



Intro to Rust Lang

Ownership

Revisited

Ownership Revisited

Today, we'll provide another way of thinking about ownership:

- Not just avoiding compile errors, but uncovering:
 - How the borrow checker works
 - The purpose of the borrow checker
- How do we write safer code by working *with* the borrow checker?

The Rules

At the beginning of this course, we learned two sets of rules...

- Ownership rules
- Borrowing rules

Rules of Ownership

- Each value in Rust has an *owner*
- A value can only have one owner at a time
- When the owner goes out of scope, the value will be *dropped*

Rules of Borrowing

- At any given time, you may have either
 - One mutable (exclusive) reference to data
 - Any number of immutable (shared) references to the same data
- There can never be dangling references

The Catch

Getting code to compile is one thing. Understanding why is another..

- Sometimes we follow the rules blindly
 - When we break the rules, we may not fully understand why it is a problem in the first place
- The compiler can be overly cautious
 - Rejects code that seems safe
 - Makes us prove safety, even when we "know" it's safe

Today's Objective

Today we're going to address these questions:

- How do ownership rules prevent memory safety issues?
- What makes the borrow checker reject seemingly safe code?

Defining Safety

What is safety?

- Safety is the absence of *undefined behavior*

Defining Unsafe

However, undefined behavior / unsafety can mean many things.



Warning: The following list is not exhaustive; it may grow or shrink. There is no formal model of Rust's semantics for what is and is not allowed in unsafe code, so there may be more behavior considered unsafe. We also reserve the right to make some of the behavior in that list defined in the future. In other words, this list does not say that anything will *definitely* always be undefined in all future Rust version (but we might make such commitments for some list items in the future).

Please read the [Rustonomicon](#) before writing unsafe code.

- Definition in the [Rust Reference](#) is much longer...

Defining Unsafe

Simplification for today: **Unsafety \Rightarrow Invalid Memory Access**

Unsafety ⇒ Invalid Memory Access

Memory access can be unsafe if we access memory that is:

- Deallocated
 - Ownership rules prevent this
- Overwritten by "someone else"
 - Borrowing rules prevent this

Unsafety ⇒ Invalid Memory Access

Memory access can be unsafe if we access **deallocated** or **overwritten** memory.

- Immutable global variables are trivially safe
 - `static` variables are read-only and valid for program's lifetime
- Today, we'll focus on *local* variables

Local Variables

Local variables live in a function's **stack frame**.

The stack frame:

- Contains everything needed for the function to run
- Is allocated on function call
- Is deallocated on function return

The Stack: Local Variables

Here is a representation of `main`'s stack frame.

```
fn main() {  
    let x = 1;  
}
```

Stack

main

x	1
---	---

The Stack: Local Variables

Now we call `my_function`, constructing its stack frame.

```
fn main() {  
    let x = 1;  
    my_function(x);  
}  
  
fn my_function(arg: i32) {  
    let y = 2;  
    let z = 3;  
}
```

Stack

main

x	1
---	---

my_function

arg	1
y	2

The Heap

Big Data

What if instead of an integer on the stack (`x = 1`)...

```
fn main() {  
    let x = 1;  
    my_function(x);  
}
```

Stack

main



Big Data

We have a 15 GB array?

```
fn main() {  
    let beef =  
        [0xDEADBEEF; HUGE_NUMBER];  
  
    my_function(beef);  
}
```

Stack

main

beef	3735928559	3735928559	37359285
------	------------	------------	----------

- 15 GB = your Google Drive storage



Storage (79% full)



11.95 GB of 15 GB used

Big Data

```
fn my_function(arg: [u32; HUGE_NUMBER]) {  
    <-- snip -->  
}
```

When we call `my_function`, we need to:

- Allocate enough space in the stack frame
- Copy all 15 GB of `0xDEADBEEF`'s...

Stack

main

beef	3735928559	3735928559	3735928559
------	------------	------------	------------

my_function

arg	3735928559	3735928559	3735928559
-----	------------	------------	------------

Big Data

Imagine being required to recreate `beef` on every single stack frame.

```
let beef = [0xDEADBEEF; 2_000_000_000];

my_function(beef);
```

- Unsustainable!



Motivating the Heap

We probably want to keep our `beef` array around for longer than a single function call.

- We can say that it is **long-lived** data
- We want other functions to use this array, instead of just a single stack frame
- How do we persist this data across function calls?

The Stack?

Instead of storing our array buffer
on the stack...

Stack

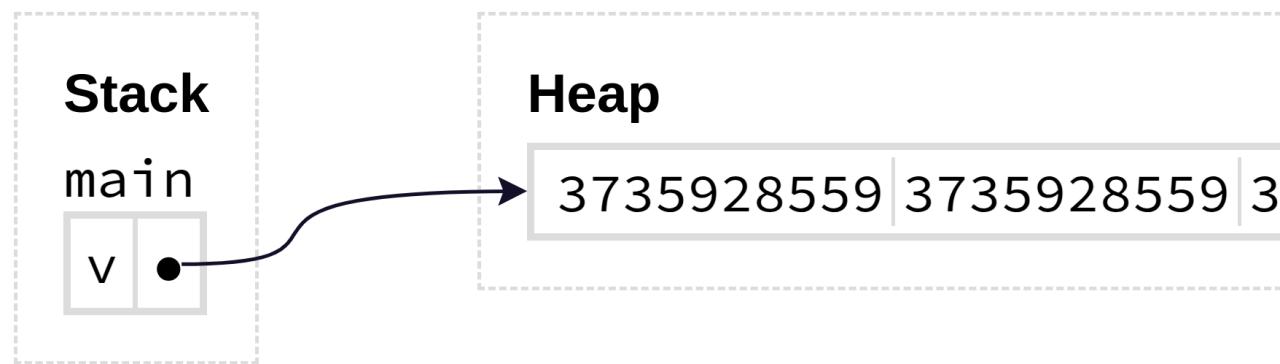
main

beef	3735928559	3735928559	37359285
------	------------	------------	----------

The Heap

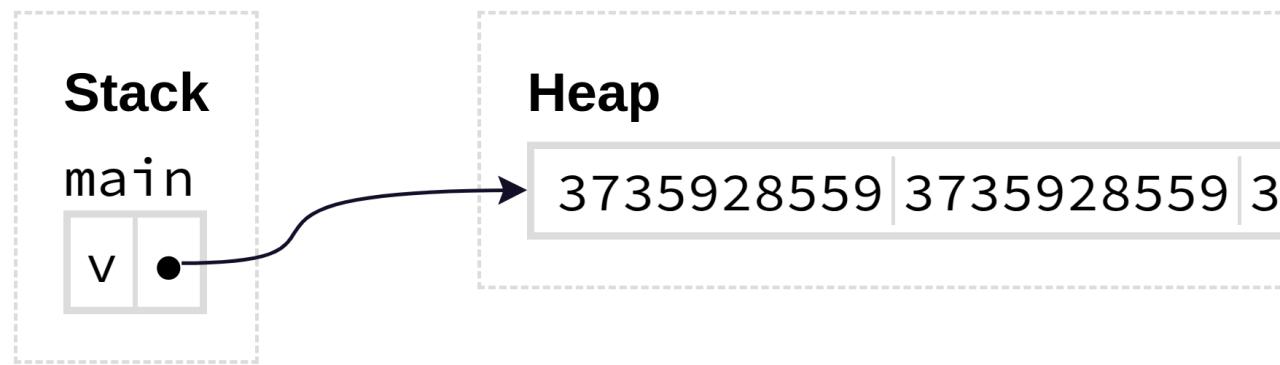
Instead of storing our array buffer
on the stack...

Let's put it on the heap!



The Heap

- If the data lives in the heap...
- The **pointer** lives on the stack



Box<T>

The simplest form of heap allocation is `Box<T>`.

Moving a value from stack to heap:

```
let val: u8 = 5;
let boxed: Box<u8> = Box::new(val);
```

- Can access value by dereferencing box as `*boxed`
- Value is automatically dropped when `boxed` goes out of scope

Box<T>

Let's put our `beef` array in a `Box`:

```
fn main() {
    // Renamed to `v`.
    let v = Box::new([0xDEADBEEF; HUGE_NUMBER]);
    my_function(v);
}

fn my_function(arg: Box<[u32]>) {
    <-- snip -->
}
```

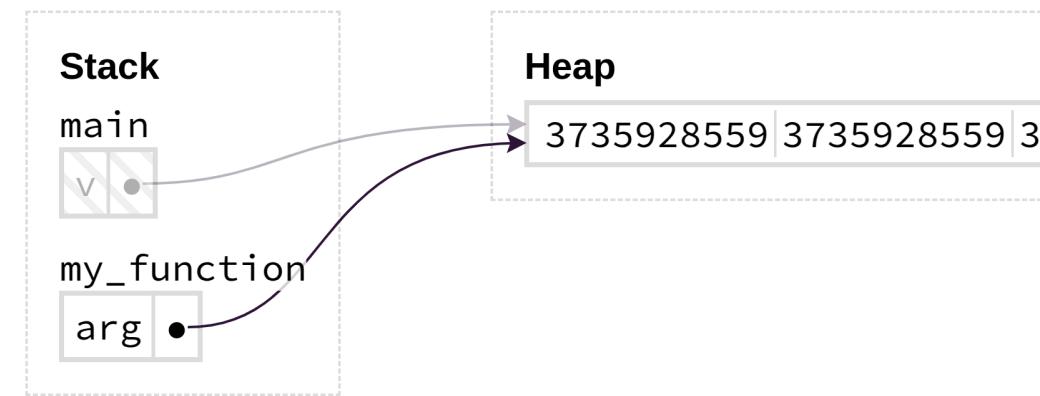
- In reality, this allocates `beef` on the stack and then copies it to the heap
 - Use `Vec<T>` and convert to a boxed slice instead!



The Heap

When we call `my_function`, we can copy the *pointer* into `arg`!

```
let v =  
    Box::new([0xDEADBEEF; HUGE_NUMBER]);  
  
my_function(beef);
```

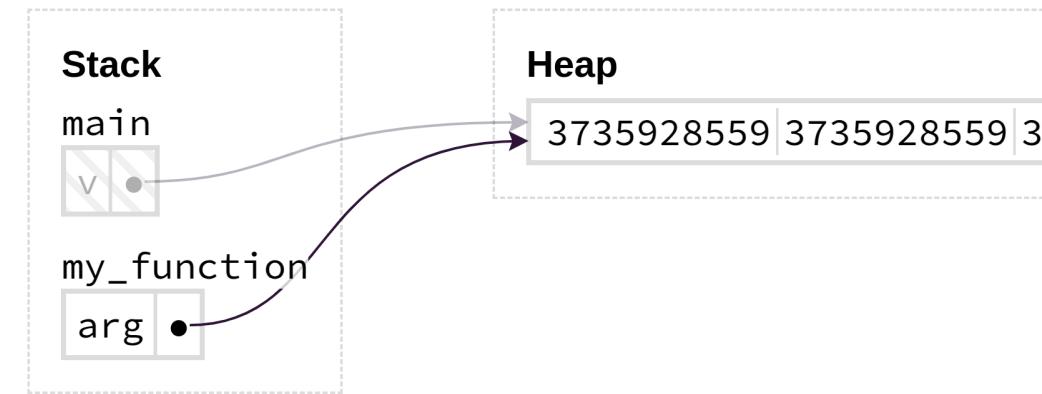


The Heap

Before: 15 GB per array

After: 15 GB + 8 bytes per pointer

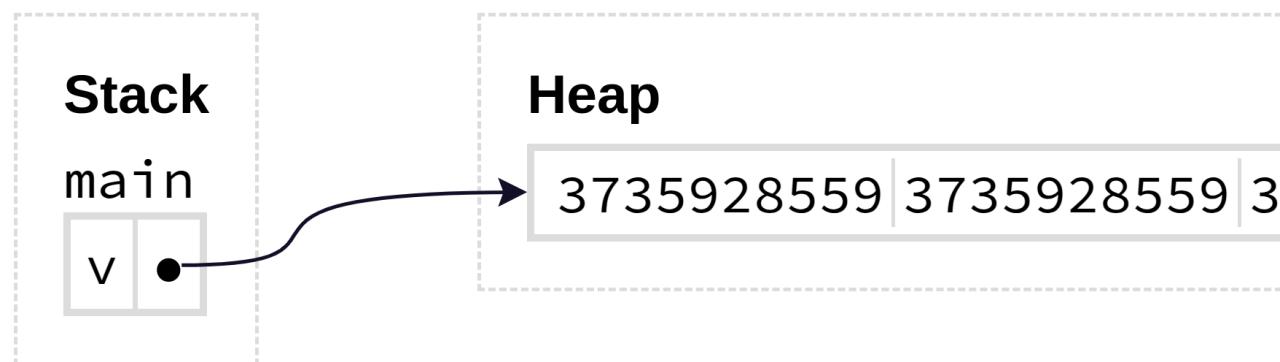
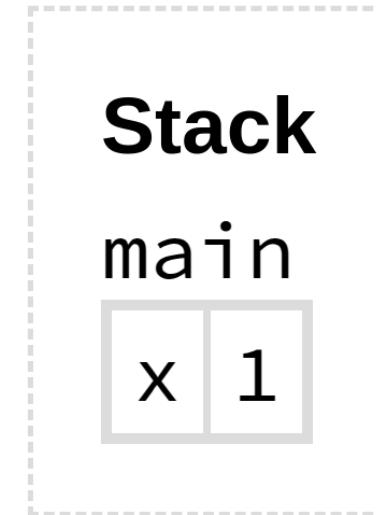
```
let v =  
    Box::new([0xDEADBEEF; HUGE_NUMBER]);  
  
my_function(beef);  
my_function(beef);
```



Recap: Stack vs. Heap

Variable placement:

- **Stack-allocated:** Data lives on the stack
- **Heap-allocated:** Data lives on the heap, the **pointer** on stack



Recap: Stack vs. Heap

Comparison	Stack	Heap
Manages	Scalar data + Pointers	Dynamically-sized / long-lived data
Allocated on	Function call	Programmer request
Deallocated on	Function return	???

Motivating Ownership

Recall that accessing **deallocated** memory is unsafe.

Motivating Ownership

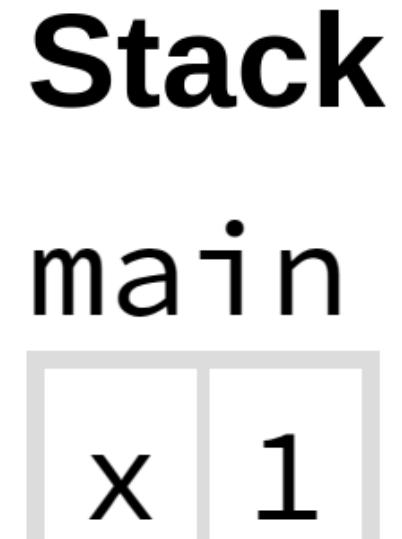
When is memory deallocated?

- Stack: deallocated when the function returns
 - Valid, unless dangling pointer 
 - We'll discuss more in the upcoming Lifetimes lecture...
- Heap: deallocated when ???
 - 
 - How can we be confident that heap memory is deallocated safely?

Motivating Ownership

Recall the behavior of local variables on the stack:

- Local variable lives in the function's **stack frame**
- Allocated on function call
- Deallocated on function return
 - Sound familiar?



Motivating Ownership

What if we say that data is "owned" by the stack frame?

- One stack frame (owner) per variable
- Data is dropped on function return
- Very similar to our previous model of ownership!

Stack
main

x	1
---	---

Rules of Ownership

Under this alternate ownership model, owners are stack frames:

- Each value in Rust has an *owner*
 - Owner is the *stack frame*
- A value can have only one owner at a time
 - Variables can only be in one stack frame
- When the owner goes out of scope, the value will be *dropped*
 - When the function returns, the stack frame is cleaned up!

Ownership of Closures

Let's re-examine **closures** again using this new ownership model:

- What does the `move` keyword really do?
- Why are captured values dropped when they are?

Ownership of Closures

When is `my_str` dropped? Who has ownership of it?

```
let my_str = String::from("x");

let take_and_give_back = move || { my_str };

assert_eq!(take_and_give_back(), "x");
```

- In `take_and_give_back`, `my_str` is dropped the first time the closure is called
 - Can only be called once

Closure Internals

When we create a closure...

```
let do_nothing_closure = |_x| {};
```

Think of it as a struct with an associated function:

```
struct Closure;

impl Closure {
    //           vvvvv Notice the immutable reference to `self`!
    pub fn call(&self, _x: &str) -> () {}
}
```

Closure Internals

The `move` keyword tells the closure to take ownership of values from its environment.

```
let take_and_give_back = move || { my_str };

// The `move` keyword tells compiler to put `my_str` in this `Closure`.
struct Closure {
    my_str: String,
}

impl Closure {
    //           vvvv Notice the owned `self` type!
    pub fn call(self) -> String {
        return self.my_str;
    }
}
```



Closure Internals

Then our code is equivalent to

```
let my_str = String::from("x");

let take_and_give_back = Closure { my_str };
//                                     ^^^^^^ `my_str` is moved!

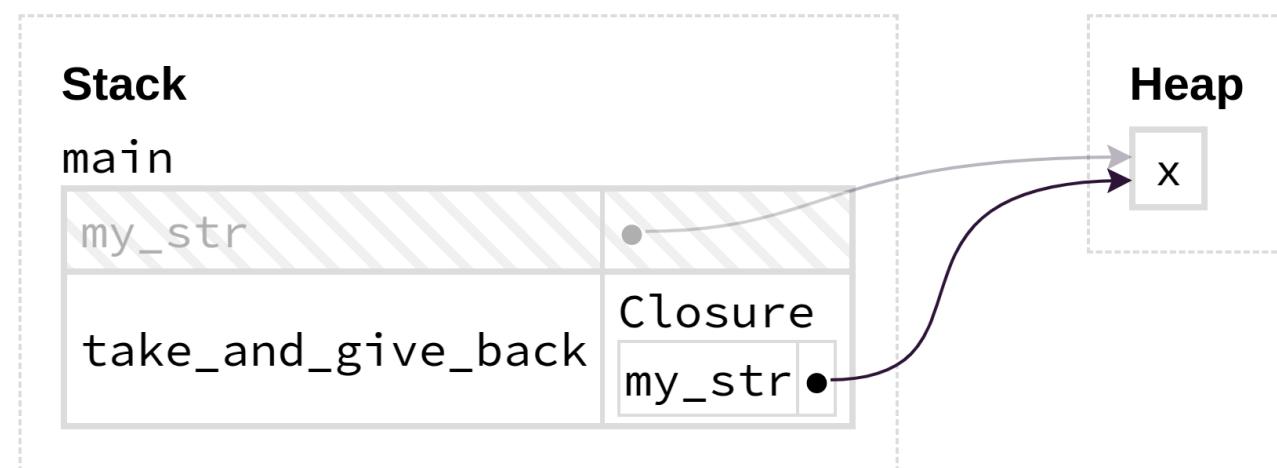
let my_returned_str: String = take_and_give_back.call();
```

- What happens when we `call` on the `Closure`?
 - *Think about the stack frames*

Closure Example

First, `my_str` is moved into our Closure.

```
let my_str = String::from("x");  
  
let take_and_give_back =  
    Closure { my_str };
```



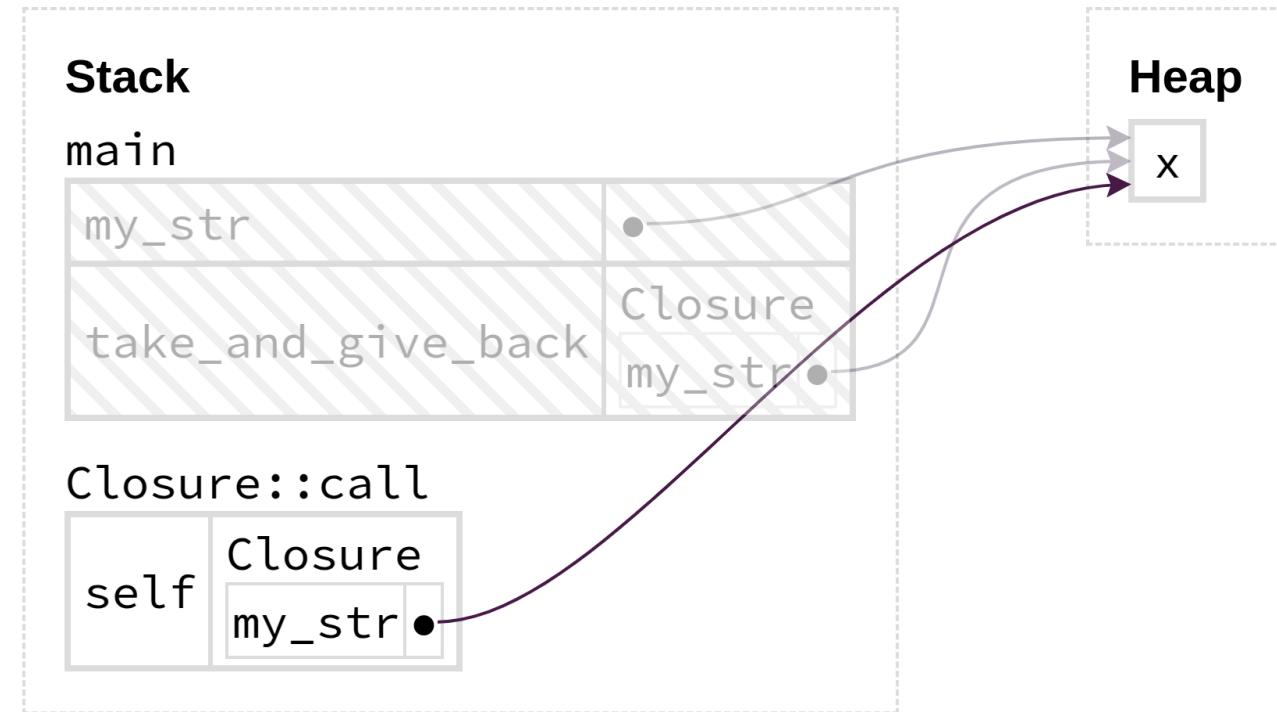
Closure Example

Next, we call our closure, which gives ownership of `my_str` to `Closure::call`'s stack frame.

```
let my_str = String::from("x");

let take_and_give_back =
    Closure { my_str };

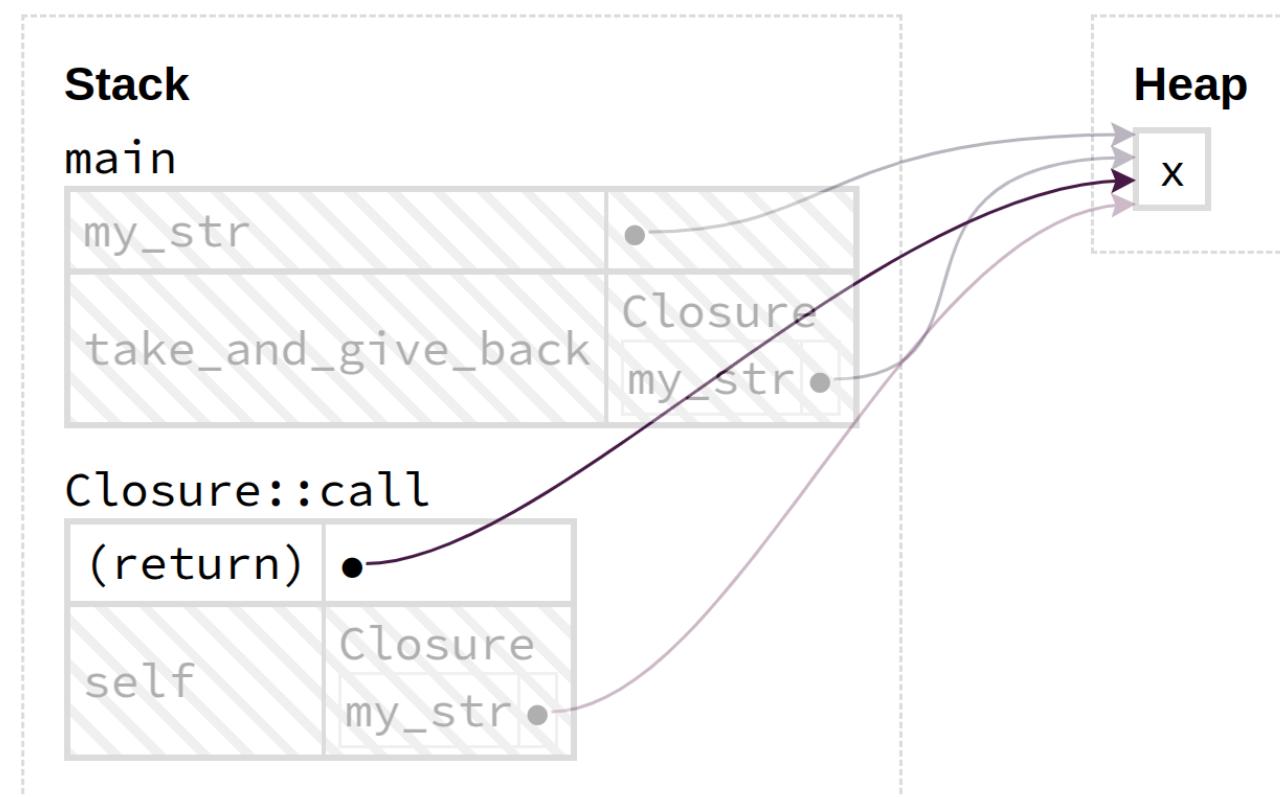
let my_returned_str =
    take_and_give_back.call();
```



Closure Example

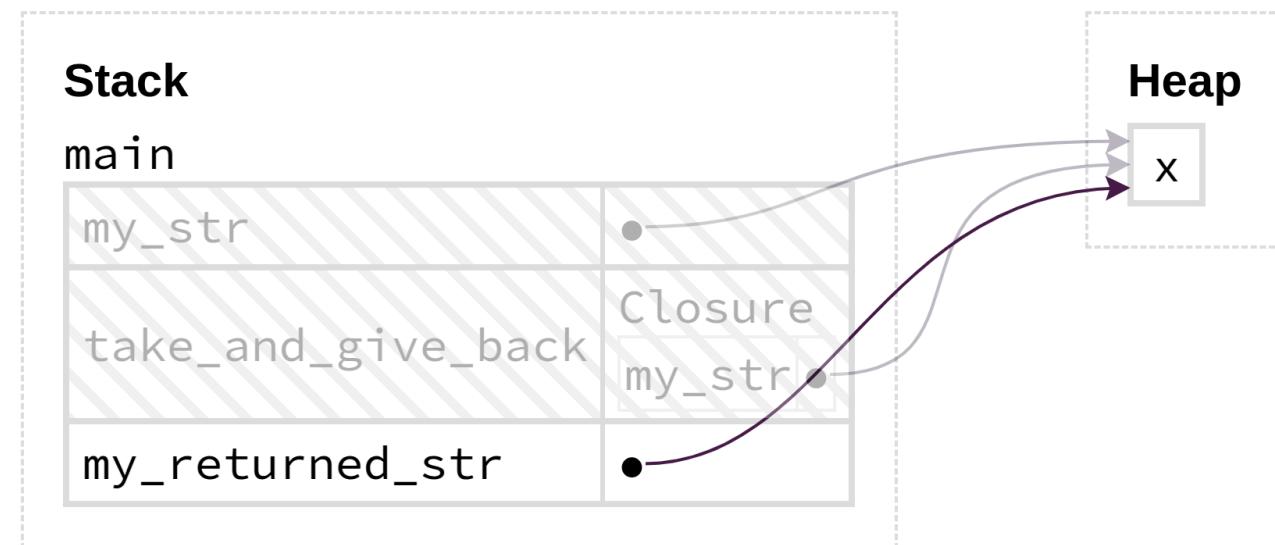
`Closure::call` gives ownership back to `main`'s stack frame...

```
pub fn call(self) -> String {  
    // Gives ownership back!  
    return self.my_str;  
}
```



Closure Example

- Closure's `my_str` is invalidated
- `my_str` is moved out of Closure's "body"
 - This is why it can only be called once!



Recap: Closure Internals

- New way of thinking about ownership
 - Owners are stack frames
- A closure is really a function that stores ("captures") values in a struct
 - Ways to capture values:
 - **Taking ownership:** Store the value in the struct, via `move` keyword
 - **Borrowing:** Store a reference to the value in the struct

Motivating Borrowing Rules

- Recall that accessing **overwritten** memory is unsafe

Vector Pop

Suppose we want to write this code.

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3]; // Get a reference to the last element  
  
v.pop(); // Remove the last element in `v`  
  
println!("{}", x); // What is `x`?
```



- What do you think the compiler will say?

Vector Pop

```
error[E0502]: cannot borrow `v` as mutable because it is also borrowed as immutable
--> src/main.rs:6:5
|
4     let x = &v[3]; // Get a reference to the last element
                  - immutable borrow occurs here
5
6     v.pop(); // Remove the last element in `v`
              ^^^^^^ mutable borrow occurs here
7
8     println!("{}", x); // What is `x`?
                      - immutable borrow later used here
```

- `x` is invalid! `&v[3]` could now be any value \Rightarrow undefined behavior
- We cannot mutate a value that someone else is borrowing

Vector Push

What if instead of removing the last element, we *add* an element to the end?

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3]; // Get a reference to the last element  
  
v.push(5); // Instead of popping, let's push!  
  
println!("{}", x); // What is `x`?
```



- Surely nothing will happen to `x` this time?

Vector Push

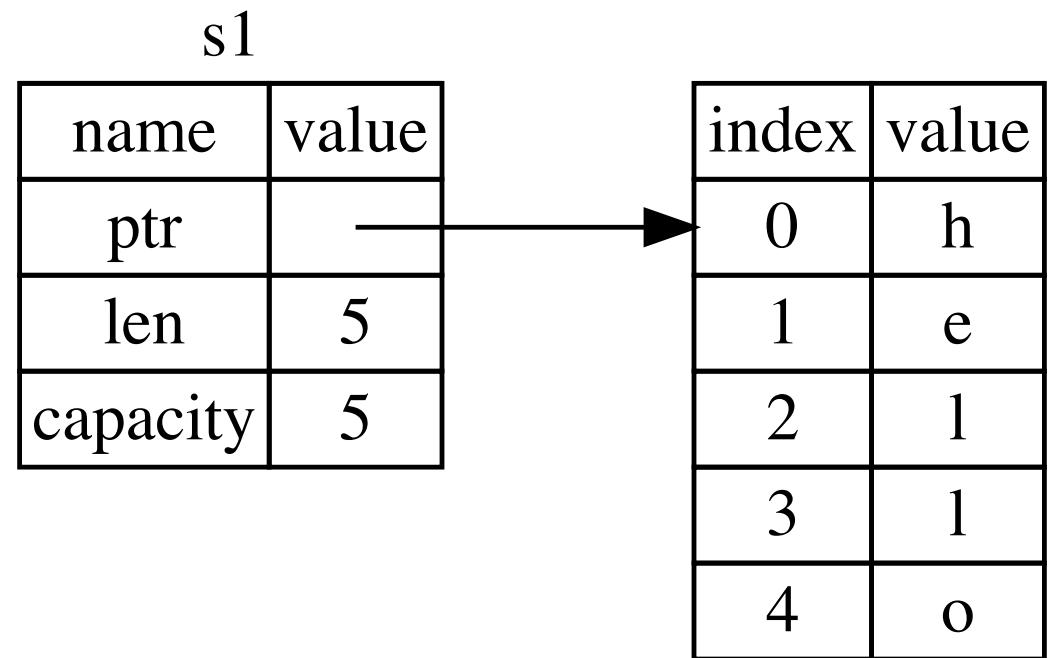
Why isn't this okay???

```
error[E0502]: cannot borrow `v` as mutable because it is also borrowed as immutable
--> src/main.rs:6:5
4     let x = &v[3]; // Get a reference to the last element
                  - immutable borrow occurs here
5
6     v.push(5); // Instead of popping, let's push!
                 ^^^^^^^^^^ mutable borrow occurs here
7
8     println!("{}", x); // What is `x`?
                  - immutable borrow later used here
```

Vector Layout

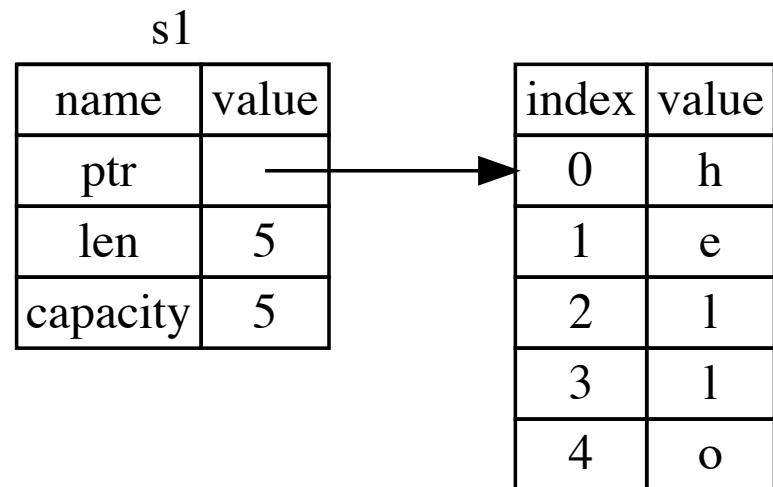
Recall that vectors are *dynamic arrays*.

- This is technically a `String`, but recall that `String` is implemented with a `Vec<u8>`



Mutating Vectors

- What if pushing 5 onto v triggers a resize?
- Resizing means:
 - Allocate new memory for v
 - Copy data to new location
 - **Deallocate old memory location**
- x would no longer point to valid memory!



Mutating Vectors

```
error[E0502]: cannot borrow `v` as mutable because it is also borrowed as immutable
--> src/main.rs:6:5
|
4     let x = &v[3]; // Get a reference to the last element
                  - immutable borrow occurs here
5
6     v.push(5); // Instead of popping, let's push!
                 ^^^^^^^^^^ mutable borrow occurs here
7
8     println!("{}", x); // What is `x`?
                      - immutable borrow later used here
```

Even though this error may seem unreasonable, the borrow checker is actually preventing you from making a hard-to-find mistake!



We Know Better...

What if you knew that this `push` doesn't resize?

- You as the programmer have vetted the implementation of `push`
- You can *guarantee* that resizing only happens with more elements

Sneak Peek: unsafe

You can use an `unsafe` block to tell the compiler that you know better.

```
let mut v: Vec<i32> = vec![1, 2, 3, 4];
// SAFETY: We know that `v` has 4 elements, so adding `3 * size_of::<i32>()` ``
// cannot overflow (wrap around the address space).
let p: *const i32 = unsafe { v.as_ptr().add(3) };

v.push(5);

// SAFETY: We have checked that a resize will never happen with only
// 5 elements, so this dereference is safe.
let elem: i32 = unsafe { *p };
println!("{}", elem);
```

- Think of `unsafe` blocks as "trust me bro" blocks
- We will talk about `unsafe` in a few weeks!

Note that this is what the `unsafe` code should *really* look like:

```
let mut v: Vec<i32> = vec![1, 2, 3, 4];

// SAFETY: We know that `v` has 4 valid elements, which means that the pointers at
// offsets +1, +2, and +3 are all valid pointers that point to values of type `i32`.
// This also means it cannot be the case that adding `3 * size_of::<i32>()` to
// `v.as_ptr()` overflows, otherwise that last element could not even exist in the
// first place. With these two guarantees, we fulfill `add`'s safety contract.
let p: *const i32 = unsafe { v.as_ptr().add(3) };

v.push(5);

// SAFETY: We showed above that `p` was a valid pointer to an `i32` value. We have
// also checked in the code of `Vec::push` that a resize and reallocation
// **cannot** happen when there are only 5 elements. So since there is no
// reallocation, and `v` is still in scope (so the memory has not been freed), this
// dereference of `p` to an `i32` value is valid.
let elem: i32 = unsafe { *p };

println!("{}", elem);
```

`unsafe` vs. Borrow Checking

You should *never* resort to using `unsafe` just to get past the borrow checker.

- `unsafe` should be used sparingly and intentionally
- You must understand *why* you need to bypass the borrow checker
- Therefore, you *must* understand the borrow checker!

The Borrow Checker

The Borrow Checker prevents you from writing unsafe code.

This leads to some questions:

- How do I know if my program is unsafe?
 - How did the borrow checker conclude this?
- How can I tell if my program is safe even if the borrow checker rejects it?

Unveiling the Borrow Checker

"His blade works so smoothly that the ox does not feel it." - The Dextrous Butcher

- Understand the borrow checker, and you'll speak its language fluently:
 - "My program is unsafe, and here's how I'll fix it"
 - And occasionally...
 - "My program is actually safe, let me tell you why"

Permissions

Permissions of Places

Denote the left side of assignments as **places**.

```
let x = &v[3];  
// ^ place
```

- The borrow checker checks the permissions of **places**

Permissions of Places

Places include:

- Variables, like `a`
- Dereferences of places, like `*a`
- Array accesses of places, like `a[0]`
- Fields of places, like `a.0`, `a.field`
- Any combination of the above, like `*a.x[i].y`

Permissions of Variables

When declared, a variable has the permissions:

- Read: can be copied
- Write: can be mutated (if declared with `mut`)
- Own: can be moved or dropped

References and Permissions

- Variables have the permissions Read (R), Write (W), and Own (O)
- Using references can *temporarily remove these permissions*

Example: Immutable References

Let's revisit our vector pop example.

```
let mut v = vec![1, 2, 3, 4];
```

Place	R	W	O
v	?	?	?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];
```

Place	R	W	O
v	?	?	?

We declare `v`, giving it:

- ?
- ?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4]; // <-
```

Place	R	W	O
v	+R	?	+O

We declare `v`, giving it:

- R, O due to variable declaration
- ?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4]; // <-
```

Place	R	W	O
v	+R	+W	+O

We declare `v`, giving it:

- R, O due to variable declaration
- W because `mut`

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <-
```

Place	R	W	O
v	R	W	O
x	?	-	?

When we create a reference `x` to `v`, we:

- ?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <- x gets R, O
```

Place	R	W	O
v	R	W	O
x	+R	-	+O

When we create a reference `x` to `v`, we:

- Give `x` R, O due to variable declaration
 - We can think of `v` "giving" R to `x`
 - `x`'s permissions are for the *reference*, not the data it is referring to

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <-
```

Place	R	W	O
v	R	W?	O?
x	R	-	O

Creating a reference `x` to `v` also changes the permissions of `v`:

- ?
- ?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <- v loses W
```

Place	R	W	O
v	R	W?	-
x	R	-	O

Creating a reference `x` to `v` also changes the permissions of `v`:

- Removes W
- ?

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <- v loses W, O
```

Place	R	W	O
v	R	-	-
x	R	-	O

Creating a reference `x` to `v` also changes the permissions of `v`:

- Removes W
- Removes O

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3];  
  
println!("{}", *x); // <-
```

Place	R	W	O
v	R	-	-
x	R	-	O
*x	R	-	-

We can access what our reference `x` is referring by dereferencing it as `*x`.

- `*x`'s permissions are different from `x`'s!
- Can only dereference if `*x` has R permissions
- `*x` can only have R if `v` has R

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3];  
  
println!("{}", *x); // <-
```

Place	R	W	O
v	R	-	-
x	R	-	O
*x	R	-	-

We can no longer mutate `v`, since we created a reference `x` to it.

When does `v` regain W, O? Either:

- All references become unused (Case 1)
- Mutate `v` before *any* reference is used (Case 2)
 - Revokes permissions of references



Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3];  
  
v.pop(); // <- v revokes x's permissions
```

Place	R	W	O
v	R	+W	+O
x	-	-	-
*x	-	-	-

This `v.pop()` is safe (Case 2).

- `v` requests W before any references are used (Case 2)
 - `v` regains W, O, *revokes permissions of all references*
 - Temporarily: `x` loses R and O, `*x` loses R

Example: Immutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3];  
  
println!("{}", *x); // Requires R on *x  
  
// x and *x lose all permissions  
  
v.pop(); // <- v regains W and O
```

Place	R	W	O
v	R	+W	+O
x	-	-	-
*x	-	-	-

This `v.pop()` is also safe (Case 1)!

- `v` requests W after all references become unused (Case 1)
 - Permanently: `x` loses R and O, `*x` loses R
 - `v` regains W, O

Example: Immutable References

However, we cannot access `*x` anymore, as its permissions have been revoked.

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &v[3];  
  
v.pop(); // Revokes permissions!  
  
// THIS DOES NOT COMPILE!!!  
println!("{}", *x); // Requires R on *x
```

Place	R	W	O
v	R	W	O
x	R	-	-
*x	-	-	-

- This code causes an error because we don't have permissions on `*x`

Recap: Immutable References

- Declaring a variable `v` gives it R, O permissions, W if `mut`
- Creating an immutable reference `x` to `v`
 - Gives `x` R, O permissions
 - Removes `v`'s W, O permissions
- Permissions are restored when either:
 - References become **unused**
 - We mutate `v` *before* any reference is used

Mutable References

- `x` and `*x` have different permissions
 - Notice how revoking permissions removes R from `*x`, but *keeps* R on `x`
 - We can create as many references as we want...
 - We just can't access them without the correct permissions
- Mutable references further illustrate this

Example: Mutable References

```
let mut v = vec![1, 2, 3, 4];  
let x = &v[3]; // <-
```

Place	R	W	O
v	R	-	-
x	R	-	O
*x	R	-	-

Recall that when we create an immutable reference `x = &v[3]` :

- `v` loses W and O permissions
 - `v` gives `x` R
- `x` gains R and O permissions
- `*x` gains R permissions

Example: Mutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &mut v[3]; // <-  
//      ^^^^^
```

Place	R	W	O
v	R?	-	-
x	R	-	O
*x	R	-?	-

However, when `x` is a mutable reference:

- ?
- ?

Example: Mutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &mut v[3]; // <-  
//      ^^^^^
```

Place	R	W	O
v	-	-	-
x	R	-	O
*x	R	-?	-

However, when `x` is a mutable reference:

- `v` loses *all* permissions, including R
- ?

Example: Mutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &mut v[3]; // <-  
//      ^^^^^
```

Place	R	W	O
v	-	-	-
x	R	-	O
*x	R	W	-

However, when `x` is a mutable reference:

- `v` loses *all* permissions, including R
- `*x` (*not* `x`) gains W permissions

Example: Mutable References

```
let mut v = vec![1, 2, 3, 4];  
  
let x = &mut v[3]; // <-  
//      ^^^^^
```

Place	R	W	O
v	-	-	-
x	R	-	O
*x	R	W	-

- v loses *all* permissions, including R
 - Prevents creation of other references (both mutable and immutable)
 - Avoids simultaneous **aliasing** and mutation
- *x (*not* x) gains W permission
 - We can write to the data, but we can't reassign x

Recap: Mutable References

An immutable reference `x` of `v`:

- Removes W and O permissions for `v` (keeps R)
- `*x` can only take R if `v` has R

A mutable reference `x` to `v`:

- Removes *all* permissions for `v` (including R)
 - Prevents creation of any other references
- `*x` (not `x`) gains W permission

Fixing Programs

Arrays and Slices

Suppose we have a vector of numbers:

```
let mut v = vec![1, 2, 3, 4];
```

Arrays and Slices

We want to take this number 2 ...

```
let mut v = vec![1, 2, 3, 4];  
// ^
```

Arrays and Slices

We want to take this number `2` ...and add it to the number in the first index.

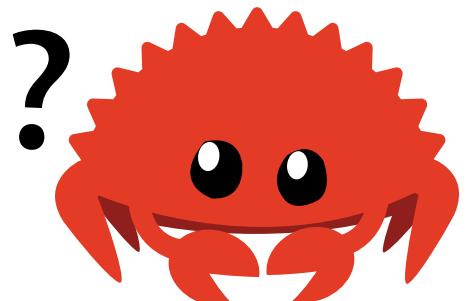
```
let mut v = vec![1, 2, 3, 4];  
//           ^
```



Arrays and Slices

Here is a seemingly reasonable solution:

```
let mut v = vec![1, 2, 3, 4];  
  
let slot1 = &mut v[0];  
  
let slot2 = &v[1];  
  
*slot1 += *slot2;
```



Arrays and Slices: Problem

```
error[E0502]: cannot borrow `v` as immutable because it is also borrowed as mutable
--> src/main.rs:9:18
8     let slot1 = &mut v[0];
                  - mutable borrow occurs here
9     let slot2 = &v[1];
                  ^ immutable borrow occurs here
10    *slot1 += *slot2;
                 ----- mutable borrow later used here
= help: use `<slice>.split_at_mut(position)` to obtain
      two mutable non-overlapping sub-slices
```

- Let's break down the permissions

Arrays and Slices: Permissions

```
let mut v = vec![1, 2, 3, 4];  
  
let slot1 = &mut v[0]; // <-  
  
let slot2 = &v[1];  
  
*slot1 += *slot2;
```

Place	R	W	O
v	-	-	-
*slot1	R	W	-

Recall that when we create a mutable reference `slot1 = &mut v[0]`:

- `v` loses all permissions
- `*slot1` gains R, W permissions

Arrays and Slices: Permissions

```
let mut v = vec![1, 2, 3, 4];  
  
let slot1 = &mut v[0];  
  
let slot2 = &v[1]; // <-  
  
*slot1 += *slot2;
```

Place	R	W	O
v	-	-	-
*slot1	R	W	-
*slot2	?	?	?

Recall that when we create an immutable reference `slot2 = &v[1]` :

- `v` loses W and O permissions (didn't have it anyways)
- `v` gives `x` R since `x` needs R on line 4
 - But `v` doesn't have R!

Arrays and Slices: Permissions

```
let mut v = vec![1, 2, 3, 4];  
  
let slot1 = &mut v[0];  
  
let slot2 = &v[1]; // <-  
  
*slot1 += *slot2; ✗
```

Place	R	W	O
v	-	-	-
*slot1	R	W	-
*slot2	-	-	-

- Mutating `*slot1` requires R, W
 - `*slot1` has both ✓
- Reading `*slot2` requires R
 - `*slot2` doesn't have R ✗
 - v "gave" R to `*slot1` !

Arrays and Slices: Permissions

```
let mut v = vec![1, 2, 3, 4];  
  
let slot1 = &mut v[0];  
  
let slot2 = &v[1]; // <-  
  
*slot1 += *slot2; ❌
```

Place	R	W	O
v	-	-	-
*slot1	R	W	-
*slot2	-	-	-

The main issue here is that the single place `v` represents the *entire* vector.

- Borrow checker does not see each index / element as a different place
- Borrow checker can't know that this code is safe
 - But we (as humans) do!

Fixing a Safe Program

Solution 1: Don't use explicit references.

```
let mut v = vec![1, 2, 3, 4];  
v[0] += v[1];  
println!("{:?}", v);
```

- This works because we mutate only `v[0]`
 - *Program evaluation is right to left*

Fixing a Safe Program

Solution 2: Drop into `unsafe` code.

`split_at_mut` uses `unsafe` under the hood:

```
let mut v = [1, 0, 3, 0, 5, 6];  
  
let (left, right) = v.split_at_mut(2);  
  
assert_eq!(left, [1, 0]);  
assert_eq!(right, [3, 0, 5, 6]);
```

- Divides a mutable slice into two mutable slices at index `mid`
 - `left` contains `[0, mid)`
 - `right` contains `[mid, len)`
- We will talk about this in a few weeks!



Sound vs. Complete

The borrow checker is **sound**, but not **complete**. This means that the borrow checker sometimes can't figure out if your program is safe.

- If you conclude it is actually safe:
 - After reasoning about stack frames
 - After reasoning about permissions
 - Repeating all steps several times
 - Consider *potentially* using `unsafe`
 - And then tell yourself that you probably don't need to use `unsafe`

Ownership Recap

- Ownership rules prevent access to deallocated memory
 - Think of owners as **stack frames**
- Borrow checker checks **permissions of places**
 - References temporarily remove permissions
- The borrow checker is your friend!

Homework 8

- This homework is a Gradescope Quiz!
- 30 questions from the [Brown Rust Book](#)
- Read through chapter 4 on ownership
 - Answer the quiz questions on the web page as you go through it
 - All answers will be revealed after you attempt!
- Each question is worth 5 points, so you don't need to do everything
- Focus on *understanding* rather than the questions themselves

Next Lecture: Lifetimes

Thanks for coming!

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