

IN: N - arr size : 10^5
 X - + increment
 K - total number
 $0 \leq t_1 \leq t_2 \leq \dots \leq t_N$

general attempt #1

$t_{\text{current}} = y$; What is Σ ?

$$0 < y < t_1 \Rightarrow \Sigma = 0$$

$$t_N < y \Rightarrow \Sigma = \begin{cases} t_1 : \Sigma_1 \\ \vdots \\ t_N : \Sigma_N \end{cases} \quad \text{all } y \text{ timer.}$$

$$\Sigma_i = \frac{y - t_i}{X} + 1$$

Step function

$$h(0) = 1$$

$\Sigma(t)$: 1. $m = \max i : t_i \leq t$. in that case

$$\Sigma(t) = \sum_{i=1}^m \Sigma_i(t) = \sum_{i=1}^m \frac{t - t_i}{X} + 1$$

$$\Sigma(t) = m + \sum_{i=1}^m \frac{t - t_i}{X}$$

Search interval : N : timer count

X : increment

K : target.

1 assumption: we sort input array asc.

2. max total time
 single timer $t_1 = 10^9$

$$X = 10^3 ; K = 10^9$$

$$\text{total time} : 10^9 \cdot 10^3 = 10^{18}$$

3 Σ_{max} is long (8 bytes)

memory limit in longs is: 33M

4 stronger assumption:

if $t_i > t_j$ and $(t_i - t_j) \% K = 0$
 we can ignore it

$$t_i \bmod K = t_j \bmod K$$

we can maintain remainder array and keep the lowest timer

at $t_N - \max$: all timers start working

$$\begin{array}{ccccccc} t_N & t_N + X & t_N + 2X & \dots \\ N & 2N & 3N & \dots \end{array}$$

$$kN \geq K \quad ; \quad k \geq \frac{K}{N} \quad ; \quad k_{\max} = \text{ceil} \left(\frac{K}{N} \right)$$

$$t_{k_{\max}} = t_N + (k_{\max} - 1)X = t_N + \frac{K}{N} X$$

$$t_{k_{\max}} 1: \quad 6 + \frac{50}{6} = 6 + 8 = 14$$

$$t_{k_{\max}} 2: \quad 22 + \frac{12 \cdot 7}{5} = 22 + 16 = 38$$
