B();
val a = new Object(); // psi= +a
b.g = a; // psi= +a, +b.g
finish {
  b.build(a); // psi= +a, +b.g, +b.f, -b.h
  async { b.e = a; } // psi= +a, +b.g, +b.f, -b.h, -b.e, -b
} // psi= +a, +b

```

4.4 Reduction

A heap H is a mapping from a given set of locations to *objects*. An object is a pair $C(F)$ where C is a class (the exact class of the object), and F is a partial map from the fields of C to locations. We say the object l is *total/cooked* (written $\text{cooked}_H(l)$) if its map is total, i.e., $H(l) = C(F)$ $\text{dom}(F) = \text{fields}(C)$.

We say that a heap H *satisfies* ϕ (written $H \vdash \phi$) if the plus assertions in ϕ (ignoring the minus assertions) are true in H , i.e., if $\phi \vdash +l$ then l is cooked in H and if $\phi \vdash +l.f$ then $H(l) = C(F)$ and $F(f)$ is cooked in H .

The reduction relation is described in Figure 17. An S-configuration is of the form s, H where s is a statement and H is a heap (representing a computation which is to execute s in the heap H), or H (representing terminated computation). An E-configuration is of the form e, H and represents the computation which is to evaluate e in the configuration H . The set of *values* is the set of locations; hence E-configurations of the form l, H are terminal.

Two transition relations \rightsquigarrow are defined, one over S-configurations and the other over E-configurations. For X a partial function, we use the notation $X[v \mapsto e]$ to represent the partial function which is the same as X except that it maps v to e . The rules defining these relations are standard. The only minor novelty is in how `async` is defined. The critical rule is the last rule in (R-STEP) – it specifies the “asynchronous” nature of `async` by permitting S to make a step even if it is preceded by `async` $\{S_1\}$. The rule (R-NEW) returns a new location that is bound to a new object that is an instance of C with none of its fields initialized. The rule (R-ACCESS) ensures that the field is initialized before it is read (f_i is contained in \bar{f}).

4.5 Results

We say a heap H is *correctly cooked* (written $\vdash H$) if a field can point only to cooked objects, i.e., for every object $o = C(F)$ in the range of H and every field $f \in \text{dom}(F)$ it is the case that every object $l = H(F(f))$ is cooked ($\text{cooked}_H(l)$). We shall only consider correctly cooked heaps (valid programs will only produce correctly cooked heaps). As the program is executed, the heap monotonically becomes more and more cooked. Formally, H' is *more cooked* than H (written $H' \vdash H$) if for every $l \in \text{dom}(H)$, we have $H(l) = C(F)$, $H'(l) = C(F')$, and $\text{dom}(F) \subseteq \text{dom}(F')$.

A heap typing Γ is a mapping from locations to classes. H is said to be typed by Γ if for each $l \in \text{dom}(H)$, the class of $H(l)$ is a subclass of $\Gamma(l)$. Since our treatment separates out effects from types, and the treatment of types is standard, we shall assume that all programs and heaps are typed.

A statement s is *closed* (written $\vdash s$) if it does not contain any free variables. We say that s is *annotable* if there exists ϕ, Ψ such that $\phi \vdash s \Psi$ can be established.²

We say that a program $P = \bar{L}S$ is *proper* if it is well-typed and each method in L can be decorated with pre-post assertions (ϕ, Ψ) , and s is annotable. The decorations must satisfy the property that under the assumption that every method satisfies its assertion (this is for use in recursive calls) we can establish for every method $\text{def } m(\bar{x} : \bar{C}) \{S\}$ with assertion (ϕ, Ψ) that it is the case that the free variables of ϕ, Ψ are contained in this, \bar{x} , and that $\phi \vdash s \Psi$.

We prove the following theorems. In all these theorems the background program P is assumed to be proper. The first theorem is analogous to subject-reduction for typing systems.

Theorem 4.1. Preservation *Let $\phi \vdash s \Psi, \vdash s, \vdash H, H \vdash \phi$. (a) If $s, H \rightsquigarrow H', H' \vdash H, H' \vdash +\Psi$. (b) If $s, H \rightsquigarrow s', H'$ then*

²An example of a statement that is *not* annotable is $\text{val } x = \text{new } C; \text{val } y = x.f; z.g = y$ where C has a field f . This attempts to read a field of a variable initialized with a brand-new object.

$\frac{s, H \rightsquigarrow H'}{\text{finish } \{s\}, H \rightsquigarrow H'} \quad \text{(R-TERM)}$		$\frac{s, H \rightsquigarrow s', H'}{\text{finish } \{s\}, H \rightsquigarrow \text{finish } \{s'\}, H'} \quad \text{(R-STEP)}$		$\frac{e, H \rightsquigarrow 1, H'}{\text{val } x = e; s, H \rightsquigarrow s[1/x], H'} \quad \text{(R-VAL)}$	
$\frac{s, H \rightsquigarrow s', H'}{\text{async } \{s\}, H \rightsquigarrow H'} \quad \text{(R-TERM)}$		$\frac{s, H \rightsquigarrow s', H'}{\text{async } \{s\}, H \rightsquigarrow \text{async } \{s'\}, H'} \quad \text{(R-STEP)}$		$\frac{s, H \rightsquigarrow s', H'}{s s_1, H \rightsquigarrow s' s_1, H'} \quad \text{(R-VAL)}$	
$\frac{1' \notin \text{dom}(H)}{\text{new } C, H \rightsquigarrow 1', H[1' \mapsto C()]} \quad \text{(R-NEW)}$		$\frac{H(1') = C(\dots) \quad \text{mbody}(m, C) = \bar{x}.S}{1', m(\bar{1}), H \rightsquigarrow s[1/\bar{x}, 1'/\text{this}], H} \quad \text{(R-INVOKE)}$		$\frac{H(1) = C(\bar{f} \mapsto \bar{1})}{1.f_i, H \rightsquigarrow 1'_i, H} \quad \text{(R-ACCESS)}$	
$\frac{H(1) = C(F) \quad \text{cooked}_H(1')}{1.f = 1', H \rightsquigarrow H[1 \mapsto C(F[\bar{f} \mapsto 1'])]} \quad \text{(R-ASSIGN)}$					

Figure 17. FX10 Reduction Rules ($s, H \rightsquigarrow s', H' \mid H'$ and $e, H \rightsquigarrow 1, H'$).

$\vdash s', \vdash H', H' \vdash H$, there exists ϕ', ψ' such that $H' \vdash \phi', \phi' s' \psi', \phi' \vdash \phi, \psi' \vdash \psi$.

Theorem 4.2. Progress Let $\phi s \psi, \vdash s, \vdash H, H \vdash \phi$. The configuration s, H is not stuck.

For proofs, please see associated technical report.

Because our reduction rules only allow reads from initialized fields, a corollary is that a field can only be read after it was assigned, and an attempt to read a field will always succeed.

5. Related Work

A static analysis [10], has been used to find some default value reads in Java programs, and supports our belief that default value reads can be found in real programs and should be considered errors. Our approach is stronger (detecting all errors at the expense of some correct programs) and considers additional language constructs that are not present in Java.

There has been a study on a large body [5] of Java code, showing that initialization order issues pervade projects from the real world. A bytecode verification system for Java initialization has also been explored [6].

An early work to support non-null types in Java [2] has the notion of a type constructor *raw* that can be applied to object types and means that the fields of the object (in X10 terminology) may violate the constraints in their types. This simply disables the type-system while an object is partially constructed while ensuring the rest of the program is typed normally. Our approach prevents errors during constructors as it does not disable the type-system, and it also permits optimization of the representation of fields whose types are very constrained, since they will never have to hold a value other than the values allowed by their type constraint.

A later work [3, 9] allows to specify the time (in the type) when the object will be fully constructed. Field reference types of a partially constructed objects must be fully constructed by the same time, which allows graphs of objects to be constructed like our *proto* design. However the system is more complicated, allowing the object to become fully constructed at a given future time, instead of at the specific time when its constructor terminates.

Masked types [9] present types that describe the exact fields that have not yet been initialized. Our type system is simpler but less expressive.

There is also a time-aware type system [7] that allows the detection of data-races, and understands the concept of shared variables that become immutable only after a certain time (and can then be accessed without synchronization). The same mechanisms can also be used to express when an object becomes cooked.

Ownership types can be used to create immutable cycles [11]. This is comparable to our *proto* design because it also allows this to be linked from an incomplete object. However the ownership

structure is used to implement a broader policy, allowing code in the owner to use a reference to its partially constructed children, whereas we only allow code to use a reference to objects that are being partially constructed in some nesting stack frame. Our approach does not use ownership types.

6. Conclusion

The hardhat design in X10 is strict but it protects the user from error-prone initialization idioms, especially when combined with a rich type system and parallel code. This paper showed the interaction between initialization and other language features, possible pitfalls in Java, and how they can be prevented in X10. It also presented the rules of this design, the virtues of these rules, and possible design alternatives. The rules were incorporated in the open-source X10 compiler, and are being used in production code.

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7. Proofs for the Formalism

A closed statement is reduced to a closed statement.

Lemma 7.1. (Closed statement) If $\vdash s$ and $s, H \rightsquigarrow s', H'$ then $\vdash s'$.

Proof. The only rules that introduce free variables are R-VAL and R-INVOKE.

In rule R-VAL we have

$$\text{val } x = e; s, H \rightsquigarrow s[1/x], H'$$

Therefore, s might have a free variable (x), but $s[1/x]$ is closed.

In rule R-INVOKE we have

$$1'.m(\bar{x}), H \rightsquigarrow s[\bar{x}/\bar{x}, 1'/\text{this}], H$$

The method body can only refer to the free variables \bar{x} and this , therefore $s[\bar{x}/\bar{x}, 1'/\text{this}]$ is closed. \square

Monotonicity of cooked heaps: during the process of reduction, the heap stays correctly-cooked and it becomes more cooked.

Lemma 7.2. (Correctly-cooked heaps) If $\vdash H$ and (i) $s, H \rightsquigarrow s', H'$ or (ii) $s, H \rightsquigarrow H'$, then $\vdash H'$ and $H' \vdash H$.

Proof. By definition: (i) $\vdash H$ if for every object $o = C(F)$ in the range of H and every field $f \in \text{dom}(F)$ it is the case that every object $1 = H(F(f))$ is cooked ($\text{cooked}_H(1)$). (ii) $H' \vdash H$ if for every $1 \in \text{dom}(H)$, we have $H(1) = C(F)$, $H'(1) = C(F')$, and $\text{dom}(F) \subseteq \text{dom}(F')$.

By structural induction on s .

For R-TERM and R-STEP, by induction $\vdash H'$ and $H' \vdash H$.

For R-VAL, $e, H \rightsquigarrow 1', H'$ in two possible ways: R-NEW or R-ACCESS. In R-NEW, we created a new location $1'$ that is not connected to any other location, so $\vdash H'$ and $H' \vdash H$. In R-ACCESS, $H' = H$.

In R-INVOKE, $H' = H$.

Only R-ASSIGN ($1.f = 1'$) changes the heap, and it requires that $\text{cooked}_H(1')$ so $\vdash H'$. Let $H(1) = C(F)$ and $H'(1) = C(F')$, where $F' = F[f \mapsto 1']$, so $\text{dom}(F) \subseteq \text{dom}(F')$. Thus $H' \vdash H$. \square

Lemma 7.3. (Properties of plus and minus) For all ϕ , (i) $\vdash \pm \phi = \pm \phi$, (ii) $\vdash \pm \phi = -\phi$.

Proof. Routine. \square

Lemma 7.4. (Properties of the logic system) Let $\phi \vdash \psi$. Then (i) $\vdash \phi \vdash \pm \psi$, (ii) $\vdash \phi \vdash -\psi$, (iii) for all ϕ' , we have $\phi', \phi \vdash \phi', \psi$.

Proof. Routine. \square

Lemma 7.5. (Properties of heaps and formulas) For all heaps H , (i) $H \vdash -\phi$, (ii) if $H \vdash \pm \phi$ then $H \vdash \phi$, (iii) if $H \vdash \phi$ and $H \vdash \psi$ then $H \vdash \phi, \psi$, (iv) if $H \vdash \phi$ and $H' \vdash H$ then $H' \vdash \phi$.

Proof. Routine. \square

The meaning of substitution for statement is to replace all the free occurrences of a variable. For example, for the following statement s

$$x.f = 1; \text{val } x = \text{new } C; x.f = 1$$

if we substitute x with $1'$, written as $s[1'/x]$, the result is

$$1'.f = 1; \text{val } x = \text{new } C; x.f = 1$$

Lemma 7.6. (Substitution lemma) Given a heap H , a location 1 whose type is C , a variable x whose type is D , a statement s , and

$$\vdash H \quad C \leq D \quad \phi \vdash \psi$$

then $\phi[1/x] \vdash s[1/x] \vdash \psi[1/x]$.

Proof. Routine (by induction on the derivation sequence of $\phi \vdash \psi$, considering each rule in Fig. 16). The only sensitive point is that the type of 1 is a subtype x , and therefore in T-INVOKE we use the fact that when method m is overridden by m' then their inferred decorations (ϕ, ψ) and (ϕ', ψ') satisfy $\phi \vdash \phi'$ and $\psi' \vdash \psi$. \square

Lemma 7.7. (Preservation for terminal configurations) Let $\phi \vdash \acute{s}$, $\vdash \acute{s}, \vdash H$, $H \vdash \acute{\phi}$, and $\acute{s}, H \rightsquigarrow H'$. Then $H' \vdash \acute{\psi}$.

Proof. By structural induction on \acute{s} . Only two rules result with a terminal configuration: R-TERM (for finish and async) and R-ASSIGN.

• In R-TERM for finish we have:

$$\acute{s} = \text{finish } \{s\} \quad s, H \rightsquigarrow H' \quad (1)$$

From $\phi \vdash \acute{\psi}$ and T-FINISH

$$\acute{\psi} = \pm \psi \quad \phi \vdash \psi \quad \acute{\phi} = \phi \quad \phi \text{ finish } \{s\} \vdash \psi \quad (2)$$

Because $s, H \rightsquigarrow H'$ and $\phi \vdash \psi$ (from (2)), by induction we have

$$H' \vdash \pm \psi \quad (3)$$

Because $\acute{\psi} = \pm \psi$ and $\pm \pm \psi = \pm \psi$ (Lem. 7.3), from (3), we conclude $H' \vdash \acute{\psi}$.

• In R-TERM for async we do the same proof but use the fact that $\pm - \psi = \pm \psi$ (Lem. 7.3).

• In R-ASSIGN we have:

$$\begin{aligned} \acute{s} &= 1.f = 1' & H(1) &= C(F) & \text{cooked}_H(1') \\ H' &= H[1 \mapsto C(F[f \mapsto 1'])] \end{aligned} \quad (4)$$

Thus, $H' \vdash 1.f$. From $\phi \vdash \acute{\psi}$ and T-ASSIGN

$$\acute{\phi} = \phi \quad \acute{\psi} = \pm 1.f \quad \phi \vdash 1.f = 1' + 1.f \quad \phi \vdash \pm 1' \quad (5)$$

From (4) and (5), we conclude $H' \vdash \acute{\psi}$. Because $\pm \acute{\psi} = \acute{\psi}$ we also have $H' \vdash \pm \acute{\psi}$. \square

Lemma 7.8. (Preservation for non-terminal configurations) Let

$$\acute{\phi} \vdash \acute{\psi} \quad \vdash \acute{s} \quad \vdash H \quad H \vdash \acute{\phi} \quad \acute{s}, H \rightsquigarrow \acute{s}, H' \quad (6)$$

Then there exists $\acute{\phi}, \acute{\psi}$ such that

$$H' \vdash \acute{\phi} \quad \acute{\phi} \vdash \acute{\psi} \quad \acute{\phi} \vdash \acute{\phi} \quad \acute{\psi} \vdash \acute{\psi} \quad (7)$$

Proof. By structural induction on \acute{s} .

• For R-TERM for sequences we have

$$\acute{s} = s \ s' \quad \acute{s} = s' \quad s, H \rightsquigarrow H' \quad (8)$$

From T-SEQ and (6) ($\acute{\phi} \vdash \acute{\psi}$),

$$\acute{\phi} = \phi \quad \acute{\psi} = \psi_1, \psi_2 \quad \phi \vdash \psi_1 \quad \phi, \psi_1 \ s' \ \psi_2 \quad (9)$$

From (8) and (9), by Lem. 7.7

$$H' \vdash \pm \psi_1. \quad (10)$$

Let $\acute{\phi} = \phi, \psi_1$ and $\acute{\psi} = \psi$. Then from (9)

$$\acute{\phi} \vdash \acute{\psi} \quad (11)$$

Because $\acute{\phi} = \phi, \psi_1$ then $\acute{\phi} \vdash \psi_1$, and because $\acute{\psi} = \psi = \psi_1, \psi_2$ then

$$\acute{\phi} \vdash \acute{\psi} \quad (12)$$

Trivially,

$$\begin{aligned} \phi, \psi_1 \vdash \phi & \quad \acute{\psi} = \psi \\ \acute{\phi} \vdash \acute{\phi} & \quad \acute{\psi} \vdash \acute{\psi} \end{aligned} \quad (13)$$

From (10) and Lem. 7.5,

$$H' \vdash \psi_1 \quad (14)$$

Because $H' \vdash H$ (Lem. 7.2) and $H \vdash \phi$, then from Lem. 7.5 $H' \vdash \phi$. Together, $H' \vdash \phi, \psi_1$. Because $\dot{\phi} = \phi, \psi_1$, we got $H' \vdash \dot{\phi}$.

• For R-STEP for finish, we have

$$\dot{s} = \text{finish } \{s\} \quad \dot{s} = \text{finish } \{s'\} \quad s, H \rightsquigarrow s', H' \quad (15)$$

Because $\dot{\phi} \dot{s} \dot{\psi}$, from T-FINISH,

$$\dot{\phi} = \phi \quad \dot{\psi} = +\psi \quad \phi \dot{s} \psi \quad (16)$$

From (15) and (16), by induction, exists ϕ' and ψ' ,

$$\phi' \dot{s}' \psi' \quad \phi' \vdash \phi \quad \psi' \vdash \psi \quad H' \vdash \phi' \quad (17)$$

From T-FINISH and (17),

$$\dot{\phi}' \text{ finish } \{s'\} + \psi' \quad (18)$$

Let $\dot{\phi} = \phi'$ and $\dot{\psi} = +\psi'$, then from (17) and from Lem. 7.4,

$$\phi' \vdash \phi \quad +\psi' \vdash +\psi \quad \dot{\phi} \dot{s} \dot{\psi} \quad H' \vdash \phi' \quad (19)$$

• The proof for the first R-STEP for `async` is like that of `finish` above (but instead we use the fact that if $\psi' \vdash \psi$ then $-\psi' \vdash -\psi$ in Lem. 7.4).

• For the second `async` R-STEP, we have

$$\dot{s} = \text{async } \{s_1\} s \quad \dot{s} = \text{async } \{s_1\} s' \quad s, H \rightsquigarrow s', H' \quad (20)$$

Because $\dot{\phi} \dot{s} \dot{\psi}$, from T-SEQ,

$$\dot{\phi} = \phi \quad \dot{\psi} = \psi_1, \psi_2 \quad \phi \text{ async } \{s_1\} \psi_1 \quad \phi, \psi_1 \dot{s} \psi_2 \quad (21)$$

From T-ASYNC we know that there exists ψ'_1 such that $\psi_1 = -\psi'_1$, therefore from Lem. 7.5, we have that for any H , it holds $H \vdash \psi_1$. Thus, $H \vdash \phi, \psi_1$. From that and $\phi, \psi_1 \dot{s} \psi_2$ we can apply the induction and get that there exists ϕ' and ψ' such that

$$\phi' \dot{s}' \psi' \quad \phi' \vdash \phi, \psi_1 \quad \psi' \vdash \psi_2 \quad H' \vdash \phi' \quad (22)$$

Then from (21), (22),

$$\dot{\phi}' \text{ async } \{s_1\} \psi_1 \quad \dot{\phi}', \psi_1 \dot{s}' \psi' \quad (23)$$

From (23) and T-SEQ

$$\dot{\phi}' \text{ async } \{s_1\} s' \psi_1, \psi' \quad (24)$$

Let $\dot{\phi} = \phi'$ and $\dot{\psi} = \psi_1, \psi'$, then

$$\dot{\phi} \text{ async } \{s_1\} s' \dot{\psi} \quad \dot{\phi}' \vdash \phi \quad \psi_1, \psi' \vdash \psi_1, \psi_2 \quad H' \vdash \dot{\phi} \quad (25)$$

• For R-STEP for sequences, we have

$$\dot{s} = s \ s_1 \quad \dot{s} = s' \ s_1 \quad s, H \rightsquigarrow s', H' \quad (26)$$

Because $\dot{\phi} \dot{s} \dot{\psi}$, from T-SEQ,

$$\dot{\phi} = \phi \quad \dot{\psi} = \psi_1, \psi_2 \quad \phi \dot{s} \psi_1 \quad \phi, \psi_1 \dot{s}_1 \psi_2 \quad (27)$$

From (26) and (27), by induction ($s, H \rightsquigarrow s', H'$ and $H \vdash \phi$ and $\phi \dot{s} \psi_1$), exists ϕ' and ψ'_1 ,

$$\phi' \dot{s}' \psi'_1 \quad \phi' \vdash \phi \quad \psi'_1 \vdash \psi_1 \quad H' \vdash \phi' \quad (28)$$

Thus, from (28), we have

$$\dot{\phi}', \psi'_1 \vdash \phi, \psi_1 \quad (29)$$

From (27) and (29),

$$\dot{\phi}', \psi'_1 \dot{s}_1 \psi_2 \quad (30)$$

From T-SEQ, (28) ($\phi' \dot{s}' \psi'_1$) and (30),

$$\dot{\phi}' \dot{s}' s_1 \psi'_1, \psi_2 \quad (31)$$

Let $\dot{\phi} = \phi'$ and $\dot{\psi} = \psi'_1, \psi_2$, then from (28) and (31) and from Lem. 7.4,

$$\phi' \vdash \phi \quad \psi'_1, \psi_2 \vdash \psi_1, \psi_2 \quad \dot{\phi} \dot{s} \dot{\psi} \quad H' \vdash \phi' \quad (32)$$

• For R-VAL,

$$\dot{s} = \text{val } x = e; s \quad \dot{s} = s[1/x] \quad e, H \rightsquigarrow 1, H' \quad (33)$$

We have two possible ways to reduce e : either with R-NEW or R-ACCESS. Consider first R-NEW, so

$$e = \text{new } C \quad 1 \notin \text{dom}(H) \quad H' = H[1 \mapsto c()] \quad (34)$$

Because $\dot{\phi} \text{ val } x = \text{new } C; s \dot{\psi}$, from T-NEW,

$$\dot{\phi} = \phi \quad \dot{\psi} = \psi \quad \phi \dot{s} \psi \quad (35)$$

Because H contains only locations 1 (not variables x), and $H \vdash \phi$, then ϕ and ψ cannot contain variables x , thus $\phi[1/x] = \phi$ and $\psi[1/x] = \psi$. From Lem. 7.6 (because H and s are well-typed, so the type of 1 is a subtype of x) and (35), we have

$$\phi \dot{s}[1/x] \psi \quad (36)$$

From Lem. 7.5, because $H' \vdash H$ (Lem. 7.2), then

$$H' \vdash \dot{\phi} \quad (37)$$

We choose $\dot{\phi} = \phi$ and $\dot{\psi} = \psi$, thus from (36) and (37),

$$H' \vdash \dot{\phi} \quad \dot{\phi} \vdash \phi \quad \dot{\psi} \vdash \psi \quad \dot{\phi} \dot{s} \dot{\psi} \quad (38)$$

Now consider R-ACCESS, so

$$e = 1'.f_i \quad H(1') = c(\bar{f} \mapsto \bar{1}'') \quad 1 = 1''_i \quad H' = H \quad (39)$$

Because $\vdash H$ then 1 is cooked, i.e.,

$$H \vdash +1$$

Because $\dot{\phi} \text{ val } x = 1'.f_i; s \dot{\psi}$, from T-ACCESS,

$$\dot{\phi} = \phi \quad \dot{\psi} = \psi \quad \phi \vdash +1'.f_i \quad \phi, +x \dot{s} \psi \quad (40)$$

Like for R-NEW, we have that $\phi[1/x] = \phi$ and $\psi[1/x] = \psi$. From Lem. 7.6 and (40), we have

$$\phi, +1 \dot{s}[1/x] \psi \quad (41)$$

Because $H' = H$ and $H \vdash \phi$ and $H \vdash +1$, then

$$H' \vdash \phi, +1 \quad (42)$$

We choose $\dot{\phi} = \phi, +1$ and $\dot{\psi} = \psi$, thus from (41) and (42),

$$H' \vdash \dot{\phi} \quad \dot{\phi} \vdash \phi \quad \dot{\psi} \vdash \psi \quad \dot{\phi} \dot{s} \dot{\psi} \quad (43)$$

• For R-INVOKE,

$$\dot{s} = 1'.m(\bar{1}) \quad \dot{s} = s[\bar{1}/\bar{x}, 1'/\text{this}] \quad H(1') = c(\dots) \quad mbody(m, c) = \bar{x}.s \quad H' = H \quad (44)$$

Because $\dot{\phi} \dot{s} \dot{\psi}$, from T-INVOKE,

$$\dot{\phi} = \phi \quad \dot{\psi} = \psi'[\bar{1}'/\text{this}, \bar{1}/\bar{x}] \quad m(\bar{x}) :: \phi' \Rightarrow \psi' \quad \phi \vdash \phi'[\bar{1}'/\text{this}, \bar{1}/\bar{x}] \quad (45)$$

From the definition of $m(\bar{x}) :: \phi' \Rightarrow \psi'$ we have that

$$\dot{\phi}' \dot{s} \dot{\psi}' \quad (46)$$

From Lem. 7.6 (because H and \dot{s} are well-typed, so the type of $\bar{1}$ is a subtype of \bar{x} , and the type of $1'$ is a subtype of this) and (46), we have

$$\dot{\phi}'[\bar{1}'/\text{this}, \bar{1}/\bar{x}] \dot{s}[\bar{1}'/\text{this}, \bar{1}/\bar{x}] \dot{\psi}'[\bar{1}'/\text{this}, \bar{1}/\bar{x}] \quad (47)$$

We choose $\dot{\phi} = \dot{\phi}'$ and $\dot{\psi} = \dot{\psi}'$, thus from (44), (45) and (47),

$$H' \vdash \dot{\phi} \quad \dot{\phi} \vdash \phi \quad \dot{\psi} \vdash \psi \quad \dot{\phi} \dot{s} \dot{\psi} \quad (48)$$

• (Note that R-ASSIGN was handled in Lem. 7.7.) \square

Theorem 7.9. (Preservation) Let

$$\phi \vdash S \quad \vdash S \quad \vdash H \quad H \vdash \phi$$

(a) If $S, H \rightsquigarrow H'$ then

$$\vdash H' \quad H' \vdash H \quad H' \vdash +\psi$$

(b) If $S, H \rightsquigarrow S', H'$ then

$$\vdash S' \quad \vdash H' \quad H' \vdash H$$

and there exists ϕ', ψ' such that

$$H' \vdash \phi' \quad \phi' \vdash S' \quad \psi' \vdash \psi \quad \phi' \vdash \phi \quad \psi' \vdash \psi$$

Proof. Follows from Lem. 7.1, Lem. 7.2, Lem. 7.7, and Lem. 7.8. \square

Progress means that a proper non-terminal configuration can always be reduced.

Theorem 7.10. (Progress) Let

$$\phi \vdash \acute{S} \quad \vdash \acute{S} \quad \vdash H \quad H \vdash \phi$$

Then there exists \acute{S}, H' such that either $\acute{S}, H \rightsquigarrow H'$ or $\acute{S}, H \rightsquigarrow \acute{S}, H'$.

Proof. By structural induction on \acute{S} . According to the syntax, \acute{S} is one of the following:

$$\begin{aligned} S &::= p.f = p; \mid p.m(\vec{p}); \mid \text{val } x = e; S \mid \text{finish } \{S\} \mid \text{async } \{S\} \mid S \mid S \\ e &::= p.f \mid \text{new } C \end{aligned}$$

Because $\vdash \acute{S}$ we know that p cannot be a variable (only a location in H), so

$$\begin{aligned} S &::= l.f = l; \mid l.m(\vec{l}); \mid \text{val } x = e; S \mid \text{finish } \{S\} \mid \text{async } \{S\} \mid S \mid S \\ e &::= l.f \mid \text{new } C \end{aligned}$$

We will show that for each of these possibilities, there is a matching reduction rule that can be applied.

- If $\acute{S} = \text{finish } \{S\}$, then because $\phi \vdash \acute{S}$, we have from T-FINISH,

$$\phi \vdash S \quad \phi = \phi \quad \psi = +\psi \quad (49)$$

Therefore, by induction, there exists S', H' such that either $S, H \rightsquigarrow H'$ or $S, H \rightsquigarrow S', H'$. Therefore, we can either apply R-TERM or R-STEP on \acute{S} , i.e., either $\acute{S}, H \rightsquigarrow H'$ or $\acute{S}, H \rightsquigarrow \text{finish } \{S'\}, H'$.

- If $\acute{S} = \text{async } \{S\}$, then the same proof as above holds (except changing $+$ to $-$).

- If $\acute{S} = S_1 S_2$, then because $\phi \vdash \acute{S}$, we have from T-SEQ,

$$\phi \vdash S_1 \quad \psi_1 \vdash S_2 \quad \psi_2 \quad \phi = \phi \quad \psi = \psi_1, \psi_2 \quad (50)$$

By induction, there exists S'_1, H' such that either $S_1, H \rightsquigarrow H'$ or $S_1, H \rightsquigarrow S'_1, H'$. Therefore, we can either apply R-TERM or R-STEP on \acute{S} , i.e., either $\acute{S}, H \rightsquigarrow S_2, H'$ or $\acute{S}, H \rightsquigarrow S'_1 S_2, H'$.

- If $\acute{S} = l'.m(\vec{l})$, then we can simply apply R-INVOKE.
- If $\acute{S} = l.f = l'$, then because $\phi \vdash \acute{S}$, we have from T-ASSIGN, that

$$\phi \vdash +l'$$

And because $H \vdash \phi$ we have that $\text{cooked}_H(l')$. Thus we can apply R-ASSIGN, i.e.,

$$H(l) = c(F) \quad \acute{S}, H \rightsquigarrow H[l \mapsto c(F[l \mapsto l'])]$$

- Finally, $\acute{S} = \text{val } x = e; S$. If $e = \text{new } C$ then by R-NEW, we have

$$e, H \rightsquigarrow l', H[l' \mapsto c()]$$

If $e = l.f$, then because $\phi \vdash \acute{S}$, we have from T-ACCESS,

$$\phi \vdash +l.f$$

And because $H \vdash \phi$, we have that l has the field f in the heap, i.e.,

$$H(l) = c(F) \quad f \in \text{dom}(F)$$

Thus, we can apply R-ACCESS and get $l.f, H \rightsquigarrow l', H$. In both cases, we have that e was reduced to l' , thus we can apply R-VAL and get

$$\acute{S}, H \rightsquigarrow S[l'/x], H'$$

\square