두 초점이 $(k, 0)$, $(-k, 0)$ 이고 길이의 차가 $2a$ 로 주어 졌을 때 쌍곡선의 방정식

(The hyperbolic equation when the two focal points are $(k, 0)$, $(-k, 0)$ and the difference in length is given by $2a$)

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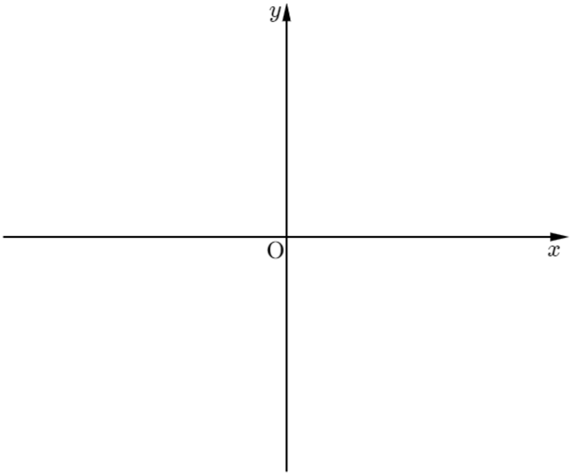

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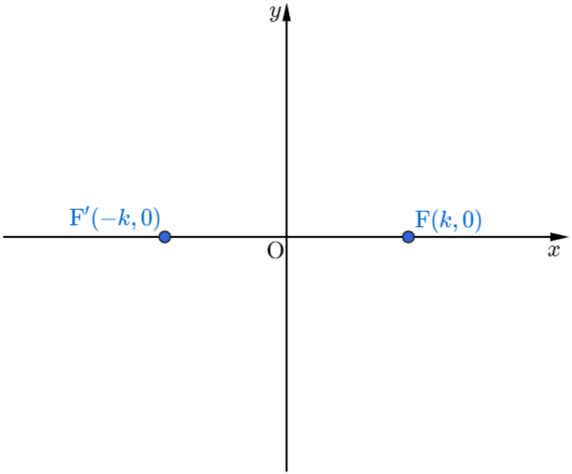

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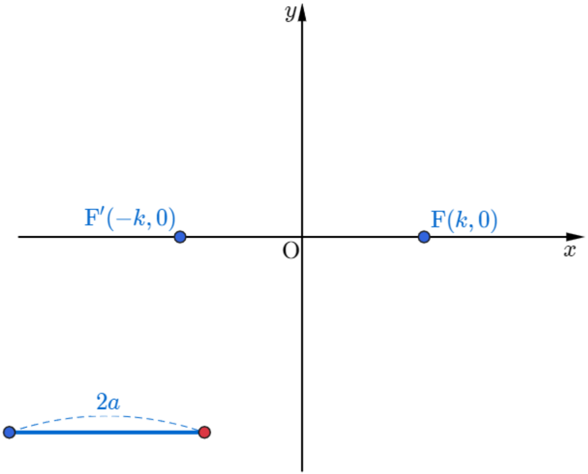

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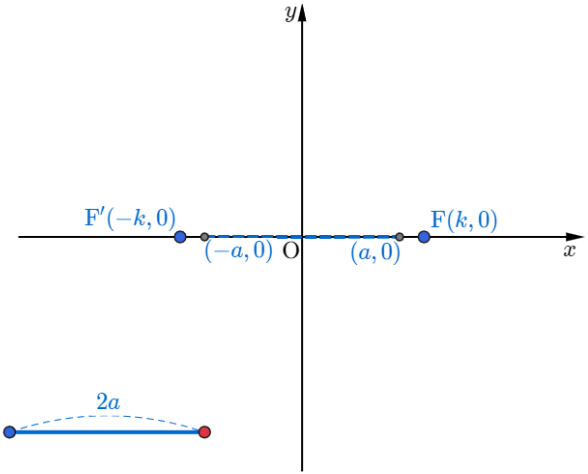

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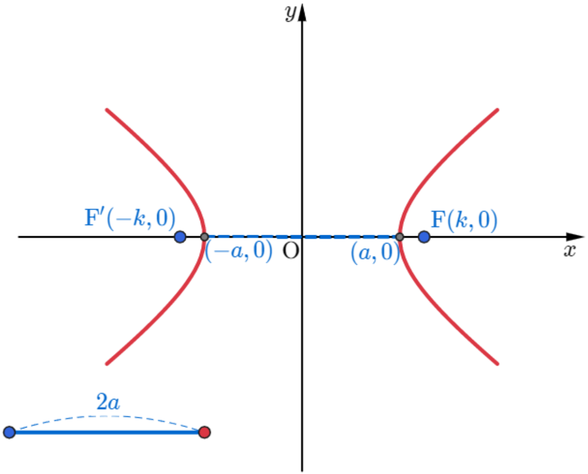

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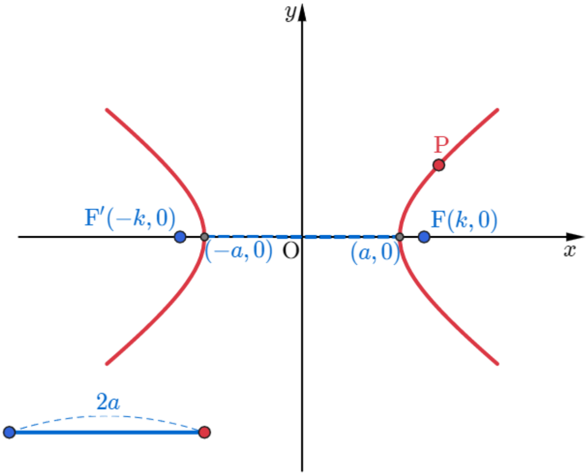

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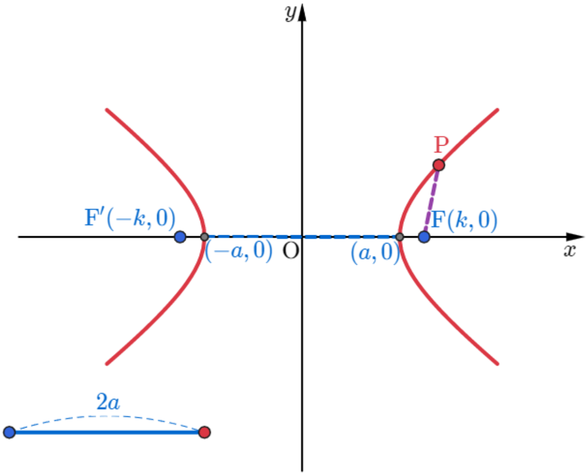

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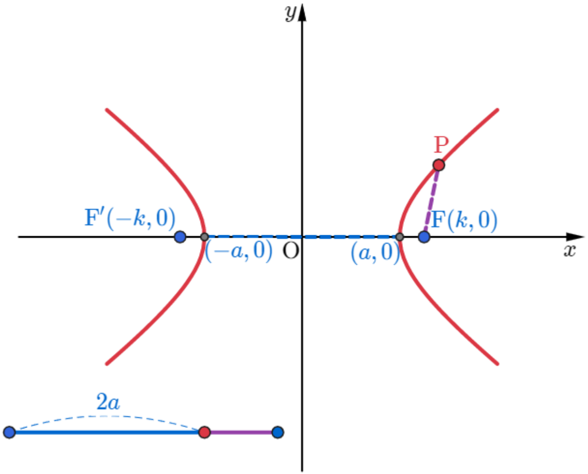

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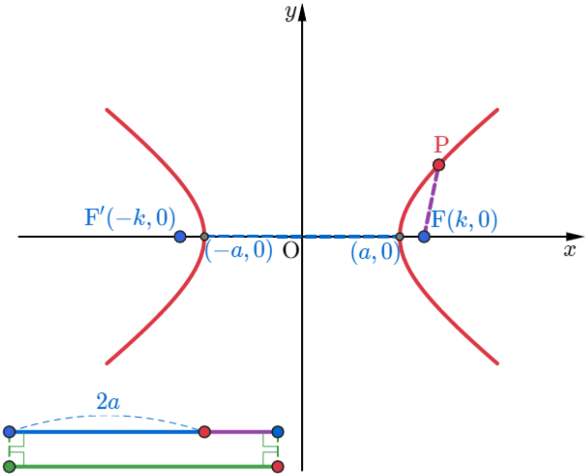

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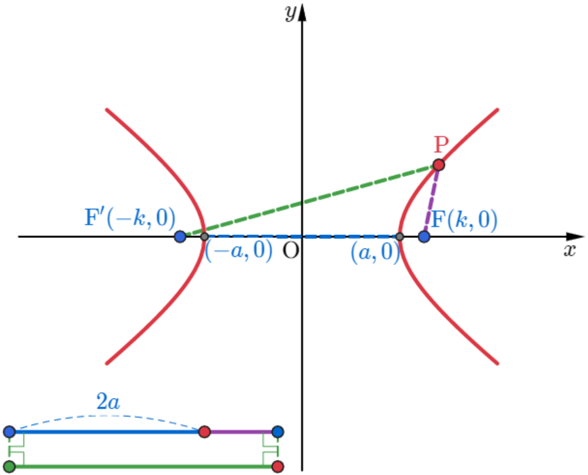

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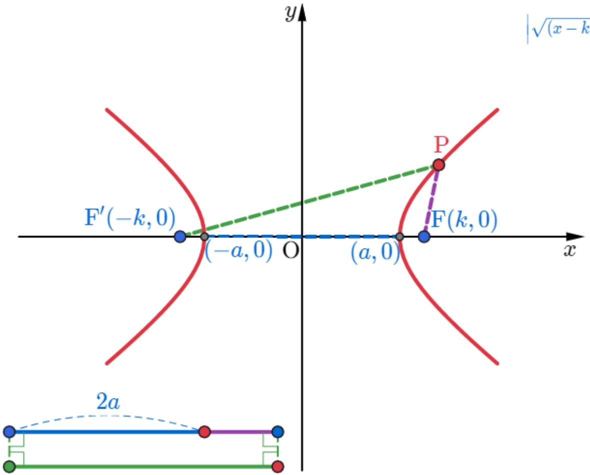

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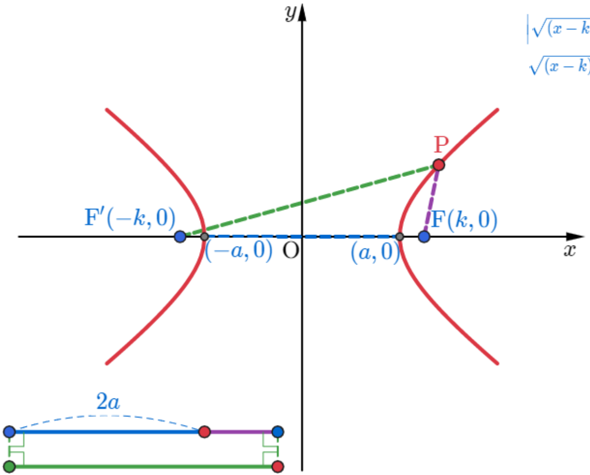

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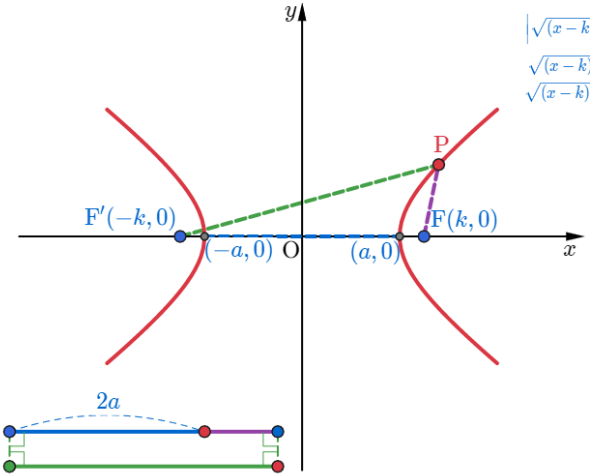

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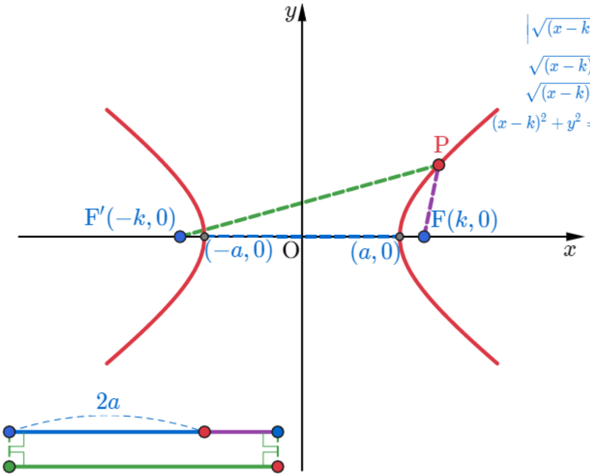

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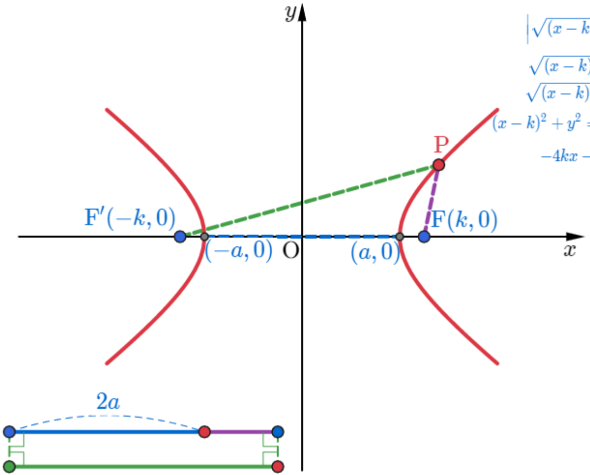

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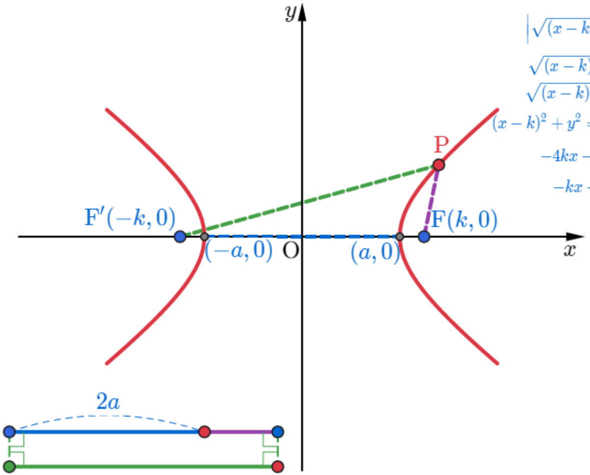

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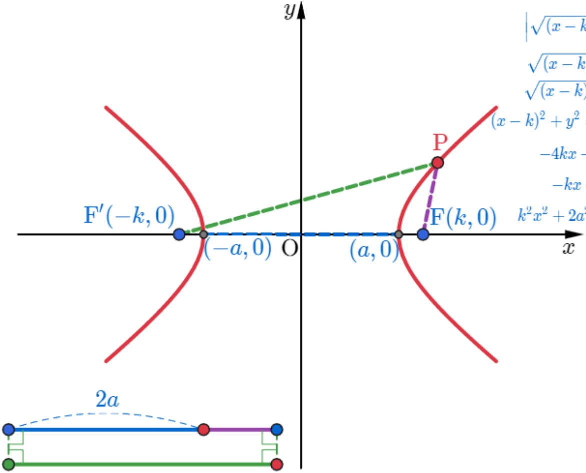

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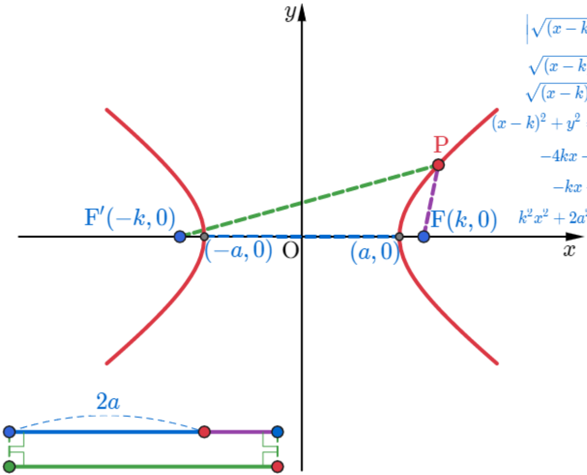

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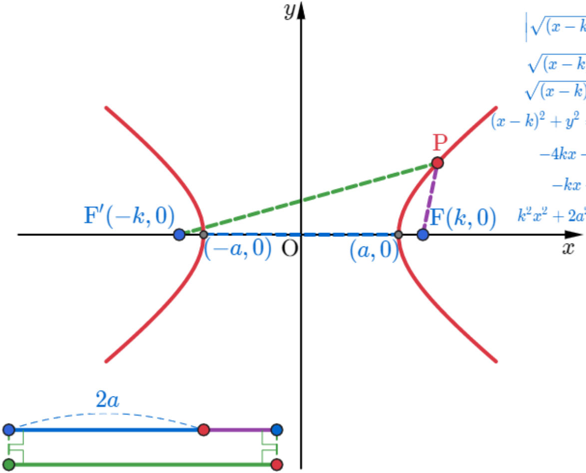

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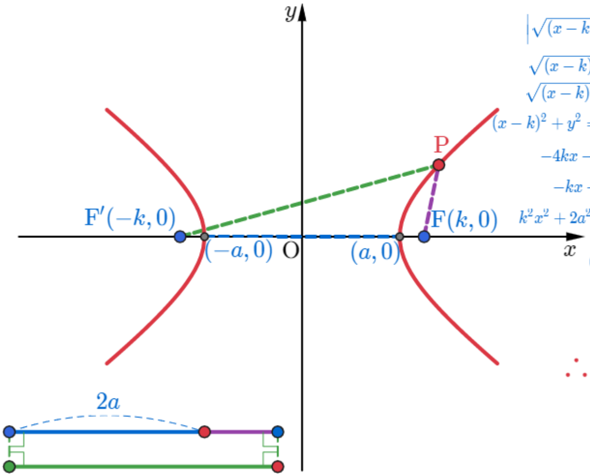

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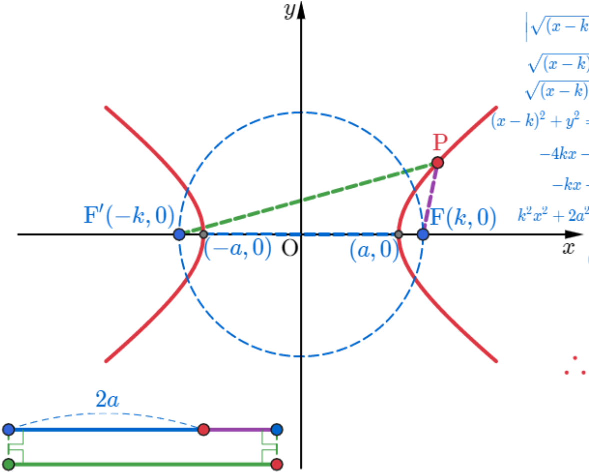

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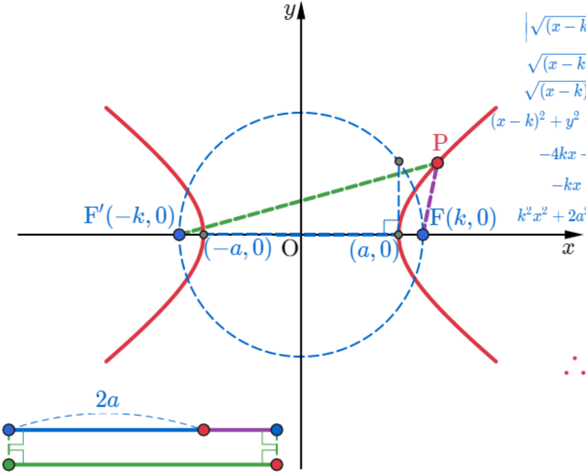

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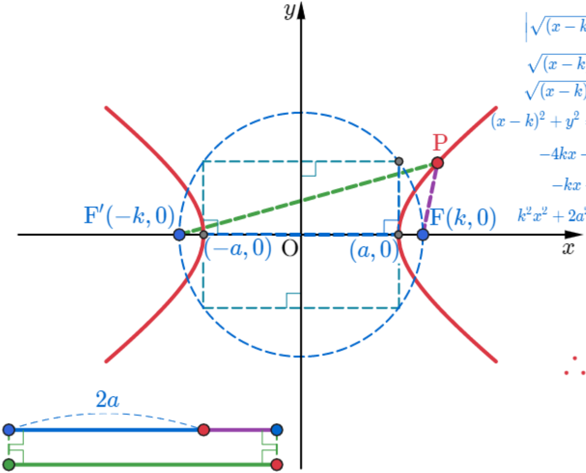

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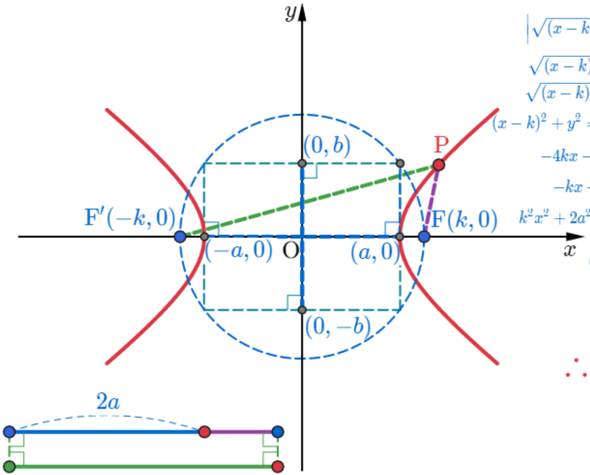

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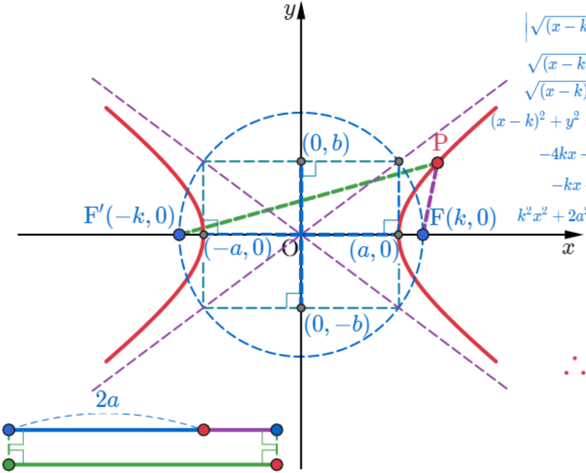

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Github:
https://min7014.github.io/math20200605001.html

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