아폴로니우스의 원 (Circle of Apollonius)









$$\begin{array}{ccc} \bullet & \bullet & \\ \mathbf{A}(x_1, y_1) & & \mathbf{B}(x_2, y_2) \end{array}$$

$$\overline{\mathrm{AP}}: \overline{\mathrm{BP}} = 1:r$$

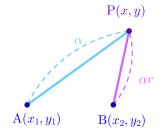
$$\begin{array}{ccc} \bullet & \bullet \\ \mathbf{A}(x_1, y_1) & & \mathbf{B}(x_2, y_2) \end{array}$$

$$\overline{\mathrm{AP}}: \overline{\mathrm{BP}} = 1:r$$

•

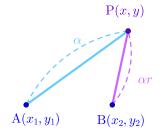
$$\begin{array}{ccc} \bullet & \bullet \\ \mathbf{A}(x_1, y_1) & & \mathbf{B}(x_2, y_2) \end{array}$$

$$\overline{\mathrm{AP}}: \overline{\mathrm{BP}} = 1:r$$



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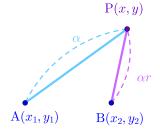
$$\overline{\mathrm{BP}} = r\overline{\mathrm{AP}}$$





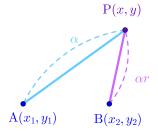
$$\overline{AP} : \overline{BP} = 1 : r$$

$$(x - x2)2 + (y - y2)2 = r2(x - x1)2 + r2(y - y1)2$$



$$\overline{AP} : \overline{BP} = 1 : r$$

$$x^{2} + y^{2} - 2\frac{x_{2} - x_{1}r^{2}}{1 - r^{2}}x - 2\frac{y_{2} - y_{1}r^{2}}{1 - r^{2}}y + \frac{x_{2}^{2} + y_{2}^{2} - (x_{1}^{2} + y_{1}^{2})r^{2}}{1 - r^{2}} = 0$$





$$\overline{AP} : \overline{BP} = 1 : r$$

$$\left(x - \frac{x_2 - x_1 r^2}{1 - r^2}\right)^2 + \left(y - \frac{y_2 - y_1 r^2}{1 - r^2}\right)^2 = \frac{\left\{(x_1 - x_2)^2 + (y_1 - y_2)^2\right\}r^2}{\left(1 - r^2\right)^2}$$

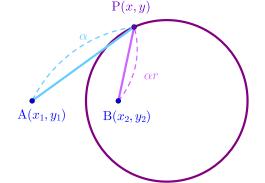
P(x,y)

$$\alpha$$
 $A(x_1, y_1)$ 
 $B(x_2, y_2)$ 



$$\overline{AP} : \overline{BP} = 1 : r$$

$$\left(x - \frac{x_2 - x_1 r^2}{1 - r^2}\right)^2 + \left(y - \frac{y_2 - y_1 r^2}{1 - r^2}\right)^2 = \frac{\left\{(x_1 - x_2)^2 + (y_1 - y_2)^2\right\}r^2}{\left(1 - r^2\right)^2}$$



#### Github:

https://min7014.github.io/math20210915001.html

Click or paste URL into the URL search bar, and you can see a picture moving.