

## Interview Questions (optional)

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1.

**Social network connectivity.** Given a social network containing  $n$  members and a log file containing  $m$  timestamps at which times pairs of members formed friendships, design an algorithm to determine the earliest time at which all members are connected (i.e., every member is a friend of a friend of a friend ... of a friend). Assume that the log file is sorted by timestamp and that friendship is an equivalence relation. The running time of your algorithm should be  $m \log n$  or better and use extra space proportional to  $n$ .

*Note: these interview questions are ungraded and purely for your own enrichment. To get a hint, submit a solution.*

using the improved version of union find algorithm, call union based on our log file, until we find that the size array after union get to  $n$ . This will tell us that this root tree contains  $n$  element. Which means these user are all connected



**Thank you for your response.**

*Hint: union-find.*



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2.

**Union-find with specific canonical element.** Add a method `find()` to the union-find data type so that `find(i)` returns the largest element in the connected component containing  $i$ . The operations, `union()`, `connected()`, and `find()` should all take logarithmic time or better.

For example, if one of the connected components is  $\{1, 2, 6, 9\}$ , then the `find()` method should return 9 for each of the four elements in the connected components.

We can keep a third array called 'Biggest'. To start with each element is equal to its index. Each time we need to combine two connected component  $p, q$  and they already are root. We update `Biggest[root]` with bigger one of `Biggest[p]` and `Biggest[q]`. Then when we need to `find()` we find its root and return `Biggest[root]`



**Thank you for your response.**

*Hint:* maintain an extra array to the weighted quick-union data structure that stores for each root  $i$  the large element in the connected component containing  $i$ .



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3.

**Successor with delete.** Given a set of  $N$  integers  $S = \{0, 1, \dots, N - 1\}$  and a sequence of requests of the following form:

- Remove  $x$  from  $S$
- Find the *successor* of  $x$ : the smallest  $y$  in  $S$  such that  $y \geq x$ .

design a data type so that all operations (except construction) should take logarithmic time or better.

We keep a status array. Initial all 0. Each time we remove  $x$  from  $S$  we check  $x-1$  and  $x+1$  see if they are already removed from  $S$ . If so we connect  $x$  to  $x-1$  or  $x+1$  respectively. Also we keep the biggest array from previous problem. If  $x+1$  have not been remove we return  $x+1$  other with we return  $\text{Bigget}[\text{root}(x)]+1$

**Thank you for your response.**

Hint: use the modification of the union-find data discussed in the previous question.

