

# HW 9

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## Research Question:

1. Would the pattern of gpa predicting changes in popularity over time differ for Hispanic vs Asian American students?
2. Would the pattern of gpa predicting changes in likability over time differ for Hispanic vs Asian American students?
3. Would the pattern of popularity predicting changes in gpa over time differ for Hispanic vs Asian American students?
4. Would the pattern of likability predicting changes in gpa over time differ for Hispanic vs Asian American students?

## Variables:

log transformation has been performed on the original gpa1 popularity1 and likability1 values to fix the skewness of the distributions

- 'ethnic1final': ethnicity of the students: 1= Hispanic 2=Asian
- 'loggpa1': log transformed gpa at time one
- 'logpop1': log transformed value for how popular students are at time one
- 'loglike1': log transformed value for how likable students are at time one
- 'gpa\_d': difference between gpa at time 1 and time 2(one year later)= (gpa2-gpa1)
- 'pop\_d': difference between popularity at time 1 and 2= pop2- pop1
- 'like\_d': difference between likability at time1 and 2 = like1-like2





## Import Data



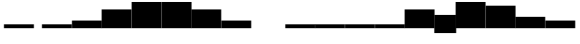

```
psyc573 <- read_sav("psyc573.sav")

# Recode `ethnic1final` to a factor variable
psyc573$ethnic1final <- psyc573$ethnic1final -1
psyc573$ethnic1final <- factor(psyc573$ethnic1final,
  levels = c(0, 1),
  labels = c("Hispanic", "Asian"))
```

## Variable Summary

```
# descriptive statistics summary by ethnic groups
datasummary( (gpa_d + pop_d + like_d + logpop1 + loglikel + loggpa1 ) *
  (N + Mean + SD + Min + Max + Histogram) ~
  factor(ethnic1final, labels = c("Hispanic", "Asian")),
  data = psyc573)
```

		Hispanic	Asian
gpa_d	N	117	218
	Mean	0.17	0.11
	SD	0.62	0.43
	Min	-1.80	-1.40
	Max	1.50	1.68
	Histogram		
pop_d	N	117	218
	Mean	-0.04	0.22
	SD	0.69	0.81
	Min	-2.64	-1.74
	Max	1.54	3.95
	Histogram		
like_d	N	117	218

	Mean	−0.10	0.25
	SD	0.88	1.02
	Min	−2.27	−2.63
	Max	1.90	3.85
	Histogram		
logpop1	N	117	218
	Mean	0.02	−0.11
	SD	0.94	0.96
	Min	−1.82	−1.59
	Max	2.03	2.47
	Histogram		
loglike1	N	117	218
	Mean	0.03	−0.01
	SD	0.94	1.00
	Min	−3.53	−2.95
	Max	1.74	1.90
	Histogram		
loggpa1	N	117	218
	Mean	1.18	1.47
	SD	0.26	0.16
	Min	0.34	0.69
	Max	1.61	1.61
	Histogram		

```
# correlation by ethnic groups
hisp<- psyc573 %>% filter(ethnic1final== 'Hispanic')
asian <- psyc573 %>% filter(ethnic1final == 'Asian')

hisp %>%
  select(gpa_d, pop_d, like_d, loggpa1, logpop1, loglike1) %>%
  datasummary_correlation(method="pearson")
```

	<b>gpa_d</b>	<b>pop_d</b>	<b>like_d</b>	<b>loggpa1</b>	<b>logpop1</b>	<b>loglike1</b>
gpa_d	1	.	.	.	.	.
pop_d	-.21	1	.	.	.	.
like_d	-.07	.30	1	.	.	.
loggpa1	-.46	.26	-.02	1	.	.
logpop1	.13	-.45	-.29	-.20	1	.
loglike1	-.08	-.11	-.57	.17	.53	1

```
asian %>%
  select(gpa_d, pop_d, like_d, loggpa1, logpop1, loglike1) %>%
  datasummary_correlation(method="pearson")
```

	<b>gpa_d</b>	<b>pop_d</b>	<b>like_d</b>	<b>loggpa1</b>	<b>logpop1</b>	<b>loglike1</b>
gpa_d	1	.	.	.	.	.
pop_d	-.17	1	.	.	.	.
like_d	-.09	.37	1	.	.	.
loggpa1	-.39	-.04	.05	1	.	.
logpop1	.02	-.14	-.12	-.03	1	.
loglike1	-.06	-.09	-.40	.10	.52	1

# Model for gpa time 1 predicting popularity

# change score :

## Model

Let  $G = \text{loggpa1}$ ,  $P = \text{pop\_d}$ ,  $E = \text{ethnic1final}$

$$P_i \sim N(\mu_i, \sigma)$$

$$\mu_i = \beta_0 + \beta_1 G_i + \beta_2 E_i + \beta_3 G_i \times E_i$$

## Prior:

$$\beta_0 \sim N(0, 1)$$

$$\beta_1 \sim N(0.1, 0.05)$$

$$\beta_2 \sim N(0.1, 0.05)$$

$$\beta_3 \sim N(0.1, 0.05)$$

$$\sigma \sim t_3^+(0, 2.5)$$

```
# gpa1 predicts popularity change score
m1 <- brm(
  pop_d ~ loggpa1 * ethnic1final,
  data = psyc573,
  prior = prior(normal(0.1, 0.05), class = "b") +
    prior(normal(0.1, 0.05), class = "b", coef = "ethnic1finalAsian") +
    prior(normal(0, 1), class = "Intercept") +
    prior(student_t(3, 0, 2.5), class = "sigma"),
  seed = 940,
  iter = 4000
)
```

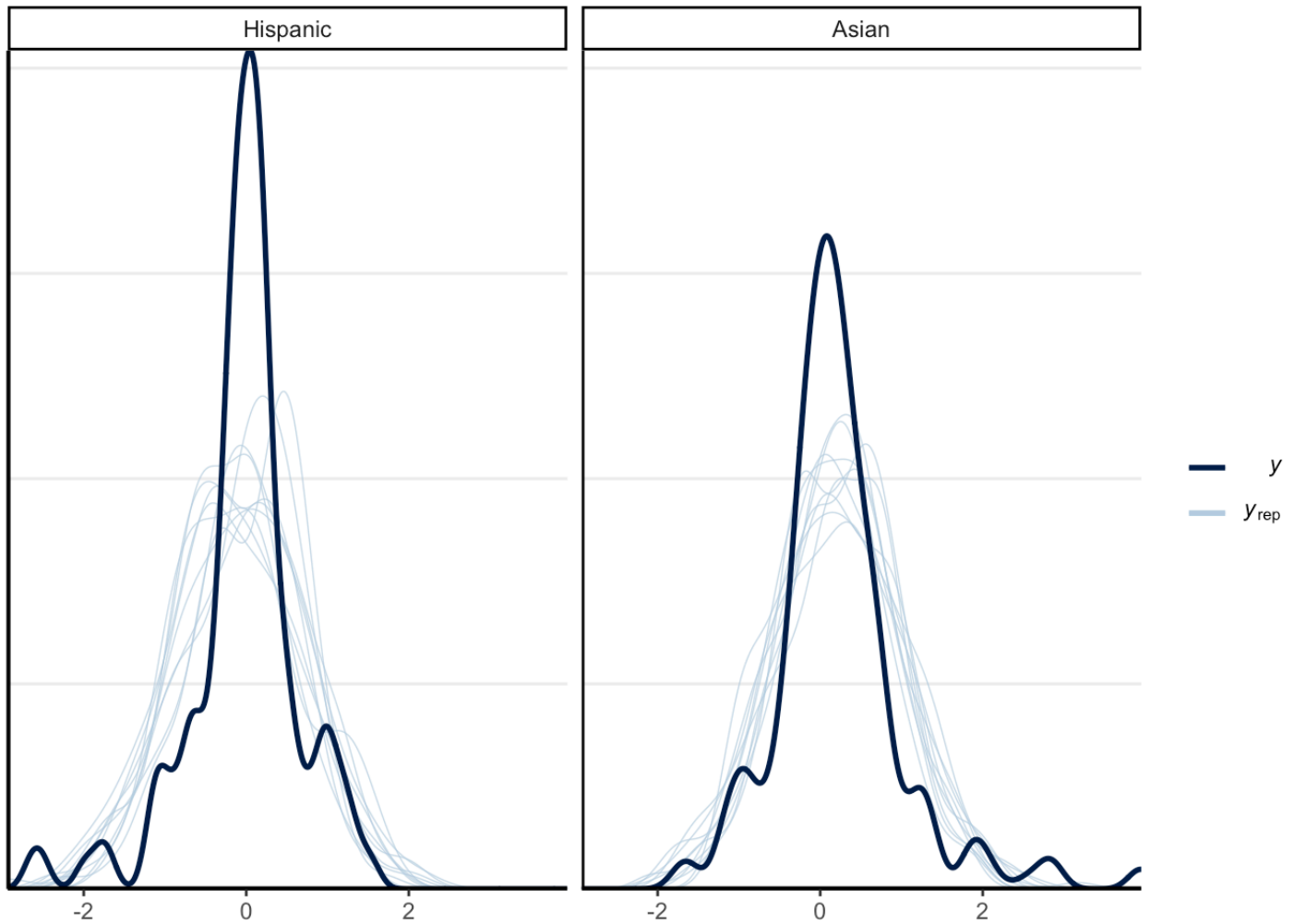
m1

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: pop_d ~ loggp1 * ethnic1final
## Data: psyc573 (Number of observations: 335)
## Draws: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
## total post-warmup draws = 8000
##
## Population-Level Effects:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS
## Intercept	-0.17	0.08	-0.33	-0.00	1.00	9661
## loggp1	0.11	0.05	0.01	0.21	1.00	9524
## ethnic1finalAsian	0.10	0.05	0.01	0.19	1.00	9199
## loggp1:ethnic1finalAsian	0.09	0.04	0.01	0.17	1.00	9696

```
##
## Tail_ESS
## Intercept
## loggp1
## ethnic1finalAsian
## loggp1:ethnic1finalAsian
##
## Family Specific Parameters:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma 0.77 0.03 0.72 0.84 1.00 8740 5688
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

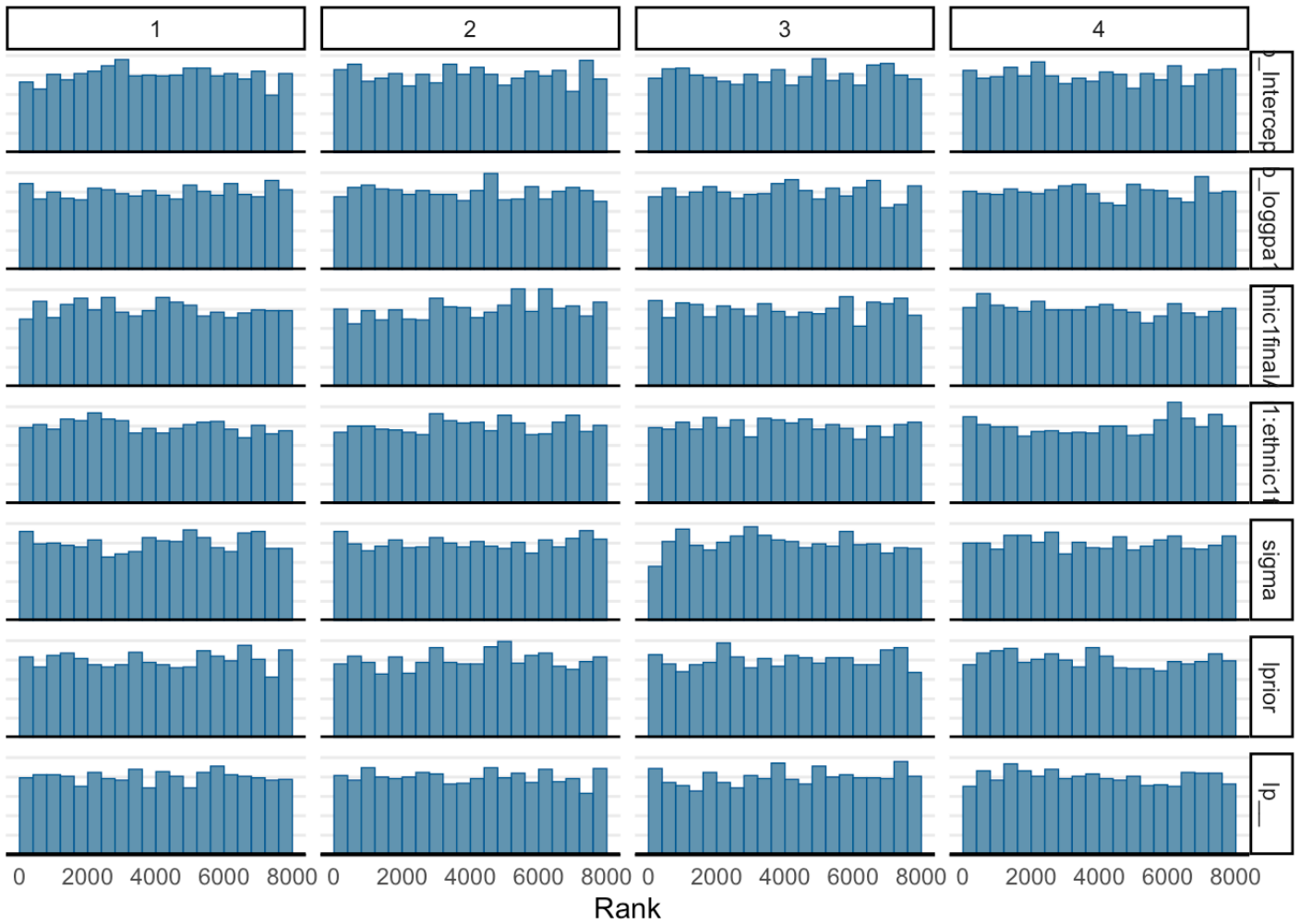
```
pp_check(m1, type = "dens_overlay_grouped", group = "ethnic1final")
```



## Results:

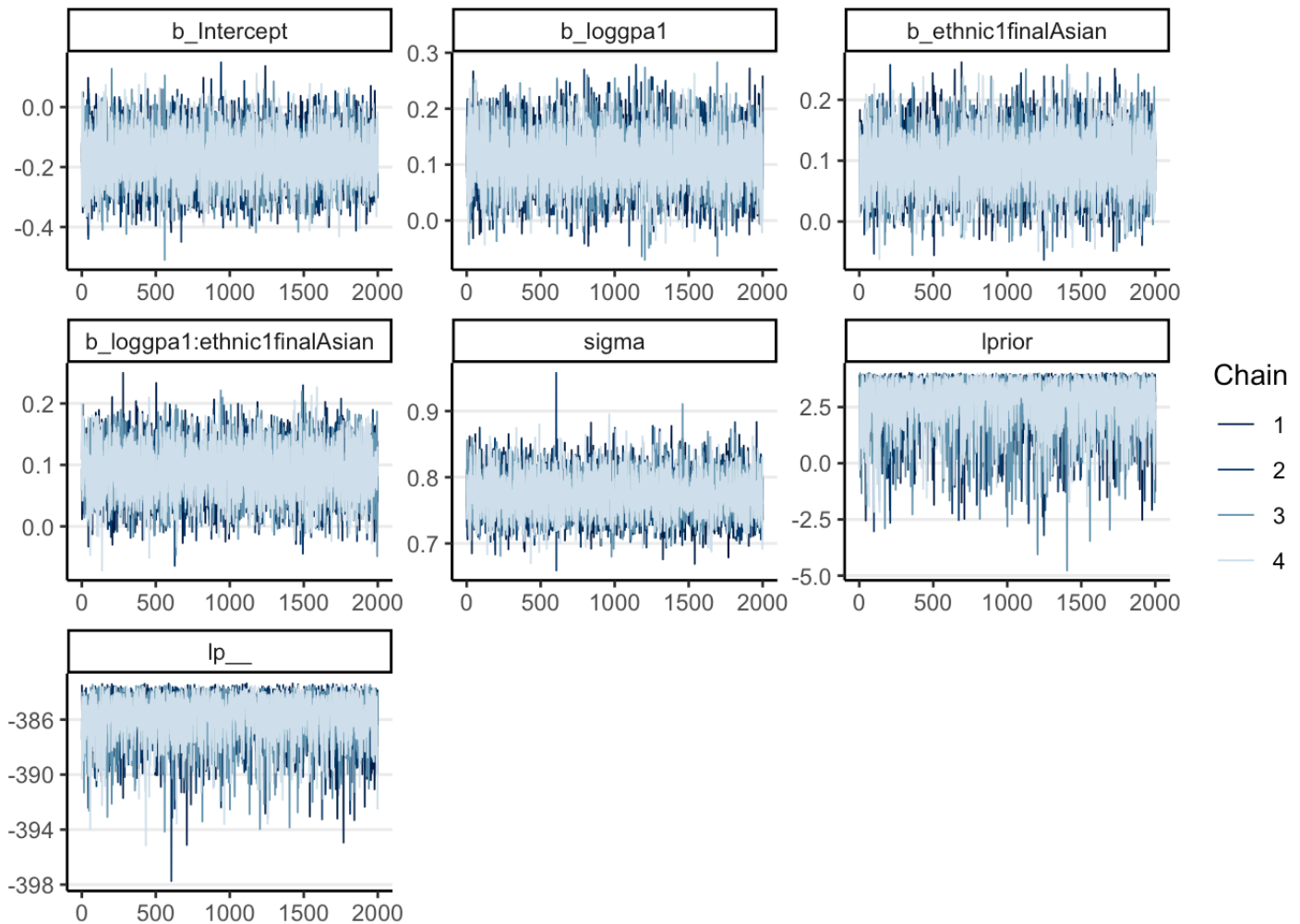
As shown in the graph below, the chains mixed well.

```
mcmc_rank_hist(m1)
```



```
mcmc_trace(as.array(m1))
```



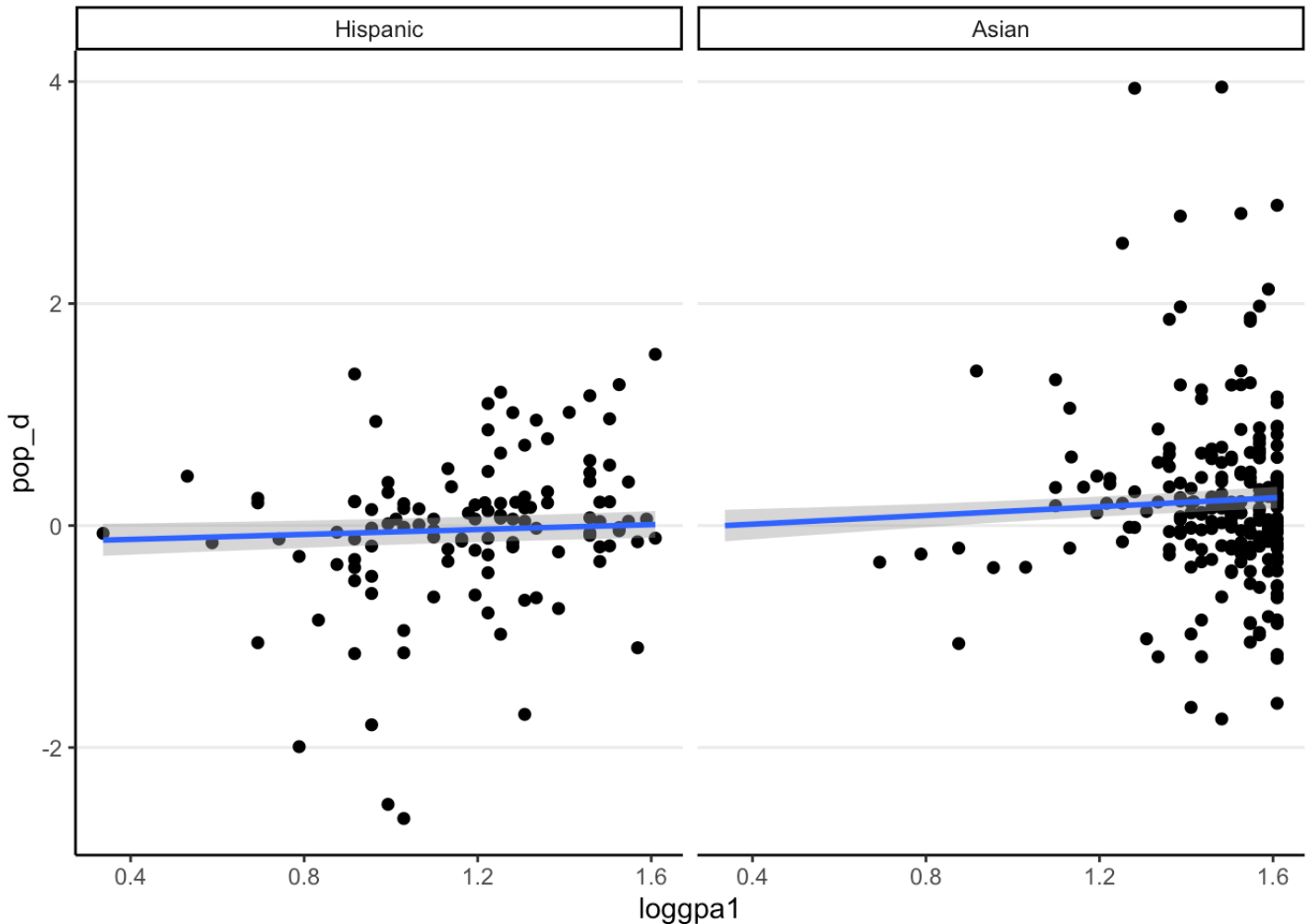


The following table and graph show the posterior distributions of `b_hispanic` and `b_asian`  
`b_loggpa1:ethnic1finalAsian`

```
as_draws(m1) %>%
  mutate_variables(
    b_hisp = b_loggpa1,
    b_asian = b_loggpa1 + `b_loggpa1:ethnic1finalAsian`
  ) %>%
  posterior::subset_draws(
    variable = c("b_hisp", "b_asian")
  ) %>%
  summarize_draws()
```

```
## # A tibble: 2 × 10
##   variable mean median    sd    mad    q5    q95  rhat ess_bulk ess_tail
##   <chr>    <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>    <dbl>    <dbl>
## 1 b_hisp  0.110  0.110 0.0486 0.0490 0.0294 0.190  1.00   9524.   5926.
## 2 b_asian 0.199  0.199 0.0593 0.0605 0.101  0.297  1.00   9212.   6200.
```

```
plot(
  conditional_effects(m1,
    effects = "loggpa1",
    conditions = data.frame(ethnic1final = c("Hispanic", "Asian"),
      cond__ = c("Hispanic", "Asian"))
  ),
  points = TRUE
)
```



## Interpretation:

The analysis showed that on average, the patterns for gpa at time 1 predicting changes in levels of popularity differed for Asian and Hispanic American middle school students.

Specifically, gpa at time1 is more strongly associated with an increase in popularity from time 1 to time2 for Asian American students (posterior mean= 0.11, 90%CI [0.10, 0.30]) than for Hispanic American students (posterior mean = 0.11, 90% CI [0.03, 0.19]).

# Model for gpa time1 predicting likability change score:

## Models

Let  $G = \text{loggpa1}$ ,  $L = \text{like\_d}$ ,  $E = \text{ethnic1final}$

$$L_i \sim N(\mu_i, \sigma)$$

$$\mu_i = \beta_0 + \beta_1 G_i + \beta_2 E_i + \beta_3 G_i \times E_i$$

## Prior:

$$\beta_0 \sim N(0, 1)$$

$$\beta_1 \sim N(0.1, 0.05)$$

$$\beta_2 \sim N(0.1, 0.05)$$

$$\beta_3 \sim N(0.1, 0.05)$$

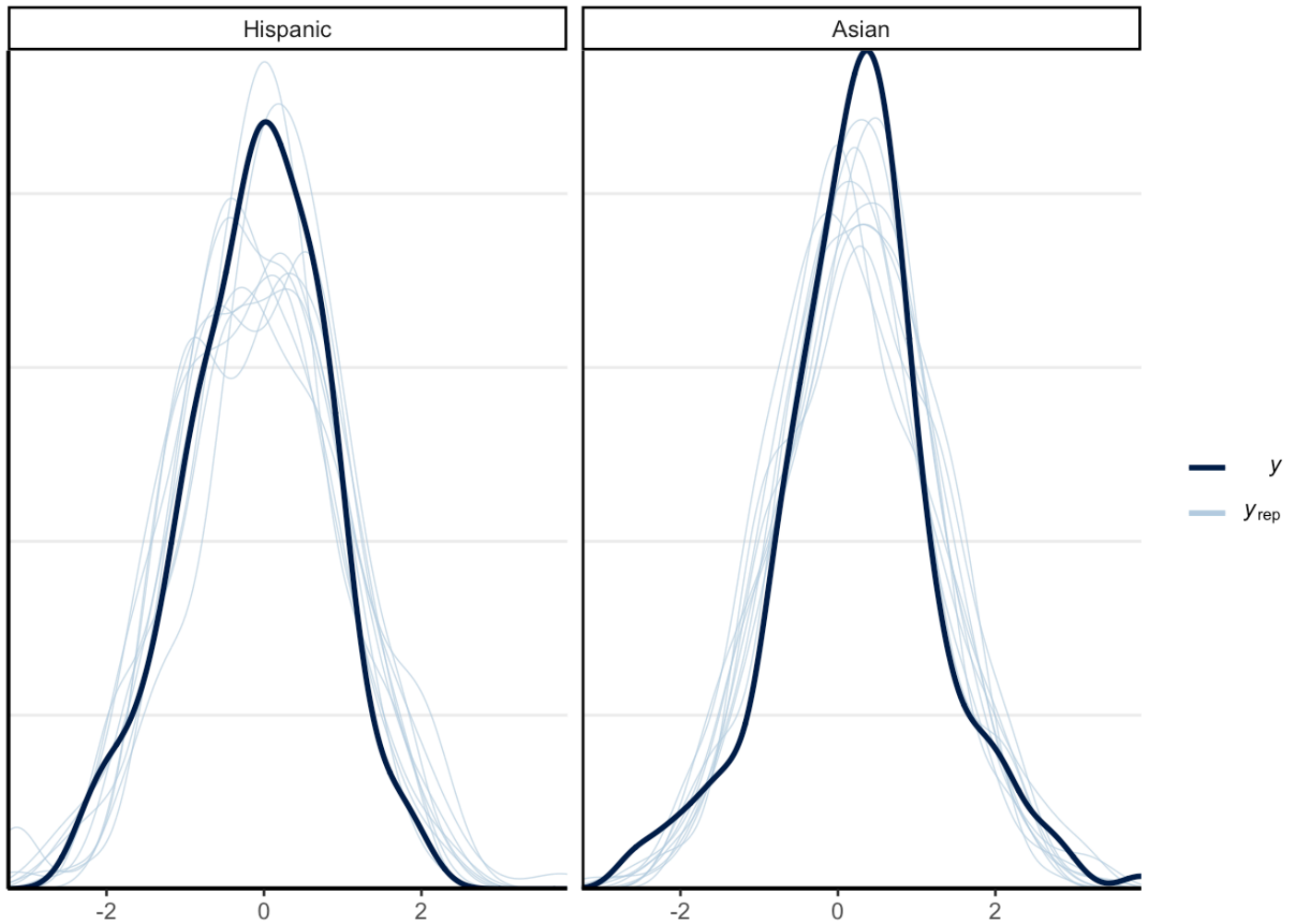
$$\sigma \sim t_3^+(0, 2.5)$$

```
# gpa1 predicts likability change score
m2 <- brm(
  like_d ~ loggpa1 * ethnic1final,
  data = psyc573,
  prior = prior(normal(0.1, 0.05), class = "b") +
    prior(normal(0.1, 0.05), class = "b", coef = "ethnic1finalAsian") +
    prior(normal(0, 1), class = "Intercept") +
    prior(student_t(3, 0, 2.5), class = "sigma"),
  seed = 941,
  iter = 4000
)
```

```
summary(m2)
```

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: like_d ~ loggp1 * ethnic1final
## Data: psyc573 (Number of observations: 335)
## Draws: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
## total post-warmup draws = 8000
##
## Population-Level Effects:
##               Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS
## Intercept      -0.19      0.09   -0.37   -0.00 1.00   10719
## loggp1          0.10      0.05    0.01    0.19 1.00   10002
## ethnic1finalAsian 0.11      0.05    0.02    0.20 1.00   10220
## loggp1:ethnic1finalAsian 0.11  0.04    0.03    0.20 1.00    9301
##               Tail_ESS
## Intercept        6355
## loggp1           6334
## ethnic1finalAsian 6160
## loggp1:ethnic1finalAsian 6574
##
## Family Specific Parameters:
##               Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma          0.97      0.04    0.90    1.05 1.00   9024   5927
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

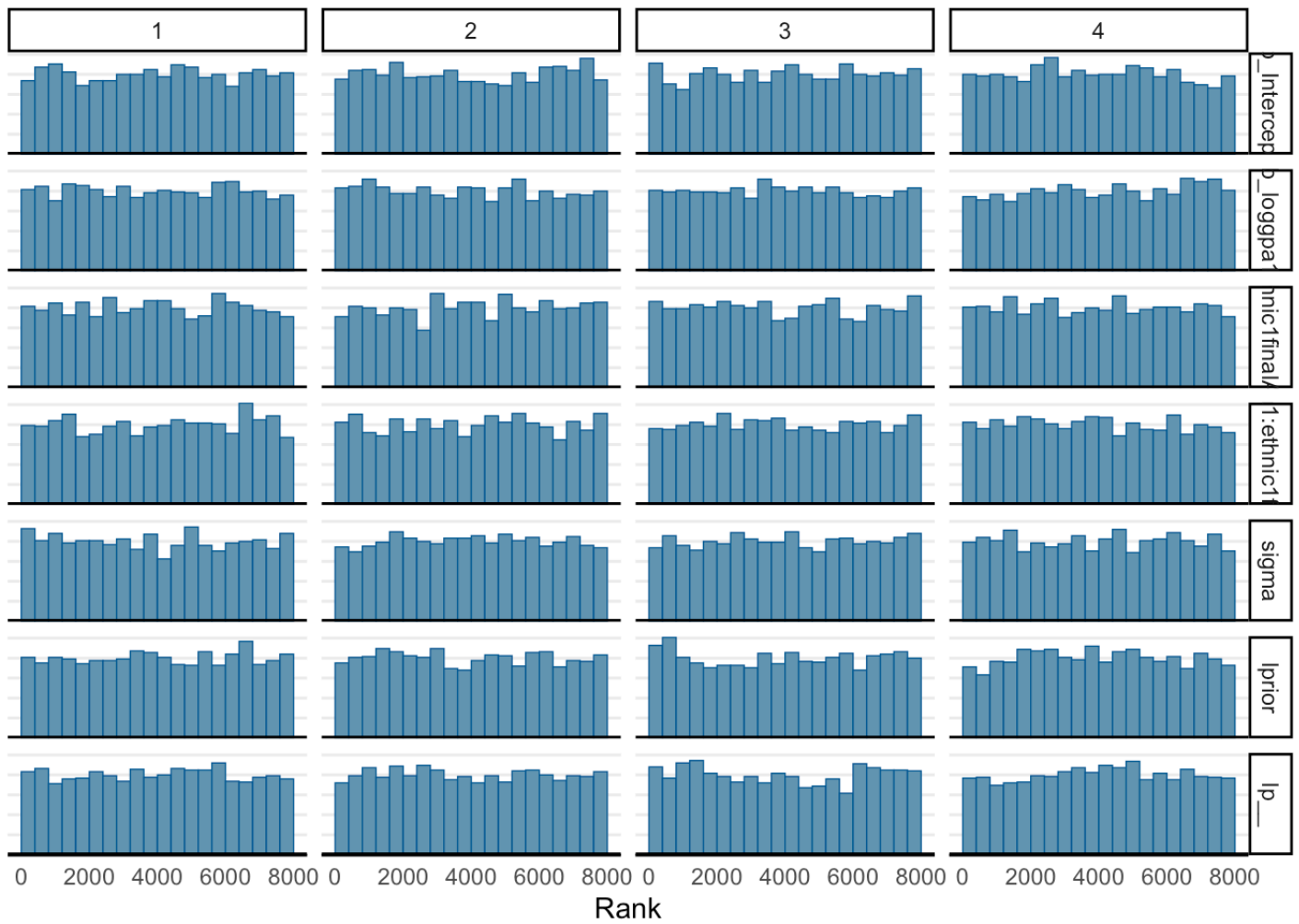
```
pp_check(m2, type = "dens_overlay_grouped", group = "ethnic1final")
```



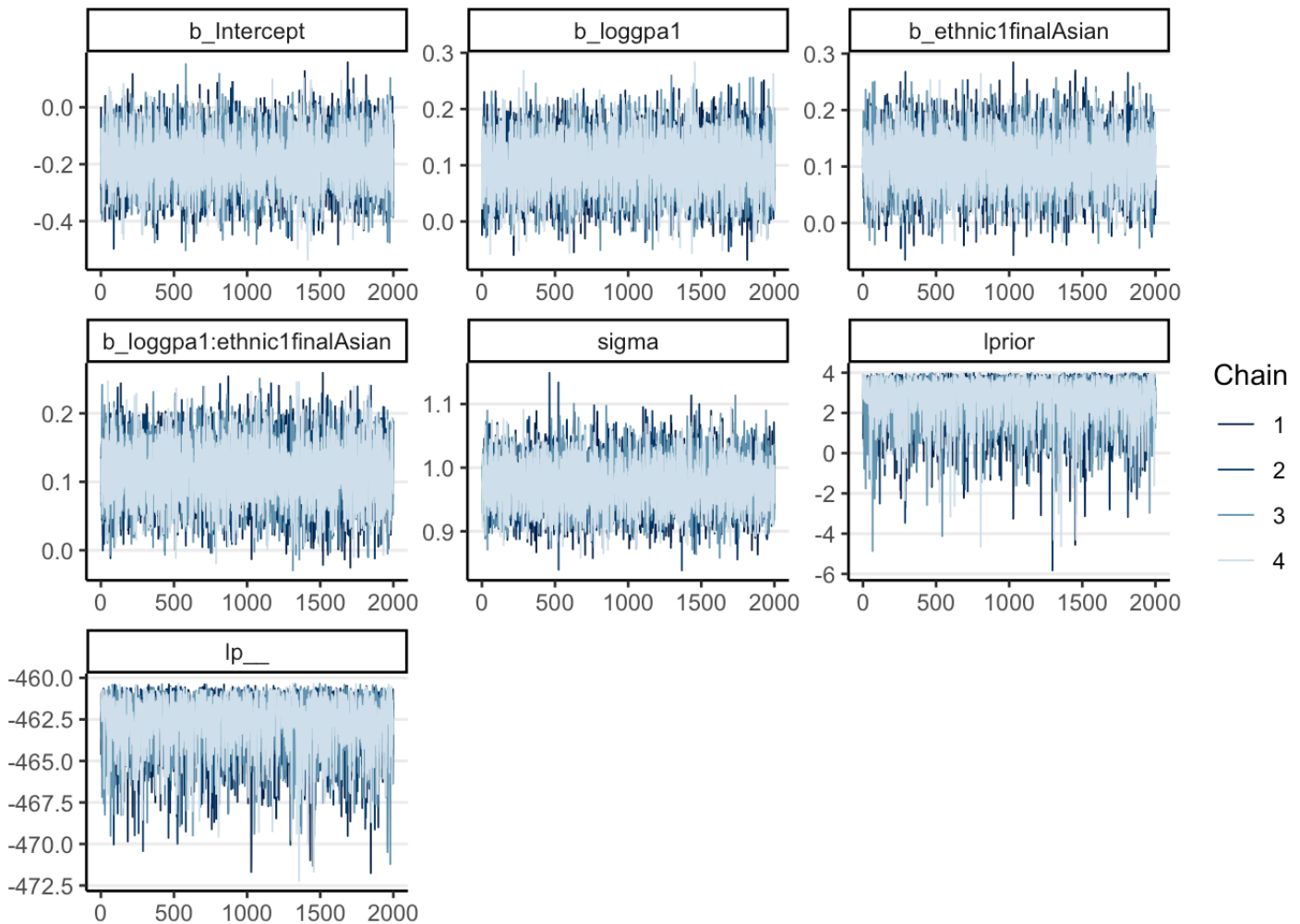
## Results:

As shown in the graph below, the chains mixed well.

```
mcmc_rank_hist(m2)
```



```
mcmc_trace(as.array(m2))
```

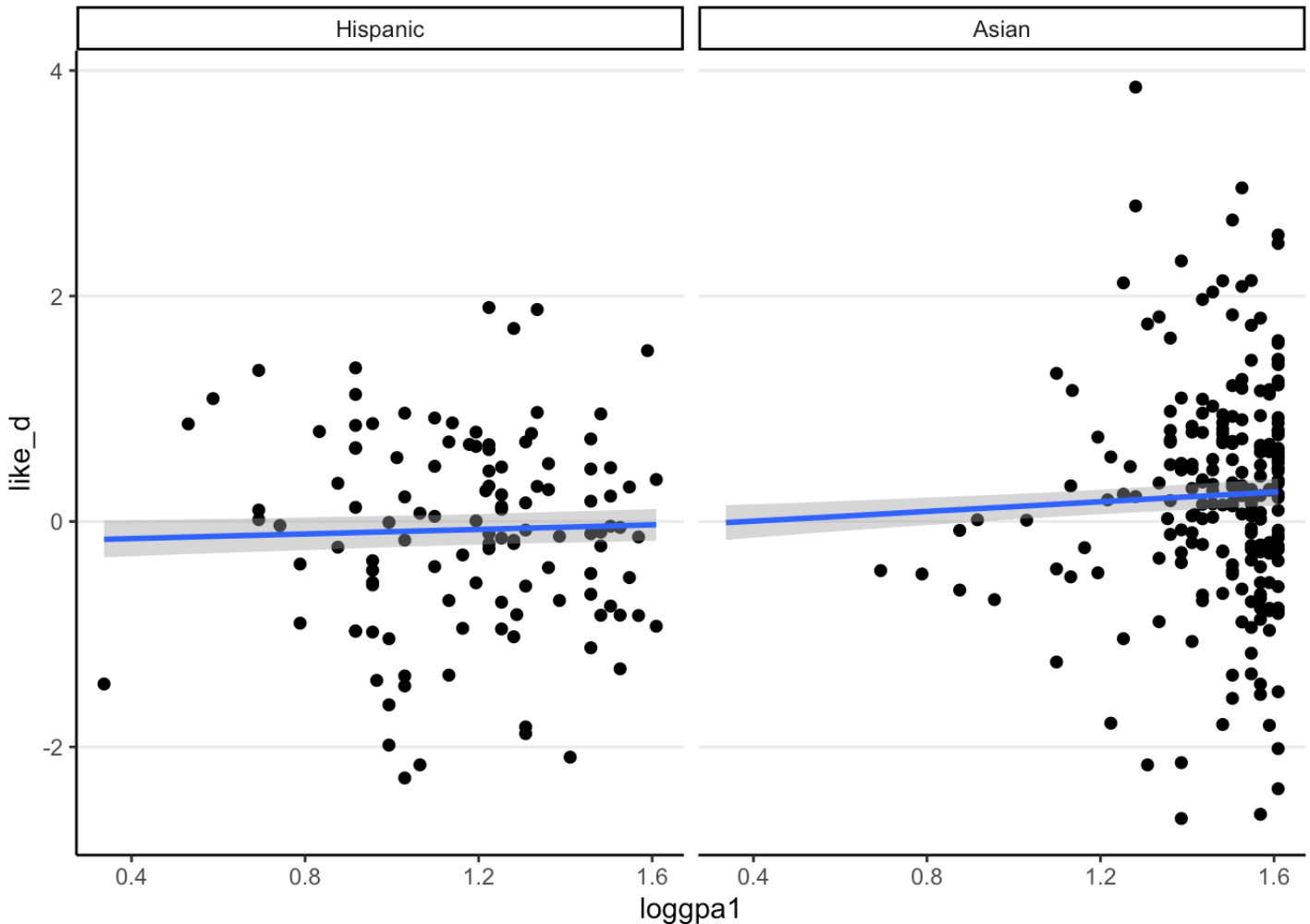


The following table and graph show the posterior distributions of `b_hispanic` and `b_asian`

```
as_draws(m2) %>%
  mutate_variables(
    b_hisp = b_loggpa1,
    b_asian = b_loggpa1 + `b_loggpa1:ethnic1finalAsian`
  ) %>%
  posterior::subset_draws(
    variable = c("b_hisp", "b_asian")
  ) %>%
  summarize_draws()
```

```
## # A tibble: 2 × 10
##   variable    mean median      sd    mad      q5    q95  rhat ess_bulk ess_tail
##   <chr>      <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>    <dbl>    <dbl>
## 1 b_hisp    0.0999  0.100 0.0488 0.0497 0.0184 0.179  1.00   10002.   6334.
## 2 b_asian   0.214   0.213 0.0625 0.0626 0.111  0.315  1.00   10008.   6406.
```

```
plot(
  conditional_effects(m2,
    effects = "loggpa1",
    conditions = data.frame(ethnic1final = c("Hispanic", "Asian"),
      cond__ = c("Hispanic", "Asian"))
  ),
  points = TRUE
)
```



## Interpretation:

The analysis showed that on average, the patterns for gpa at time 1 predicting changes in levels of likability differed for Asian and Hispanic American middle school students.

Specifically, gpa at time1 is more strongly associated with an increase in likability from time 1 to time2 for Asian American students (posterior mean= 0.21, 90%CI [0.11, 0.32]) than for Hispanic American students (posterior mean = 0.10, 90% CI [0.02 0.18]).



# Model for pop1 predicting gpa change score :

## Model:

Let  $G$  = gpa\_d,  $P$  = logpop1,  $E$  = ethnic1final

$$G_i \sim N(\mu_i, \sigma)$$

$$\mu_i = \beta_0 + \beta_1 P_i + \beta_2 E_i + \beta_3 P_i \times E_i$$

## Prior:

$$\beta_0 \sim N(1, 0.5)$$

$$\beta_1 \sim N(0.5, 0.5)$$

$$\beta_2 \sim N(0.5, 0.5)$$

$$\beta_3 \sim N(0.5, 0.5)$$

$$\sigma \sim t_3^+(0, 2.5)$$

```
# pop1 predicts gpa change score
m3 <- brm(
  gpa_d ~ logpop1 * ethnic1final,
  data = psyc573,
  prior = prior(normal(0.5, 0.5), class = "b") +
    prior(normal(0.5, 0.5), class = "b", coef = "ethnic1finalAsian") +
    prior(normal(1, 0.5), class = "Intercept") +
    prior(student_t(3, 0, 2.5), class = "sigma"),
  seed = 939,
  iter = 4000
)
```

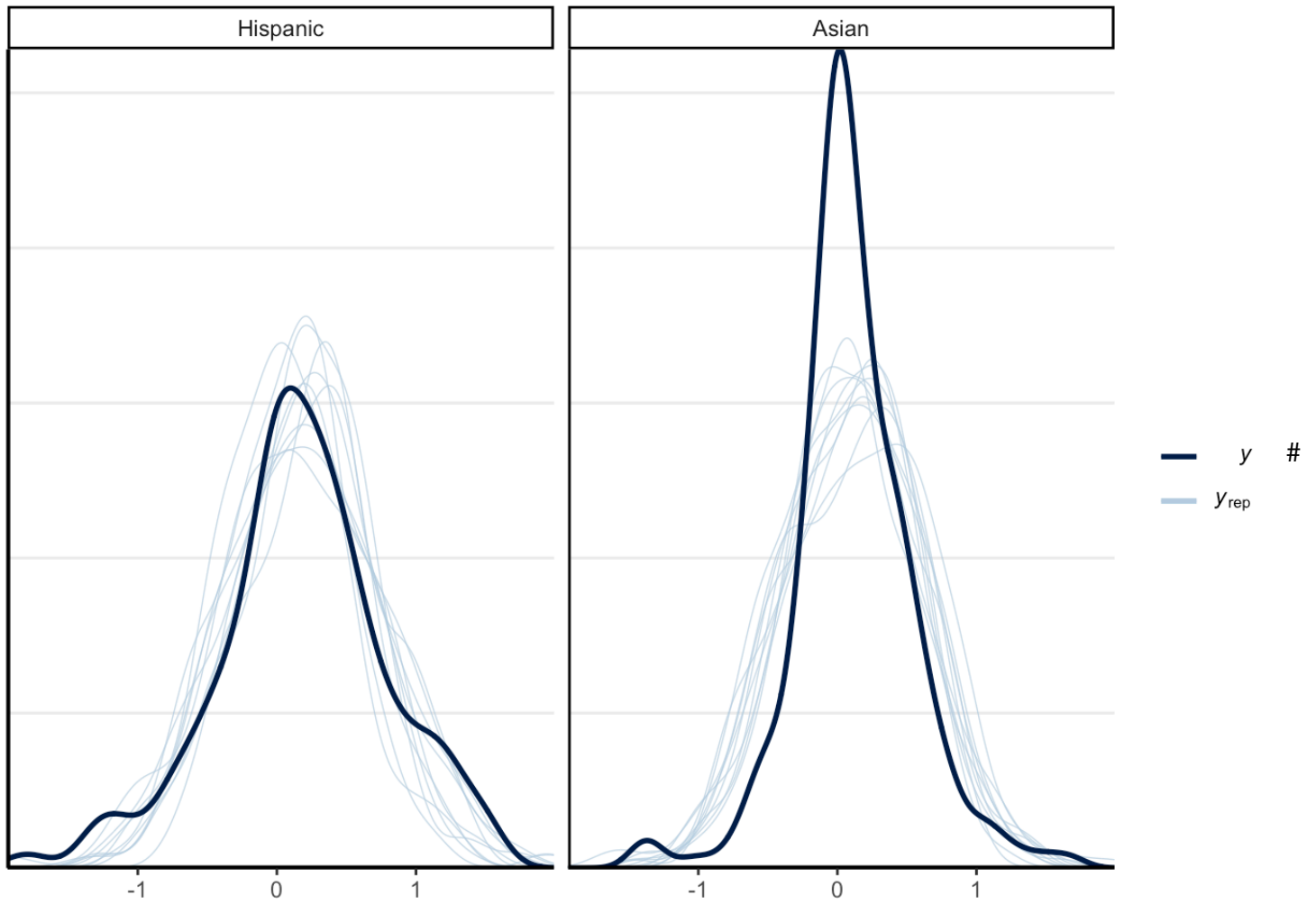
```
summary(m3)
```

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: gpa_d ~ logpop1 * ethniclfinal
## Data: psyc573 (Number of observations: 335)
## Draws: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
## total post-warmup draws = 8000
##
## Population-Level Effects:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS
Intercept	0.17	0.05	0.08	0.26	1.00	7367
logpop1	0.08	0.05	-0.02	0.18	1.00	4356
ethniclfinalAsian	-0.05	0.06	-0.16	0.07	1.00	8470
logpop1:ethniclfinalAsian	-0.07	0.06	-0.18	0.05	1.00	4296

```
## Tail_ESS
## Intercept 5381
## logpop1 5080
## ethniclfinalAsian 5385
## logpop1:ethniclfinalAsian 4785
##
## Family Specific Parameters:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma 0.50 0.02 0.47 0.54 1.00 8024 5871
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

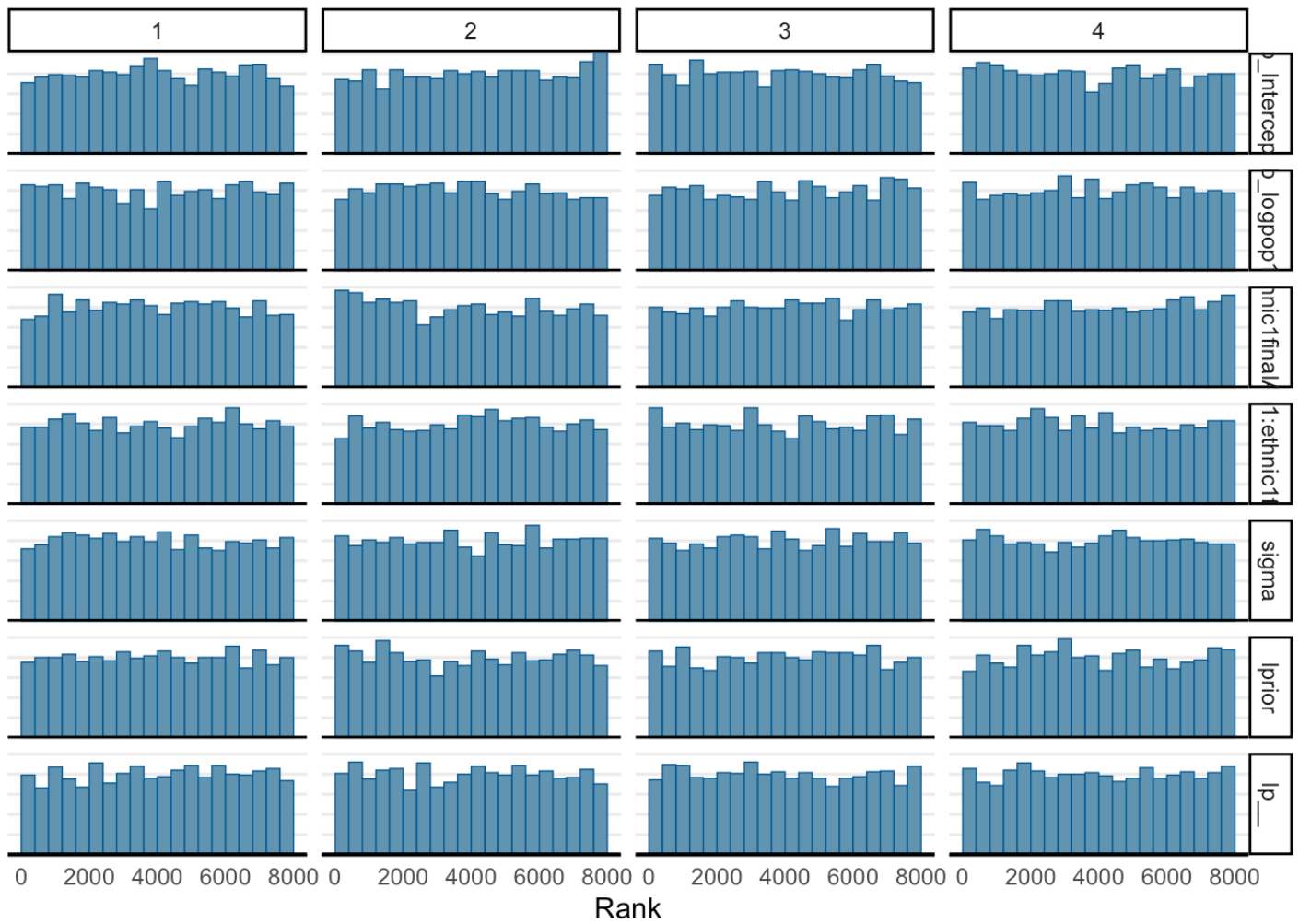
```
pp_check(m3, type = "dens_overlay_grouped", group = "ethniclfinal")
```



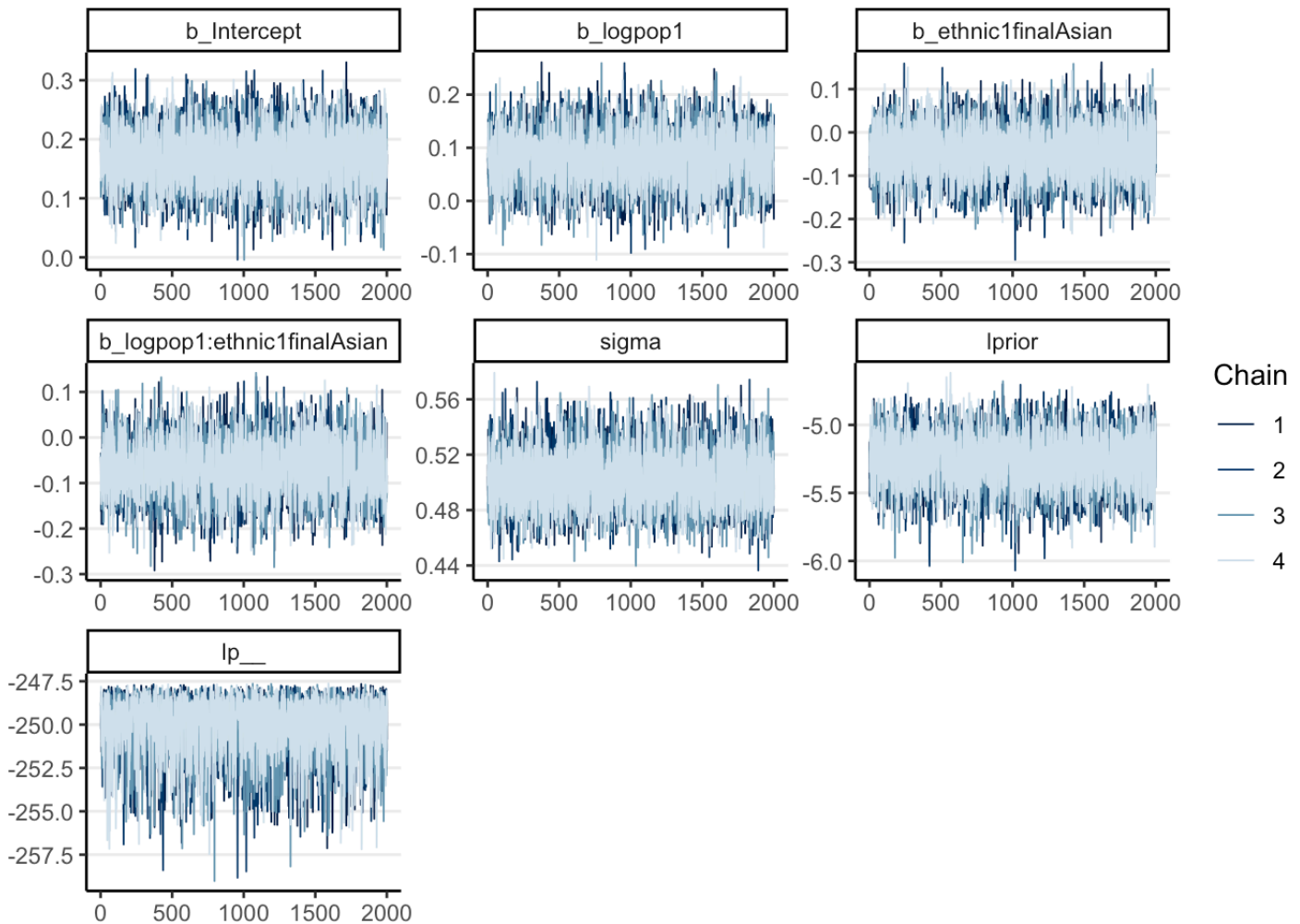
Results:

As shown in the graph below, the chains mixed well.

```
mcmc_rank_hist(m3)
```



```
mcmc_trace(as.array(m3))
```

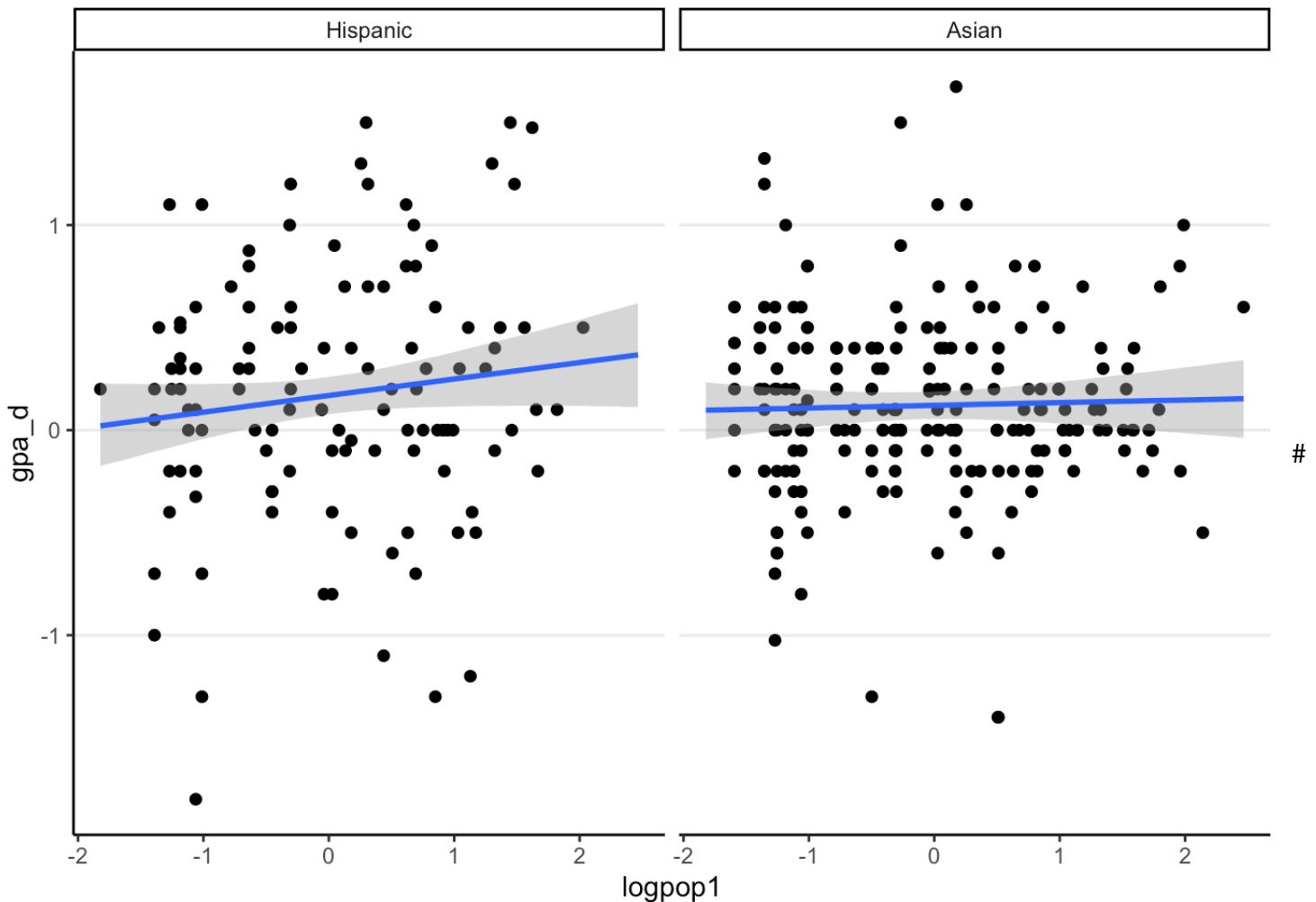


The following table and graph show the posterior distributions of `b_hispanic` and `b_asian`

```
as_draws(m3) %>%
  mutate_variables(
    b_hisp = b_logpop1,
    b_asian = b_logpop1 + `b_logpop1:ethnic1finalAsian`
  ) %>%
  posterior::subset_draws(
    variable = c("b_hisp", "b_asian")
  ) %>%
  summarize_draws()
```

```
## # A tibble: 2 × 10
##   variable    mean median      sd    mad      q5     q95  rhat ess_bulk ess_tail
##   <chr>      <dbl> <dbl>   <dbl> <dbl>   <dbl> <dbl> <dbl>   <dbl>   <dbl>
## 1 b_hisp    0.0808 0.0809 0.0491 0.0488 0.0000931 0.161 1.00    4356.    5080.
## 2 b_asian   0.0132 0.0131 0.0355 0.0356 -0.0448    0.0724 1.00    9242.    6223.
```

```
plot(
  conditional_effects(m3,
    effects = "logpop1",
    conditions = data.frame(ethnic1final = c("Hispanic", "Asian"),
      cond__ = c("Hispanic", "Asian"))
  ),
  points = TRUE
)
```



Interpretation:

The analysis indicates that the patterns for popularity at time 1 predicting increase in gpa from time1 and time2 did not differ for Hispanic (posterior mean= 0.08, 90 CI [0.00, 0.16]) and Asian (posterior mean= 0.01, 95% CI[-0.00, 0.07]) American students ( $\beta_3$  (the beta for pop1 x gpa\_d)=-0.017, 95% CI [-0.18 0.05])

## Model for like1 predicting gpa change score :

# Model

Let  $G$  = gpa\_d,  $P$  = loglike1,  $E$  = ethnic1final

$$G_i \sim N(\mu_i, \sigma)$$

$$\mu_i = \beta_0 + \beta_1 L_i + \beta_2 E_i + \beta_3 L_i \times E_i$$

## Prior:

$$\beta_0 \sim N(1, 0.5)$$

$$\beta_1 \sim N(0.5, 0.5)$$

$$\beta_2 \sim N(0.5, 0.5)$$

$$\beta_3 \sim N(0.5, 0.5)$$

$$\sigma \sim t_4^+(0, 3)$$

```
# like1 predicts gpa change score
m4 <- brm(
  gpa_d ~ loglike1 * ethnic1final,
  data = psyc573,
  prior = prior(normal(0.5, 0.5), class = "b") +
    prior(normal(0.5, 0.5), class = "b", coef = "ethnic1finalAsian") +
    prior(normal(1, 0.5), class = "Intercept") +
    prior(student_t(3, 0, 2.5), class = "sigma"),
  seed = 938,
  iter = 4000
)
```

```
summary(m4)
```

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: gpa_d ~ loglikel * ethniclfinal
## Data: psyc573 (Number of observations: 335)
## Draws: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
## total post-warmup draws = 8000
##
## Population-Level Effects:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS
## Intercept	0.17	0.05	0.08	0.26	1.00	8019
## loglikel	-0.05	0.05	-0.15	0.04	1.00	4012
## ethniclfinalAsian	-0.05	0.06	-0.17	0.06	1.00	7944
## loglikel:ethniclfinalAsian	0.03	0.06	-0.09	0.15	1.00	3814

```
##
```

	Tail_ESS
## Intercept	5221
## loglikel	5048
## ethniclfinalAsian	5180
## loglikel:ethniclfinalAsian	5018

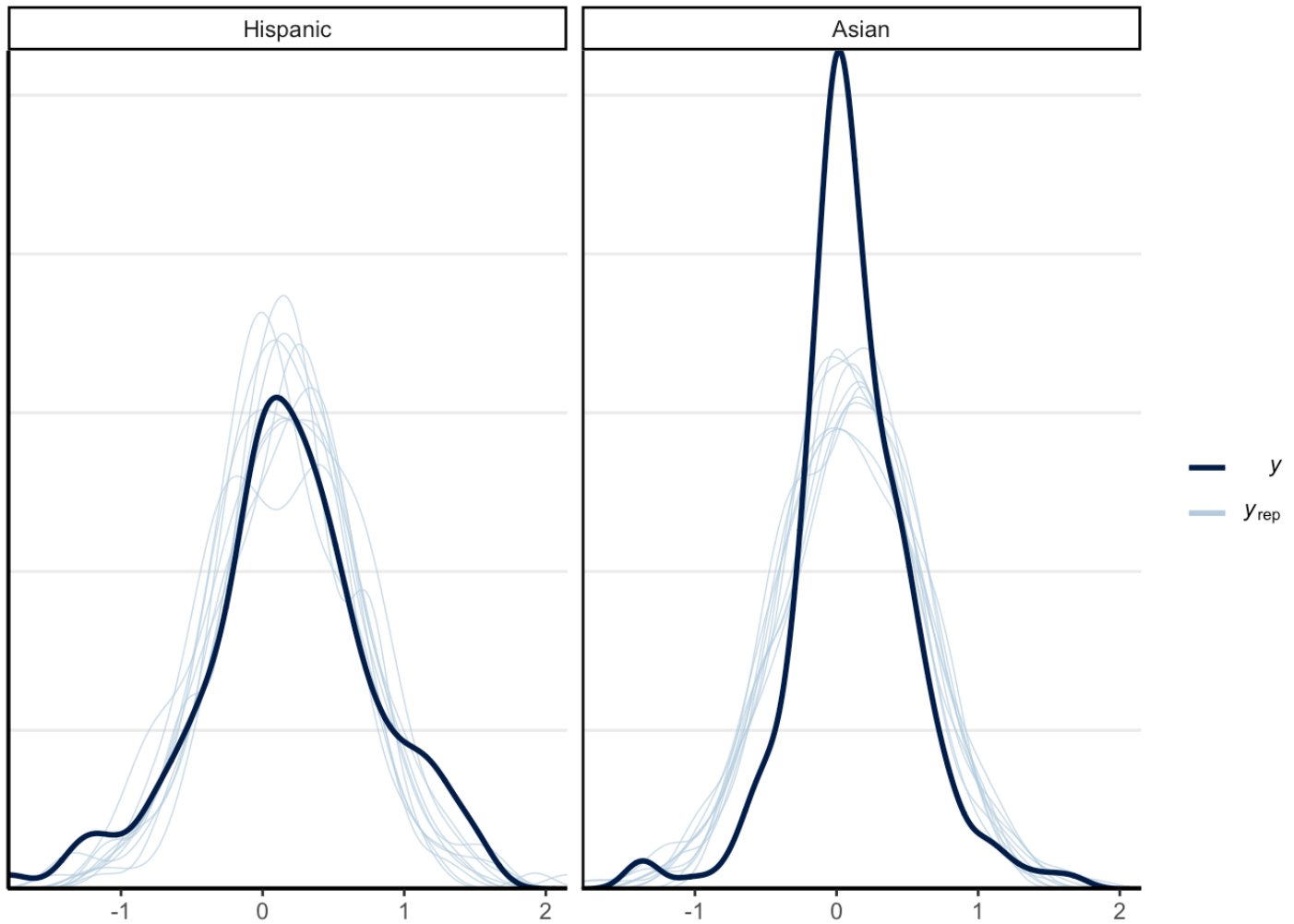
```
##
## Family Specific Parameters:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
## sigma	0.50	0.02	0.47	0.54	1.00	7934	5507

```
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
pp_check(m4, type = "dens_overlay_grouped", group = "ethniclfinal")
```

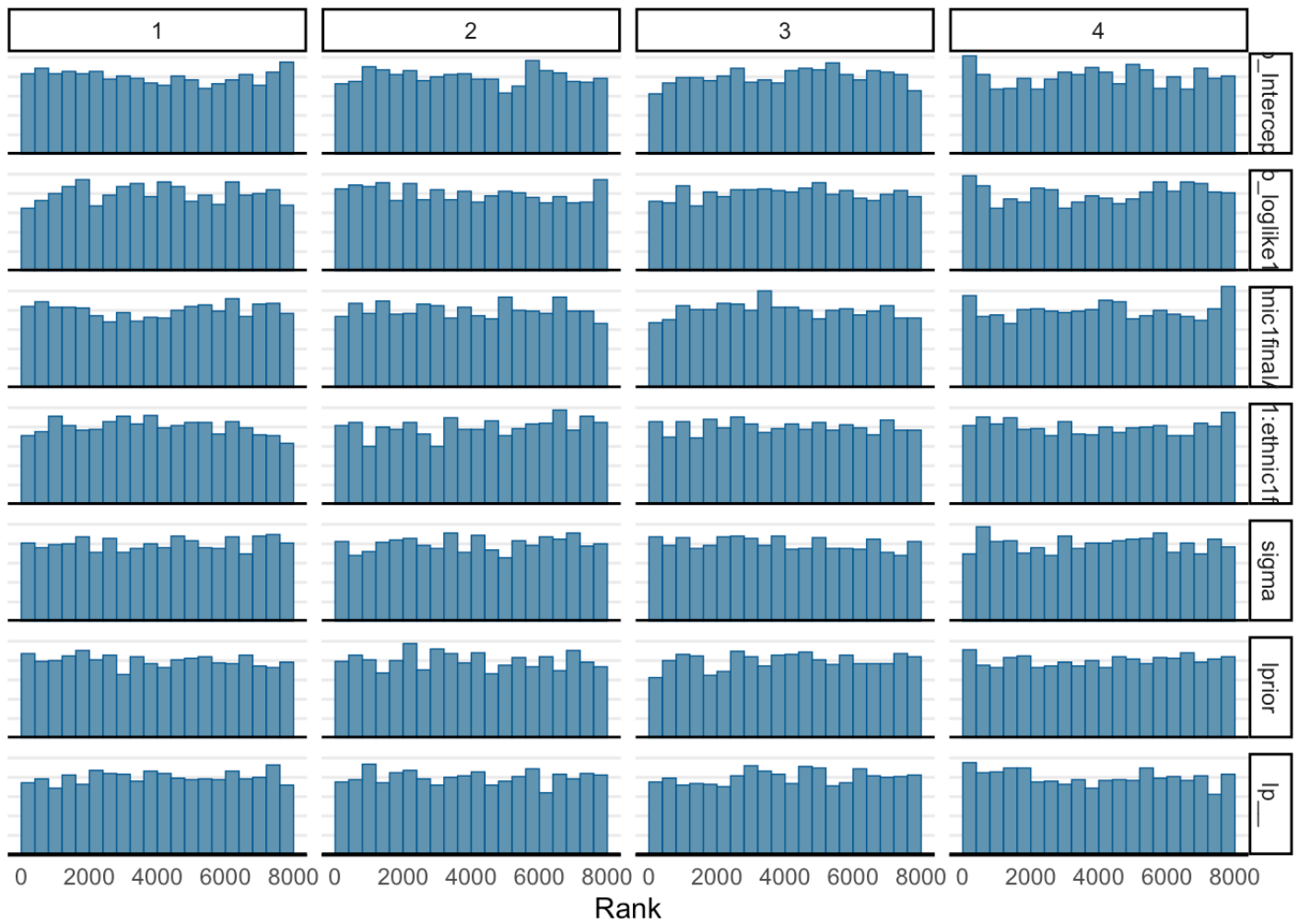




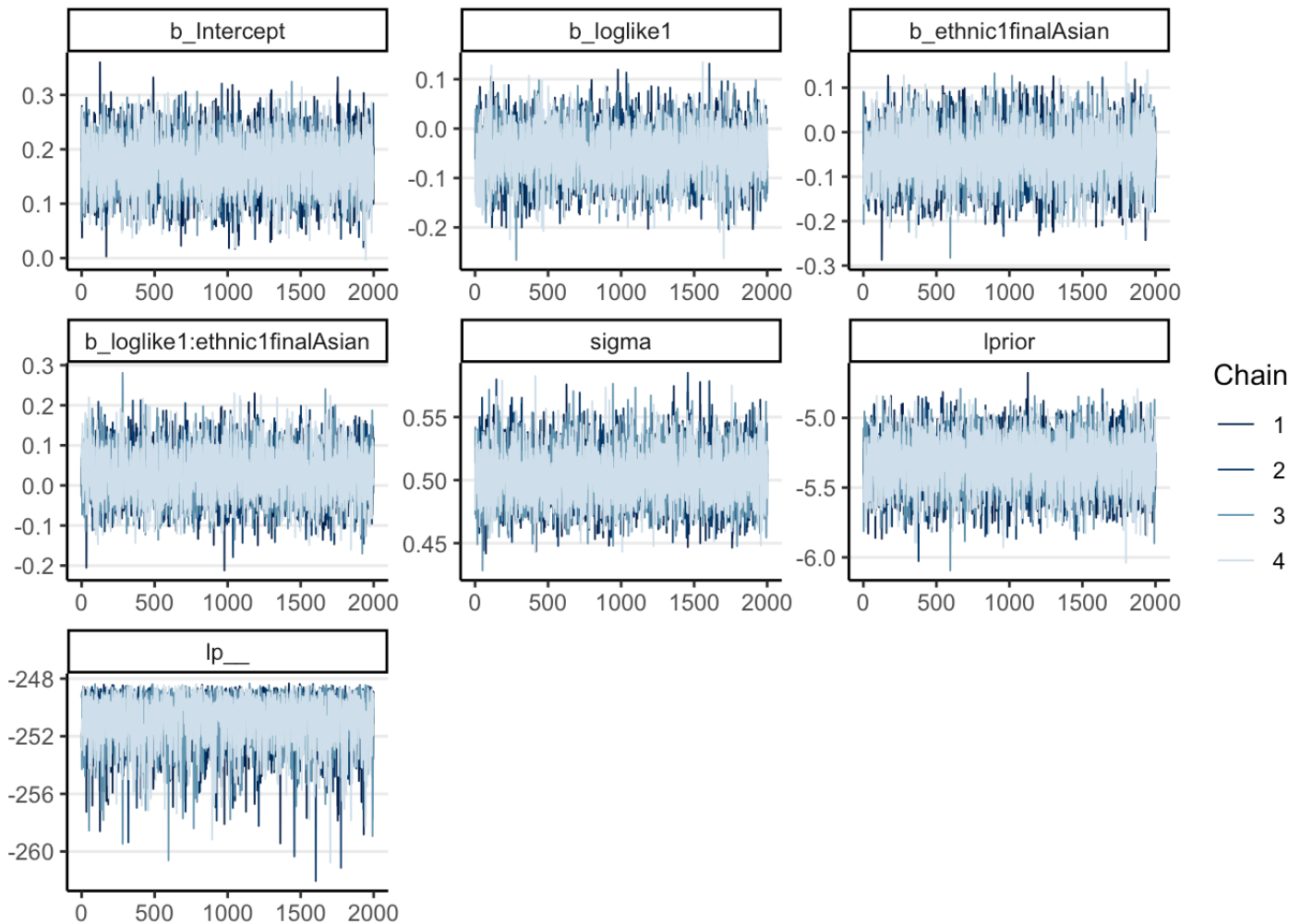
## Results:

As shown in the graph below, the chains mixed well.

```
mcmc_rank_hist(m4)
```



```
mcmc_trace(as.array(m4))
```

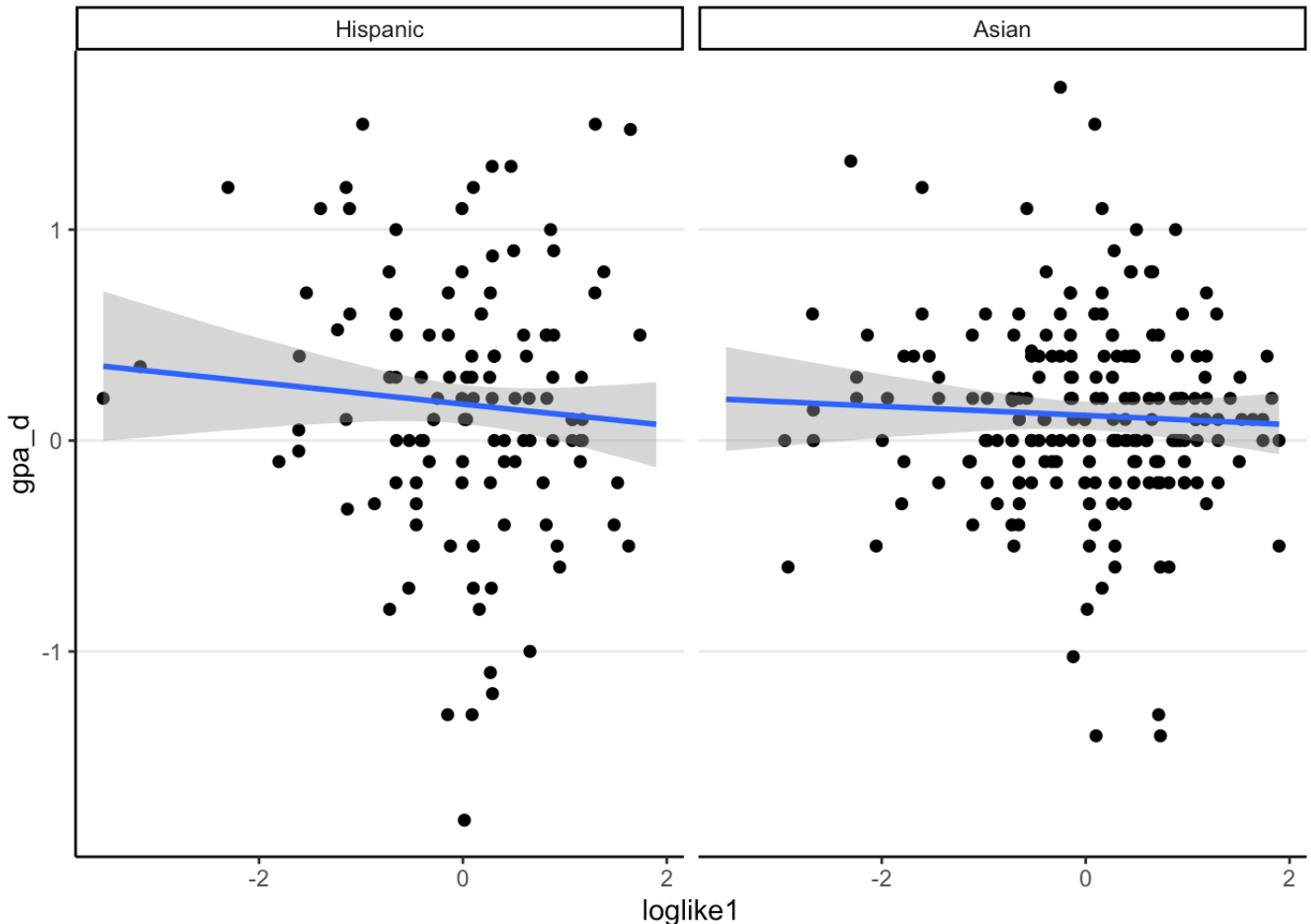


The following table and graph show the posterior distributions of `b_hispanic` and `b_asian`

```
as_draws(m4) %>%
  mutate_variables(
    b_hisp = b_loglike1,
    b_asian = b_loglike1 + `b_loglike1:ethnic1finalAsian`
  ) %>%
  posterior::subset_draws(
    variable = c("b_hisp", "b_asian")
  ) %>%
  summarize_draws()
```

```
## # A tibble: 2 × 10
##   variable    mean  median    sd    mad     q5     q95  rhat  ess_bulk  ess_tail
##   <chr>      <dbl>  <dbl>  <dbl>  <dbl>  <dbl>  <dbl> <dbl>    <dbl>    <dbl>
## 1 b_hisp   -0.0510 -0.0507 0.0491 0.0495 -0.133  0.0275 1.00    4012.    5048.
## 2 b_asian  -0.0220 -0.0217 0.0348 0.0354 -0.0788 0.0345 1.00    8768.    6339.
```

```
plot(
  conditional_effects(m4,
    effects = "loglike1",
    conditions = data.frame(ethnic1final = c("Hispanic", "Asian"),
      cond__ = c("Hispanic", "Asian"))
  ),
  points = TRUE
)
```



## Interpretation:

The analysis indicates that the patterns for likability at time 1 predicting increase in gpa from time1 and time2 did not differ for Hispanic (posterior mean= -0.05, 90 CI [-0.13, 0.03]) and Asian (posterior mean= -0.02, 95% CI[-0.08, 0.03]) American students ( $\beta_3$  (the beta for like1 x gpa\_d)=0.03, 95% CI [-0.09 0.15])