SHA Hashing Notes

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Contents

1	$\mathbf{SH}A$	A 256	3
	1.1	Introduction	9
	1.2	Implementation	9
	1.3	Preprocessing	4

List of Tables

1.1]	Notation Reference																																				3
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Chapter 1

SHA 256

1.1 Introduction

SHA256 is a 256 bits hash. Ment to provide 128 bits of security against collision attack.

1.2 Implementation

SHA256 operates in a manner of MD4, MD5 and SHA-1. The message to be hashed is

- 1. Padded with its length in such a way that the result is multiple of 512 bits long.
- 2. Parsed into 512 bits message blocks M^1, M^1, \dots, M^1 ,
- 3. Message blocks are processed one block at a time: Beginning with a fixed initial hash value $H^{(0)}$, sequentially compute

$$H^{(i)} = H^{(i-1)} + C_{M^{(i)}}(H^{(i-1)})$$

where C is the SHA-256 compression function and + means word-wise $\mod 2^{32}$ addition. $H^{(N)}$ is the **hash** of M.

SHA-256 operates on 512-bits message block and a 256-bits intermidiate hash value. It essentially is a 256-bit cypher algorithm which encripts intermidiate hash value using the message block as key. Hence, their are two main components:

- Compression Function
- message schedule

Notation	Meaning
\oplus	Bitwise XOR
V	Bitwise AND
^	Bitwise OR
	Bitwise Complement
+	$\mod 2^{32}$ addition
\mathbb{R}^n	right shift by n bits
S^n	right rotate by n bits

Table 1.1: Notation Reference

All of the operators in 1.1 table act on 32-bit words.

The initial value of $H^{(0)}$ is the following sequence of 32 bit words (which are obtained by taking the fractional parts of the square roots of the first eight primes.)

$$H_1^{(0)} = 6a09e667 (1.1)$$

$$H_2^{(0)} = bb67ae85 (1.2)$$

$$H_3^{(0)} = 3c6ef372 (1.3)$$

$$H_4^{(0)} = a54ff53a (1.4)$$

$$H_5^{(0)} = 510e527f (1.5)$$

$$H_6^{(0)} = 9b05688c (1.6)$$

$$H_7^{(0)} = 1f83d9ab (1.7)$$

$$H_8^{(0)} = 5be0cd19 (1.8)$$

1.3 Preprocessing

Computing the hash of message begins by padding the message:

1. Pad the message in usual way: Suppose the length of message M, in bits, is l. Append the bit "1" to the end of message, and the the k zero bits, where k is the smallest non-negative solution to the equation $l+1+1\equiv 448 \mod 512$. To this append the 64-bit block which is equal to the number l written in binary. For example, the (8-bit ASCII) message "abc" has length $8\cdot 3=24$ so it is padded with a one, then 448-(24+1)=423 zero bits, and then the length to become the 512-bit padded message:

$$011000010110001001100011\underbrace{00\dots0}_{423-bits}\underbrace{00\dots011000}_{64-bits}$$