

# imaging\_ai

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```
import sys
sys.executable
```

```
'/opt/hostedtoolcache/Python/3.10.16/x64/bin/python3'
```

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title: Task 1

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## Task 1

The Fourier transformation  $f(x, y) \mapsto F(u, v)$  of a greyscale image  $f(x, y)$  results in a band-limited signal in the spatial frequency range with maximum frequencies  $f_{umax}$  and  $f_{vmax}$ . For representation in the computer, the (partial) image is sampled in x direction with 20 sampling points per mm and in y direction with 10 sampling points per mm.

1. What is the theoretical maximum value of  $f_{umax}$  and  $f_{vmax}$  if error-free image reconstruction from the digital image should be possible (not using any compressive-sensing techniques)? (6pts)

According to the Nyquist sampling theorem, the maximum representable frequency (Nyquist frequency) in each direction is half the sampling frequency. The sampling frequency can be derived from the given sampling points per mm.

- Sampling frequency in x is  $f_{sx}$  and the Nyquist frequency in x is  $f_{umax}$ :

$$f_{sx} = 20 \text{ points/mm} = 20 \times 10^3 \text{ points/m}$$
$$\Rightarrow f_{umax} = \frac{f_{sx}}{2} = 10.0 \text{ cycles/mm}$$

- Sampling frequency in y is  $f_{sy}$  and the Nyquist frequency in y is  $f_{vmax}$ :

$$f_{sy} = 10 \text{ points/mm} = 10 \times 10^3 \text{ points/m}$$

$$\Rightarrow f_{vmax} = \frac{f_{sy}}{2} = 5.0 \text{ cycles/mm}$$

This ensures error-free reconstruction, as the digital image will contain all frequency components of the original image within the Nyquist limit. Frequencies above these limits would result in aliasing, violating error-free reconstruction conditions.

What is the minimum memory requirement for the color image  $f_F(x, y)$  when stored in a conventional computer system, if 1024 values are to be distinguished per color channel. Describe the image format to be used.

To start lets find the number of ixels

Let the image dimensions in mm be  $L_x$  (width) and  $L_y$  (height).

- Pixels in  $x$ -direction:  $N_x = 10.0 \cdot L_x$  - Pixels in  $y$ -direction:  $N_y = 5.0 \cdot L_y$  - Total number of pixels:

$$N_{\text{pixels}} = N_x \cdot N_y = 50.0 \cdot L_x \cdot L_y$$

Each pixel in a color image has values for three color channels: Red, Green, and Blue (RGB). Each channel can store 1024 distinct values, which means  $\log_2^{1024} = 10.0$  bits per channel.

Total bits per pixel:  $b = 10.0 \times 3 = 30.0$  bits/pixel.

The memory requirement is the product of the number of pixels and bits per pixel:

$$\text{Used Memory} = N_{\text{pixels}} \cdot b = (50.0 \cdot L_x \cdot L_y) \cdot b \text{ bits} = 6.25 \cdot L_x \cdot L_y \cdot 30.0 \text{ bytes} = 187.5 \cdot L_x \cdot L_y \text{ bytes}$$

How many colors could be represented with the quantization chosen in sub-task 3? (2pts)

Each channel (Red, Green, and Blue) can represent 1024 intensity levels. With 10 bits per channel and 3 channels, the total number of colors is:

$$\text{Total colors} = 1024^3 = 1,073,741,824$$

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title: "task 2"

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## Task 2

For the subjective enhancement of a greyscale image  $G = g(x, y)$ , a transformation  $T_G$  is performed as a so-called gamma correction in the form  $T_G : g \rightarrow f$  with  $f(x, y) = cg^\gamma(x, y)$  where  $g, f \in [0, 255]$ .

Sketch the transformation curve  $T_G$  for  $\gamma_1 = 0.5$  and  $\gamma_2 = 2$

The first step is to find the values of  $c$  for both cases. Since  $\max(f) = \max(g) = 255$ , we have  $c = 255/255^\gamma$ .

```
from matplotlib import pyplot as plt
import numpy as np

def draw_transform_curve(gamma: float, ax: plt.Axes = None, label: bool = True):
    if not ax:
        fig, ax = plt.subplots()
    x = np.linspace(0, 255, 256)
    c = 255 / 255**gamma
    y = c * x**gamma
    message = f"$f = {c:0.4f} \times g^{{{gamma}}}$"
    if label:
        ax.plot(x, y, label=message)
    else:
        ax.plot(x, y)
    ax.set_xlabel("g")
    if label:
        ax.set_ylabel("f")
    else:
        ax.set_ylabel(message)

fig, ax = plt.subplots()
for gamma in [0.5, 2]:
    draw_transform_curve(gamma, ax)
ax.set_title(f"Transformation curve for $\gamma=0.5$ and $\gamma=2$")
ax.legend()
plt.show()
```



How is the coefficient  $c$  typically determined? (2pts)

The coefficient  $c$  is typically determined such that the maximum value of the input image is mapped to the maximum value of the output image. This is done to ensure that the full dynamic range of the output image is used.

As mentioned above,  $c = 255/255^\gamma$ .

In which respect and for which type of input images  $G$  do the two gamma values  $\gamma_1, \gamma_2$  lead to an image enhancement respectively? (2pts)

For  $\gamma < 1$ , the transformation curve is concave, which means that the lower intensity values are stretched more than the higher intensity values. This leads to a brighter image with more contrast. This is useful for images with low contrast.

For  $\gamma > 1$ , the transformation curve is convex, which means that the higher intensity values are stretched more than the lower intensity values. This leads to a darker image with more contrast. This is useful for images with high contrast.

What should be the minimum slope of the transform function?

1. for a grey value spread (2pts)
2. for a grey value compression (2pts)

It's important to note that a slope of exactly 1 implies no change in contrast, as the transformation function becomes an identity mapping. Also, a slope of 0 implies that the output image will be a constant value, which is not useful for image enhancement.

1. For a grey value spread, the minimum slope of the transform function should be 1.
2. For a grey value compression, the minimum slope of the transform function should be 0 (and smaller than 1). For instance, in this function:



As we can see, the gray values between `spread_range[0]` are stretched between `spread_range[1]` which has a slope greater than 1. On the other hand, the gray values between `compress_range[0]` are compressed between `compress_range[1]` which has a slope smaller than 1.

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title: "task 3"

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## Task 3

In this task you will need to perform threshold-based image analysis:

Read the grayscale image `brain.png`, which is provided on the lecture homepage. Reduce the salt and pepper noise in the image using a median filter. (3pts)

```

import cv2
import numpy as np
import matplotlib.pyplot as plt
import os

img_noise = cv2.imread("brain-noisy.png", cv2.IMREAD_GRAYSCALE)
if img_noise is None:
    img_noise = cv2.imread("./reports/brain-noisy.png", cv2.IMREAD_GRAYSCALE)
assert img_noise is not None, "Image not found {}".format(os.listdir())
img = cv2.medianBlur(img_noise, 5)
img = cv2.GaussianBlur(img, (5, 5), 0)

fig, ax = plt.subplots(1, 3, figsize=(15, 5))
ax[0].imshow(img_noise, cmap="gray")
ax[0].set_title("Original image")
ax[0].axis("off")
ax[1].imshow(cv2.medianBlur(img_noise, 3), cmap="gray")
ax[1].set_title("Median filtered image (3x3)")
ax[1].axis("off")
ax[2].imshow(img, cmap="gray")
ax[2].set_title("Median filtered image (5x5)")
ax[2].axis("off")

plt.show()

```

[ WARN:000.010] global loadsave.cpp:241 findDecoder imread\_('brain-noisy.png'): can't open/read image: can't open/read file: no such file or directory



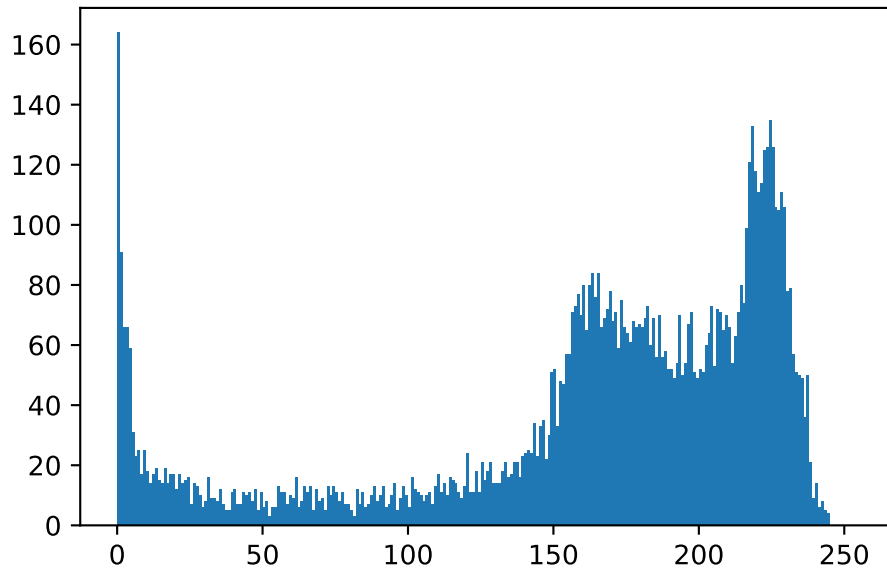
As we can see the kernel size of  $3 \times 3$  is not enough to remove the noise, while the kernel size of  $5 \times 5$  is sufficient.

**Otsu** thresholding is a histogram-based method for image segmentation. Use it to find an intensity threshold to segment brain pixels from background. Use Otsu thresholding again to find the threshold only over the brain pixels to segment brain's grey matter from the white matter. Using the two thresholds create three binary masks brain-bg.png, brain-gm.png, brain-wm.png, which should be white in regions of background, grey matter, and white matter, respectively, and black elsewhere. (4pts)

```
values, bin_edge = np.histogram(img, bins=256, range=(0, 256))
bin_centers = (bin_edge[:-1] + bin_edge[1:]) / 2
# values = values[1:]
# bin_centers = bin_centers[1:]
m = values.mean() * 2
values[values > m] = m

plt.bar(bin_centers, values, lw=2)
plt.title("Bounded histogram of the image (values capped at 2x the mean)")
plt.show()
```

Bounded histogram of the image (values capped at 2x the mean)



The correct way to use Otsu thresholding with several values is to use (Arora et al. 2008), which is not implemented in OpenCV. However, we can use the implementation in the **skimage** library (which implemented based on (Liao et al. 2001))

```

from skimage.filters import threshold_multiotsu

def otsu_threshold(
    img: np.ndarray, classes: int
) -> tuple[list[np.ndarray], np.ndarray]:
    threshold = threshold_multiotsu(img, classes=classes).tolist()
    threshold = [0] + threshold + [255]
    assert (
        len(threshold) == classes + 1
    ), "The number of thresholds should be equal to the number of classes - 1"
    masks = [(img >= t1) & (img < t2) for t1, t2 in zip(threshold, threshold[1:])]
    # masks.append(img >= threshold[-1])
    assert all(mask.dtype == bool for mask in masks), "Masks should be boolean"
    assert (
        len(masks) == classes
    ), "The number of masks should be equal to the number of classes"
    return masks, threshold[1:-1]

(brain_bg, brain_gm, brain_wm), threshold = otsu_threshold(img, 3)

```

```

colors = ["r", "g", "y"]
(brain_bg, brain_gm, brain_wm), threshold = otsu_threshold(img, 3)

print(f"Threshold for the whole image: {threshold}")

values, bin_edge = np.histogram(img, bins=256, range=(0, 256))
bin_centers = (bin_edge[:-1] + bin_edge[1:]) / 2
m = values.mean() * 2
values[values > m] = m

plt.bar(bin_centers, values, lw=2)
for th, color in zip(threshold, colors):
    plt.axvline(th, color=color, lw=2, ls="--", label=f"Threshold: {th}")
plt.legend()
plt.title("Bounded histogram of the image (values capped at 2x the mean)")
plt.show()

```

Threshold for the whole image: [77, 182]



Bounded histogram of the image (values capped at 2x the mean)



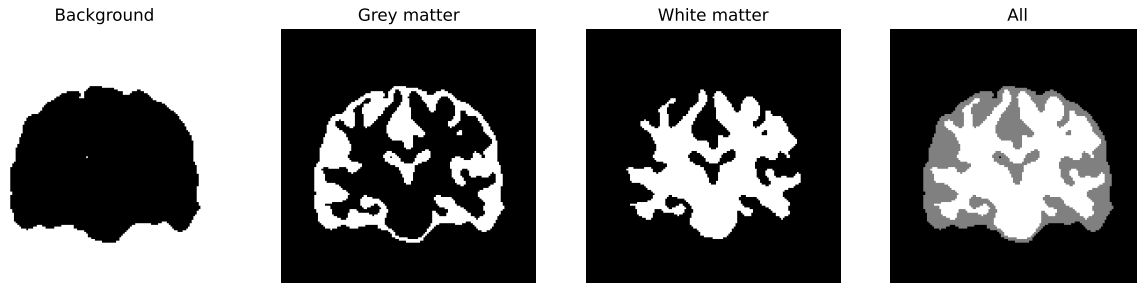
```
fig, ax = plt.subplots(1, 4, figsize=(15, 5))
ax[0].imshow(brain_bg, cmap="gray")
ax[0].set_title("Background")
ax[0].axis("off")

ax[1].imshow(brain_gm, cmap="gray")
ax[1].set_title("Grey matter")
ax[1].axis("off")

ax[2].imshow(brain_wm, cmap="gray")
ax[2].set_title("White matter")
ax[2].axis("off")

ax[3].imshow(brain_bg * 1 + brain_gm * 2 + brain_wm * 3, cmap="gray")
ax[3].set_title("All")
ax[3].axis("off")

plt.show()
```

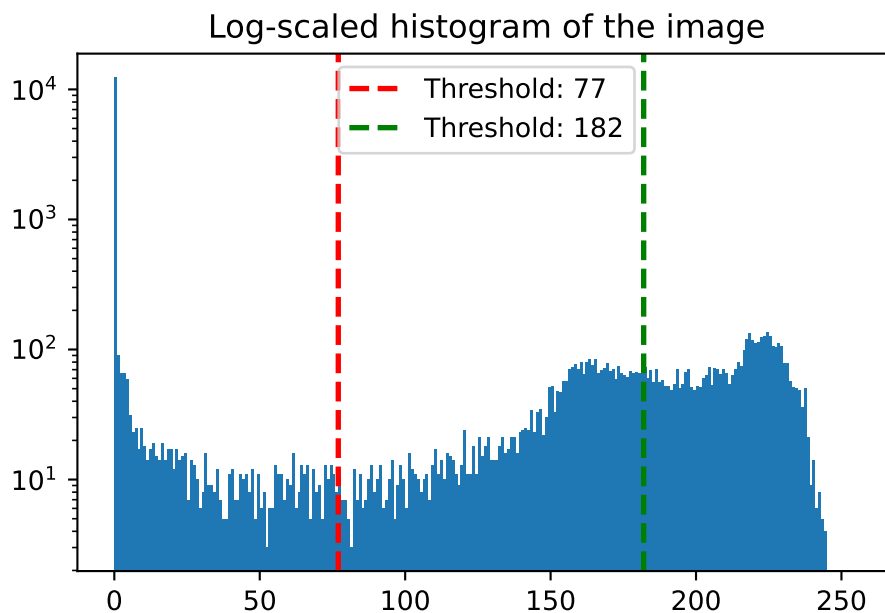


Plot a log-scaled histogram of the image, which should show how frequently different intensity values occur in the image. How could you roughly estimate the two thresholds you found in the previous task just by looking at the histogram? (3pts)

```
values, bin_edge = np.histogram(img, bins=256, range=(0, 256))
bin_centers = (bin_edge[:-1] + bin_edge[1:]) / 2
plt.bar(bin_centers, values, lw=2)
plt.yscale("log")

for th, color in zip(threshold, colors):
    plt.axvline(th, color=color, lw=2, ls="--", label=f"Threshold: {th}")

plt.legend()
plt.title("Log-scaled histogram of the image")
plt.show()
```



As we can see, the histogram has two peaks, which correspond to the grey matter and white matter. The two thresholds can be estimated by finding the two peaks in the histogram. (The purpose of otsu thresholding is to find the optimal threshold for the two peaks)

Combine the three masks into a single colour image so that background, grey matter, and white matter are mapped to red, green and blue, respectively. (3pts)

```
combined_brain = np.stack([brain_bg, brain_gm, brain_wm], axis=-1).astype(np.uint8) * 255

plt.imshow(combined_brain)
plt.axis("off")
plt.show()
```

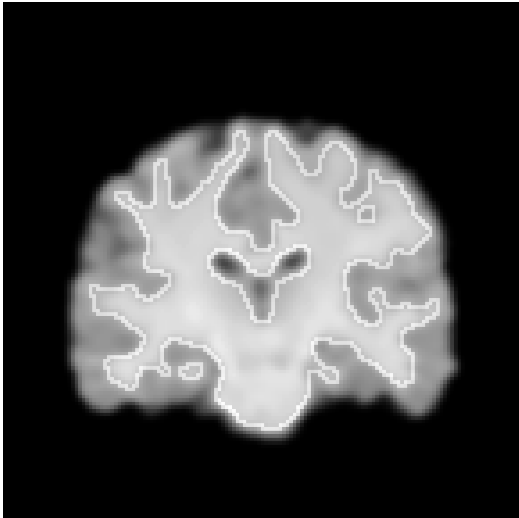


Use erosion (or any other morphological) filter to produce a border between the grey and white matter. Overlay that border on the denoised input image. (3pts)

```
kernel = np.ones((3, 3), np.uint8)
brain_wm_eroded = cv2.erode(brain_wm.astype(np.uint8), kernel, iterations=1)
brain_wm_dilated = cv2.dilate(brain_wm_eroded, kernel, iterations=1)
border = (brain_wm_dilated - brain_wm_eroded) * 255
alpha = 0.85
bordered_img = cv2.addWeighted(img, alpha, border, 1 - alpha, 0)

# plt.imshow(img, cmap="gray")
# plt.imshow(border, cmap="gray", alpha=0.5)
plt.imshow(bordered_img, cmap="gray")
```

```
plt.axis("off")
plt.show()
```



Use bilinear interpolation to up-sample the image by a factor of four along each axis. Apply the same thresholds as in 2) to obtain a segmentation into background, grey matter, and white matter. Up-sample the masks from 2) in the same way and compare the up-sampled masks to the masks from the up-sampled image. Can you see a difference? Why? Repeat the same procedure using nearest neighbour interpolation. Can you see a difference now? (4pts)

```
def upsample(img: np.ndarray, factor: int, interpolation: int) -> np.ndarray:
    return cv2.resize(
        img, (img.shape[1] * factor, img.shape[0] * factor), interpolation=interpolation
    )

masks, threshold = otsu_threshold(img, 3)
img_upsampled = upsample(img, 4, cv2.INTER_LINEAR)
masks_upsampled, threshold_upsampled = otsu_threshold(img_upsampled, 3)

fig, ax = plt.subplots(2, 4, figsize=(15, 10))
fig.suptitle(
    "Comparison of upsampled masks and upsampled image using linear interpolation",
    fontsize=16,
)

titles = ["Background", "Grey matter", "White matter", "All"]
```

```

masks.append(masks[0] * 1 + masks[1] * 2 + masks[2] * 3)
masks_upsampled.append(
    masks_upsampled[0] * 1 + masks_upsampled[1] * 2 + masks_upsampled[2] * 3
)

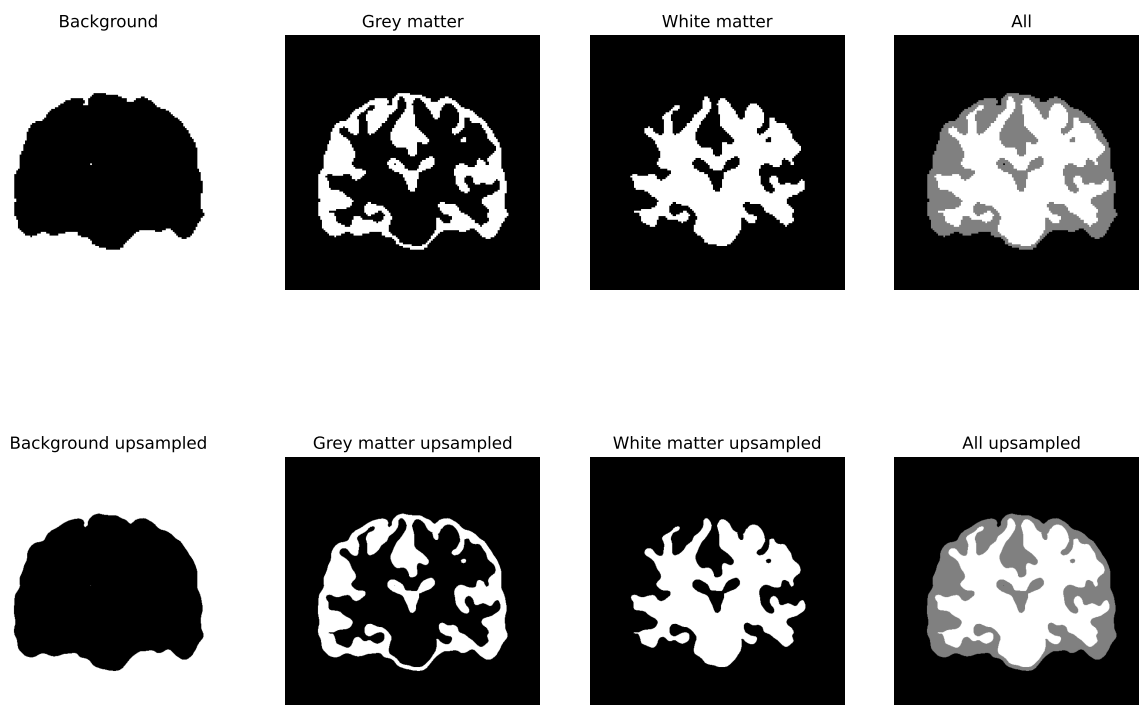
for i, (mask, mask_upsampled, title) in enumerate(zip(masks, masks_upsampled, titles)):
    ax[0, i].imshow(mask, cmap="gray")
    ax[0, i].set_title(title)
    ax[0, i].axis("off")

    ax[1, i].imshow(mask_upsampled, cmap="gray")
    ax[1, i].set_title(f"{title} upsampled")
    ax[1, i].axis("off")

plt.show()

```

Comparison of upsampled masks and upsampled image using linear interpolation



Clearly, we can see much smoother edges in the upsampled masks compared to the upsampled image. This is because the interpolation method used in the up-sampling process is linear,

which smooths the edges.

Now, let's repeat the same procedure using the nearest neighbour interpolation method.

```

masks, threshold = otsu_threshold(img, 3)
img_upsampled = upsample(img, 4, cv2.INTER_NEAREST)
masks_upsampled, threshold_upsampled = otsu_threshold(img_upsampled, 3)

fig, ax = plt.subplots(2, 4, figsize=(15, 10))
fig.suptitle(
    "Comparison of upsampled masks and upsampled image using nearest neighbour interpolation",
    fontsize=16,
)

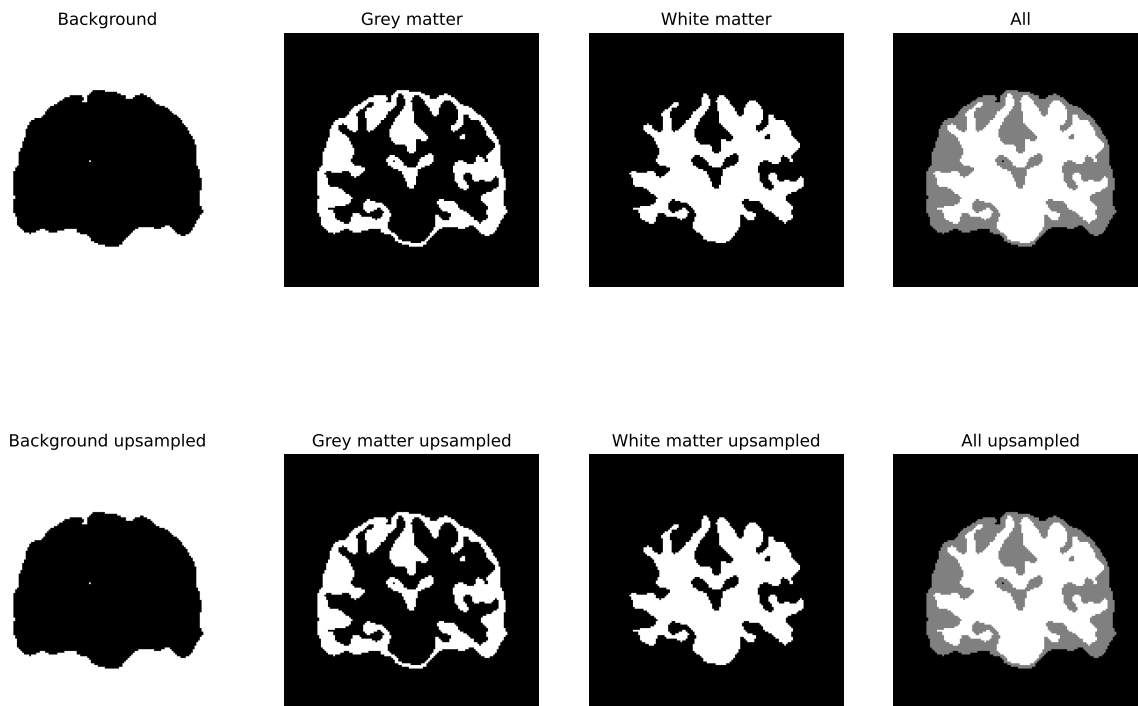
titles = ["Background", "Grey matter", "White matter", "All"]
masks.append(masks[0] * 1 + masks[1] * 2 + masks[2] * 3)
masks_upsampled.append(
    masks_upsampled[0] * 1 + masks_upsampled[1] * 2 + masks_upsampled[2] * 3
)

for i, (mask, mask_upsampled, title) in enumerate(zip(masks, masks_upsampled, titles)):
    ax[0, i].imshow(mask, cmap="gray")
    ax[0, i].set_title(title)
    ax[0, i].axis("off")

    ax[1, i].imshow(mask_upsampled, cmap="gray")
    ax[1, i].set_title(f"{title} upsampled")
    ax[1, i].axis("off")

plt.show()
```

### Comparison of upsampled masks and upsampled image using nearest neighbour interpolation



We can see the edges are much sharper in the upsampled masks compared to the upsampled image. This is because the nearest neighbour interpolation method does not smooth the edges.

TODO: Test same thing with pyrUp

```
def upsample_pyramid_(img: np.ndarray) -> np.ndarray:
    # return cv2.resize(
    #     img, (img.shape[1] * factor, img.shape[0] * factor), interpolation=interpolation
    # )
    return cv2.pyrUp(img, dstsize=(img.shape[1] * 2, img.shape[0] * 2))

def upsample_pyramid(img: np.ndarray, factor: int) -> np.ndarray:
    if factor <= 1:
        raise ValueError("Factor should be greater than 1")
    f = 1
    while f < factor:
        img = upsample_pyramid_(img)
        f *= 2
```

```

return img

print(img.shape)
img_upsampled = upsample_pyramid(img, 4)
print(img_upsampled.shape)
fig, ax = plt.subplots(1, 2, figsize=(10, 5))
ax[0].imshow(img_upsampled, cmap="gray")
ax[0].set_title("Upsampled image")
ax[0].axis("off")

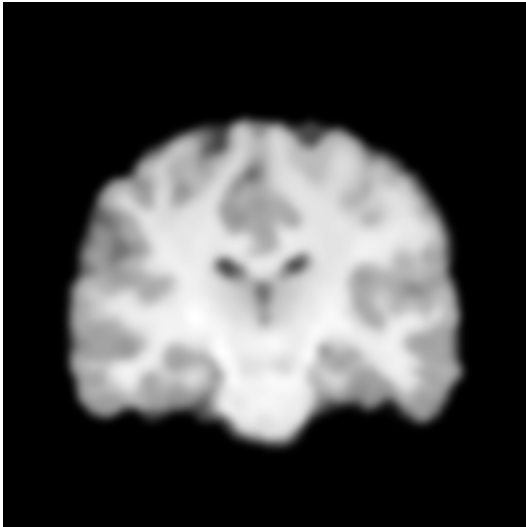
ax[1].imshow(img, cmap="gray")
ax[1].set_title("Original image")
ax[1].axis("off")

plt.show()

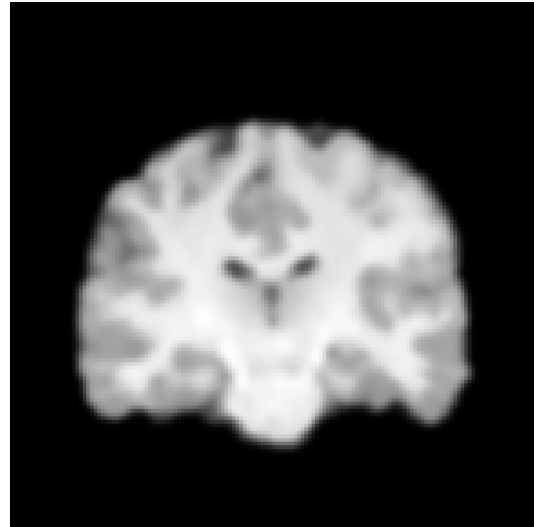
```

(145, 145)  
(580, 580)

Upsampled image



Original image




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title: "Task 4"

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## Task 4

### Data Handling and Preprocessing (10 Points)

- You can focus for now on loading the T1-weighted images and the matching labels.
- Create a dataloader for the data using PyTorch's Dataloader (or Monai's Dataloader class)
- Create suitable augmentations for the task to solve. Please note: If you apply transformations to the input data, you should think about if you need to apply any transformation to the label of the image as well.

We didnt used Monai's Dataloader class, because we wanted to use the data in the HPC. The dataset implementation is availabel in the `task4/brats_segmentations/dataloader.py`

file name: `task4/brats_segmentation/dataloader.py`

```
class RobustZScoreNormalization(MapTransform):
    """
    Apply robust Z-score normalization to the image volumes.
    """
    def __call__(self, data):
        d = dict(data)
        for key in self.key_iterator(d):
            mask = d[key] > 0 # Only normalize within the brain mask

            lower = np.percentile(d[key][mask], 0.2)
            upper = np.percentile(d[key][mask], 99.8)

            d[key][mask & (d[key] < lower)] = lower
            d[key][mask & (d[key] > upper)] = upper

            y = d[key][mask]
            d[key] -= y.mean()
            d[key] /= y.std()

        return d

# Custom transform to remap labels
class RemapLabels(MapTransform):
    """
    Remap labels to sequential class indices.
```

```

Original labels: 0, 1, 2, 4
Remapped labels: 0, 1, 2, 3
"""
def __call__(self, data):
    d = dict(data)
    label = d["label"]
    label[label == 4] = 3 # Map class 4 to 3
    d["label"] = label.long()
    return d

# Preprocessing and augmentation
def get_transforms(roi_size, augment=True):
    """
    Generate transformation pipelines for training, validation, and testing.

    Args:
        roi_size (tuple): Size of the region of interest for cropping.
        augment (bool): Whether to apply augmentations (True for training).

    Returns:
        Compose: Transformation pipeline.
    """
    transforms_list = [
        # Load and standardize image and label data
        LoadImaged(keys=["t1", "t1ce", "t2", "flair", "label"]),
        EnsureChannelFirstd(keys=["t1", "t1ce", "t2", "flair", "label"]),
        ConcatItemsd(keys=["t1", "t1ce", "t2", "flair"], name="image"),
        Orientationd(keys=["image", "label"], axcodes="RAS"),
        Spacingd(keys=["image", "label"], pixdim=(1.0, 1.0, 1.0), mode=("bilinear", "nearest")),
        RobustZScoreNormalization(keys=["image"]), # Apply robust Z-score normalization
        RemapLabels(keys=["label"]), # Add label remapping
    ]

    if augment:
        # Augmentations for training data
        transforms_list.extend([
            RandSpatialCropSamplesd(
                keys=["image", "label"],
                roi_size=roi_size,
                random_center=True,
                random_size=False,

```

```

        num_samples=2 # Multiple crops per image
    ),
    RandFlipd(keys=["image", "label"], prob=0.5, spatial_axis=0),
    RandFlipd(keys=["image", "label"], prob=0.5, spatial_axis=1),
    RandFlipd(keys=["image", "label"], prob=0.5, spatial_axis=2),
    RandRotate90d(keys=["image", "label"], prob=0.5, max_k=3),
    RandGaussianNoised(keys=["image"], prob=0.2, mean=0.0, std=0.1),
    RandScaleIntensityd(keys=["image"], factors=0.1, prob=1.0),
    RandShiftIntensityd(keys=["image"], offsets=0.1, prob=1.0),
])

# Add tensor conversion
transforms_list.append(ToTensord(keys=["image", "label"]))

return Compose(transforms_list)

# DataLoader setup
def get_dataloaders(split_dir, roi_size, batch_size, num_workers=4):
    """
    Create data loaders for training, validation, and testing.

    Args:
        split_dir (str): Path to the directory containing split JSON files.
        roi_size (tuple): Size of the region of interest for cropping.
        batch_size (int): Batch size for data loaders.
        num_workers (int): Number of workers for data loading.

    Returns:
        tuple: Training, validation, and test DataLoaders.
    """
    # Generate transforms for train and validation/test
    train_transform = get_transforms(roi_size, augment=True)
    val_transform = get_transforms(roi_size, augment=False)

    # Load dataset splits
    with open(f"{split_dir}/train.txt", "r") as f:
        train_files = json.load(f)
    with open(f"{split_dir}/validation.txt", "r") as f:
        val_files = json.load(f)
    with open(f"{split_dir}/test.txt", "r") as f:
        test_files = json.load(f)

```

```

# Create datasets
train_ds = Dataset(data=train_files, transform=train_transform)
val_ds = Dataset(data=val_files, transform=val_transform)
test_ds = Dataset(data=test_files, transform=val_transform)

# Create data loaders
train_loader = DataLoader(train_ds, batch_size=batch_size, shuffle=True, num_workers=num_wor
val_loader = DataLoader(val_ds, batch_size=batch_size, shuffle=False, num_workers=num_wor
test_loader = DataLoader(test_ds, batch_size=batch_size, shuffle=False, num_workers=num_wor

return train_loader, val_loader, test_loader

if __name__ == "__main__":
    # Example usage
    split_dir = "./splits/split1"
    roi_size = (128, 128, 128)
    batch_size = 2
    num_workers = 4

    train_loader, val_loader, test_loader = get_dataloaders(split_dir, roi_size, batch_size,

# Inspect one batch from the training DataLoader
print("Testing the training DataLoader...")
for batch in train_loader:
    print(f"Image shape: {batch['image'].shape}")
    print(f"Label shape: {batch['label'].shape}")
    print(f"Label unique values: {torch.unique(batch['label'])}")
    break

```

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