

## dB Calculations

- Allows for dealing with large and small numbers easily
- $\text{dB} = 10 \log(\text{Distance})$

Distance		dB
1mm	0.001m	-30dB
1m	-	0 dB
10m	-	10 dB
100m	-	20dB
1km	1000m	30 dB
10km	10000m	40dB

Thermal Noise Power ( $N_0$ ) =  $kT$ 

(measured in watts/Hz)

 $k$ : Boltzmann's constant =  $1.380649 \times 10^{-23} \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1}$  $T$ : Absolute temperature (room temp.  $20^\circ\text{C} = 293\text{K}$ )

## Thermal Noise

$$N = -204 + 10 \log_{10}(B) \text{ — dBW} \quad N_0 = -204 \text{ dBW/Hz}$$

$$N = -174 + 10 \log_{10}(B) \text{ — dBm} \quad N_0 = -174 \text{ dBm/Hz}$$

↓  
Bandwidth

## Noise Factor

$$\text{noise factor, } F = \frac{\left(\frac{S}{N}\right)_{\text{in}}}{\left(\frac{S}{N}\right)_{\text{out}}}$$

## Noise Figure

$$\text{in dB, noise figure, } F = \left(\frac{S}{N}\right)_{\text{in}} (\text{dB}) - \left(\frac{S}{N}\right)_{\text{out}} (\text{dB})$$

## Total Noise

$$N = -204 + F(\text{dB}) + 10 \log_{10}(B) \text{ — dBW}$$

## path Loss

$$L = 20 \log_{10} \left( \frac{4\pi R}{\lambda} \right) \text{ dB}$$

$R$  = distance from transmitter  
 $\lambda$  = wavelength of signal from speed of light over frequency

Example: WiFi @ 2.4GHz → GHz ⇒  $10^9$   
 @ 100mW → THz ⇒  $10^{12}$

$$\lambda = \frac{3 \times 10^8 \text{ m/s}}{2.4 \times 10^9 \text{ Hz}} = 0.125 \text{ m}$$

$$L = 20 \log_{10} \left( \frac{4\pi(100)}{0.125} \right) = 80 \text{ dB}$$

Communication System	Received Power	Transmit Power
GSM	-51 dBm	Varies @ 900 & 1800 MHz
GPS	-155 dBW (-125 dBm)	25.6W @ 1573 MHz
WiFi	-75 dBm or better	100mW @ 2.4 GHz
Voyager Space Ships	-231 dBm	18W @ 8 GHz

## Summary Question 1:

Calculate path loss given  $f = 800 \text{ MHz}$  andPlympton 11 km &  $P_{\text{Tx}} = 400 \text{ W}$ Caradon 19 km &  $P_{\text{Tx}} = 100 \text{ kW}$ 

Then calculate the received power

⇒ Answer:

$$\text{dB calculations: } 10 \log_{10}(400) = 26 \text{ dBW}$$

$$10 \log_{10}(100 \times 10^3) = 50 \text{ dBW}$$

$$\lambda = \frac{3 \times 10^8}{800 \times 10^3} = 0.375 \text{ m}$$

$$\text{Path Loss: } 20 \log_{10} \left( \frac{4\pi(11000)}{0.375} \right) = 111 \text{ dB}$$

$$20 \log_{10} \left( \frac{4\pi(19000)}{0.375} \right) = 116 \text{ dB}$$

## Received Power

$$P_{\text{Tx}} - P_{\text{L}} = P_{\text{Rx}}$$

$$26 \text{ dB} - 111 \text{ dB} = -85 \text{ dBW} \rightarrow \text{Plympton}$$

$$50 \text{ dB} - 116 \text{ dB} = -66 \text{ dBW} \rightarrow \text{Caradon}$$

## Summary Question 2:

The WiFi in garage is 2.4GHz with bandwidth of 20MHz

 $P_{\text{Tx}} = 100 \text{ mW}$  and distance = 25m. Find  $P_{\text{Rx}}$  and SNR

$$\Rightarrow P_{\text{Rx}} = P_{\text{Tx}} - P_{\text{L}}$$

$$P_{\text{Tx}} = 100 \text{ mW} = 10 \log_{10}(100) = 20 \text{ dBW}$$

$$P_{\text{L}} = 20 \log_{10} \left( \frac{4\pi(25)}{0.125} \right) = 68 \text{ dB}$$

$$\text{Hence, } P_{\text{Rx}} = 20 \text{ dBW} - 68 \text{ dB} = -48 \text{ dBW}$$

$$\text{SNR} = P_{\text{Rx}} - N$$

$$N = -174 \text{ dBm} + 10 \log_{10}(20 \times 10^6) = -100$$

$$\text{SNR} = -48 \text{ dBm} - 100 = 52 \text{ dB}$$