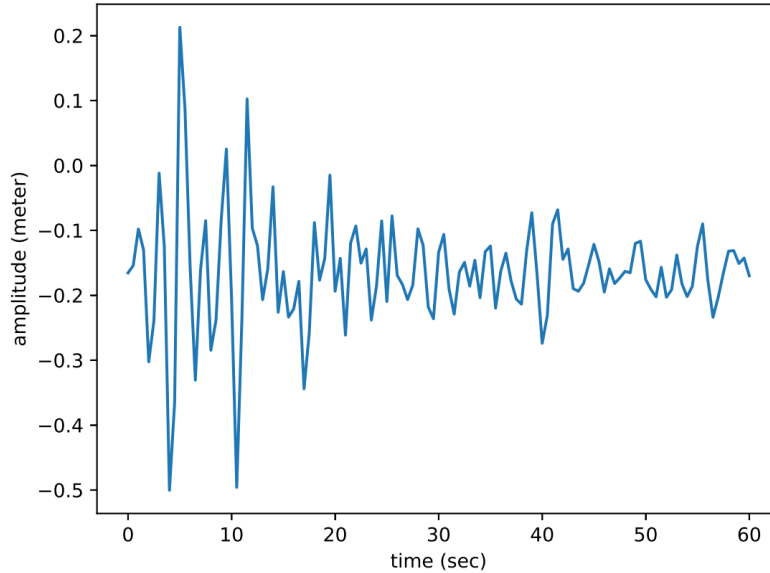


(100 points)

**Question:** In this homework, you will need to write a code to do Fourier transformation on a time-series data and filter the data within a range of period. The data is named “HW11.input.dat” under the homework folder. A plot of the data is shown below:



*You may notice that this is the same data for HW06 in which we practiced the method of interpolation:)*

### Review:

If  $f(x)$  is a function defined on  $[0, 2L]$ , and is represented by a list of equally spaced discrete data points of  $(x_i, f(x_i))$  for  $i = 1, 2, 3, \dots, np$ , where  $np$  is the number of data points,  $x_1 = 0$  is  $x$  value for the first data point,  $x_{np} = 2L$  is the  $x$  value for the last data points,  $\Delta x$  is the increment of  $x$  between every two neighboring data points, then  $f(x)$  can be represented by:

$$f(x) = a_0 + \sum_{n=1}^{\frac{np-1}{2}} \left[ a_n \cos\left(\frac{n\pi x}{L}\right) + b_n \sin\left(\frac{n\pi x}{L}\right) \right], \quad (1)$$

where,

$$a_0 = \frac{\Delta x}{2L} \sum_{i=1}^{np-1} f(x_i), \quad (2)$$

$$a_n = \frac{\Delta x}{L} \sum_{i=1}^{np-1} f(x_i) \cos\left(\frac{n\pi x_i}{L}\right), \quad (3)$$

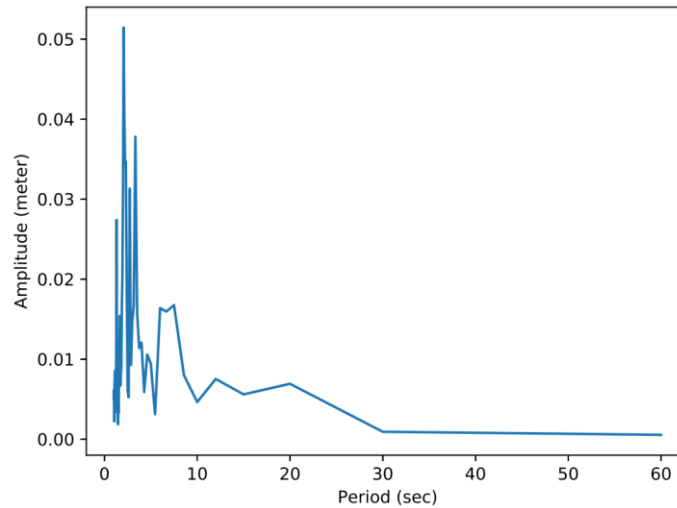
$$b_n = \frac{\Delta x}{L} \sum_{i=1}^{np-1} f(x_i) \sin\left(\frac{n\pi x_i}{L}\right), (4)$$

The amplitude at period of  $T_n = 2L/n$  is given by  $A_n = \sqrt{a_n^2 + b_n^2}$ , for  $n$  ranges from 1 to  $(np - 1)/2$ .

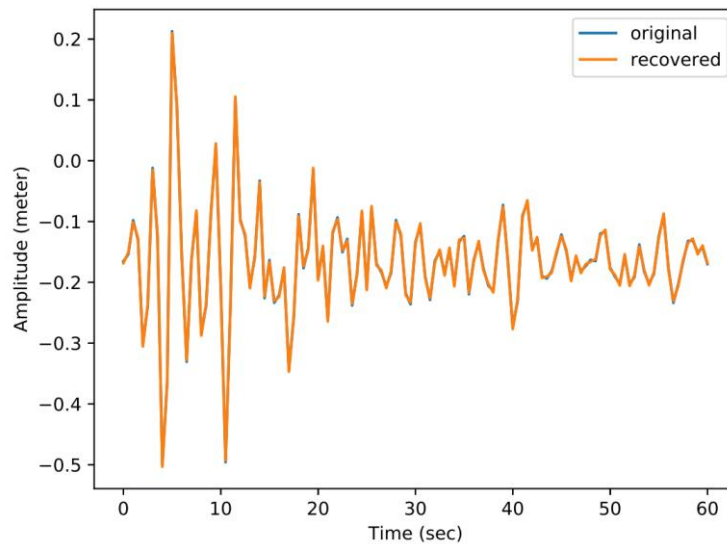
Because  $(np - 1)/2$  needs to be an integer, therefore,  $np$  needs to be an odd number. If  $np$  is an even number in the data, you need to reduce 1 last point of the data, by  $np = np - 1$ .

#### Requirements:

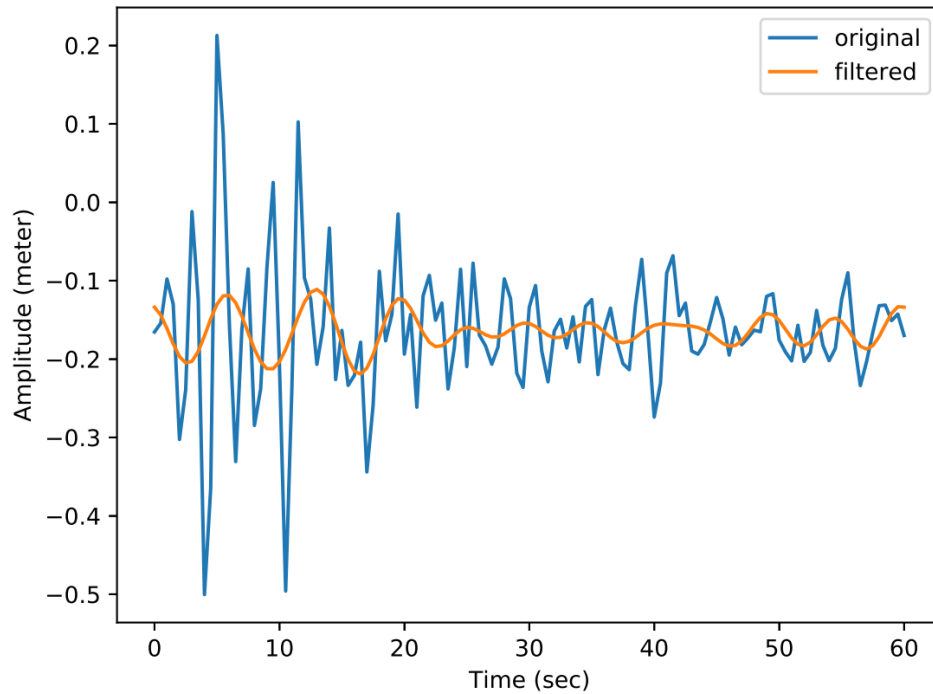
- You need to output the amplitude for the period in the range of [1.0, 60.0] into a file named "dft.dat", then make a plot of this file, same as below (or hw11-1.pdf):



- You need to output the  $x$  values (1<sup>st</sup> column), the observed  $y$  values (2<sup>nd</sup> column), and the approximated  $y$  values recovered by dft (3<sup>rd</sup> column) in a single file named "compare.dat", and then plot the 1<sup>st</sup> column vs the 2<sup>nd</sup> and the 3<sup>rd</sup> column. An example plot is shown below (or hw11-2.pdf):



- Filter the data in the period range of [5,10], save it in a file named “filter.dat”, and then plot the filtered data and the original data in the same plot. See an example below (or hw11-3.pdf):



- For your comparison, I have provided my output of dft.dat, compare.dat, and filter.dat in the homework folder.

### How to submit your homework

1. Change the name of your C code as 'FirstName-LastName-HW11.c'.
2. Send your code file to [Mingming.Li@asu.edu](mailto:Mingming.Li@asu.edu) and enter the email subject title as “Numerical Methods Homework 11”.