

대수적으로 이차부등식 풀기

$$(ax^2 + bx + c > 0 \ (a > 0, b, c \in \mathbb{R}))$$

(Solving Quadratic Inequalities ($ax^2 + bx + c > 0$ ($a > 0, b, c \in \mathbb{R}$))
in Algebra)

Solving Quadratic Inequalities ($ax^2 + bx + c > 0$ ($a > 0, b, c \in \mathbb{R}$)) in Algebra

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$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

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$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

Let $D = b^2 - 4ac$

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- $D > 0$: Let α and β

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$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

Let $D = b^2 - 4ac$

- $D > 0$: Let α and β be roots

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Let $D = b^2 - 4ac$

- $D > 0$: Let α and β be roots of $ax^2 + bx + c = 0$

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Let $D = b^2 - 4ac$

- $D > 0$: Let α and β be roots of $ax^2 + bx + c = 0$ where $\alpha < \beta$.

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 $\therefore \alpha < x$

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$\therefore \alpha < x < \beta$ ▶ proof

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Let $D = b^2 - 4ac$

- $D > 0$: Let α and β be roots of $ax^2 + bx + c = 0$ where $\alpha < \beta$.
 $\therefore \alpha < x < \beta$ ▶ proof
- $D \leq 0$
 \therefore

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$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

Let $D = b^2 - 4ac$

- $D > 0$: Let α and β be roots of $ax^2 + bx + c = 0$ where $\alpha < \beta$.
 $\therefore \alpha < x < \beta$ ▶ proof
- $D \leq 0$
 \therefore No solutions ▶ proof

Solving Quadratic Inequalities ($ax^2 + bx + c > 0$ ($a > 0, b, c \in \mathbb{R}$)) in Algebra

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$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

$$x^2 + \frac{b}{a}x + \frac{c}{a} < 0 \quad (\because a > 0)$$

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Let α and β

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Let α and β be roots

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Let α and β be roots of $ax^2 + bx + c = 0$

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$$x^2 + \frac{b}{a}x + \frac{c}{a} < 0 \quad (\because a > 0)$$

$$\left(x + \frac{b}{2a}\right)^2 - \frac{b^2}{4a^2} + \frac{c}{a} < 0$$

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\therefore No solutions ($\because b^2 - 4ac \leq 0$)

Github:

<https://min7014.github.io/math20210514001.html>

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and you can see a picture moving.