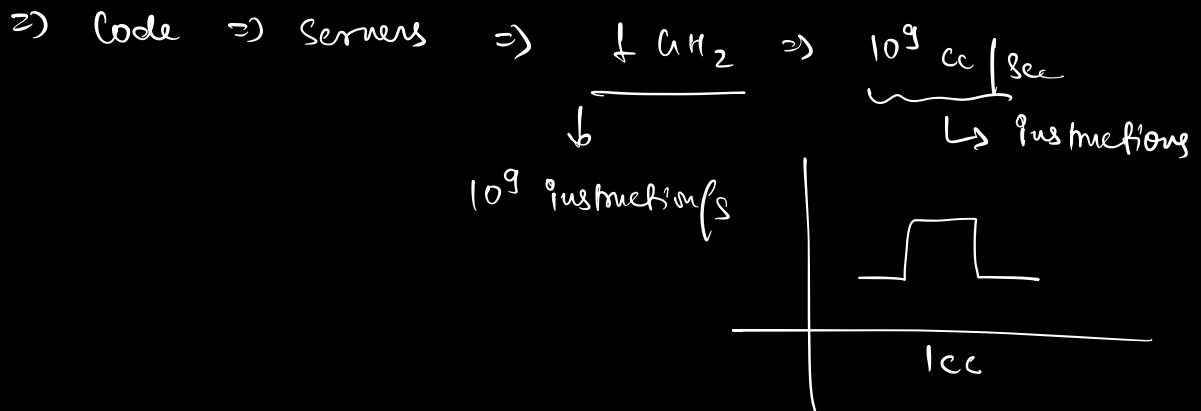


TLE :- Time Limit exceeded.

: Why TLE occurs?



: In general, Time Limit in online service \Rightarrow 1 sec

Time \Rightarrow 1 sec

Speed \Rightarrow 10^9

instructions
allowed to
compute \Rightarrow 10^9 (max).

ex \Rightarrow

```
for (i=0; i<N; i++) {  
    if (i%2 == 0)  
        print(even)  
    else  
        print(odd)  
}
```

: iterations \rightarrow N.

: instructions
per iteration
 \rightarrow 5

: total no. of
instructions \Rightarrow 5N

ex \Rightarrow ①

1 iteration \Rightarrow 10 instructions

\Rightarrow max^m instructions allowed \Rightarrow 10^9

\Rightarrow " iteration \Rightarrow $\frac{10^9}{10} \Rightarrow$ 10^8 iterations

②

1 iteration \Rightarrow 100 instructions

\Rightarrow max^m instructions $\Rightarrow 10^9$

\Rightarrow max^m iterations $\Rightarrow \frac{10^9}{100} \Rightarrow$ 10^7

In general, 1 iteration should have [10-100] instructions.
 \Rightarrow max^m instructions $\Rightarrow 10^9$

So, we can have $[10^7 - 10^8]$ iterations
 $\leftarrow \hspace{10em} \rightarrow$

\Rightarrow every question, has a constraint :-

\downarrow
defined range of
input values.

Q. Given array $[N]$, calculate no. of eqm indices.

Constraints: $1 \leq N \leq 10^5$

$1 \leq arr[i] \leq 10^9$

Sol-1

a) Brute force soln with nested loops.

TC $\Rightarrow O(N^2)$

↓

at max iteration $\Rightarrow N = 10^5 \Rightarrow (N)^2 \Rightarrow 10^{10}$
(X)

b) \Rightarrow constraint $\Rightarrow 1 \leq N \leq 10^3$.

at max iterations $\Rightarrow N^2$

$\Rightarrow (10^3)^2 \Rightarrow 10^6$ (✓)

Sol-2

Solved using a loop & Pf-sum

TC $\Rightarrow O(N)$

At max $\Rightarrow N \Rightarrow 10^5$ (✓)
iteration

eg. 1

constraints \Rightarrow

$$1 \leq N \leq 10^3$$

$$1 \leq arr[i] \leq 10^7$$

Solⁿ 1 $\Rightarrow O(N^3) \Rightarrow$ max^m iteration $\Rightarrow (10^3)^3 \Rightarrow 10^9$ (xx)

Solⁿ 2 $\Rightarrow O(N^2) \Rightarrow$ max^m iteration $\Rightarrow (10^3)^2 \Rightarrow 10^6$ (✓)

↓

$$O(\log N)$$

↓

$$\underline{\underline{O(N)}}$$

∴ TRICK

i) Read Question

ii) Read constraints

iii) Come up with a logic

\rightarrow Solⁿ \rightarrow check TC & max^m iteration

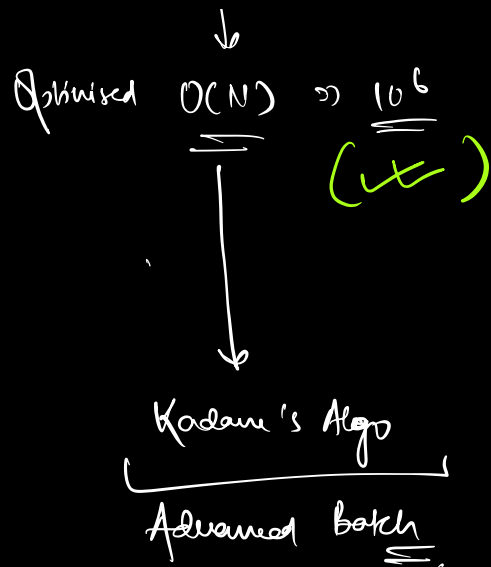
↓

decide to code

or not

∴ Max^m Subarray Sum

constraints $\Rightarrow 1 \leq N \leq 10^6 \Rightarrow O(N^2) \Rightarrow (10^6)^2 \Rightarrow \underline{\underline{10^{12}}}$
| (xxx)



Q1. Given arr[12], print start & end index of all subarrays of size 'k'.

ex \Rightarrow arr[12] \Rightarrow 3 4 2 -1 6 7 8 9 3 2 -1 4
 0 1 2 3 4 5 6 7 8 9 10 11
 └──────────┘
 k=3.

OP

[0 2]

[1 3]

[2 4]

[3 5]

[4 6]

[5 7]

[6 8]

[7 9]

k=6

[0 5]

[1 6]

[2 7]

[3 8]

[4 9]

[5 10]

[6 11]

[s e] \Rightarrow e-s+1.

[0 e] \Rightarrow k

\Rightarrow e \Rightarrow k-1

k = e - 0 + 1

\Rightarrow e = k-1

[8 10]
[9 11]

Generalise

subarray of size k .

[0 $k-1$]

[1 k]

[2 $k+1$]

[3 $k+2$]

[4 $k+3$]

⋮
}

[$N-k$ $N-1$] \rightarrow last subarray.

[S $N-1$] $\Rightarrow k$

$$\Rightarrow (N-1) - S + 1 = k$$

$$\Rightarrow S = N - 1 + 1 - k$$

$$\Rightarrow S = \underline{\underline{N - k}}$$

pseudo

$S = 0, e = k-1$

while ($e \leq (N-1)$) {

 print (S, e)

$S++$

$e++$

}

||

$S = 0, e = k-1$

while ($S \leq (N-k)$) {

 print (S, e)

$S++$

$e++$

}

$$TC \Rightarrow O(N-k)$$

$$SC \Rightarrow O(1)$$

\Rightarrow How many subarrays are there with $len = k$?

$$s \Rightarrow [0, N-k]$$

$$\text{no. of } \Rightarrow N-k-0+1$$

$$\text{subarrays} \Rightarrow \underline{\underline{[N-k+1]}}$$

Q2. Given $arr[N]$, find max subarray sum of $len = k$.

$$arr[10] \Rightarrow \begin{array}{cccccccccccc} -3 & 4 & -2 & 5 & 3 & -2 & 8 & 2 & -1 & 4 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{array}$$

$$k = 5$$

s	e	→ sum
0	4	7
1	5	8
2	6	12
3	7	16
4	8	10
5	9	11

$$Op = \underline{\underline{16}}$$

Soln 1.

for every subarray of size 'k', find its sum and maintain overall.

pseudo

msum = INT_MIN

s = 0

e = k-1

while (e <= (N-1)) {

sum = 0

for (i = s; i <= e; i++) {

sum = sum + arr[i]

}

msum = max (msum, sum)

s++;

e++;

}

TC $\Rightarrow O((N-k+1) * k)$

$\Rightarrow O((N-k) * k)$

SC $\Rightarrow O(1)$

for what value of k
we can get worst possible
TC.

k = 1

TC $\Rightarrow O((N-1) * 1)$

$\Rightarrow O(N)$

$$k = N \Rightarrow TC \Rightarrow O((N - N + 1) * N)$$

$$\Rightarrow \underline{\underline{O(N)}}$$

$$k = N/2 \quad TC \Rightarrow O((N - N/2) * (N/2))$$

$$\Rightarrow O\left(\frac{N^2}{4}\right)$$

$$\Rightarrow \underline{\underline{O(N^2)}}$$

$$\text{Worst case is } k = N/2$$

$$TC \Rightarrow \underline{\underline{O(N^2)}}$$

Soln - 2

Optimised Soln using \rightarrow pfsum

$$\text{Subarray } [s \ e] \Rightarrow \text{sum}(s \ e).$$

pseudo

1) Create pfsum Array

2) $s = 0$, $e = k - 1$, $minsum = \text{INT_MIN}$.

while ($e < N$) {

sum = [pfsum queries]

$$maxSum = \max(maxSum, sum)$$

}

$$TC \Rightarrow O(N + N - k + 1)$$

$$\Rightarrow O(2N - k)$$

$$\Rightarrow \underline{\underline{O(N - k)}}$$

Worst
case

$$k = \underline{\underline{1}}$$

$$TC \Rightarrow O(N + N - 1 + 1)$$

$$\Rightarrow O(2N)$$

$$\Rightarrow \underline{\underline{O(N)}}$$

$$SC \Rightarrow \underline{\underline{O(N)}}$$

eg

$$arr[10] \Rightarrow \begin{array}{cccccccccccc} -3 & 4 & -2 & 5 & 3 & -2 & 8 & 2 & 1 & 4 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{array}$$

$$k = \underline{\underline{6}}$$

$$[0 \ 8] \Rightarrow 5$$

pink - red + green = yellow

$$[1 \ 6] \Rightarrow 5 - arr[0] + arr[6] = 5 - (-3) + 8 = 16$$

$$[2 \ 7] \Rightarrow 16 - \text{arr}[1] + \text{arr}[7] = 16 - 4 + 2 = 14.$$

$$[3 \ 8] \Rightarrow 14 - \text{arr}[2] + \text{arr}[8] = 14 - (-2) + 1 = 17.$$

$$[4 \ 9] \Rightarrow 17 - \text{arr}[3] + \text{arr}[9] \Rightarrow 17 - 5 + 4 = \underline{16}.$$

: Sliding Window Technique

general

N, \underline{k}

1st sub $[0 \ k-1] \Rightarrow$ iterate from $\Rightarrow \underline{\text{sum}}$
 $[0 \ k-1]$

2nd sub $[1 \ k] \Rightarrow \text{sum} = \text{sum} - \text{arr}[0] + \text{arr}[k]$

3rd sub $[2 \ k+1] \Rightarrow \text{sum} = \text{sum} - \text{arr}[1] + \text{arr}[k+1]$

4th sub $[3 \ k+2] \Rightarrow \text{sum} = \text{sum} - \text{arr}[2] + \text{arr}[k+2]$

⋮

get max sum

pseudo

msum = INF - MIN.

sum = 0

for (i = 0; i <= (k-1); i++) {

sum = sum + arr[i]

}

msum = max(msum, sum);

S = 1

e = k

while (e < N) {

sum = sum - arr[S-1] + arr[e]

msum = max(msum, sum)

S++

e++

}

total iterate $\Rightarrow k + (N-k) \Rightarrow \underline{\underline{N}}$

TC $\Rightarrow O(N)$

SC $\Rightarrow O(1)$

Q4. Spiral Order Matrix

Given a no. N , create a 2D matrix of size $N \times N$, containing nos. from 1 to N^2 in spiral order.

$$N = 4,$$

1 to 4^2

1 to 16

1	2	3	4
12	13	14	5
11	16	15	6
10	9	8	7

$$D = 0, 1, 2, 3,$$

$$T = 0 \quad L = 0 \quad R = N-1 \quad B = N-1,$$

$$K = 1$$

while ($K \leq N^2$) {

if ($D == 0$) {

for ($i = L; i \leq R; i++$) {

arr[T][i] = K++

}

$$D = 1$$

if (D == 1)

for (i = 1; i <= B; i++) {

arr[i][R] = k++;

}

R--;

D = 2

if (D == 2) {

for (i = R; i >= L; i--) {

arr[B][i] = k++

}

B--;

D = 3

if (D == 3) {

for (i = B; i >= 1; i--) {

arr[i][L] = k++

}

L++

D == 0,

}

		L	R	
		↓	↓	
1	2	3	4	
12	13	14	5	← 1
11	16	15	6	← B
10	9	8	7	

TC $\Rightarrow O(N^2)$

SC $\Rightarrow O(N^2)$