



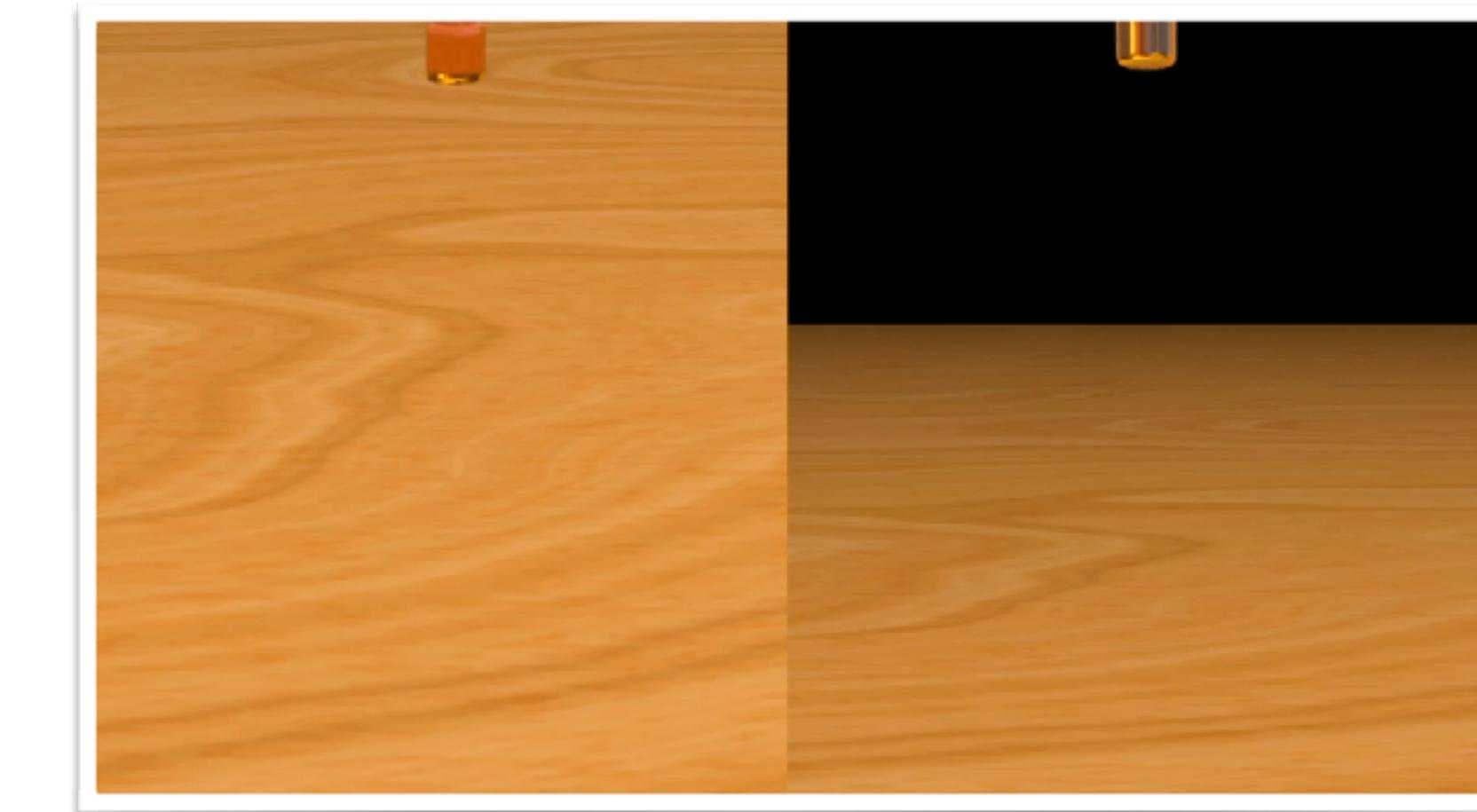
Sparse Paged Grid and its Applications to Adaptivity and Material Point Method

Ming Gao

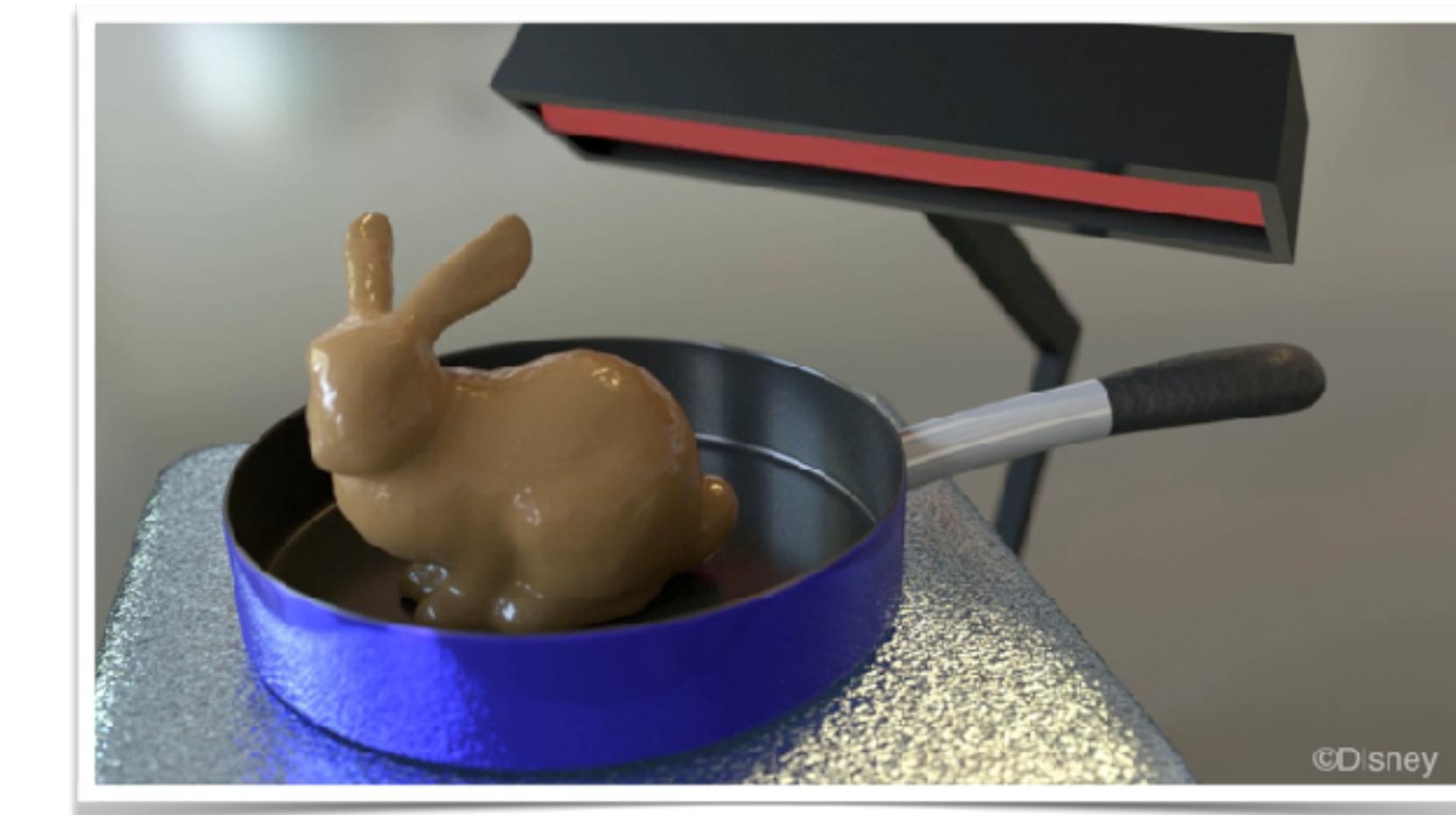
Motivation - expanding feature set



Wet cloth - [Fei et al. 18]

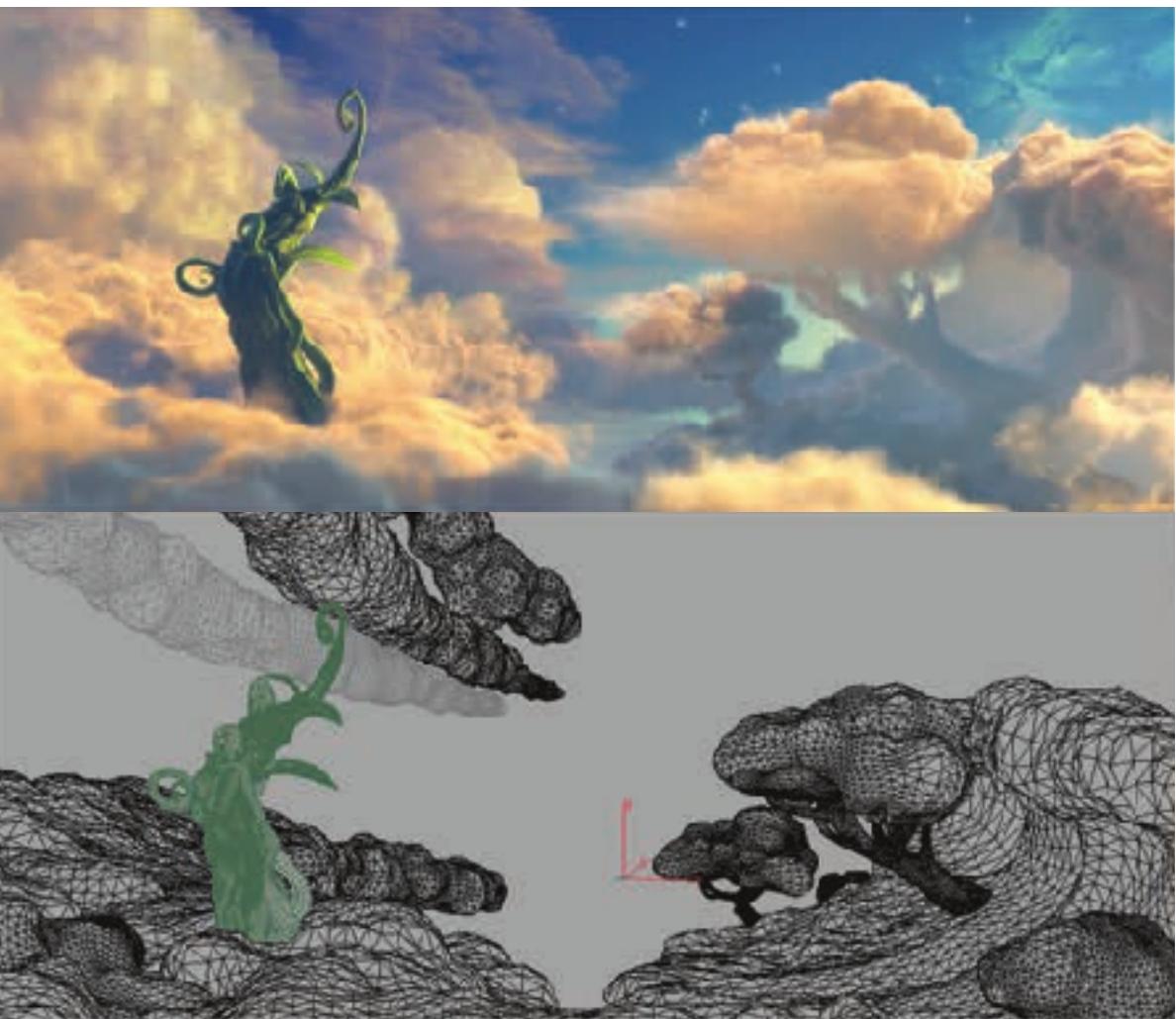


Snow - [Stomakhin et al. 13]



Melting - [Stomakhin et al. 14]

Motivation - accelerating performance



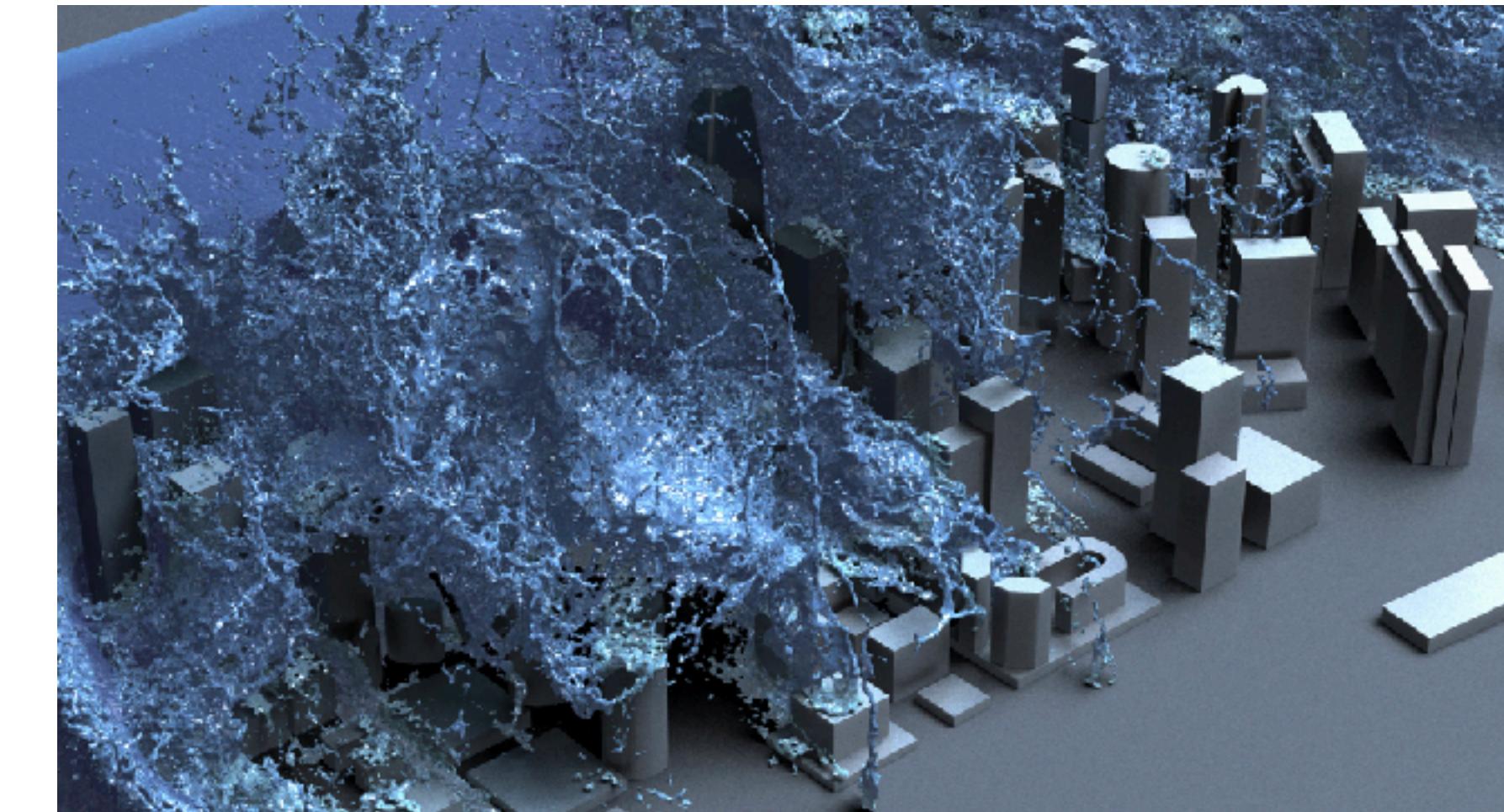
OpenVDB - [Museth et al. 13]



PhysGrid - [Milne et al. 16]



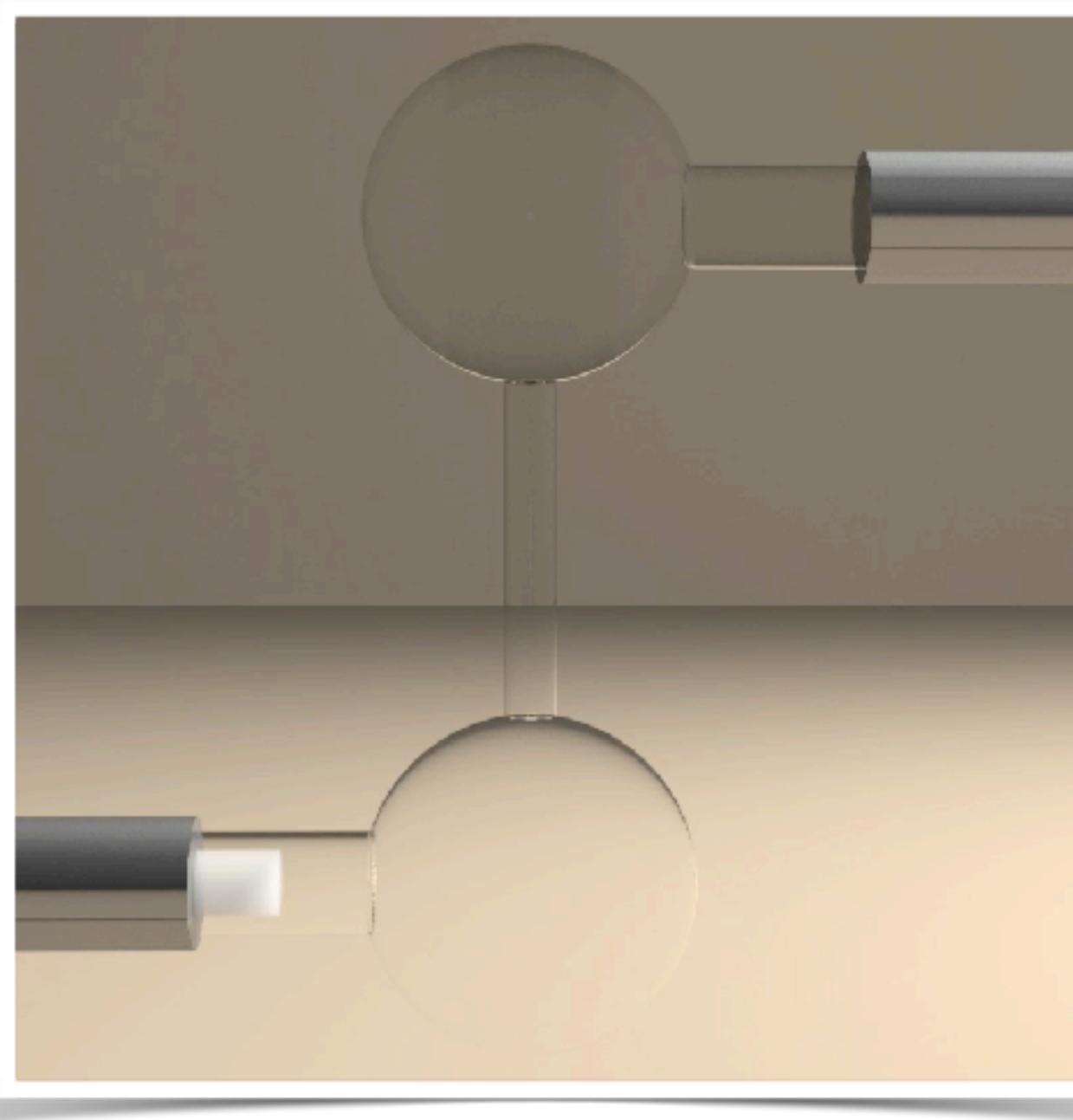
Cloth - [Tang et al. 16]



Fluid - [Wu et al. 18]

Feature breadth vs. optimal performance

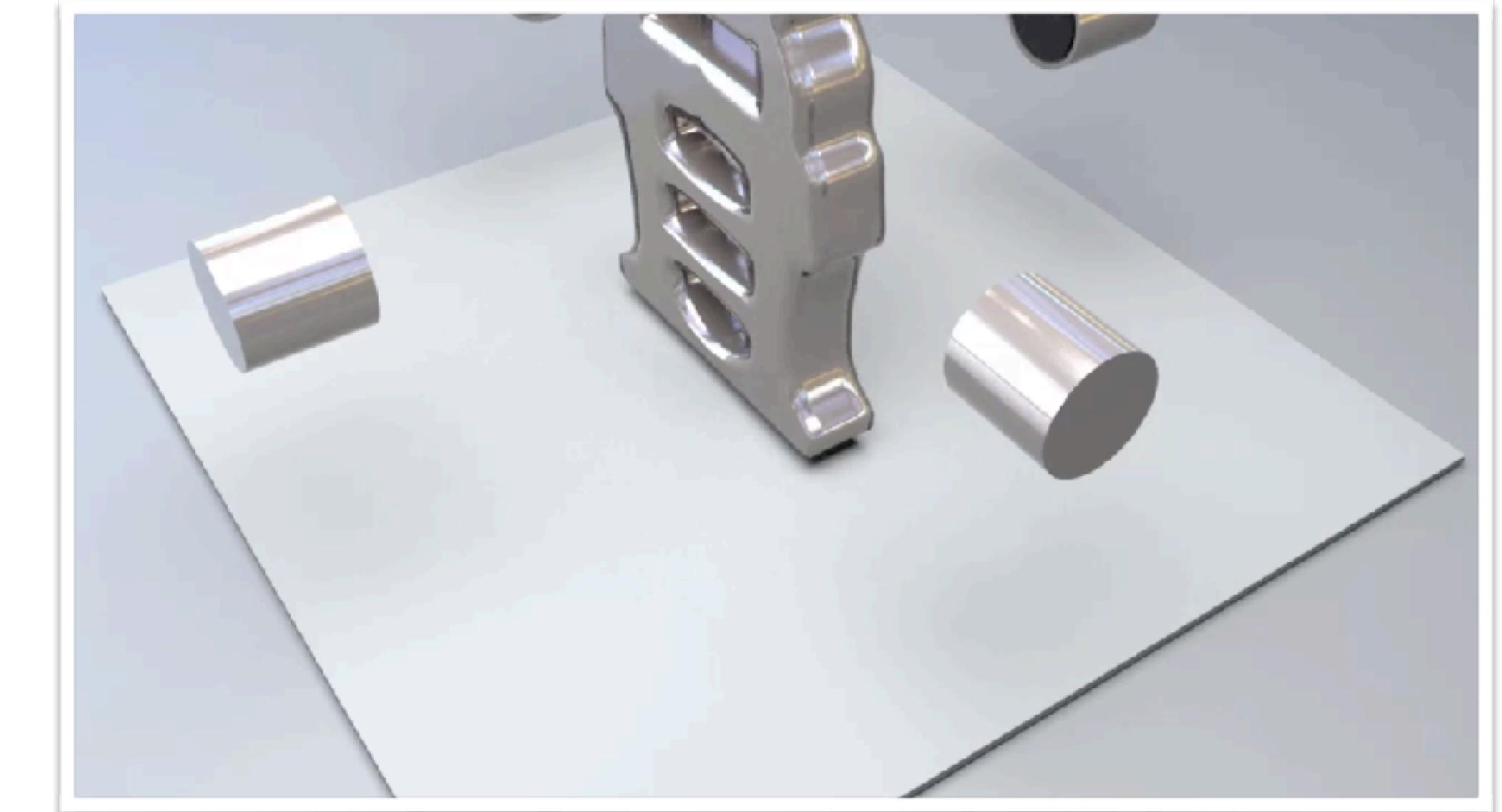




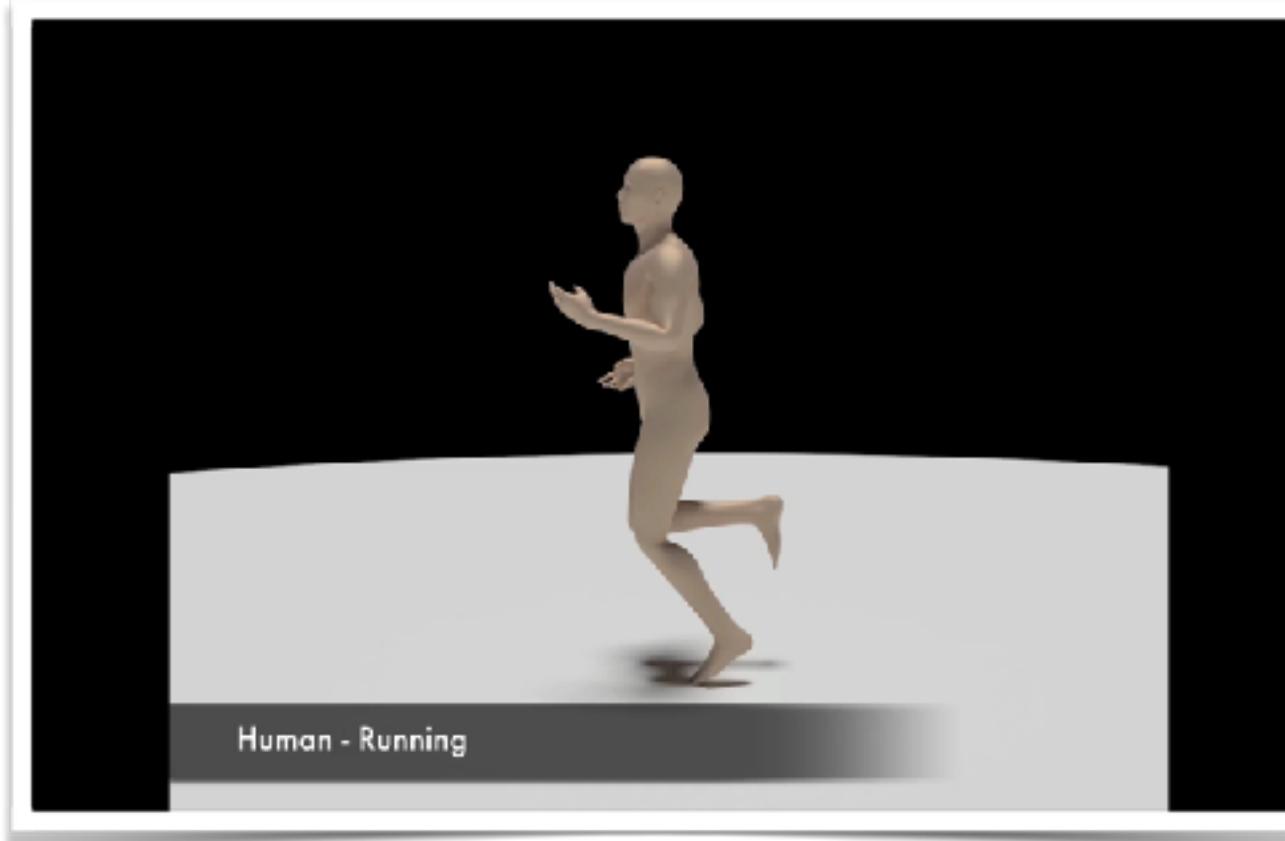
Sparse paged grid



Material point method



Adaptivity

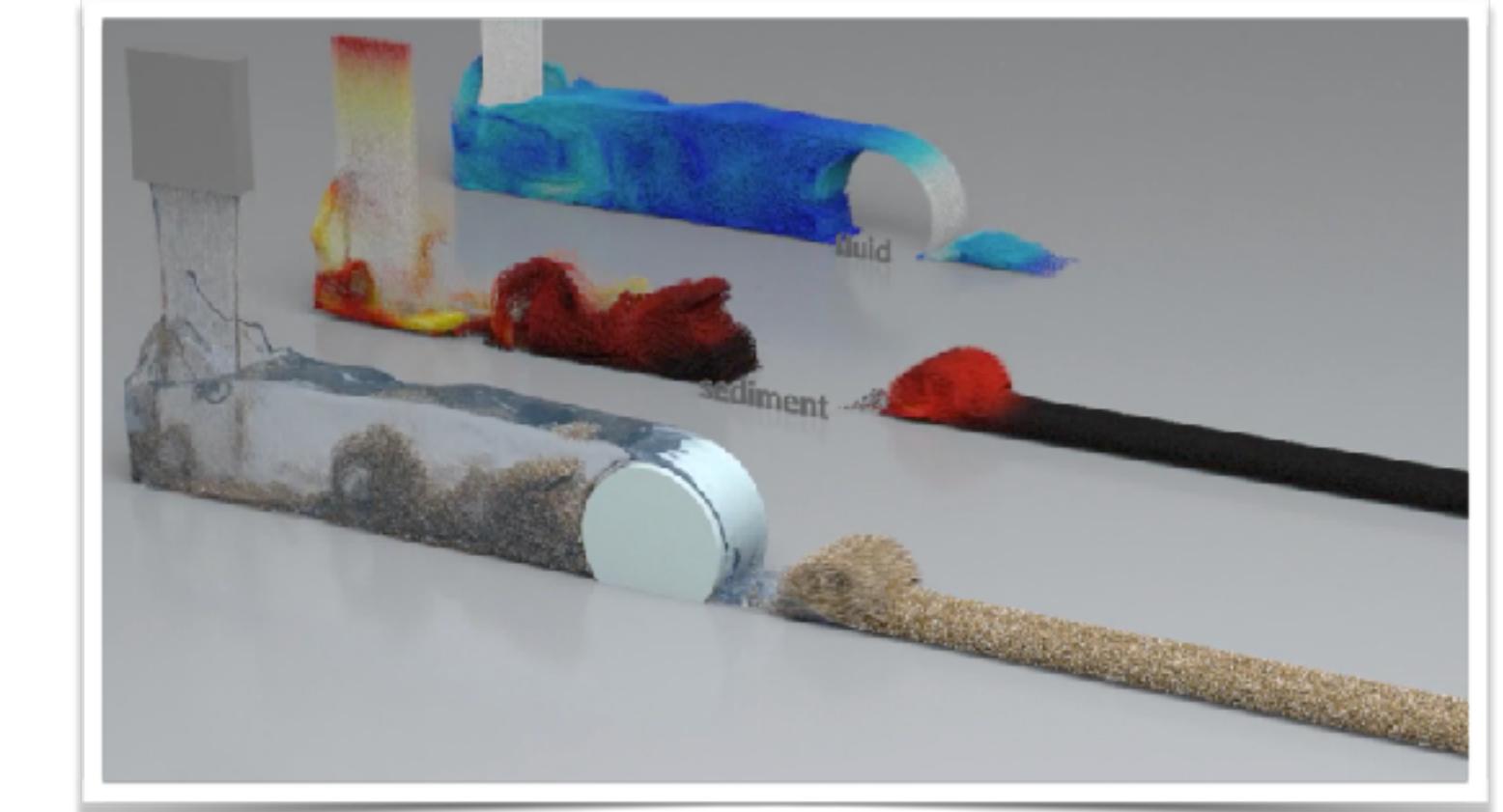


Human - Running

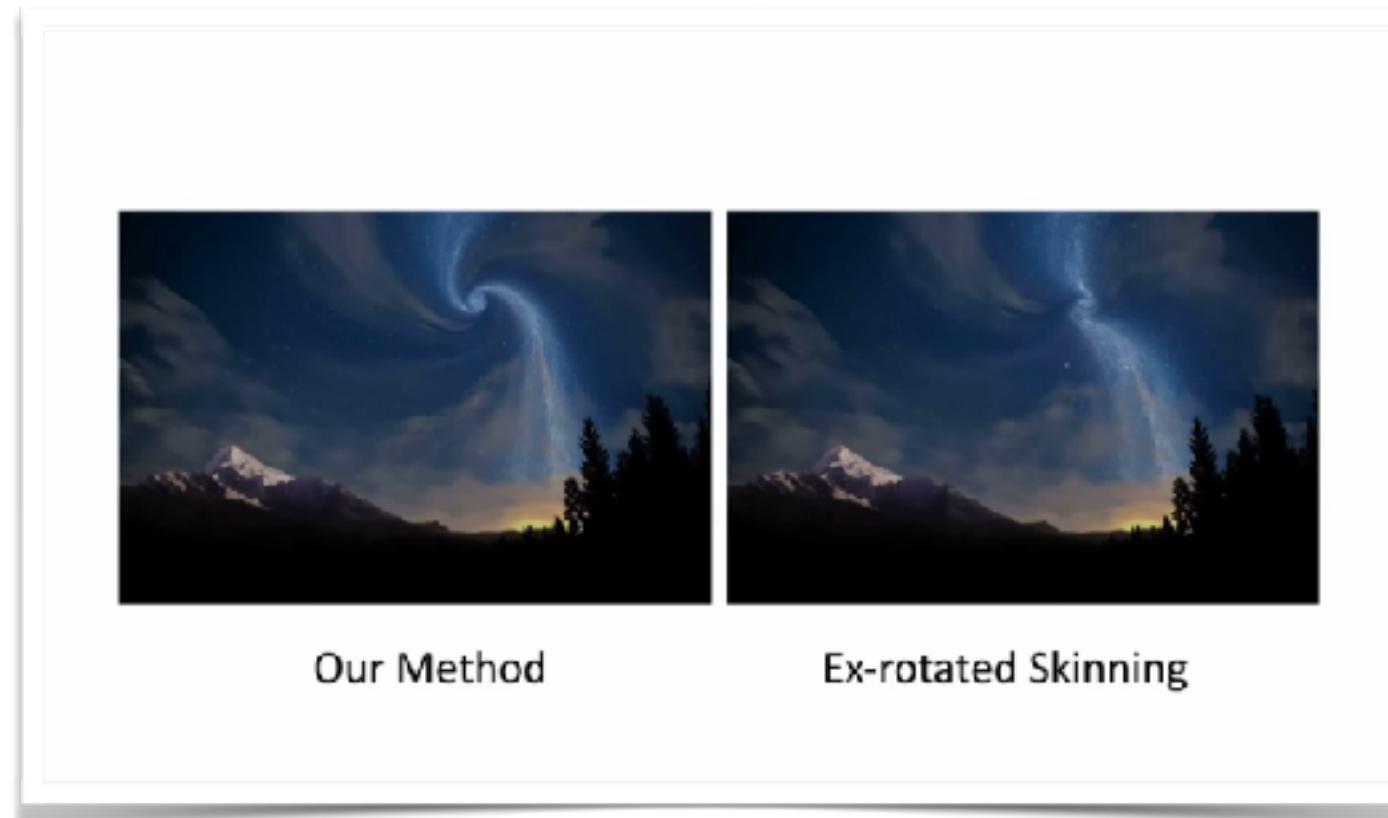
SCA 14



SIGGRAPH 17



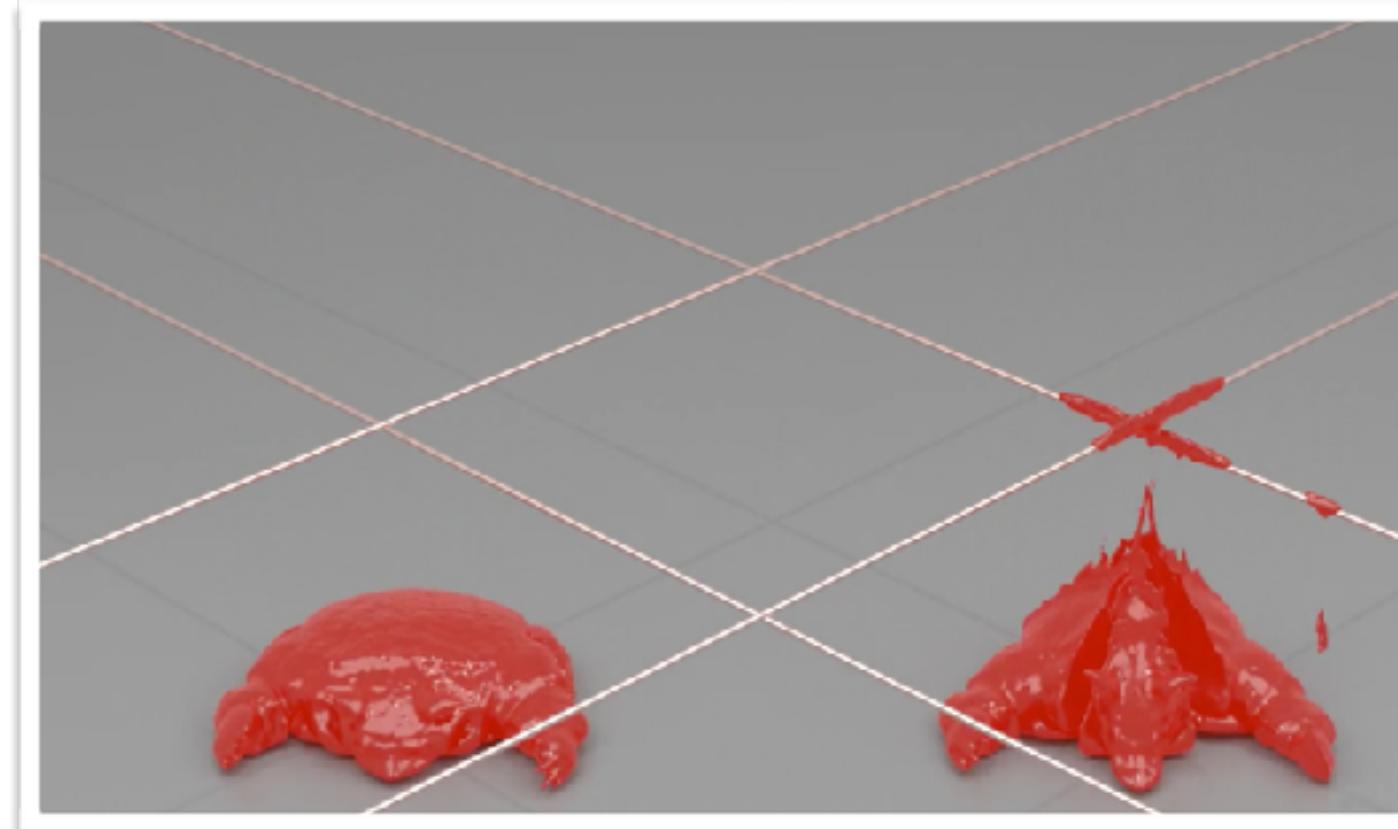
SIGGRAPH 18



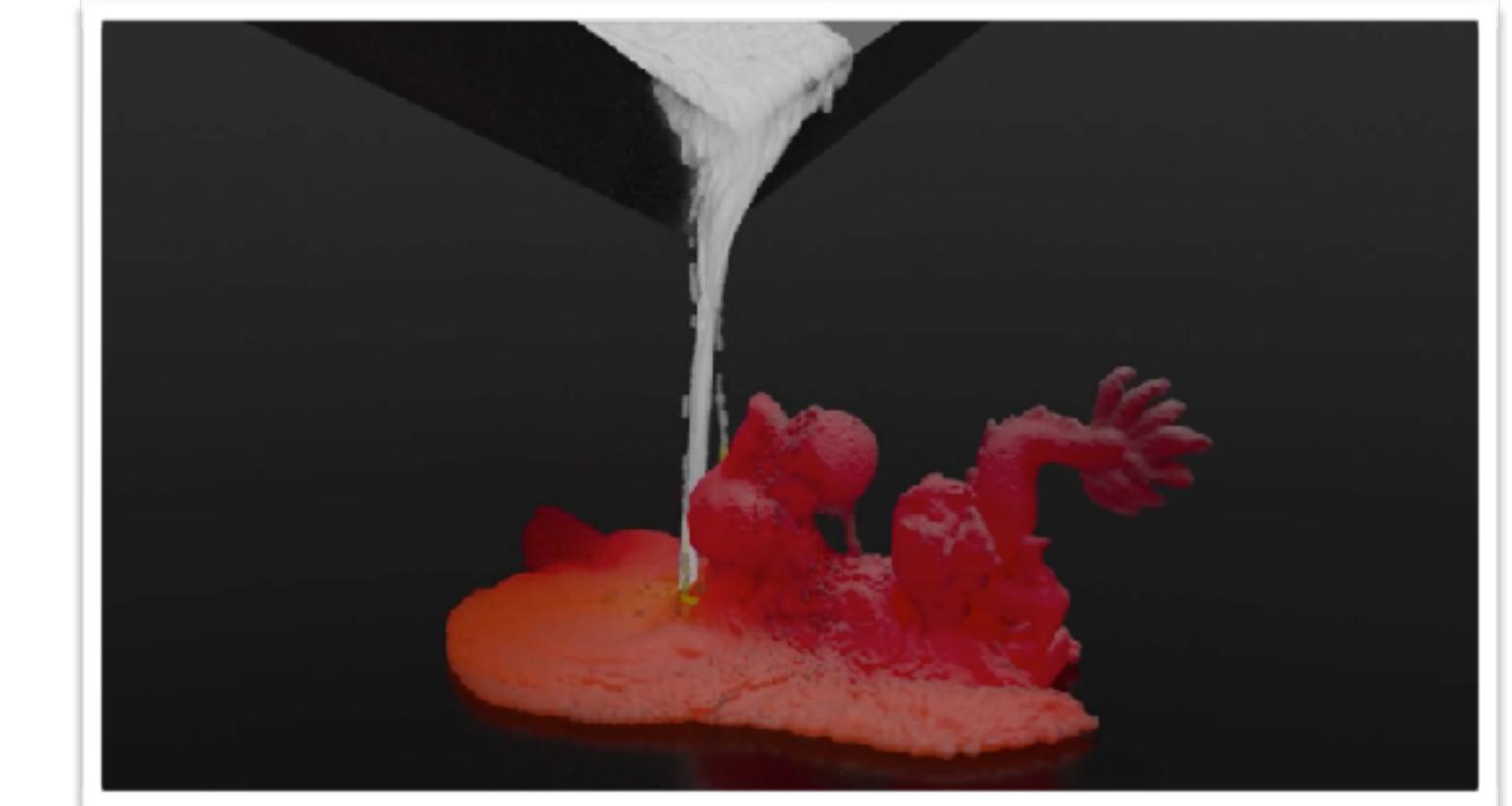
Our Method

Ex-rotated Skinning

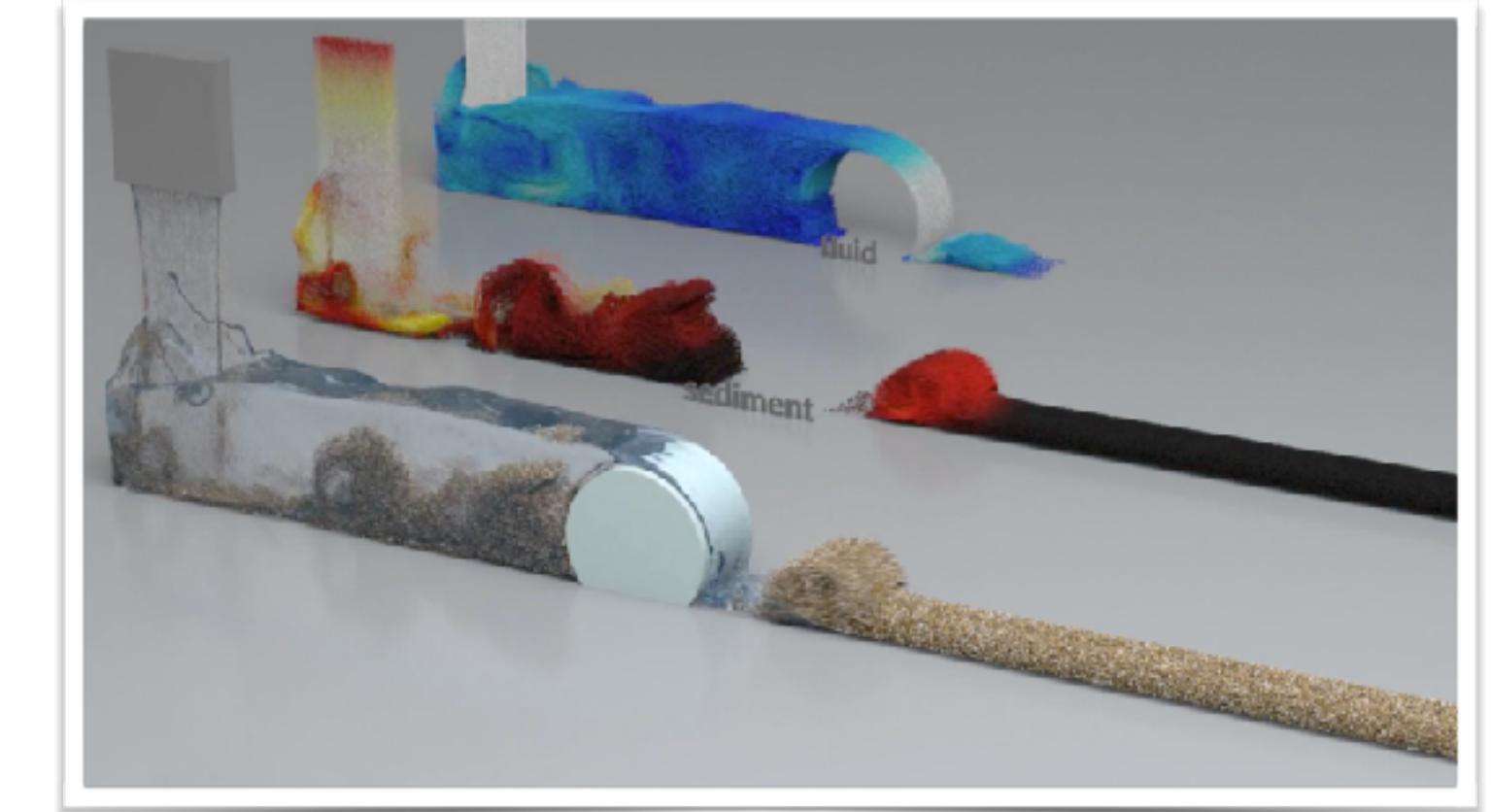
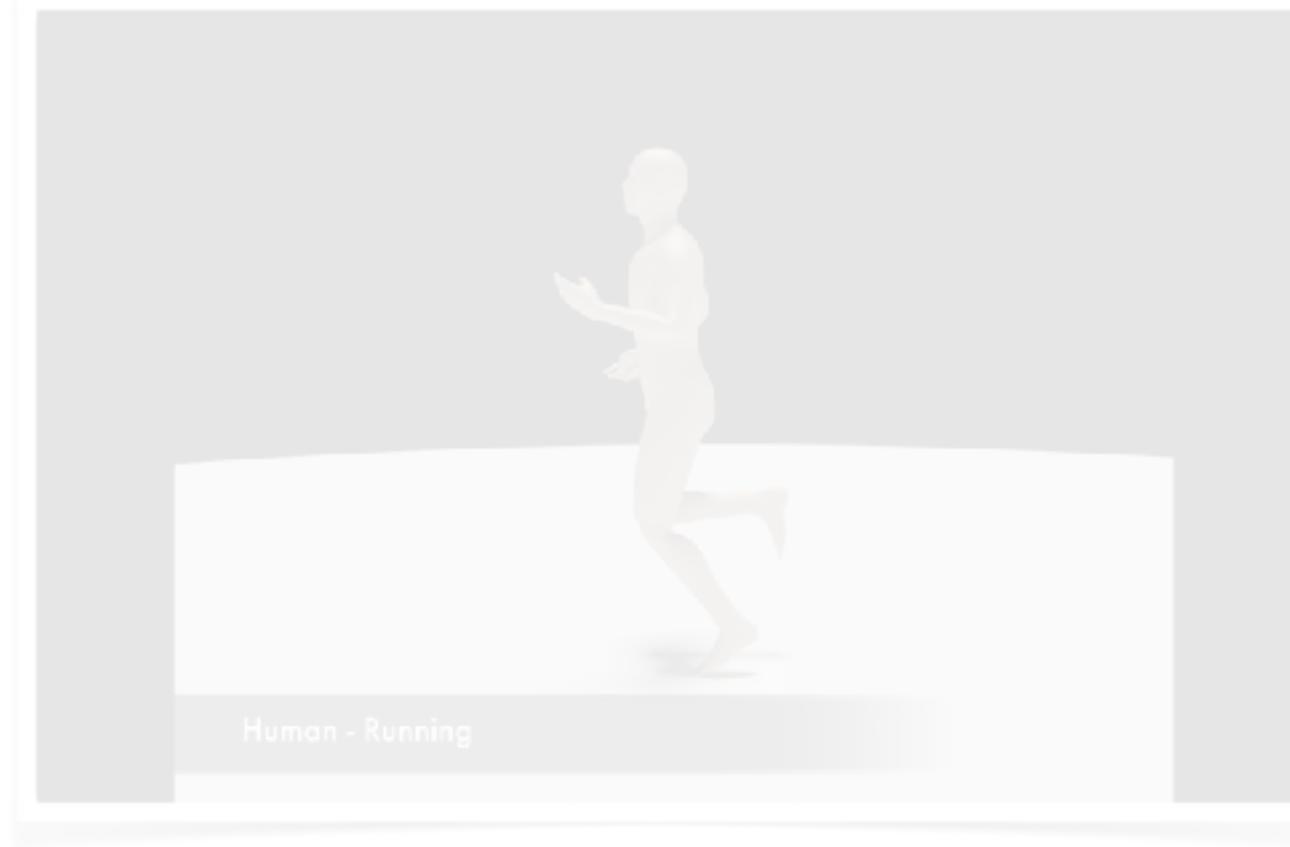
Eurographics 16



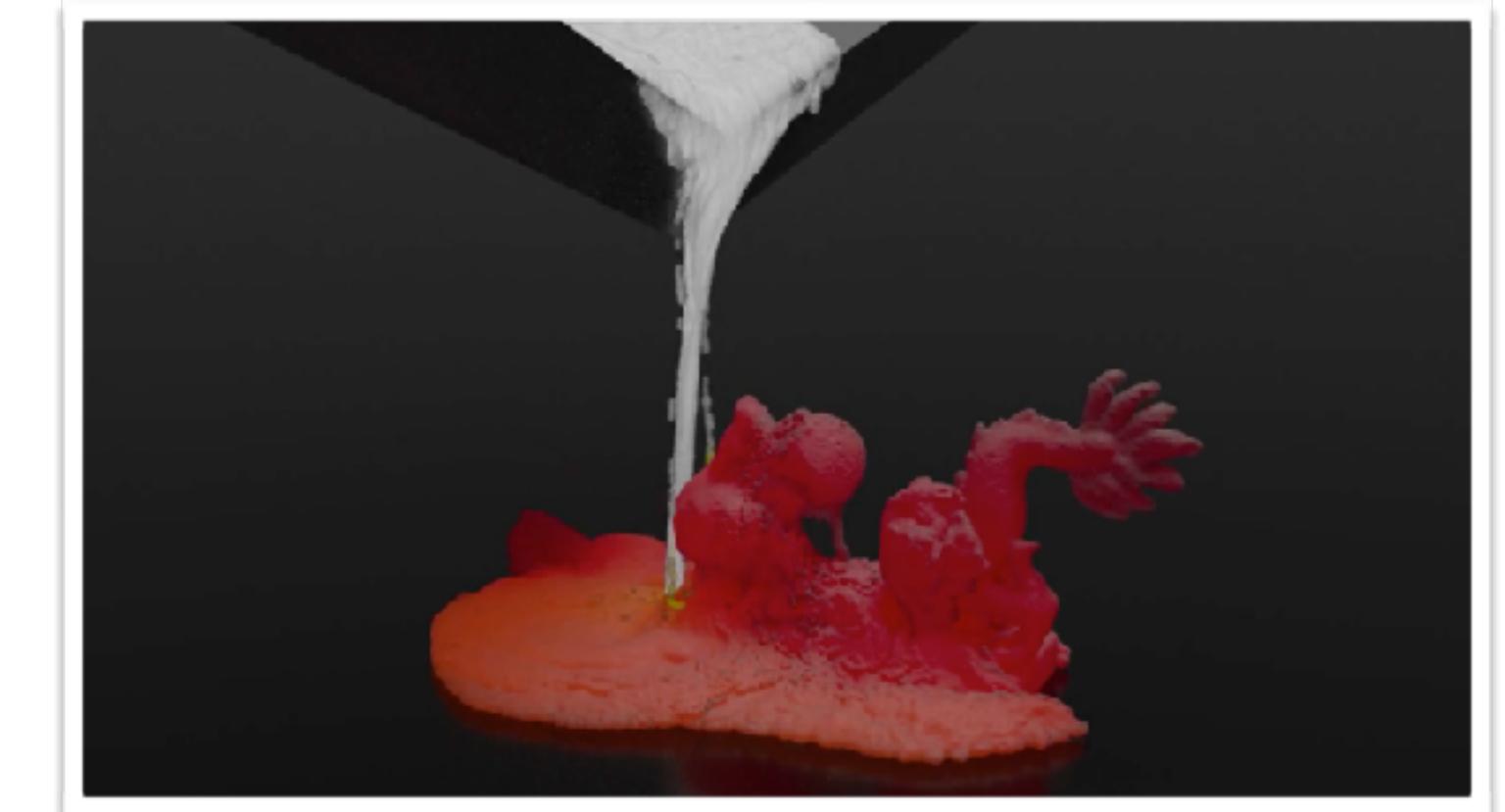
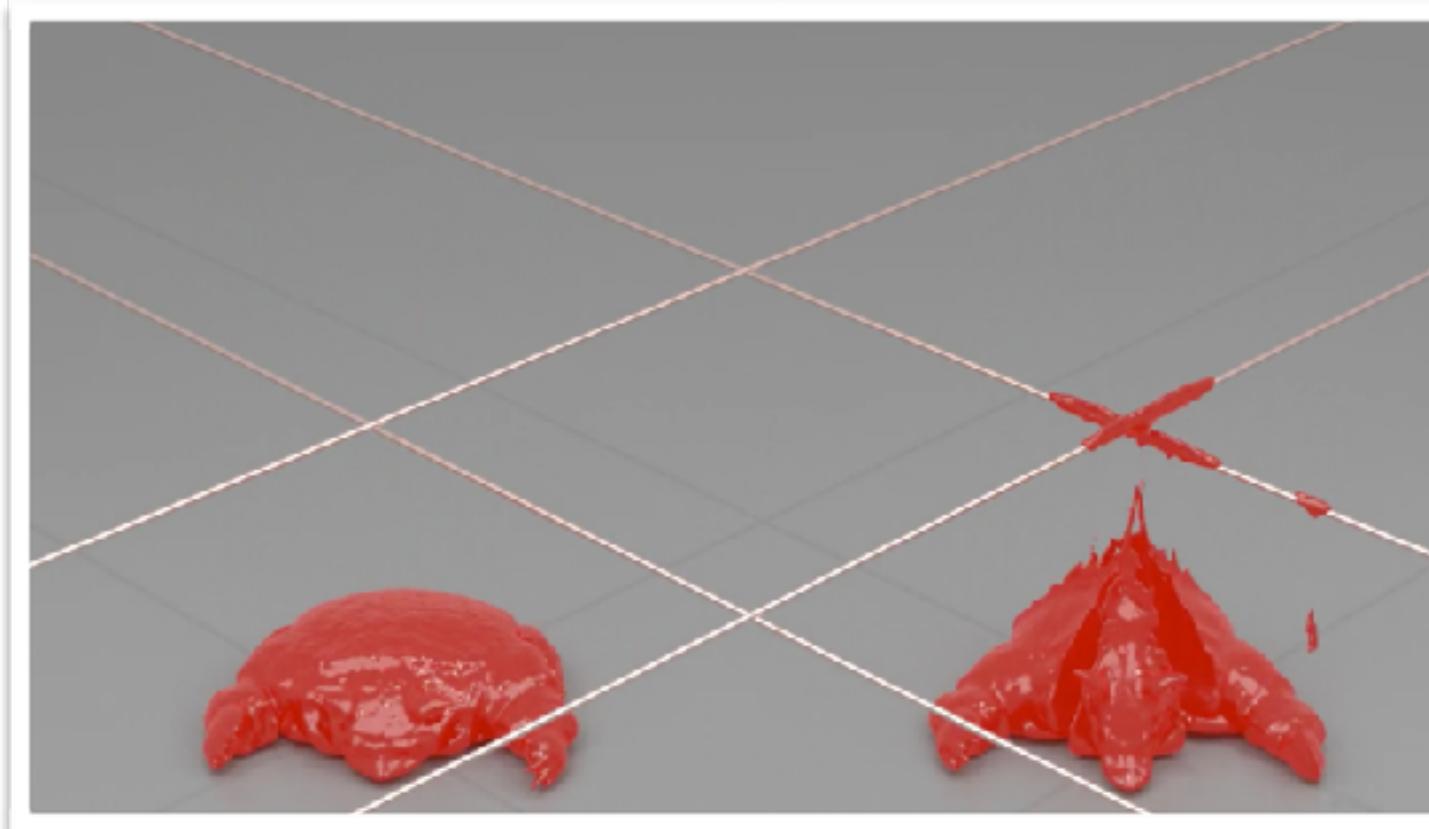
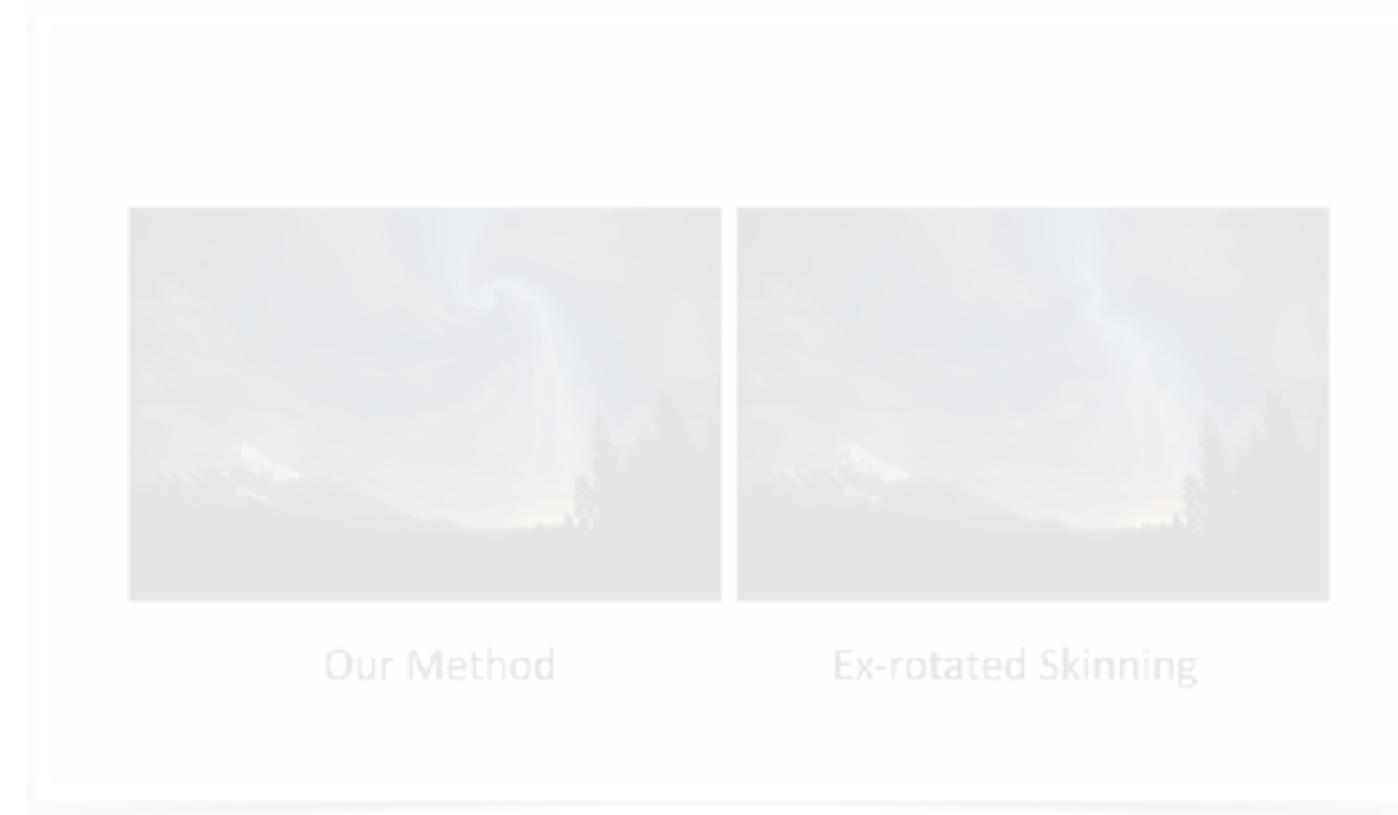
SIGGRAPH Asia 17



SIGGRAPH Asia 18
(under review)



SPGrid / Adaptivity

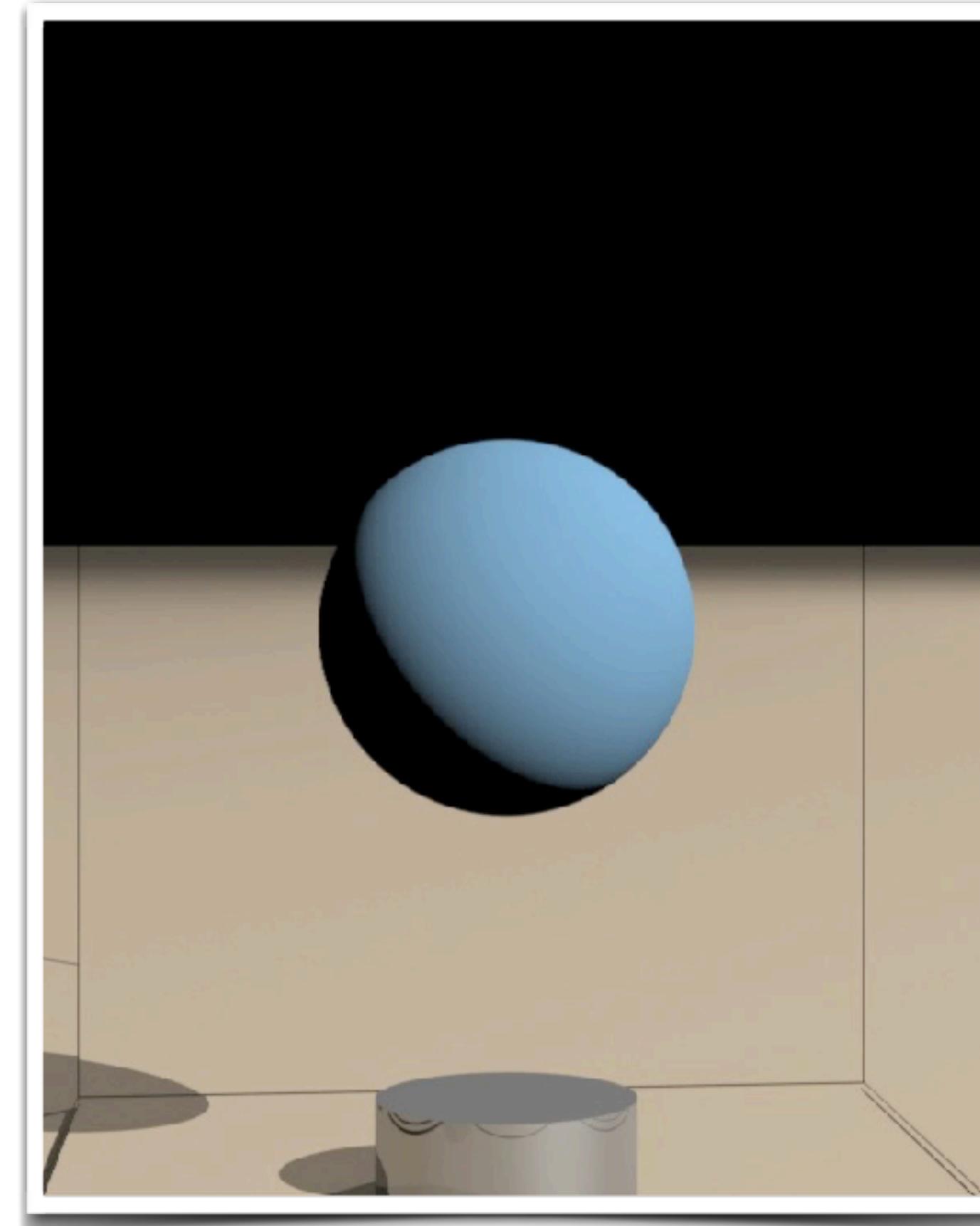


SPGrid / MPM / Adaptivity

SPGrid / MPM / GPU

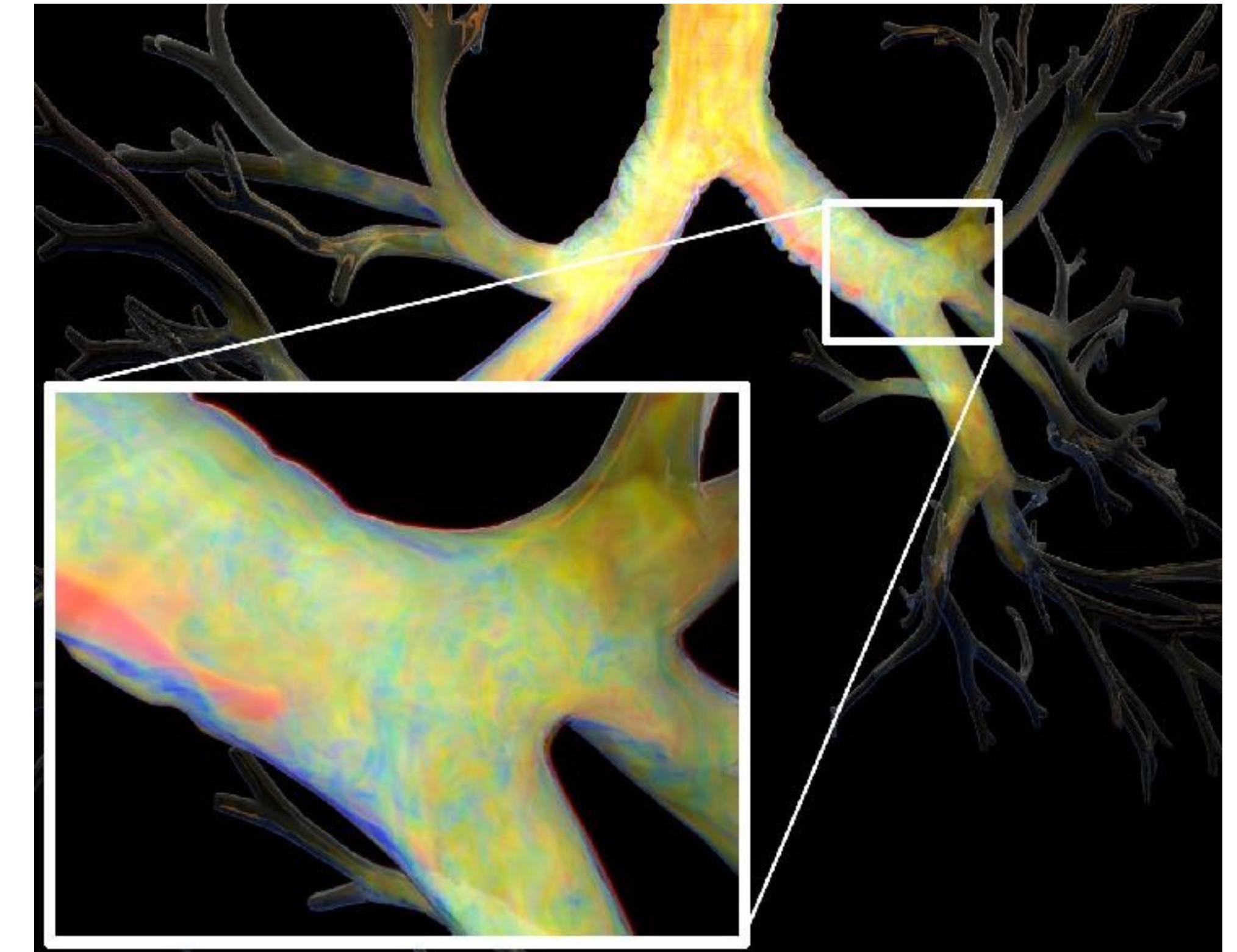
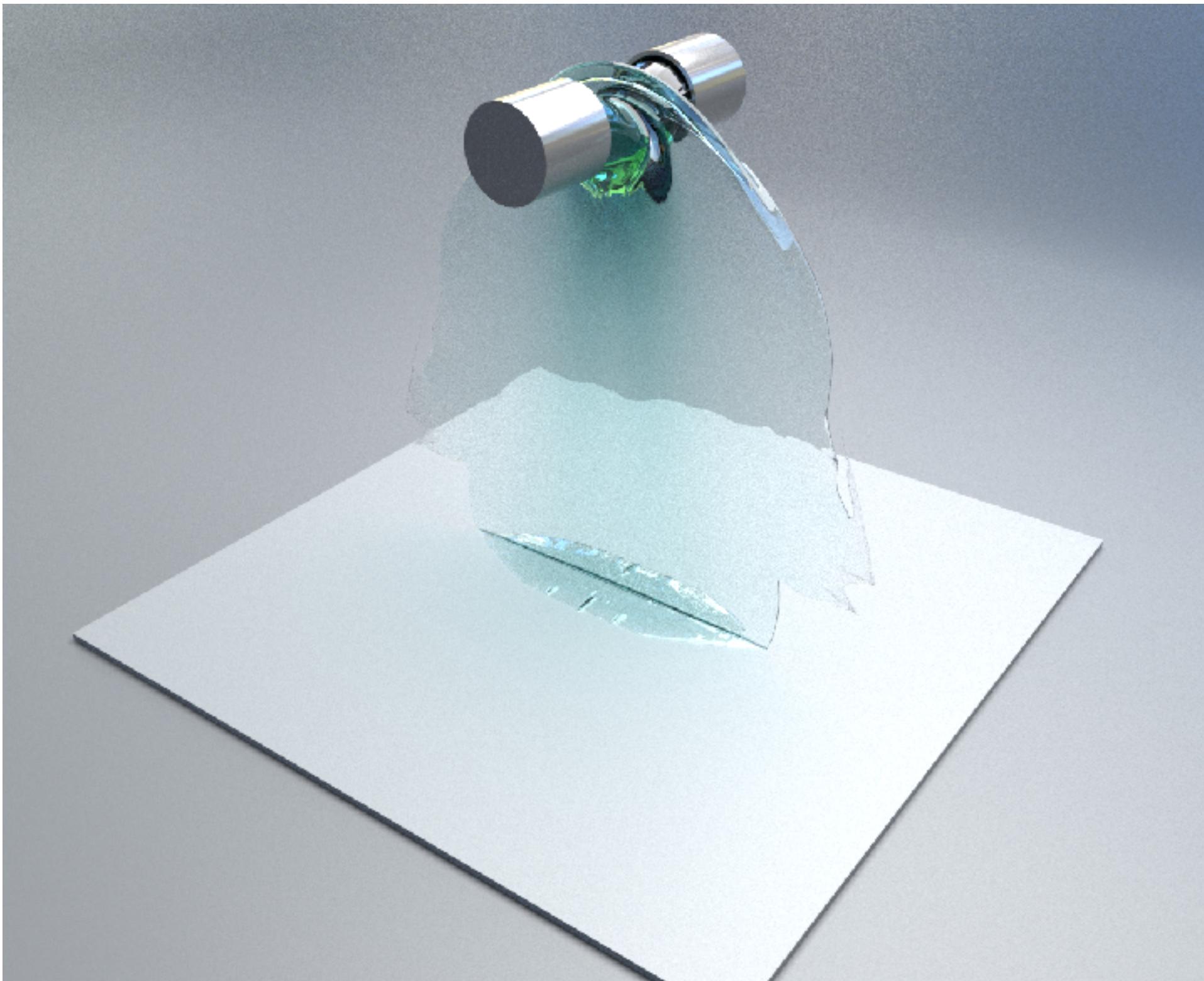
Sparse paged grid (SPGrid)

135M voxels
23GB



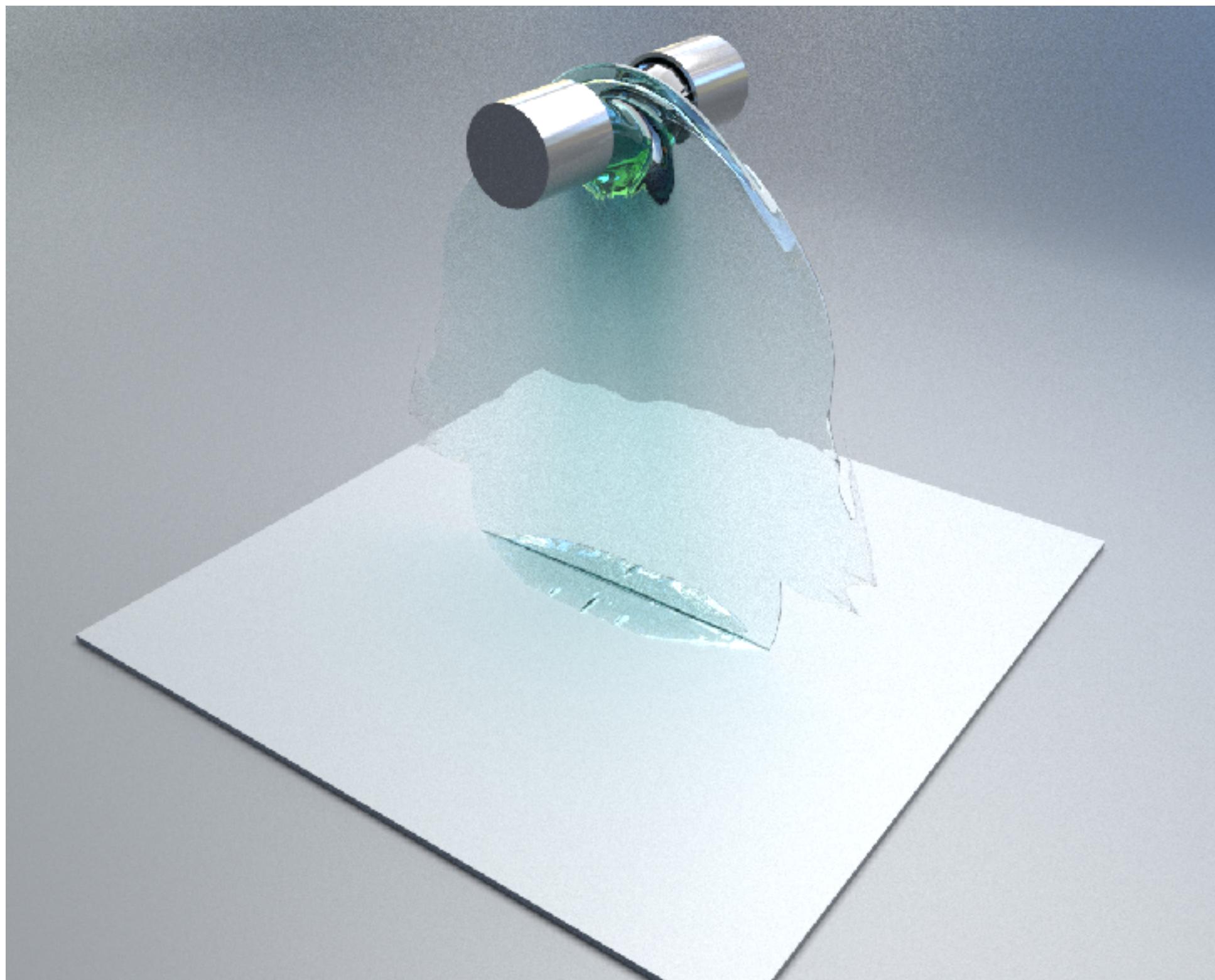
Sparsity

Liu et al. 16

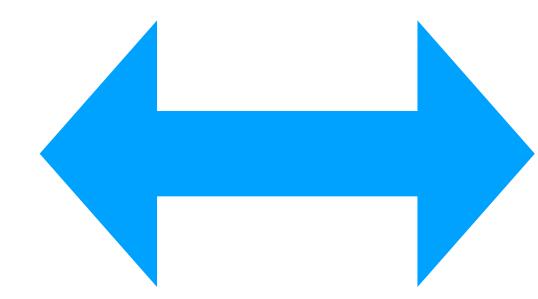


Resolution: $8192 \times 8192 \times 4096$

Sparsity



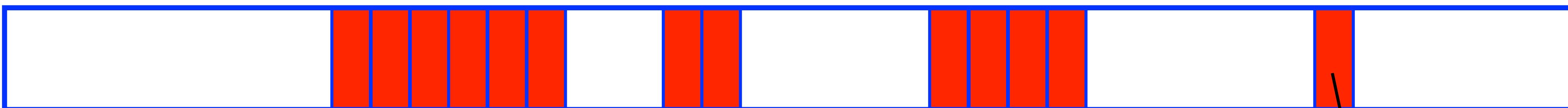
SPGrid
sparsity



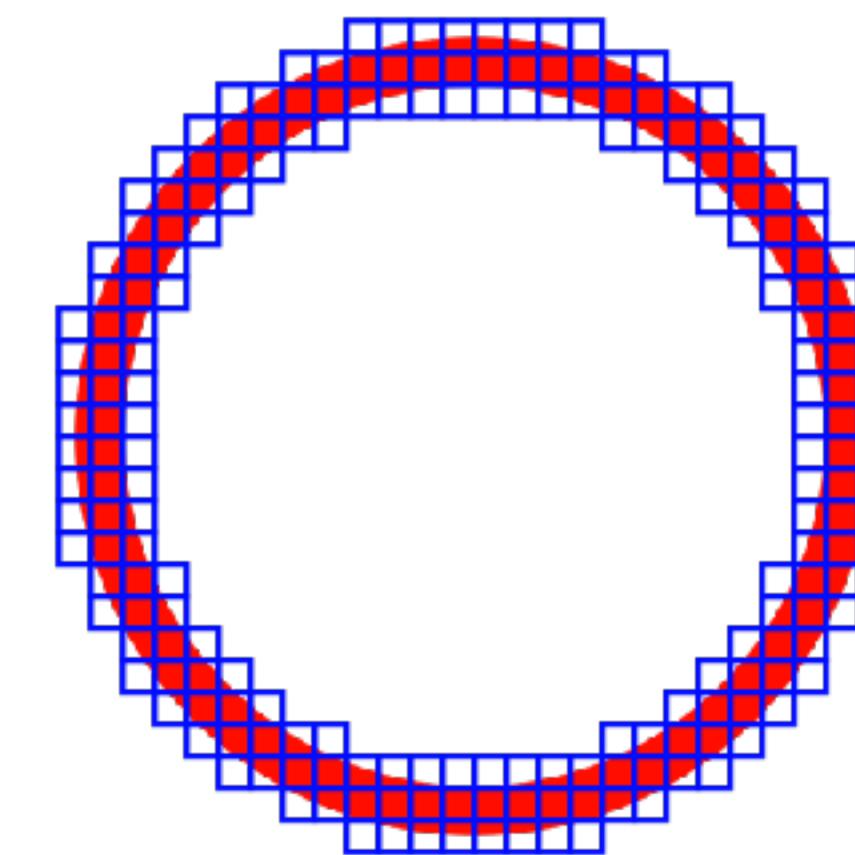
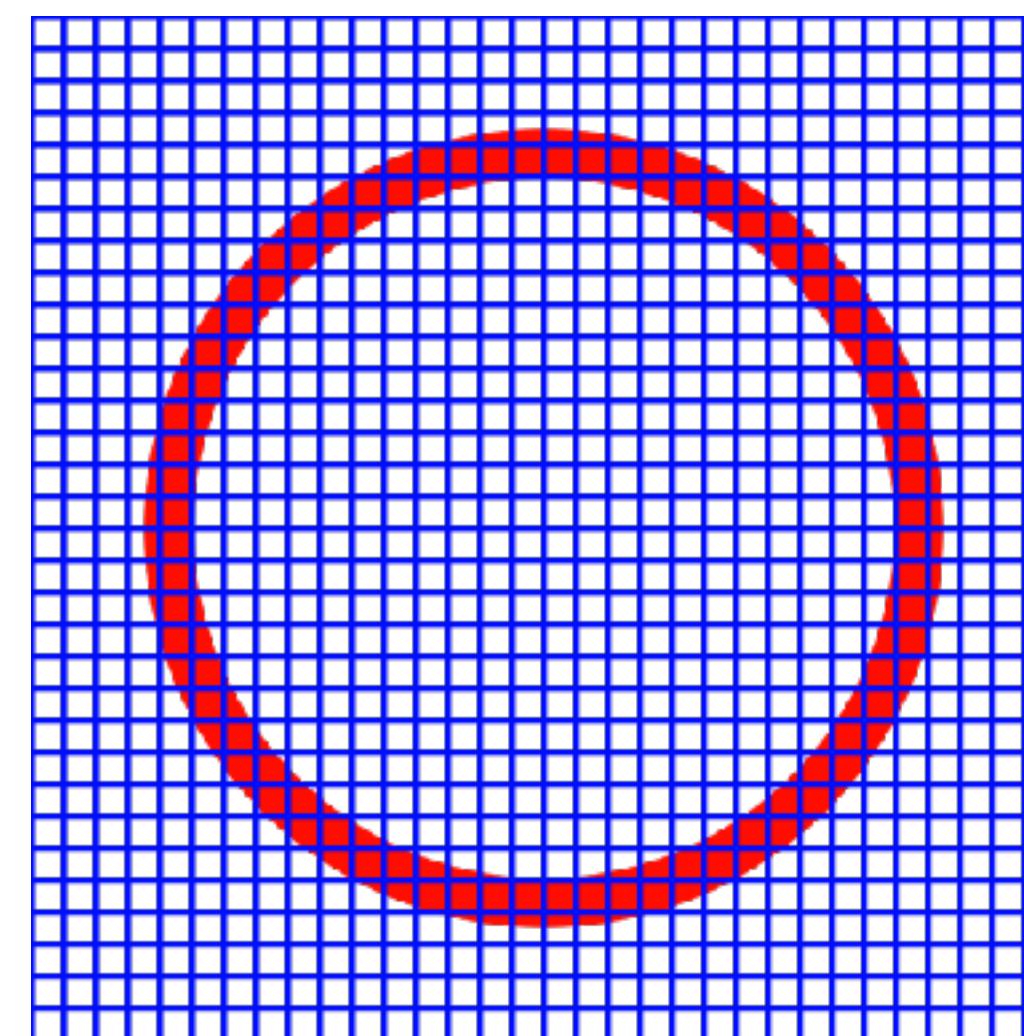
Virtual
memory

Virtual memory

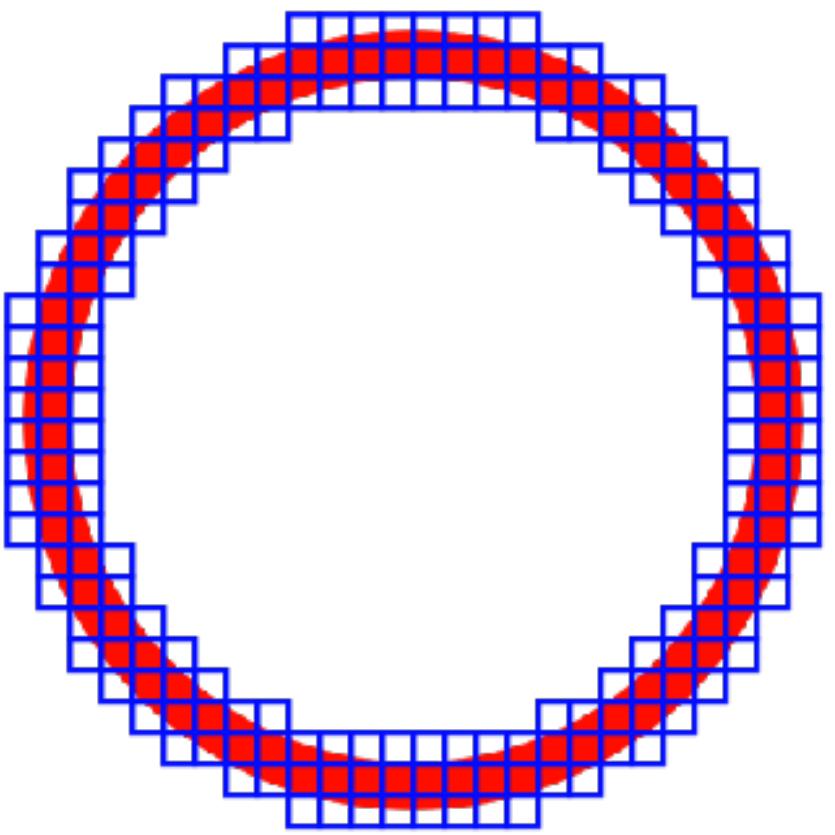
128 TB



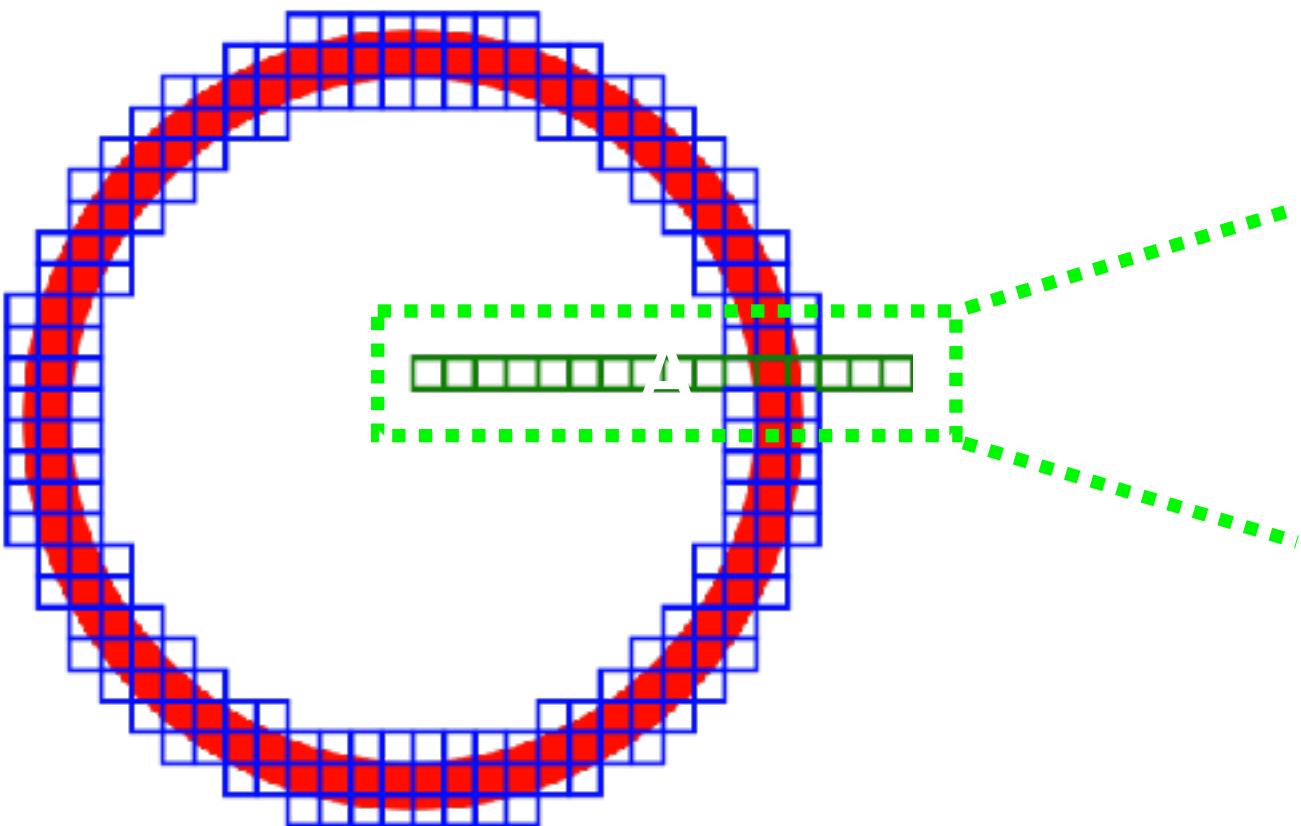
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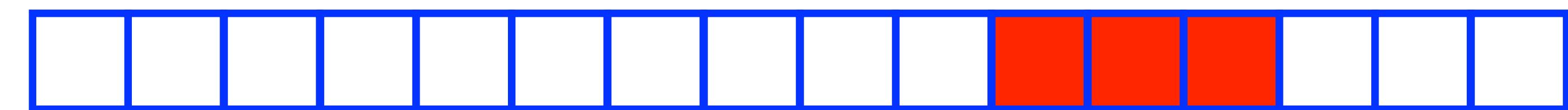
Cell ordering



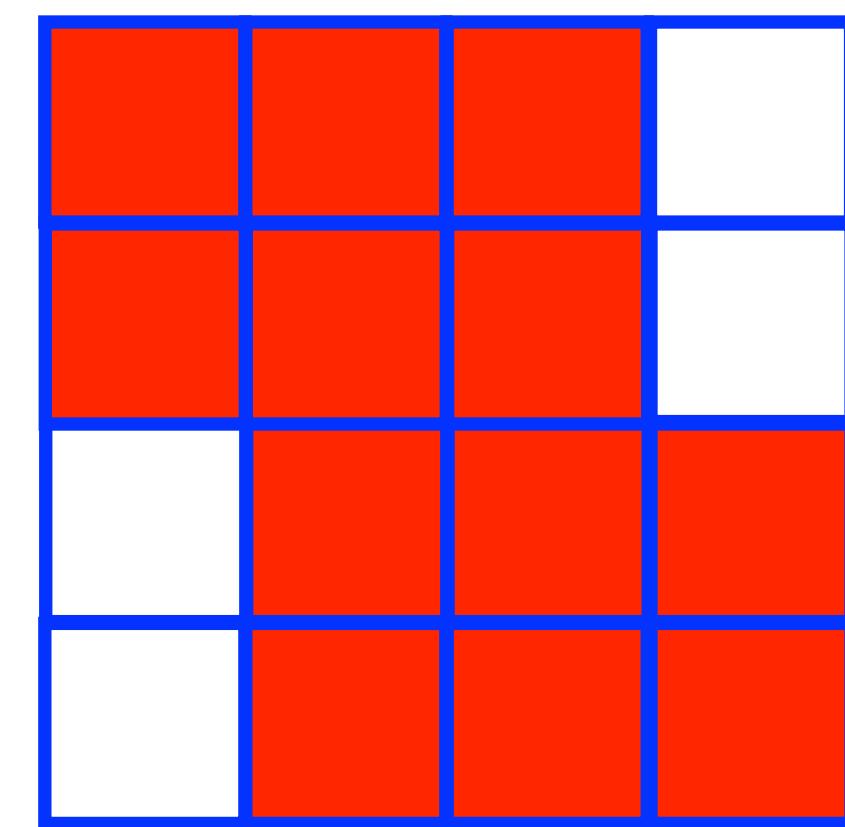
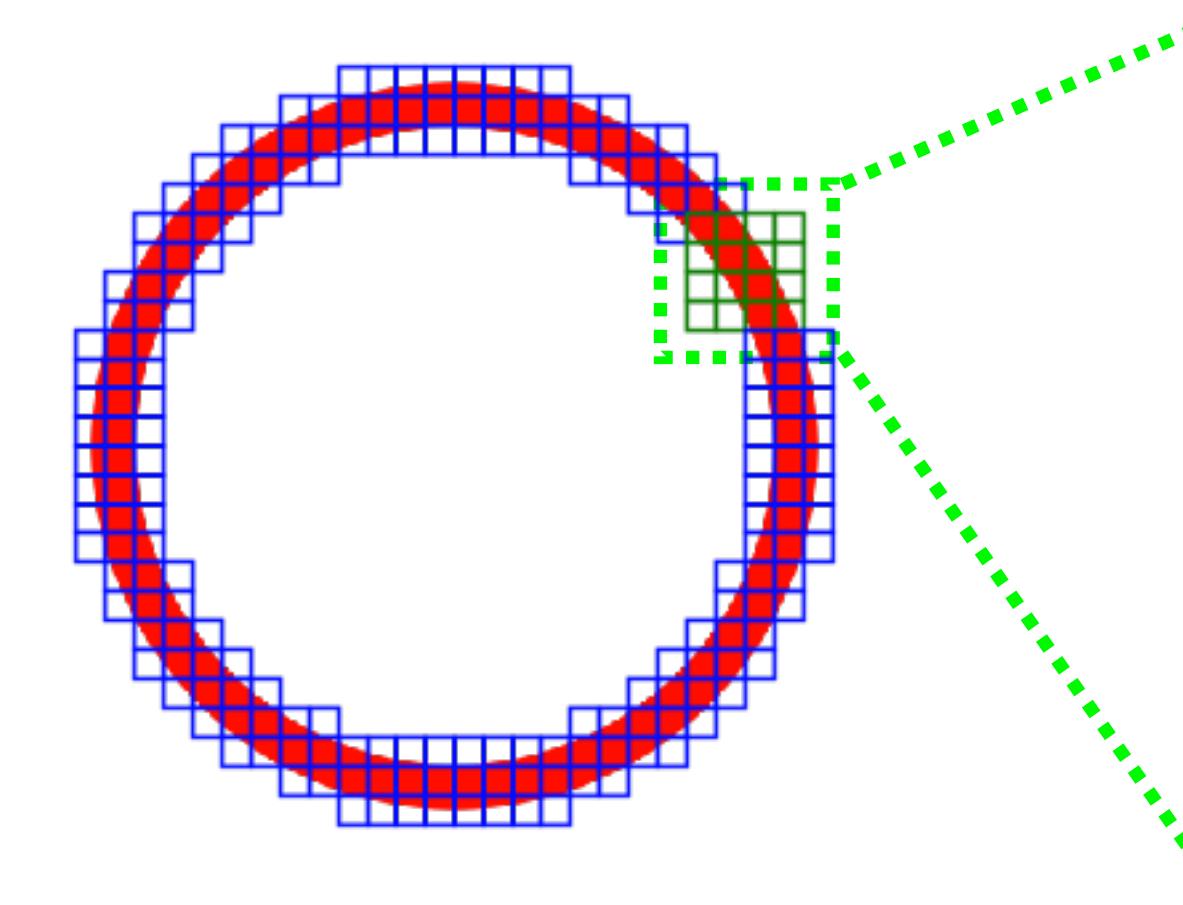
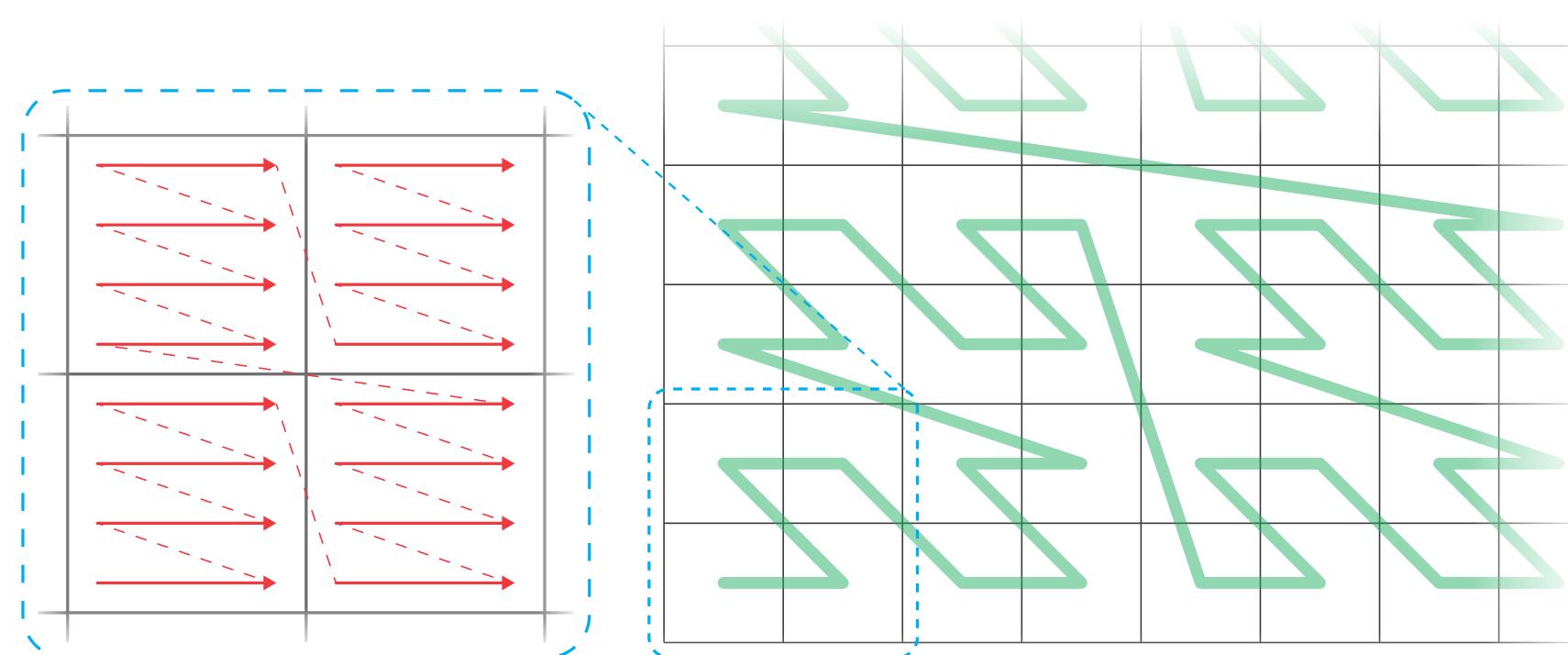
Cell ordering



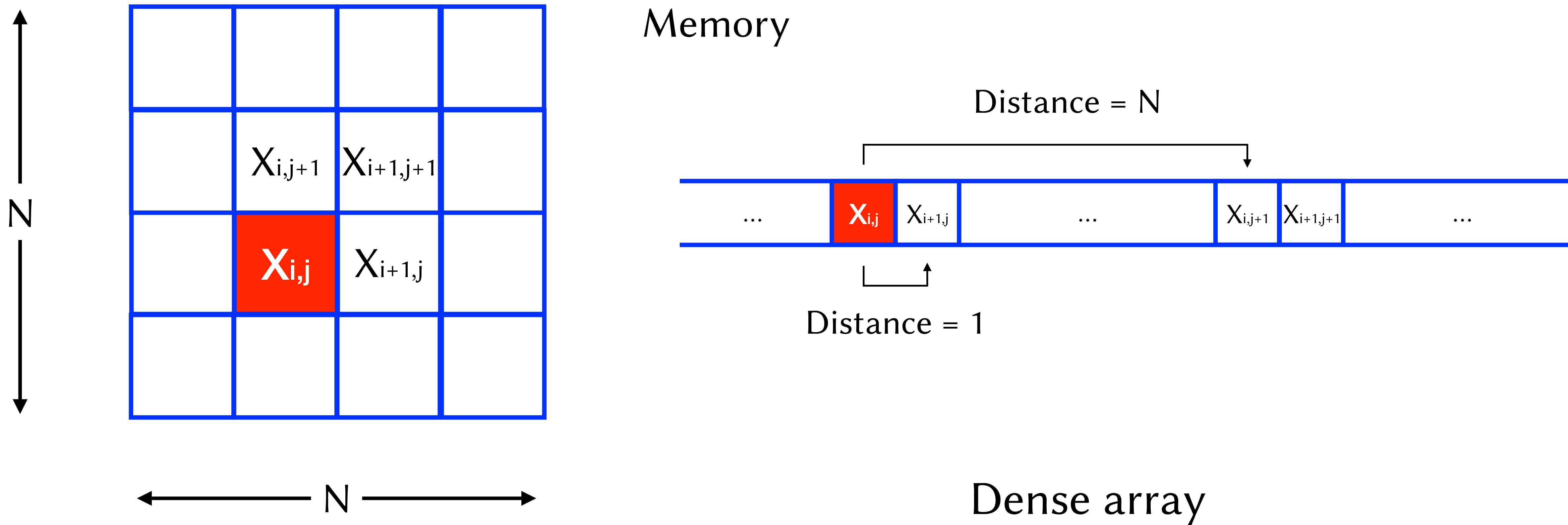
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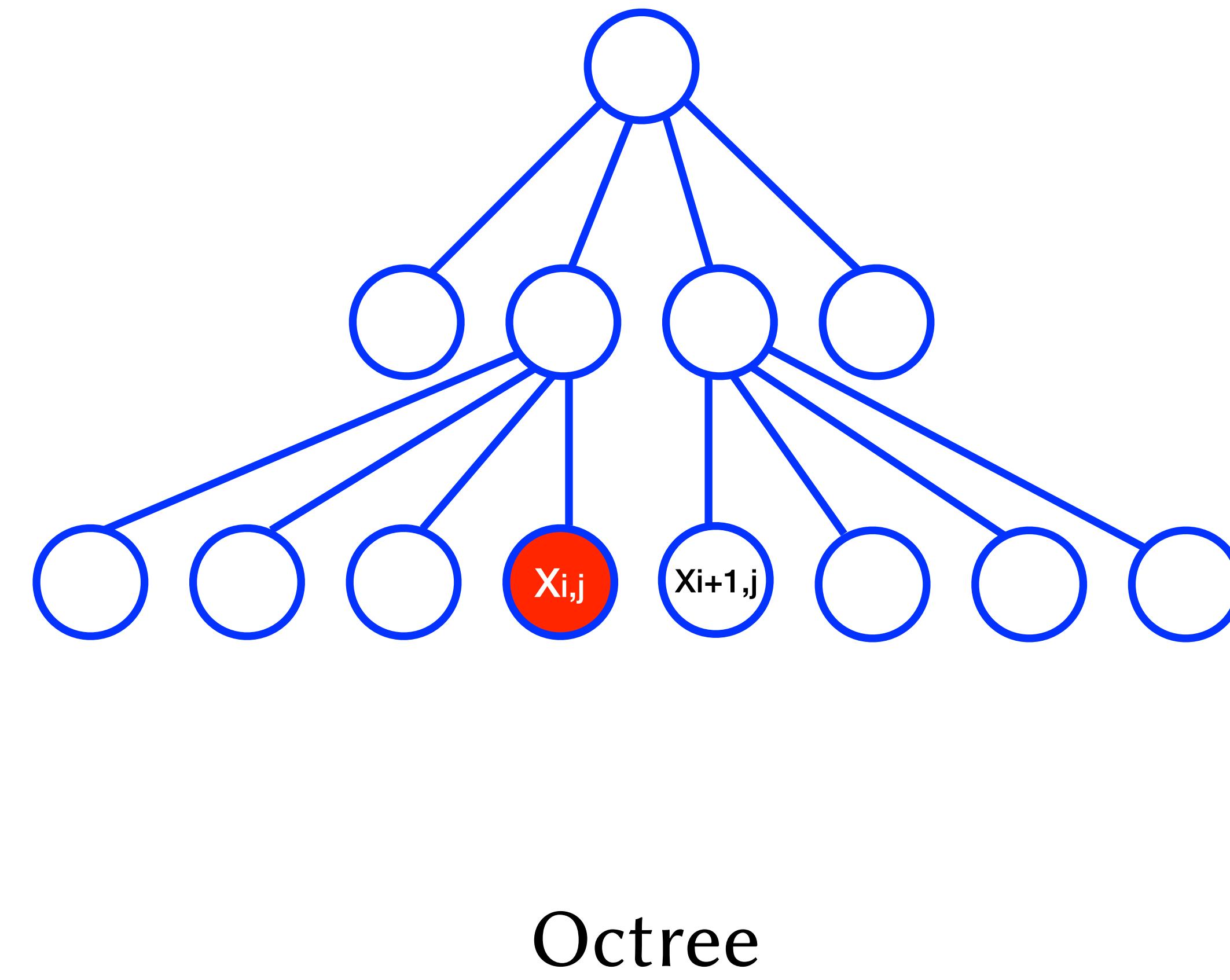
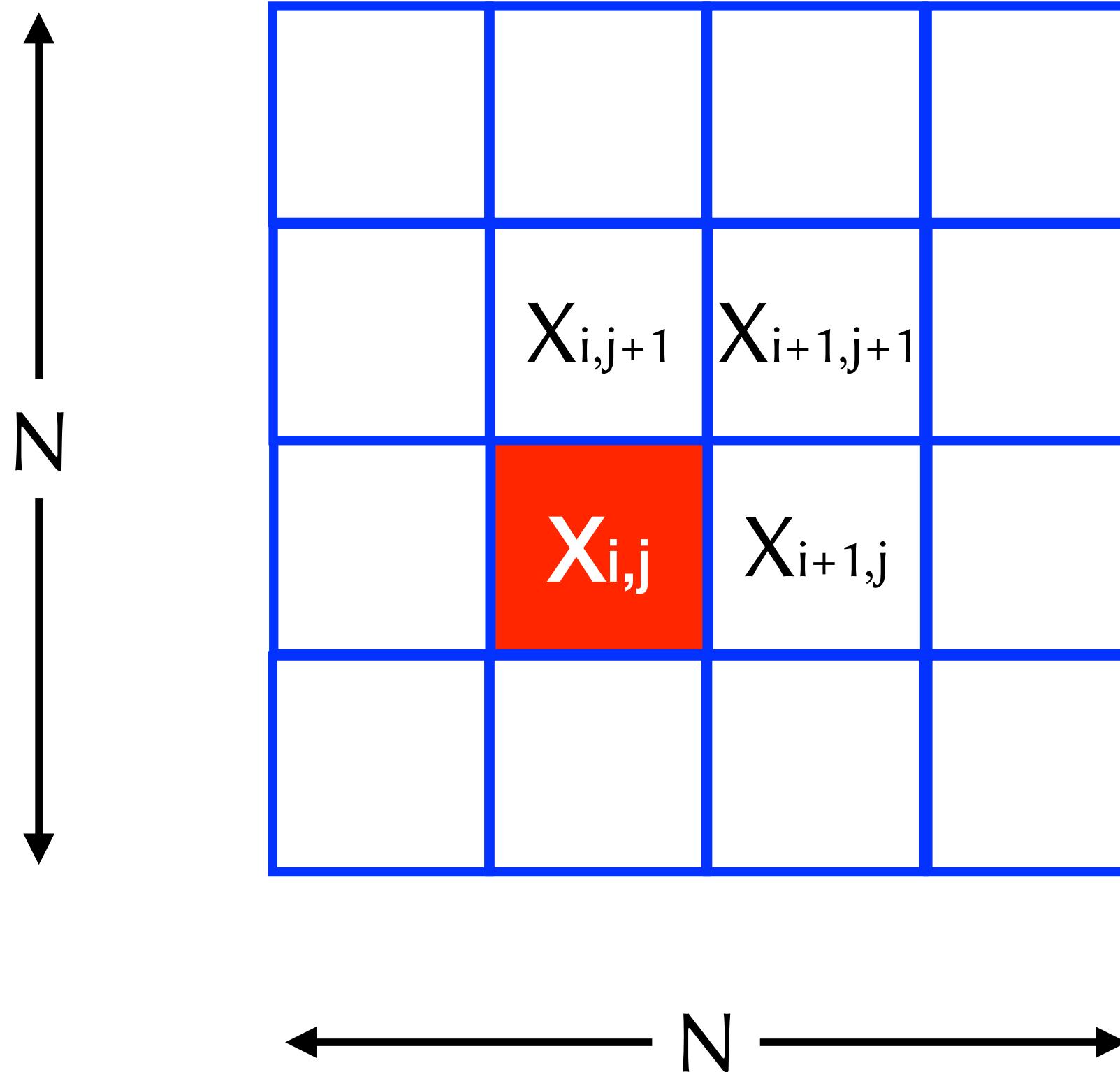
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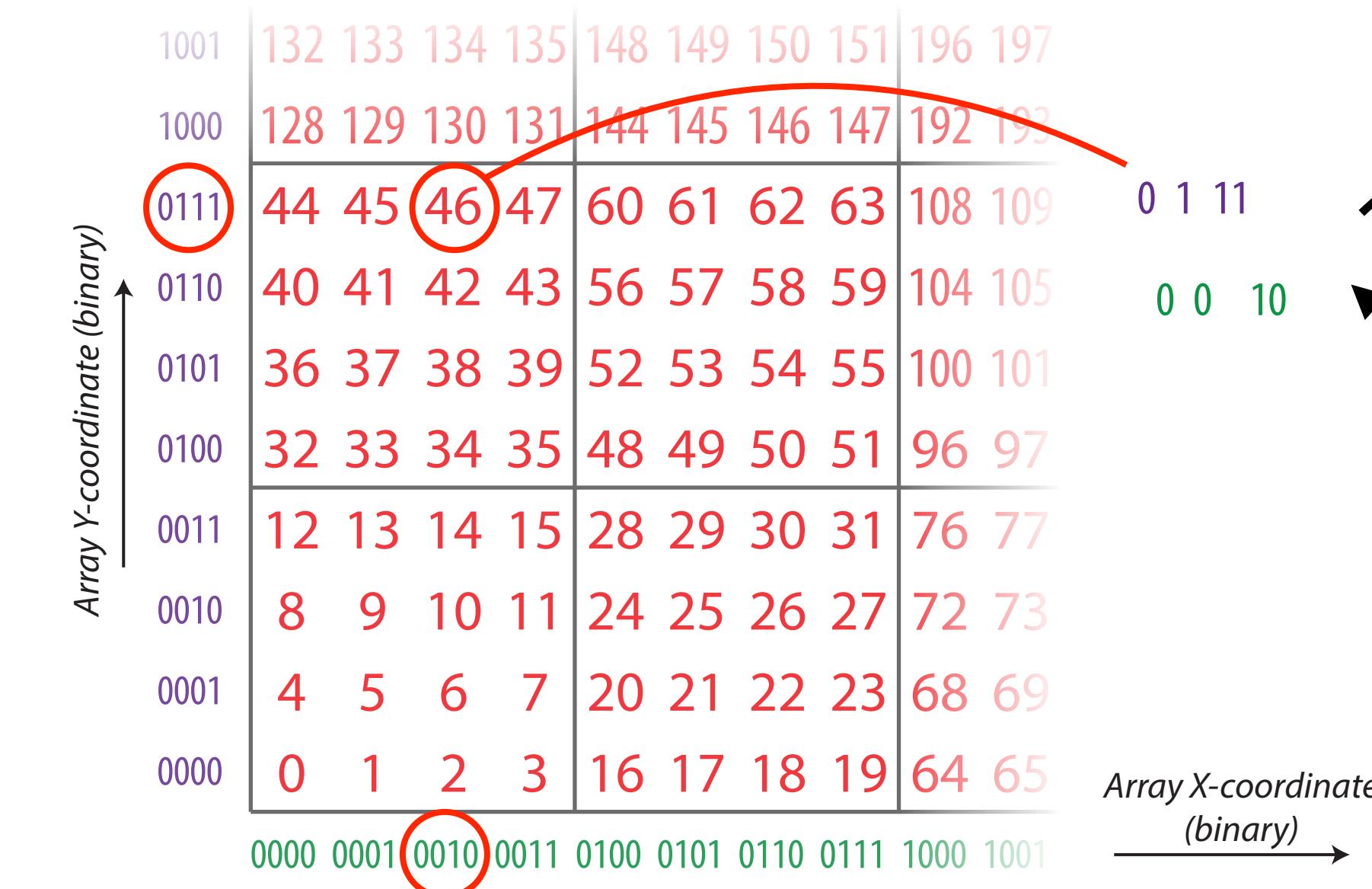
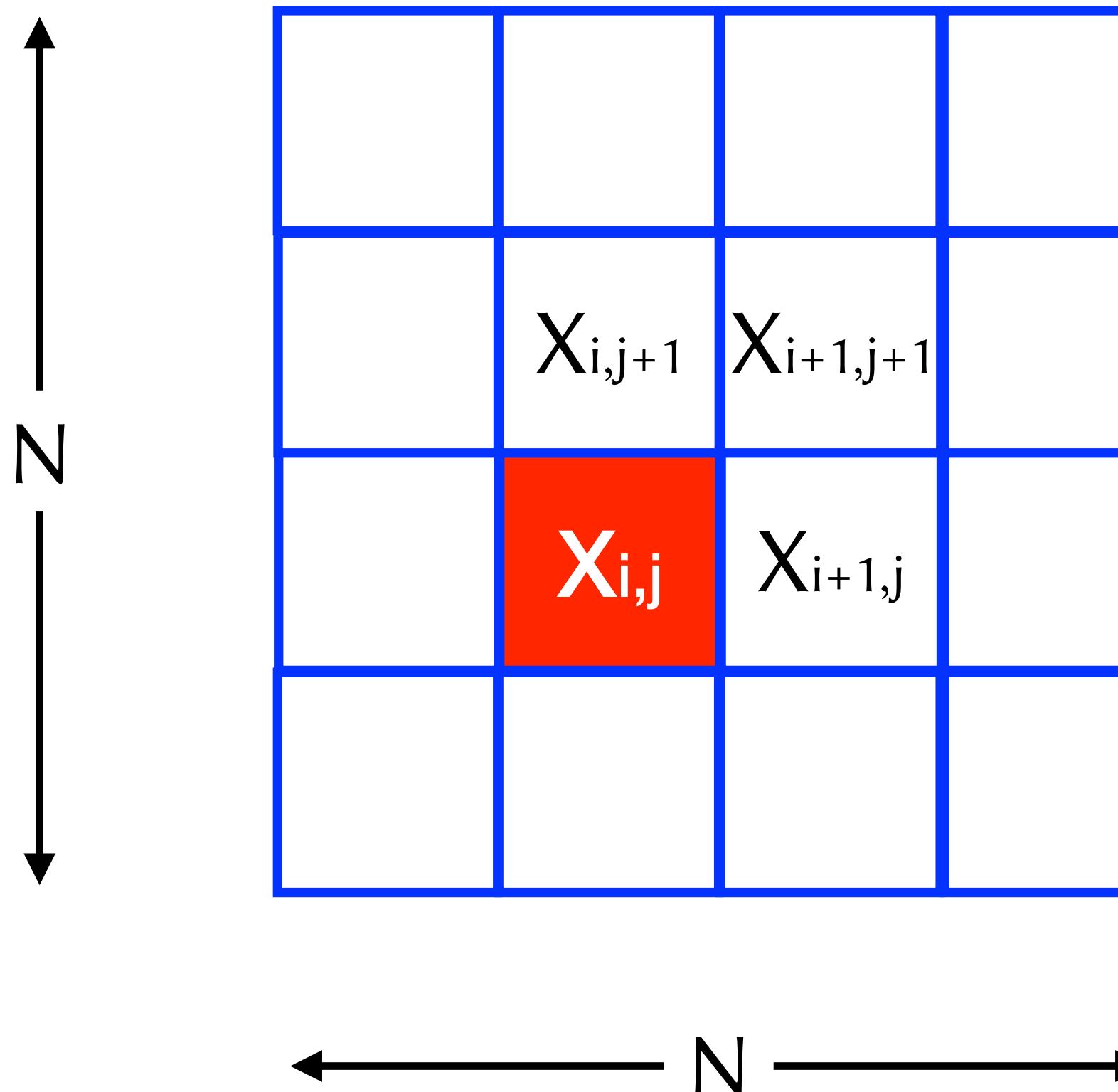
Stencil operations



Stencil operations



Stencil operations



SPGrid

Material point method (MPM)

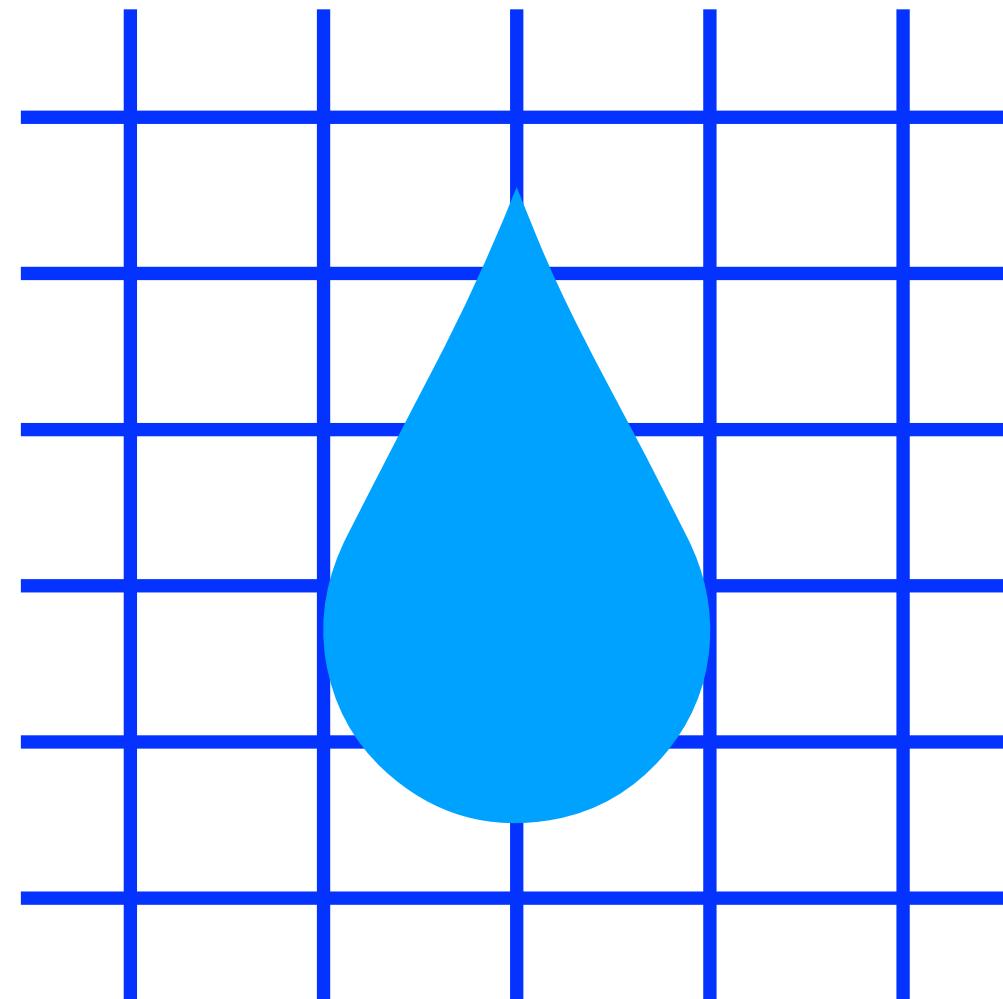


Stomakhin et al. 13



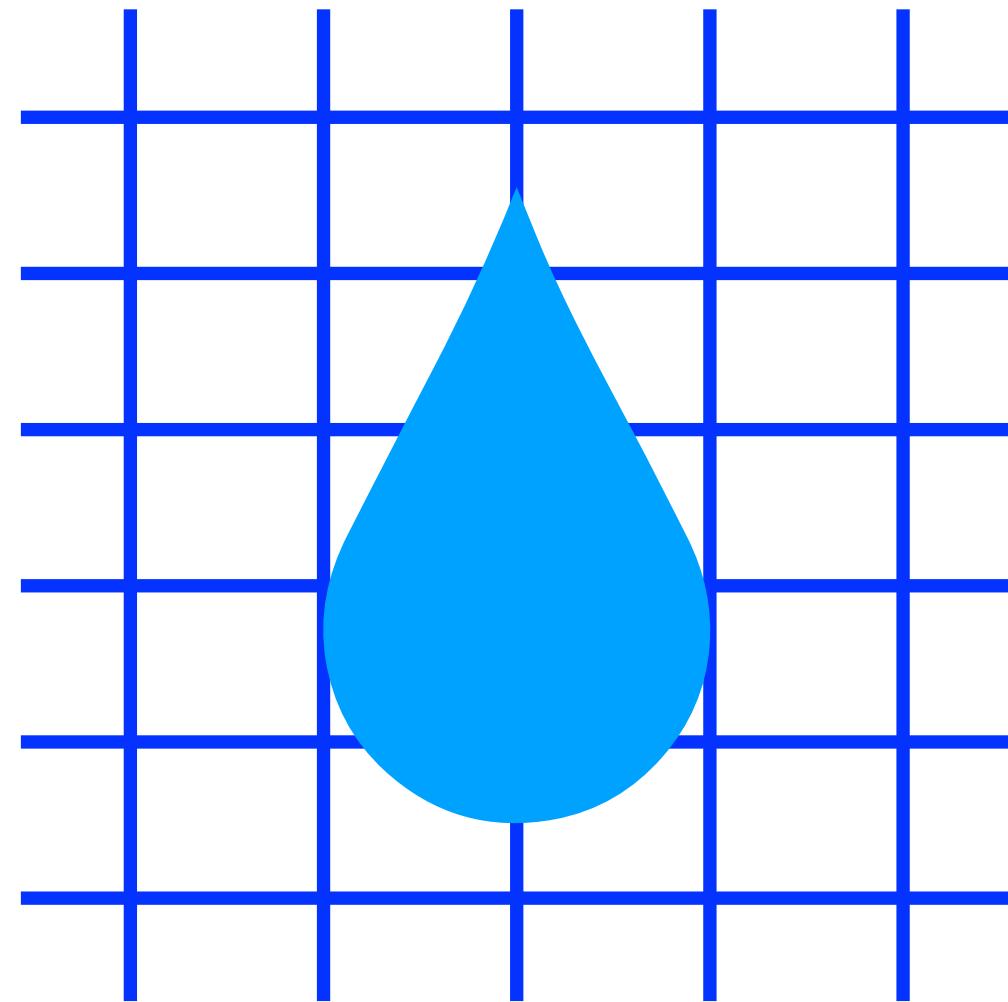
Gao et al. 18

Discretization schemes

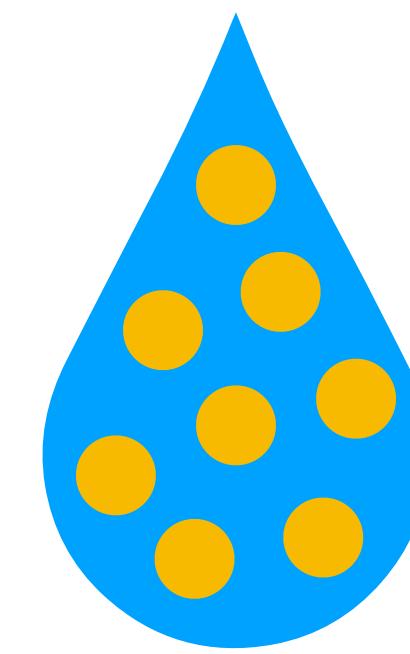


Grid

Discretization schemes

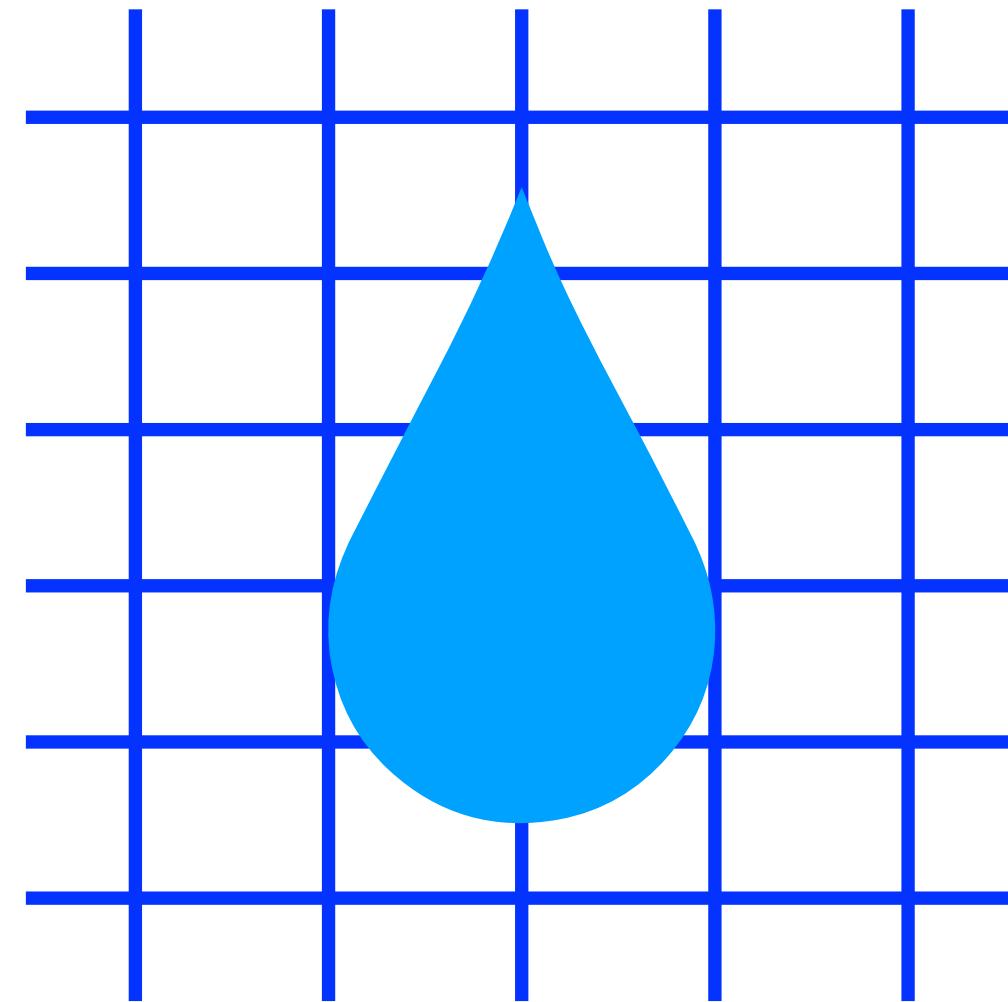


Grid

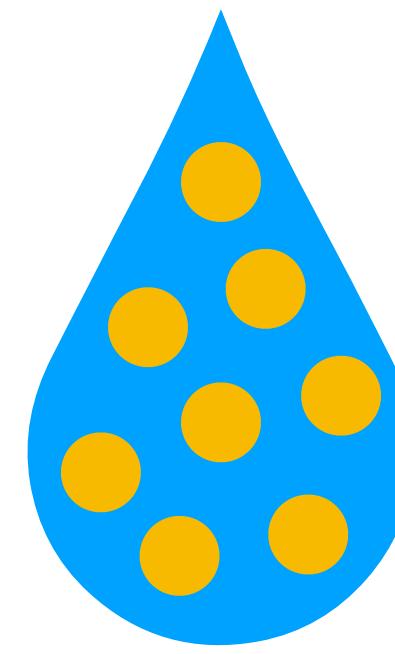


Particle

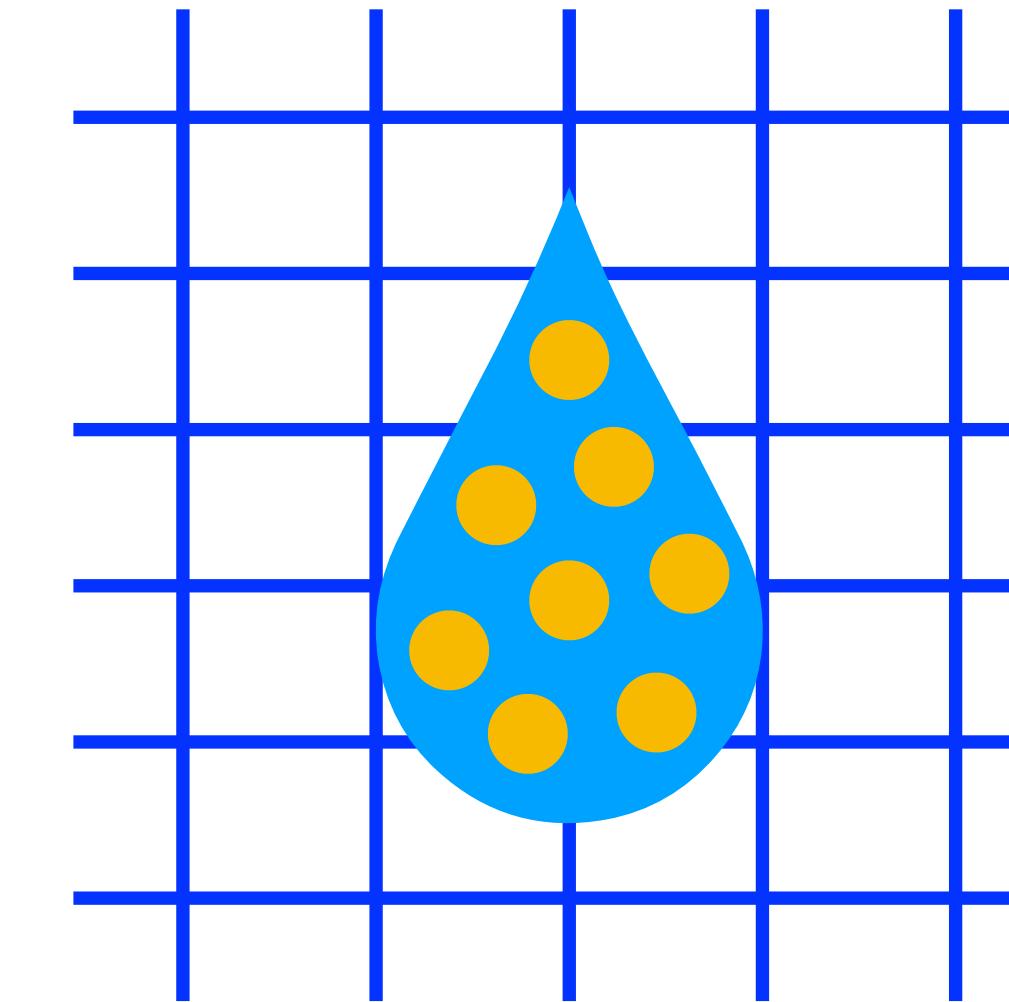
Discretization schemes



Grid

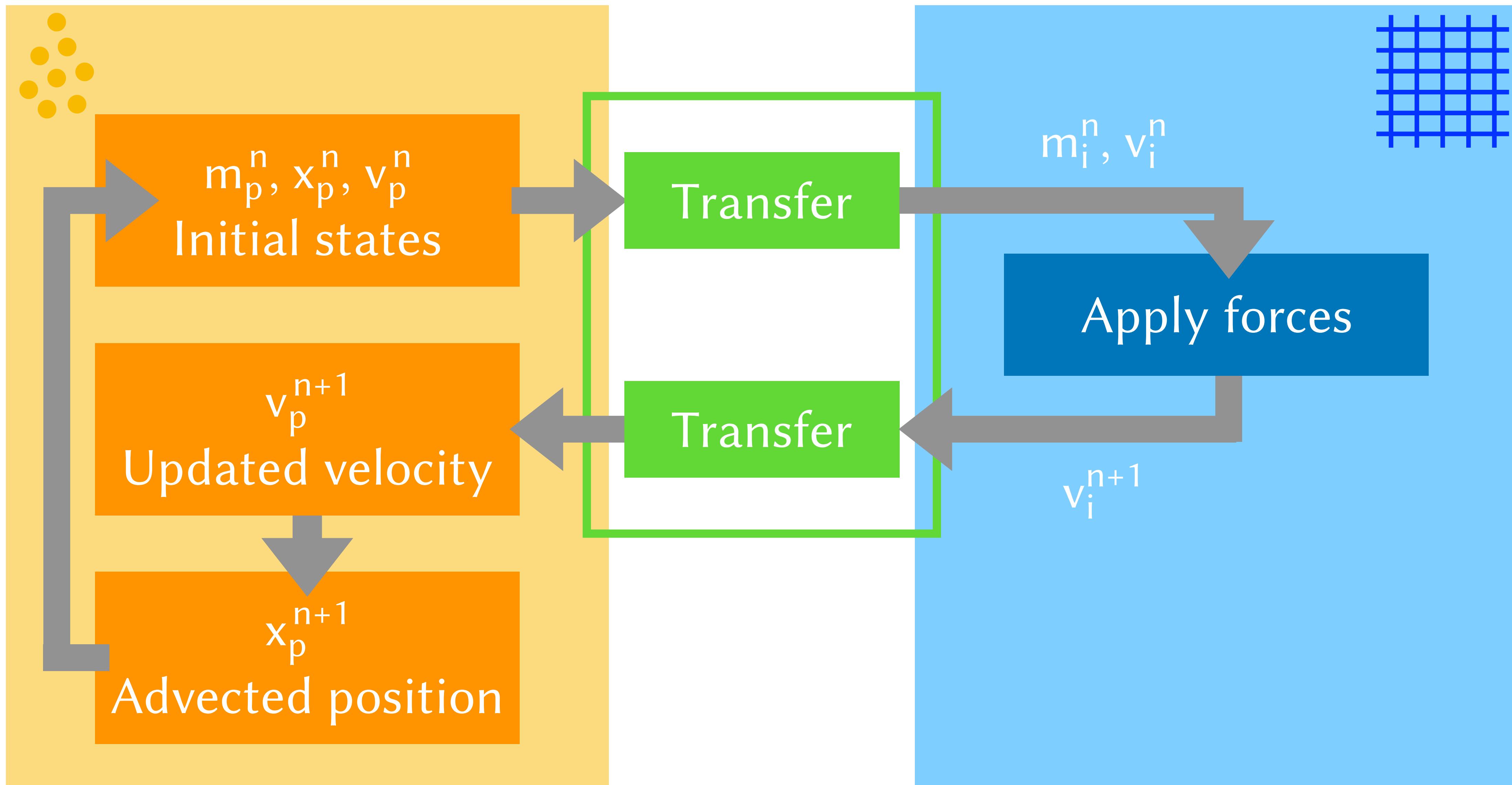


Particle

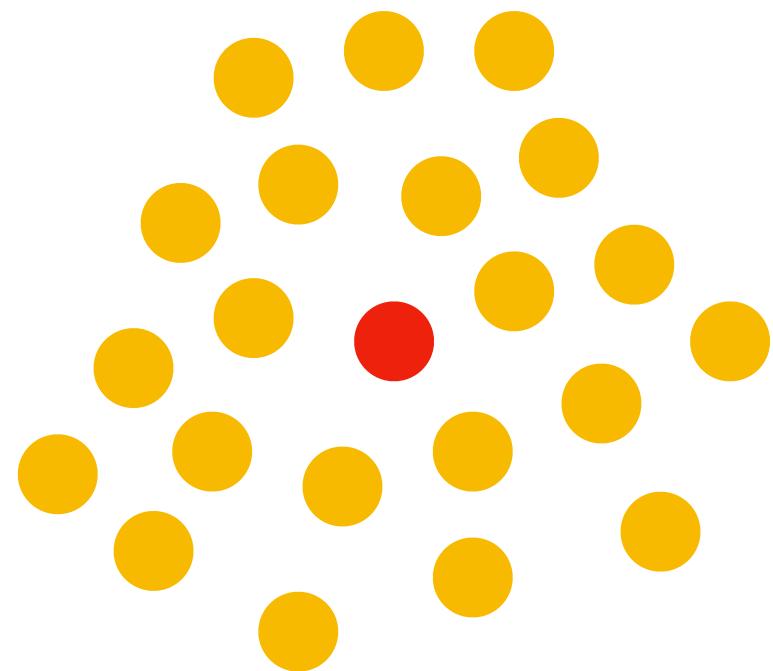


Hybrid

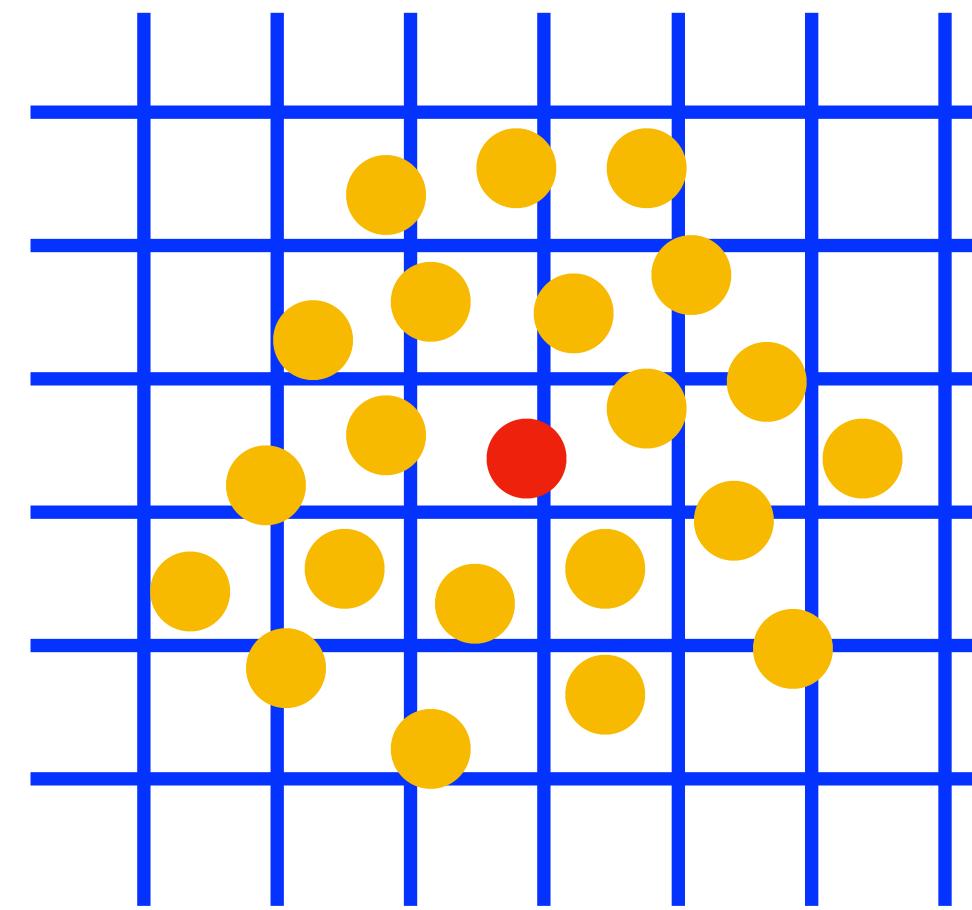
Data flow



Particle communication

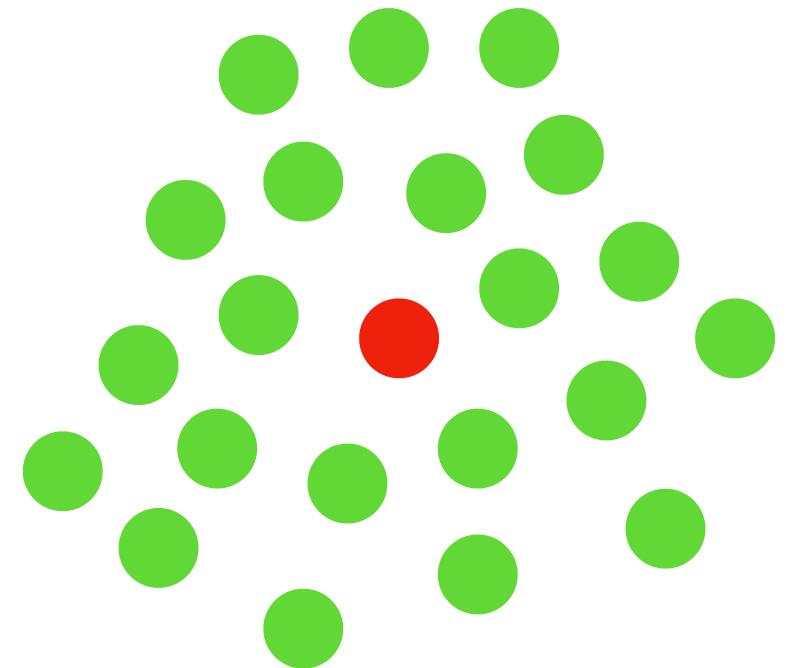


SPH

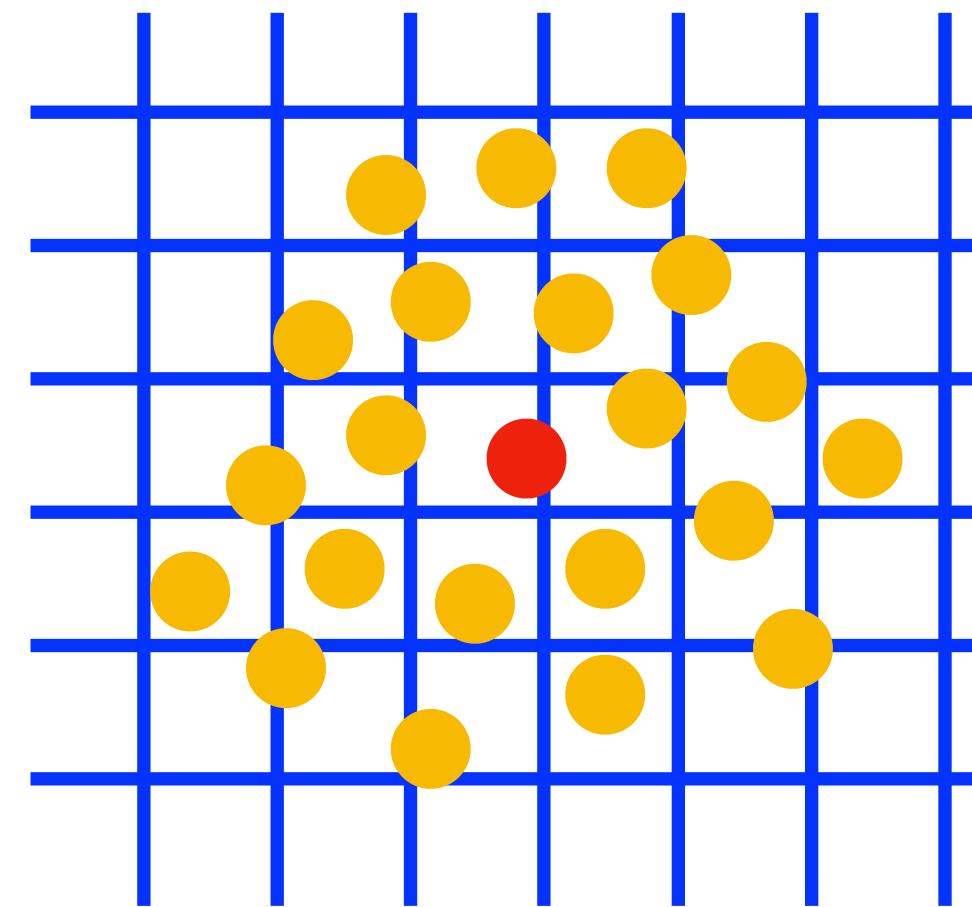


MPM

Particle communication

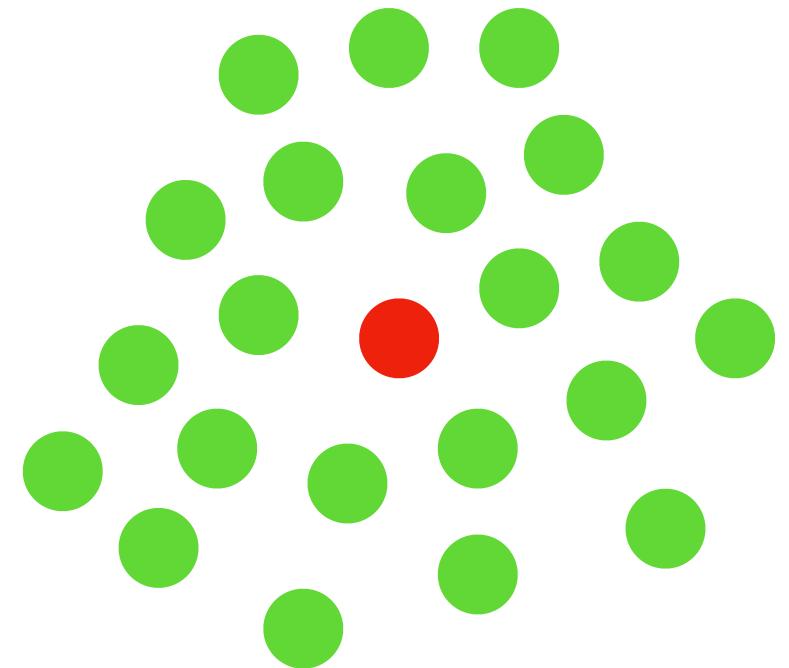


SPH

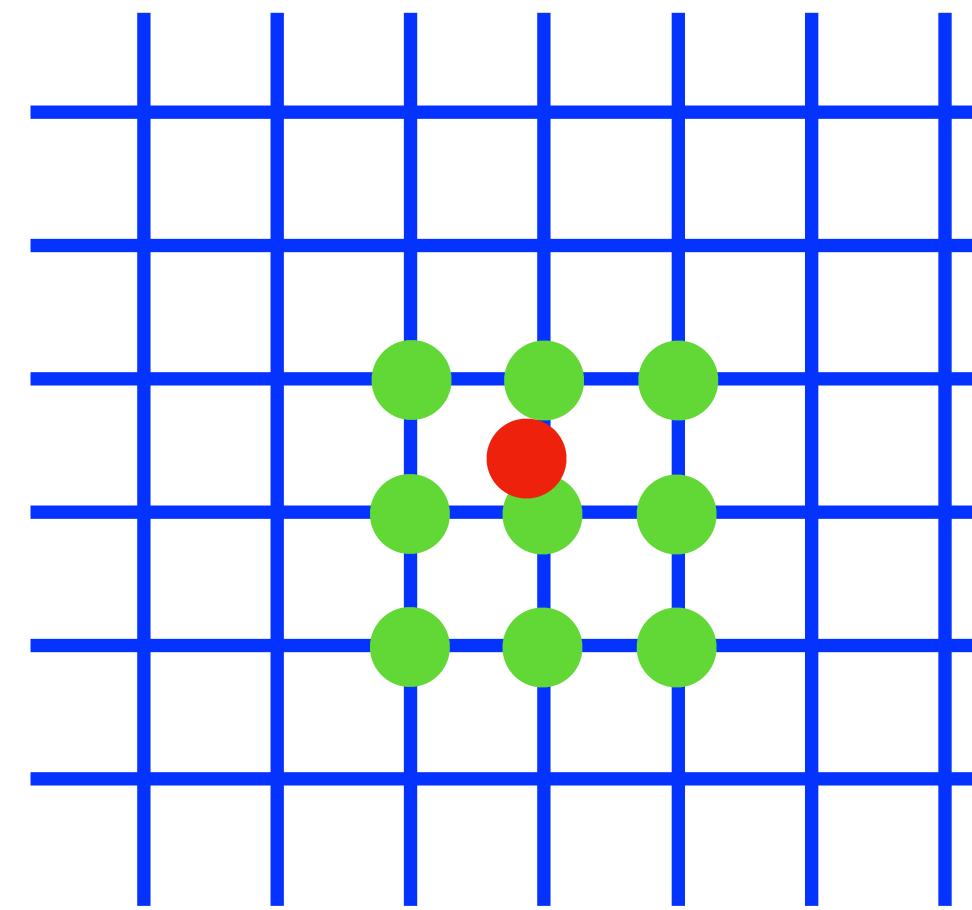


MPM

Particle communication

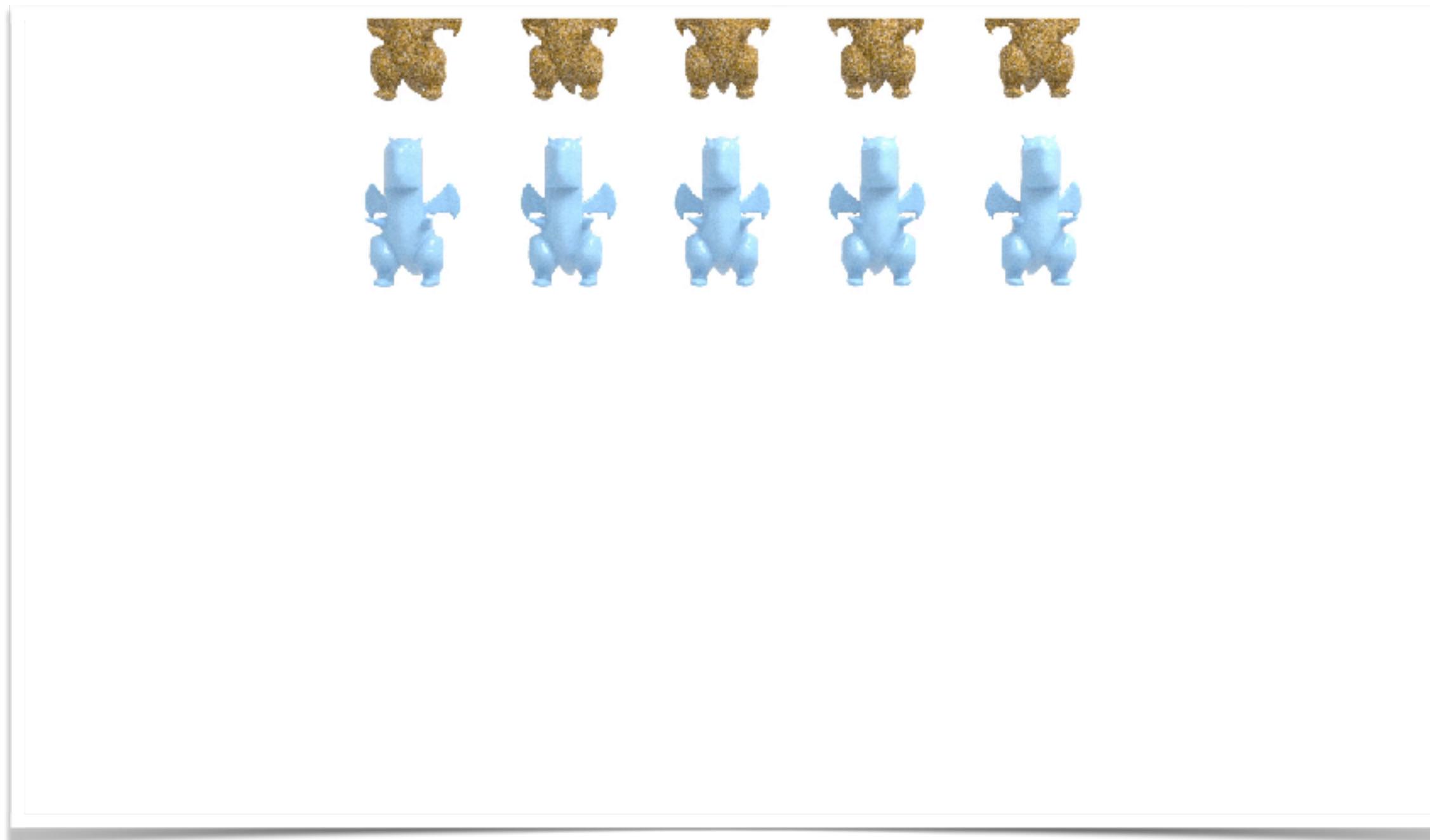


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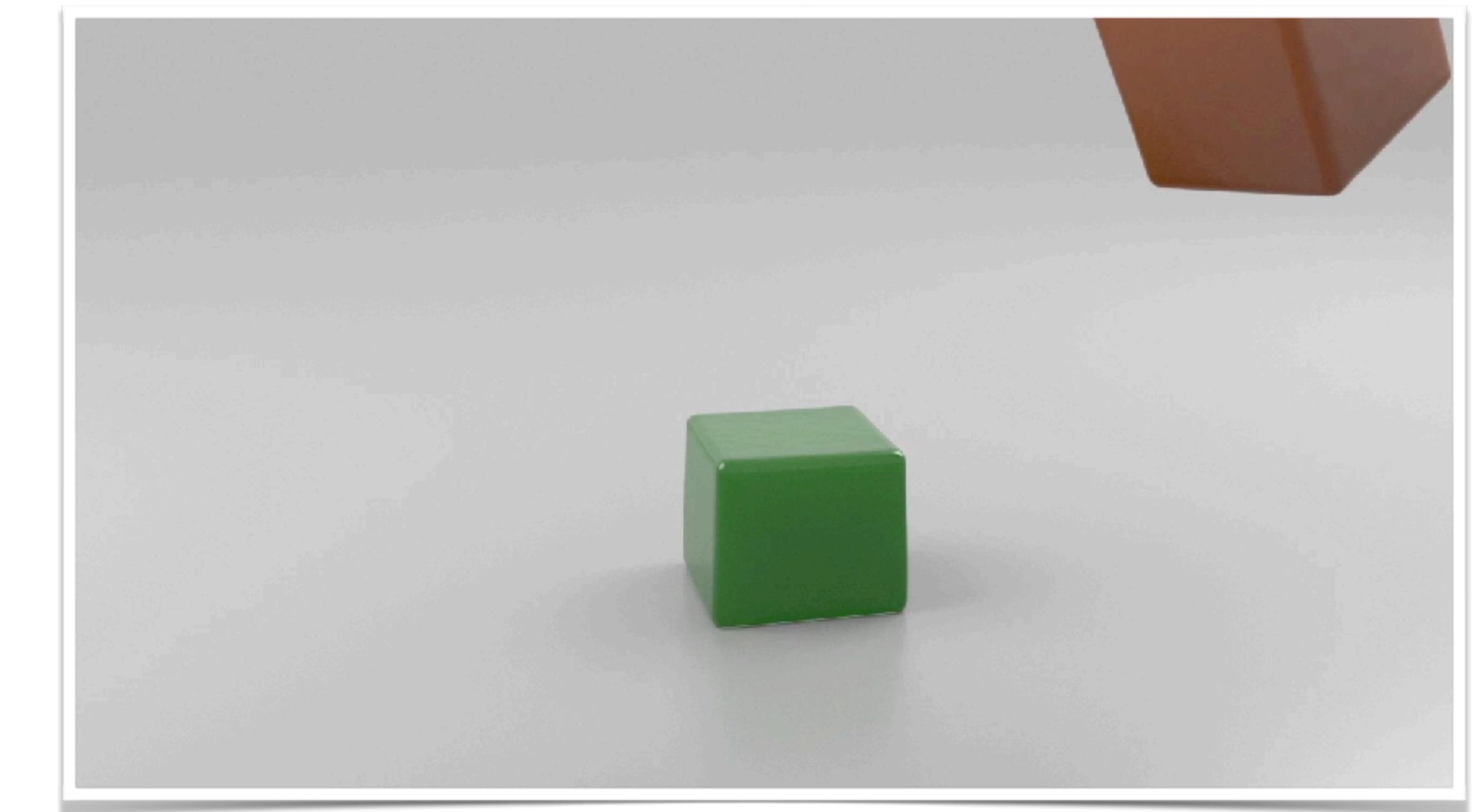


MPM

Sparsity



Gao et al. 18



Gao et al. 17

Power Diagrams and Sparse Paged Grids for High Resolution Adaptive Liquids

Power Diagrams and Sparse Paged Grids for High Resolution Adaptive Liquids

MRIDUL AANJANEYA^{†*}, Rutgers University
MING GAO[†] and HAI XIANG LIU, University of Wisconsin - Madison
CHRISTOPHER BATTY, University of Waterloo
EFTYCHIOS SIFAKIS, University of Wisconsin - Madison

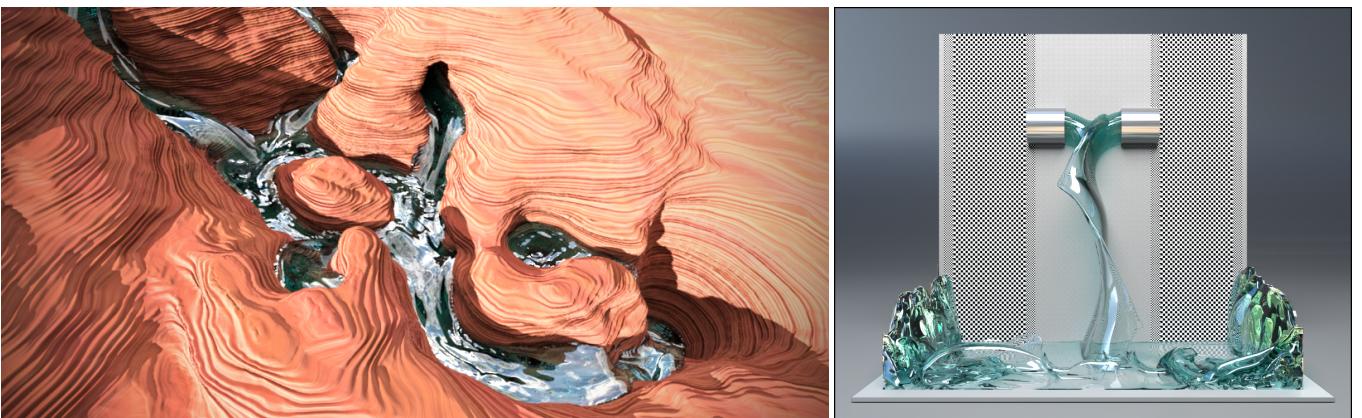


Fig. 1. (Left) Water filling a river bed surrounded by a canyon, with effective resolution $512^2 \times 1024$. Three refinement levels are used, based on proximity to the terrain. (Right) Sources inject water into a container and collide to form a thin sheet, with effective resolution 512^3 . Adaptivity pattern shown on background.

We present an efficient and scalable octree-inspired fluid simulation framework with the flexibility to leverage adaptivity in any part of the computational domain, even when resolution transitions reach the free surface. Our methodology ensures symmetry, definiteness and second order accuracy of the discrete Poisson operator, and eliminates numerical and visual artifacts of prior octree schemes. This is achieved by adapting the operators acting on the octree's simulation variables to reflect the structure and connectivity of a *power diagram*, which recovers primal-dual mesh orthogonality and eliminates problematic T-junction configurations. We show how such operators can be efficiently implemented using a pyramid of sparsely populated uniform grids, enhancing the regularity of operations and facilitating parallelization. A novel scheme is proposed for encoding the topology of the power diagram in the neighborhood of each octree cell, allowing us to locally reconstruct it on the fly via a lookup table, rather than resorting to costly explicit meshing. The pressure Poisson equation is solved via a highly efficient, matrix-free multigrid preconditioner for Conjugate Gradient, adapted to the power diagram discretization. We use another sparsely

[†] M. Aanjaneya and M. Gao are joint first authors.

* M. Aanjaneya was with the University of Wisconsin - Madison during this work.

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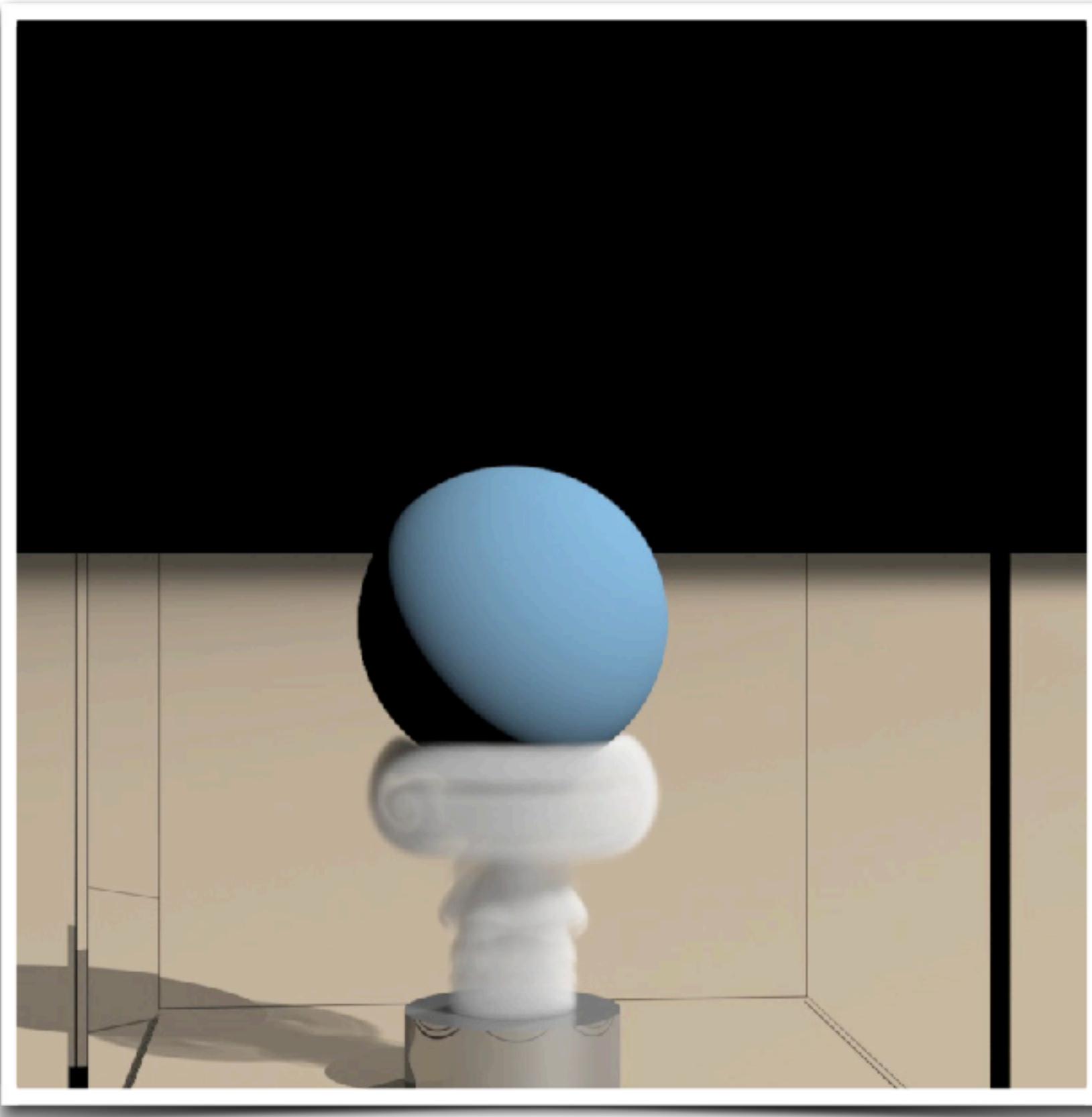
DOI: <http://dx.doi.org/10.1145/3072959.3073625>

M. Aanjaneya*, M. Gao* (joint first authors), H. Liu, C. Batty, E. Safaris
ACM Transactions on Graphics (Proceedings of ACM SIGGRAPH), 2017

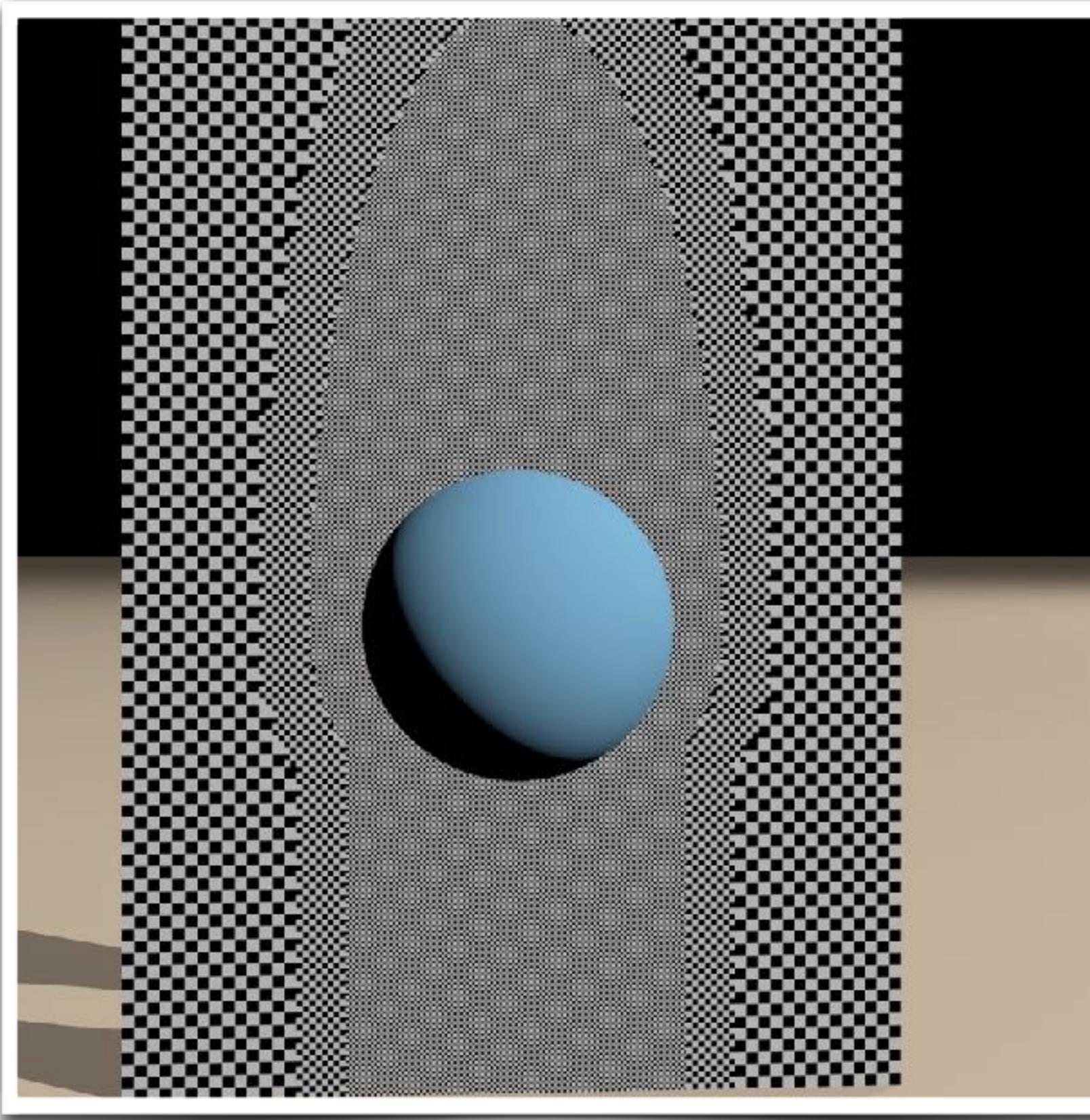
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SIGGRAPH 2017



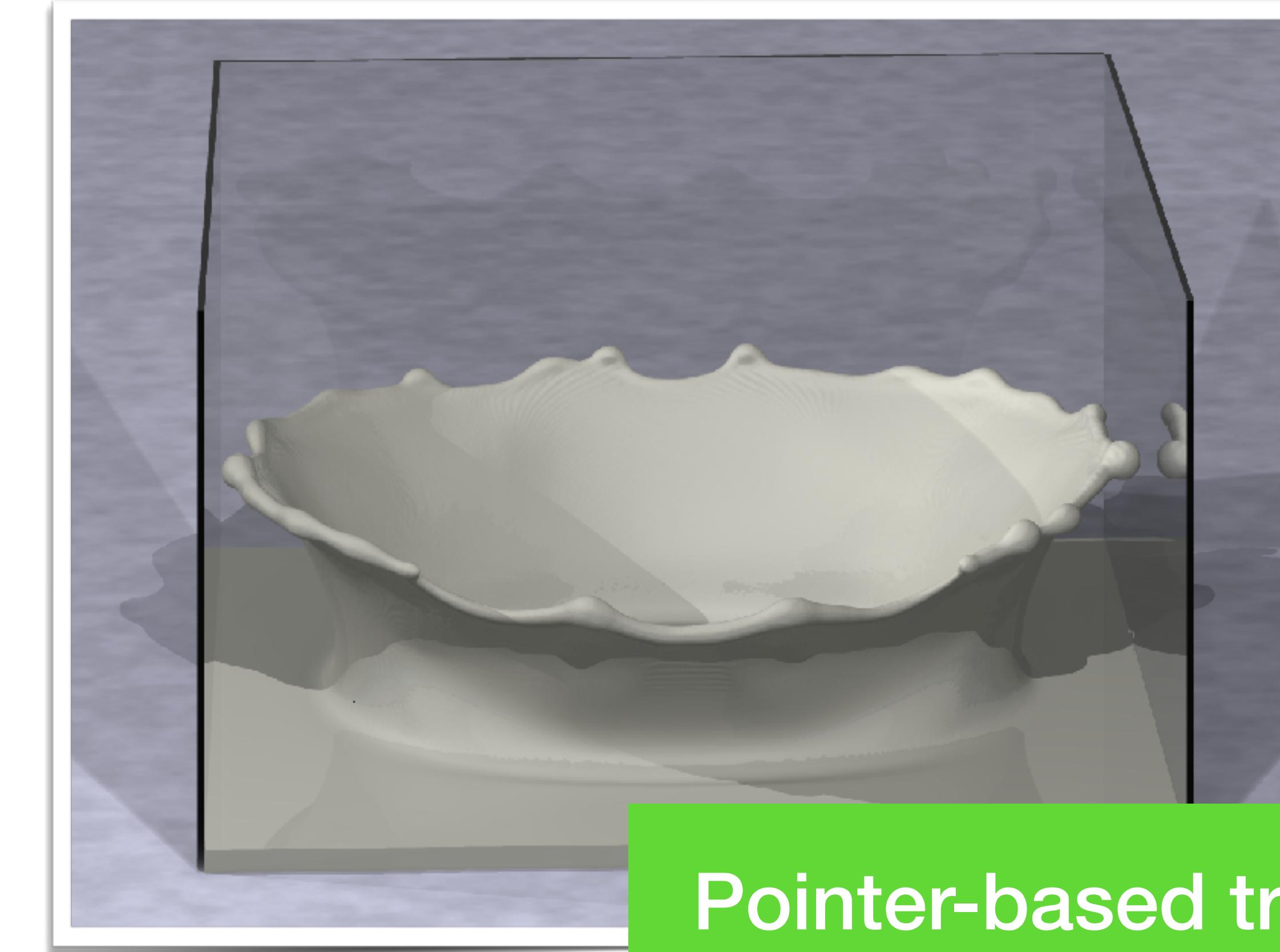
Previous work



Previous work



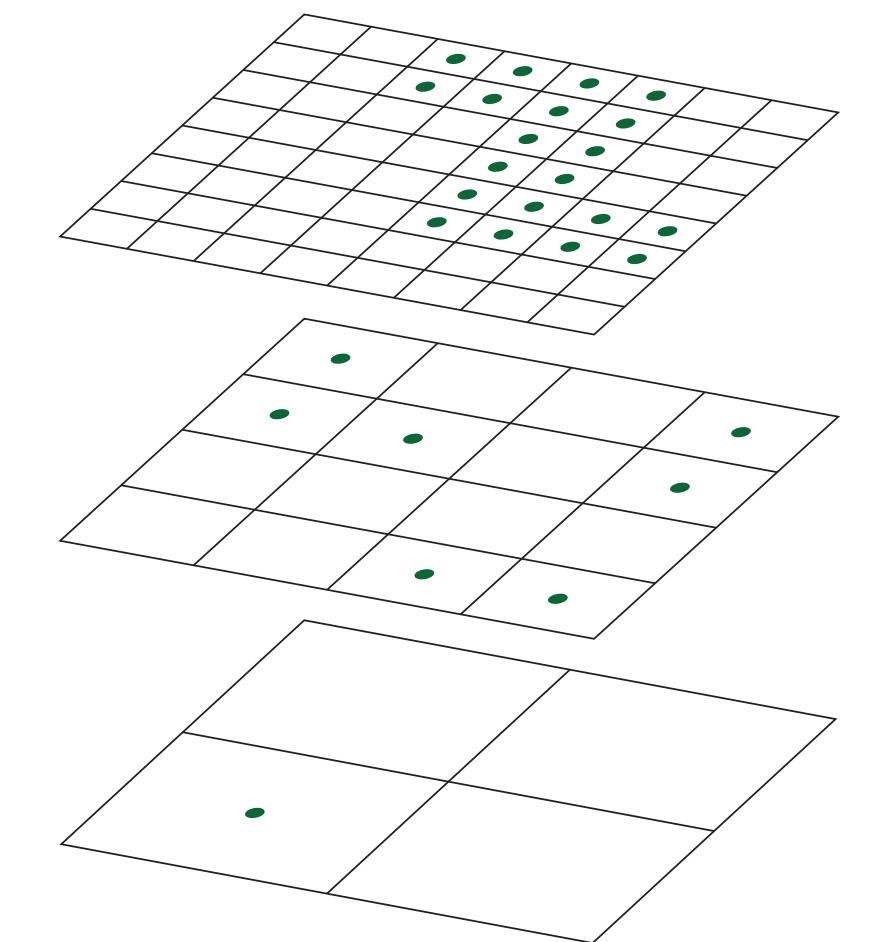
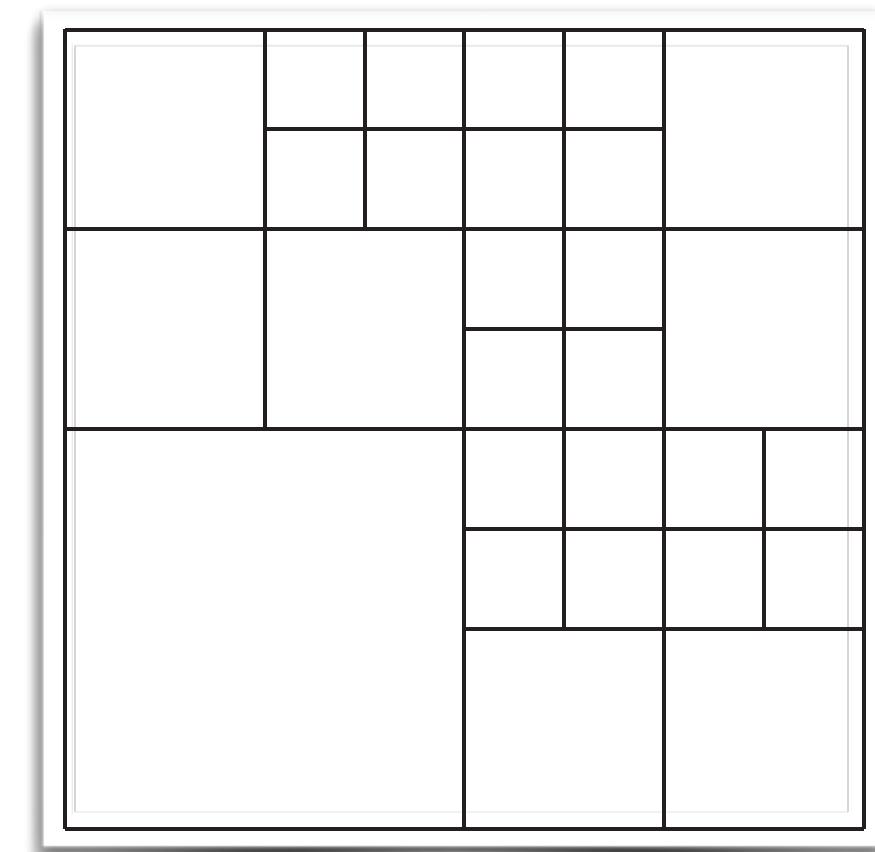
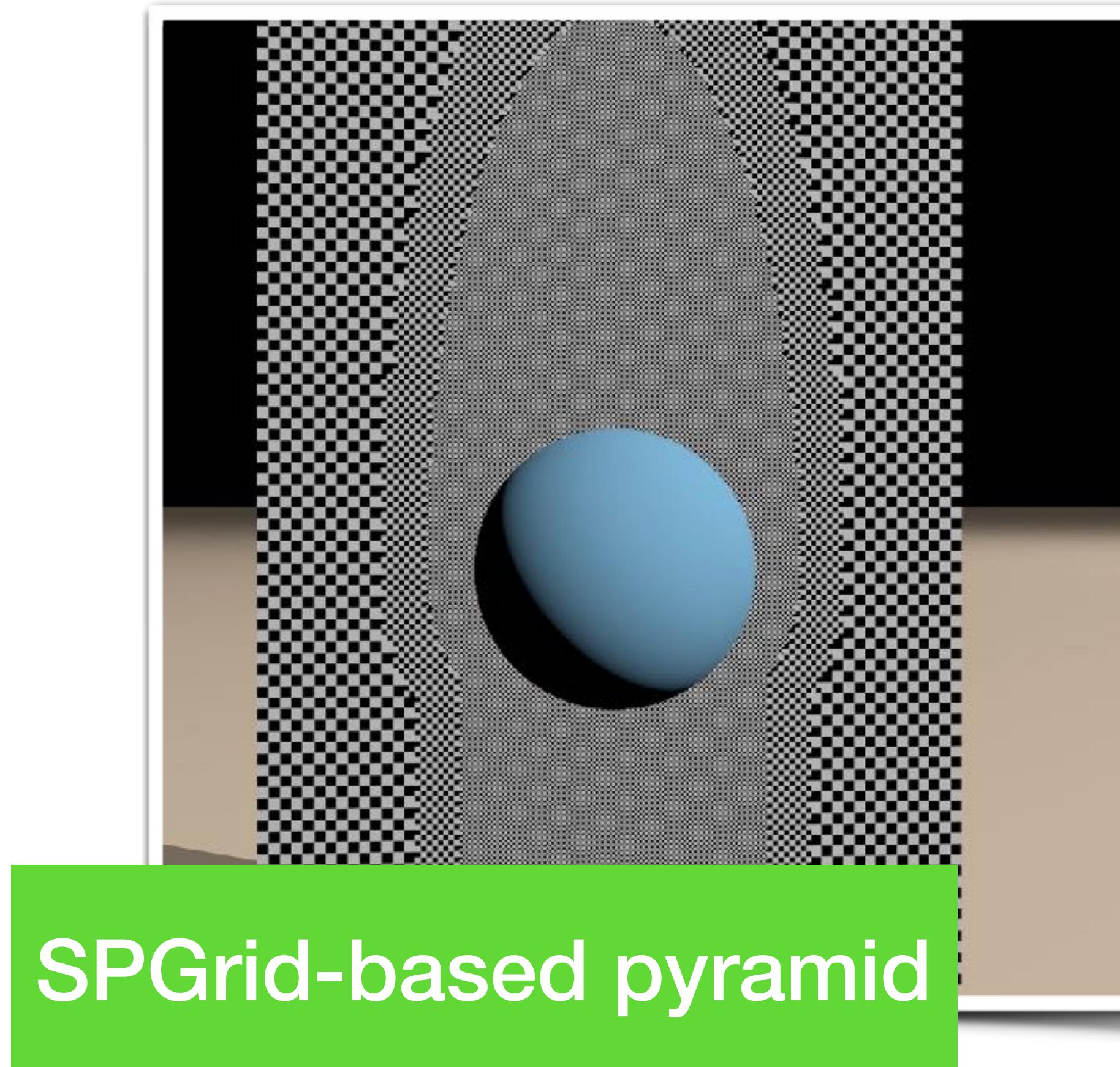
Setaluri et al. 14



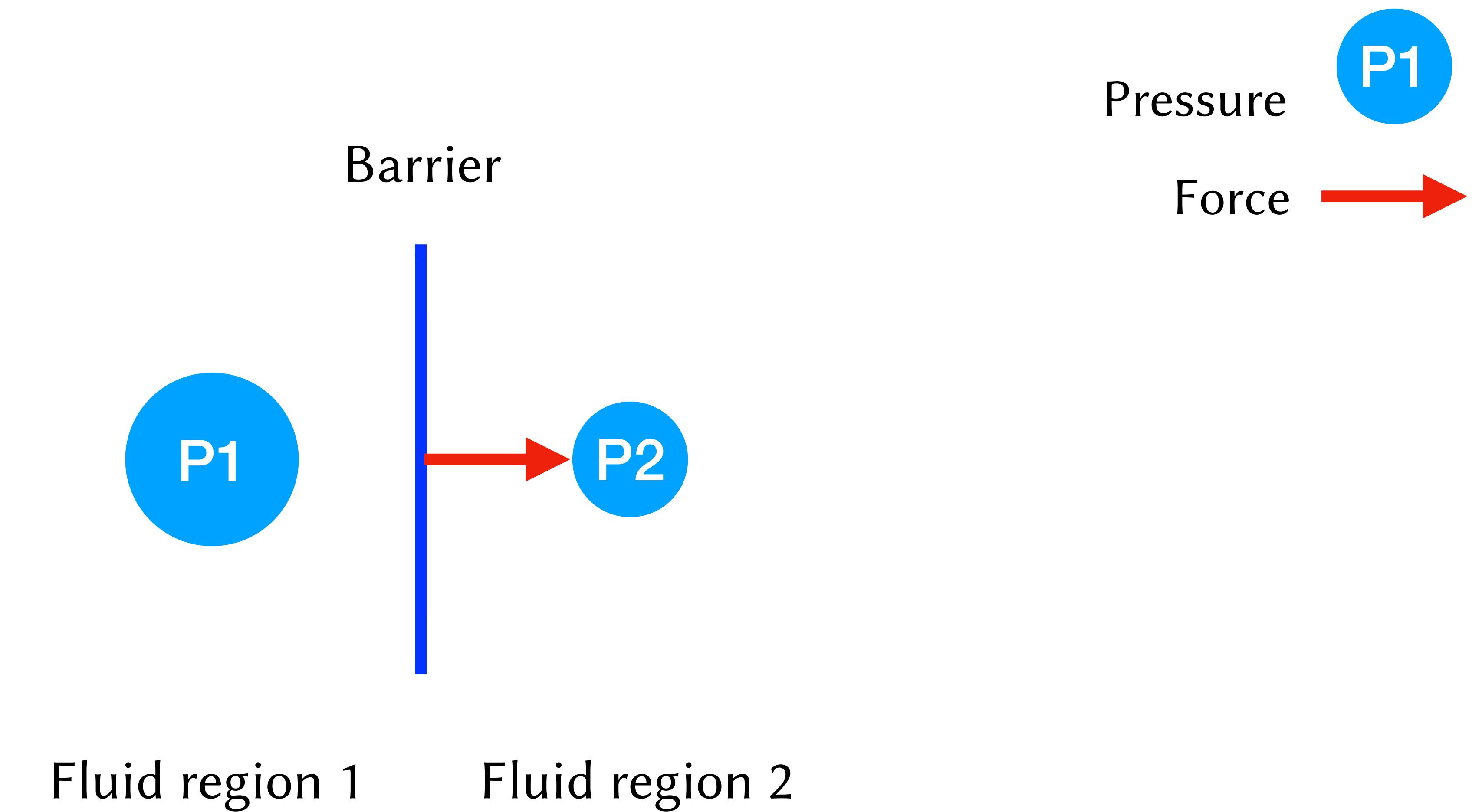
Pointer-based tree

Losasso et al. 04

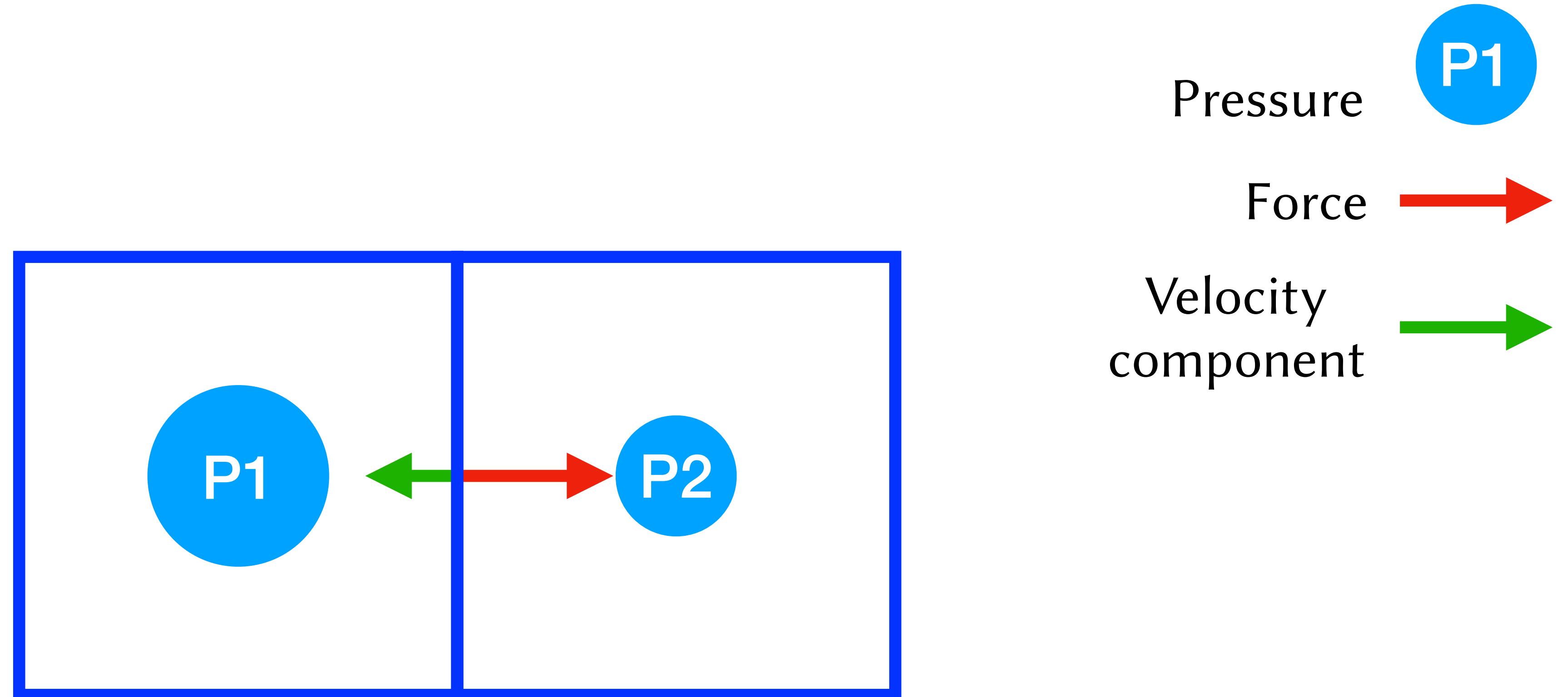
Previous work



Loss of orthogonality

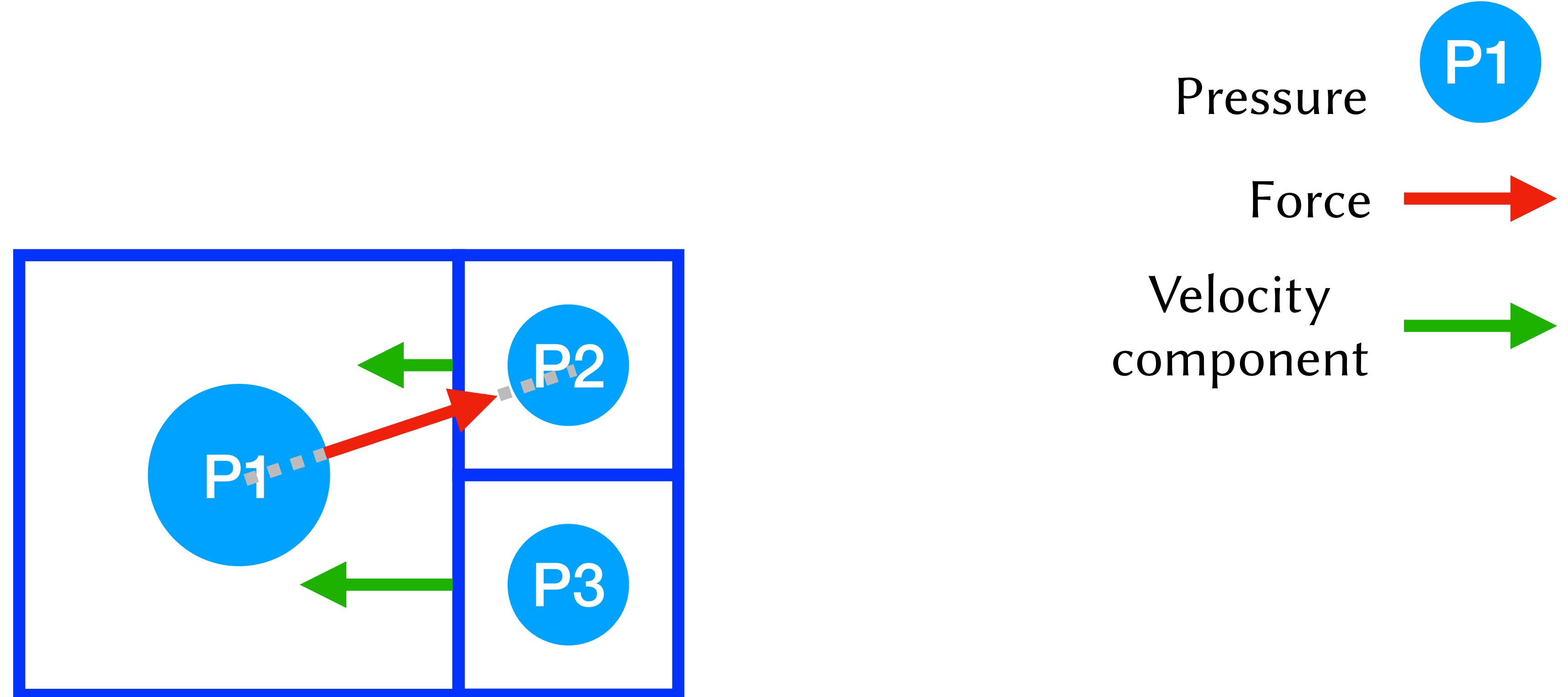


Loss of orthogonality

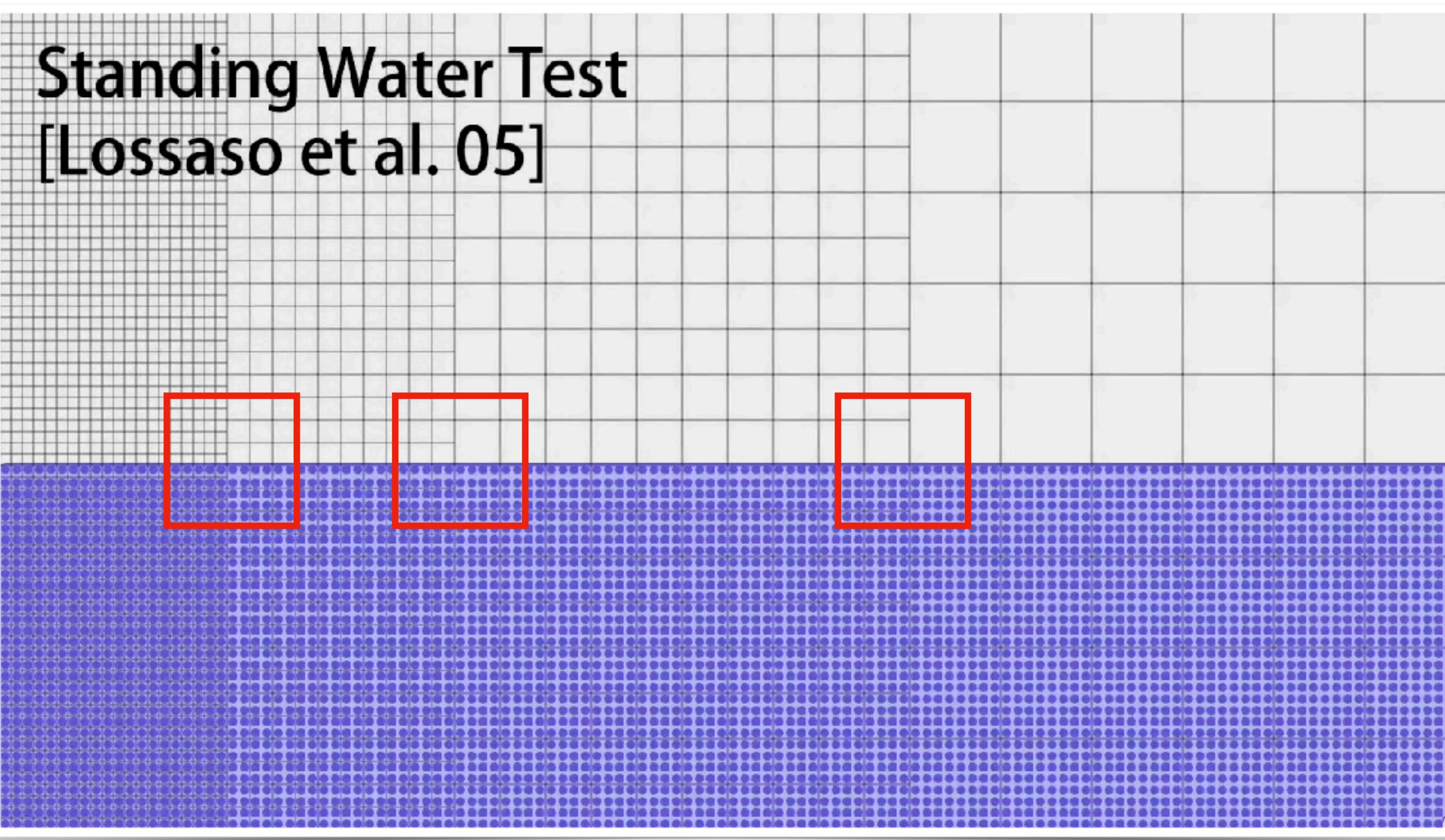


Staggered grid

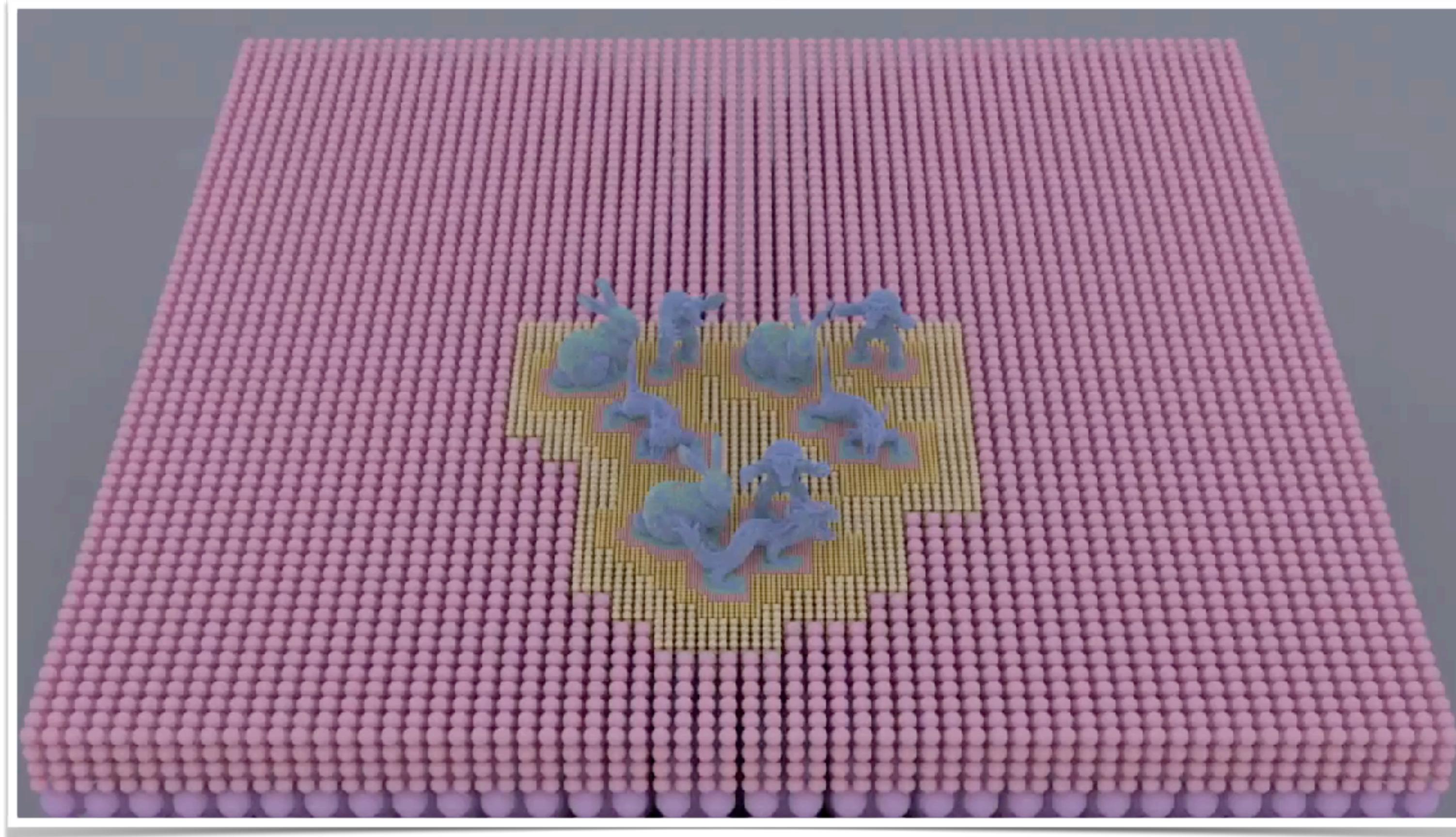
Loss of orthogonality



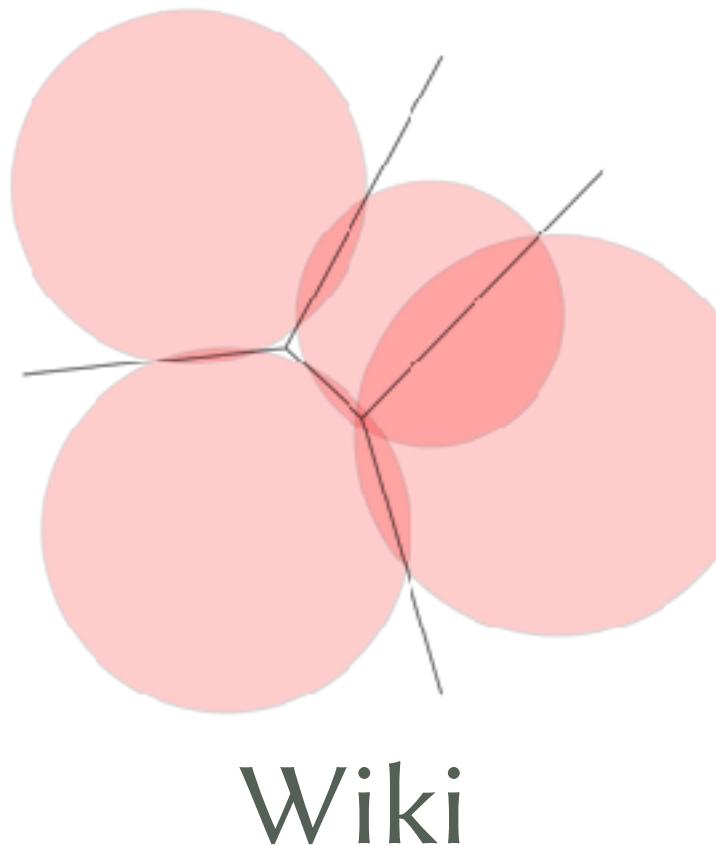
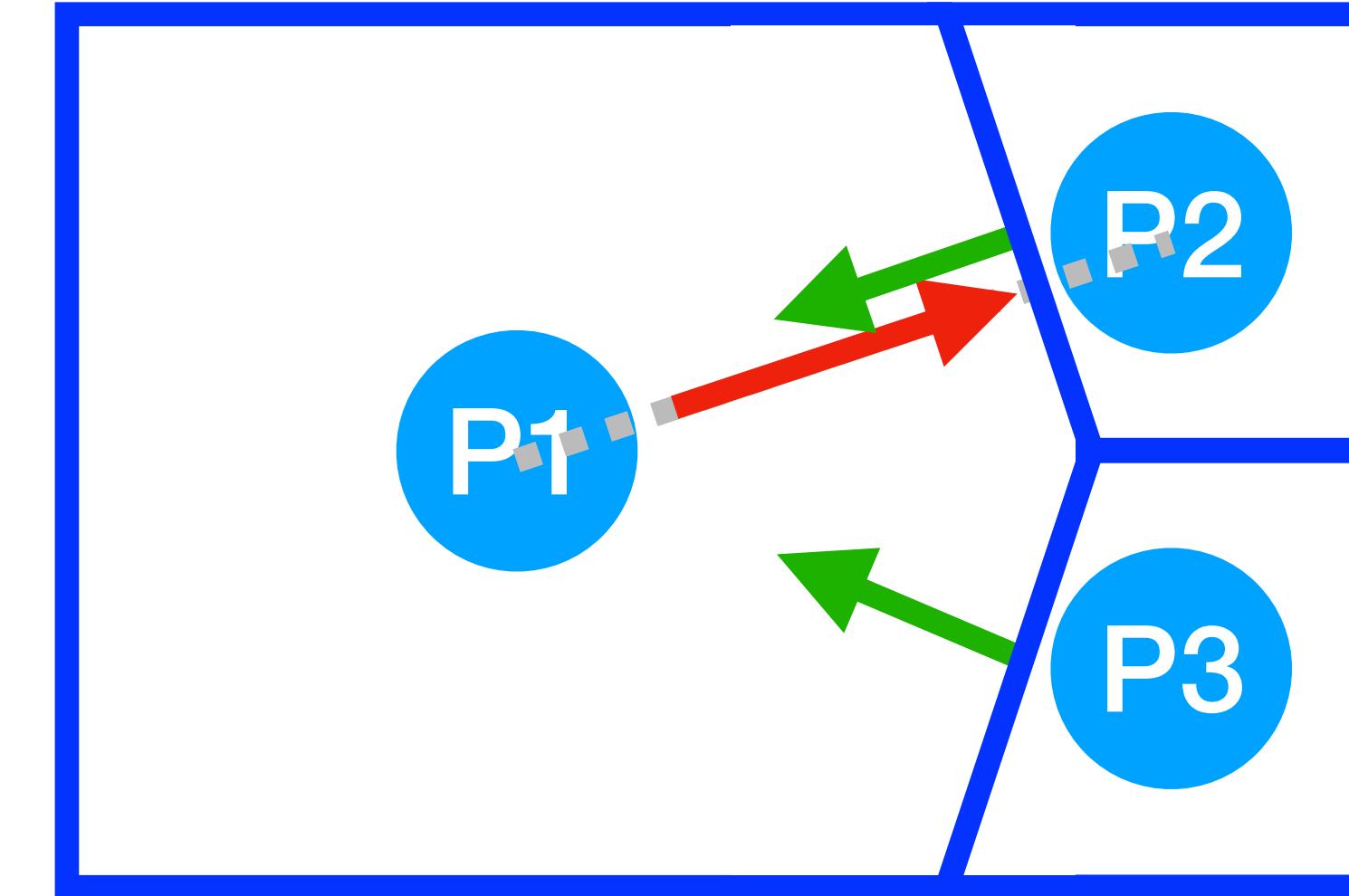
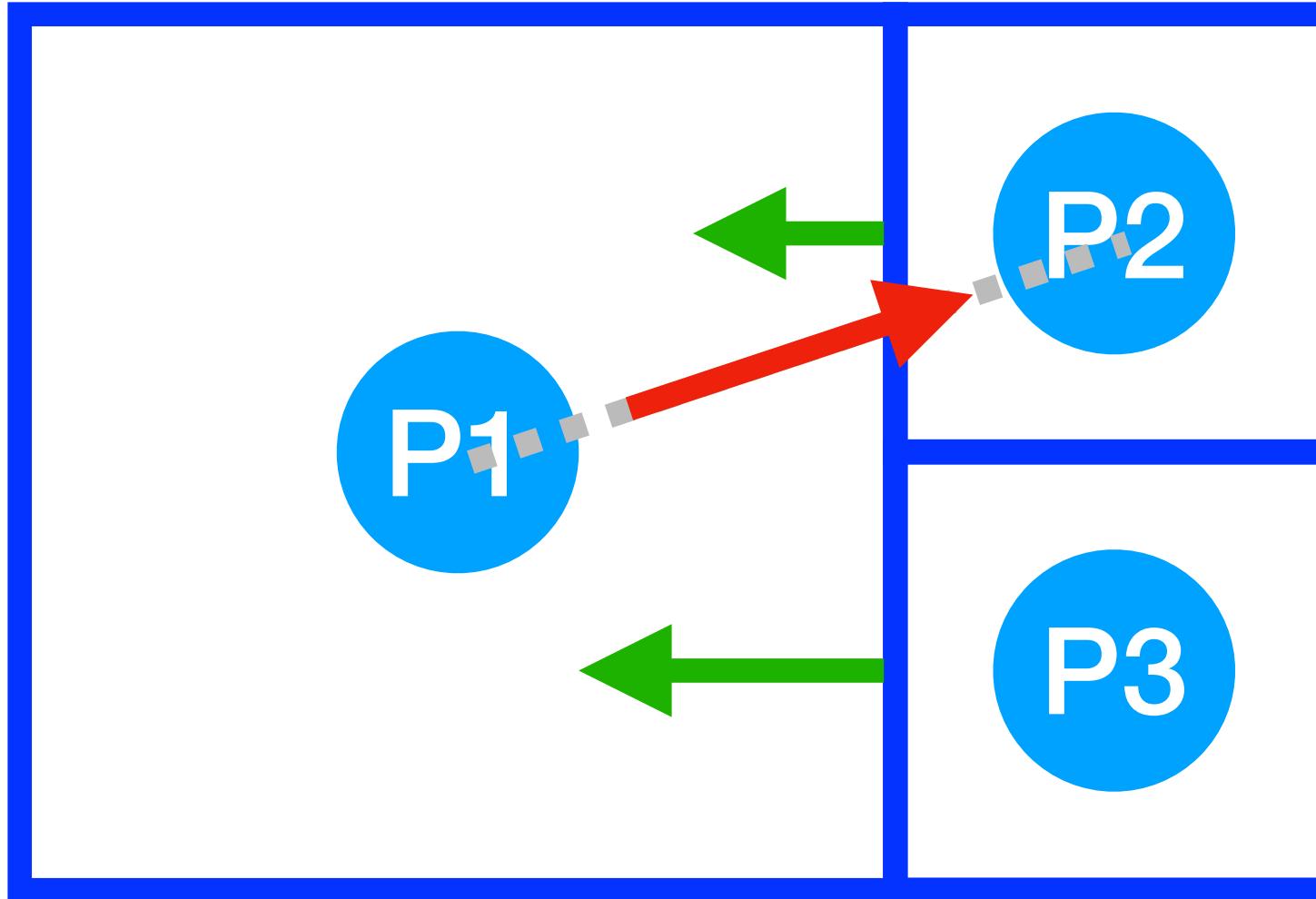
Spurious motions



Unstructured mesh

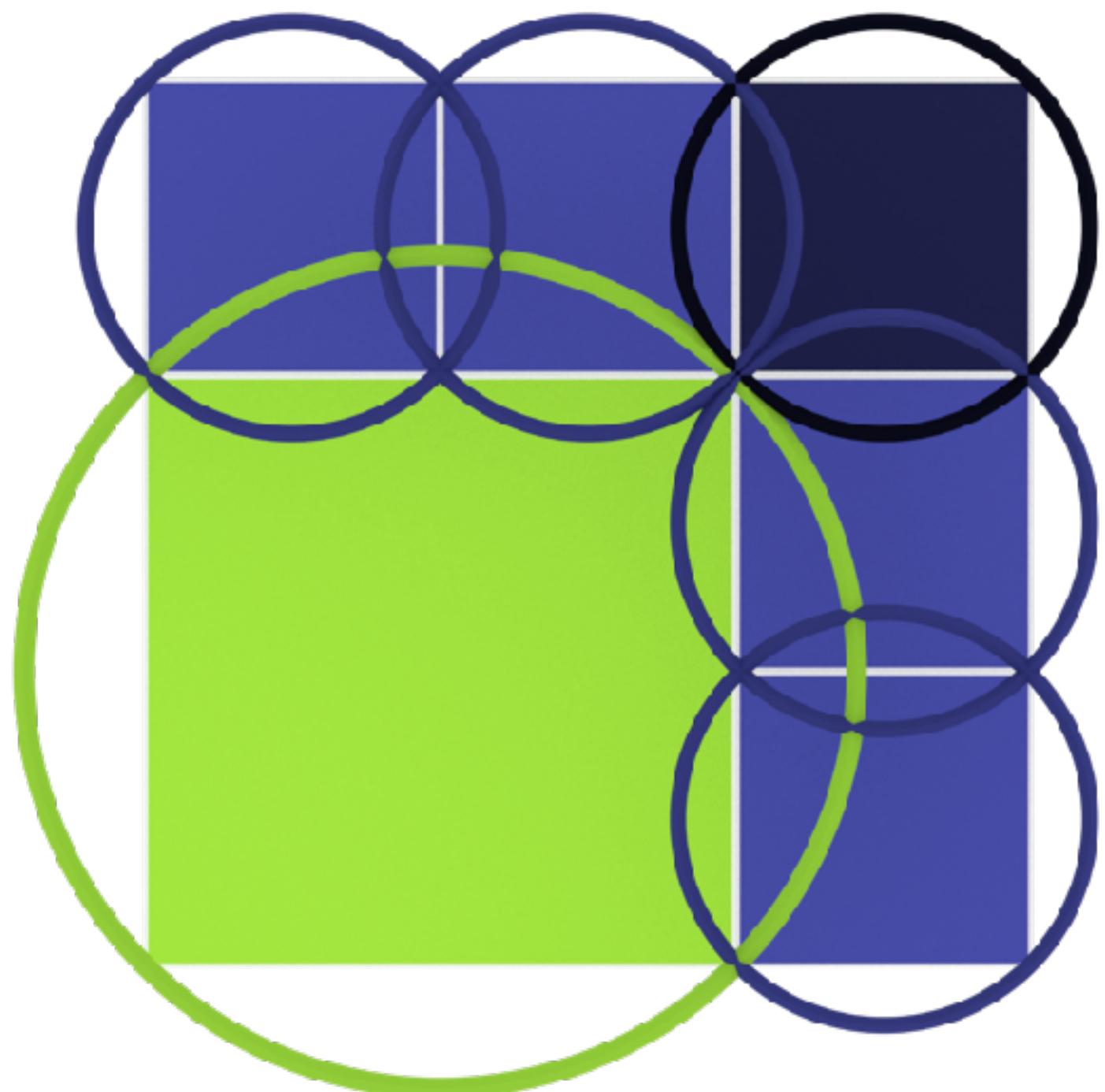


Our solution: power diagram

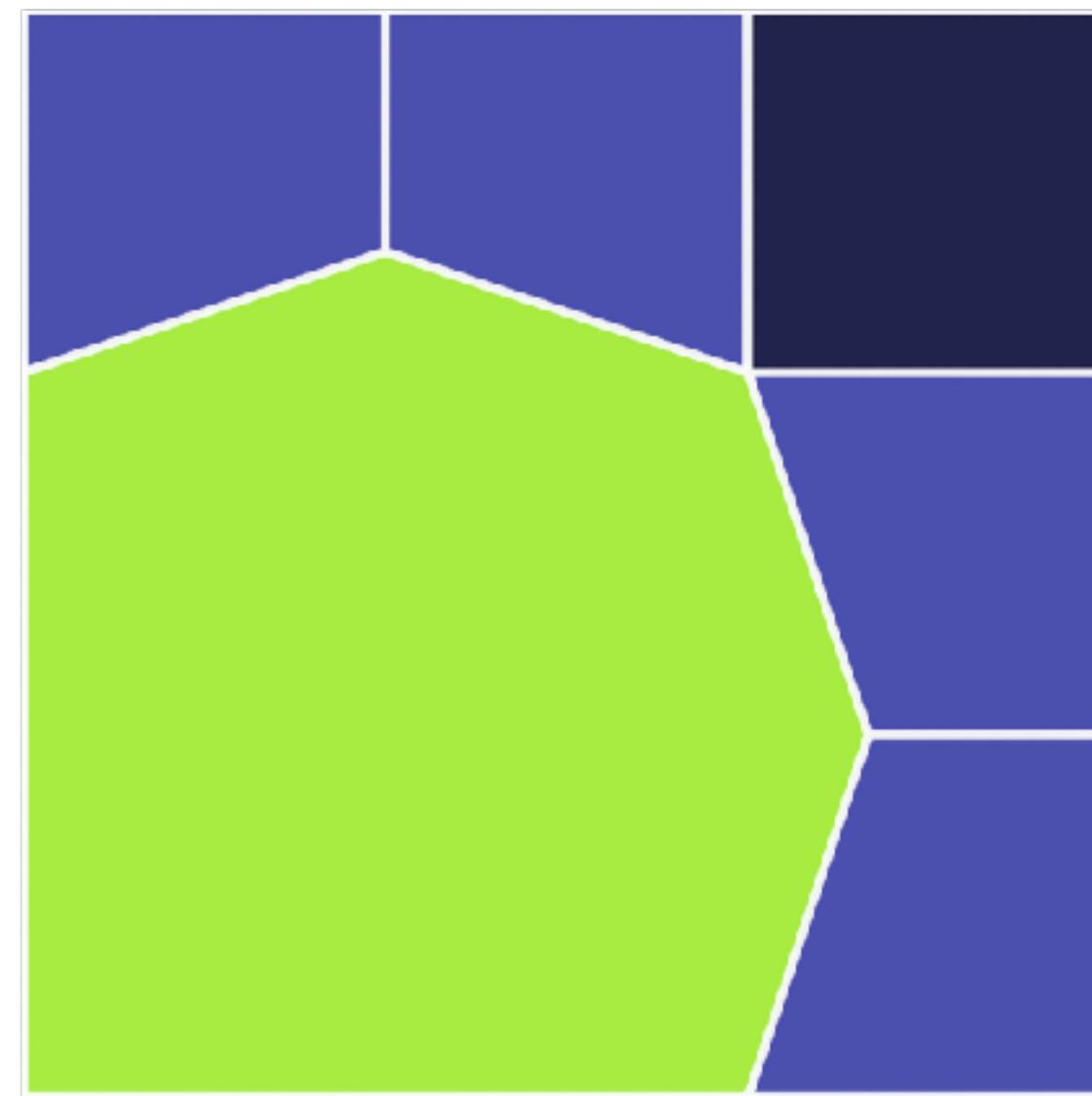


Comparison

Original topology

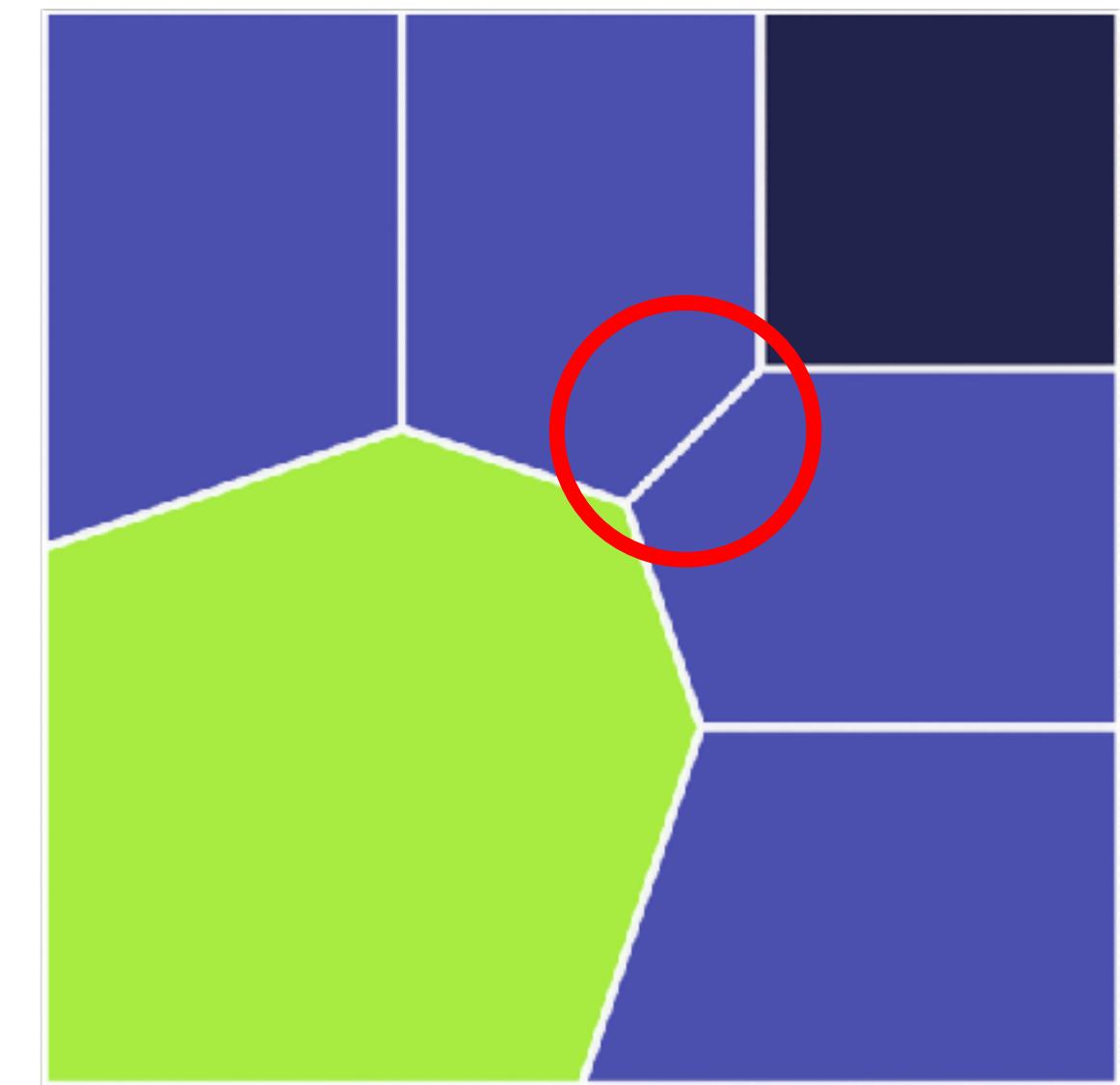


Power diagram



$$d^2 - r^2$$

Voronoi diagram



$$d^2$$

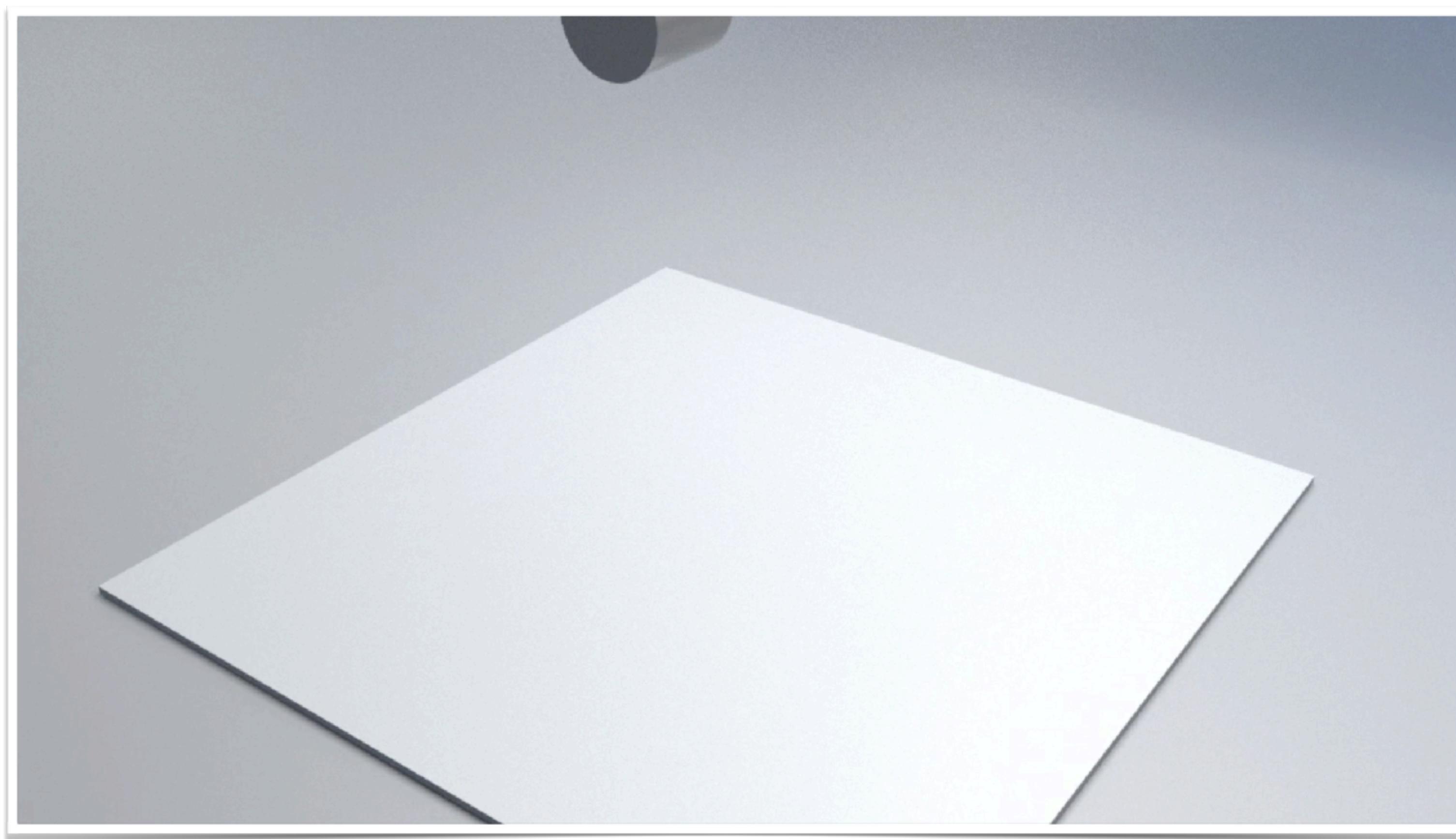
Opportunities

- Power diagram ensures orthogonality
- Can still use octree for storage
- Accelerate via SPGrid

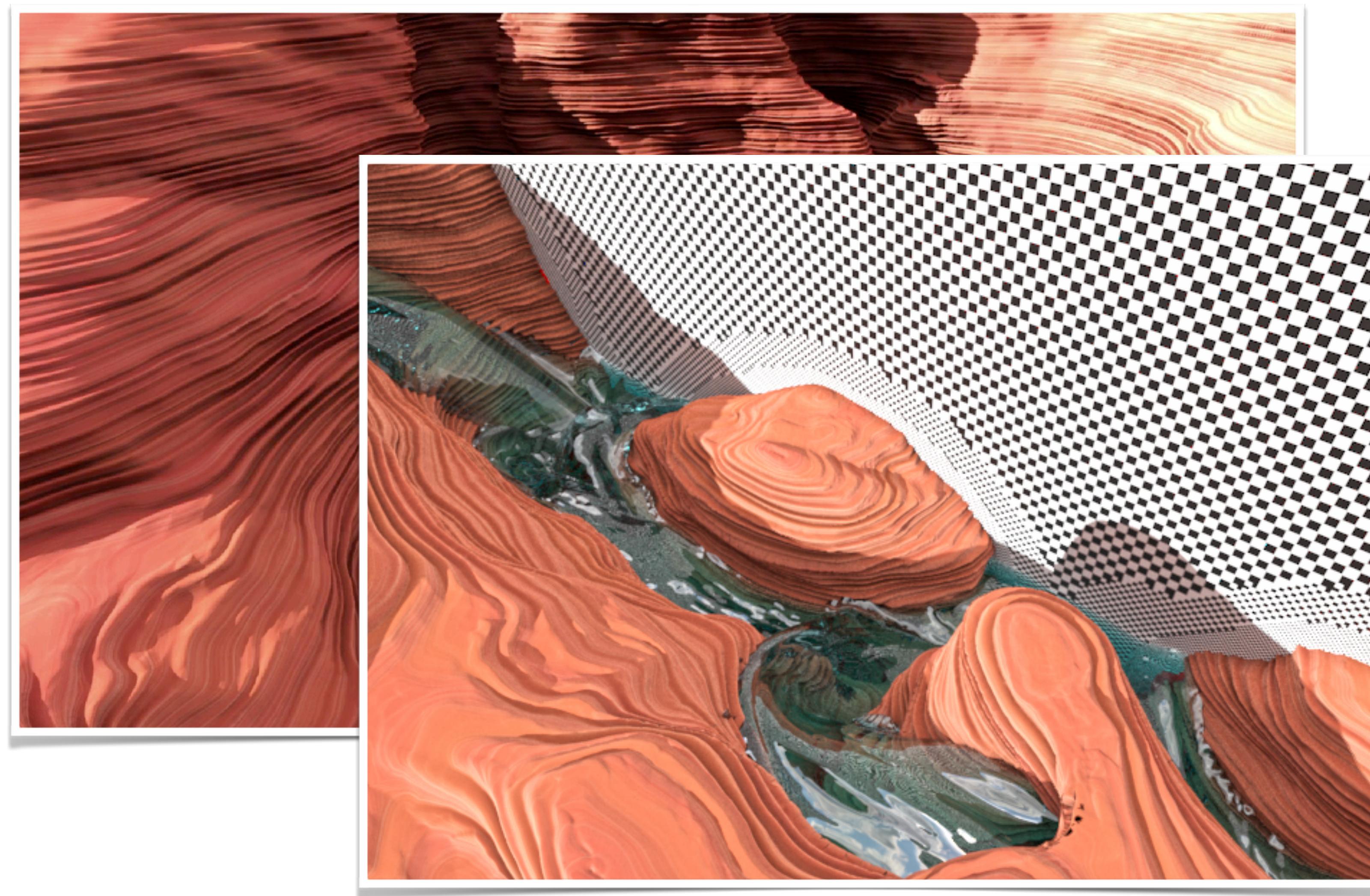
Further technicalities (see thesis)

- Minor topological complications (3D)
- Velocity interpolation
- Retrieval of Poisson equation stencils

Results



Results



An Adaptive Generalized Interpolation Material Point Method for Simulating Elastoplastic Materials

An Adaptive Generalized Interpolation Material Point Method for Simulating Elastoplastic Materials

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ANDRE PRADHANA TAMPUBOLON, University of Pennsylvania
CHENFANFU JIANG, University of Pennsylvania
EFTYCHIOS SIFAKIS, University of Wisconsin Madison

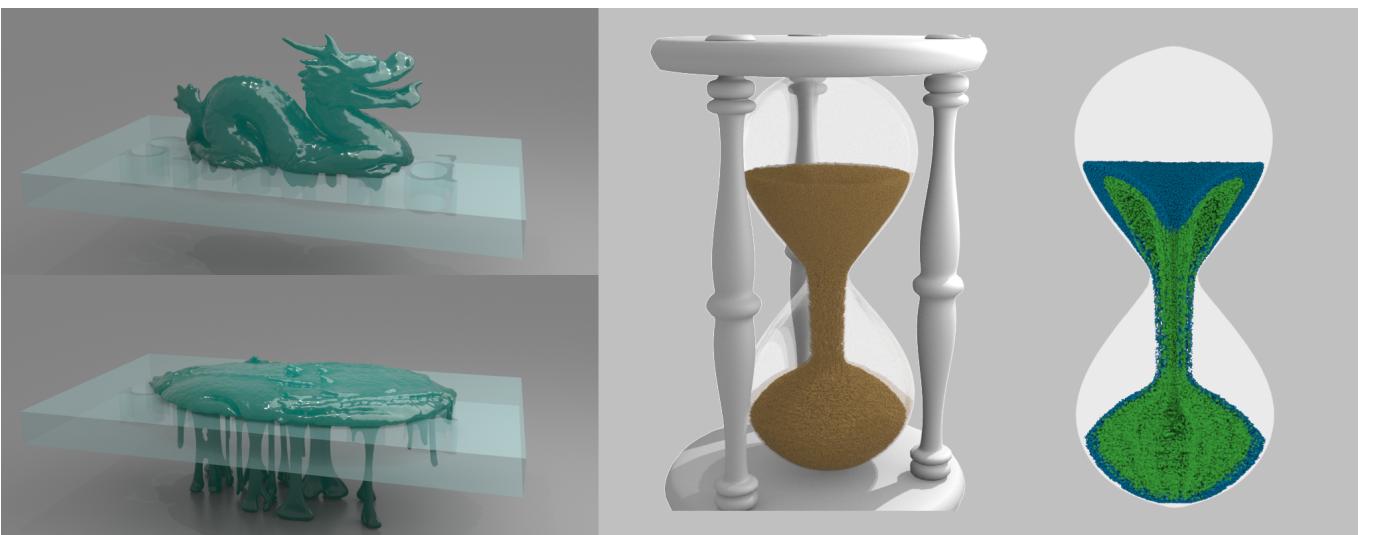


Fig. 1. Left: An elastoplastic model is dropped into a plane with a thin perforation pattern; our adaptive discretization allows the material to drip through. Right: Adaptive sand simulation with a visualization of the underlying grid refinement. We color refine particles with blue and coarse ones with green.

We present an adaptive Generalized Interpolation Material Point (GIMP) method for simulating elastoplastic materials. Our approach allows adaptive refining and coarsening of different regions of the material, leading to an efficient MPM solver that concentrates most of the computation resources in specific regions of interest. We propose a C^1 continuous adaptive basis function that satisfies the partition of unity property and remains non-negative throughout the computational domain. We develop a practical strategy for particle-grid transfers that leverages the recently introduced SPGrid data structure for storing sparse multi-layered grids. We demonstrate the robustness and efficiency of our method on the simulation of various elastic and plastic materials. We also compare key kernel components to uniform grid MPM solvers to highlight performance benefits of our method.

CCS Concepts: • Computing methodologies → Physical simulation;

Additional Key Words and Phrases: Material Point Method (MPM), Generalized Interpolation Material Point (GIMP), Adaptive grids, Elastoplasticity

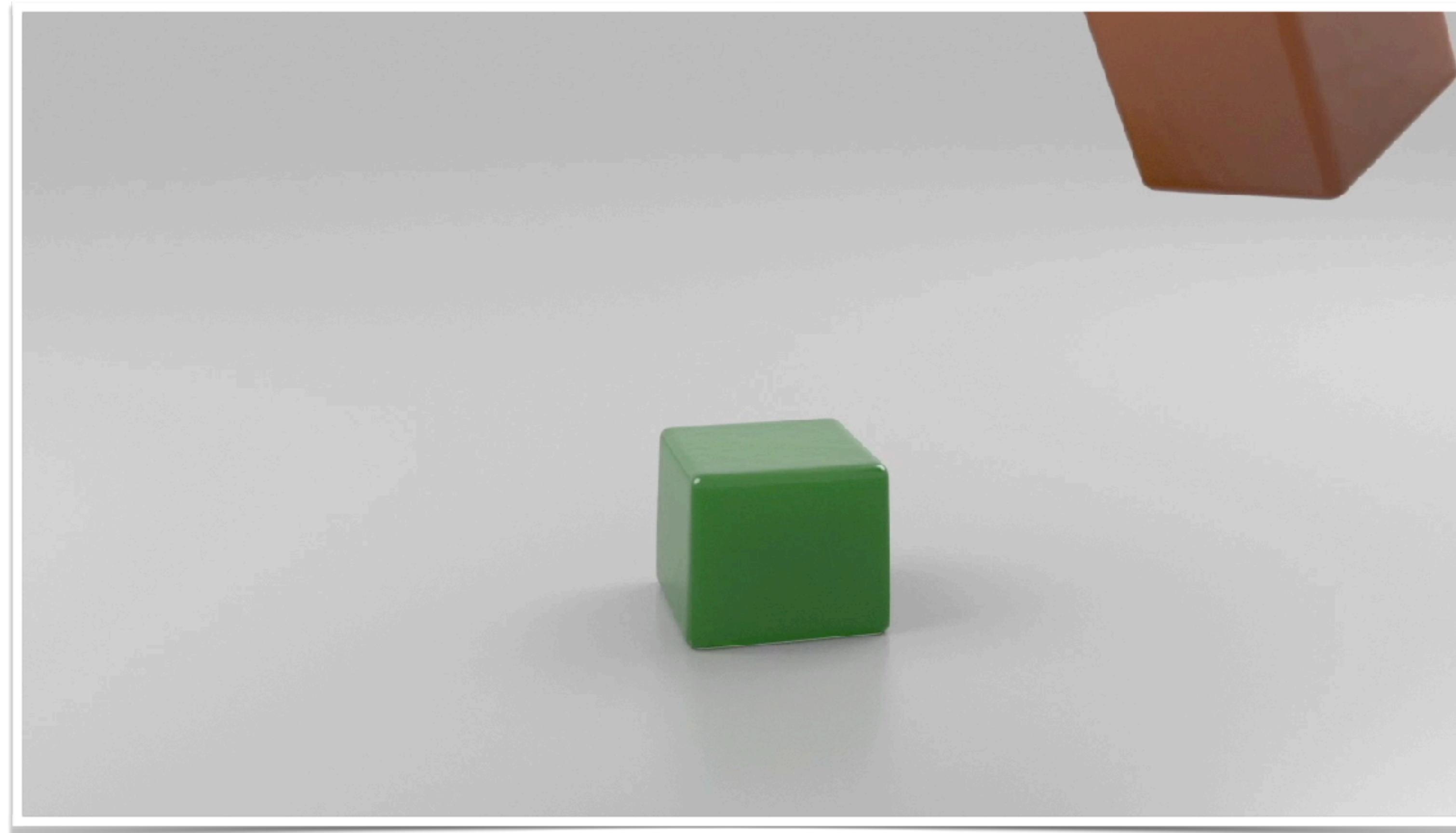
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DOI: 10.1145/3130800.3130879

ACM Transactions on Graphics, Vol. 36, No. 6, Article 223. Publication date: November 2017.

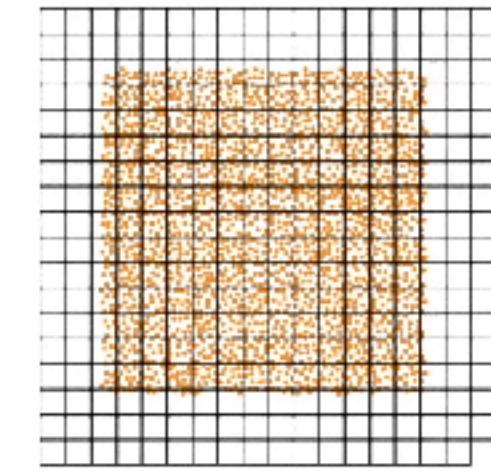
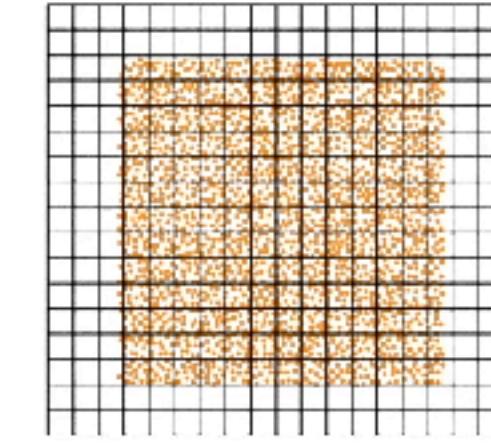
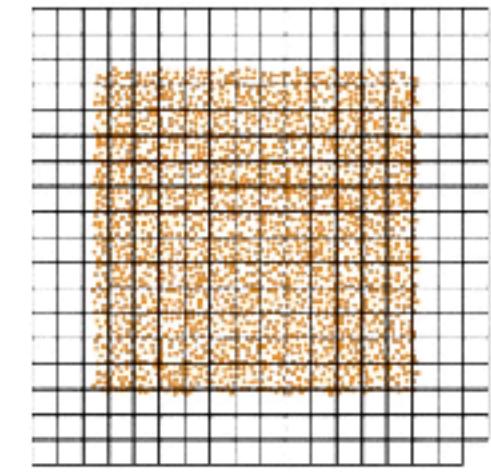
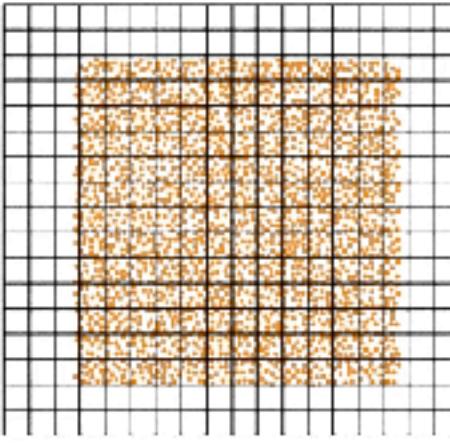
M. Gao, A. Tampubolon, C. Jiang, E. Sifakis
ACM Transactions on Graphics (Proceedings of ACM SIGGRAPH Asia), 2017



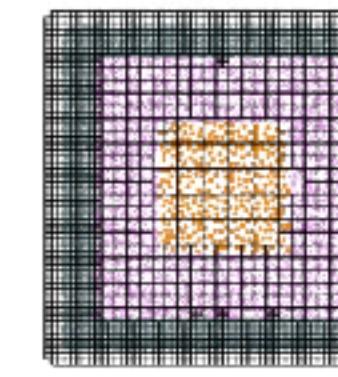
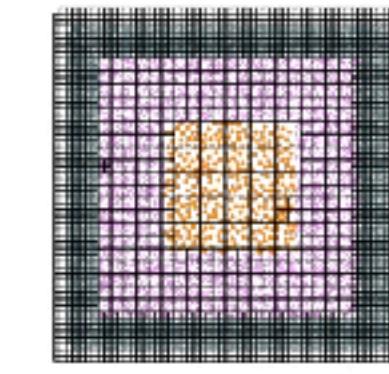
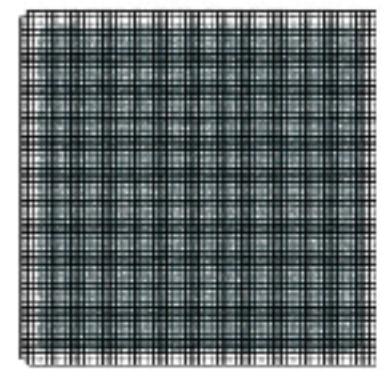
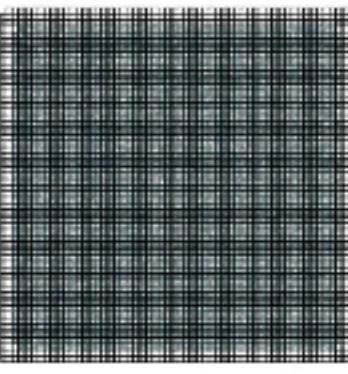
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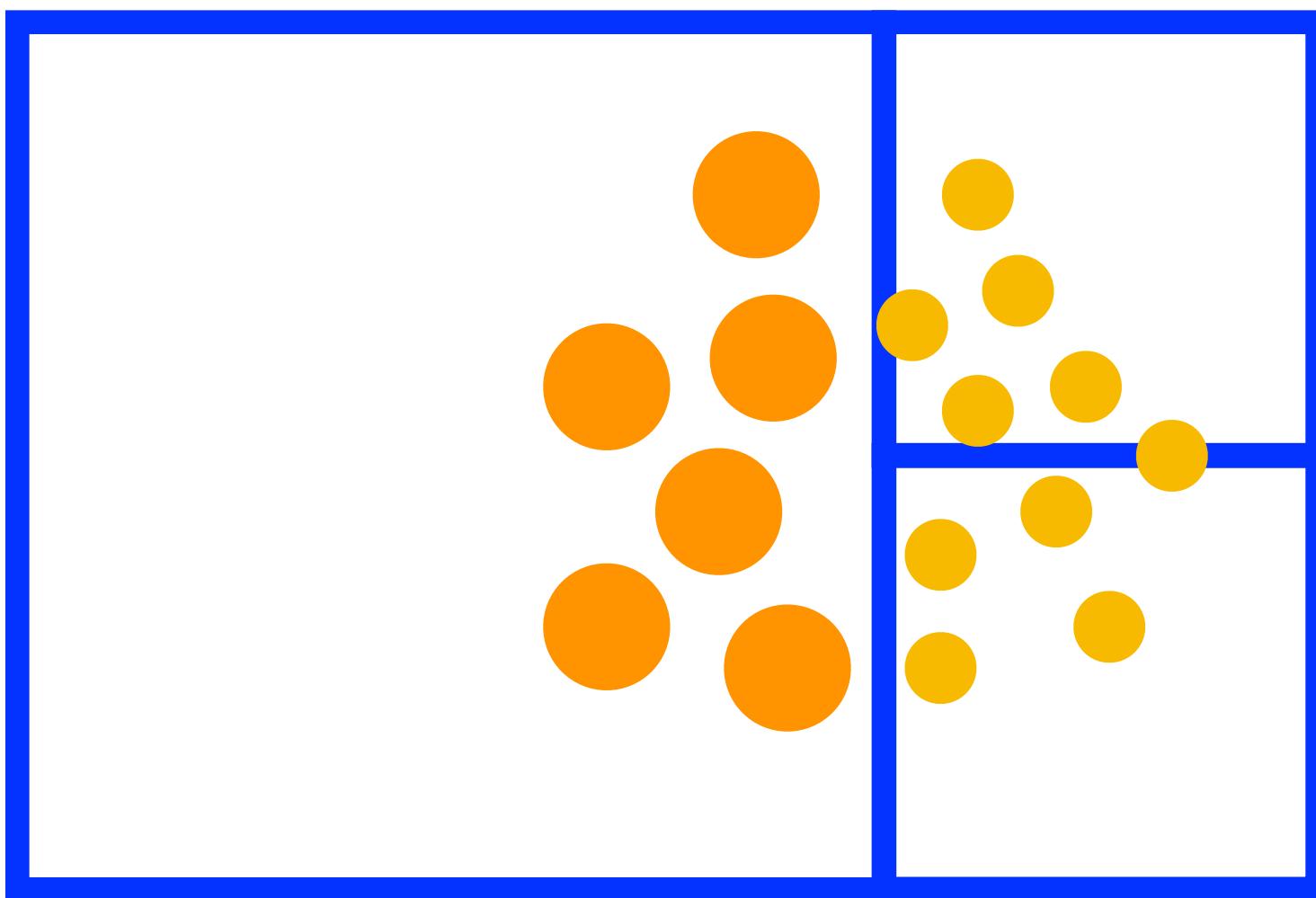
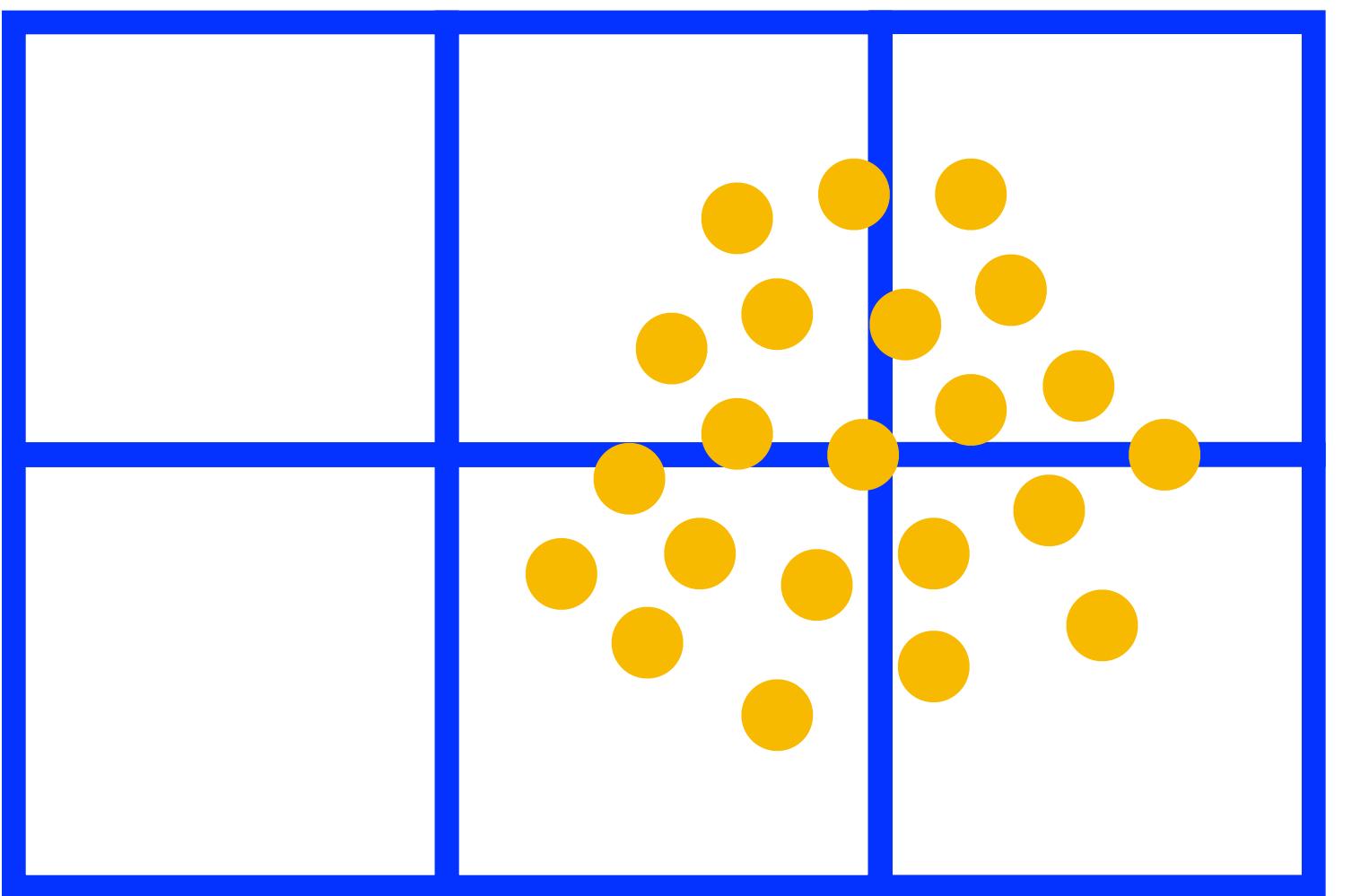
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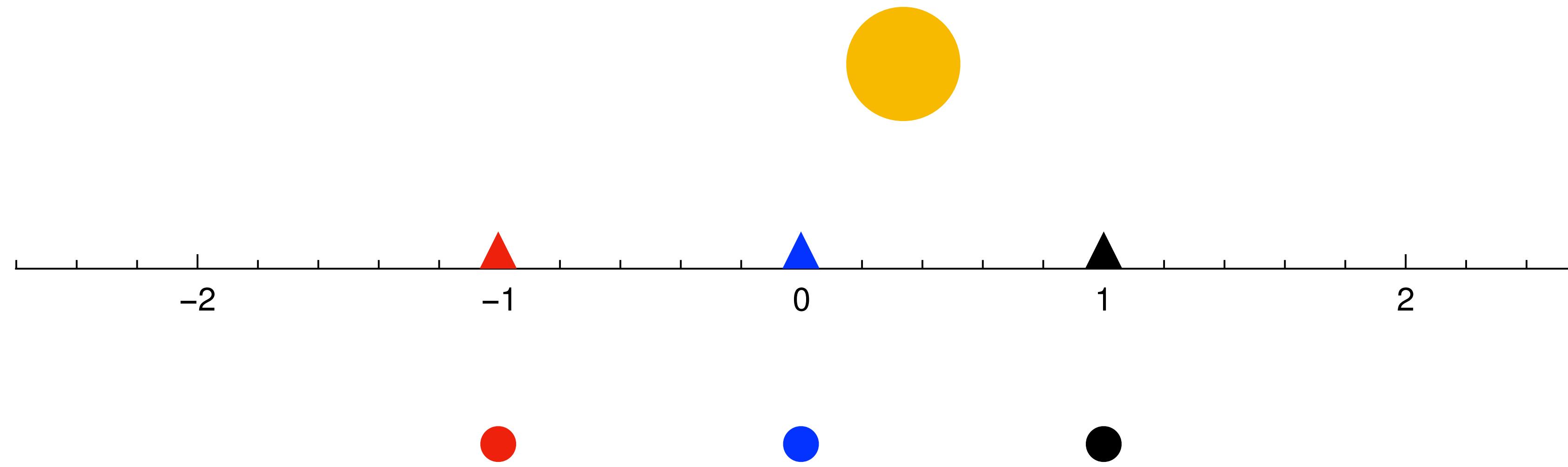
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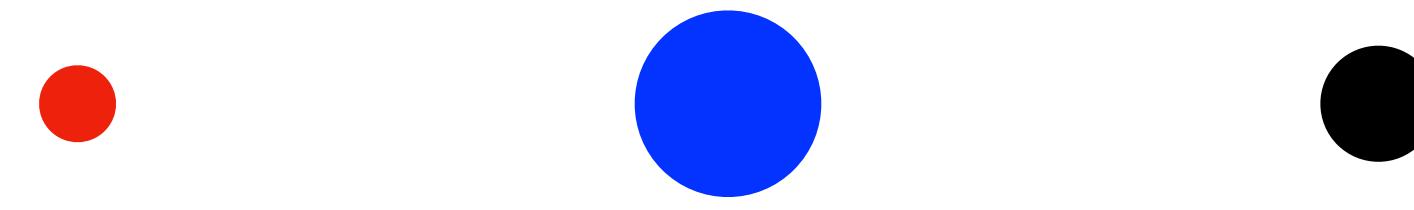
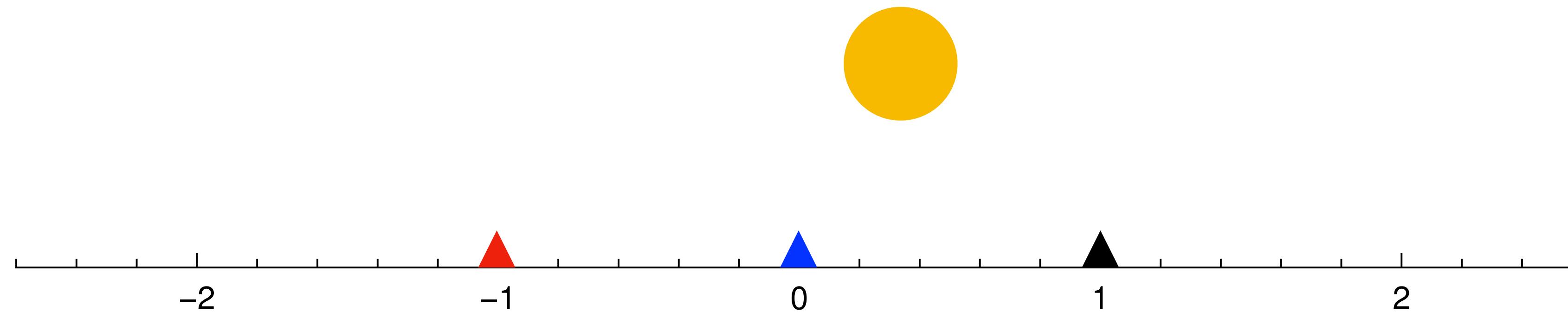
MPM adaptivity



Transfer of mass



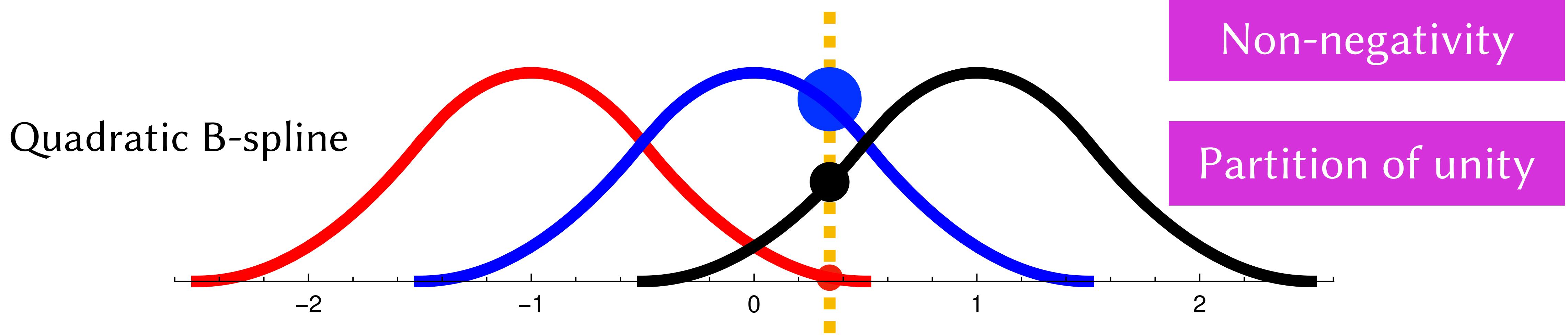
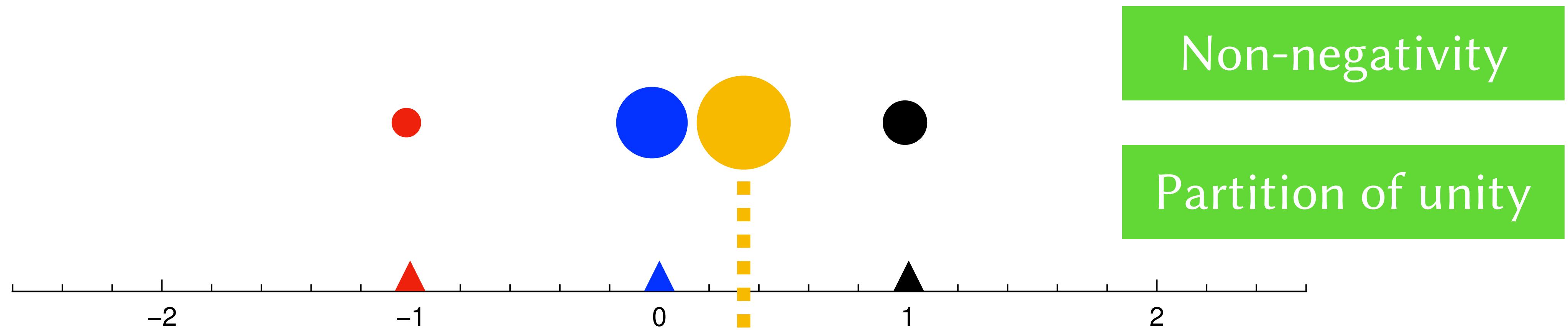
Transfer of mass



Non-negativity

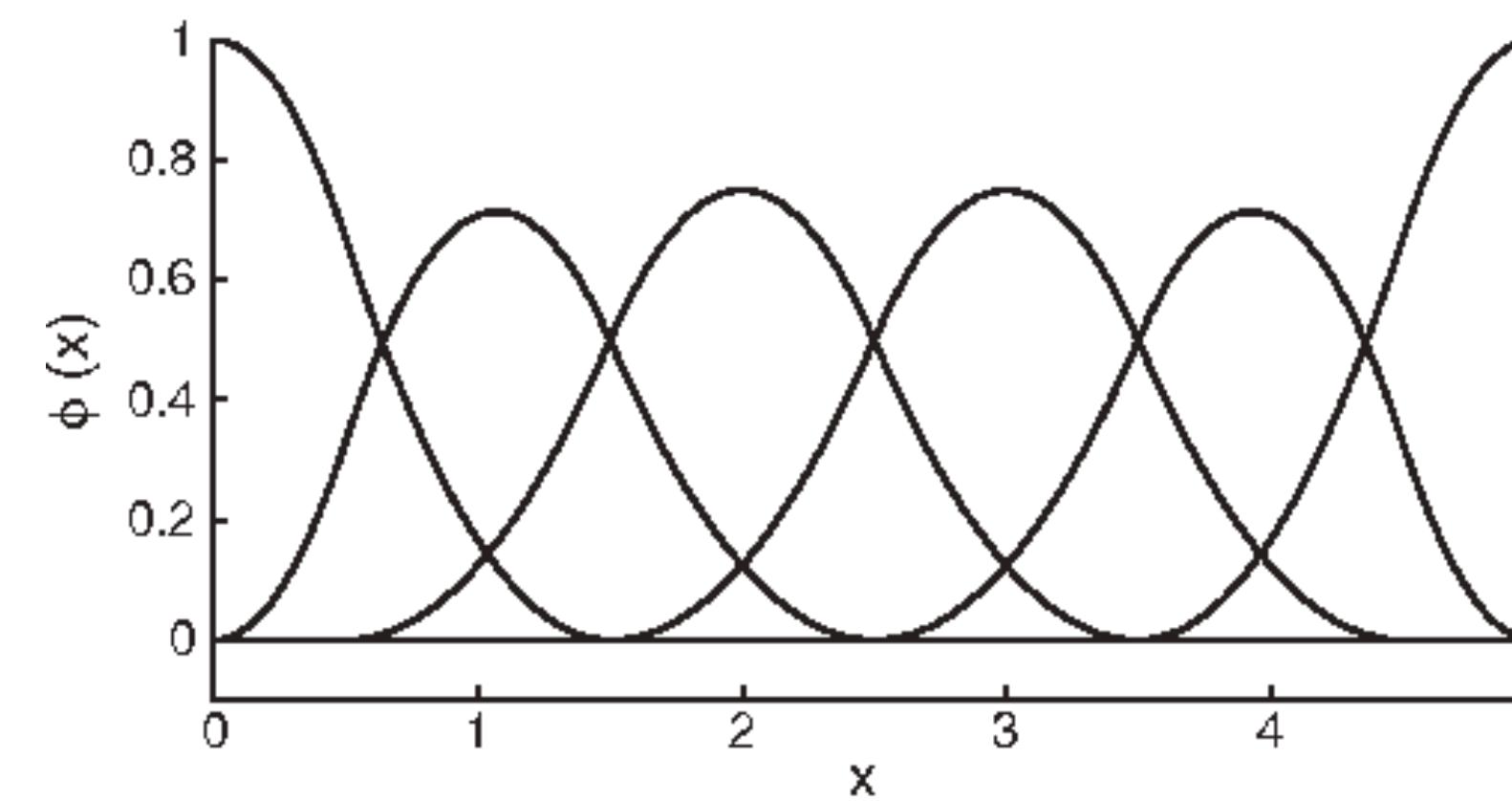
Partition of unity

Transfer of mass

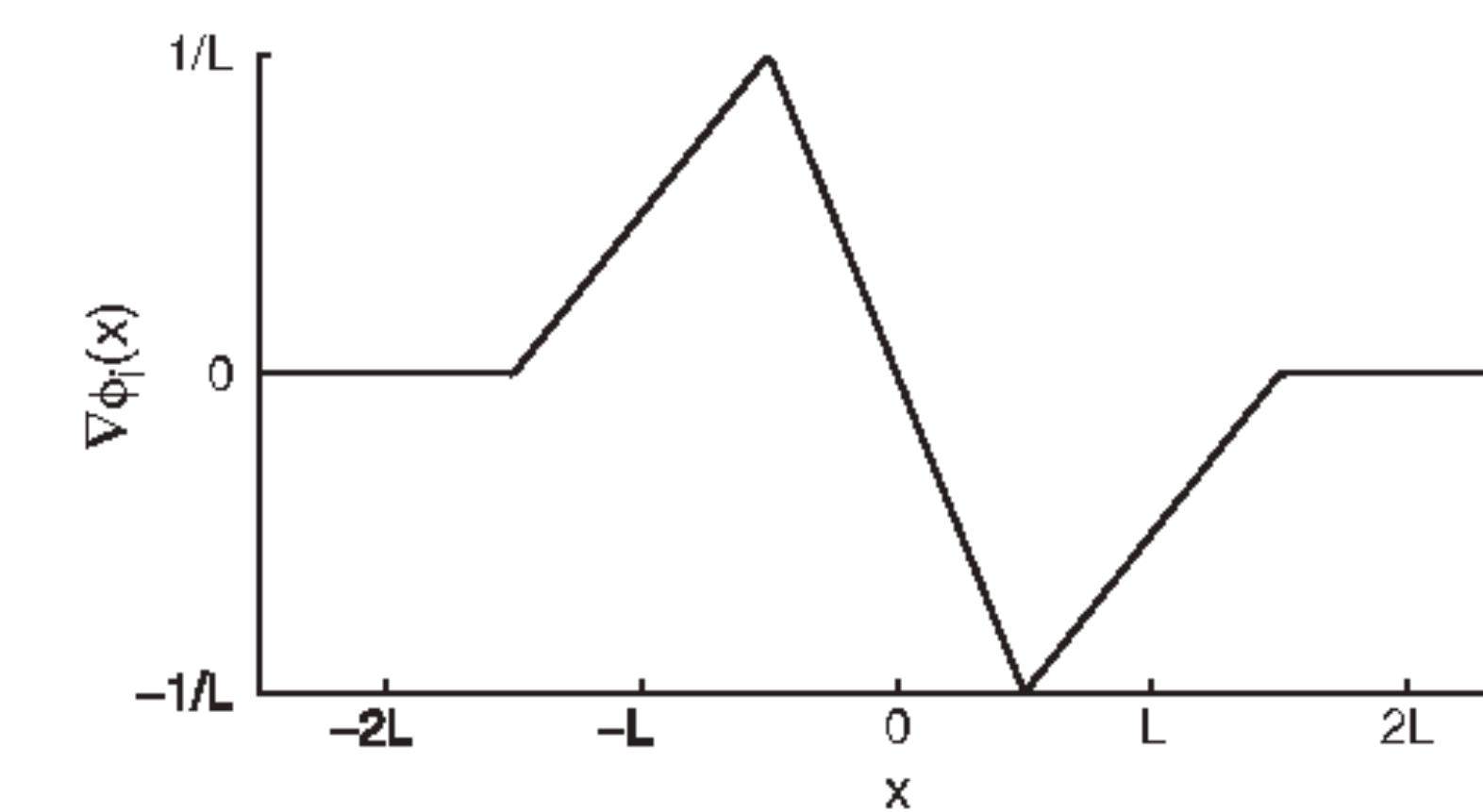


C^1 continuity

Weight / mass



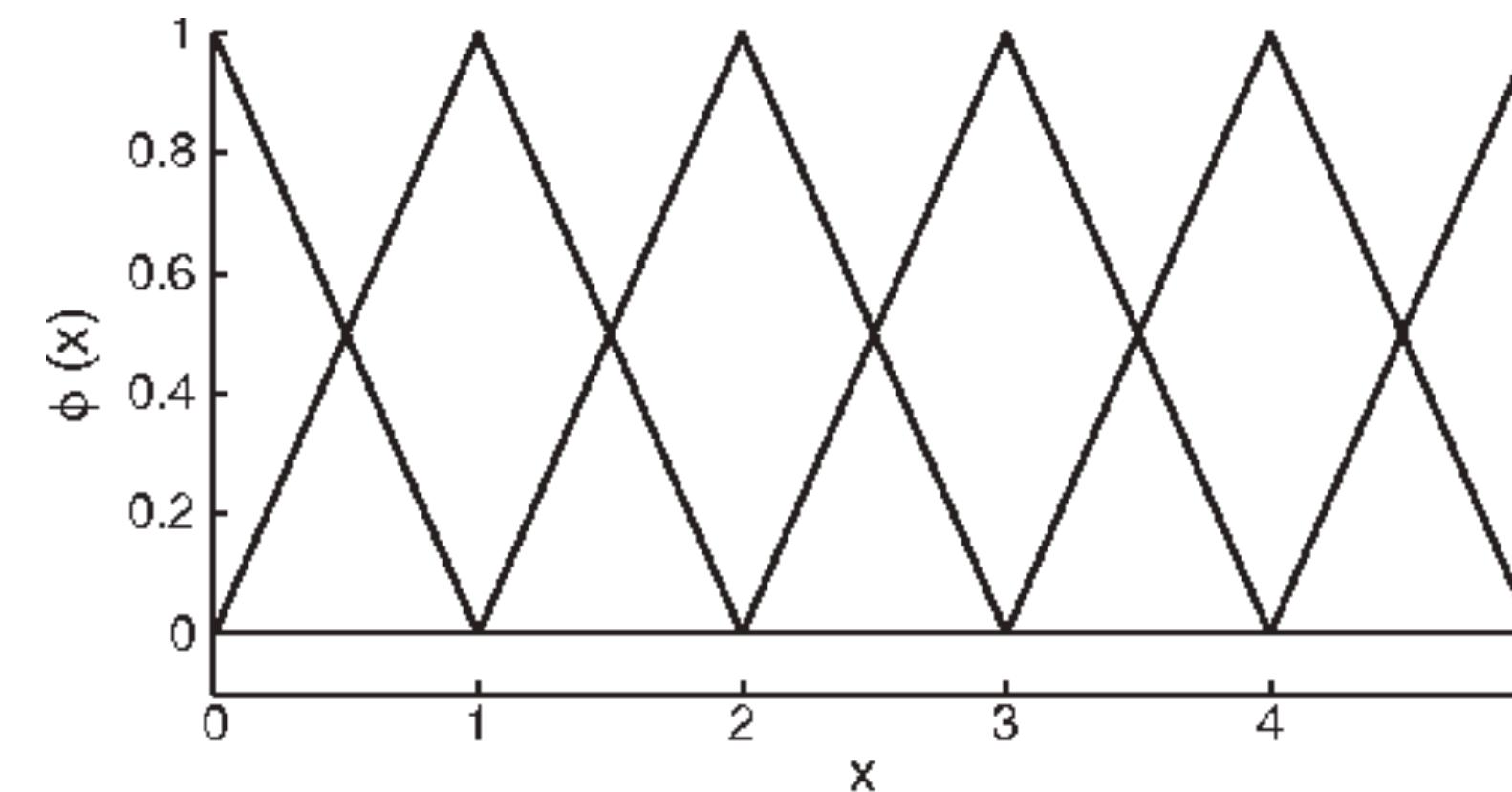
Weight gradient / force



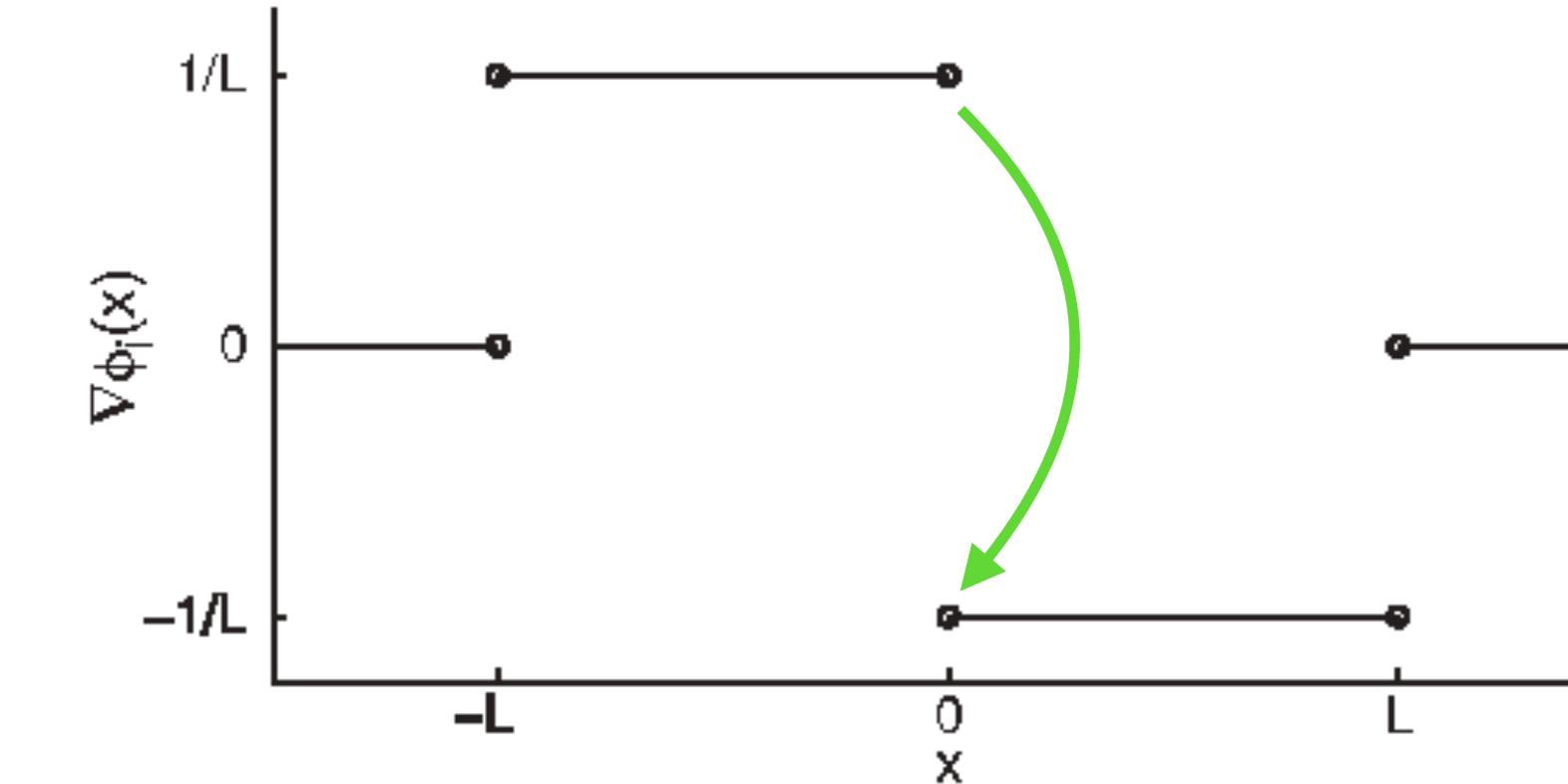
Steffen et al. 08

C^0 continuity

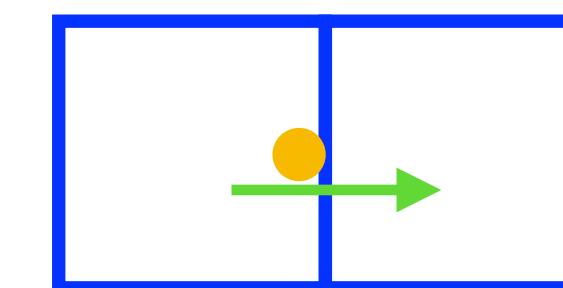
Weight / mass



Weight gradient / force

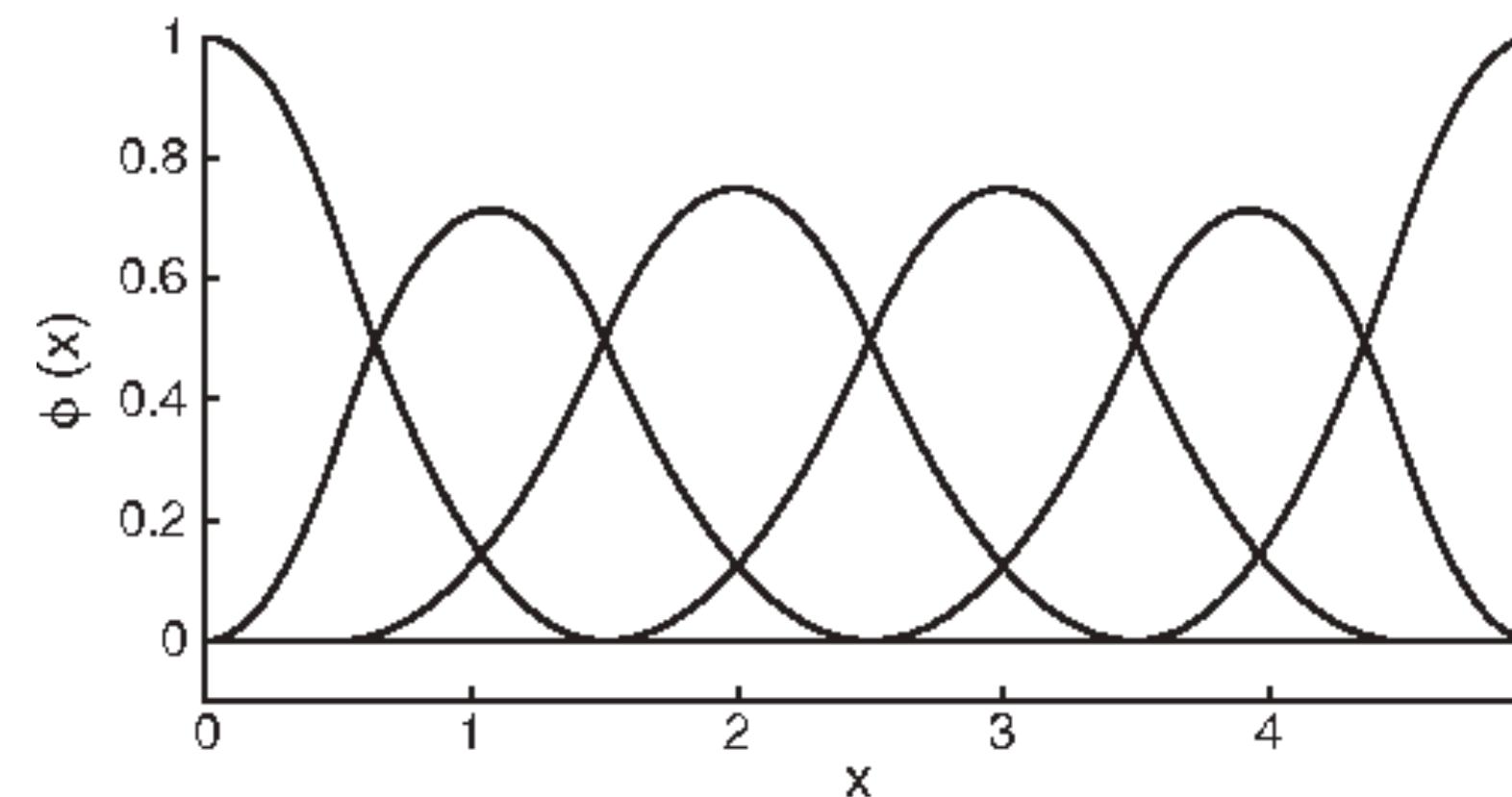


Steffen et al. 08

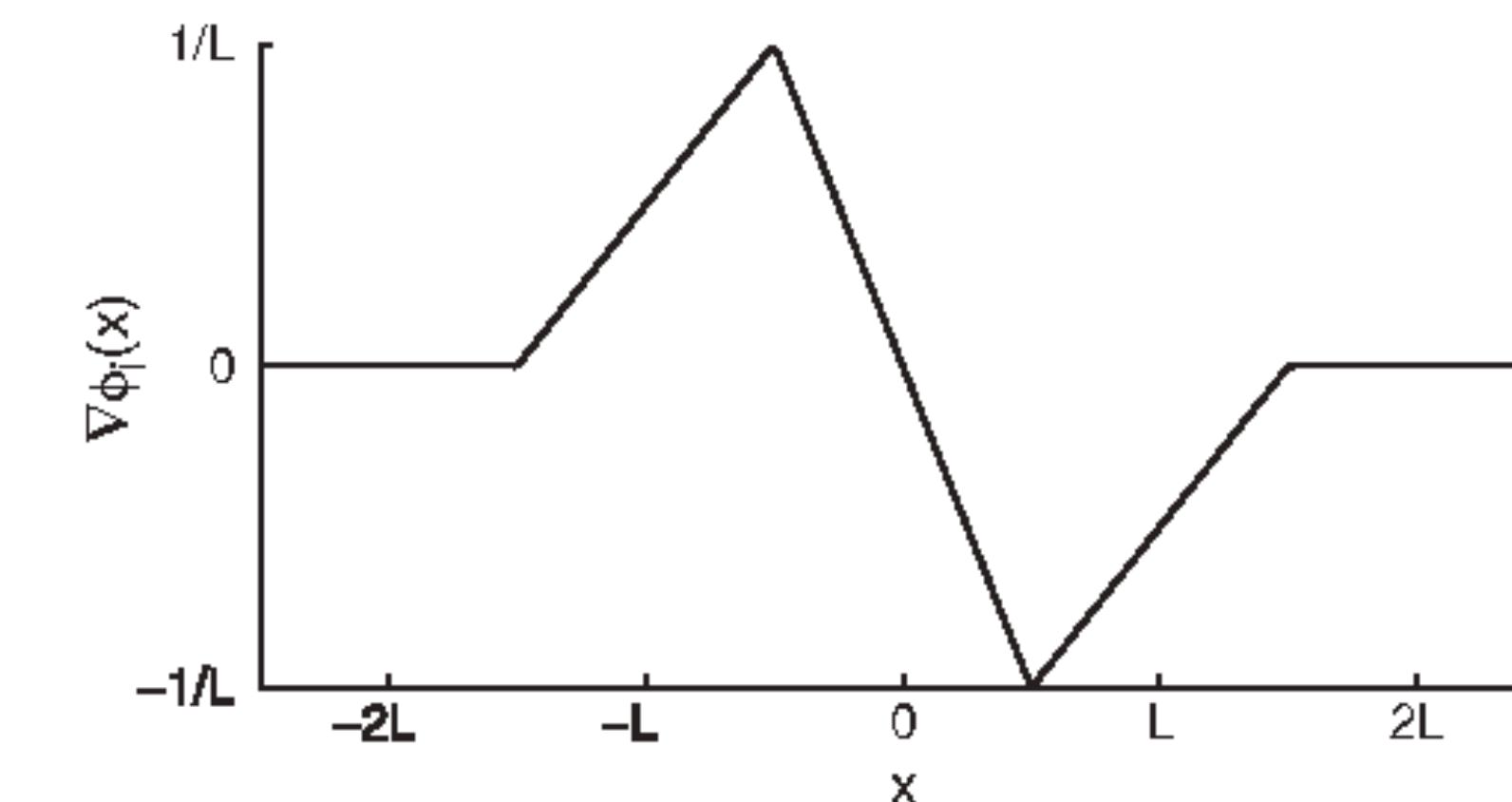


C^1 continuity in octree ?

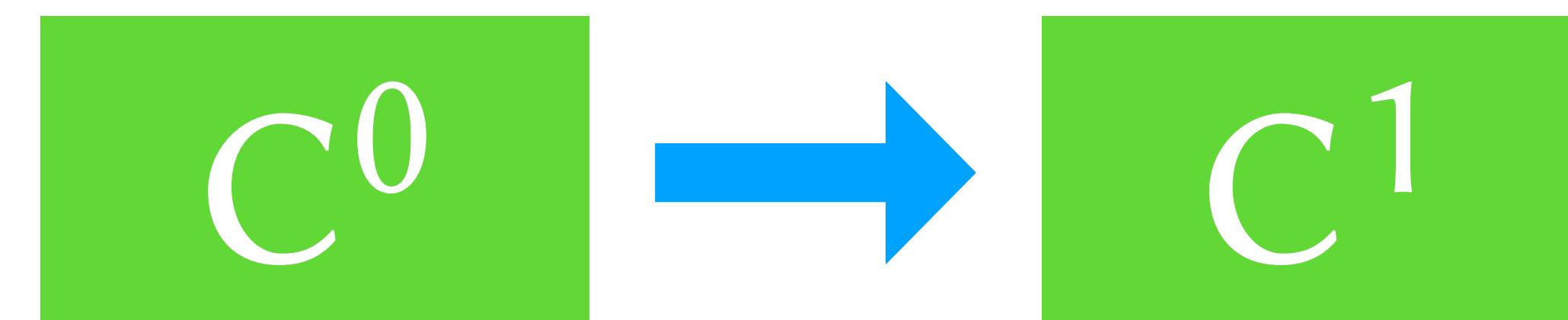
Weight / mass



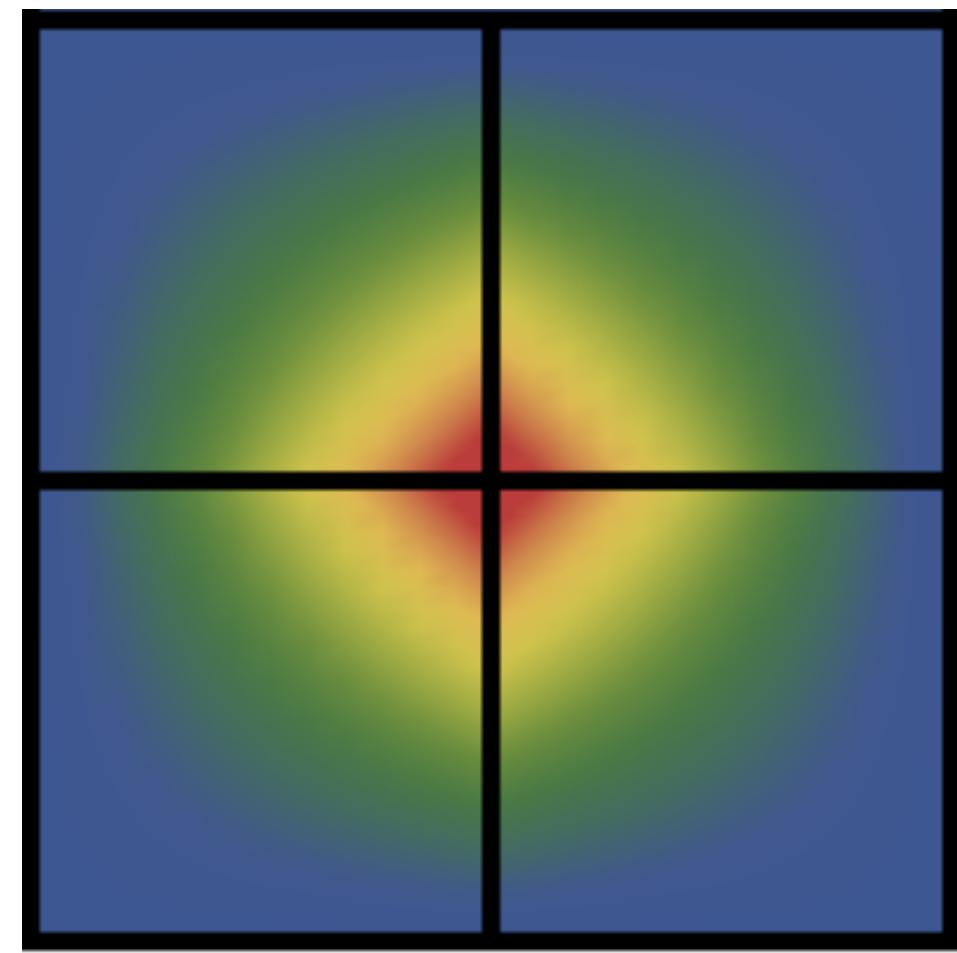
Weight gradient / force



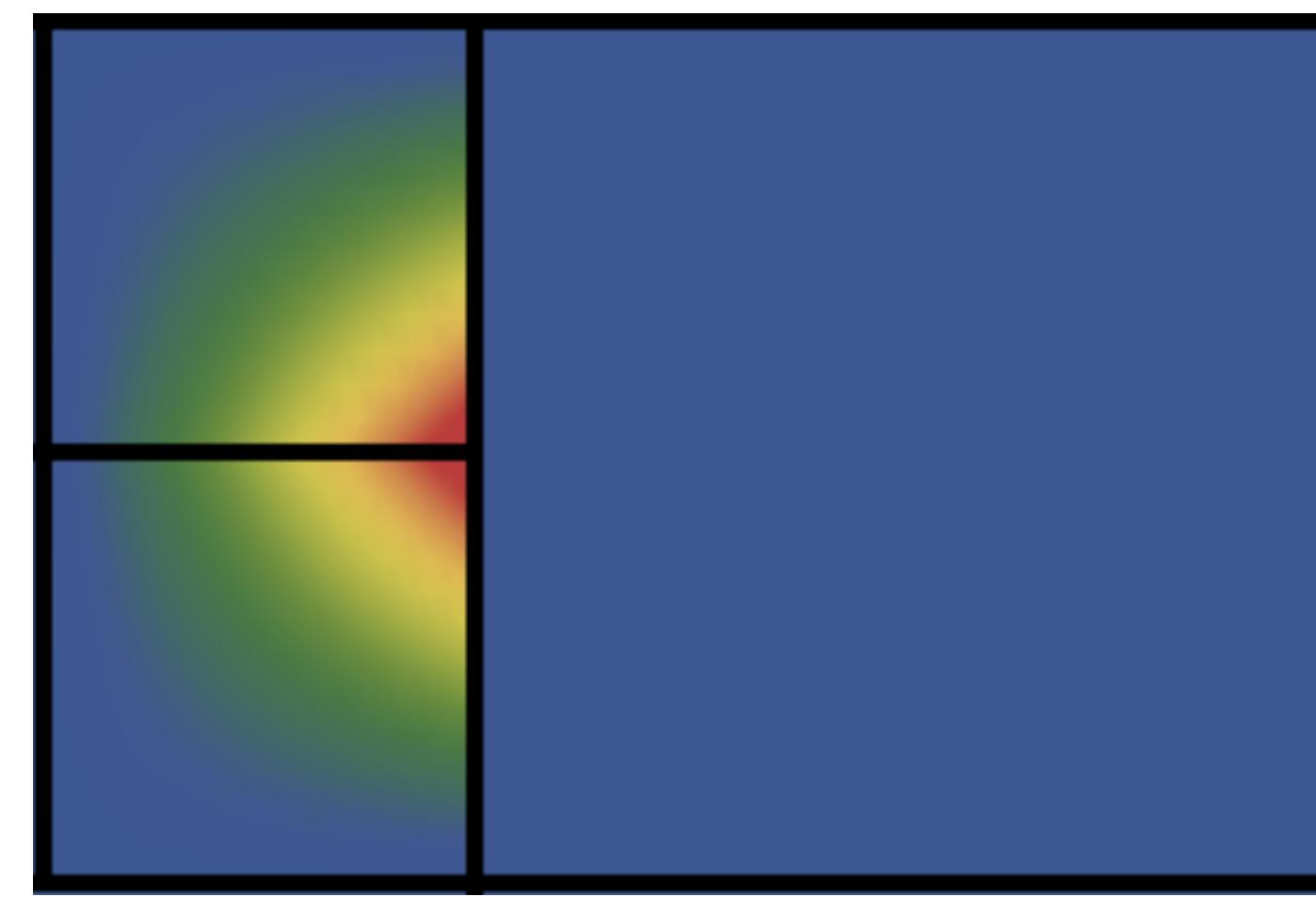
Steffen et al. 08



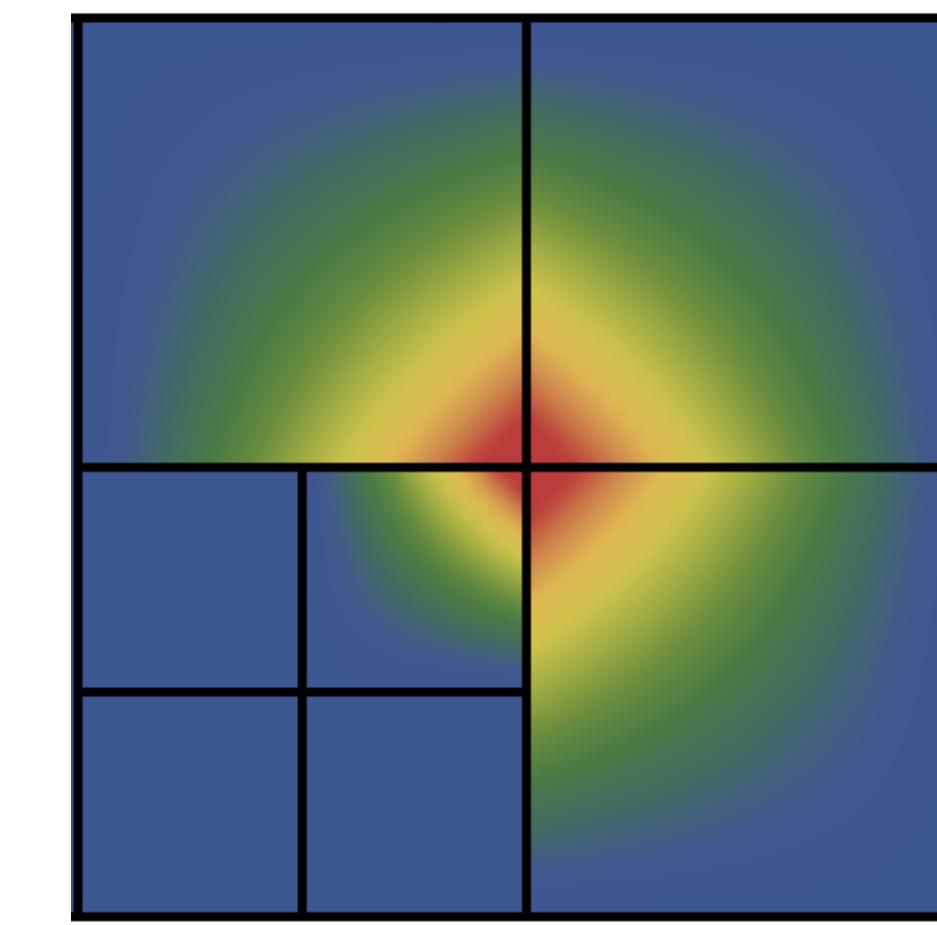
C^0 from uniform to quadtree



Uniform

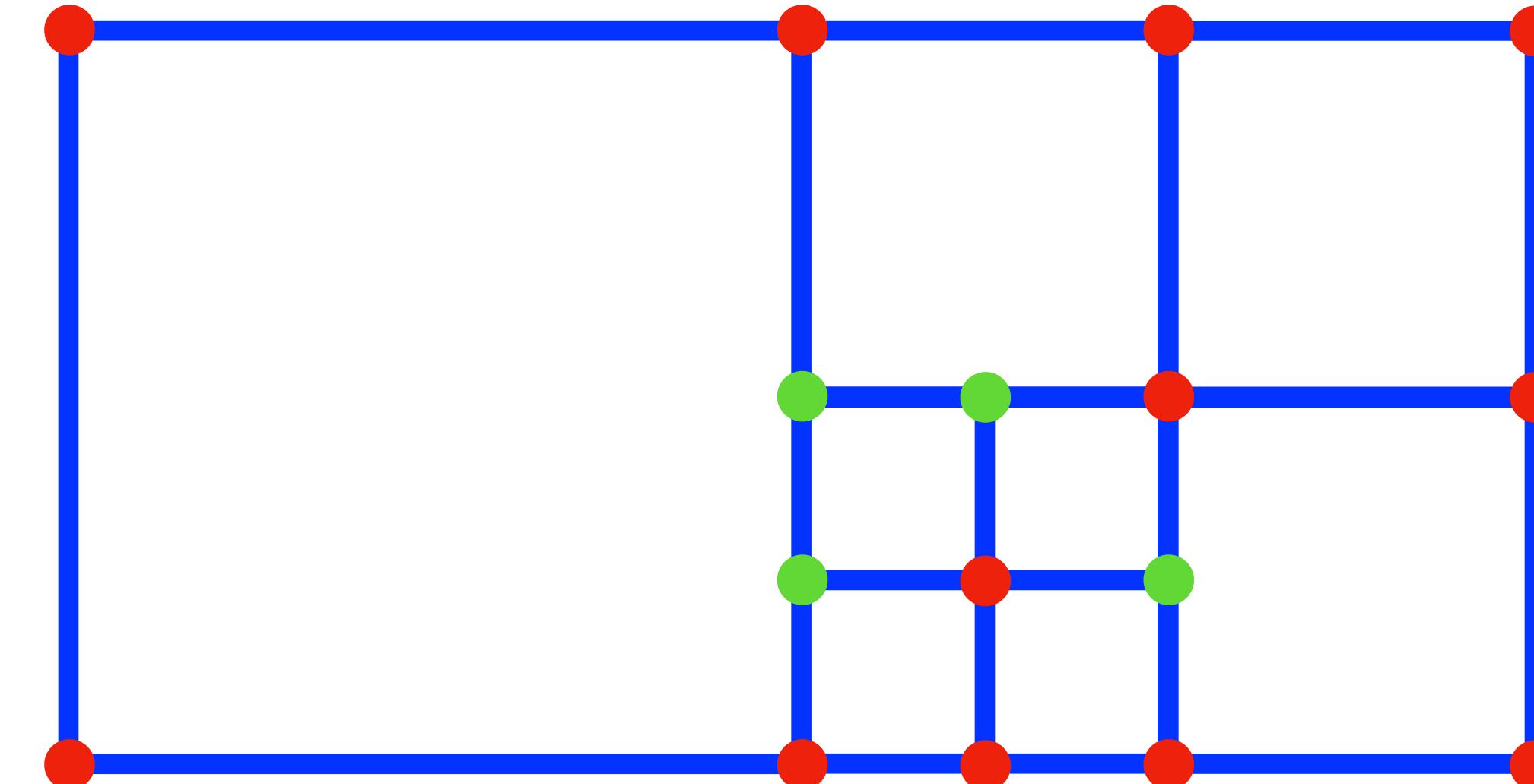


Quadtree



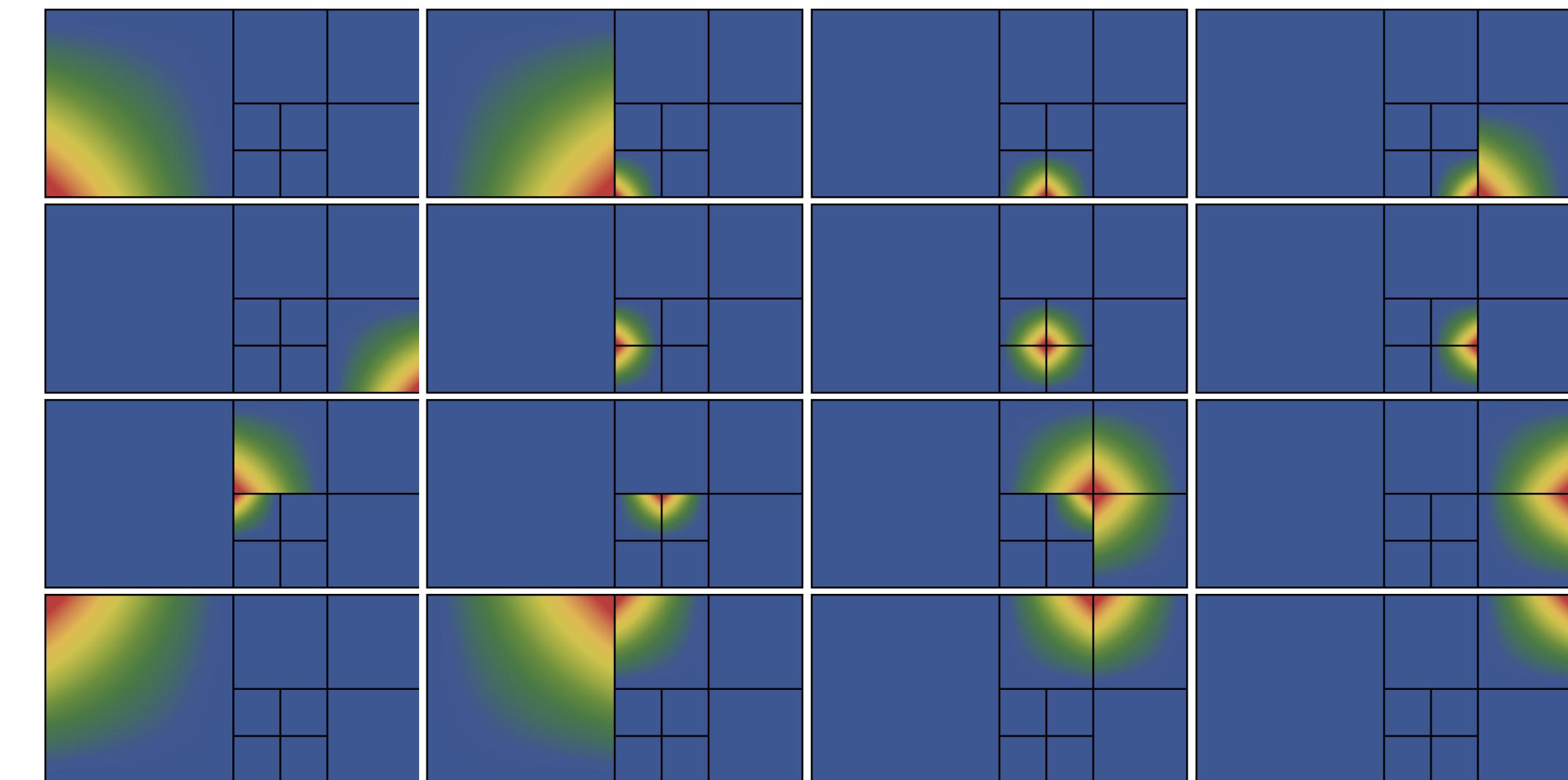
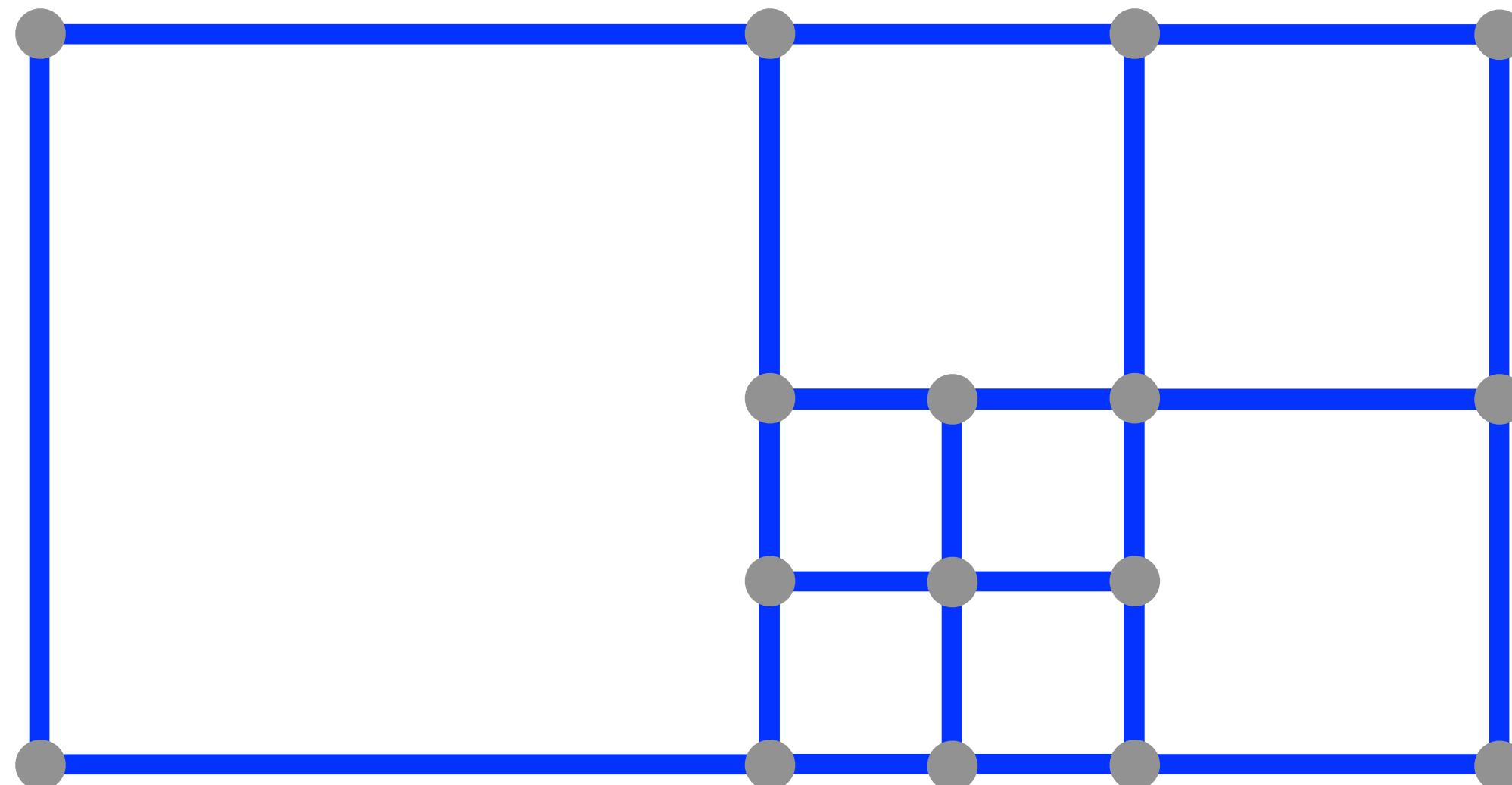
Embedding T-junctions

- DOF node
- Embedded node / T-junction node



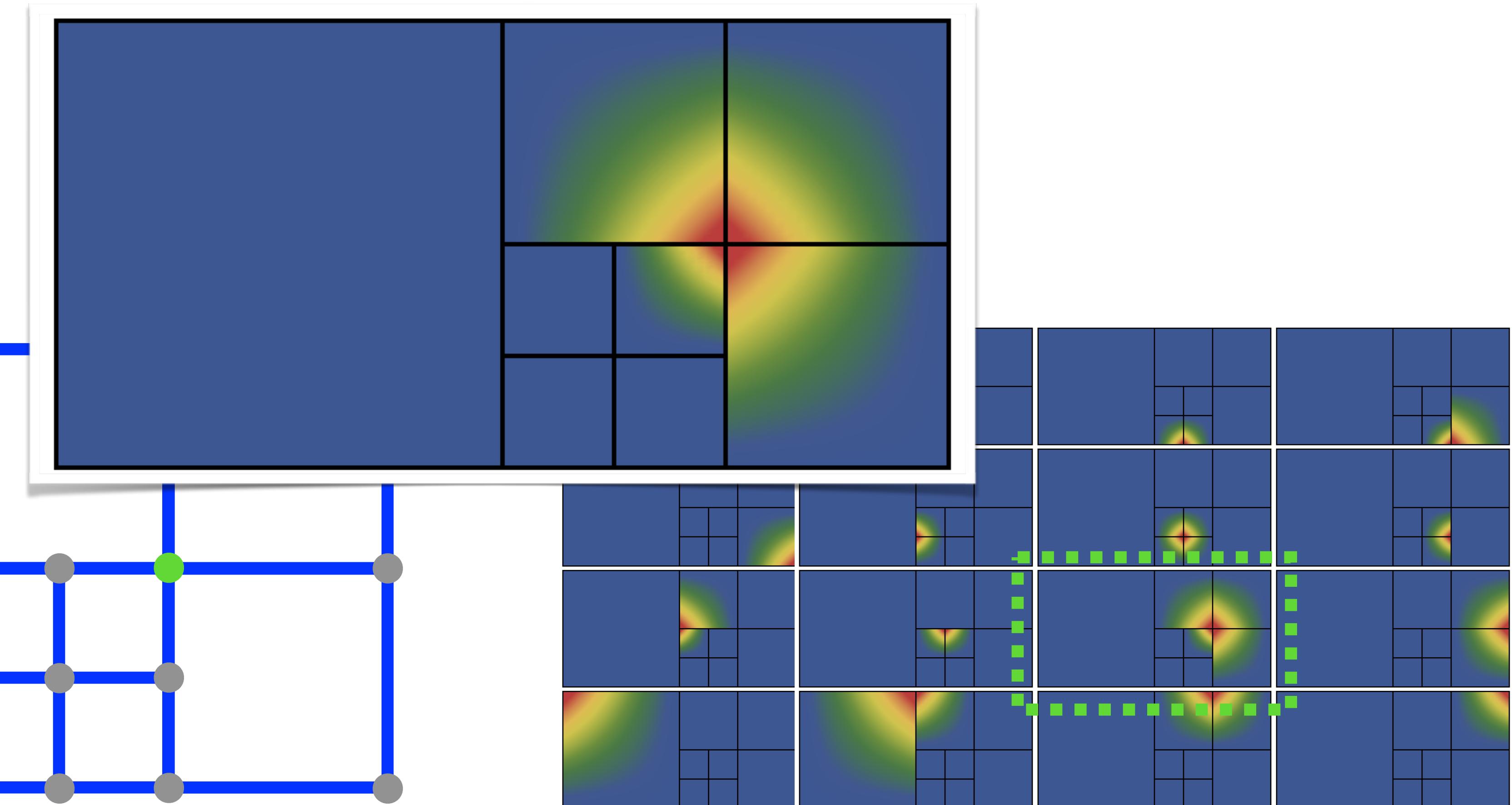
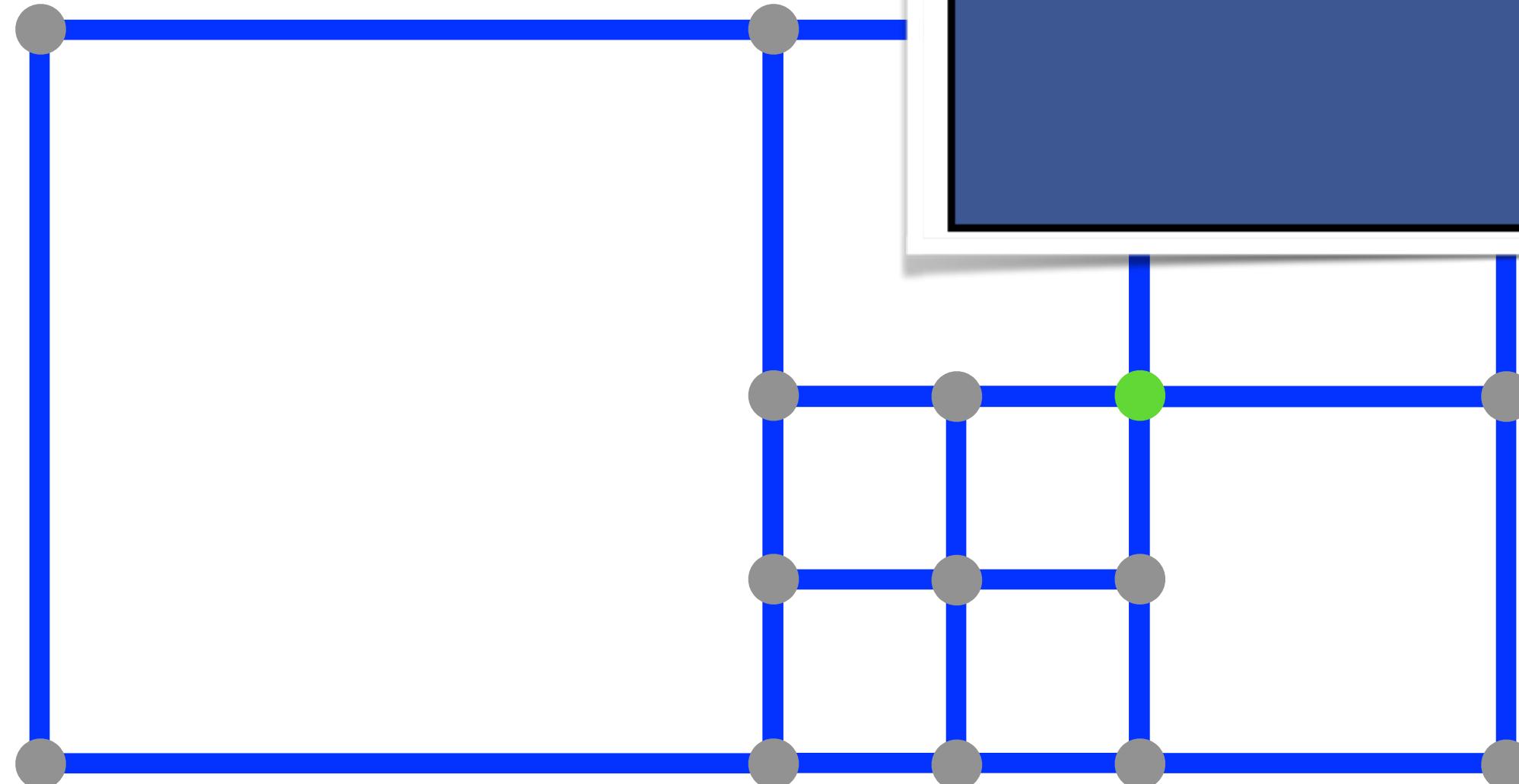
Step1 - set all nodes free

- Free node



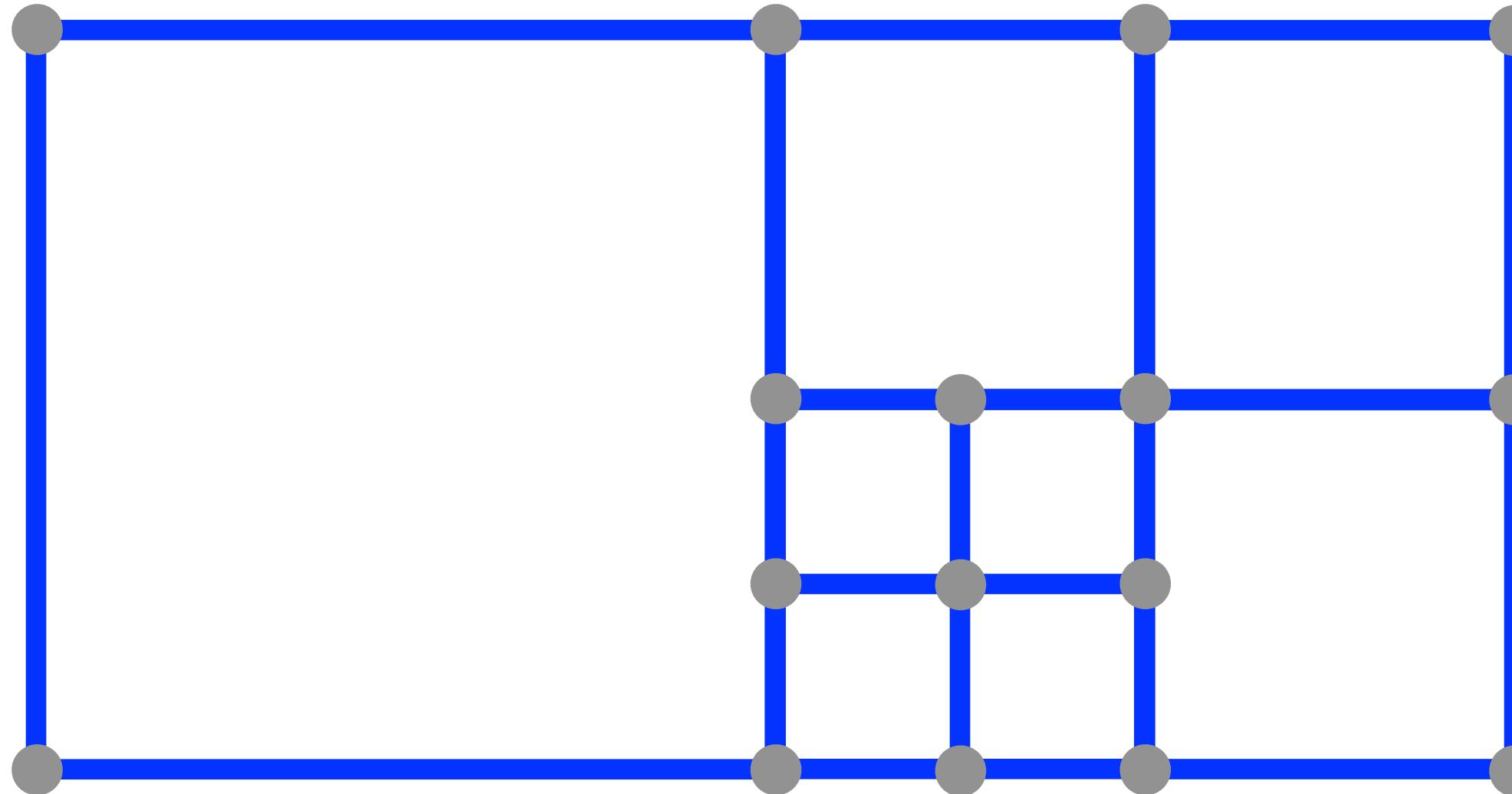
Step1 - set all nodes free

- Free node



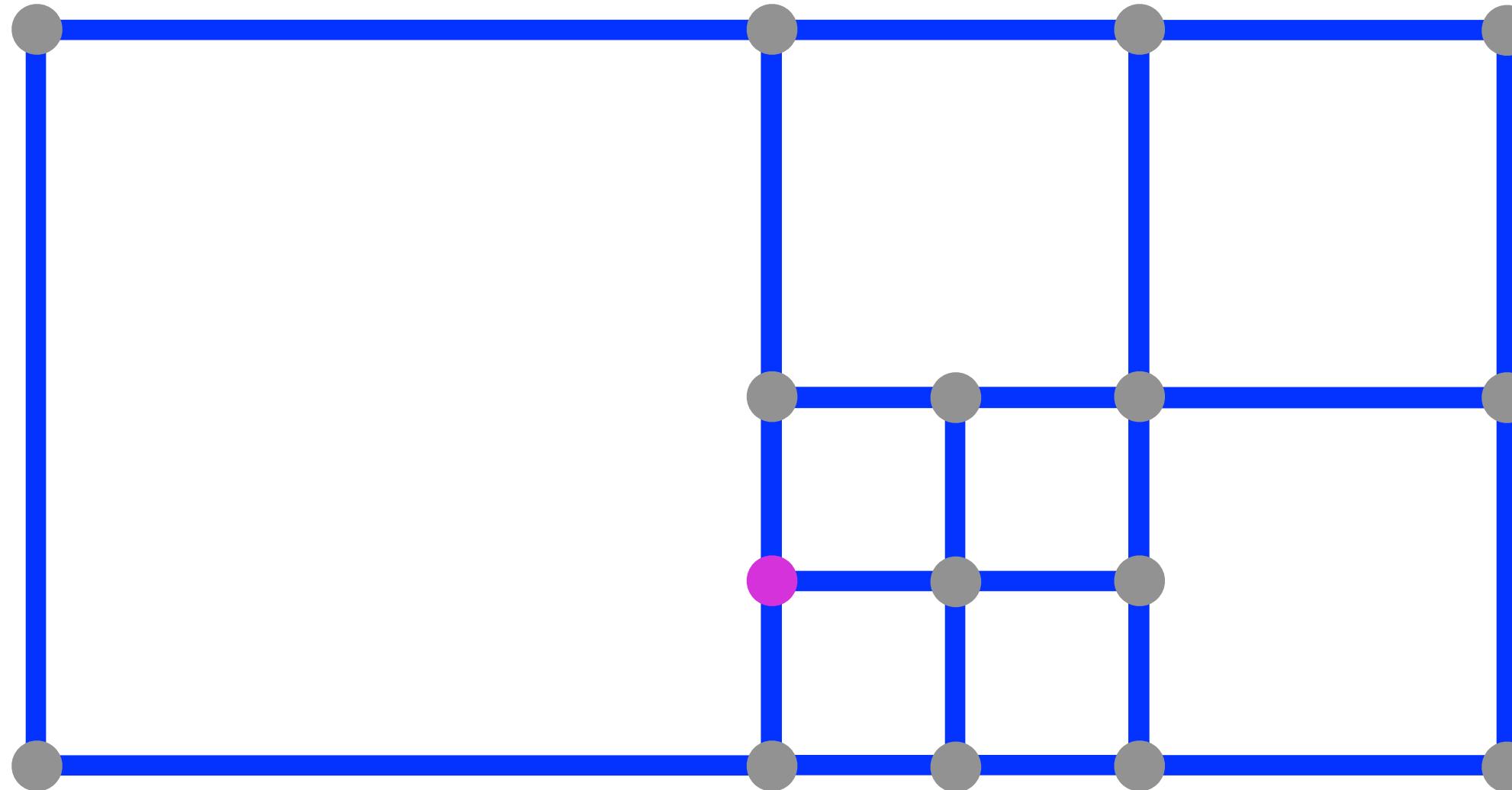
Step 2 - constrain T-junctions

- Free node



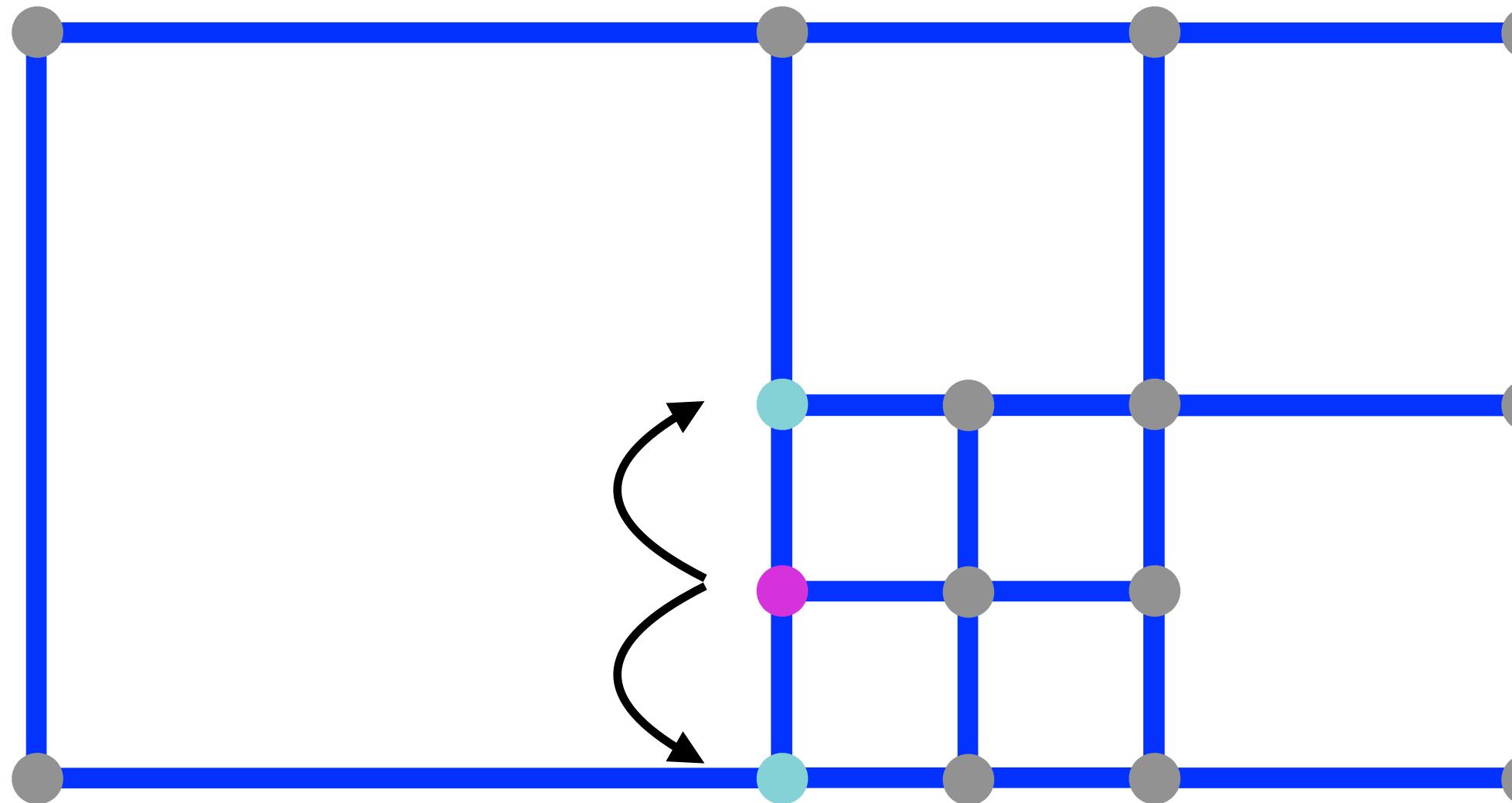
Step 2 - constrain T-junctions

- Free node
- T-junction node



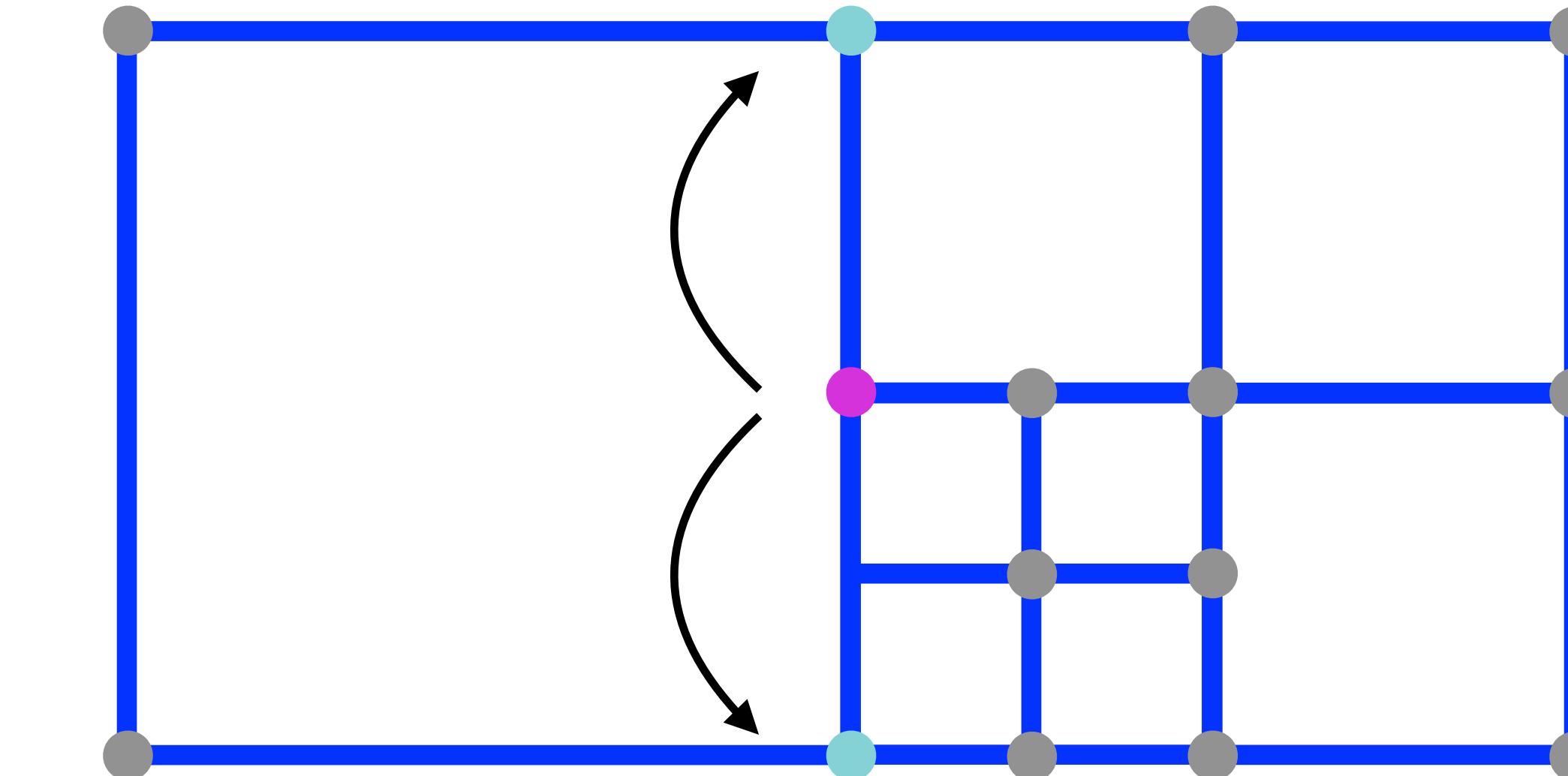
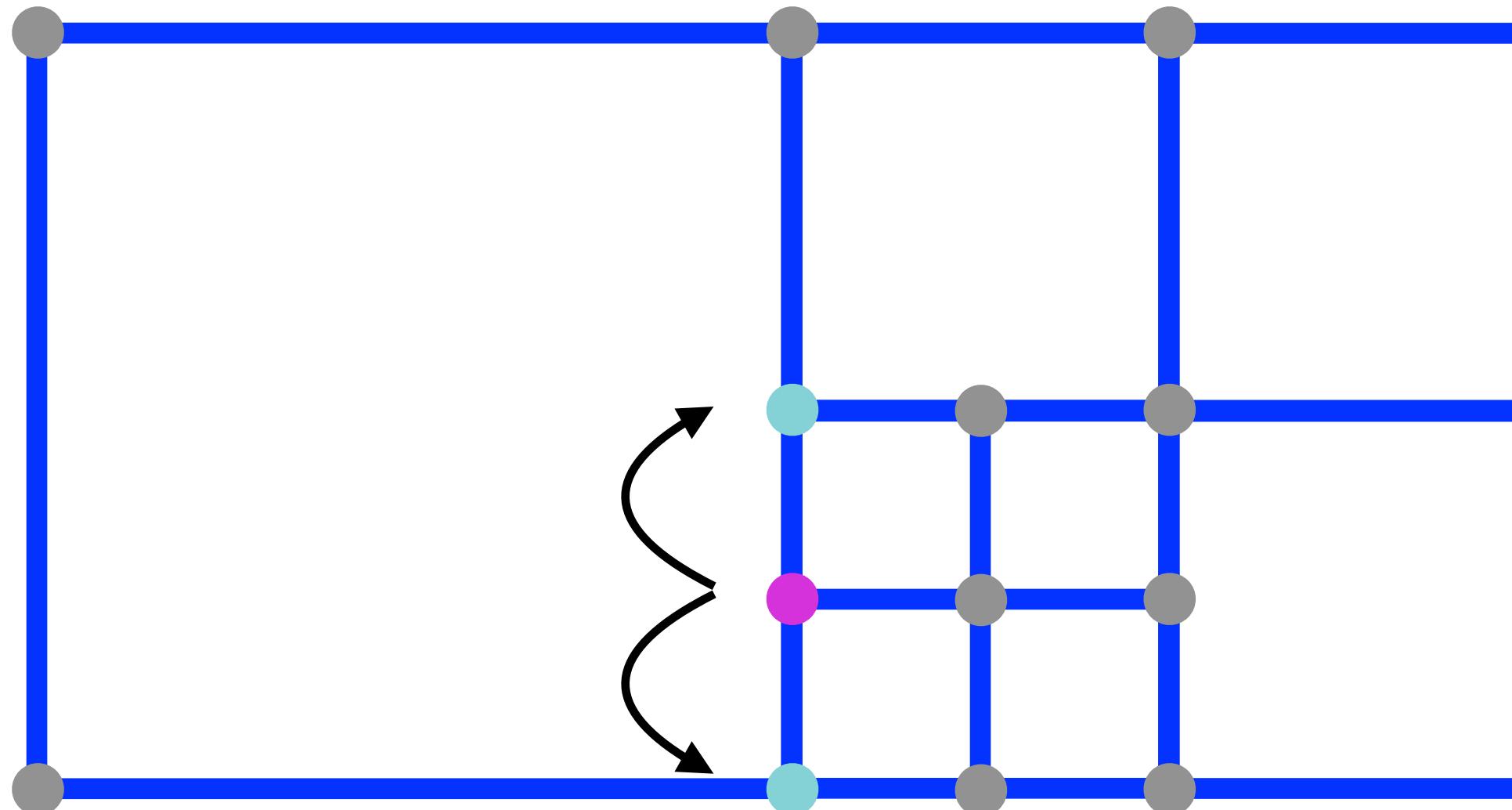
Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



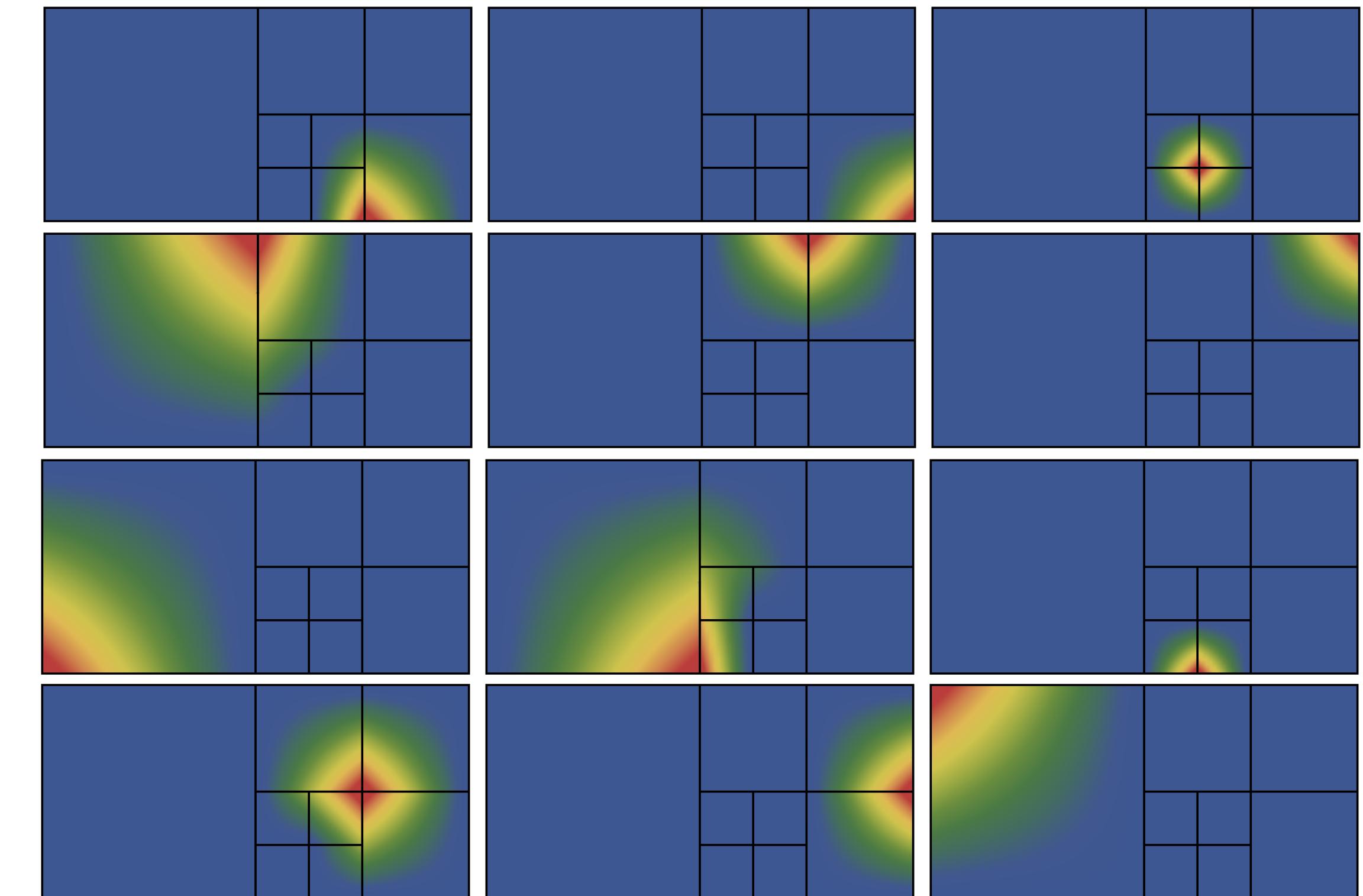
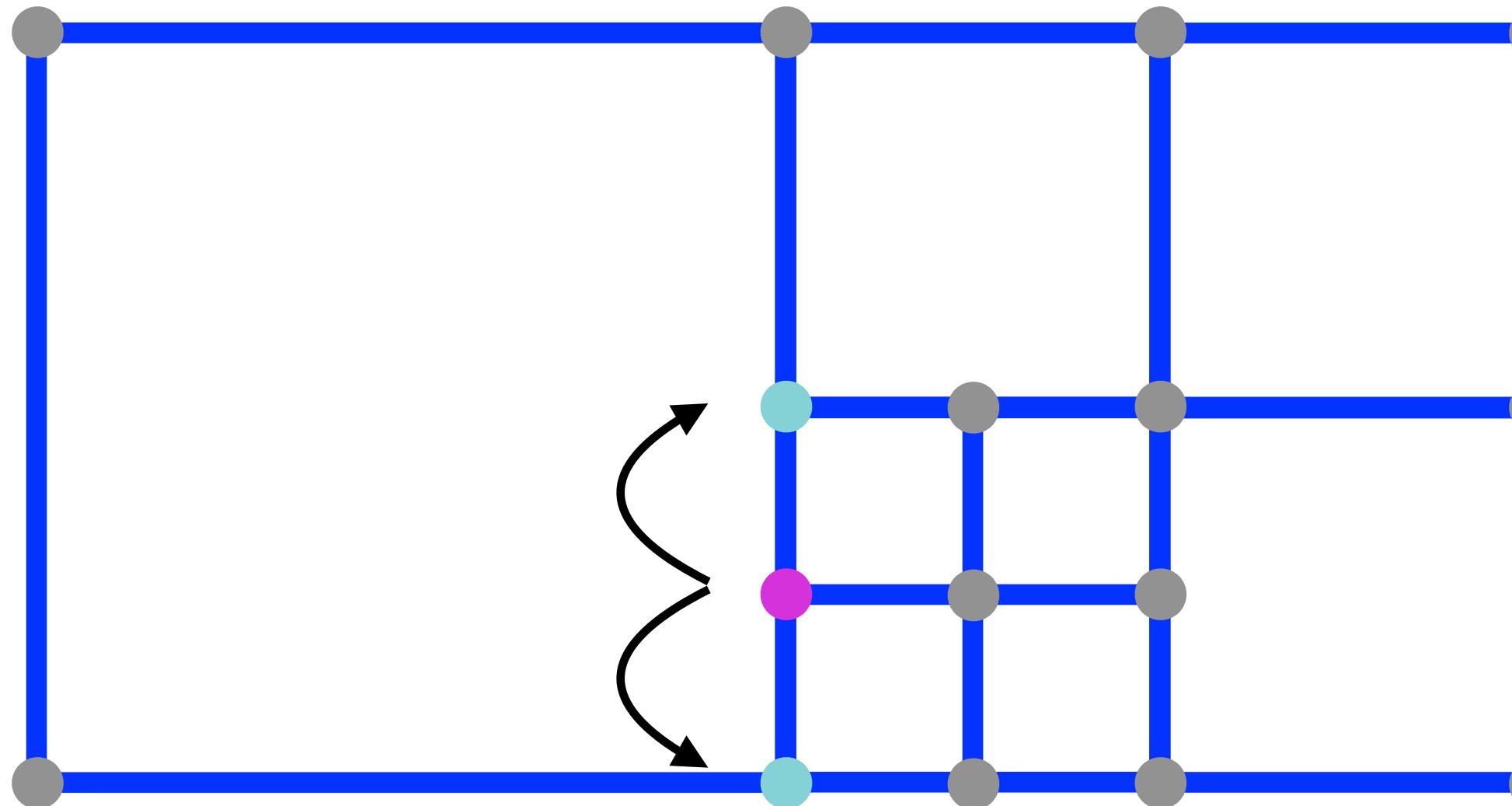
Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



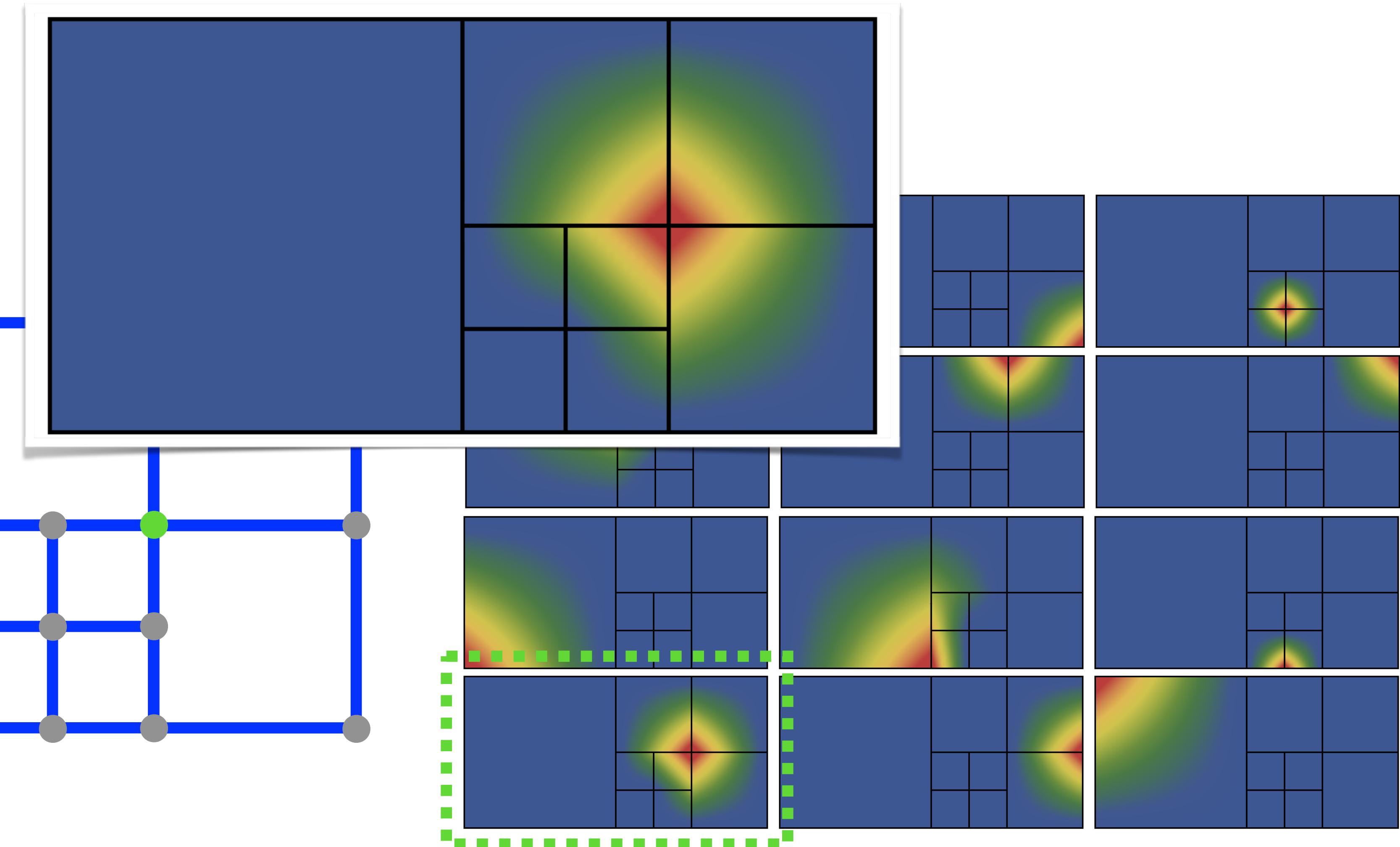
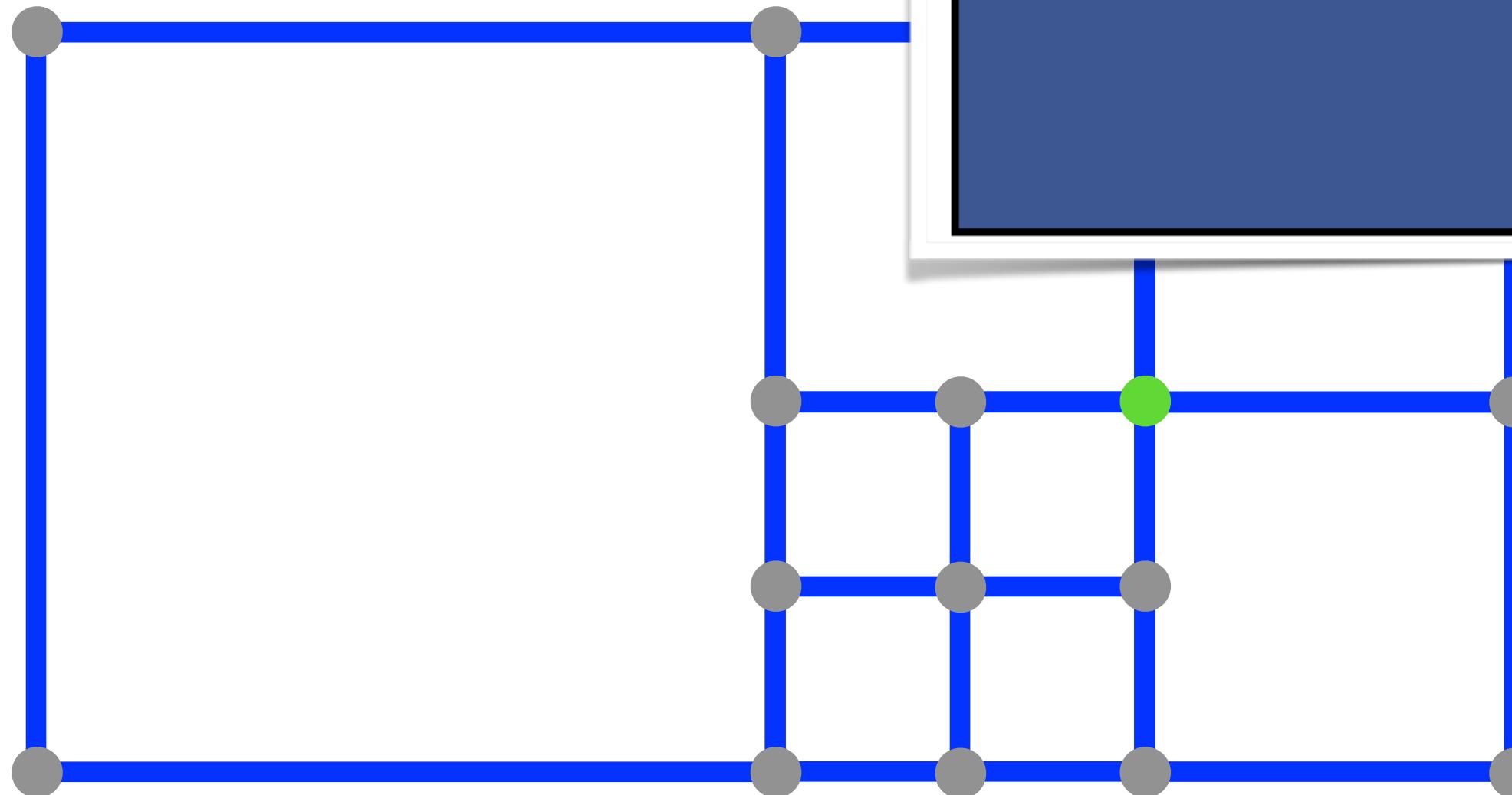
Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node

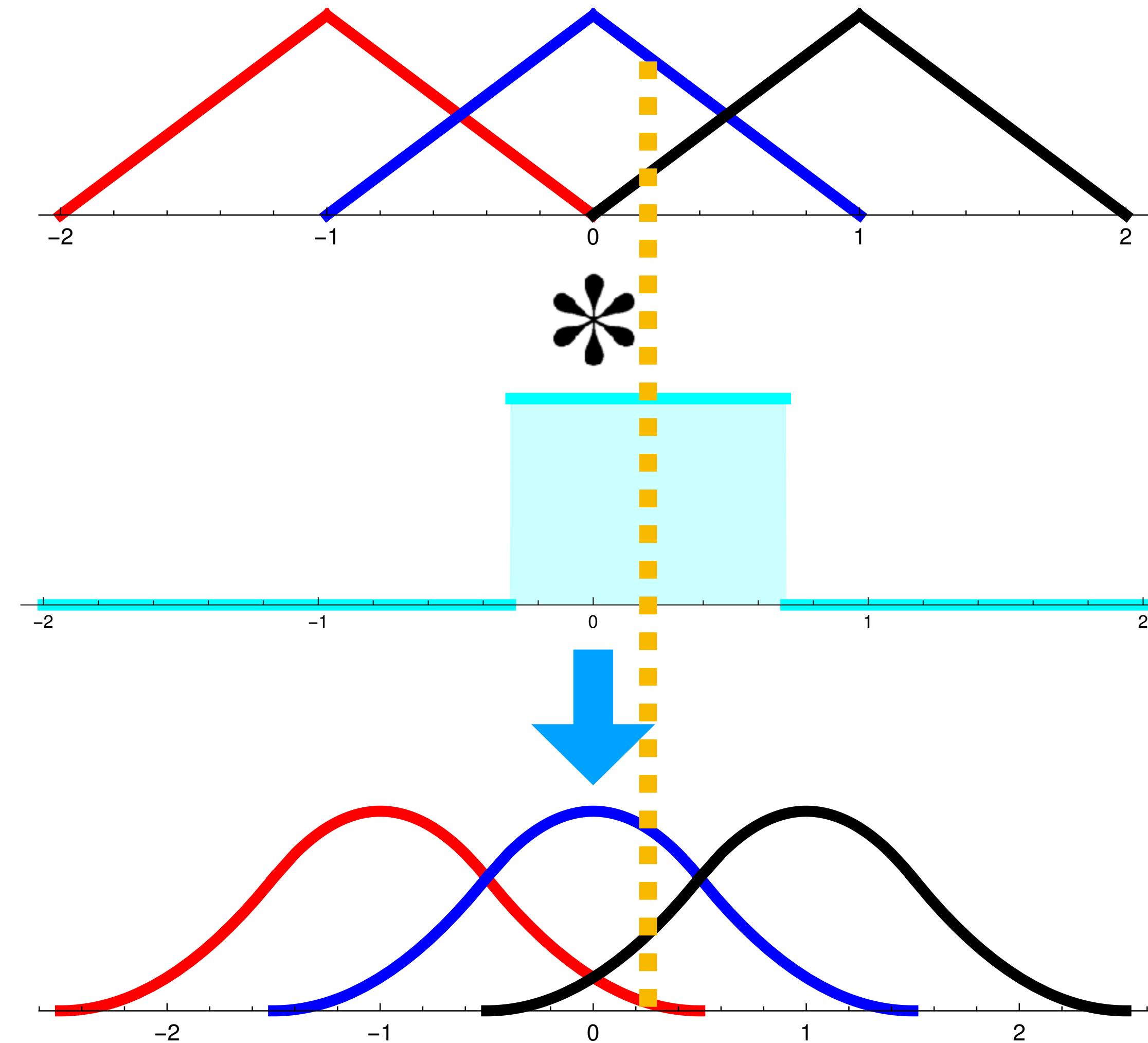


Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



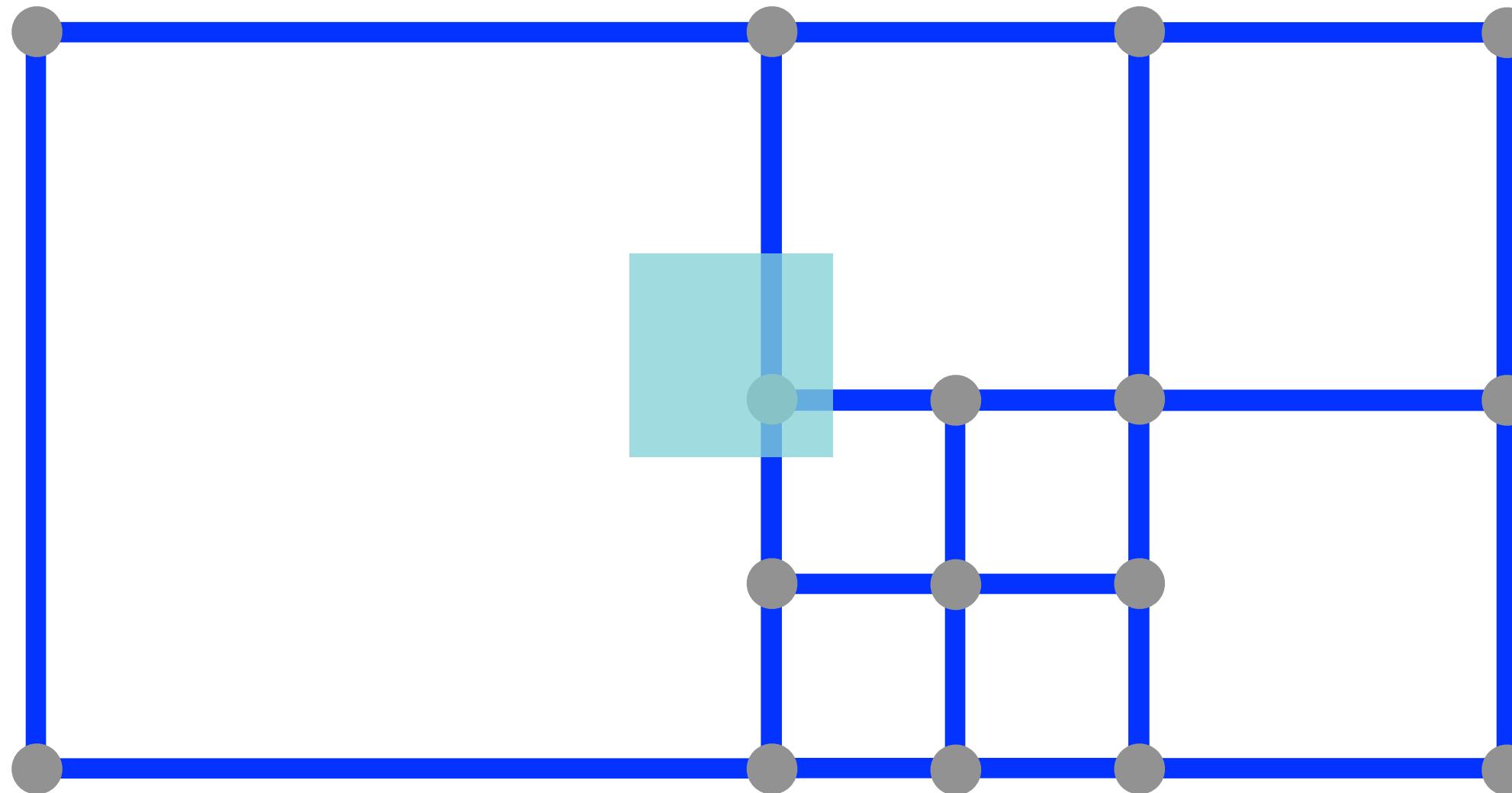
Step 3 - upgrade to C^1 continuity



GIMP

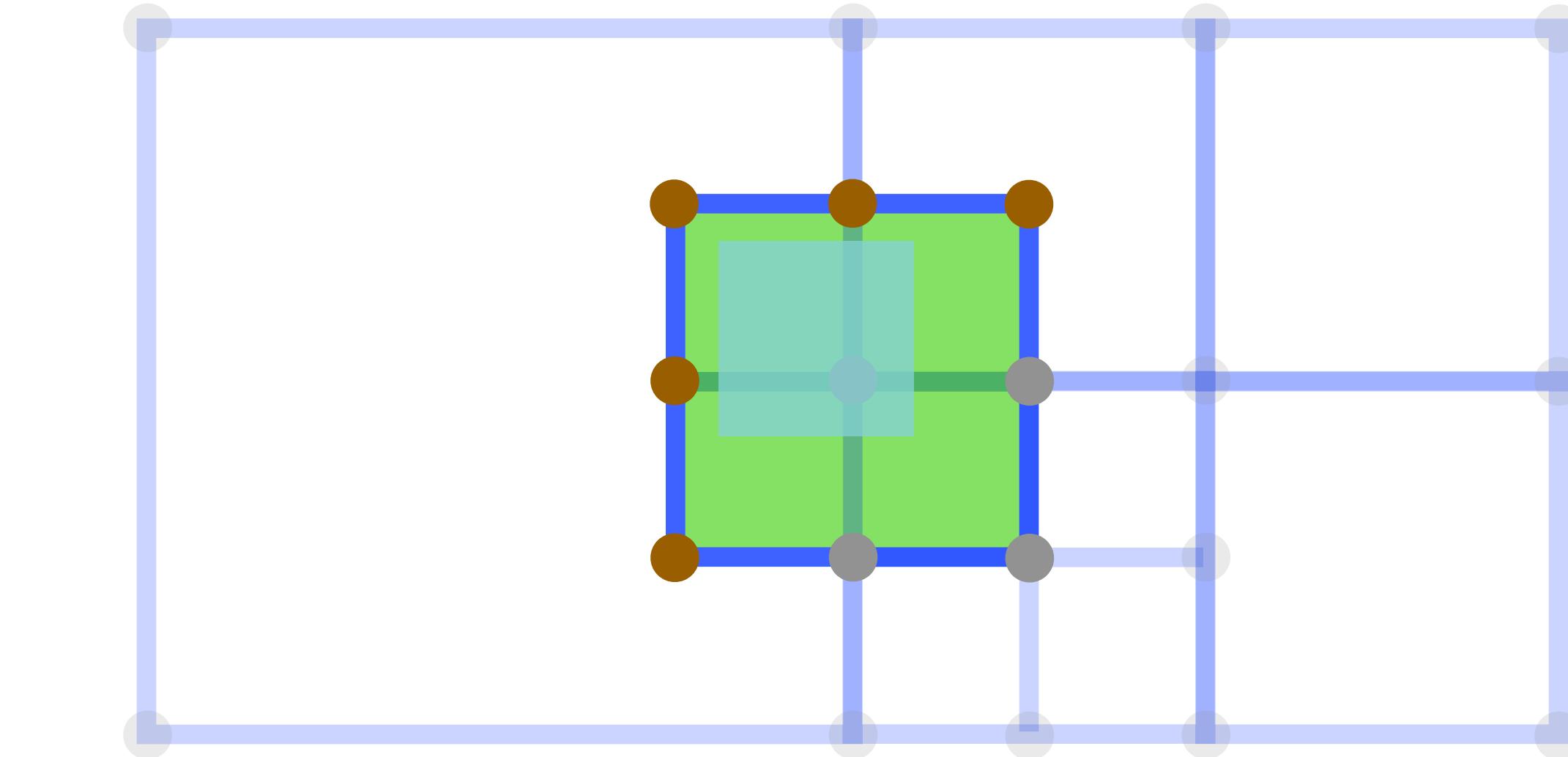
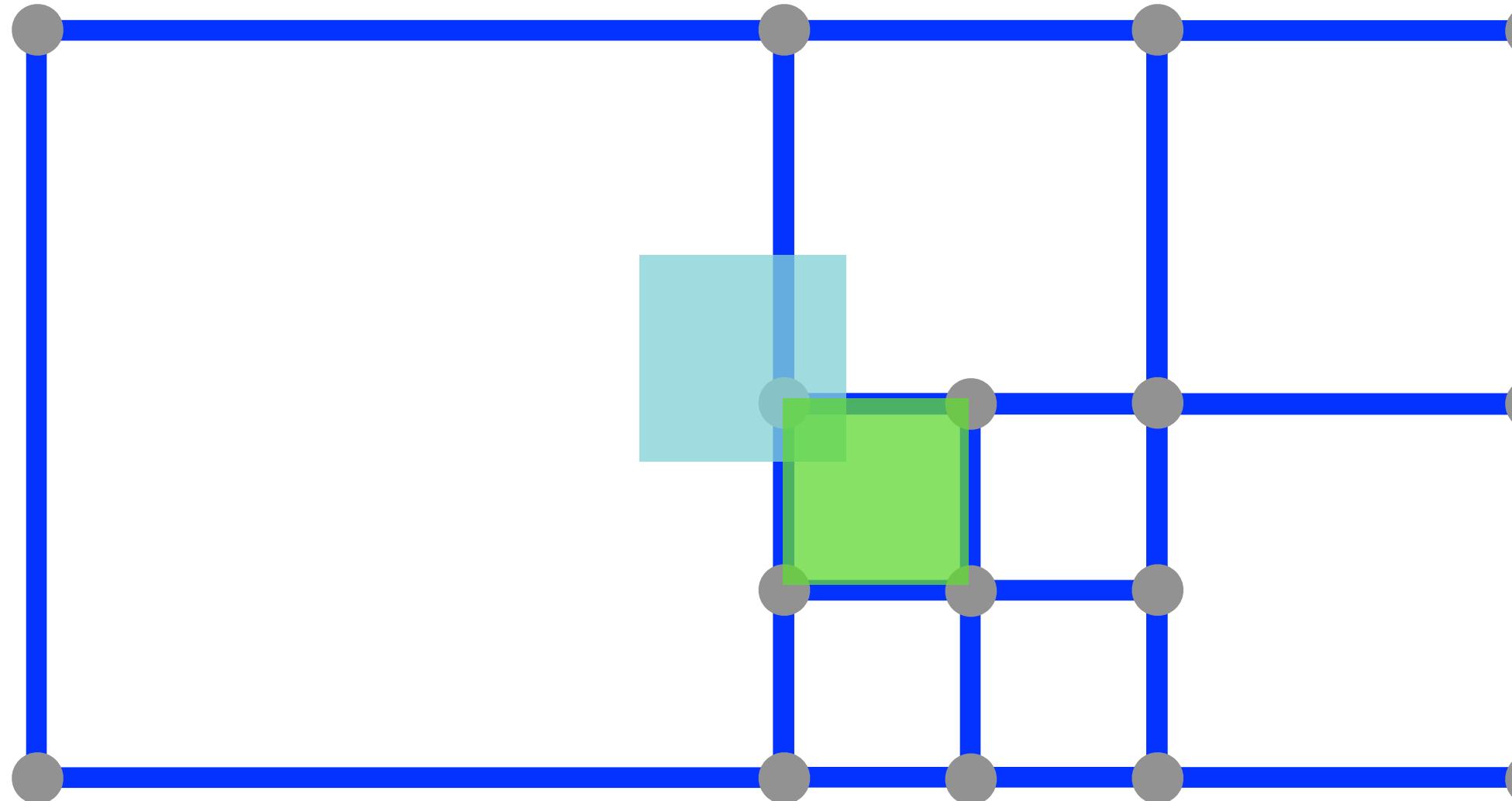
Step 3 - upgrade to C^1 continuity

- Free node



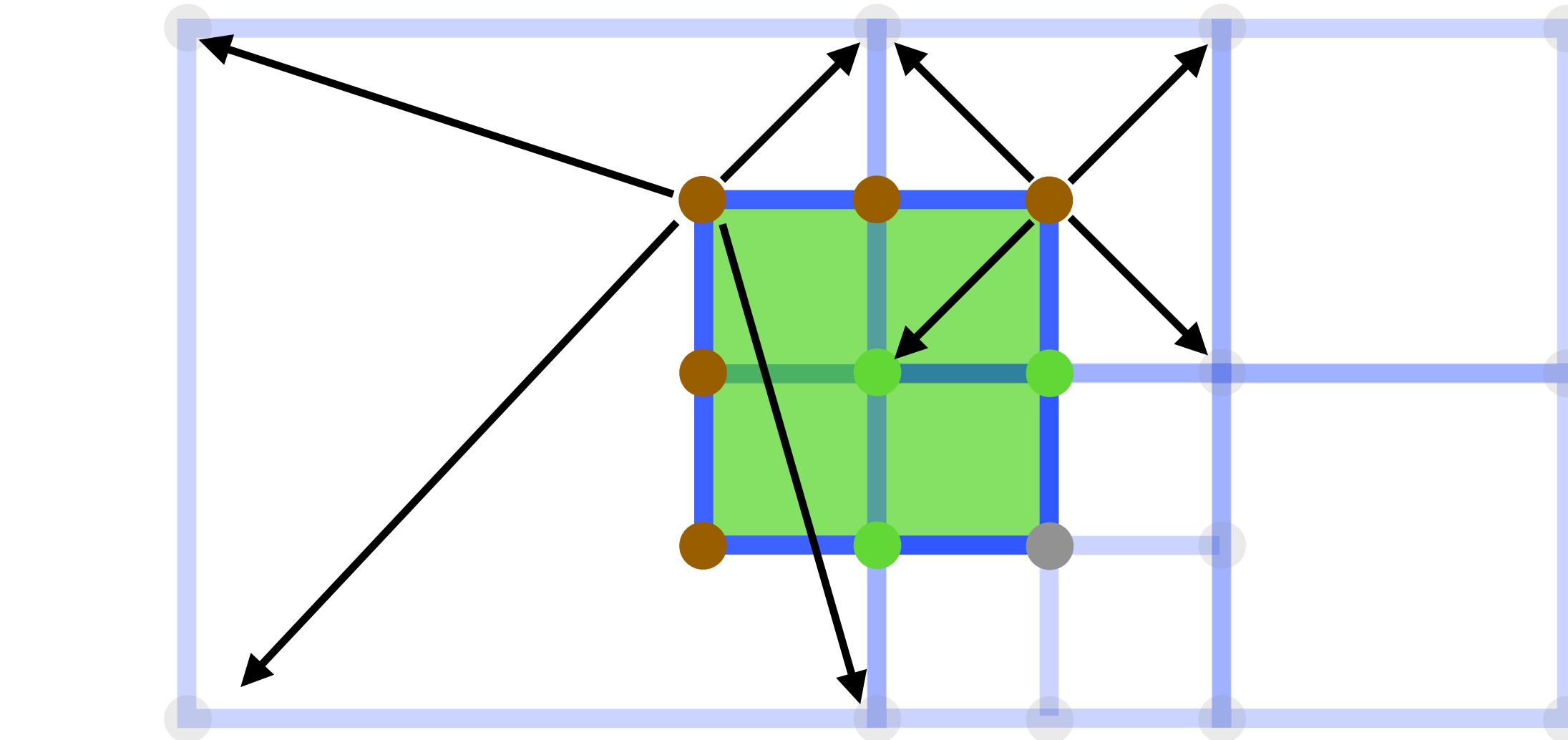
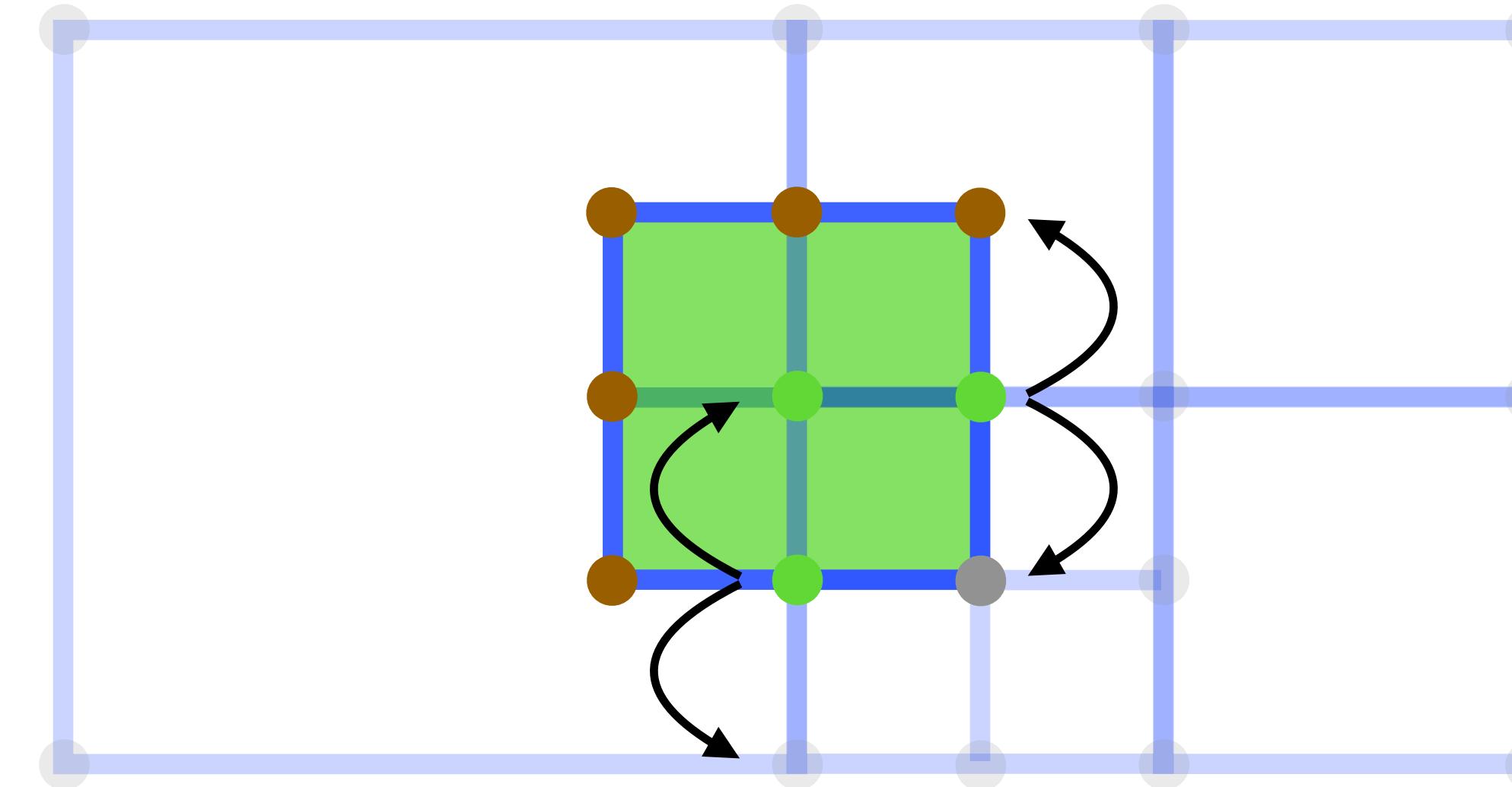
Parallelism optimization

- Free node
- Ghost node

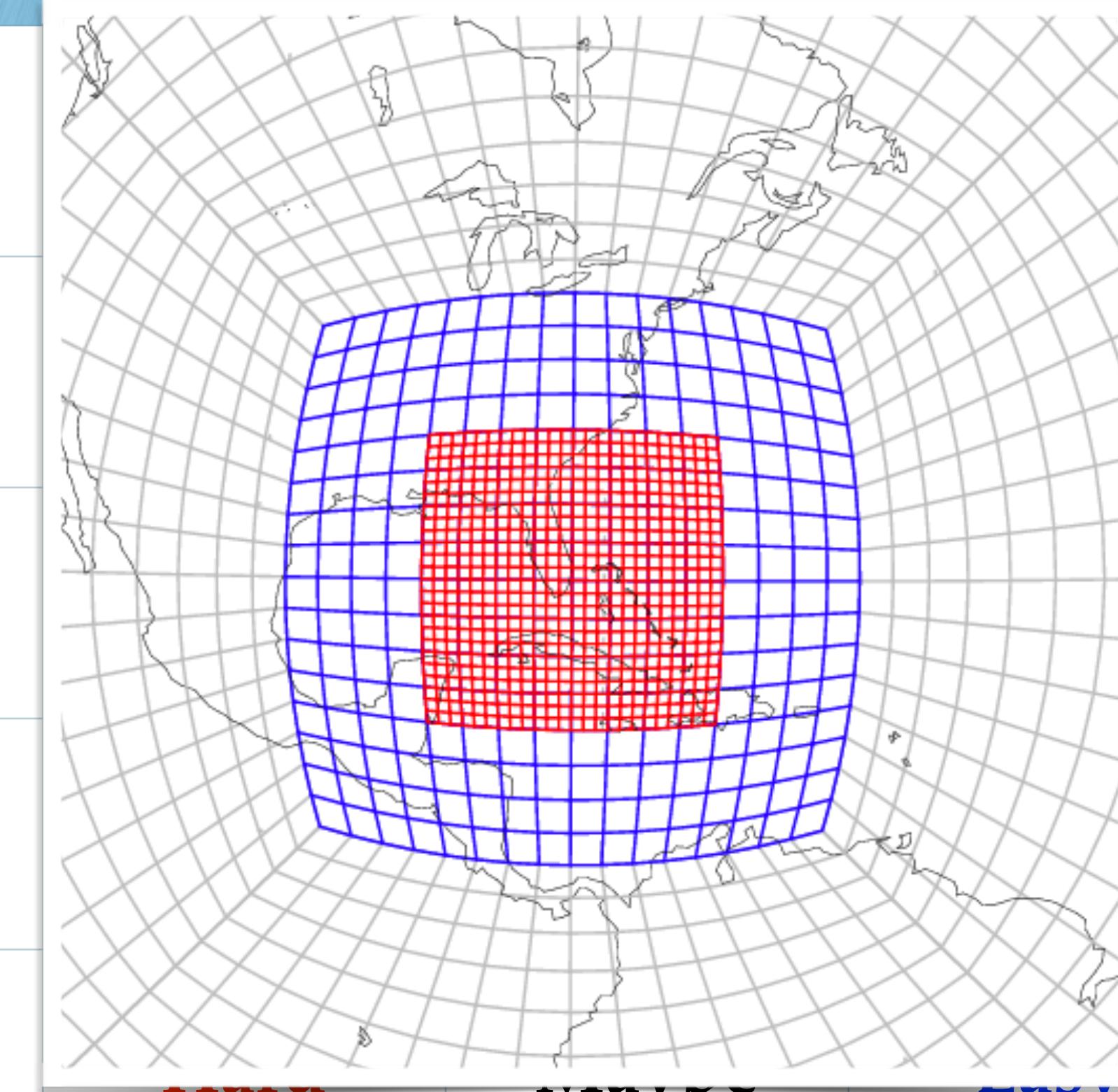


Parallelism optimization

- Free node
- Ghost node
- T-junction node

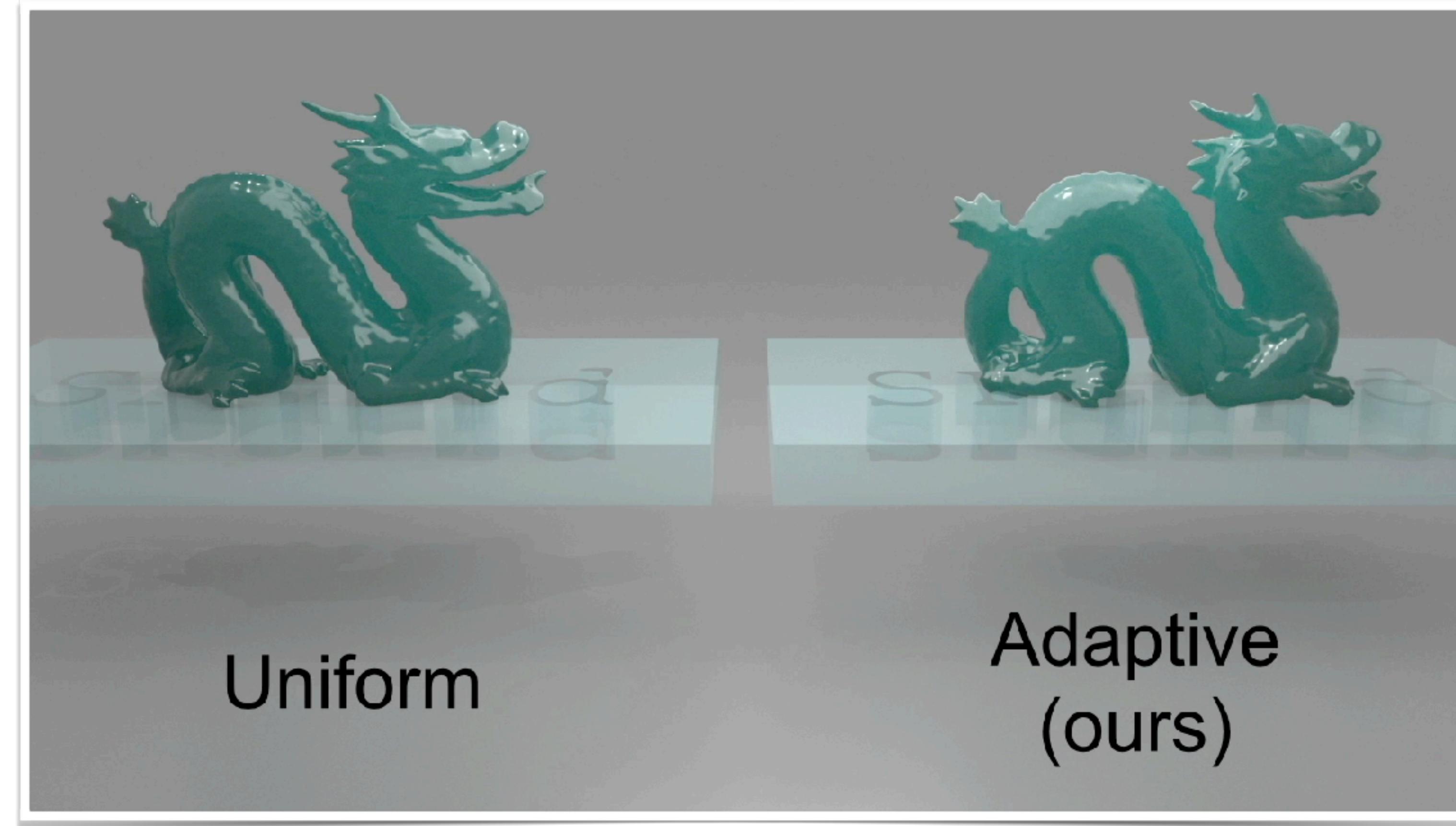


	Tan 02	Ma 05	Lian 14	Lian 15	Our
C1 continuity	No	Yes			
Partition of unity	Yes	Yes			
Non-negativity	Yes	Yes			
Arbitrary octree	Yes	No			
Ease of parallelism	Hard	Maybe			

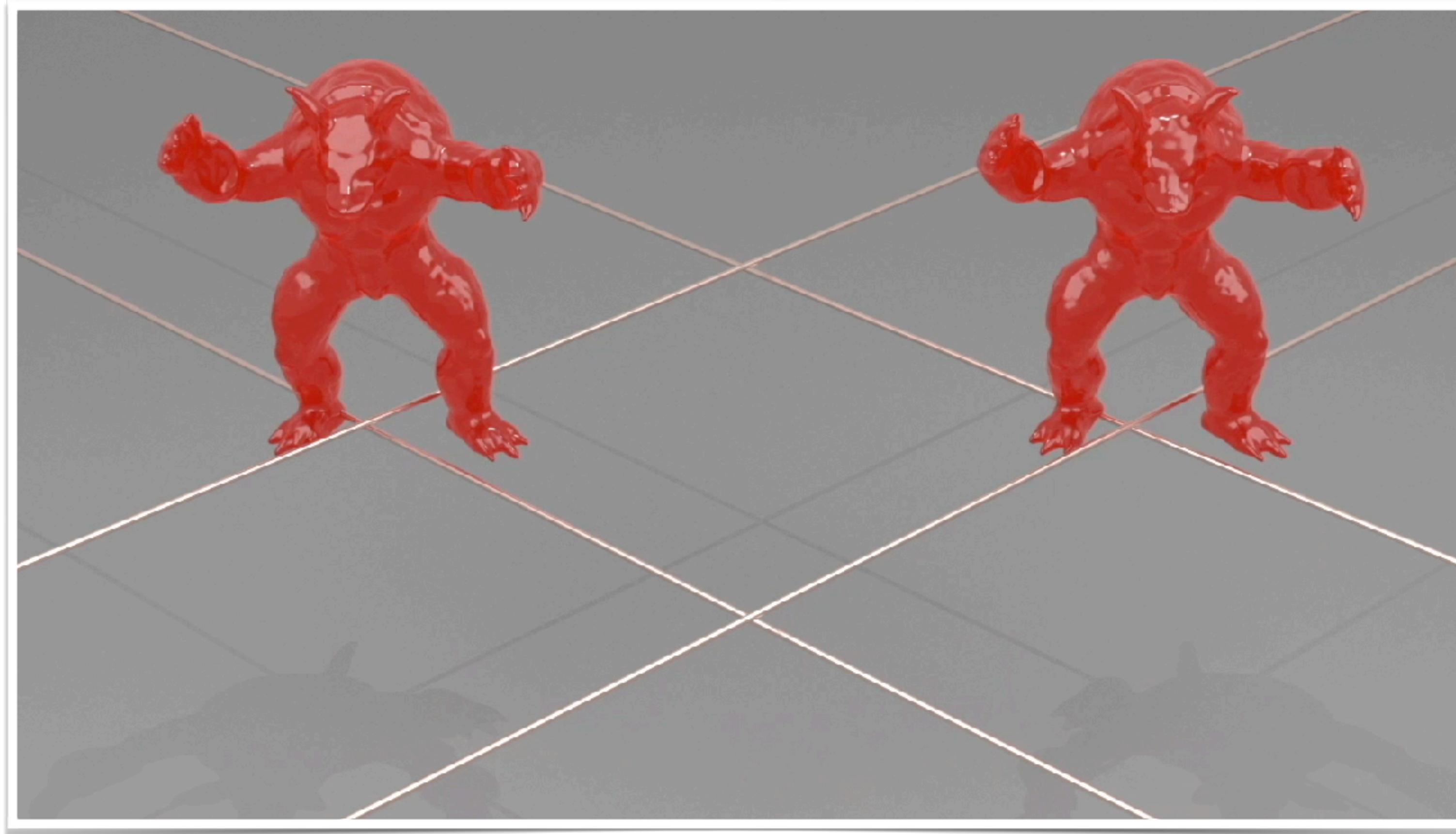


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- J. Ma, H. Lu, B. Wang, S. Roy, R. Hornung, A. Wissink, and R. Komanduri. 2005. **Multiscale simulations using generalized interpolation material point (GIMP) method and SAMRAI parallel processing.** Comp Model Eng & Sci 8, 2 (2005), 135–152.
- Y. Lian, X. Zhang, F. Zhang, and X. Cui. 2014. **Tied interface grid material point method for problems with localized extreme deformation.** Int J Imp Eng 70 (2014), 50–61.
- Y.P. Lian, P.F. Yang, X. Zhang, F. Zhang, Y. Liu, and P. Huang. 2015. **A mesh-grading material point method and its parallelization for problems with localized extreme deformation.** Comp Meth App Mech Eng 289 (2015), 291 – 315.

Results



Results



Animating Fluid Sediment Mixture in Particle-Laden Flows

Animating Fluid Sediment Mixture in Particle-Laden Flows

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XUCHEN HAN, University of California, Los Angeles
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GRANT KOT, Phosphorus
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CHENFANFU JIANG, University of Pennsylvania



Fig. 1. **Sediment transport:** Our method can animate intricate two-way coupled particle-laden flows such as sediment transport in liquid.

In this paper, we present a mixed explicit and semi-implicit Material Point Method for simulating particle-laden flows. We develop a Multigrid Preconditioned fluid solver for the Locally Averaged Navier Stokes equation. This is discretized purely on a semi-staggered standard MPM grid. Sedimentation is modeled with the Drucker-Prager elastoplasticity flow rule, enhanced by a novel particle density estimation method for converting particles between representations of either continuum or discrete points. Fluid and sediment are two-way coupled through a momentum exchange force that can be easily resolved with two MPM background grids. We present various results to demonstrate the efficacy of our method.

CCS Concepts: • Computing methodologies → Physical simulation;

Additional Key Words and Phrases: Material Point Method (MPM), particle-fluid interaction, multiphase, sedimentation, sediment transport

ACM Reference format:

Ming Gao, Andre Pradhana, Xuchen Han, Qi Guo, Grant Kot, Eftychios Sifakis, and Chenfanfu Jiang. 2018. Animating Fluid Sediment Mixture in Particle-Laden Flows. *ACM Trans. Graph.* 37, 4, Article 1 (August 2018), 11 pages.

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1 INTRODUCTION

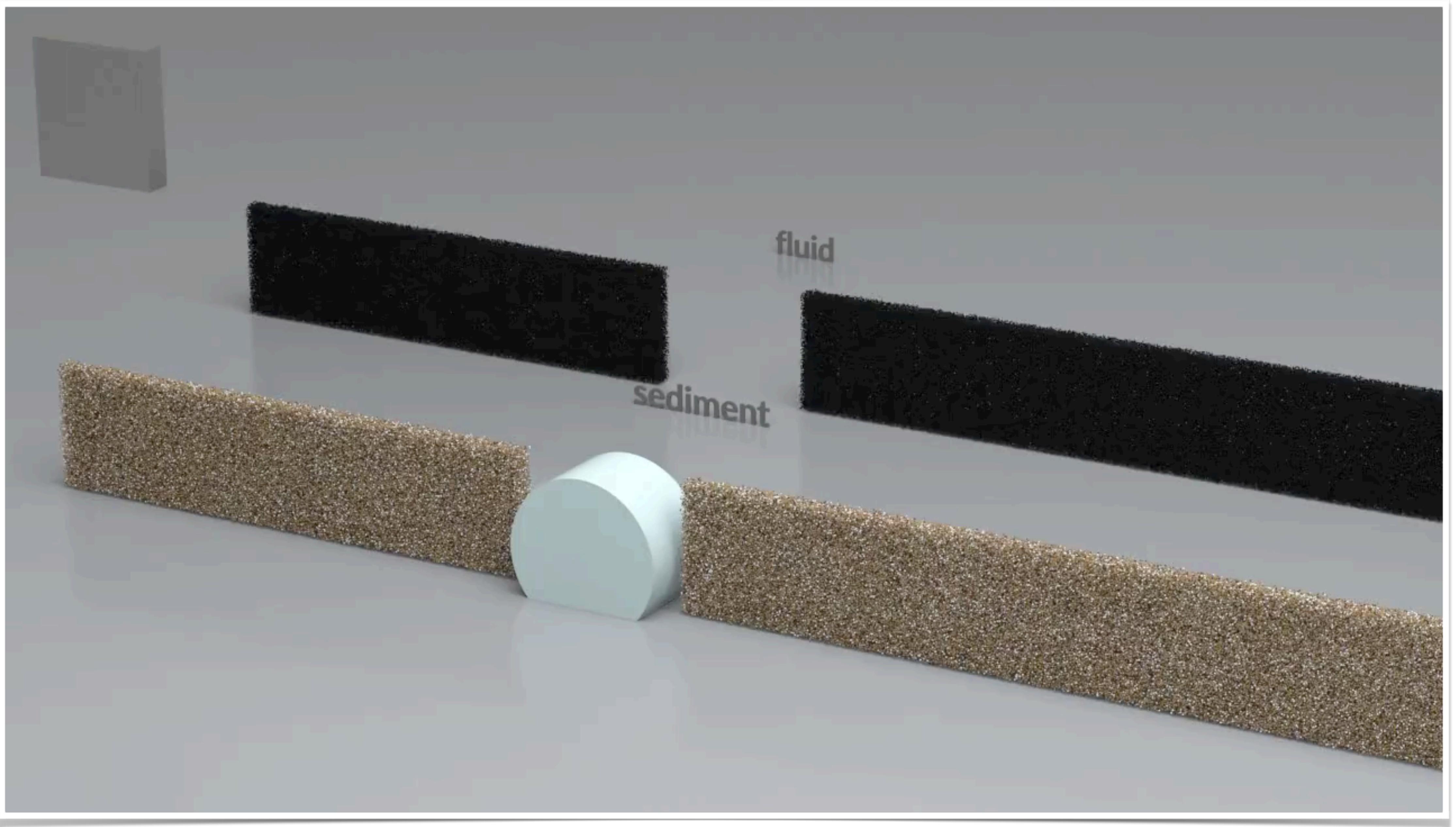
Recently, multi-phase multi-material simulations are increasingly gaining attention from computer graphics researchers. Simulating various phases or materials in a unified framework is particularly favored. Existing work includes coupled Lagrangian particle simulation with Position Based Dynamics (PBD) [Macklin et al. 2014], water-gas mixtures [Nielsen and Østerby 2013] with an Eulerian method, solid-fluid phase-change [Stomakhin et al. 2014] and porous granular media [Pradhana-Tampubolon et al. 2017] with Material Point Method (MPM), as well as interactive solids and fluids based on the mixture model with Smoothed Particle Hydrodynamics (SPH) [Yan et al. 2016].

Most of the existing approaches are based on *continuum* mixture theory [Manninen et al. 1996]. The continuum assumption for each material phase is essential for simulations of macroscopic porous media (e.g., landslides and liquid blending). However, it may fail to capture the correct behavior of particle-laden flows where the solid phase is on a relatively small scale. Note that particle-laden sediment flow is ubiquitous in natural systems. Typical examples include sediment transport, sedimentation, volcano eruption, dune migration by erosion with ripples, and dust storms. The significance of understanding and simulating these phenomena is also recognized in many engineering applications, such as granular material fluidization [van der Hoef et al. 2006] and coastal erosion prediction [Sun and Xiao 2016a].

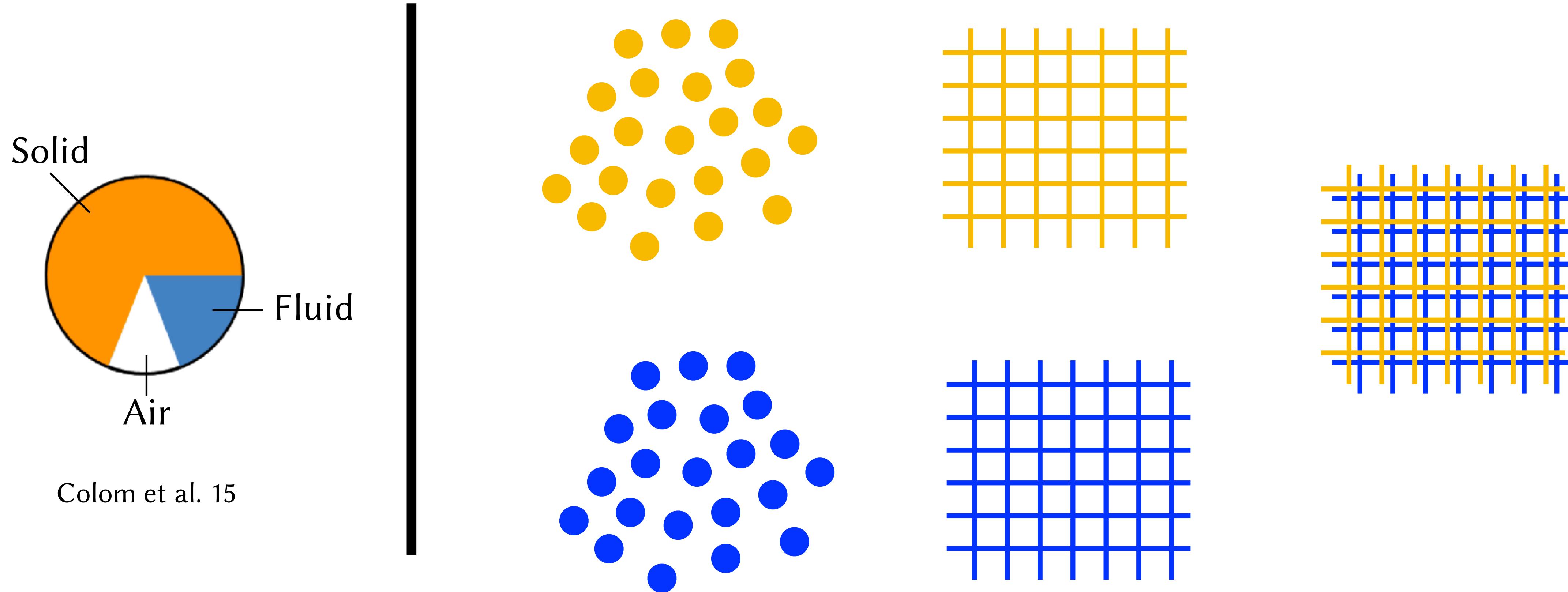
M. Gao, A. Tampubolon, X. Han, Q. Guo, G. Kot, E. Sifakis, C. Jiang
ACM Transactions on Graphics (Proceedings of ACM SIGGRAPH), 2018



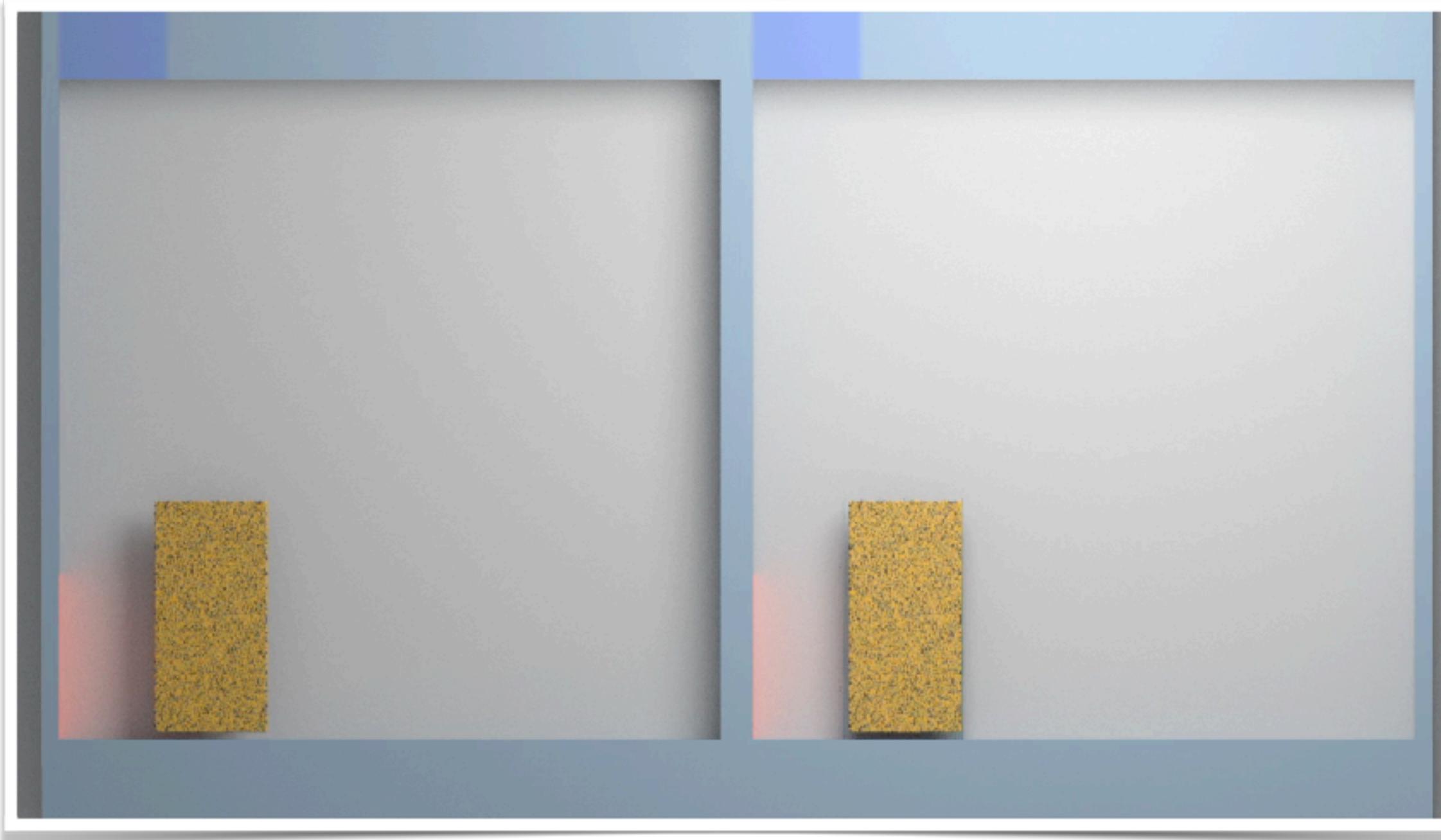
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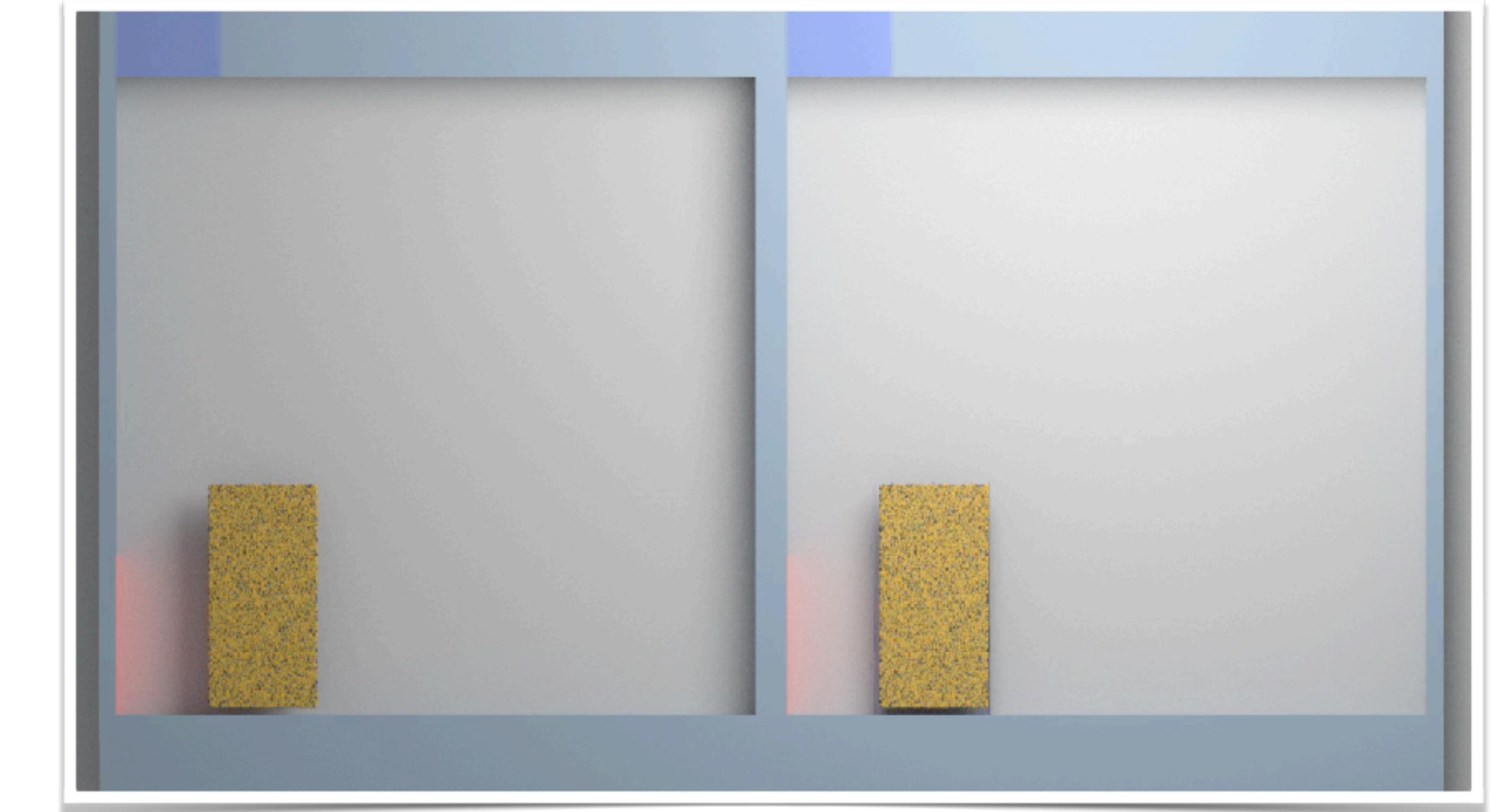
Approach: mixture in particles vs. grid



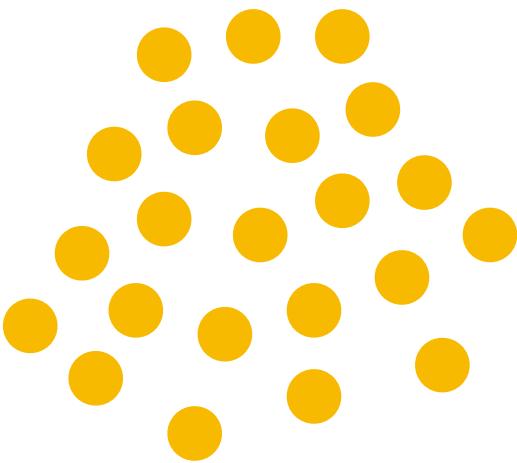
Approach: one-way coupling vs. two-way



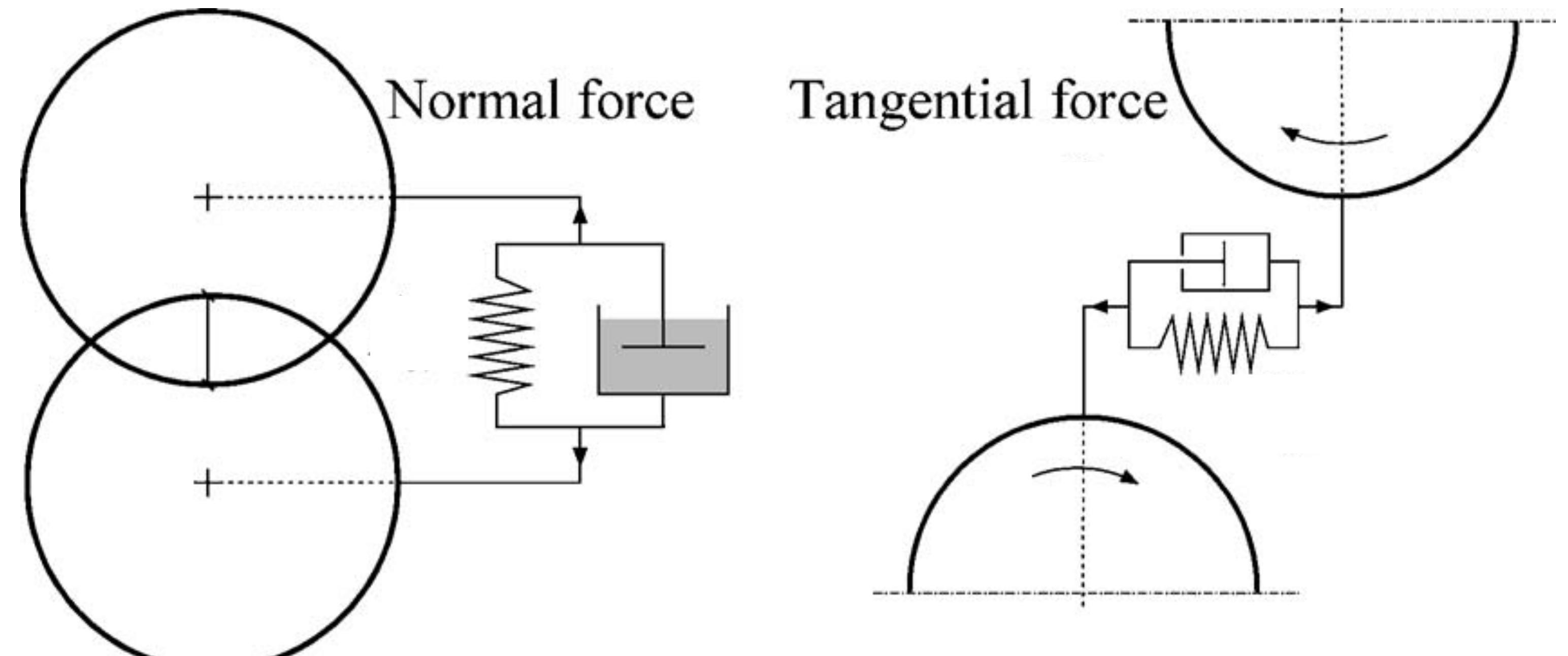
One way coupling



Two way coupling



Approach: DEM vs. MPM

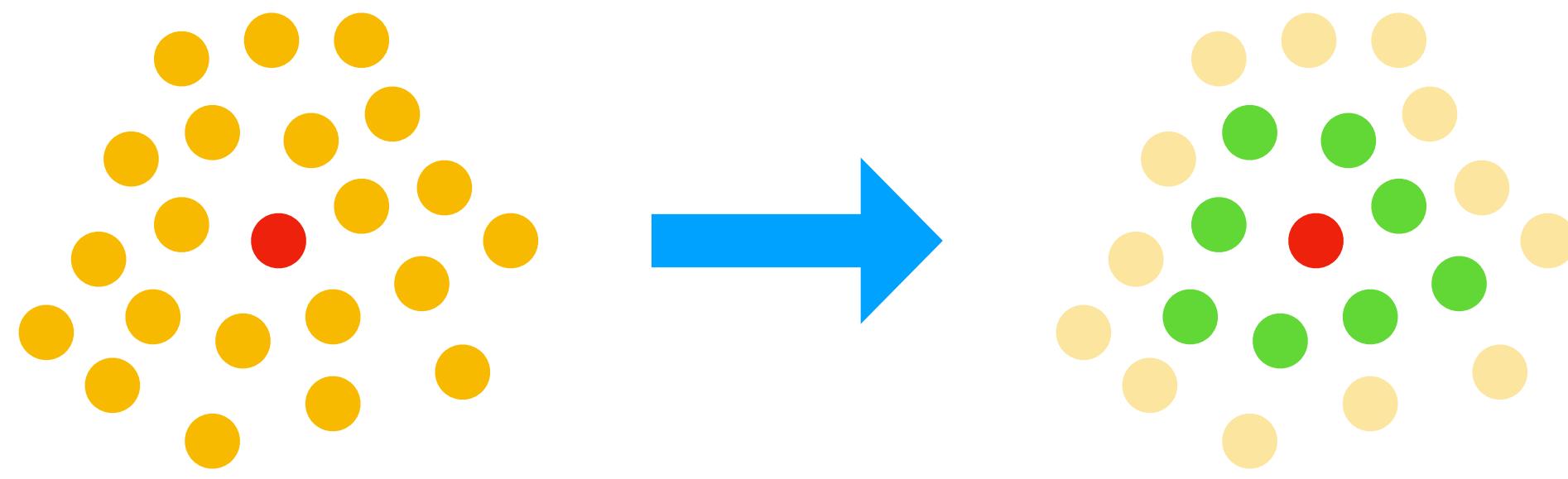


Kruger-Emden et al. 05

Translational interaction

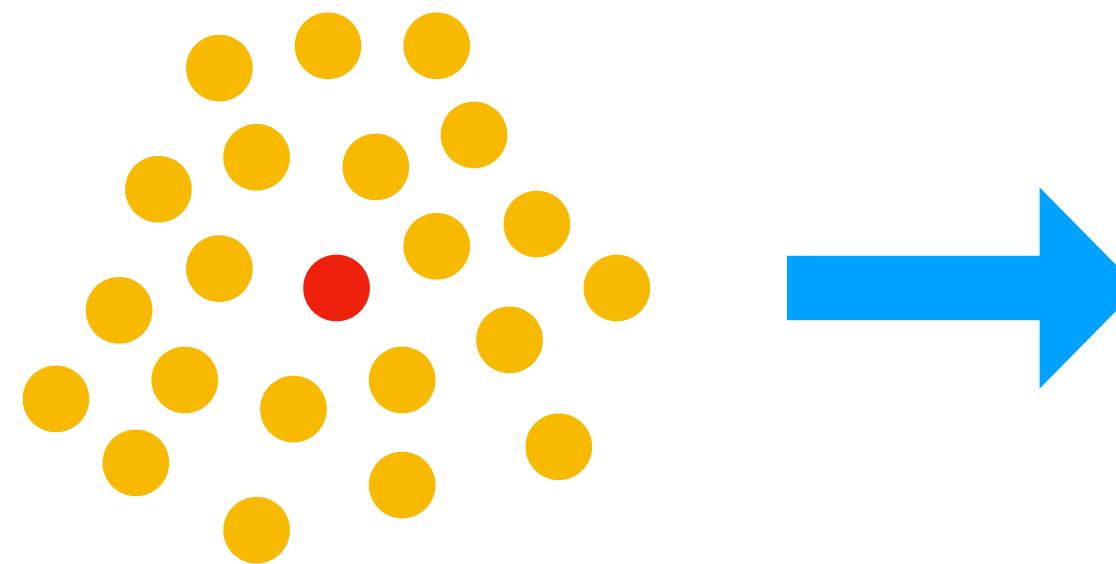
Rotational interaction

Approach: DEM vs. MPM

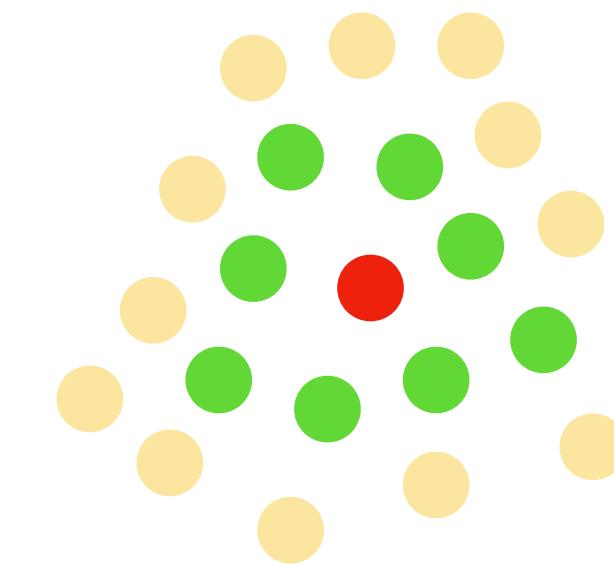


DEM - discrete view

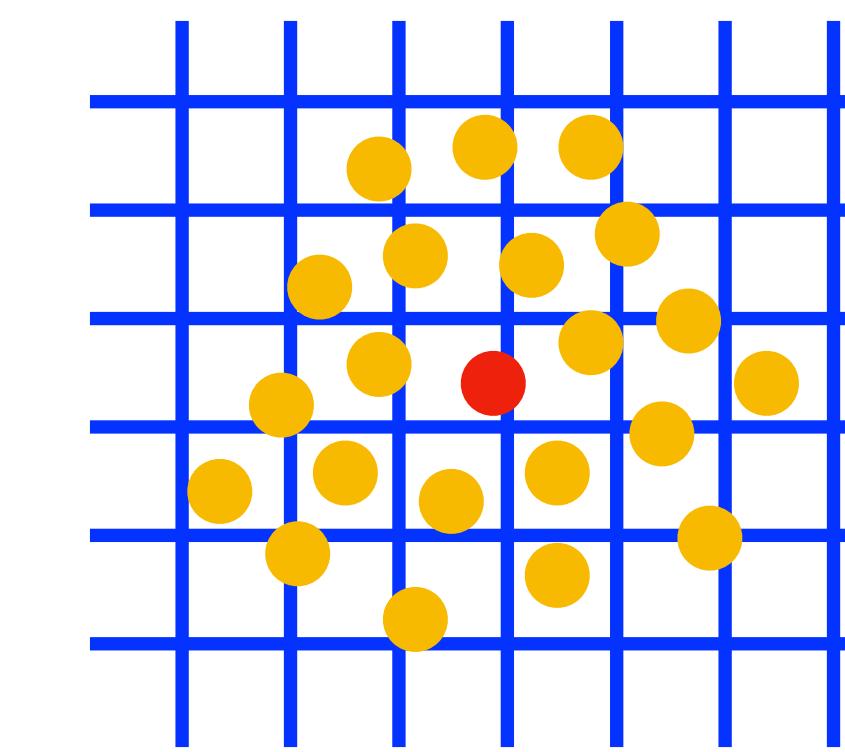
Approach: DEM vs. MPM



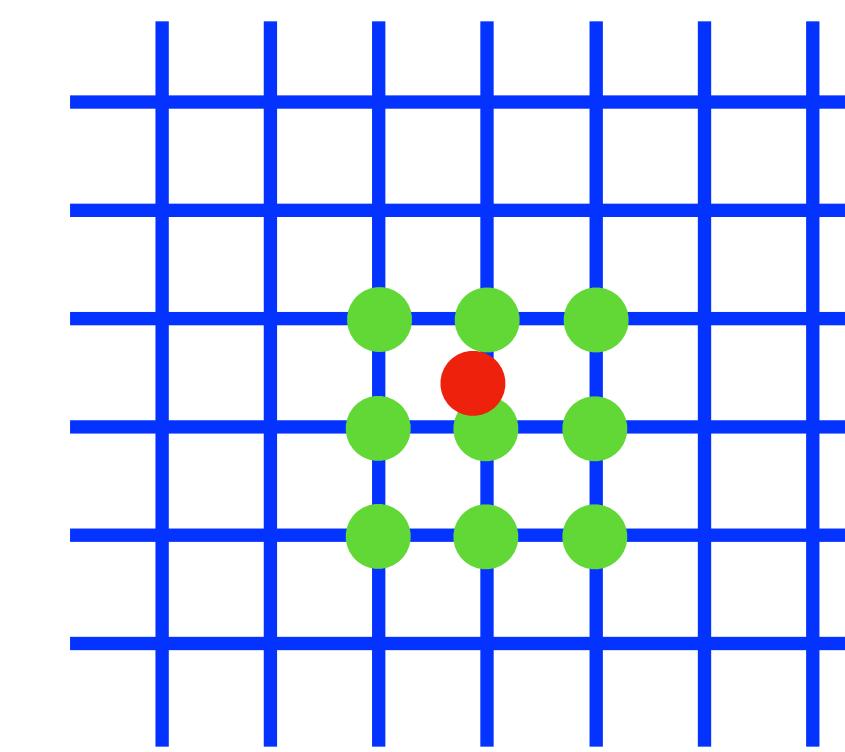
DEM - discrete view



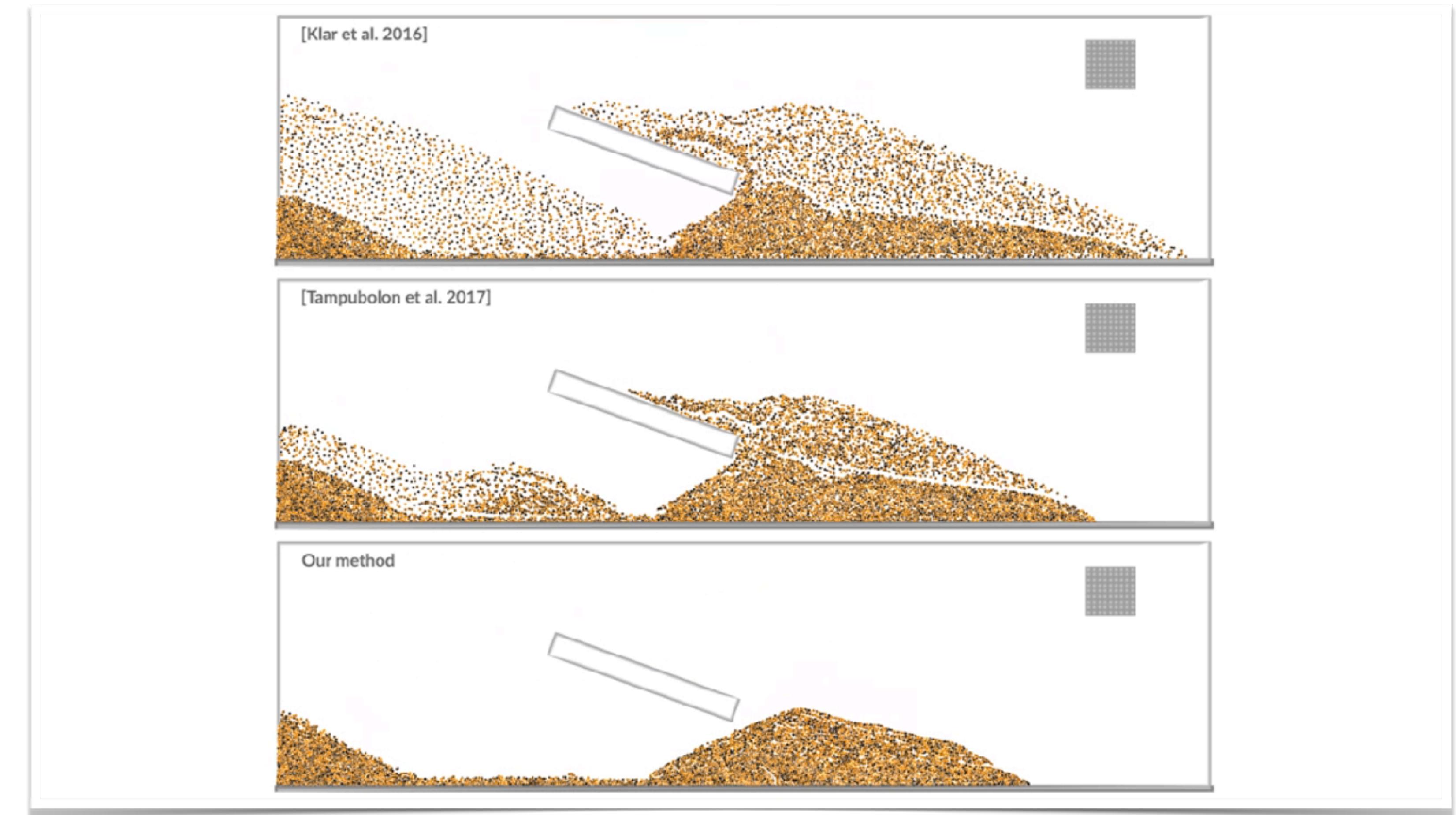
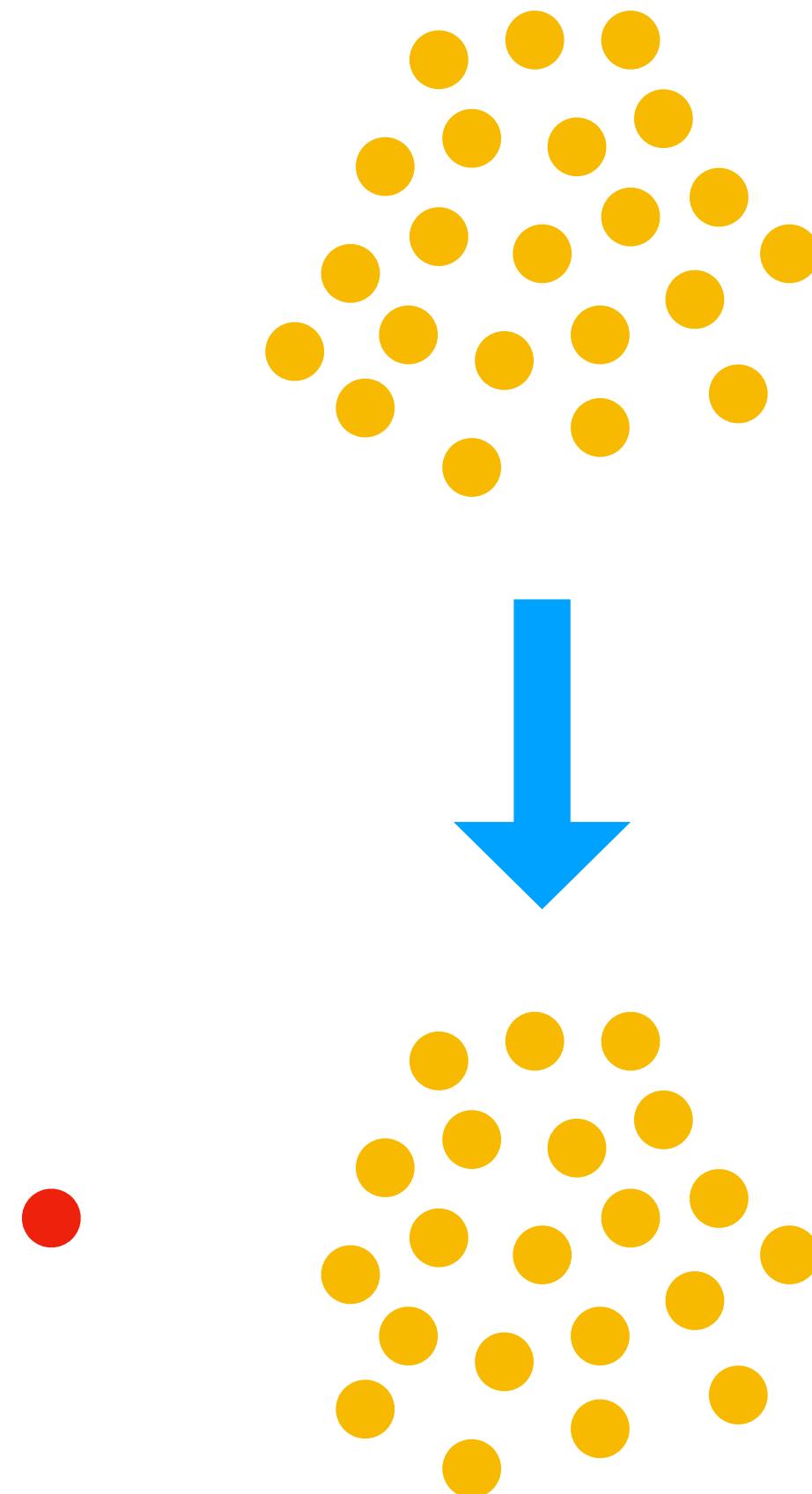
|



MPM - continuum view



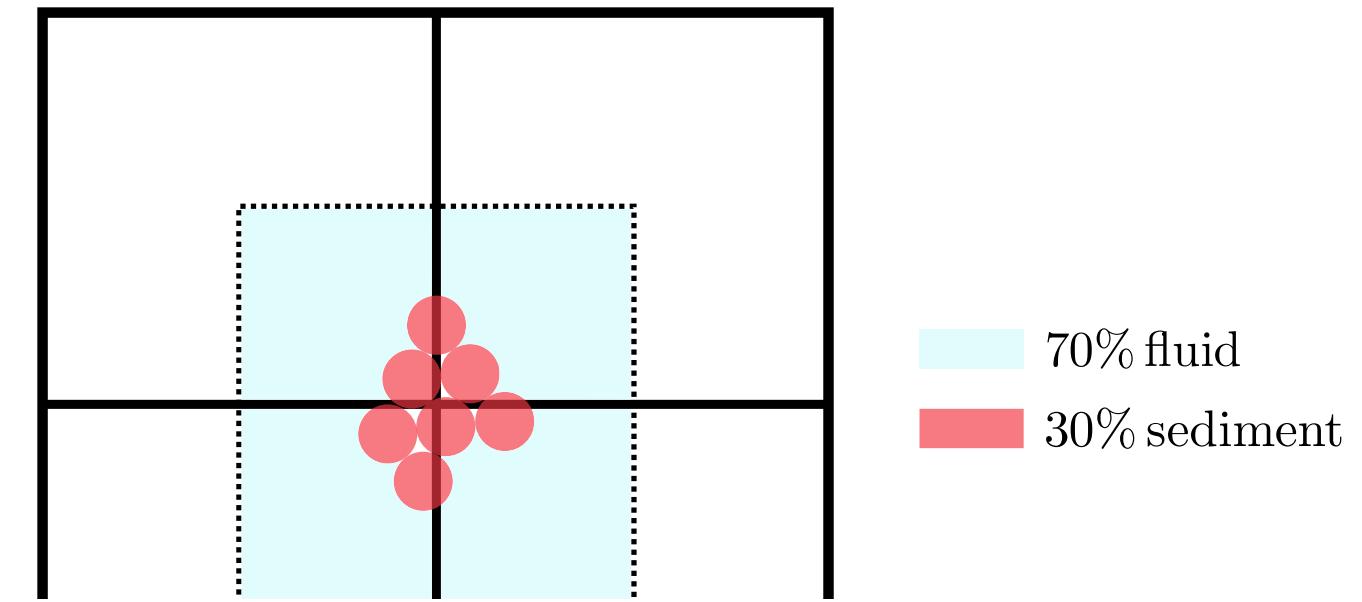
Challenge of MPM: handle discrete particles



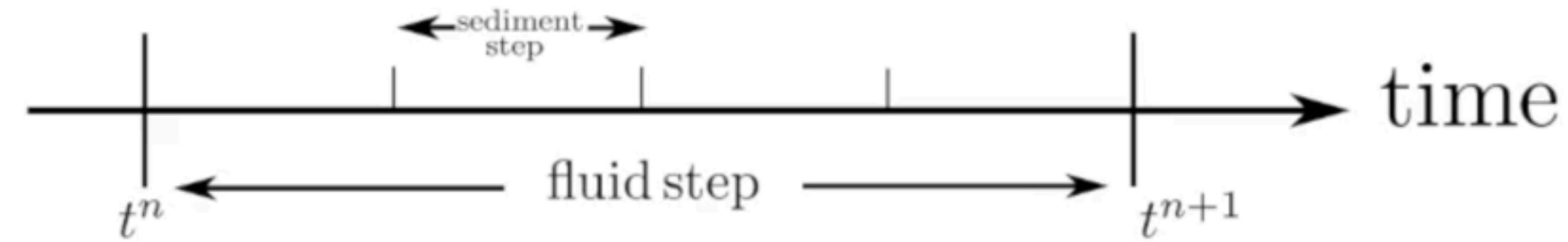
Volume gain problem

Challenges

- Mixture theory

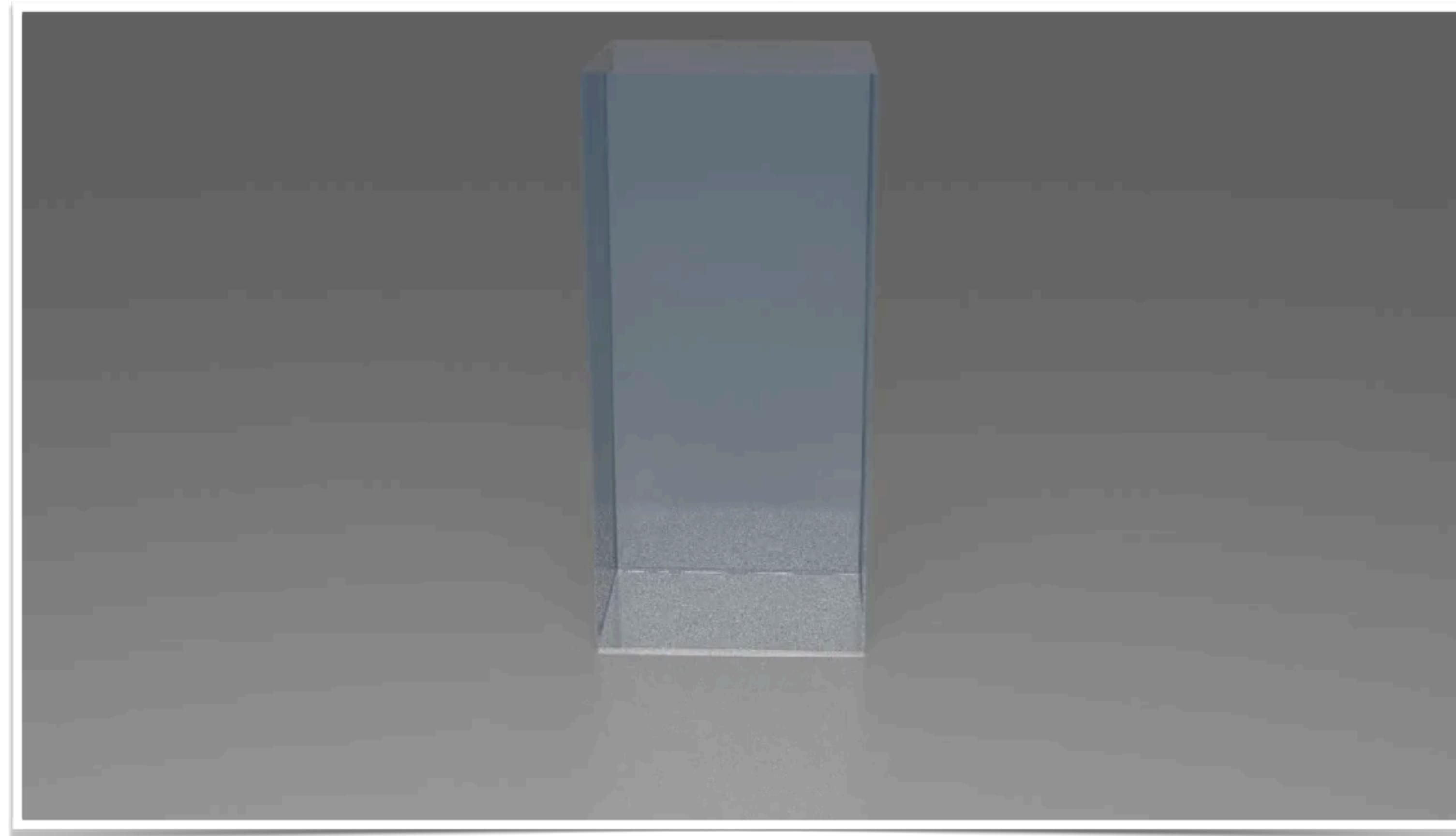


- Sub-stepping

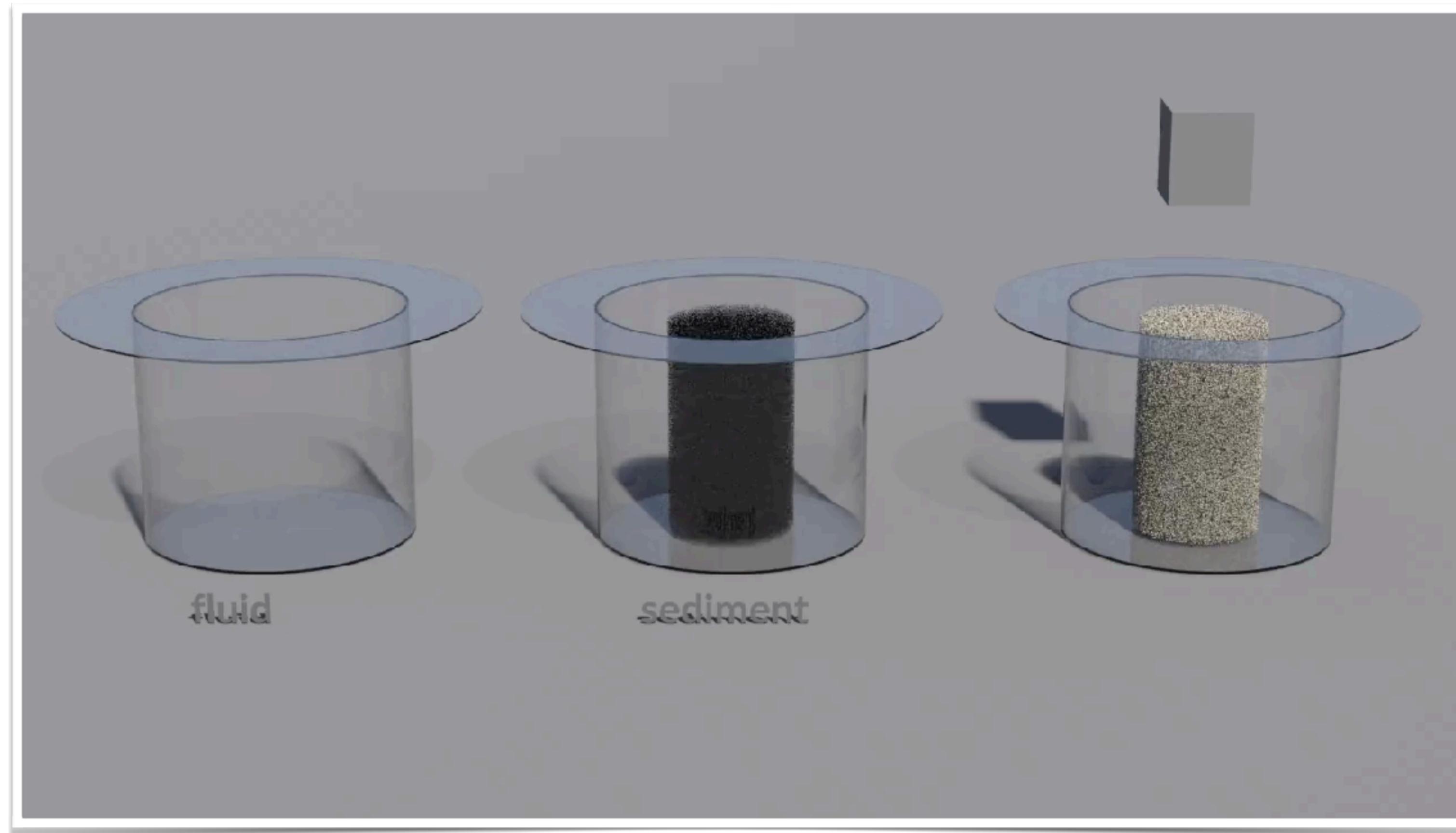


- Momentum conservation

Results



Results



GPU Optimization of Material Point Method

1 GPU Optimization of Material Point Methods
2
3 Paper ID: 250
4
5
6 ANONYMOUS AUTHOR(S)



22 Fig. 1. **How to melt your dragon.** Melting an elastoplastic dragon with 4.2 million particles on a 256^3 grid using our GPU-optimized implicit MPM dynamics
23 and heat solvers on a Nvidia Quadro P6000 GPU at an average 10.5 seconds per 48Hz frame.

24
25 The Material Point Method (MPM) has been shown to facilitate effective
26 simulations of physically complex and topologically challenging materials,
27 with a wealth of emerging applications in computational engineering and
28 visual computing. Borne out of the extreme importance of regularity, MPM is
29 given attractive parallelization opportunities on high-performance modern
30 multiprocessors. Unlike the conceptually simple CPU parallelization, a GPU
31 optimization of MPM that fully leverages computing resources presents chal-
32 lenges that require exploring an extensive design-space for favorable data
33 structures and algorithms. In this paper we introduce methods for addressing
34 the computational challenges of MPM and extending the capabilities of
35 general simulation systems based on MPM, particularly concentrating on
36 GPU optimization. In addition to our open-source high-performance frame-
37 work, we also perform performance analyses and benchmark experiments to
38 compare against alternative design choices which may superficially appear
39 to be reasonable, but can suffer from suboptimal performance in practice.
40 Our explicit and fully implicit GPU MPM solvers are further equipped with a
41 Moving Least Squares MPM heat solver and a novel sand constitutive model
42 to enable fast simulations of a wide range of materials. We demonstrate
43 that more than an order of magnitude performance improvement can be
44 achieved with our GPU solvers. Practical high-resolution examples with up
45 to ten million particles run in less than one minute per frame.

46 CCS Concepts: • Computing methodologies → Physical simulation;

47 Additional Key Words and Phrases: Material Point Method (MPM), GPU,
SPGrid, GVD, Hybrid Particle/Grid

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57 © 2018 ACM. 0730-0301/2018/11-ART1 \$15.00
58 DOI: 10.1145/3197517.3201309

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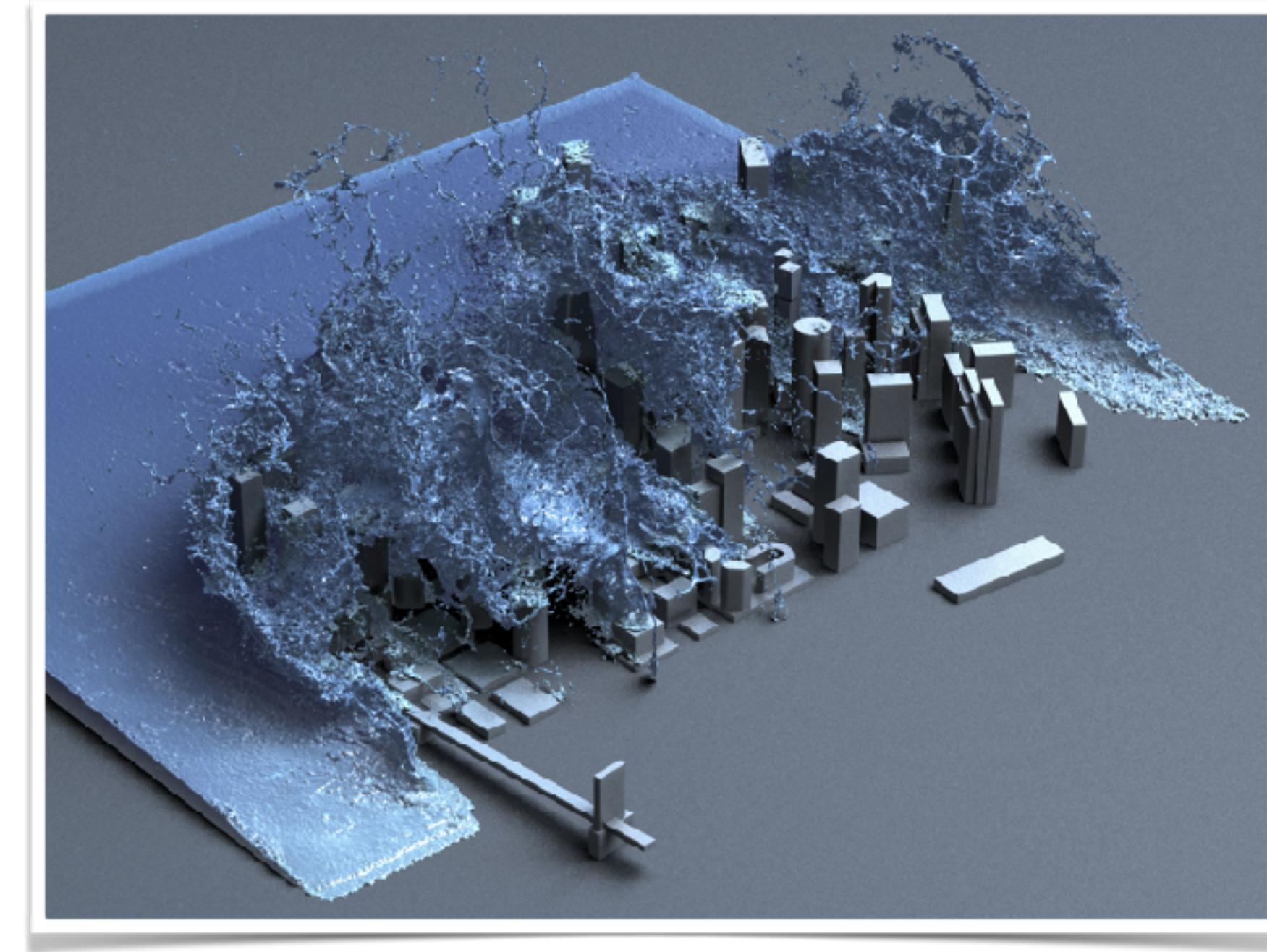
M. Gao*, X. Wang*, K. Wu*(joint first authors),
A. Tampubolon, E. Sifakis, C. Yuksel, C. Jiang
SIGGRAPH Asia 2018 (under review)



Acceleration for hybrid methods

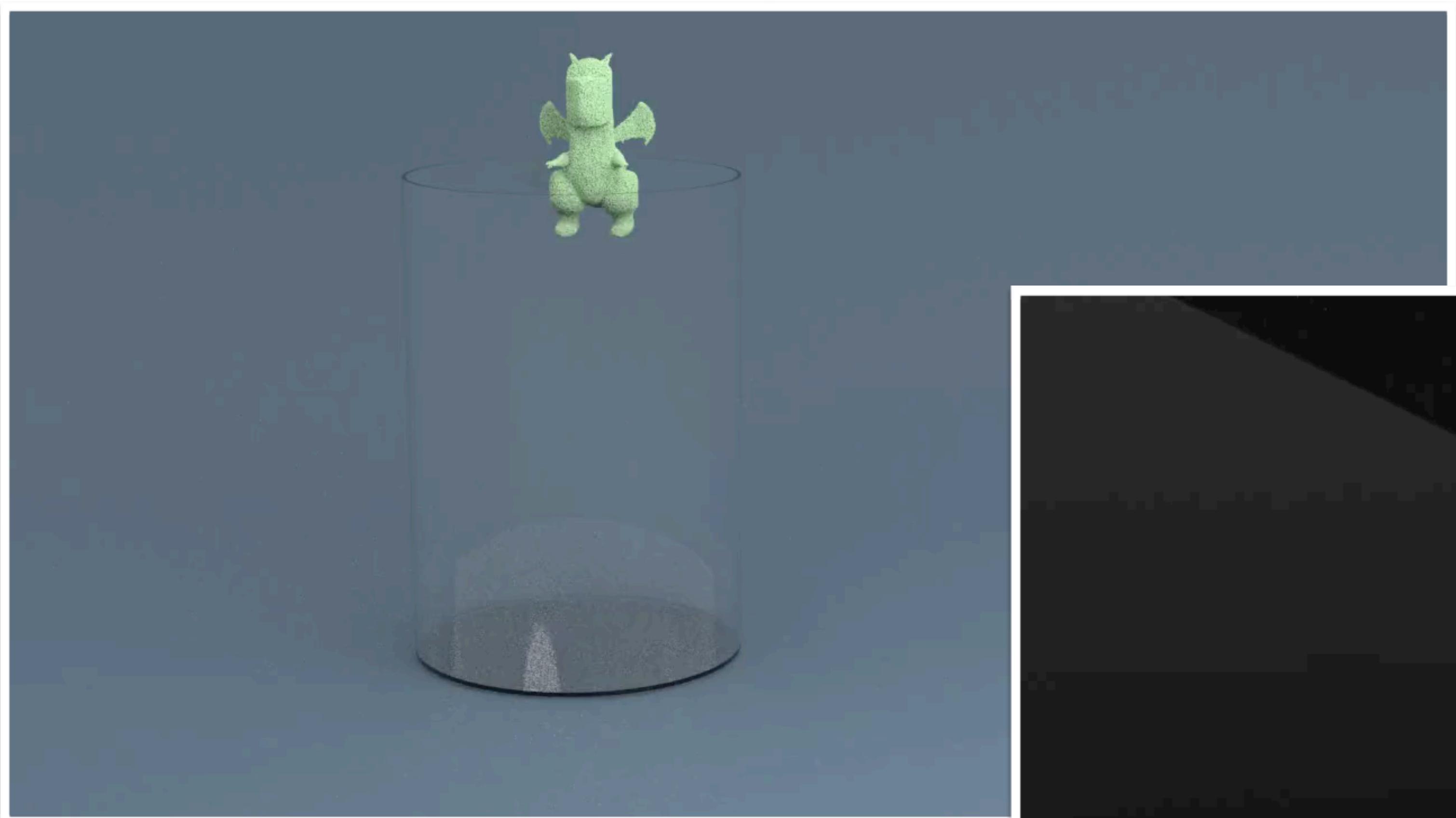


Klar et al. 17



Wu et al. 18

Target benchmarks



Particles: 9.0 M

Grid resolution: 512^3

Simulation: 21.88 secs/frame

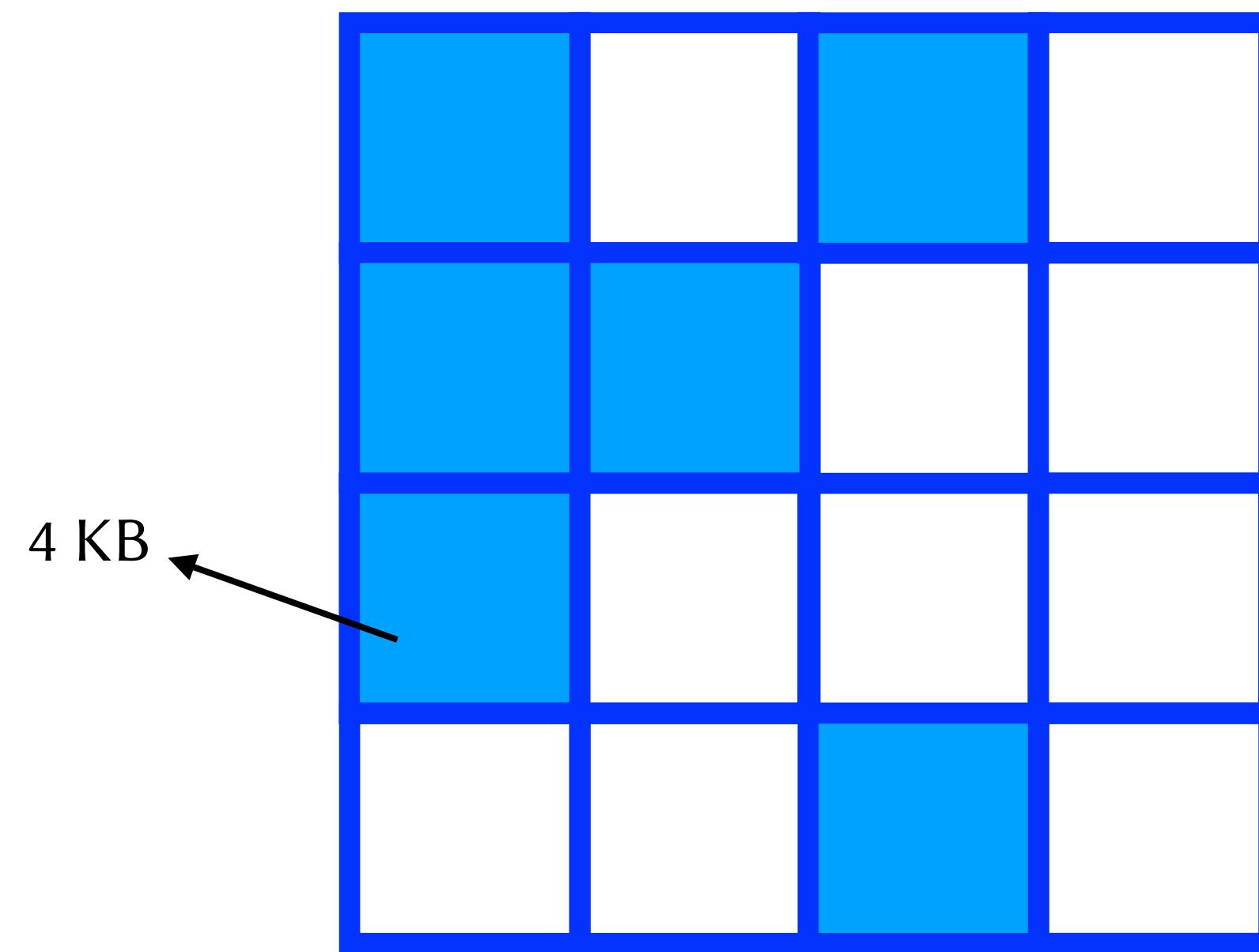
Particles: 4.2 M

Grid resolution: 256^3

Simulation: 10.48 secs/frame



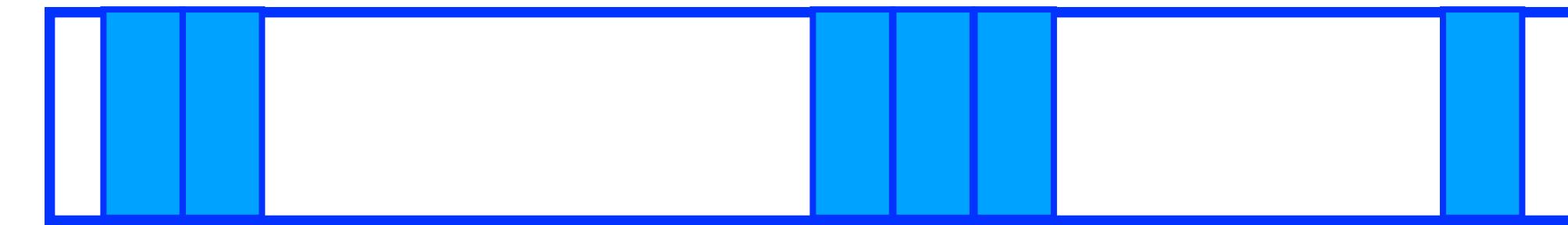
Sparsity - (G)SPGrid



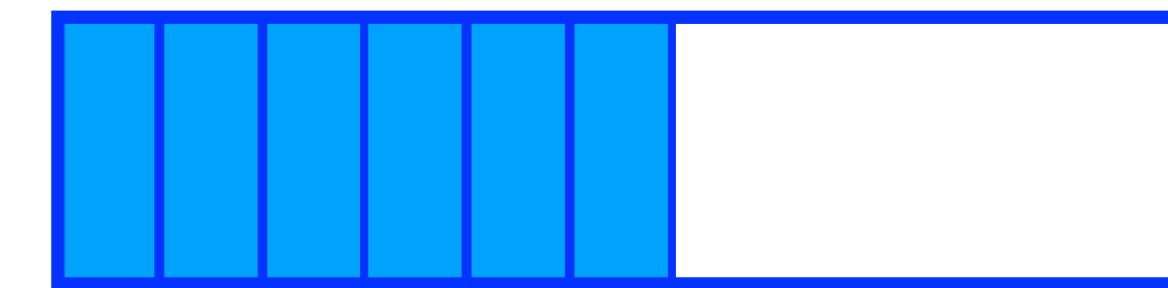
CPU - SPGrid

GPU - GSPGrid

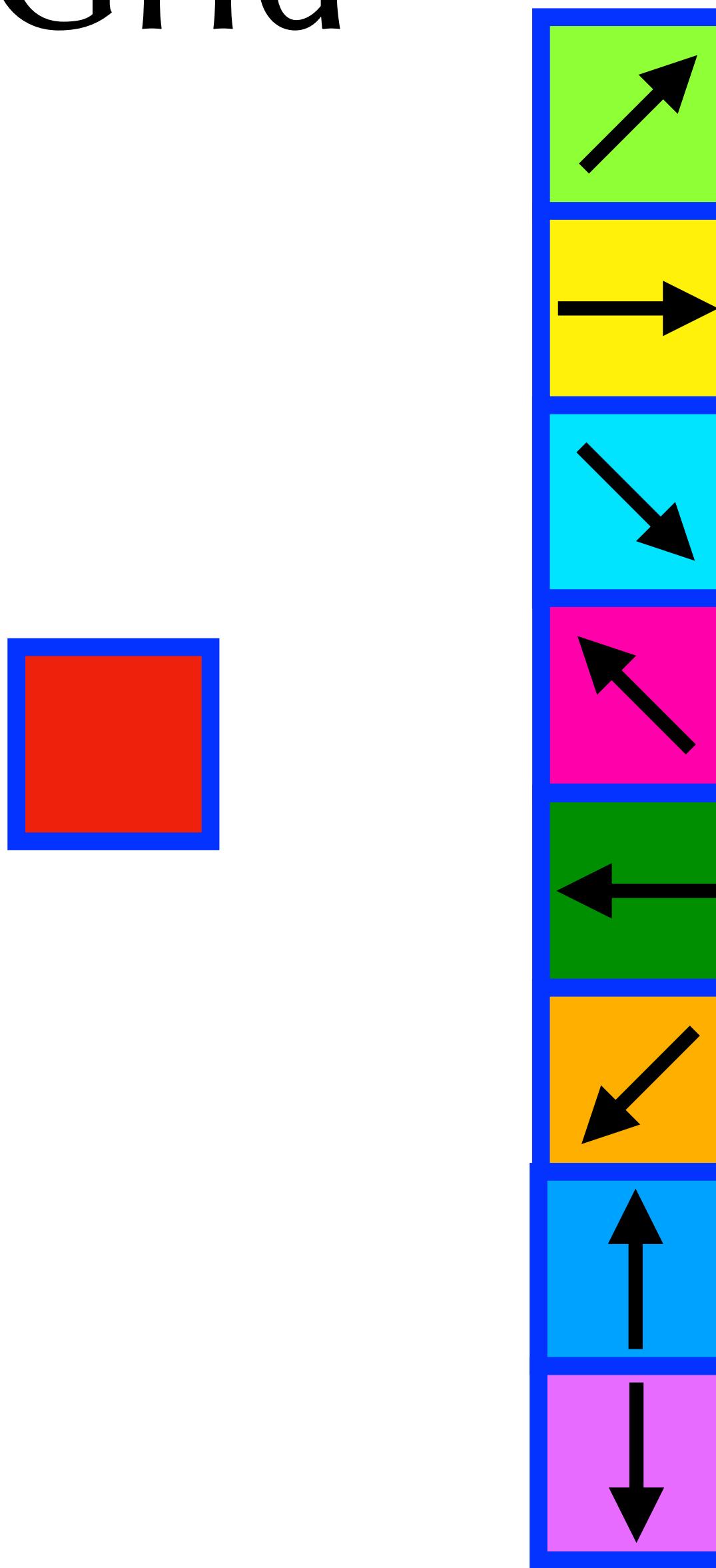
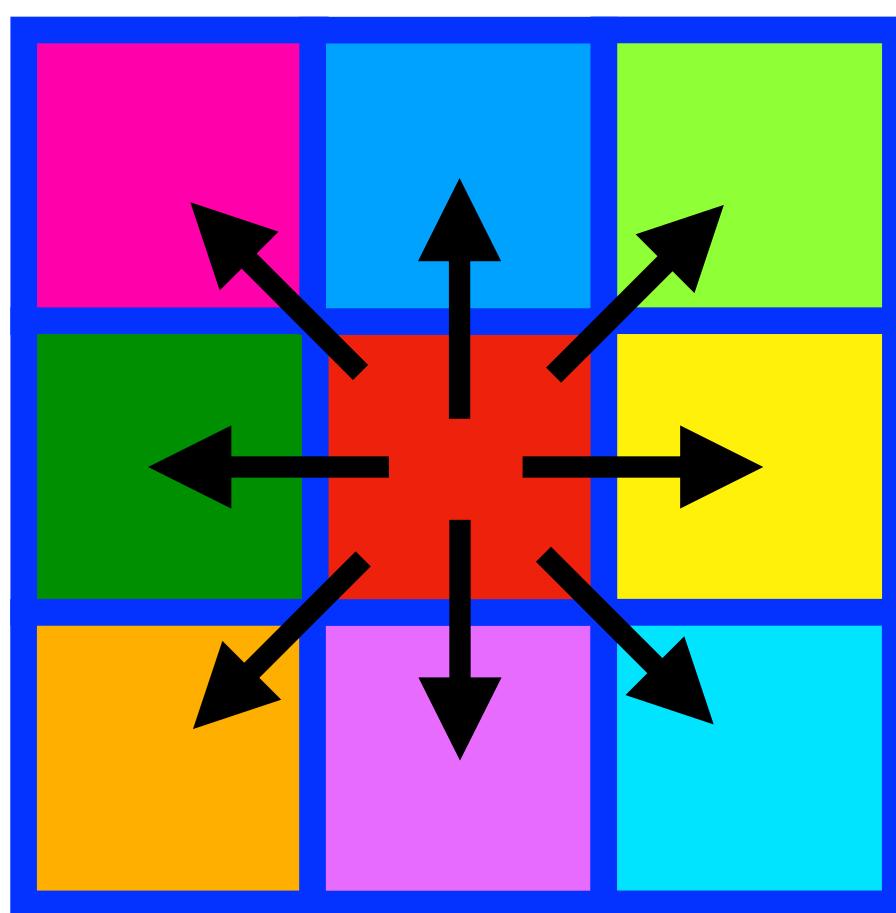
CPU virtual memory



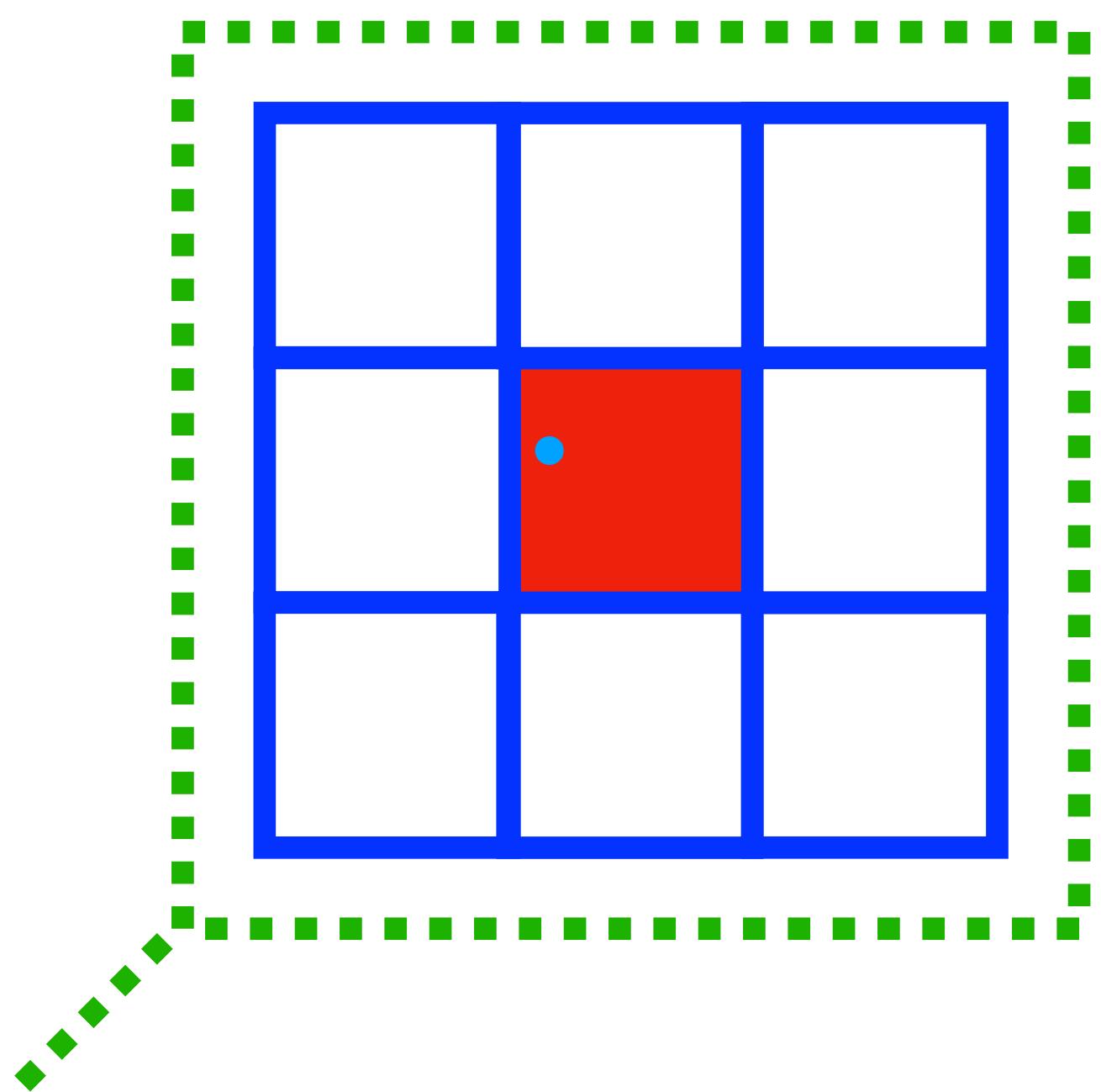
GPU memory



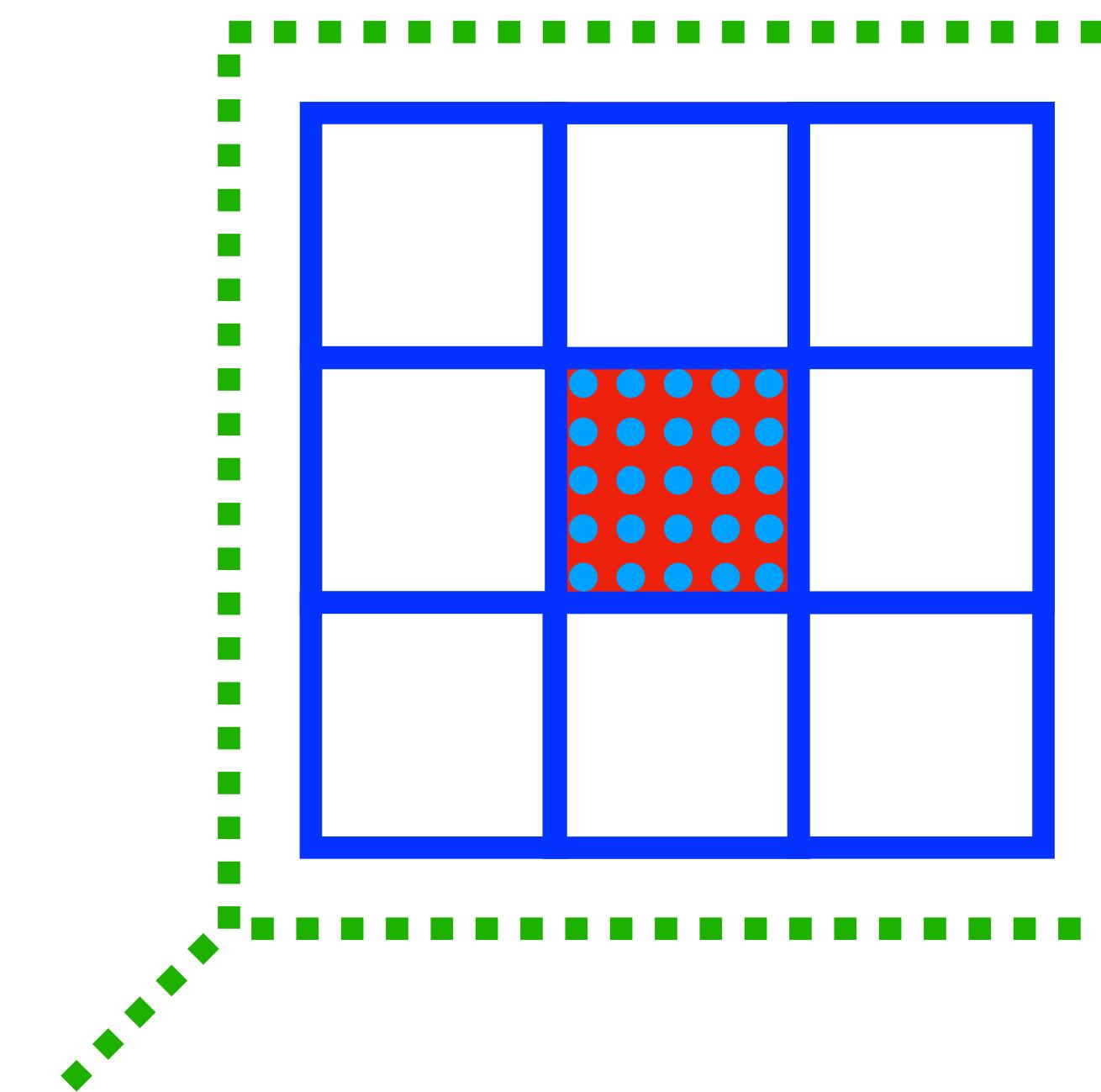
Sparsity - GSPGrid



Sparsity - GSPGrid

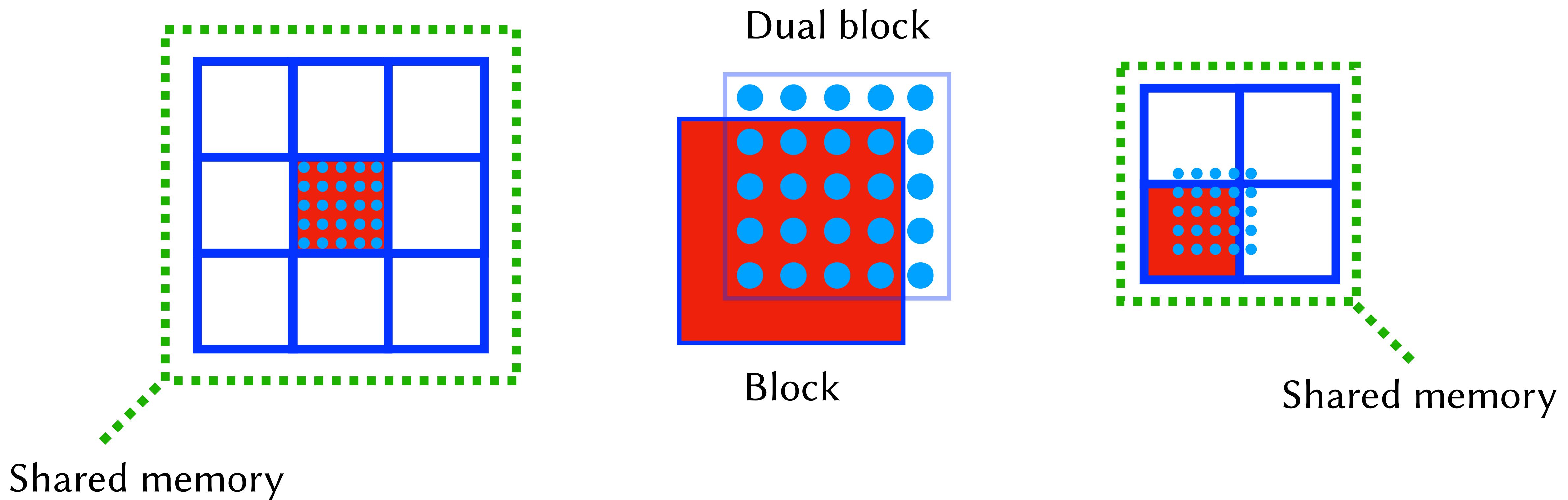


Shared memory

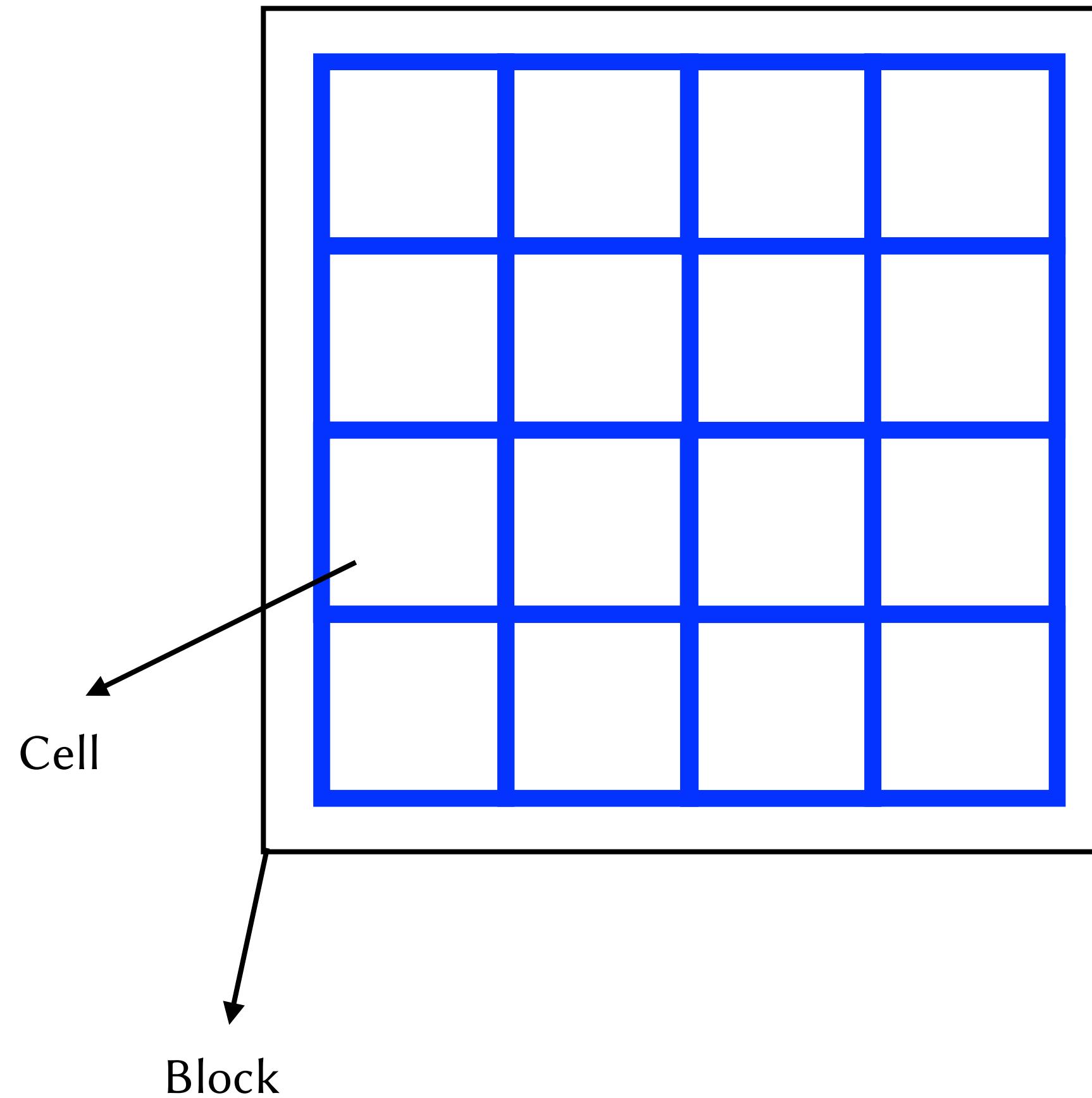


Shared memory

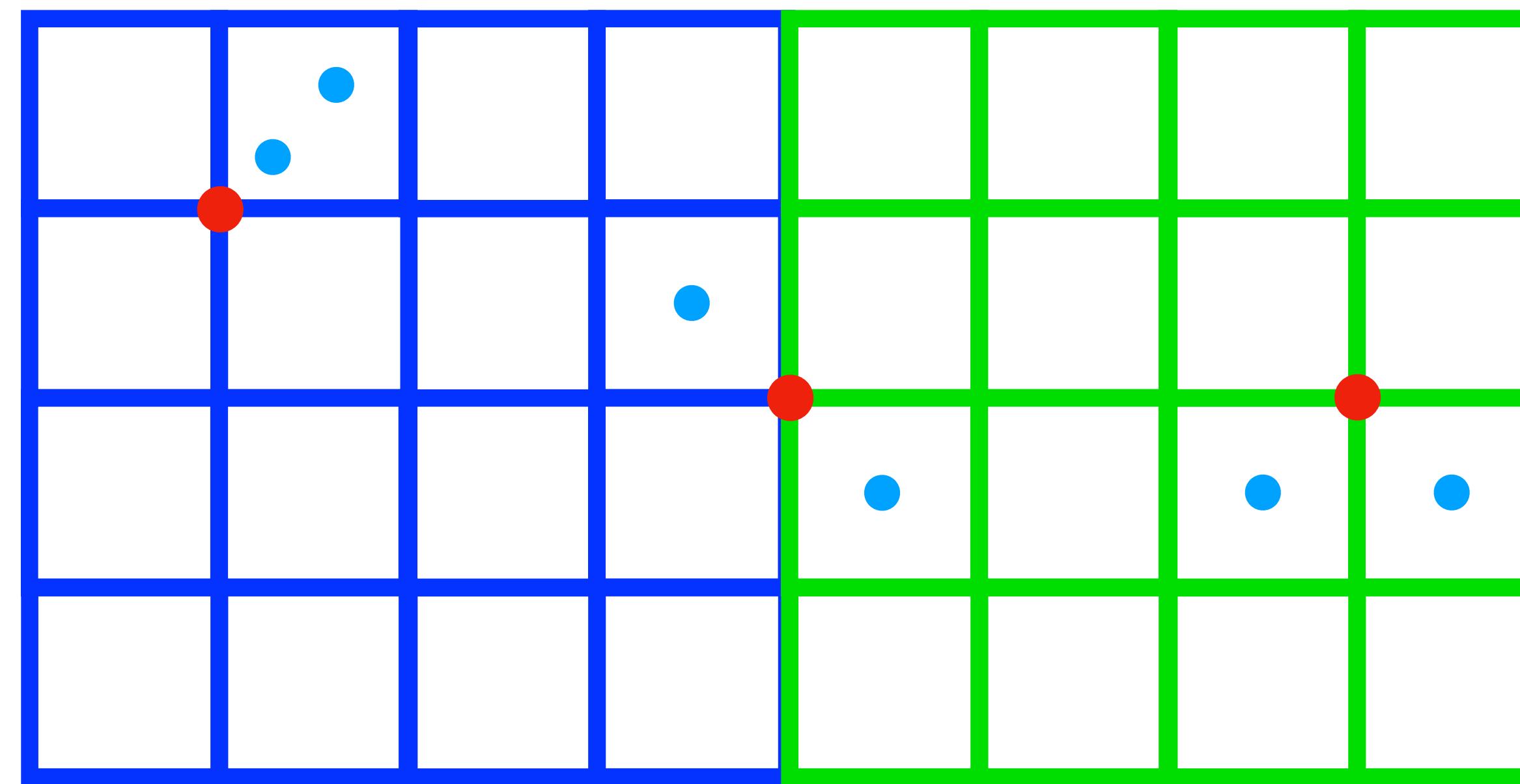
Sparsity - GSPGrid



Write hazards



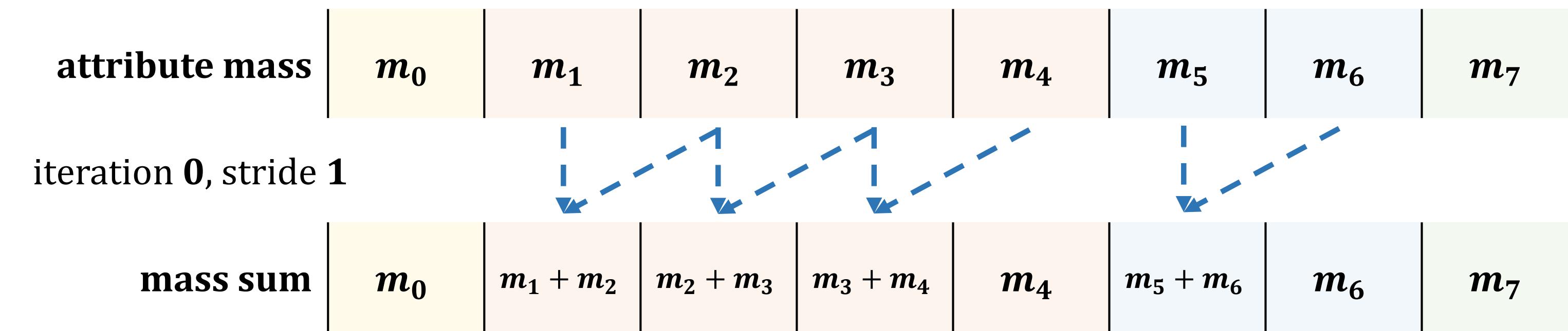
Write hazards



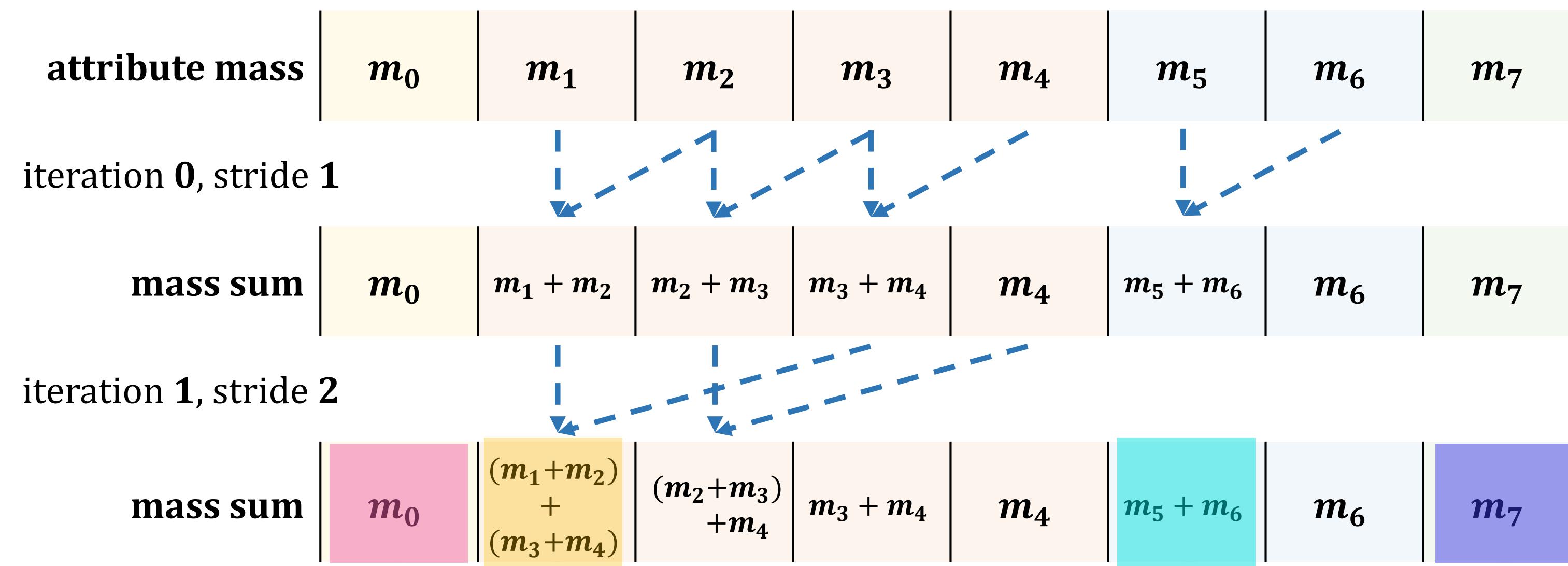
CUDA thread - ●

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node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3

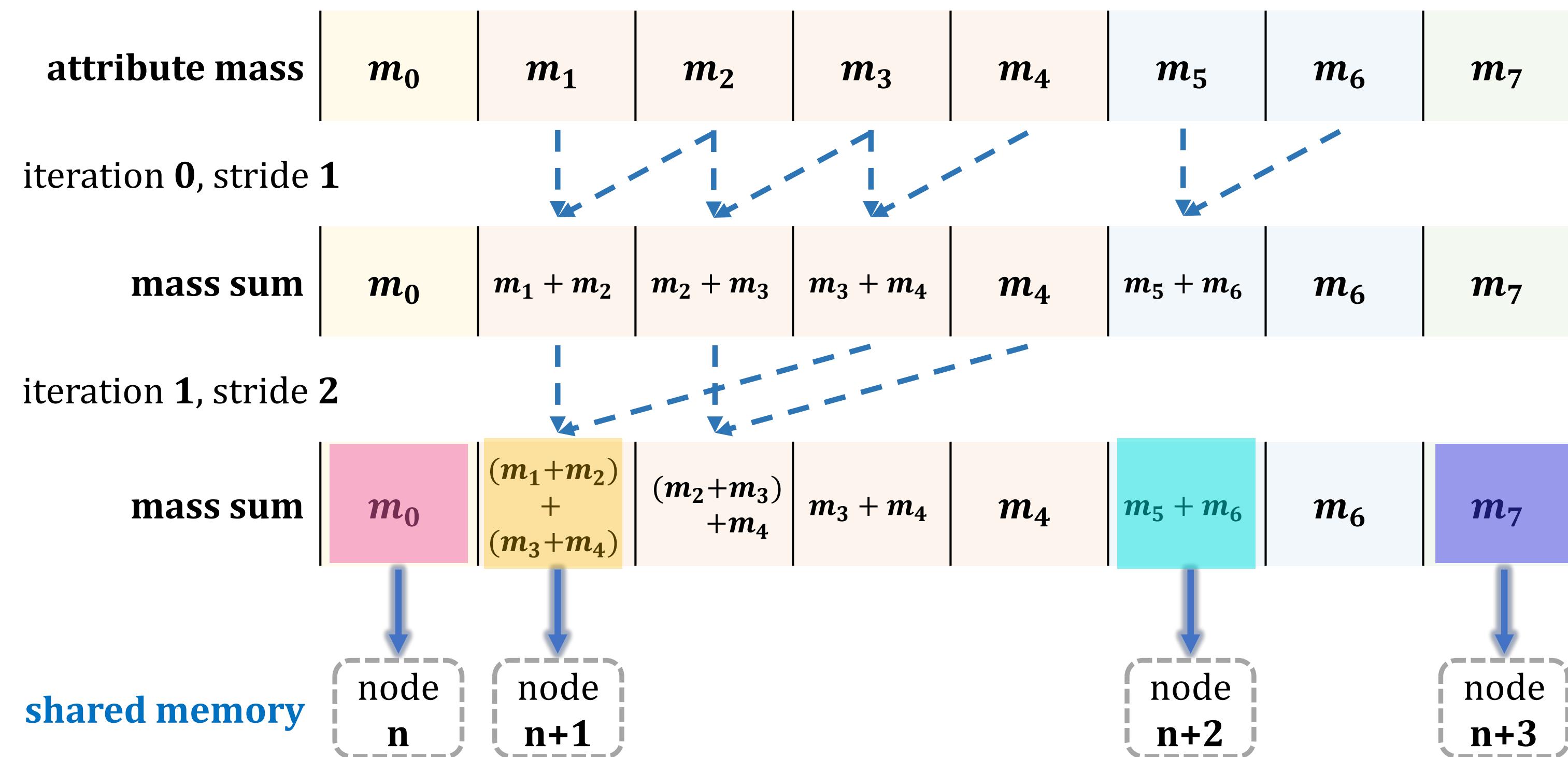
lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



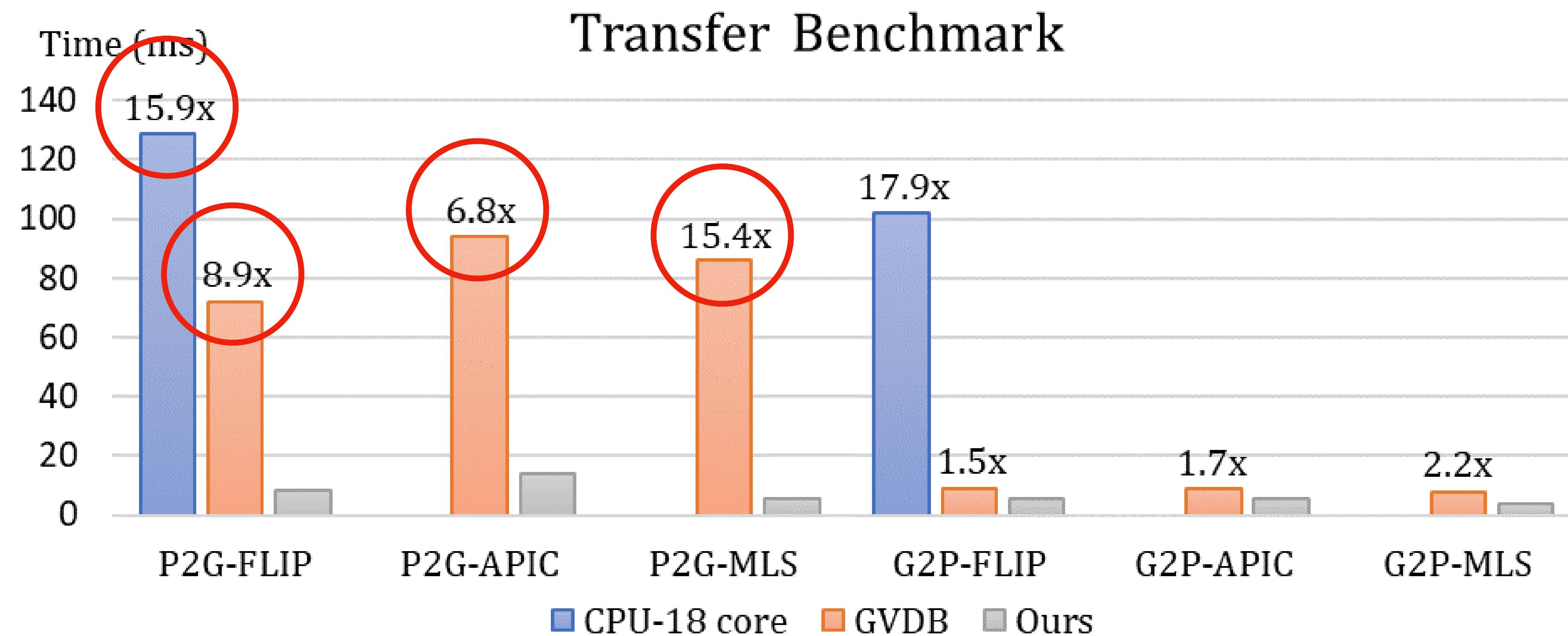
lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



Benchmark



Additional contributions

- Accelerated particle sorting
- Avoiding explicit particle reordering
- A new sand model for semi-implicit integration
- A MPM-based heat solver

Conclusion

SPGrid
GSPGrid



Conclusion

Breadth of simulation



Parallel efficiency

Price paid:

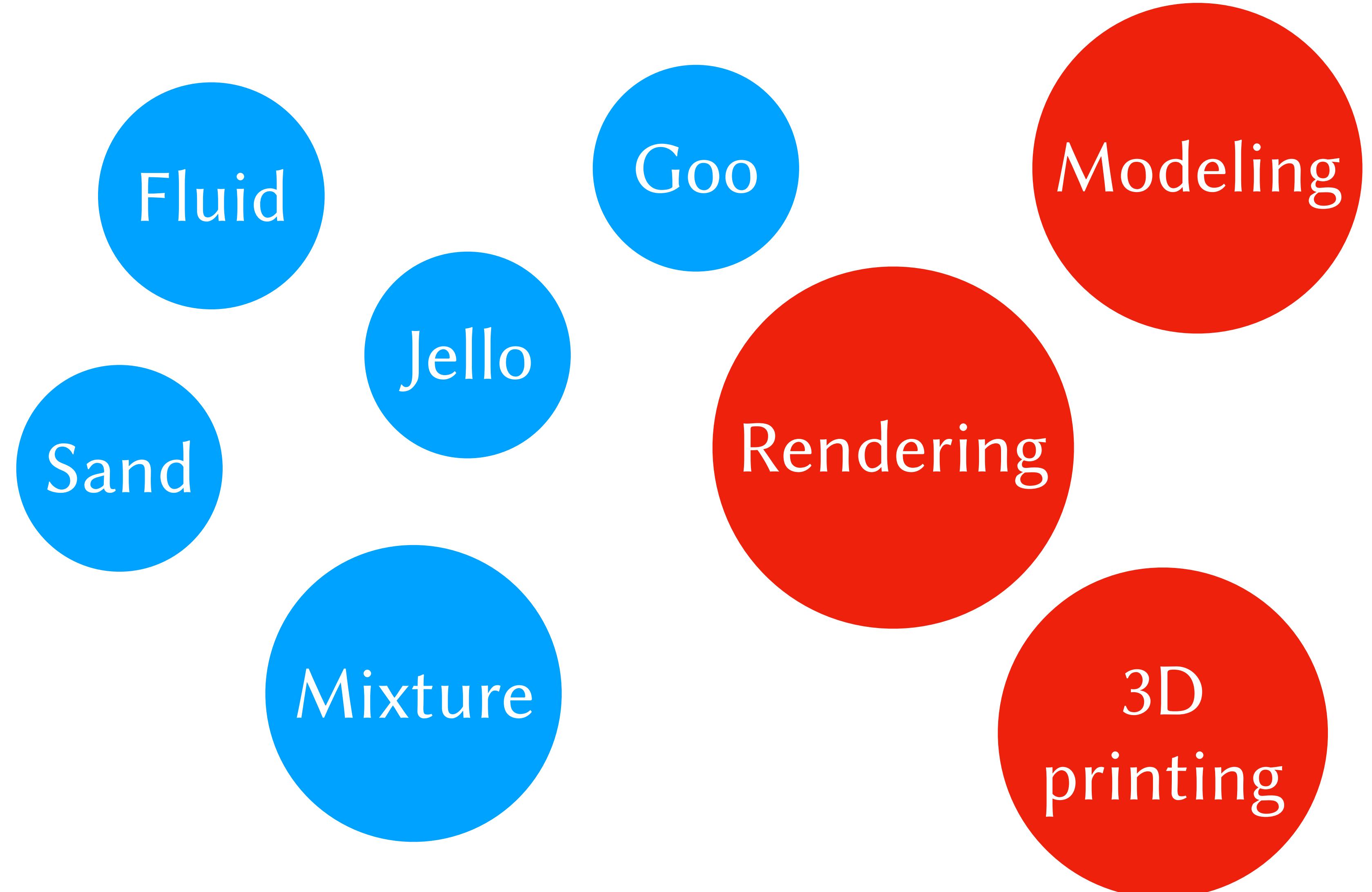
Platform-specific solutions

Optimizations far from automatic

Focus on **visual** appeal

Future work

SPGrid
GSPGrid



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- My advisor: Prof. Eftychios Sifakis
- Committee:
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- National Science Foundation for funding

