

When a directrix is $y = -p$ and a focus is $(0, p)$, find the equation for the tangent line to the parabola at a given point (x_1, y_1) . [Geometric Approach]

준선이 $y = -p$ 이고 초점이 $(0, p)$ 일 때, 포물선
상의 점 (x_1, y_1) 에서의 접선의 방정식을
구하여라. [기하적 접근]

(When a directrix is $y = -p$ and a focus is $(0, p)$, find the equation
for the tangent line to the parabola at a given point
 (x_1, y_1) . [Geometric Approach])

When a directrix is $y = -p$ and a focus is $(0, p)$, find the equation for the tangent line to the parabola at a given point (x_1, y_1) . [Geometric Approach]

▶ Start

▶ End

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$$y = -p$$

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$F(0, p)$

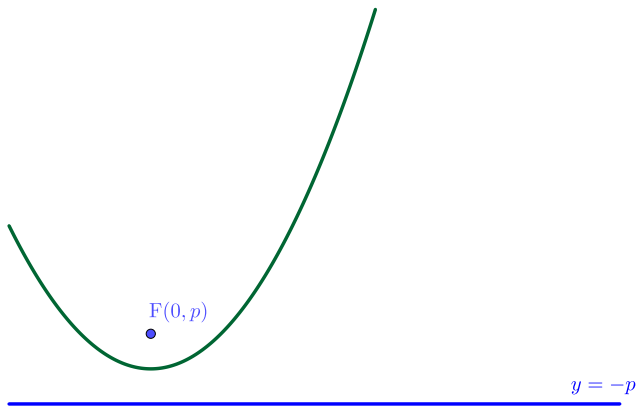


$y = -p$

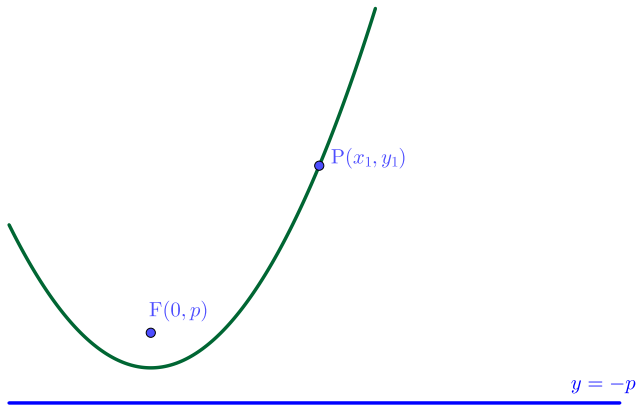
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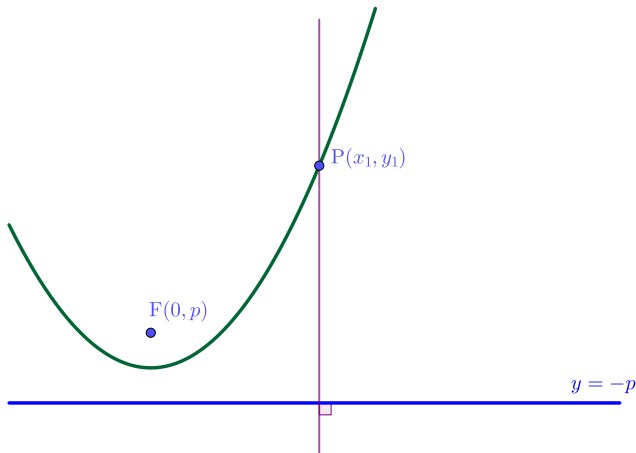
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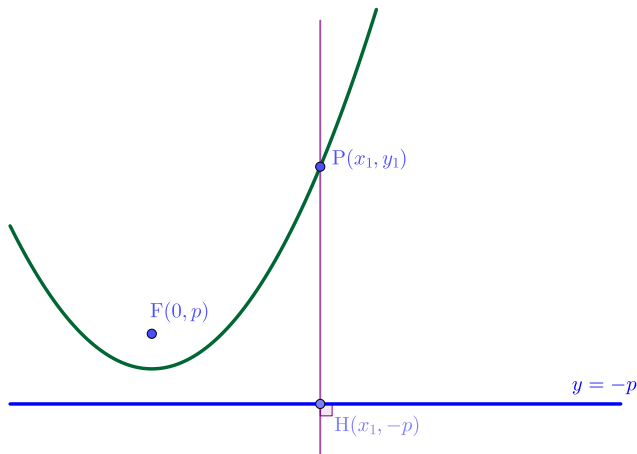
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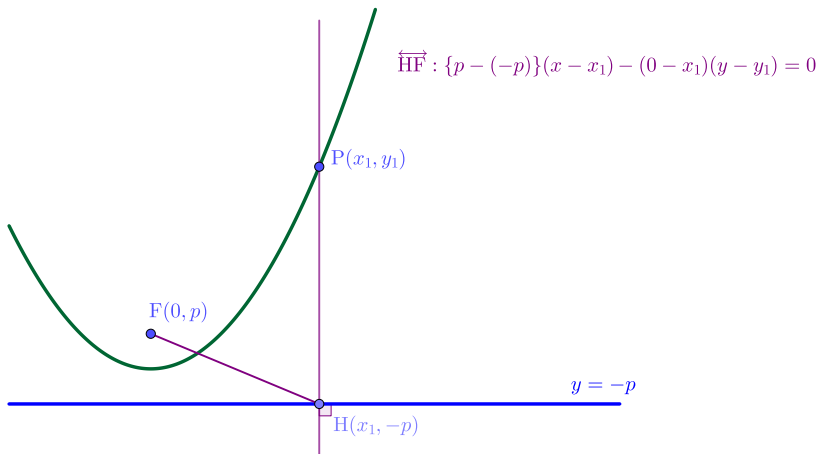
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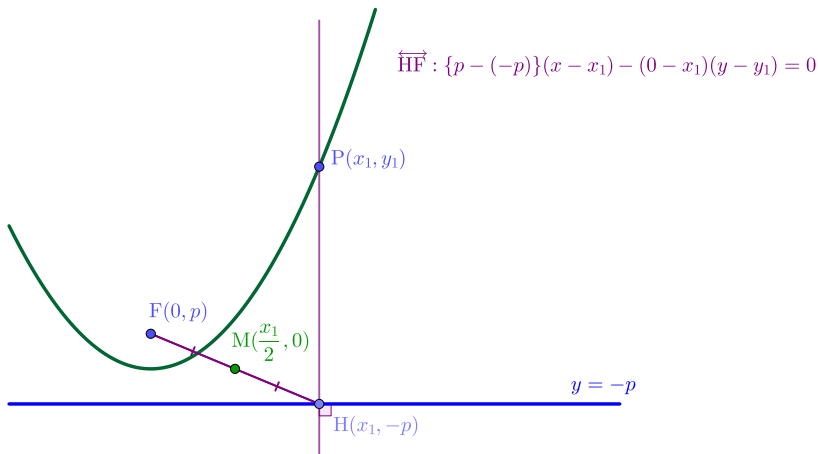
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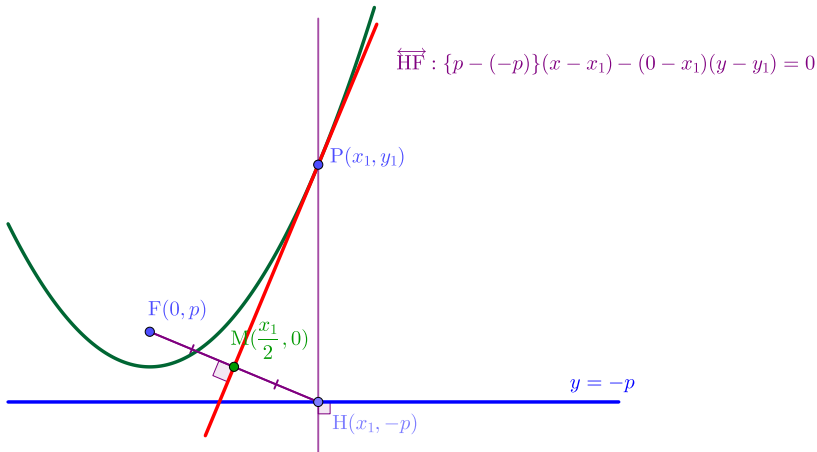
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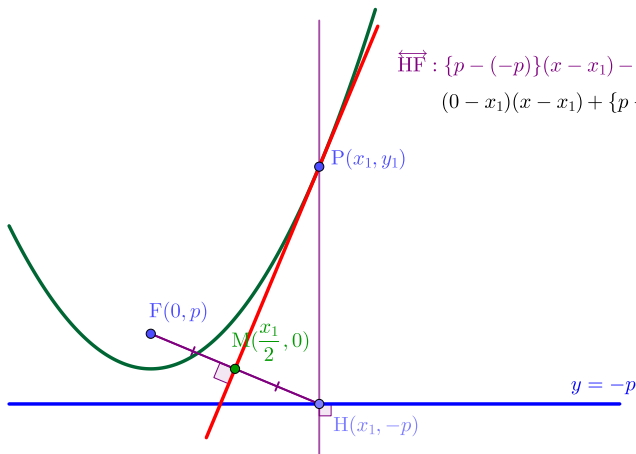
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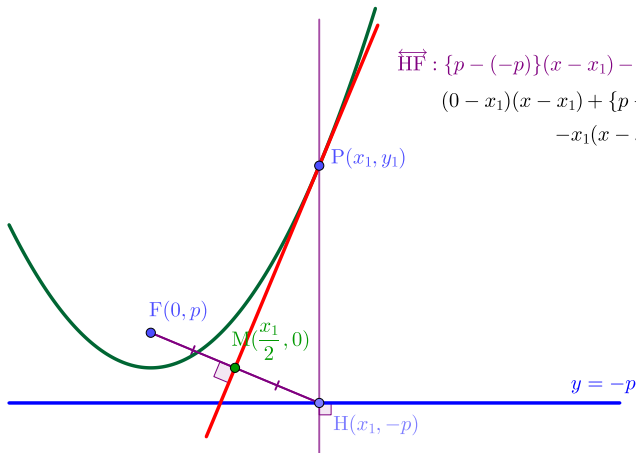


$$\begin{aligned}\overleftrightarrow{HF} : \{p - (-p)\}(x - x_1) - (0 - x_1)(y - y_1) &= 0 \\ (0 - x_1)(x - x_1) + \{p - (-p)\}(y - y_1) &= 0\end{aligned}$$

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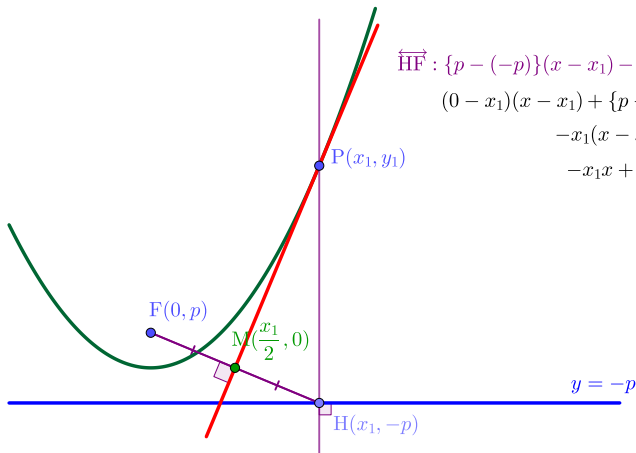


$$\begin{aligned}\overleftrightarrow{HF} : \{p - (-p)\}(x - x_1) - (0 - x_1)(y - y_1) &= 0 \\ (0 - x_1)(x - x_1) + \{p - (-p)\}(y - y_1) &= 0 \\ -x_1(x - x_1) + 2p(y - y_1) &= 0\end{aligned}$$

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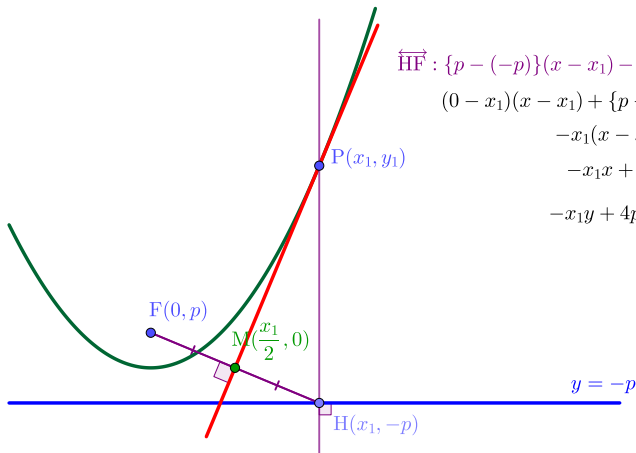


$$\begin{aligned}\overleftrightarrow{HF} : \{p - (-p)\}(x - x_1) - (0 - x_1)(y - y_1) &= 0 \\ (0 - x_1)(x - x_1) + \{p - (-p)\}(y - y_1) &= 0 \\ -x_1(x - x_1) + 2p(y - y_1) &= 0 \\ -x_1x + x_1^2 + 2py - 2py_1 &= 0\end{aligned}$$

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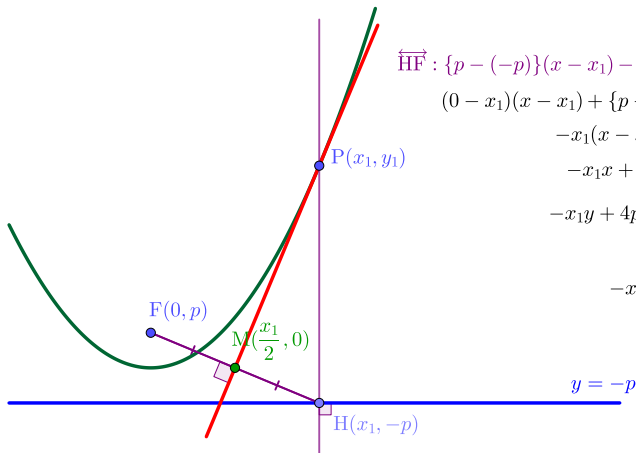


$$\begin{aligned}
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 -x_1(x - x_1) + 2p(y - y_1) &= 0 \\
 -x_1x + x_1^2 + 2py - 2py_1 &= 0 \\
 -x_1y + 4py_1 + 2py - 2py_1 &= 0 \\
 (\because x_1^2 = 4py_1)
 \end{aligned}$$

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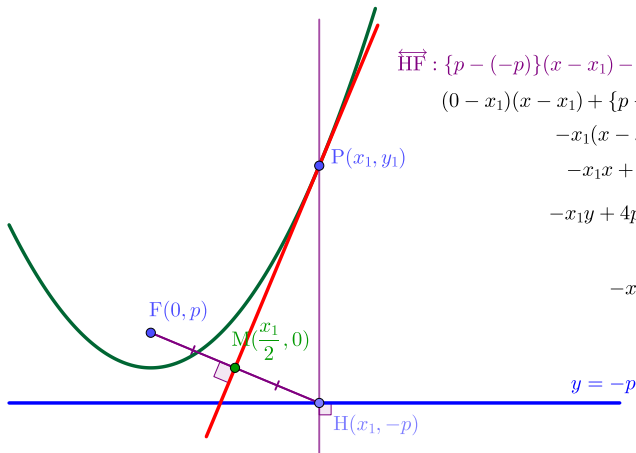
$$(\because x_1^2 = 4py_1)$$

$$-x_1x + 2py + 2py_1 = 0$$

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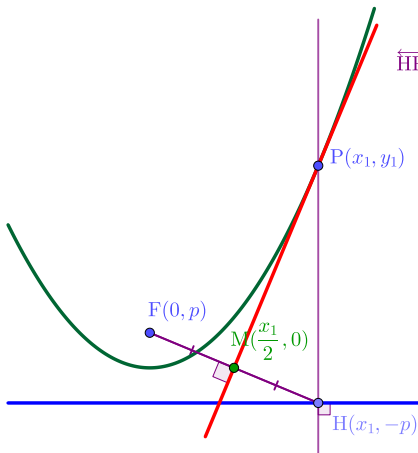
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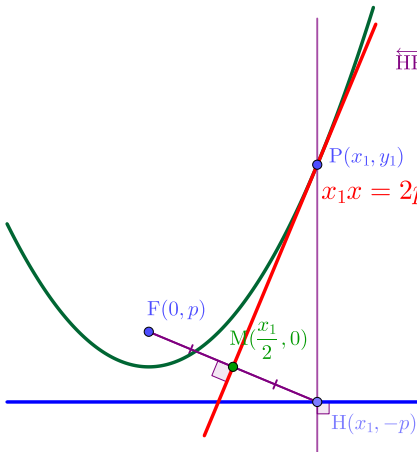
$$(\because x_1^2 = 4py_1)$$

$$-x_1x + 2py + 2py_1 = 0$$

$$2py + 2py_1 = x_1x$$

$$2p(y + y_1) = x_1x$$

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$$-x_1(x - x_1) + 2p(y - y_1) = 0$$

$$-x_1x + x_1^2 + 2py - 2py_1 = 0$$

$$-x_1y + 4py_1 + 2py - 2py_1 = 0$$

$$(\because x_1^2 = 4py_1)$$

$$-x_1x + 2py + 2py_1 = 0$$

$$2py + 2py_1 = x_1x$$

$$2p(y + y_1) = x_1x$$

$$\therefore y_1 y = 2p(x + x_1)$$

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Github:

<https://min7014.github.io/math20220320001.html>

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and you can see a picture moving.