도수분포에서의 분산 (Variance of Frequency Distribution)







x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$



x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1+f_2+f_3+\cdots+f_n$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$\begin{array}{c} \frac{if_i}{f_1} \\ \vdots \\ if_n \end{array} \qquad f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i$$

→ Start → End

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 = f_1 = f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

→ Start → End

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 = f_1 - f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance:

▶ Start ▶ End

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance : σ^2

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
$$\sigma^2 = \frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
	•	•
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
$$\sigma^2 = \frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i} = \frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i}}{x_{1}} \frac{f_{i}}{f_{1}} \frac{x_{i}f_{i}}{x_{1}f_{1}}$$

$$\vdots \quad \vdots \quad \vdots \\
x_{n} \quad f_{n} \quad x_{n}f_{n}$$

$$Variance : \sigma^{2} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2} f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2} f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2}) f_{i}$$

▶ End

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i} | f_{i} | x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = \frac{x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = \frac{x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = N$$

$$\frac{x_{i} | f_{i} | x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2} f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2} f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2}) f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i}$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
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x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i} | f_{i} | x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = \frac{x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = N$$

$$\frac{x_{i} | f_{i} | x_{i} f_{i}}{x_{1} | f_{1} | x_{i} f_{i}} = \frac{x_{i} f_{i}}{x_{n} | f_{n} | x_{n} f_{n}} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2} f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2} f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2}) f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
	•	•
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i}}{x_{1}} \frac{f_{i}}{f_{1}} \frac{x_{i}f_{i}}{x_{1}f_{1}}$$

$$\frac{x_{1}}{x_{1}} \frac{f_{1}}{f_{1}} \frac{x_{1}f_{1}}{x_{1}f_{1}}$$

$$\vdots \quad \vdots \quad \vdots \\
x_{n} \quad f_{n} \quad x_{n}f_{n}$$

$$Variance : \sigma^{2} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2} f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2} f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2}) f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_{i} f_{i}$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i}}{x_{1}} = \frac{f_{i}}{f_{1}} = \frac{x_{i}f_{i}}{x_{1}f_{1}}$$

$$\vdots \quad \vdots \quad \vdots \\ x_{n} = f_{n} = x_{n}f_{n}$$

$$Variance : \sigma^{2} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2}f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2}f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2})f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2}f_{i} - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_{i}f_{i} + m^{2}$$

x_i	f_i	$x_i f_i$
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$$f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i}}{x_{1}} \frac{f_{i}}{f_{1}} \frac{x_{i}f_{i}}{x_{1}f_{1}}$$

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x_{n} \quad f_{n} \quad x_{n}f_{n}$$

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$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_{i} f_{i} + m^{2} \times \frac{1}{N} \sum_{i=1}^{n} f_{i}$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
•	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i}}{x_{1}} \frac{f_{i}}{f_{1}} \frac{x_{i}f_{i}}{x_{1}f_{1}}$$

$$\frac{x_{1}}{x_{1}} \frac{f_{1}}{f_{1}} \frac{x_{1}f_{1}}{x_{1}f_{1}}$$

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x_{n} \quad f_{n} \quad x_{n}f_{n}$$

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$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_{i} f_{i} + m^{2} \times \frac{1}{N} \sum_{i=1}^{n} f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i}$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
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x_n	f_n	$x_n f_n$

$$f_1 = f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
$$\sigma^2$$
 = $\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1$$
 $f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$

Variance :
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 = $\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$ = $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$ = $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m$

x_i	f_i	$x_i f_i$
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$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

$$\frac{x_{i} | f_{i} | x_{i} f_{i}}{x_{1} | f_{1} | x_{1} f_{1}} \\
\vdots | \vdots | \vdots \\
x_{n} | f_{n} | x_{n} f_{n}$$

$$Variance : \sigma^{2} = \frac{\sum_{i=1}^{n} (x_{i} - m)^{2} f_{i}}{\sum_{i=1}^{n} f_{i}} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - m)^{2} f_{i} = \frac{1}{N} \sum_{i=1}^{n} (x_{i}^{2} - 2mx_{i} + m^{2}) f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_{i} f_{i} + m^{2} \times \frac{1}{N} \sum_{i=1}^{n} f_{i}$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} f_{i} - 2m \times m + m^{2}$$

x_i	f_i	$x_i f_i$
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$$f_1$$
 $f_1 + f_2 + f_3 + \cdots + f_n = \sum_{i=1}^n f_i = N$

Variance :
$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - m)^2 f_i}{\sum_{i=1}^n f_i} = \frac{1}{N} \sum_{i=1}^n (x_i - m)^2 f_i = \frac{1}{N} \sum_{i=1}^n (x_i^2 - 2mx_i + m^2) f_i$$

$$= \frac{1}{N} \sum_{i=1}^n x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^n x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^n f_i$$

$$= \frac{1}{N} \sum_{i=1}^n x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$$

x_i	f_i	$x_i f_i$
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	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
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 = $\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i$

x_i	f_i	$x_i f_i$
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:	:	:
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$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
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= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 + \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 +$

x_i	f_i	$x_i f_i$
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Variance :
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 = $\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$
= $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 + m^2$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
	•	•
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
$$\sigma^2 = \frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i} = \frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i = \frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 + m^2 = \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i$$

x_i	f_i	$x_i f_i$
x_1	f_1	x_1f_1
:	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
$$\sigma^2$$
 =
$$\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i} = \frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i = \frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$$

$$= \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 + m^2 = \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - m^2$$

x_i	f_i	$x_i f_i$
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	:	:
x_n	f_n	$x_n f_n$

$$f_1 + f_2 + f_3 + \dots + f_n = \sum_{i=1}^n f_i = N$$

Variance :
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 = $\frac{\sum_{i=1}^{n} (x_i - m)^2 f_i}{\sum_{i=1}^{n} f_i}$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i - m)^2 f_i$ = $\frac{1}{N} \sum_{i=1}^{n} (x_i^2 - 2mx_i + m^2) f_i$ = $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times \frac{1}{N} \sum_{i=1}^{n} x_i f_i + m^2 \times \frac{1}{N} \sum_{i=1}^{n} f_i$ = $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m \times m + m^2 \times \frac{1}{N} \times N$ = $\frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - 2m^2 + m^2 = \frac{1}{N} \sum_{i=1}^{n} x_i^2 f_i - m^2$

Github:

https://min7014.github.io/math20230524001.html

Click or paste URL into the URL search bar, and you can see a picture moving.