
Algorithm 1: CCC algorithm

1 **Function** get_partitions(\mathbf{v} , k_{\max}):

Output:

Ω_r : clustering with r clusters over n objects

2 **if** $\mathbf{v} \in \mathbb{R}^n$ **then**

3 **for** $r \leftarrow 2$ **to** $\min\{k_{\max}, |\mathbf{v}| - 1\}$ **do**

4 $\rho \leftarrow (\rho_\ell \mid \Pr(v_i < \rho_\ell) \leq (\ell - 1)/r), \forall \ell \in [1, r + 1]$

5 $\Omega_{r\ell} \leftarrow \{i \mid \rho_\ell < v_i \leq \rho_{\ell+1}\}, \forall \ell \in [1, r]$

6 **else**

7 $\mathcal{C} \leftarrow \cup_j \{v_i\}$

8 $r \leftarrow |\mathcal{C}|$

9 $\Omega_{rc} \leftarrow \{i \mid v_i = \mathcal{C}_c\}, \forall c \in [1, r]$

10 $\Omega \leftarrow \{\Omega_r \mid |\Omega_r| > 1\}, \forall r$

11 **return** Ω

12

13 **Function** ccc(\mathbf{x} , \mathbf{y} , k_{\max}):

Input:

\mathbf{x} : feature values on n objects

\mathbf{y} : feature values on n objects

k_{\max} : maximum number of internal clusters

Output:

c : similarity value for \mathbf{x} and \mathbf{y} ($c \in [0, 1]$)

14 $\Omega^{\mathbf{x}} = \text{get_partitions}(\mathbf{x}, k_{\max})$

15 $\Omega^{\mathbf{y}} = \text{get_partitions}(\mathbf{y}, k_{\max})$

16 $c \leftarrow \max\{\mathcal{A}(\Omega_p^{\mathbf{x}}, \Omega_q^{\mathbf{y}})\}, \forall p, q$

17 **return** $\max(c, 0)$
