

Q1. Given a char[] s, calculate no. of pairs  $[i, j]$ , such that  $i < j$  &  $s[i] == 'a'$ , &  $s[j] == 'g'$ , all characters are lowercase alphabets  $[a, b, c, d, \dots]$

ex  $\Rightarrow$  arr  $\Rightarrow$  b a a g d c a g  
 0 1 2 3 4 5 6 7

valid pairs  $\leftarrow$   $\langle 1, 3 \rangle$   $\langle 2, 3 \rangle$   $\langle 6, 7 \rangle$   
 $\langle 1, 7 \rangle$   $\langle 2, 7 \rangle$   
 ~~$\langle 3, 6 \rangle$~~   ~~$\langle 6, 3 \rangle \rightarrow i < j$~~

$Q_p = 5$

ex  $\Rightarrow$  arr  $\Rightarrow$  b c a g g a a g  
 0 1 2 3 4 5 6 7  
 $Q_p = 5$

ex  $\Rightarrow$  arr  $\Rightarrow$  a c g d g a g  
 0 1 2 3 4 5 6  
 $Q_p = 4$

Brute force

check all possible pairs of  
(i, j).

```
c = 0
for (i = 0; i < N; i++) {
    for (j = i + 1; j < N; j++) {
        if (s[i] == 'a' && s[j] == 'g')
            c++;
    }
}
print(c)
```

TC  $\Rightarrow O(N^2)$

SC  $\Rightarrow O(1)$

\* if  $s[i] \neq 'a'$ , then second loop is not required.

```
for (i = 0; i < N; i++) {
    if (s[i] == 'a') {
        for (j = i + 1; j < N; j++) {
            if (s[j] == 'g')
                c++;
        }
    }
}
print(c)
```

Still

TC  $\Rightarrow O(N^2)$

SC  $\Rightarrow O(1)$

work  
card

↓ ↓ ↓  
a a a a a a a a

→  
→

ex ⇒

0 1 2 3 4 5 6 7 8  
a d g a g a g f g

$i=0$  →  $\text{count}(g) = 4$

$i=3$  → 3

$i=5$  → 2

$Qp = 9$

⇒ what is redundant?

$4 + 3 + 2 = 9$

Counting of g is redundant

Carry forward  
technique

a d g a g a g f g

X  $c_{g++}$   $c_{g++}$   $c_{g++}$   $c_{g++}$

$ans = ans + c_g = 9$   
 $c_g = 4$

$Qp = 9$

$TC \Rightarrow O(N)$   
 $SC \Rightarrow O(1)$

pseudo

ans = 0, cg = 0.

```
for (i = N-1; i >= 0; i--) {  
    if (arr[i] == 'g') {  
        cg++;  
    }  
    else if (arr[i] == 'a') {  
        ans = ans + cg;  
    }  
}  
print(ans)
```

TC  $\Rightarrow O(N)$

SC  $\Rightarrow O(1)$

idea 2

For every 'g' calculate no. of 'a' on the  
(left - right) side :-

what to carry :-

1) ans

2) count of a (Ca)

→ left to right

How  $\rightarrow$  pseudocode 

Q2. leaders in an array:

Given an  $arr[N]$ , you have to find all leaders in  $arr[]$ .  
An element is a leader, if it is strictly greater than  
all its elements on the right side.

: Note:  $[N-1]$  is always a leader.

ex  $\Rightarrow arr[] \Rightarrow$  15 -1 7 2 5 4 2 3  
                          ✓ ✗ ✓ ✗ ✓ ✓ ✗ ✓

$Op = 5.$

$arr[] \Rightarrow$  10 7 9 3 2 4 5  
                  ✓ ✗ ✓ ✗ ✗ ✗ ✓

$Op = 3.$

$arr[] \Rightarrow$  8 -2 4 7 6 5 1  
                  ✓ ✗ ✗ ✓ ✓ ✓ ✓

$Op = 5.$

$arr[] \Rightarrow$  10 8 8  
                  ✓ ✗ ✓

$Op = 2.$

Brute force

take each element, and compare  
to all elements toward right, and  
check if it's leader

$$TC \Rightarrow O(N^2) \quad SC \Rightarrow O(1)$$

pseudo  $\rightarrow$  How

Optimised

10 7 9 3 2 4 5

$9 > 5 \rightarrow 9$  is a leader

$3 < 5 \rightarrow 3$  is not a leader.

for any idx  $i$ , need to know the max from  $(i+1$  to  $N-1)$

if ( $arr[i] > max$ )

C++

$\downarrow$						
10	7	9	3	2	4	5
0	1	2	3	4	5	6

count = 1 2 3  $\rightarrow$  3  
 $max = 5$  9 10

pseudo

$c = 1, \text{max} = \text{arr}[N-1]$

for ( $i = N-2; i \geq 0; i--$ ) {

if ( $\text{arr}[i] > \text{max}$ ) {

$c++$ ,

$\text{max} = \text{arr}[i]$

}

}

print(c)

TC  $\Rightarrow O(N)$

SC  $\Rightarrow O(1)$

$\Rightarrow$  Subarrays :

Basics  $\rightarrow$

1) continuous part of an array is called subarray

1) a single element is a subarray

eg  $\Rightarrow \text{arr}[1] = [1 \ 4 \ 3 \ 2 \ 5]$

$[4], [3], [2]$  - - subarrays

2) entire array is also a subarray

eg  $\Rightarrow \text{arr}[1] = [1 \ 4 \ 3]$

$\uparrow$   
also a subarray.

3) empty[] can't be a subarray.

ex) arr[]  $\Rightarrow$ 

-3	4	6	2	8	7	14	9	21
0	1	2	3	4	5	6	7	8

$\Rightarrow$  pda  $\Rightarrow$  [2 3 4 5]  $\checkmark$   $\Rightarrow$  [2-5]

$\Rightarrow$  ida  $\Rightarrow$  [3 4 6 7 8]  $\times$   $\rightarrow$  5 is skipped

$\Rightarrow$  ida  $\Rightarrow$  [1-3]  $\checkmark$

$\Rightarrow$  ida  $\Rightarrow$  [4]  $\checkmark$

$\Rightarrow$  pda  $\Rightarrow$  [5-8]  $\checkmark$

[ ]  $\rightarrow$   $\times \times \times$ .

subarray  $\Rightarrow$  [3-7]  $\Rightarrow$ 

3	4	5	6	7
$\underbrace{\hspace{1.5cm}}$				

 $\rightarrow$  5 elements  
 $\downarrow$   
 $\underbrace{7-3+1}_{5} \Rightarrow$  elements.

subarray  $\Rightarrow$  [s-e]  $\Rightarrow$  length =  $e-s+1$   
 $\underbrace{\hspace{1.5cm}}$



⇒ usage of predefined func:-

⇒  $\min(a, b) \rightarrow$  returns the  $\min$  of  $a$  &  $b$ .  
TC  $\Rightarrow O(1)$

⇒  $\max(a, b) \rightarrow$  returns the  $\max$  of  $a$  &  $b$ .  
TC  $\Rightarrow O(1)$

⇒  $\text{sort}(arr) \rightarrow$  arranges the array into asc order  
by default;  
TC  $\Rightarrow O(N \log N)$

⇒ always consider TC of predefined func in  
overall TC.  
Σ

→ find the  $\min$  no. of an array:-

$\min^u = arr[0]$

for ( $i=0$ ;  $i < N$ ;  $i++$ ) {

$\min^u = \min(arr[i], \min^u)$

}

}

```
if (arr[i] < min) {  
    min = arr[i];  
}
```

### Q 3. Closest Min Max

Given an array find the length of smallest subarray which contains both min & max of array?

ex  $\Rightarrow$  arr  $\Rightarrow$  1 2 3 1 3 4 6 4 6 3  
0 1 2 3 4 5 6 7 8 9

min = 1, max = 6.

idx  $\Rightarrow$  [0 8] = 9.

[3 8] = 6.

[3 6] = 4  $\rightarrow$  shortest  $\Rightarrow$  4

ex  $\Rightarrow$  arr  $\Rightarrow$  2 2 6 4 5 1 5 2 6 4 1  
0 1 2 3 4 5 6 7 8 9 10

min = 1

max = 6

idx [1 7]  $\Rightarrow$  7

[2 5]  $\Rightarrow$  4

[8 10]  $\Rightarrow$  (3)  $\rightarrow$  3

ex  $\Rightarrow$  arr[] = 8 8 8 8 8 8 8

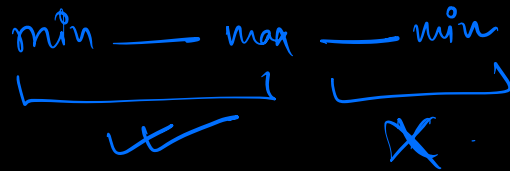
min = 8

max = 8

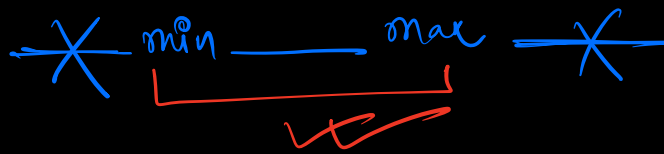
Qp = 1.

## Observations

- i) Our final shortest subarray, can only contain 1 min & 1 max



- ii) min & max should always be at boundaries.



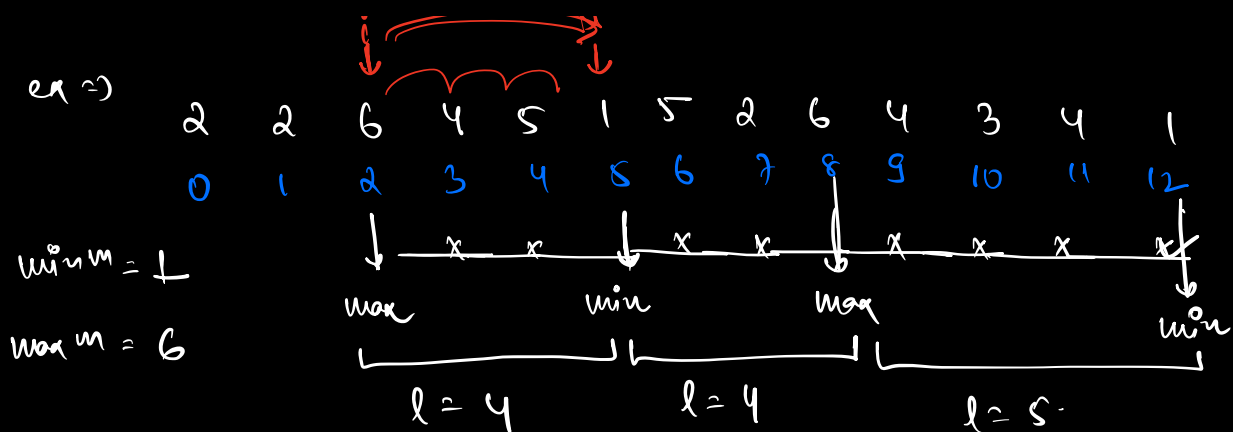
- iii) from pt 1 & pt 2, there are only 2 possibilities:

Case 1 → [min — max]

if standing at min, find the nearest max on right side.

Case 2 → [max — min]

if standing at max, find the nearest min on right side.



Qp  $\Rightarrow$   $\min len = 4$

pseudo

ans = N.

iterate and get  $\max m \rightarrow \max$

iterate and get  $\min m \rightarrow \min$

for ( $i = 0; i < N; i++$ ) {

if ( $arr[i] == \min$ ) { // find nearest max

for ( $j = i+1; j < N; j++$ ) {

if ( $arr[j] == \max$ ) {

ans =  $\min(ans, j - i + 1)$ .

break

}

}

}

else if ( $arr[i] == \max$ ) { // find nearest min

for ( $j = i+1; j < N; j++$ ) {

if ( $arr[j] == \min$ ) {

ans =  $\min(ans, j - i + 1)$ .

}  
 }  
 } break

TC  $\Rightarrow O(N^2)$   
 SC  $\Rightarrow O(1)$

arr  $\Rightarrow$

8 3 8 7 3 1 2 8  
 0 1 2 3 4 5 6 7

min = 1

max = 8

max  
 ↓

break  $\leftarrow$  i

break and start  
 again to find min, i = 2

update before  
 pseudo code with this  
code

$\Rightarrow$  if starting from max to find min.

and we encounter a max  $\rightarrow$  break & start  
 again from  
 new max

$\Rightarrow$  if starting from min to find max

and we encounter a min  $\rightarrow$  break & start  
 again from  
 new min

TC  $\Rightarrow O(N^2) \rightarrow$  How TC  $\Rightarrow O(N)$

$\rightarrow$  first next class

min = 1, max = 6.

ans = N  
minL = -1  
maxL = -1

ex  $\Rightarrow$   $\downarrow$

	0	1	2	3	4	5	6	7	8	9	10	11	12
	1	6	4	6	5	1	5	2	6	4	4	2	1
			X		X		X	X		X	X	X	
minL = 0													
maxL = 1													
L = 2													
ans = 2													
		maxL = 1 minL = 5 L = 5 ans = 3		maxL = 3 minL = 5 L = 3 ans = 3		minL = 5 maxL = 8 L = 4, ans = 4		minL = 12 maxL = 8 L = 5, ans = 5					minL = 12 maxL = -1

$\rightarrow$  Qp = 2

TC  $\Rightarrow O(N)$   
SC  $\Rightarrow O(1)$

pseudo

1) iterate  $\rightarrow$  get min & max  
if (min == max)  
return L

11) ans = N  
minL = -1  
maxL = -1

for (i = N-1; i >= 0; i--) {  
if (arr[i] == min) {

if (minL != -1  
& maxL != -1

minL = i  $\rightarrow$  abs.  
L = (maxL - minL) + 1

```

        ans = min(ans, l)
    }
    else if ( arr[i] == max ) {
        max = i
        l = (max - min) + 1
        ans = min(ans, l)
    }
}
print(ans)

```

*if (min != -1  
 & max != -1*

*also.*

```

max = arr[0], c = 0;
for ( i = 0; i < N; i++ ) {
    if ( arr[i] == max )
        c++;
    else if ( arr[i] < max ) {
        max = arr[i]
        c = 1
    }
}
}

```