

## Assignment 3 reading

Sunday, September 24, 2017 8:23 PM

`Equal` → test two arguments, and returns true if they have the same Works on atoms & lists  
`(equal (t2 a) b))` → T Expression!

Eql → test two arguments, returns true if have same Values or Symbols

$(\text{eql } 4 \ 4.0) \rightarrow \text{NIL}$   
 $(\text{eql } 4 \ 4) \rightarrow T$

`Eq` → tests if two arguments share the same bunch of memory; therefore the same symbols

$$(\varepsilon_1 \ 4 \ 4) \text{ NIL} \quad (\varepsilon_1 \ 4 \ 4) \rightarrow T$$

`Member` → `True` if the first argument is a two-level element in the second list argument. Returns the rest of list w/ argument.

- any symbol beginning with a colon is said to be a Keyword. Keywords evaluate to themselves.
- any argument that follows a keyword is a Keyword Argument. Its purpose is to modify a function's basic behavior suggested by the argument.

#) → produces procedure objects from procedure names      → Old form      (Function Equal) ≡ #) Equal  
 defun → stores procedure descriptions as procedure objects under procedure names.      #) <expression> from (Function <expression>)

:Test indicates that the next argument specifies the test that function is to use

procedure name → Equal, defun, +

procedure object → the actual computer code that actually perform the work.

atom → test a single argument; return T if it is an atom

`numberp` → test a single argument; return `T` if it is a numeric atom

`symbolp` → test a single argument, return T if it a non numeric atom

`listp` → test a single argument, return T if it is a list

## Predicates

If → (if <test>  
      <then form>  
      <else form>  
    )

example: (set f day-or-date 'monday)  
(if (symbolp day-or-date)  
    'day  
    )date  
    )  
→ Day

```
← if <test>  
← then return  da  
← else return  dat
```

example. (setf high 98 temp 102)  
(when (> temp high)  
  (setf high temp)) ← side effects

- > New Record
- > high  
→ 102
- > 103

( Cond ( <test 1> <consequence 1> ... < )  
      ( <test 2> <consequence 2> ... < )  
          :  
      ( <test n> <consequence n> ... < ) ))

## Defun w/ Conditionals

```
(defun express-probability (p)
  (cond ((> p .75) 'very likely)
        ((> p .50) 'likely)
        ((> p .25) 'unlikely)
        (+ 'very unlikely))))
```

```

(define my-sum (l))
  (let ((x (sum (cdr l))))           ; Returns the sum over a list
    (x (sum (rest l)))               ; x = (sum (rest l)) // the sum of the rest of the list
    (+ (car l) x)))                 ; To return the actual answer we
                                    ; Add the first E to X

(define my-negative (l))
  (let ((x (neg-sums (cdr l))))     ; If (neg-sums (cdr l)) = 0
    (if (numberp (car l))            ; Then (car l) = x
        (cons (car l) x)
        x))

(define my-incr-tot-2 (l n))
  (let ((x (my-incr-tot-2 (cdr l) n)))
    (cons (car l) x)))

(define my-represent (l))
  (let ((x (insert n (cdr l))))     ; If (cdr l) = 0
    (if (lessp (car l) n)
        (append l (list n))
        (cons (car l) x)))

(define my-represent! (l))
  (let ((x (my-represent (cdr l))))  ; If (cdr l) = 0
    (list (append (list (car l)) (second x))
          (first x)))))

(define my-partition (l p))
  (let ((x (partition (cdr l) p)))
    (if (lessp (car l) p)
        (list (first x)
              (append (second x) (rest (car l)))))
        (list (append (first x) (rest (car l)))
              (second x)))))

(define neg-numbers (l))
  (cond ((empty? l) 0)
        ((lessp (car l) 0) (+ (first l) (sum (rest l))))           ; if the list is empty () = 0
        (else (neg-numbers (cdr l)))))                                ; if L = (3) then 3 + 0 = 0

(define inc-list-2 (l n))
  (cond ((empty? l) 0)
        ((lessp (car l) n) (inc-list-2 (cdr l) n)))                ; if L is empty return 0
        (else (cons (car l) (inc-list-2 (cdr l) n)))))             ; make a list of (first l) & (neg-num (rest l))

(define insert (n l))
  (cond ((empty? l) (cons n l))
        ((lessp (car l) n) (cons (car l) (insert n (cdr l)))))      ; if inserting N on l then (list n)
        (else (cons (car l) (insert n (cdr l)))))

(define insert! (n l))
  (cond ((empty? l) (list n))
        ((lessp (n (first l))) (make-a-list (first l) n))           ; make a list of (first l) and (insert n (rest l))
        (else (make-a-list (first l) n) (insert n (rest l)))))

(define split-list (l))
  (cond ((empty? l) '())
        (else (let ((x (split-list (cdr l)))))                      ; if L is empty ( ) /& make the split-lists
              (list (cons (car l) (second x)) (first x))))))

(define position (l p))
  (cond ((empty? l) '())
        ((lessp (car l) p) (list (cons (car l) (first x)) (second x))) ; if (first l) < p (list (cons (first l) (first x)) (second x))
        ((else (list (cons (car l) (first x)) (second x))
                    (list (car x) (cons n (second x)))))))           ; otherwise (first l) >= p (list (first x) (cons (first l) (second x)))

(define set-difference (l s))
  (cond ((empty? l) '())
        ((empty? s) '())
        ((equalp (car l) (car s)) (list (cons (car l) (rest l)) (rest s))))
        (else (cons (car l) (set-difference (rest l) (rest s))))))

(define set-union (s1 s2))
  (cond ((empty? s1) s2)
        ((empty? s2) s1)
        ((member (car s1) s2) (set-union (cdr s1) s2))
        (else (cons (car s1) (set-union (cdr s1) s2)))))

(define set-difference! (l s))
  (cond ((empty? l) '())
        ((empty? s) '())
        ((equalp (car l) (car s)) (cdr s)))
        (else (cons (car l) (set-difference! (rest l) (rest s))))))

(define Singlenes (e))
  (cond ((empty? e) '())
        ((member (car e) (cdr e)) (cons (car e) (cdr e)))
        ((set-difference (car e) (cons (car e) (cdr e)))))))
```

X = sum of rest of the list  
To return the actual answer we  
Add the first E to X

```

(define min-2 (l))
  (cond ((not (numberp (car l))) 'error)
        ((not (numberp (cadr l))) 'error)
        ((lessp (car l) (cadr l)) 'error)
        (else (list (car l) (cadr l)))))

(define safe-cdr ((x y))
  (if (and (numberp x) (numberp y))
      (/ (+ x y) 2)
      'error))

(define add-1!-million (x))
  (let ((x (integerp x))) (+ x 1000000) (add1 x)))

(define multiple-of-member ((x L))
  (if (and (atom x) (listp L))
      (member x (member x L))
      'error))

(define months-as-integer ((m))
  (cond ((equal m "January") 1)
        ((equal m "February") 2)
        ((equal m "March") 3)
        ((equal m "April") 4)
        ((equal m "May") 5)
        ((equal m "June") 6)
        ((equal m "July") 7)
        ((equal m "August") 8)
        ((equal m "September") 9)
        ((equal m "October") 10)
        ((equal m "November") 11)
        ((equal m "December") 12)
        (else 'error)))

(define score-grade ((s))
  (cond ((>= s 90) 'A)
        ((>= s 80) 'B)
        ((>= s 70) 'C)
        ((>= s 60) 'D)
        ((<= s 50) 'F)
        (else 'error)))

(define merge-2lists (x y))
  (cond ((and (numberp x) (numberp y)) (+ x y)))
        (else 'error))

(define remove-add-dupl (l))
  (cond ((null? l) '())
        ((not (null? (cdr l))) (if (equal? (car l) (cdr l)) (remove-add-dupl (cdr l)))
                                 (cons (car l) (remove-add-dupl (cdr l)))))))

(define merge-elts (l))
  (cond ((null? l) '())
        ((not (null? (cdr l))) (if (equal? (car l) (cdr l)) (cons (car l) (merge-elts (cdr l))))
                                 (cons (car l) (merge-elts (cdr l)))))))

(define unrepeat-elts (l))
  (cond ((null? l) '())
        ((not (null? (cdr l))) (if (not (equal? (car l) (cdr l))) (unrepeat-elts (cdr l)))
                                 (else (unrepeat-elts (cdr l)))))))

(define sub-elts ((y))
  (cond ((and (numberp x) (numberp y)) (not (zero? y)))
        (or (and (zero? x) (zero? y))
            (and (< x 0) (> y 0))
            (and (> x 0) (< y 0))))))

(define count-rep-cdr (l))
  (cond ((null? l) 0)
        ((not (null? (cdr l))) (if (not (equal? (car l) (cdr l))) (count-rep-cdr (cdr l)))
                                 (1+ (count-rep-cdr (cdr l)))))))

(define count-repetitions (l))
  (cond ((null? l) 0)
        ((not (null? (cdr l))) (if (not (equal? (car l) (rest l))) (count-repetitions (cdr l)))
                                 (1+ (count-repetitions (cdr l)))))))

(define count-subset (f))
  (cond ((null? f) 0)
        ((not (null? (cdr f))) (if (not (equal? (car f) (cdr f))) (count-subset (cdr f)))
                                 (1+ (count-subset (cdr f)))))))

(define our-some? (f))
  (cond ((null? f) #t)
        ((not (null? (cdr f))) (if (our-some? (cdr f)) #t
                                  (our-some? (cdr f))))))

(define our-every? (f))
  (cond ((null? f) #t)
        ((not (null? (cdr f))) (if (not (our-every? (cdr f))) #t
                                  (our-every? (cdr f))))))

(define our-some1 (p))
  (cond ((null? p) '())
        ((not (null? (cdr p))) (let ((p1 (partition1 (cdr p) (car p))))))
        (append (qsort1 p (car p)) (cons (car p) (qsort1 p (cdr p)))))))

(define our-every1 (p))
  (cond ((null? p) '())
        ((not (null? (cdr p))) (let ((p1 (partition1 (cdr p) (car p))))))
        (append (qsort1 p (car p)) (cons (car p) (qsort1 p (cdr p)))))))

(define foo (f))
  (cond ((null? f) '())
        ((not (null? (cdr f))) (let ((f1 (tr-mul (cdr f) (* (car f) res))))))
        (cons (cons (f1 (car f)) (cdr f)) (map (lambda (list) (cons (car list) (tr-mul (cdr list) (* (car list) (tr-mul (cdr list) (car list))))))) (cdr f (cdr f)))))))

(define tr-mul (l r))
  (cond ((null? l) r)
        ((not (null? (cdr l))) (let ((l1 (tr-mul (cdr l) r)))
        (tr-mul (car l) (* (car l) l1)))))

(define tr-fac (n))
  (cond ((zero? n) 1)
        ((not (zero? n)) (* (tr-fac (- n 1)) (tr-fac n)))))

(define slow-prime? (n))
  (cond ((not (primep n)) #t)
        ((not (primep (tr-fac n))) #t)
        ((not (primep (tr-fac (tr-fac n)))) #t)
        (else #f)))

(define transpose1 (m))
  (cond ((empty? m) '())
        ((not (empty? (cdr m))) (map list (map car m) (map (lambda (list) (cons (car list) (map cdr (cdr list)))) (cdr m))))))

(define transpose2 (m))
  (cond ((empty? m) '())
        ((not (empty? (cdr m))) (map list (map car m) (map (lambda (list) (cons (car list) (map cdr (cdr list)))) (cdr m))))))

(define transpose3 (m))
  (cond ((empty? m) '())
        ((not (empty? (cdr m))) (apply map list m))))
```



# Venus

Saturday, September 2, 2017 2:55 PM

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## Context free grammar

$F ::= \text{blank}$   
| tab  
| newline

$\langle F \rangle ::= \text{blank} \mid \text{tab} \mid \text{newline}$   
 $\langle T \rangle ::= \langle F \rangle \mid \langle T \rangle \langle F \rangle$

$T ::= T-T$   
| F



$\langle \text{Letters} \rangle ::= a \mid \dots \mid z \mid A \mid \dots \mid Z$

$\langle \text{Digits} \rangle ::= 1 \mid \dots \mid 9$

$\langle \text{Sequence} \rangle ::= \langle \text{Sequence} \rangle \langle \text{Sequence} \rangle$   
|  $\langle \text{Sequence} \rangle \langle \text{Letters} \rangle$   
|  $\langle \text{Sequence} \rangle \langle \text{Digits} \rangle$

$\langle \text{main} \rangle ::= \langle \text{Letters} \rangle \mid \langle \text{Letters} \rangle \langle \text{Sequence} \rangle$

8/28/17

Monday, August 28, 2017 3:21 PM

⑤

82817

```

addition (+ x y)
define function (defn (a))
sum constant MySum
  (myfunc (x))
    x
Java
  f(x,y) {
    return (f * y);
}
myfunc (x) (myfunc x)
variables in Lisp don't have a type

```

## int f (int x)

```

  {
    return mySum;
  }
  3

```

Programs in C++ & Java are usually written in an imperative style. Imperative programs are thought of as specifying a sequence of actions that tell the machine to perform. These actions frequently change the values stored in variables and components of data structures.

Functional programming is different. A functional program does not specify a sequence of actions, and never changes the values that are stored in variables and data structure components. Variables & data structures of a functional program are immutable. Once a variable is set, given a value, it will have that value for as long as it (the var) exists. Once a data structure has been created, its contents will never change.

A functional program consists of a set of functions, each of which returns a value without doing anything else - these are functions that have no side effects.

In particular:

- never do I/O
- never update values stored in data structure components
- never throw exceptions

To write a functional program:

- A functional program can be used by writing any expression that calls one or more of its functions. And/or also calls library functions (true, \*, ...).

- The value of the expression is the result.

- The body of a function in functional program usually consists of just one expression, whose value will be returned when the function is called.

In Java, the body of such a function can be written as follows:

```

  {
    return [an expression];
  }

```

## Ex: Factorial

We will write a function such that when passed an non-negative int argument, the function returns the factorial of its argument.

```

3! = 5 * 4 * 3 * 2 * 1 = 120
  !!
  0! = 1

```

$n! = n * (n-1)!$

Java

```

long factorial (int n)
  {
    return n == 0 ? 1 : n * factorial (n-1); // mutual expression
  }

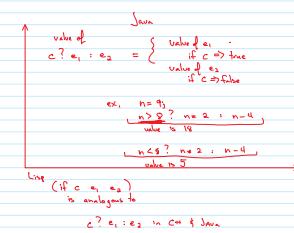
```

Lisp

```

(define factorial (n)
  (if (= n 0)
    1
    (* n (factorial (- n 1)))))

```



Recursion & conditional expressions are fine in using functional programs.

But iteration is not used:

(Note: Lisp does not force you to use functional style; the teacher does. Many Lisp programs use do use iteration (ch7))

## Lisp Assignment 1

1. ( $\star 30 (-7 2)$ )
2. a) ( $\star (+3 5) (\star 4 4)$ )
  - b) ( $\star (\star 3 17) (\star 4 4 19)$ )
  - c) ( $\star (- (+ (\star 12 12) (\star 11 11))) (+ (4 4 4) (10 10 10))$ )
3. a) ( $\sqrt{30} (-7 2)$ )
  - b) ( $\sqrt{300} (-70 3.0)$ )
4. ( $\star (/ (+ 93 93 95 91 97) \pi))$ )
- 5.
- 6.

a) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-4) (\star (0) (-13 0))))) (\star 2 1))$ )

b) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

c) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

d) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

e) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

f) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

g) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

h) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

i) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

j) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

k) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

l) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

m) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

n) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

o) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

p) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

q) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

r) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

s) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

t) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

u) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

v) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

w) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

x) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

y) ( $\star ((\star (-1 -1)) (\star (+ (-1) (-1)) (\star (-1) (\star (-13 0))))) (\star 2 1))$ )

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9/6/17

Thursday, September 7, 2017 10:00 AM

You will receive email from me tonight or tomorrow, it will be sent to your euclid account. H.W. 15-20 exercises on pg 36

Functional Programming:

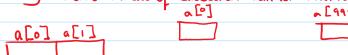
- ① Advantages of functional programming:
  - Since variables and data structures are immutable. The code is easier to understand, and reason about, and is quite likely to have fewer bugs.
  - ② Code is easier to test: You never have to worry that a variable or data structure will be changed in inappropriate ways.

In fact, Func prog typically consists mainly of functions that do not use non-local variables and data structures.

A function that has no side effects and does not use non-local variables is called a **pure function**. The value returned by a call to a pure function depends only on its argument values. So a pure function can be tested just by calling it with different arguments and verifying that the returned values are correct.

- ③ Code can be automatically parallelized. Different subexpressions can be evaluated in parallel

because code executing in one thread of execution cannot interfere with code in another thread



Lisp is a good language to use for functional programming. Lisp programs often make use of features in Lisp that are not used in functional programming - Such as assignment iteration, & functionality. However you should not make use of these features in this course.

Lisp was developed by McCarthy and coworkers at M.I.T in the late 1950s. It's the 2nd oldest high level programming language. 1st Fortran. For about 25 years until early 1980s Lisp was the dominant prog lang in A.I.

S-expressions

Expressions in Lisp are called S-expressions. There are two kinds:

- 1. Actions

- 2. Lists

The empty list () is both an atom & a list

Atoms include:

- a) Numbers i.e. 1, 2, 1/3, 3.5
- b) Symbols ..
- c) other kinds of atoms we won't see/use in this course

Numbers (numeric atoms) There are 4 kinds:

- 1) Integers
- 2) Ratios // 5/11 or 8/7
  - Lisp always prints ratios in lowest terms
  - An integer is equivalent to a ratio w/ denominator 1
- 3) Floating point numbers
  - short float
  - single float = the default 32 bits
  - double float
  - long float
- 4) Complex numbers # c(3 7) represents 3+7i

Symbols (symbolic atoms)

Ex: +7 = P0 G x23  
symbols are used

- as variable names (including parameter names)
- as function names
- as names of special forms and macros ↗ user-defined function
- as data

A variable is a symbol thought of as a name for a place to store a value

Evaluation of Atoms

Evaluation is defined as := computation for the value of

Evaluation of a Symbol:

returns whatever value the symbol may have as a variable

Evaluation of any other kind of atom returns that same atom

Lisp Assignment 2

Can an atom be a variable?

Yes, when a symbolic atom is given a value.

Can a number be a variable?

No, you cannot assign a value to numeric symbols

Can a list be a variable?

Can an atom have no value?

Yes NIL

Can an atom have more than 1 value at the same time

9/11/17

Monday, September 11, 2017 3:13 PM



Audio Recording...

Last Time:Lisp expressions are called S-expressions ( $S = \text{symbolic}$ )

S-expressions are used:

① As Lisp code (i.e. expressions that are to be evaluated by Lisp) Ex:  $(\text{sqrt} (+ (\text{factorial} 3) (+ 1 1))) = \sqrt{8}$ ② As Lisp data  $((\text{name} (\text{john smith})) (\text{job} (2005 + 1)))$ 

When an S-expression can be successfully evaluated, the resulting value is always a S-expression : Atoms

$\xrightarrow{\text{Symbol}}$  (ex. T, nil, x3, defun, factorial)  
 $\xrightarrow{\text{other kinds}}$  (ex. strings)  
 $\xrightarrow{\text{numbers}}$   
 $\xrightarrow{\text{not into first couple}}$

In  $(\text{defun} f (n))$   
 $(*)$  Symbol defun is a special form name  
 $(*)$  F is a function name  
 $(*)$  n is a variable (formal parameter) name

Lowercase letters in symbol names

when automatically converted to uppercase

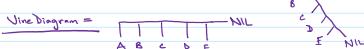
Evaluation of AtomsSymbols evaluate to whatever value they have as a variable constant. If a symbol has no value, then its evaluation produces an error.  
all other atoms evaluate to themselves

$$\begin{array}{ll} > 73.0 & > \frac{1}{3} \\ 73.0 & \frac{1}{3} \end{array}$$

Special symbols T & NIL are constants that evaluate to themselves  
 $\xrightarrow{T}$  is used to represent "true"  
 $\xrightarrow{\text{NIL}} \text{NIL} = ()$  is used to represent "false"  
 however any expression other than NIL is true

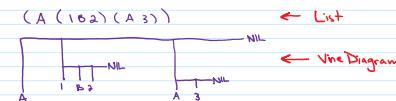
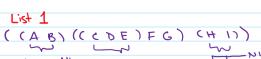
ListsA proper/true lists has the form:  $(E_1 E_2 \dots E_K)$  where each  $E_i$  is an S-expression. (Thus  $E_i$  may be an Atom or a List)  
 where K is the length of the list.  
 $()$  or NIL is the list of length 0

Side note: the construction of these lists are similar to Context-Free Grammars &amp; Regular Expressions

Vine Diagrams / Trees of ListsList =  $(a b c d e)$  vs.

Lists as Vine Diagrams  
 $(A B) = \overbrace{A \quad B}^{\text{NIL}} = \boxed{A \rightarrow B \rightarrow \boxed{\text{NIL}}}$   
 $(A) = \overbrace{A}^{\text{NIL}}$   
 $() = \text{NIL}$

Symbol in Lisp are unique in memory  
 These A's in the same code are the same.

Dotted List $(A B C \dots E)$   
is an ex. of a dotted list

Vine Diagram  $\neq$   $(A B C D E)$  NIL =  $(A B C D E \text{ - NIL})$  NIL =  $(A B \dots (C D E))$  NIL

Simplest form of Dotted List = Dotted Pair  
 $(A \dots B) \Rightarrow \boxed{A} \rightarrow \boxed{B}$

A dotted list has the form:  
 $(E_1 E_2 \dots E_K \dots a)$  where a is an atom other than NIL

Which S-expression can be evaluated

A list cannot be evaluated unless its first element is:  
 1) A symbol that is the name of a function (\*, + ...)  
 2) A symbol that is the name of a macro or special form  
 3) A lambda expression

Ex:	$(3 + 4)$	no	3 not symbol
	$((+ 3 4))$	no	$(+ 3 4)$ is not symbol
	$(3)$	no	
	$(+ 3 4)$	yes	3 numeric atom

In cases 1-3 how is the list evaluated

Case 1  $(F \text{ expr, expr, expr})$  → check values of arguments  
→ pass values to function as parametersif the first element of the list is a function name, then Lisp evaluates each other element of the list,  
and then calls the Function with the values of elements as arguments

Case 2 If the first element of the list is the name of a special form, then the way Lisp evaluates the list depends on the special form/macros

Case 3  $> ((\text{lambda} (n)) (+ n 3)) \rightarrow = 20$   
 $n \rightarrow n+3$ 

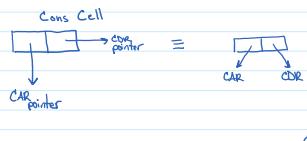
In this case the list is evaluated the same way as Case 1, except the function given by the lambda expression

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Wednesday, September 13, 2017 3:17 PM



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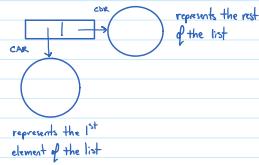


Any list is represented as a Cons cell connected to 2 other S-expressions



The CAR of a list is the first of the list  
CDR is the rest of the list (the remaining list after removing CAR)

These are built-in functions:  
 $\text{CAR}(\text{E}_1 \text{ E}_2 \text{ E}_3) \Rightarrow \text{E}_1$   
 $\text{CDR}(\text{E}_1 \text{ E}_2 \text{ E}_3) = \text{E}_2 \text{ E}_3$



### Quoting

$$(\text{CAR } (\text{E}_1 \text{ E}_2 \text{ E}_3)) = \text{E}_1$$

Quote: ' is Special Form  
 $(\text{Quote } [\text{S-exp}])$   
 $= \text{S-exp}$

$$' \neq '$$

Quote does not evaluate S-exp  
but returns the seen value of S-exp

### No Quoting

$$(\text{CAR } (\text{E}_1 \text{ E}_2 \text{ E}_3)) \equiv \text{CAR}(\text{E}_1 \text{ E}_2 \text{ E}_3) \rightarrow \text{usually an Error unless } \text{E}_1 \text{ is defined as a function name}$$

### Exercise:

How to write def / setf to correctly produce  
 $(\text{car } (\text{A } \text{B } \text{C } \text{D})) \Rightarrow \text{A}$

```
(defun a (x y z)
  x) // return x
  (setf b ' (a w)) // b= (a w)
  (setf c '789) // c=789 (car (A B C D)) => (car (A (B C D)))
  (setf d '81) // d=81 (car (B))
                                         (car (B)) // a (B) will return (B C D)
                                         (car (B)) // car (B) will return B
                                         (car (a w)) = a B will evaluate to
```

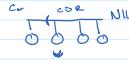
(car (A B C D)) in Lisp will eval to  
 $\rightarrow (\text{car } (\text{A }'(\text{B } \text{C } \text{D})))$   
 so A was set to a func w/ args BCD and B is the list (A w)  
 so car receives list (A w) then returns A

CAR = Content of the Address part of register

CDR = Contents of the Decrement part of register

### C...R functions

$$(\text{CADR } \text{L}) = (\text{car } (\text{car } \text{L})) = \text{second element}$$



$$(\text{CADDR } \text{L}) = (\text{car } (\text{cdr } (\text{cdr } \text{L}))) = \text{third element}$$

) An similarly for other sequences of up to 4 A's & D's between C & R

$$(\text{CADDR } \text{L}) = (\text{car } (\text{car } (\text{car } (\text{cdr } \text{L})))) = \text{fourth element}$$

) Use a tree diagram to better understand what is returned

$$(\text{CAAR } \text{L}) = (\text{car } (\text{car } (\text{car } (\text{cdr } \text{L})))) = \text{1st element of 1st element of L}$$

$$(\text{NTH } n \text{ L}) = \text{n}^{\text{th}} \text{ element of List}$$

### Cons, Append, List

Cons : takes two arguments

Append: take any # of arguments

List : take any # of arguments

) only one will be correct given the circumstance

$$(\text{Cons } x \text{ L}) = \begin{matrix} \text{Cons Cell} \\ \downarrow \quad \downarrow \\ \text{value of } x \quad \text{value of L} \end{matrix}$$

$$\begin{matrix} \text{Cons Cell} \\ \boxed{A} \leftarrow \quad \rightarrow \quad \boxed{B} \quad \boxed{C} \quad \boxed{D} \rightarrow \text{NIL} \end{matrix} \quad (\text{Cons } 'A ' (B C D)) = (A B C D)$$

$$>(\text{Cons } '((A) B (C D)) '((P Q) R S (T U))) \\ (((A) B (C D)) (P Q) R S (T U))$$

$$(\text{append } \underset{(A B)}{L_1} \underset{(C D)}{L_2} \dots \underset{(X Y Z)}{L_k}) \Rightarrow (A B C D \dots X Y Z)$$

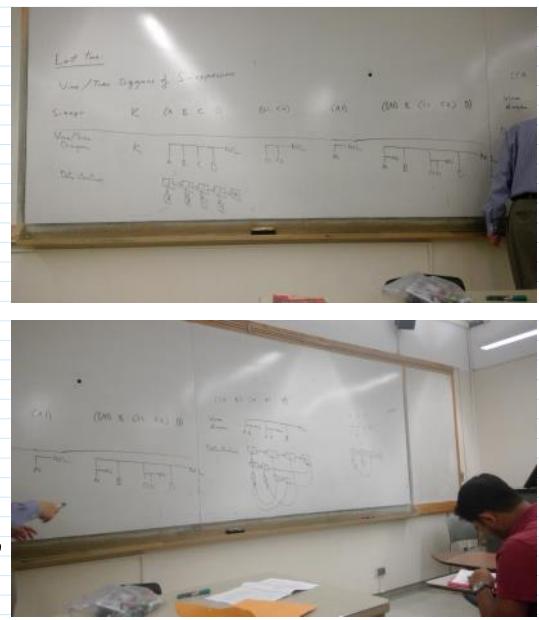
Append returns a New List obtained by concatenating the Lists passed as arguments to the function. Not changing those lists

$$w(\text{List } a_1 \text{ a}_2 \dots \text{ a}_k) \Rightarrow ((a_1)(a_2) \dots (a_k))$$

List of length k whose elements are the Values of the list

$$(\text{Append } '(1 2 3) ' (P Q R S)) \Rightarrow (1 2 3 P Q R S)$$

$$(\text{list } ' (1 2 3) ' (P Q R S)) = ((1 2 3) (P Q R S))$$





(if c x<sub>1</sub> x<sub>2</sub>) → c? e<sub>1</sub> e<sub>2</sub>

Ex: (define kind (e))  
(if (eq? e 0)  
(integer-is-0 e)  
(if (number? e)  
(list 'num e)  
(if (compx e)  
(list 'non-empty-list e)  
(list 'non-numeric-atom e) ))))

function name parameter list

```
( define kindofelement (e)
  (if (eq? e 0)
    (integer-is-0 e)
    (if (number? e)
      (list 'num e)
      (if (compx e)
        (list 'non-empty-list e)
        (list 'non-numeric-atom e) )))))
```



$(\text{or } e_1 \dots e_n)$  is analogous to  $(e_1 \text{||} \dots \text{||} e_n)$  in Java

$(\text{and } e_1 \dots e_n)$   $(e_1 \& \dots \& e_n)$

However, when the value of  $(\text{or } e_1 \dots e_n)$  is "true", then its value is the value of  $e_i$

when the value of  $(\text{and } e_1 \dots e_n)$  is "true", then its value is the value of  $e_n$

$(\text{or } (\text{member } 'A' : (B \text{ A } P))$

$(\text{member } 'B' : (B \text{ A } B))$

)  $\rightarrow (A \circ)$

$(\text{and } (\text{member } 'A' : (B \text{ A } P))$

$(\text{member } 'B' : (B \text{ A } P))$

)  $\rightarrow (B \text{ A } P)$





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10/4/17

Wednesday, October 4, 2017 3:05 PM

Audio recording started: 3:11 PM Wednesday, October 4, 2017

```
(defun list-length (L)
  (if (endp L)
      0
      (+ (* x (list-length (cdr L)))
         1)))
```

```
(defun list-length (L)
  (if (endp L)
      0
      (+ (+ (list-length (cdr L)) 1))))
```

w/c is used just once, there is no need for list so can change code to:

Another example: Well write a func factorial, such that:  $(\text{factorial } n) \Rightarrow n \times (n-1) \times \dots \times 1$   
 $(\text{factorial } 0) \Rightarrow 1$

```
(defun factorial (n)
  (if (zerop n)
      1
      (* (* x (factorial (- n 1))))
```

whenever n is a non-negative int  
 //be careful of the small cases

General Pattern:

Let  $(f e)$  be a function whose argument  $e$  is either a list, of a kind such that the  $(\text{car } e)$  is also a valid list or a non-negative integer, then you well may be able to write the func  $f$ , in such a way

→ list → number

```
(defun f (e)
  (if (endp e)
      (zerop e)
      ...))
  → expr ⇒ (f nil) or (f 0)

else → (let ((x ((f (car e))
                  (f (- e 1)))))

*)   *)
```

template

(\*) expression that compute  $(f e)$  from  $x$  and possibly  $e$

- Note 1) the (\*) expr may have more than one case!! → It may be a cond, or an if expr  
 2) If you see any case(s) where  $X$  does not need to be used (even if  $x$  actually is used), then move that/those cases out of the Let so as to avoid making unnecessary recursive calls (to compute  $x$ ) in those cases.  
 3) If there is no cases in which  $X$  is used more than once, then eliminate the Let, and substitute  $(f (\text{car } e))$  for each occurrence of  $X$

Write a function Evens such that if  $L \Rightarrow$  list of numbers then  $(\text{evens } L) \Rightarrow$  a list obtained from the list  $L$  by cutting out all odd elements

```
> (evens ()) ⇒ NIL
> (evens '(2 1 7 4 5 3 6 8)) ⇒ (2 4 6 8)
```

(\*) → expression that computes  $(\text{evens } L)$  from  $X$  and possibly  $L$

To write the (\*) expr, we'll try examples  
 → Suppose  $L = (2 1 7 4 3 6 8)$

→ the  $X \Rightarrow (4 6 8)$   
 next  $X$ -expr  $\Rightarrow (2 4 6 8)$

a good guess for this problem  $\Rightarrow (\text{cons } (\text{car } L) X) \rightarrow$  if first elem is even

lets try an example where  $(\text{car } L)$  is odd  
 → Suppose  $L = (3 4 0 1 6 5 2)$

$X \Rightarrow (4 6 2)$

\*-expr  $\Rightarrow (4 6 2)$

a good \*-expr is  $X$

```
(defun evens (L)
  (if (endp L)
      NIL
      et ((x (evens (cdr L)))))
```

(defun evens (L)
 (if (endp L)
 NIL
 et ((x (evens (cdr L)))))

(defun evens (L)
 (if (endp L)
 NIL
 et ((x (evens (cdr L)))
 (if (oddp (car L))
 X
 (cons (car L) X)))))

(defun evens (L)
 (if (endp L)
 NIL
 et ((if (oddp (car L))
 (even (car L))
 (cons (car L) (evens (cdr L)))))))

b/c  $X$  is only used once we can eliminate the Let

Write a Safe-Sum such that: if  $L \Rightarrow$  a list of numbers  
 then  $(\text{safe-sum } L) \Rightarrow$  the sum of list  $L$

if  $L \Rightarrow$  a list whose elements are not all numbers  
 then  $(\text{safe-sum } L) \Rightarrow$  error

```
> (safe-sum '(1 7 2 5 4)) ⇒ 19
> (safe-sum '(1 7 2 5 a)) ⇒ error
> (safe-sum ()) ⇒ 0
```

```
(defun safe-sum (L)
  (if (endp L)
      0
      (let ((x (safe-sum (cdr L))))
```

↗ expr that computes  
(safe-sum L)  
from x, possibly, L also

→ To write the ~~exp~~ well try examples  
 Suppose  $L = (1 \ 2 \ 5 \ 4)$   
 then  $x = (7 \ 2 \ 5 \ 4) = 18$   
 want ~~exp~~  $\Rightarrow 1 + (7 \ 2 \ 5 \ 4) = 19$   
 $\downarrow (+ (\text{car } L) \ x)$   
 ↳ this is good when  $x$  is not "error"  
 ↳ we also see that if  $(\text{car } L)$  is not a number or if  
 $x$  is not a number "error" is a good ~~exp~~

```

(defun safe-sum (L)
  (if (endp L)
      0
      (if (not (numberp (car L)))
          'error
          (let ((x (safe-sum (cdr L))))
            (if (eq x 'error)
                'error
                (+ (car L) x)))))))
    
```

### Functions of 2 or more arguments

In simple cases (such as  $\text{HtV}$  func with 2 args) just one of the arguments needs to change in the recursive calls

Pattern (assuming the 2nd arg will change in the recursive calls)

```

(defun f (e1 e2)
  ((if (zerop e2))
   (if (endp e2))
   expr that computes  
(f e1 0) or (f e1 nil)
   (let ((x (f e1 (- e2 1) )))
     expr that computes  
(f e1 e2)  
from x, and possibly,  
e1 or e2
     ))))
```

Ex: Write a function Prepend - 2 such that

$(\text{prepend-2 } L1 \ L2)$  returns the same result  
as  $(\text{append } L2 \ L1)$

```

(defun prepend-2 (L1 L2)
  (if (endp L2)
      L1
      (let ((x ((\text{prepend-2 } L1 (cdr L2)))))
        (cons (car L2) x)))))
```

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Simple Recursive Functions

```
(defun f (e)
  (if
    { (cadr e) }
    { (zeroe e) }
    → Some expression for ⇒ (f e) or (f nil) case
```

```
(let ((x (f { (cdr e)
                { (- e 1) }
                expr that computes
                (f e)
                from X and, possibly, e
              })))
```

→ If there are 2 or more Args, often just one, if them needs to change in the recursive call, and essentially the same pattern can be used

Single ArgumentMore Sophisticated Recursion

Sometimes we may want to produce a smaller argument for the recursive call in a different way than by using (cdr e) or (- e 1).

Common Alternatives include:

(caddr e)  
 (- e 2)  
 Split List could be written this way  
 Split them could be written this way

(floor e 2) =  $\lfloor \frac{e}{2} \rfloor = e \gg 1$  for int e in Java

= e/2 for ints e ≥ 0 in Java

Note if e ≤ 0, then  $\lfloor \frac{e}{2} \rfloor \neq e \% 2$  in Java b/c  $\lfloor \frac{-1}{2} \rfloor = -1$ ; So if e might be a -int then -1 needs to be dealt w/ as base case if we use (floor e 2) to produce a smaller Arg

• (cadr e), where e1 is a suitable transformation of e

Patterns:

```
(defun f (e)
  (if
    { e is a base case }
    ...
    (let ((x (f (smaller-version -of e)))))
```

General Case

expr that computes  
 from X and, possibly, e

• If you see cases which X need not be used in the \*-expr then move those cases out of the Let avoid making unnecessary recursive call

• If there is no case in which X is used more than once then you can eliminate the Let

- Make sure your base case code deals w/ all cases in which the general case could not work (see BCL-BCL3 checks in assignment 5)

```
(defun split-list (l)
  [base case code]
  (let ((x (split-list (cddr l))))
```

expr that computes  
 (split-list e)  
 from X and/or e

To write the \*-expr lets try an example

the list e = (A B C D E F G)

we want our X = ((CEG) (DF))

This way the \*-expr = ((A E G) (B D F))

An expression that can produce the \*-expr looks like:

\* (list (cons (car e) (car X)) (cons (cadr e) (cadr X)))  
 (list (cons (first e) (first X)) (cons (second e) (second X)))

To determine the base case from the general case, when will this code not work

when e = (A)

then X = (nil nil)

\* ⇒ ((A) nil); but the above \* will produce ((A) (nil)) = wrong!

So far this case, (list e nil) ⇒ ((A) nil) = Right

Since X is not used in this case, this can move out the Let, and be a base case, also

when e = () = a base case since (cddr e) = e

↳ In this case (split-list e) should give ⇒ (nil nil). And (list e nil) works again

The predicate (endp (cdr e)) (endp (rest e)) can be used to test whether e = a list of length  $\leq 1$

(defun split-list (l)

```
(if (endp (rest e))
  (list e nil)
  (let ((x (split-list (cddr l))))
    (list (cons (first e) (first X))
          (cons (second e) (second X)))))
```

↳ create split-nums using an exercise  
 (- e 2)

Example: Write a function power such that:  $y \Rightarrow$  a number &  $n \Rightarrow$  positive integer then  $(\text{power } y n) \Rightarrow y^n$

The idea is  $y^n = (y^{\lfloor \frac{n}{2} \rfloor})^2$  if n is even

$y^n = (y^{\lfloor \frac{n}{2} \rfloor})^2$  if n is odd

$n=1$  is a base case  
 $n=0$  is not a valid arg  $\lfloor \frac{n}{2} \rfloor = 0$ , which will make a valid arg val for us.

(defun power (y n)

(if (= n 1)

```
(let ((x (power y (floor n 2)))))
  (if (evenp n)
    (* x x)
    (* x x y))))
```

Depth of recursion = (no. of bits in the binary representation of n) - 1

SSort is HW#5

(ssort L)  $\Rightarrow$  a list of the numbers in L in ascending order  
(ssort '( 5 4 4 1 6 6 1 2 5 6 6 2 ))  
 $\rightarrow$  ( 1 1 2 2 4 4 5 5 6 6 6 )

(Min-First '( 5 4 4 1 6 6 1 2 5 6 6 2 ))  
 $\rightarrow$  ( 1 5 4 4 1 6 6 1 2 5 6 6 2 )  
  \underbrace{   }\_{e1}

Compute from ssort (cdr e1) where e1 = min-first

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Last time:

Alternative ways of producing a smaller argument for a recursive call:

- $(\text{cddr } e) = (\text{rest } (\text{rest } e))$

- $(-e 2)$

- $(\text{floor } e 2) = \lfloor \frac{e}{2} \rfloor$  This can be used for when  $e$  is an Exponent being reduced

- $(\text{cdr } el)$  where  $el$  is a suitably transformed version of  $e$

$(\text{ssort } L) \Rightarrow$  a list where elements are those of  $L$ , in non-decreasing order

$(\text{ssort } L)$  can be computed from  $(\text{ssort } L_1)$  where  $L_1 = (\text{min-first } L)$

$\hookrightarrow L$  has the first occurrence of its least element in the front

$L = (4 4 1 6 6 1 8 2 5 6 6 2 7)$

$L_1 = (\underline{1} \underline{4} \underline{4} \underline{6} \underline{6} \underline{1} \underline{8} \underline{2} \underline{5} \underline{6} \underline{6} \underline{2} \underline{7})$

core  $L$

Sometimes it is appropriate to change more than one argument for a recursive call

Example: Index from HW 5

Another Example: Write a function Power such that if  $y = \text{a number}$  &  $n = \text{positive int}$  then  $(\text{power } y n) = y^n$

Method 1  $y^n = (y^{\lfloor \frac{n}{2} \rfloor})^2$  if  $n$  is even &  $y^n = (y^{\lfloor \frac{n}{2} \rfloor})^2 y$  if  $n$  is odd

Base Case

$n=1 \Rightarrow y^n = y$

$(\text{let } (\times (\text{power } y (\text{floor } n 2)))$   
 $(\text{if } (\text{evenp } n))$   
 $(\ast x x)$   
 $(\ast x x y)))$

Method 2  $y^n = (y^2)^{\lfloor \frac{n}{2} \rfloor}$  if  $n$  is even &  $y^n = (y^2)^{\lfloor \frac{n}{2} \rfloor} y$  if  $n$  is odd

base case  $y^n = y$

$(\text{defun power } (y n))$   
 $(\text{if } (= n 1))$

$\hookrightarrow$   
 $(\text{let } ((\times (\text{power } (\ast y y) (\text{floor } n 2))))$   
 $(\text{if } (\text{evenp } n))$   
 $(\ast x x))$

$(\text{defun power } (y n))$   
 $(\text{if } (= n 1))$

$y$   
 $(\text{power } (\ast y y) (/ n 2))$   
 $(\ast (\text{power } (\ast y y) (\text{floor } n 2)) y)))$

$y^n = y^{n-1} y$  is another recursive strategy, but the recursive depth would be high whereas the depth of the  $\lfloor \frac{n}{2} \rfloor = n \gg 1$   
strategy is  $(\text{number of bits in } n) - 1$

Sometimes it is appropriate to use different recursive call for different argument values

Ex: Merge-List in Assignment 5

$(\text{merge-list } L_1 L_2) \Rightarrow$  a single list whose elements are those of  $L_1$  and  $L_2$  in non-decreasing order

$L_1 = (1 1 2 2 3 3 4 8 10 11)$

$L_2 = (5 6 4 6 9 10 10 10)$

$(\text{merge-list } L_1 L_2)$

$\Rightarrow (1 1 2 2 3 3 4 5 5 6 6 6 8 9 10 10 10 10 11)$

$(\text{merge-list } L_1 L_2)$  may be computed from

$\begin{cases} 1^{\text{st}} & (\text{merge-list } (\text{cdr } L_1) L_2) \\ 2^{\text{nd}} & (\text{merge-list } L_1 (\text{car } L_2)) \end{cases}$



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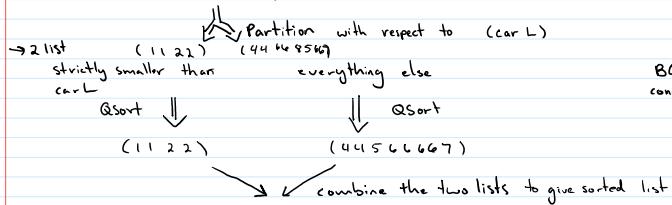
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QSort example of double recursion

L = (4 4 1 6 6 1 8 2 5 6 6 2 7)



BC-3 is a recursion condition  
(f x)  
(f (smaller x))

Warning:

It is possible the first list used by partition will be empty, and the second list hold all the elements (example of a BC-3 case). //In this case you will continue to call QSort on a list equal to the first list. Because the argument for the recursive call is not smaller than the original list, so we must treat this possibility as a base case of the above recursive strategy.

→ an alternative approach is to use the (partition (cdr L)) with respect to (car L) → This avoids the BC-3 case above.) You would of course have to put the car of L into the result list.

Errors

BC-1  
BC-2

### Functions that take functions as arguments

like QSort1 in Assignment 5

Sigma Notation  $\sum_{j=2}^7 f(j) = f(2) + f(3) + f(4) + f(5) + f(6) + f(7)$ How can we write a func Sigma such that: ( $\text{Sigma } #'f \ 2 \ 7 \Rightarrow \sum_{j=2}^7 f(j)$ )

if f is the name of a function that takes 1 numerical argument

$$\begin{aligned} (\text{defun } f (n) (* n 3)) \\ (\text{sigma } #'f \ 2 \ 7) = \sum_{j=2}^7 f(j) = 3 \cdot 2 + 3 \cdot 3 + 3 \cdot 4 + 3 \cdot 5 + 3 \cdot 6 + 3 \cdot 7 \\ = 81 \end{aligned}$$

Why the #' ??

In Lisp (as well as Java) the value of a symbol (as a variable) is a different property of that symbol from its function definition.

P may have both a value and a function definition  
or a value but no function definition  
or no value but have a function definition  
or neither

Java  
 $p + 3$ Lisp  
 $(\lambda p \dots)$ uses value of p  
uses function definition of p( $\text{Sigma } f \ 2 \ 7$ ) would use the value of f not the function definition $\#f = (\text{function } f) \Rightarrow$  function definition of f → similar to →  $'f = (\text{Quote } f)$ to set the value of a symbol is setf, or ( $\text{defun } f (n) (+ n 3)$ ) and running ( $f 19$ ) now  $n=19$   
defun sets the function definition of a symbol(defun f (n) (+ n 3))

(setf f 9)

f run  
( $\text{Sigma } f \ 2 \ 7$ ) → you will get an Error because 9 is not a function and so for the 1<sup>st</sup> parameter of SigmaExample:

(setf f #'sqrt)

(defun f (n) (+ n 3))

so ( $\text{Sigma } f \ 2 \ 7 \Rightarrow \sqrt{2} + \sqrt{3} + \sqrt{4} + \sqrt{5} + \sqrt{6} + \sqrt{7}$

(defun f (n) (+ n 3))

so ( $\Sigma f \ 2 \ 7 \Rightarrow \sqrt{2} + \sqrt{3} + \sqrt{4} + \sqrt{5} + \sqrt{6} + \sqrt{7}$ )

( $\Sigma \#f \ 2 \ 7 \Rightarrow 3 \cdot 2 + 3 \cdot 3 + 3 \cdot 4 + 3 \cdot 5 + 3 \cdot 6 + 3 \cdot 7$ )

Example:

Rule:

(defun g (x) (+ x 5))  
(setf g #'(lambda (x) (+ x 5)))

→ If a symbol p is the first element of a list, then the function definition of p is used by Lisp when evaluating that list.

→ If it is not the first element, then the value of p will be used

> (g 3) → 8  
↓  
3

FunCall

(Funcall f e<sub>1</sub> ... e<sub>n</sub>)

call the function given by the value of f, then passes elements e<sub>1</sub>, ..., e<sub>n</sub> as arguments to f

Example:

(defun g (\* x y z) (\* x y z))  
(setf g #'\*)

Note: In Scheme, function definition is just a special case of "value"

(g 2 3 4) ⇒ 2 · 3 · 4 = 24

(funcall g 2 3 4) ⇒ 2 + 3 + 4 = 9

(funcall #'g 2 3 4) ⇒ 2 · 3 · 4 = 24

How can we write Sigma

<sup>supposed to return</sup>  
<sub>↓ base case ↓</sub>  
<sub>↑ recursive general part ↑</sub>  
(defun sigma (f m n) ⇒ f(m) + f(m+1) + f(m+2) ... f(n)  
(if (> m n) 0  
else  
(let ((x (sigma f (+ m 1) n)))  
(+ (funcall f m) x)))

Mapcar ↗ Built-in function

(defun f (x) (\* x 7))

→ (mapcar #'f '(0 1 0 2 3 -1 6)) → returns a list with the function definition applied to every element  
<sub>↑ (funcall f 0)</sub>  
=⇒ (0 7 0 14 27 -7 42)

→ (mapcar #'car '((A B C) (D E) ((F G) H I) J))  
=⇒ ( A D (F G) J )

→ (mapcar #'cdr '((A B C) (D E) ((F G) H I) J))  
=⇒ ( (B C) (E) (I J) )  
( funcall g '(A B C))

Our Own Version of mapcar

(defun our-mapcar (g l)  
(if (endp l)  
nil  
else  
(let ((x (our-mapcar g (cdr l))))  
(cons (funcall g (car l)) x))))

the built-in mapcar is more powerful.  
It can map functions of 2 or more args

Built-in Map Car  
→ (mapcar #'1+ '(1 0 1 2 2))  
=⇒ (2 1 0 3)  
→ (mapcar #'1+ '(7 1 2 1 0))  
=⇒ (11 3 9 5 10)  
→ (mapcar #'1+ '(1 1 6 1 5))  
=⇒ (11 3 9 5 10)  
→ (mapcar #'1+ '(4 5 6 7 8))  
=⇒ (11 12 13 14 15)  
→ (mapcar #'1+ '(1 2 3 4))  
=⇒ (A 12) (B 34) ((67) X Y) (D (34) W))



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Very Important !! Do the reading and Exercise you were asked to do.

Last Time : Spoke on Tokens e.g. Identifier,  $>=$ ,  $,$ ,  $+$ ,  $,$ , unsigned-int-literal  
 Instance includes:  
 apple,  $x = 3$   
 1 instance each

Multiple Instances :

An instance of a sequence of tokens  $T_1, \dots, T_n$  is a piece of text that the compiler or interpreter should decompose into a sequence of tokens  $T_1, \dots, T_n$ .

Identifier  $\geq$  unsigned-int-literal  
 $x \geq 23$   
 $\frac{x}{x}$

Next, we will define the concept of a syntactically valid X where X is a programming language construct such as: "Java while statement" or "C++ compilation unit".

$x = y [17] / 34 ;$  possibly legal  
 $a = a[17] / 0 ;$  illegal, but syntactically valid // b/c the correct tokens line up correctly, in proper place

To do this we first define the concept of a syntactically valid sequence of tokens. The language designer is responsible for formulating a definition this concept such that:

- A sequence of tokens  $T_1, \dots, T_n$  is syntactically valid if (and roughly speaking, only if) some instance  $T_1, \dots, T_n$  is a possibly legal X  
 \* possibly legal = legal in an appropriate arrangement

 $x = y [17] / 34 ;$ 

Identifier = Identifier [unsigned-int-literal] / unsigned-int-literal ; ← A syntactically valid sequence of tokens for a Java assignment statement

→ Any instance of a syntactically valid sequence of tokens is then called a syntactically valid X.

An important part of the compiler/interpreter is to verify if the source program is syntactically correct // The first phase of code checkingFor most programming languages the only tokens that have more than one instance are Identifier & literals of various types e.g. unsigned-int-literal  
 unsigned-double-literal  
 charstring-literal

When X is a construct of such a language, we have that: A piece of text is syntactically valid X if (and roughly only if) it can be obtained from a possibly legal X by making zero or more changes of the following kinds:

1. Replace an occurrence of identifier with another instance of Identifier
2. Replace an occurrence of a literal with another literal of the same type.

## Syntax & Semantics of Expressions

Expressions can be written in many notations.

Let us consider the Java expression:  $f(g(h(1,2), f(3,4)), 5)$ 

we can write this:  $\underbrace{((1 \ h \ 2) \ g \ (3 \ f \ 4)) \ f \ 5}$

① Infix notation : each binary operator is written between its operands

② In an Infix notation with precedence classes, in which  $f$  &  $g$  have equal precedence and  $h$  has a higher precedence than  $f$  &  $g$ , and the precedence classes are left-associative $\underbrace{1 \ h \ 2} \ g \ (3 \ f \ 4) \ f \ 5$ if  $f = +, g = -, h = *$   $\Rightarrow 1 * 2 - (3 + 4) + 5$  vs.  $(1 * 2) - (3 + 4) + 5$ 

③ In Lisp Notation

 $(f \ g \ (h \ 1 \ 2) \ (f \ 3 \ 4), 5)$ 

④ Prefix-Notation [= Lisp Notation without parentheses]

 $f \ g \ h \ 1 \ 2 \ f \ 3 \ 4 \ 5$  // this is bad if you know the arity of each function

⑤ In "anti-Lisp" notation, which is like Lisp notation except function name is written after its arguments

 $(+ 3 4 5) \rightarrow Add = (3 4 5)$  $(F(g(h(1,2)(f(3,4)), 5)) \rightarrow (((1,2)H)(3,4)F)g)5 F$ 

⑥ Post-fix (also called RPN = Reverse Polish Notation) or (Anti-Lisp notation w/o parenthesis)

 $((1,2)H)(3,4)F)g)5 F \rightarrow 1 1 2 H 3 4 F G 5 F$ 

## Infix Notation:

What is a Syntactically Valid infix notation expression (SVID)  
 can be defined as follows  
 $e$  is an SVID if

- ①  $e$  is an instance of a Identifier
- ②  $e$  is  $(e_1)$  where  $e_1$  is a SVID
- ③  $e$  is  $e_1 op e_2$  where "op" is a binary operator and each  $e_1$  &  $e_2$  are SVID
- ④  $e$  is  $'op' e_1$  where "op" is a prefix unary operator &  $e_1$  is an SVID
- ⑤  $e$  is  $e_1 'op'$  where "op" is a postfix unary operator &  $e_1$  is an SVID

As you can see from 1-5 only operators of arity  $> 2$  are not allowed in Infix Notation  
 Moreover each unary operator needs to be classified as a prefix operator or a postfix

## Warning:

In many cases, more than one of 3-5 applies to an SVID

and 3 may apply in more than one way as in:

 $a - b * c + d$ 

possible choices of "op" for rule 3

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Monday, October 30, 2017 3:04 PM

Last Time: An SUIE (Syntactically invalid Infix Expression) is an expr of the following forms:

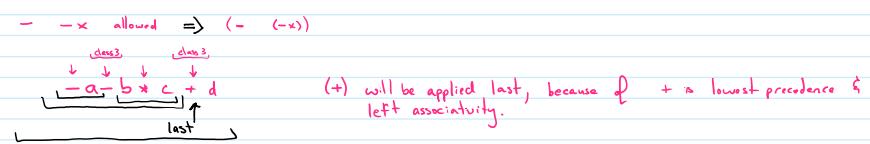
- ①  $E$  is an instance of a Identifier
- ②  $E$  is  $(e_1)$  where  $e_1$  is a SUIE
- ③  $E$  is  $e_1 \text{ op } e_2$  where "op" is a binary operator and each  $e_1 \& e_2$  are SUIE
- ④  $E$  is ' $\text{op}'  $e_1$ ' where "op" is a prefix unary operator &  $e_1$  is an SUIE$
- ⑤  $E$  is  $e_1 'op'$  where "op" is a postfix unary operator &  $e_1$  is an SUIE

### Semantics

The semantics of an expr tells you how an expr should be evaluated.

- If  $e$  is an identifier or literal constant (case 1 ↑) then the val of  $e$  = the val of identifier or literal
- If  $e$  is  $(e_1)$  (case 2 ↑) then  $e.\text{val} = e_1.\text{val}$
- Otherwise (case 3-5), let "op" be the operator that should be applied last  $\xrightarrow{\text{last}}$  ← Note: We will explain below precedence & associativity rules can be used to return which operator then if  $e$  is  $e_1 \text{ op } e_2$ , then  $e.\text{val} = \text{the result of applying op with } e_1 \text{ as 1st operand } \& e_2 \text{ as 2nd operand}$
- If  $e$  is " $\text{op}' e_1$ " or " $e_1 'op'$ " then  $e.\text{val} = \text{the value of applying "op" to } e_1$

	prefix	binary	associativity
Class 1	-		right
Class 2		*	left
Class 3		+	left



Note: If it is possible that  $e.\text{val}$  has no meaning according to the above rules b/c of Semantic errors such as:  
an uninitialized value, type mismatch, divided by 0 or ( in a language that requires variable to be declared ) → undeclared variable

### How to determine which operator should be applied last

The precedence & associativity rules of an infix notation (which are specified by the designers of that notation) partition the operators in to ranked precedence classes & they specify for each class whether the class is left/right associative.

Step 0: Let  $e' = e$  w/o any of the surrounding parens // example:  $e = ((-a(b*c)+d))$  then  $e' = -a - ((b*c)+d)$

Step 1: Find all top-level operators of lowest precedence in  $e'$  not in parens () // then  $- -$  are the top-level

→ with all the precedence classes binary "ops" is the lowest precedence of top level operators

Step 2: The "op" that should be applied last → the rightmost or leftmost "ops" found by step 1 according to left or right - associativity

### Another Example

	binary	pre ~	post	associativity
Class 1				right
Class 2	+-	+-		left
Class 3	^ @			right
Class 4	# \$			left

### Find last applied op

$$\begin{aligned} A: & (- \times + z \# (\text{~} y \# z) \& a @ \text{~} z \wedge \times \# \text{~} y = 1) \\ B: & (- \times + z \# (\text{~} y \# z) \& a @ \text{~} z \wedge \times \# \text{~} y = 1) \end{aligned}$$

Step 1 = locate lowest precedence (?)

Step 2 Assoc = left → look for rightmost = #

Assoc = right → look for leftmost = @

Warning: Precedence & Associativity rules do not (in general) uniquely determine which operator is applied first

### Prefix & Postfix Notations

An expression  $E$  is a S.V. prefix notation expr if:

1.  $E$  is an identifier or a literal constant
2.  $E$  is " $\text{op}' e_1 \dots e_k$ " where op is a K-ary op

An expr  $E$  is a S.V. postfix notation expr if:

1.  $E$  is an identifier or literal constant
2.  $E$  is  $e_1 \dots e_k 'op'$  where "op" is a K-ary op

2.  $E$  is " $op$ "  $e_1 \dots e_k$  where  $op$  is a  $K$ -ary op

2.  $E$  is  $e_1 \dots e_k "op"$  where " $op$ " is a  $K$ -ary op

### Semantics

In case 2,  $e_{\text{val}}$  = the result of applying " $op$ " to  $e_{\text{val}}_1, \dots, e_{\text{val}}_k$  with  $e_{\text{val}}_i$  as the  $i^{\text{th}}$  operand of  $op$

### Differences from Infix:

- No parenthesis
- Operators have arity  $\geq 2$
- precedence classes are not used

Prefix & Postfix expr can be evaluated using a stack as follows:

- Read the expr left to right (postfix)
  - when you see a variable or constant, push its value on right to left (prefix)
  - when you see a K-ary operator, pop  $k$  values from stack & apply the operator to the values
  - then push result onto the stack

11/6/17

Monday, November 6, 2017 3:05 PM

### Lexical Syntax (Sec. 2.3)

The syntax of programming languages is specified in terms of:

Examples:

① Tokens → if, /, ), (, \*, +, unsigned int literal  
→ if ( identifier <= unsigned-int-literal ) identifier ++;

② A chosen set of language constructs (such as "if statement", "expression", "variable declaration" and "statement")  
- Note: Some of these constructs may be special cases of the others

Two kinds of questions that syntax specification needs to answer are:

A) For each token, exactly what sequence of characters constitute a valid instance of that token?

- Note: For most tokens will have just one instance or a few instances. However tokens that = Identifier or -literal may have many instances.

B) For each of the chosen language constructs, exactly what sequences of tokens constitute a Syntactically Valid sequence of tokens?

The part of the syntax specifications that answers A is called the lexical syntax spec. However the "main" part of syntax specification will relate to B

\* Recall that the answer to B for a language construct X should have the following property:

- A sequence of Tokens  $T_1, \dots, T_n$  is syntactically valid if (and, roughly speaking, only if) some instance  $T_1, \dots, T_n$  is a possibly legal X  
\* possibly legal = legal in an appropriate arrangement

Identifier: An identifier is the name of a variable, function, class, etc.

Keyword: A token such as (if, while, do) that look like an identifier but has an entirely different role in programs.

Reserved Word: A token that look like an identifier but cannot be used as an Identifier is Reserved.

In many languages (including C++ & Java) every Keyword is also a reserved word

However Lisp keywords are not reserved words. Lisp has no reserved words. Any Lisp Keyword can be used as an identifier in the right context

Example:

(defun nil (if)	> (nil 7)
(if (> if 5)	10
(+ if 5)	> (nil 3)
(- if 2))	1

Is every reserved word a keyword? → Authors disagree on this. A language may have reserved words that do nothing (E.g. goto, const) In Java

As mentioned earlier, tokens that represent an Identifier or -literal constants of certain types have many instances. However, it should be noted that two different instances of the same token might be semantically equivalent.

For example: 0x7A & 122 are semantically equivalent instances of the "unsigned-int-literal" token

apple	adviser	buses
orange	adviser	buses

3.10 3.1 3.1 e 0

- are semantically equivalent to the "unsigned-double-literal" token

dog, Dog, and dog

- are semantically equivalent instances of the "identifier" token

- Most languages today are free-format languages. In a free-format language white space characters (blanks, tabs, newline) are ignored when they appear before a token

Example: while (        =    while (x < 3);  
                          x < 3  
                          );

In free-format languages the programmers has much flexibility in formatting code. However programmers have to read poorly formatted code

### Context Free Grammars (Sec. 2.4)

Context free grammars are one way to precisely specify a set of finite sequences of symbols [A set of finite sequences of symbols is sometimes called a formal language]

Context free grammars were introduced by Chomsky in the 1950's; he used them to specify the syntax of natural languages (such as English). A few years later, Backus independently reinvented the same concept, and proposed that context-free grammars be used to specify the syntax of the lang Algol 60

Context tree grammars are one way to precisely specify a set of finite sequences of symbols. A set of finite sequences of symbols is sometimes called a terminal language.]

Context free grammars were introduced by Chomsky in the 1950s; he used them to specify the syntax of natural languages (such as English). A few years later, Backus independently reinvented the same concept, and proposed that context-free grammars be used to specify the syntax of the lang Algol 60. This proposal was adopted in the Algol 60 report.

The grammar notation used in the Algol 60 report is called BNF (Backus-Naur Form), however we will use the term more loosely to mean:

An commonly used notation for writing context-free grammar



## Lecture #18

Wednesday, November 8, 2017 15:10

Median = 18.5  
 N = 35  
 "Good Scores" -> [>= 22 = 88%]  
 Aim for 6 hours per week  
 Do all reading assignments and homework exercises  
 Read lecture notes  
 Read first-da handout  
 Read all emails (check email on euclid using pine =>2 times each week  
 Attend all classes

- Context free grammars (sec 2.4)
  - Note: Sethi uses the term BNF to mean the grammar notation that was used in the algo60 report, but we (like many other authors today) will use the term more loosely, to mean any commonly used notation for writing grammars
    - Example: Figure 2.6 on p42 of sethi is an example of BNF in our sense (but not Sethi's sense)
    - Figure 2.10 on p46 of Sethi shows how the same grammar can be written in what Sethi would call BNF
    - Fig2.6 - this is BNF in our sense, not Sethi's
      - E ::= E + T
      - Some authors use an arrow instead of the ::=
      - E → E + T
    - Fig2.10 - this is BNF in both senses
      - <Expression> ::= <expression> + <term>
  - Grammars are used to precisely specify sets of finite sequences of symbols
    - The symbols here are called the terminals of the grammar
    - Each of the specified sets is called a non-terminal of the grammar
    - One of the non-terminals is considered to be the "main" non-terminal
      - This non-terminal is called the starting nonterminal (or start-symbol or sentence symbol)
    - The set of finite sequences of terminals that is denoted by the starting nonterminal is called the language of (or language generated by) the grammar. We often think of the other nonterminals as "helping" nonterminals that have been defined so
  - "Helping" nonterminals that have been defined so they can be used to define the starting nonterminal
  - Two uses of grammars are:
    1. In lexical syntax specification to specify the set of sequences of characters that constitute a valid instance of a token T that has many instances [Here T maybe a token that represents an identifier or a literal constant of some type]
      - 1) In the above, the terminals of the grammar are characters
    2. To specify sets of syntactically valid sequences of tokens for language constructs (such as "While statement", "statement", or "compilation unit")
      - 1) In the above, the terminals of the grammar are tokens
  - It is also common to "compose" grammars of type 1 with a grammar of type 2 to produce a grammar whose terminals are characters and some nonterminals represent tokens that have many instances.
    - 1) Note it is also common to do 1 using regular expression notation or just using English sentences

- Example from textbook
  - Here is an example of 1, this example is essentially the same as the grammar in Fig. 2.3 on p.36 of Sethi. You should also read footnote on page 38
  - The following grammar specifies unsigned floating point literals in a single programming language
  - In this language, such literals have the form
    - d . . . D DOT d . . . D
      - Think dot as giant period, think of it as a decimal point
      - D ->D means one ore more digits, brackets underneath it
    - In our language
      - 43143.4112 is good
      - .4112 is bad
      - 43142. is bad
      - 4.31e+3 is bad
  - Unsigned floating point literal -> UFPL
    1. UFPL ::= ip . f
      - Ip is the "integer part", f is a "fraction"
    2. Ip ::= d
      - 1) Ip ::= ip d //going to be erased in a minute, this is originally 3
      - 2) This is saying anything that is ip ... well if 4162.413 where before dot is ip, after dot is f, then that is a ufpl
      - 3) 3 is an ip, 34 is an ip d, 343 is an ip d with 34 and d, so that is an ip as well
      - 4) So the reason we omit the 1) is because they both have the same lefthand side, as such we draw a single bar to the next line like so
    3. | ip d
      - 1) The above lines 2 and 3 can be rewritten as Ip ::= d | ip d
    4. F ::= d
      - 1) So why is 3432 where 343 = 343 ip, 2 = 2 d a good decompositon? b/c 343 = ((343) \* 10 + 2 ; ip ::= ip1 d, ip.value = ip1.value) \* 10 + d
      - 2) The issue however lies with fractions

4.  $t ::= a$
5.  $| d f$ 
  - 1) So why is 3432 where  $343 = 343 \cdot ip_1 \cdot 2 + 2 \cdot d$  a good decomposition? b/c  $343 = ((343) * 10 + 2 ; ip ::= ip_1 \cdot d, ip.value = ip_1.value) * 10 + d$
  - 2) The issue however lies with fractions
    - a)  $0.3432 = 0.3432 \cdot 3 + 0.432)/10$
    - i)  $f ::= df$
    - ii)  $f.value(d.value + f_1.value)/10$
6.  $d ::= 0$   
.....
15.  $d ::= 0$

11/13/17

Monday, November 13, 2017 3:08 PM

111317

Audio recording started: 3:14 PM Monday, November 13, 2017

Tiny J Assignment 1 is now Available.

Do the installation before Wednesday's Class / Read Assignment Document before class  
Read the examples + debugging hints document / Before Exam II do exercises & reading for syntax  
Before the final, do assignment reading on C++ virtual functions

Last Time:

unsigned floating point literal grammar  
 $\text{ufpl} ::= \text{ip} . \text{f}$   
one or more digits    one or more digits  
2313 . 262 → 2313.262

- (1)  $\text{ufpl} ::= \text{ip} . \text{f}$
- (2)  $\text{ip} ::= \text{d}$
- (3)  $\text{d} ::= \text{ip} \text{ d}$
- (4)  $\text{f} ::= \text{d}$
- (5)  $\text{d} ::= \text{df}$

- (6)  $\text{d} ::= \text{O}$
- (7)  $\text{d} ::= \text{I}$
- (15)  $\text{d} ::= \text{9}$

This grammar has 10 terminals : O, I, ..., 9, . / It has 4 nonterminals : ufpl, ip, f, d

A terminal is an undefined constant symbol. A nonterminal is a variable that denotes a set of finite sequences of terminals

[In the above grammar we will see that ip denotes the set of all non-empty finite sequences of digits, and f denotes the same set.]

The grammar above consists of 15 grammar rules called Productions.  
Each production has the form:

a single non-terminal  $\rightarrow N ::= \alpha$  → a (possible empty) sequence of terminals and/or non-terminals

Note | is the "alternative" symbol : It means "The left side of this production is the same as the left side of the previous production."

Grammar Notation is free format — whitespace characters (including N/) are ignored

$\text{ip} ::= \text{d}$   
 $\text{ip} ::= \text{ip d}$  →  $\text{ip} ::= \text{d} \mid \text{ip d}$

$N ::= \alpha$  says "any  $\alpha$  is an N"

Ex:  $\text{d} ::= 4$  says "4 is a d"  
 $\text{ip} ::= \text{d}$  says "any d is a ip"  
 $\text{ip} ::= \text{ip d}$  says "if you take an ip and append a d to that ip then you will get another ip"  
↳ Examples:  $3 \in D$ ;  $4 \in ip$ ;  $43 \in ip$ ;  $434 \in ip$ ;  $4344 \in ip$

For this grammar ufpl is the starting non-terminal

- unless otherwise indicated, the starting non-terminal that appears on the left side of the very first production
- recalls that every non-terminal denotes a set of finite sequences of terminals. The set of sequences denoted by the starting non-terminal is called the language of (or language generated by) the grammar  
This set is regarded as the most important set specified by the grammar

- An empty grammar looks like  $N ::= \langle \text{empty} \rangle$   $\langle \text{empty} \rangle, \epsilon$ , and  $\lambda$  are 3 ways to represent the empty string.

Example of using  $\langle \text{empty} \rangle$ : Suppose we want to modify the above grammar so the ufpl → Replace (2) with  $\text{ip} ::= \langle \text{empty} \rangle$  may have NO digit before the decimal point:

## Parse Trees

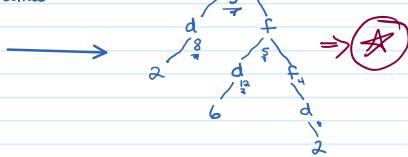
Question: Exactly which sequences of terminals belong to the set of sequences specified by a given non-terminal N

Answer: Use Parse Trees: A sequence of non-terminals  $T_1, \dots, T_n$  belongs to the set denoted by N if and only if  $T_1, \dots, T_n$  has a parse tree whose root is N.  
Note: unless otherwise indicated "parse tree" means "parse tree whose root is the starting non-terminal"

Example: Here is a parse tree which proves that the sequence of terminals 262 belongs to the set of sequences denoted by non-terminal f

So here the root is f

Parse tree of 262 whose root is f



A parse tree with root N is an ordered rooted tree that has properties:

- ① Each leaf is either a terminal or the symbol  $\langle \text{empty} \rangle$ ; an empty leaf has no children
- ② Each non-leaf node is a non-terminal
- ③ The sequence of the children of a non-leaf node K is the right side of the production whose left side is the matching non-terminal
- ④ The root of the tree is the non-terminal N

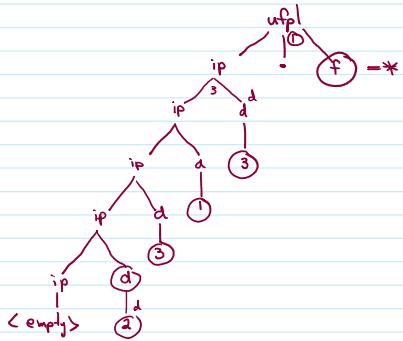
6<sup>2</sup>  
d  
2

③ The sequence of the children of a non-leaf node K is the right side of the production whose left side is the matching non-terminal

④ The root of the tree is the non-terminal N

A parse tree of a sequence of terminals  $T_1, \dots, T_k$  is the parse tree with the root N whose sequence of non-empty leaves in left to right order is  $T_1, \dots, T_k$

Here is a parse tree proving that 2312.262 belongs to the language by the modified grammar with ② as ip=empty

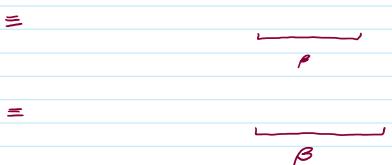


EBNF = Extended BNF  
= BNF + (...) + [...] + { ... }

Any set of sequences of terminals that can be specified in EBNF  
can be specified in BNF but  
EBNF is usually more concise & readable

Example  $N ::= \alpha (\gamma_1 \mid \dots \mid \gamma_k) \beta = N ::= \alpha \gamma_1 \beta$

$$\begin{aligned} & \quad | \alpha \gamma_2 \beta \\ & \quad : \\ & \quad \alpha \gamma_k \beta \rightarrow N ::= (\gamma_1 \mid \gamma_2) = N ::= \gamma_1 \quad \rightarrow \quad N ::= (\gamma_1) = N ::= \gamma_1 \end{aligned}$$



11/15/17

Wednesday, November 15, 2017 3:21 PM

$$[\gamma] = (\gamma \mid \langle \text{empty} \rangle)$$

$$\{\gamma\} = (\langle \text{empty} \rangle \mid (\gamma) \mid (\gamma)(\gamma) \mid \dots) = 0 \text{ or more}$$

Translating EBNF Rules into BNF

The following Method always works. The idea is to produce a new non-terminal for each:  $\{\dots\}$

Example: Translate

$$\begin{aligned} e &::= [+|-] \in \{\text{(+|-)}\} \\ e &::= \text{opt-sign} \in \text{rest} \\ \text{opt-sign} &::= + \mid - \mid \langle \text{empty} \rangle \\ \text{op} &::= + \mid - \\ \text{rest} &::= \langle \text{empty} \rangle \mid \text{rest op} \end{aligned}$$

(...)

{...}

$$\begin{aligned} \{\alpha\beta\} &= A ::= B / \alpha B \\ \alpha\{\alpha\beta\} &= A ::= \beta / A\alpha \end{aligned}$$

$$\left. \begin{aligned} \text{ip} &::= \langle \text{empty} \rangle \mid \text{ip d} \\ \text{defines ip as the set of } 0 \text{ or more d's} \end{aligned} \right\}$$





**The TINY Compiler's Static and Stack-Dynamic Memory Allocation Rules**

**Stack-Memory Allocation for Static Variables in TINY**

The  $i^{th}$  static int or array reference variable in a TINY source file is given the data memory location whose address is  $a + i - 1$  (the address of the first such variable is 0). This rule *does not apply* to Scanner variables, because they are dynamically allocated, so space is allocated to them.

**Stack-Memory Allocation for String Literals in TINY**

The  $i^{th}$  string literal character in the source file is placed into the data memory location whose address is  $a + i - 1$  (the address of the first such character is 0). This rule *does not apply* to Scanner variables, because they are dynamically allocated, so space is allocated to them.

**Stackframe of Method Calls and Returns Within Stackframes**

Each time a method is called during program execution, a block of contiguous data memory locations known as the call's **stackframe** or **activation record** is allocated; this block of memory locations will be deallocated when the method returns. The stackframe for each method call contains local variables declared in the method's body; each location within the stackframe is referred to by its *offset* relative to the stackframe's base address. Each location within the stackframe is referred to by its *offset* relative to the stackframe's base address. The offset of the stackframe's base address is 0; the offset of the first local variable is 1; the offset of the second local variable is 2; and so on. The offset of the last local variable in each method's stackframe is  $n - 1$ . EXAMPLE:

```

int f(int a, int b) {           4, 5
    int c = a + b;             6, 7
    if (c < 0) {                8, 9
        cout << "negative";    10, 11
        exit(1);               12, 13
    }
    else {                     14, 15
        cout << "positive";   16, 17
        exit(0);               18, 19
    }
}

```

In this example,  $a$ 's offset is 1,  $b$ 's offset is 2,  $c$ 's offset is 3,  $c$ 's offset is 4, and  $c$ 's offset is 5. When  $c$  is declared, it is at an offset of scope. So  $c$ 's offset is 4,  $a$ 's offset is 1,  $b$ 's offset is 2, and  $c$ 's offset is 3.

**Memory Allocation Rule for Local Variables in Methods in Tiny Method Bodies**

When a local variable is declared in a local-variable declaration (*Scanner variable* is the body of a method), that local variable is given the first stackframe location with offset  $\geq 1$  which has NOT already been allocated to another local variable in this stackframe. If no such offset exists, the local variable is given the first stackframe location with offset  $\geq 1$  which has NOT already been allocated to another local variable in all stackframes preceding Scanner variable declarations in each method's stackframe.

EXAMPLE: In a stackframe of any call of `int g(int p, int q, int r)`, `int s`, `s`'s offset is 2, giving Scanner variable `s`'s offset is 3. In a stackframe of any call of `int h(int t)`, `int u`, `u`'s offset is 2, giving Scanner variable `u`'s offset is 3. The offset of the local variable in each method's stackframe is reset.

*(This does not apply to methods in TINY, since local variable declarations have no locations with negative offsets.)*

The offset of the lower functions are reset.

As if there was a function func\_2, then the offsets within the function's variables would be reset and reassigned according to the declarations within.

Formal params (the params of a function) have negative effects

`int g (int p, int q, int r)`  
 $\quad \quad \quad -2 \quad -3 \quad -4$   
 $\quad \quad \quad o-1$   
 overtake

#### Use of Offsets in Code - 1) This subsection is relevant mostly to Tiny 1 Assignment 3

The stack frame location an offset is just 1 more information that is used to support return of control from a called method to its caller. Specifically:

In each stackframe other than main(), stackframe, the **return address** is stored at offset 0. (In main(), stackframe, the location of offset 0 stores an implementation-dependent pointer.) In stackframe  $i$ , the **return address** is the address of the instruction that links to a pointer to the data memory location at offset 0 in the stackframe of the method's caller.

In each stackframe other than main() stackframe, the **current address** is stored at offset -1. The current address is the address of the instruction that is to be executed after the current method returns control to its caller. (In main() its stackframe's base location at offset -1.)

#### Allocation and Deallocation of Stackframes: An Example

Suppose a TINY program has methods main, `f(1)`, `g(1,2,3)`, and `h()`; stackframes are deallocated at times (6) and (7). Thus there will be just 4 stackframes in data memory immediately after (8). Listed in order of decreasing memory allocation, those 4 stackframes will be:

- (1) main()'s stackframe, the location of offset 0 is the return address for call (11)
- (2) the stackframe of `g(1)` allocated for call (2)
- (3) the stackframe of `g(1)` allocated for call (5)
- (4) the stackframe of `h()` allocated for call (6)

Note that the stackframes of `h()` and `f(1)` allocated at times (4) and (5) would no longer exist. The stackframe of `h()` allocated at time (4) would have been deallocated at time (6), and the stackframe of `f(1)` allocated at time (5) would have been deallocated at time (7).

#### Comments on Scanner Variables

The data memory allocation rules for TINY variables *do not apply* to Scanner variables (such as the local variable `char Input` of `handshakeString()` in CS3162c.java and the static variable `Input` in `CS3162c.java`). **No scanner var is allocated for Scanner variables in TINY.** A Scanner variable in TINY is a reference to a Scanner object. A Scanner object is a reference to a memory location in standard input encoding system. (In reality it is usually associated with the keyboard) and returning its value. So the Scanner variable is completely irrelevant to why TINY essentially ignores Scanner variables. It is irrelevant to the TINY compiler what the value of a Scanner variable is, as *it is irrelevant* when a Java program executes `x.nextInt()`. Is `x` a Scanner object itself? No, it is an instance of `java.util.Scanner`. `nextInt()` is a method of `Scanner` object. It is the `Scanner` object that is doing the work. That is why TINY ignores it. In TINY the Scanner variable `x` is `x.nextInt()`. There only reason we want TINY to be a subset of Java is so that TINY programs will be compilable by a Java compiler.

#### Effects of Executing Each Tiny 3 Virtual Machine Instruction

Tiny VM Instruction	Effects of Executing the Instruction
ENTER	Halts the machine
END	Does nothing
PUSHCONST <i>value</i>	Pushes an item on the stack
PUSHINT <i>value</i>	Pushes the nonnegative integer value <i>n</i> .
PUSHSTACADDR <i>addr</i>	Pushes a pointer to the data memory location whose address is <i>addr</i> .
PUSHLOCADDR <i>addr</i>	Pushes a pointer to the data memory location that is offset <i>addr</i> from the currently executing method activation's stackframe.
SAVETOADDR <i>addr</i>	Pushes the item <i>p</i> , which is assumed to be a pointer to a data memory location.
LOADFROMADDR <i>addr</i>	Pushes the memory location to which <i>p</i> points.
WRITEINT <i>addr</i>	Pushes an item <i>v</i> , which is assumed to be a pointer to a data memory location.
WRITETINT <i>addr</i>	Pushes the integer <i>v</i> to the memory location to which <i>p</i> points.
WRITESTRING <i>addr</i> <i>str</i>	Pushes the integer <i>v</i> to the memory location to which <i>p</i> points.
READINT	Assumes the character sequence of <i>str</i> will be entered on the keyboard.
CHANGECODE	Reads the sequence and computes the value it represents.
CHANGEBIN	Pushes the integer <i>v.</i>
NOT	Pushes the Boolean value <i>NOT v</i> .
$\oplus = ADD, SUB, MUL, DIV, MOD, EQ, LT, GT, NE, GE, LE$	Pushes the Boolean value <i>v</i> .
$\oplus = AND, OR$	Pushes an item <i>v</i> , which is assumed to be a Boolean value.
JUMP <i>addr</i>	Leads <i>addr</i> into the program counter register.
JUMPNIFALSE <i>addr</i>	Leads <i>addr</i> into the program counter register if and only if <i>v</i> is false.
PASSPARAM	Allocates <i>loc</i> to be the statically allocated part of data memory.
CALLSTATMETHOD <i>addr</i>	Allocates one location in the stack-dynamically allocated part of data memory.

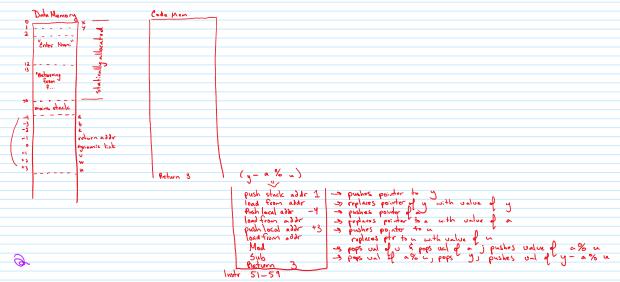
*pushstaddr* → for static variable, or vars from outside the current stackframe  
*pushlocaddr* → for the var defined in the current running method

$\oplus = AND, OR$	Pushes an item <i>v</i> , which is assumed to be a Boolean value.
JUMP <i>addr</i>	Pushes an item <i>v</i> , which is assumed to be a Boolean value.
JUMPNIFALSE <i>addr</i>	Pushes an item <i>v</i> , which is assumed to be a Boolean value.
PASSPARAM	Allocates <i>loc</i> to be the statically allocated part of data memory.
CALLSTATMETHOD <i>addr</i>	Allocates one location in the stack-dynamically allocated part of data memory.



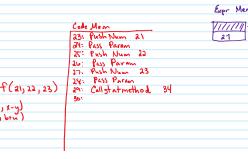
JUMP <i>label</i>	Loads <i>label</i> into the program counter register.
PASSVALFALSE <i>addr</i>	Push <i>addr</i> item, which is known to be a Boolean value. Load <i>addr</i> into the program counter register. If the value of <i>addr</i> is 1 it is false.
PASSPAIRAM	Alocates one location in the stack-dynamically allocated part of data memory. Pushes <i>addr</i> and <i>value</i> into the stack-dynamically allocated part of data memory. Push the first item that is passed and stored by the value of an argument of a method if the block is about to be called.
CALLSTATMTHOD <i>addr</i>	Alocates one location in the stack-dynamically allocated part of data memory; this will be the location in <i>addr</i> . In the caller's stack: Stores the program counter in the allocated location; the stored address is the location of the current method. Locals add into the program counter register.
INITSTKFRM <i>a</i>	Alocates one location in the stack-dynamically allocated part of data memory; this will be the location in <i>a</i> . In the current method activation's stack: Stores the frame pointer in the allocated location; this will serve as the stack-frame dynamic-link pointer. Pushes a pointer to the allocated location from the previous register Allocation's stack into the current activation's stack. If the data memory, this will be the location at <i>a</i> ; through it <i>a</i> can access the stack-frame dynamic-link pointer.
RETURN <i>a</i>	Assumes <i>a</i> is the pointer of memory of the currently executing method. Assumes the location of <i>a</i> is off the current memory executing method activation's stack-frame dynamic-link pointer. Assumes the location of <i>a</i> is off the currently executing activation's stack-frame; contains the return address. Locals add into the program counter register. Loads the return address into the program counter register. Dumps the stack-frame dynamic-link pointer to contain the currently executing method activation's stack-frame.
HEAPALLOC	Pushes <i>size</i> , which is assumed to be a nonnegative integer. Allocates <i>size</i> bytes of memory in the heap. It is assumed that the expected the second through <i>size</i> + 1 of those locations will be the start elements of an array of <i>elements</i> . Stores the location of the first location to the first location <i>loc</i> . The second through <i>size</i> + 1 locations will all contain PadValue.
ADDEOPTPR	Pushes <i>ptr</i> , which is assumed to be a nonnegative integer. Pushes <i>obj</i> , which is assumed to be a pointer to the data memory element <i>obj</i> . Pushes <i>array</i> , which is assumed to be a pointer to the class memory element <i>array</i> . Pushes <i>ptr</i> which is a pointer to the location where the class memory element <i>array</i> has <i>S</i> + 1 elements in case an array is repeated.

Example: The TinyJ Compiler of Assignment 2 should translate the following TinyJ source file into the TinyJ VM instructions shown on the next page.



**Instructions Separate**

4.	PISSETTAKAN	1	24.	HEUTTEKAN	3
5.	PAHETAKAN	16	25.	PISSETTAKAN	1
6.	PAHETTAKAN	3	26.	PISSETTAKAN	1
7.	PAHETTAKAN	3	27.	HETTEKAN	1
8.	MUHTETTAKAN	3	28.	HETTEKAN	-2
9.	PAHETTAKAN	3	29.	HETTEKAN	1
10.	HEAHTAKAN	61	30.	PAHETTAKAN	-3
11.	DAHETTAKAN	51	31.	PAHETTAKAN	1
12.	PAHETTAKAN	57	32.	LOAFSPRONGE	1
13.	PAHETTAKAN	57	33.	LOAFSPRONGE	1
14.	PISSETTAKAN	1	34.	LOAFSPRONGE	1
15.	PAHETTAKAN	1	35.	LOAFSPRONGE	1
16.	PAHETTAKAN	1	36.	LOAFSPRONGE	1
17.	PAHETTAKAN	51	37.	LOAFSPRONGE	-4
18.	PAHETTAKAN	51	38.	LOAFSPRONGE	3
19.	CALLETTAKAN	34	39.	POBLACACION	3
20.	ULCETTAKAN	55	40.	POBLACACION	1
21.	PAHETTAKAN	51	41.	POBLACACION	1
22.	LOAFSPRONGE	51	42.	POBLACACION	1
23.	PAHETTAKAN	21	43.	POBLACACION	1
24.	PAHETTAKAN	23	44.	REUTEN	3
25.	PAHETTAKAN	23	45.	REUTEN	1
26.	PAHETTAKAN	65	46.	HEUTTEKAN	1
27.	PAHETTAKAN	23	47.	HEUTTEKAN	1
28.	PAHETTAKAN	62	48.	POBLACACION	1
29.	CALLETTAKAN	34	49.	LOAFSPRONGE	1
30.	PAHETTAKAN	51	50.	LOAFSPRONGE	1
31.	MUHTETTAKAN	61	51.	LOAFSPRONGE	-2
32.	PAHETTAKAN	51	52.	LOAFSPRONGE	1
33.	STOP	67	53.	HETTEKAN	1
34.	PAHETTAKAN	51	54.	PAHETTAKAN	1



When executing **PUSH1** at address *a*, remember to push the pointer corresponding to address *a*. In other words, remember to push *a* onto **POINTERTAG, so that the memory stack now has a pointer. If *p* is on top of the stack, then the data memory address is located here in *p* — **POINTERTAG**.**

When executing **SAVETOADDR**, remember that the second item in the stack is a pointer. If *p* is on top of the stack, then the data memory address is located here in *p* — **POINTERTAG**.

When executing **CALLSTDMETHOD**, **INSTEKPRIM**, **PASHPARM**, and **RETURN**, remember that **ASP** is a pointer to the data memory address. **ASP** is **POINTERTAG**. When executing **SUPERPUSHLOC**, **INSTEKPRIM**, or **RETURN**, you should add **POINTERTAG** to *p*? You also should add **POINTERTAG** to *p*? before storing it in **ASP**. **INSTEKPRIM** and **PASHPARM** both have the same effect. They both add the **POINTERTAG** to the stack during execution of **RETURN**. Similarly, since **ASP** is **POINTERTAG** before store pointers, do we add **POINTERTAG** when copying from **ASP** into **PP** via **CALLSTDMETHOD** execution of **INSTEKPRIM**?

**WHEN EXECUTING WRITESTRING**: A remember that *a* is an ordinary data memory address, not a pointer to another data memory address.

**POINTERTAG** is *not* used with code memory addresses. Never subtract **POINTERTAG** from PC, and never add **POINTERTAG** to a code memory address.

#### How to Test Your Solution

You have correctly completed all the incomplete **executeC()** methods, and completed each of the modified **intc.c** Java files, for your assignment on the 16 **CS131midterm.java**. The **intc.c** Java files are located in the **CS131midterm** folder. You can run them on your PC, or in a Java virtual machine. After running, the **class** file is executed by the Java virtual machine. Also, the **dump** after execution of, say, 100 instructions should be the same for your program as for my solution. Recall that you can run my

`java -cp T2midclasses: T2as.jar C131midterm.java <ion> <ion> <ion> <ion>`

`java -cp T2midclasses: T2as.jar C131midterm.java <ion> <ion> <ion> <ion>`

`java -cp T2midclasses: T2as.jar C131midterm.java <ion> <ion> <ion> <ion>`

**How to Submit Your Solution**

This assignment can be submitted no later than **Thursday, December 21**. However, from this point forward, you will receive a 10% deduction for every day late that you submit.

When you submit, make sure to include **COMMENT**. Also, if you accidentally post your code on the disk file, do not decline to submit. Try to resubmit the file, and do an early day if possible. See page 3 for the **late** section.

The assignment counts 25 towards your grade if the grade is computed using rule A. You may work up to two other students, when two or three students work together, **each student must submit**.

If you have been working on **exclct**, return by following steps 1, 2, 3, and 4 on the next page. If you have not been working on **exclct**, return by following steps 1, 2, 3, and 5 on the next page. Your working directory should be your home directory or **venus:/cs131/intc/intc** on a PC.

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1. Return any **executeC()** class file you have **NOT** successfully compiled from the **T2midclasses** folder, or the folder of the solution you have been working on.

2. This step does **NOT** apply if you have been working on **exclct**. If and only if you have been working on **exclct** on your PC (**CS131midterm**), enter the following command on **exclct**:

**Test your solution**

If you have been working on **exclct**, you should now see **JavaException**. If you have been working on your PC, create a jar archive of all the **intc\*.java** files, and then run:

`jar cvf intc.jar T2as/virtualMachine/intc.class lib/intcVirtualMachine.jar`

This creates a jar archive file **intc.jar** on your PC. Use the **jar** command to copy **intc.jar** to your **CS131midterm** folder. If you have been working on **exclct**, you should not do this. Instead, follow how to do this, see the second paragraph of the **"How to Submit Your Solution"** section of the first Assignment 3 document, but substitute **intc.jar** for **CS131midterm.jar** and **intcVirtualMachine.jar** for **intcVirtualMachine.jar**.

Then logon to **exclct** and extract the archived **intc.jar** file as follows:

`cd /home/exclct`

`jar xf intc.jar > intc.java`

20 If you have been working on **exclct**, you should now see **JavaException**. If you have been working on your PC, run the **intc** command on your PC, and then run:

3. On **exclct**, compile all the **intc\*.java** files you have compiled, as follows:

`javac -d lib/intcVirtualMachine.jar intc.java`

If you have been working on your PC, run the **intc** command on your PC, and then run:

4. Test your program on **exclct**. (See the section **"How to Test Your Solution"** above.)

**IMPORTANT!** Do NOT spec any of your submitted **\*intc\*.java** files is an **edit** on **exclct**. If you do, you will receive a 10% deduction for every day late that you submit.

**How to Submit Your Solution**

Please contact me to day no later than **6pm** on **December 21**. If **exclct** says that the submission of this project is complete, and you are progressing smoothly (including corrected submissions) with the accepted code on **Friday, December 21**, but the submission deadline will not be extended if **exclct** goes down for any reason. If **exclct** goes down for any reason, you should resubmit on **Dec 22**. If **exclct** goes down for any reason, there is a possibility that it might not be brought back up until after noon on **Dec 22**, which causes those students who did not submit before **exclct** went down may not be able to submit again. To avoid the risk of not being able to submit, make any late -corrected submissions no later than **1pm** on **Thursday, December 21**.

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#### Hints for Tiny Assignment 3

Before you work on the assignment, carefully read page 4 above. When writing the **executeC()** method for an instruction, if you are not clear as to what that instruction should do when it is executed, refer back to the **"Effects of Executing Each Tiny Virtual Machine Instruction"** pages at <http://www.cs.toronto.edu/~mccoll/cs131/Assignment3.html#InstructionsAndWhatTheyDoForAnyC0f>

**Remarks on the executeC() Methods You Have to Write**

**Instructions That Do Not Deal With Pointers to Data Memory Locations and Have No Operands**

**ABR, DIV, MUL, MOD, AND, OR**

As you implement **executeC()**, the **ABR**, **DIV**, **MUL**, **MOD**, **AND**, and **OR** can be written analogously. Use **if** and **return true** or **false**. You can use **intcVirtualMachine** to help you.

**GE, LE, LT, GT, EQ, NE**

The implementation of **GE**, **LE**, **LT**, **GT**, **EQ**, **NE**, and **NOT** methods for these instructions is in use conditional expressions.

**NOT** is implemented as **NOT** method could be implemented as follows:

`NOTMETHOD: {D0} == (EXTRACTC(D0) == (EXTRACTC(D0)))`

**UNPUSH, NOT, WRITEINT, AND, OR, ANDNOT, ORNOT**

The implementation of **UNPUSH**, **NOT**, **WRITEINT**, **AND**, **OR**, **ANDNOT**, and **ORNOT** methods for these instructions is in use conditional expressions.

**PUSHINT, JUMP, JUMPOUNSE, JUMPNOT, JUMPNOTF**

The implementation of **PUSHINT**, **JUMP**, **JUMPOUNSE**, **JUMPNOT**, and **JUMPNOTF** methods for these instructions is in use conditional expressions.

**WRITESTRING, T1, DATA, POP, PUSHPARM, CALLSTDMETHOD, INSTEKPRIM, RETURN**

The implementation of **WRITESTRING**, **T1**, **DATA**, **POP**, **PUSHPARM**, **CALLSTDMETHOD**, **INSTEKPRIM**, and **RETURN** methods for these instructions is in use conditional expressions.

**LOADFROMADDR, SAVETOADDR, INSTEKPRIM, PUSHPARM, CALLSTDMETHOD, INSTEKPRIM, RETURN**

The implementation of **LOADFROMADDR**, **SAVETOADDR**, **INSTEKPRIM**, **PUSHPARM**, **CALLSTDMETHOD**, **INSTEKPRIM**, and **RETURN** methods for these instructions is in use conditional expressions.

**INSTRUCTIONS ASSOCIATED WITH CALL OF STATIC METHODS AND BETTER FROM CALLED METHODS**

Recall from p. 1 that **ASP** stores a **pointer** to the first memory location in the stack-dynamically allocated part of data memory — i.e., **ASP** points to the **first location** above the currently allocated locations in data memory.

So **ASP** must be increased (decreased) by 1 when a stack-frame locations are allocated (deallocated).

We will write:

`S-PUSH y for T2.data[0] == &POINTERTAG == p;`

We will write:

`S-POP y for y = T2.data[-ASP - &POINTERTAG];`

**S-PASSPARM**

should **S-PUSH** a value that is popped off **EXPSTACK** — i.e., we should **S-PUSH EXPSTACK -&PT**

**S- CALLSTDMETHOD**

should **S-PUSH** **IC** — (some memory location, i.e., new free space)

and then **Set PC=677** (handles control to the called method code).

**S1: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S2: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S3: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S4: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S5: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S6: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S7: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S8: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S9: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S10: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S11: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S12: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S13: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S14: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S15: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S16: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S17: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S18: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S19: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S20: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S21: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S22: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S23: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S24: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S25: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S26: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S27: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S28: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S29: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S30: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S31: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S32: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S33: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S34: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S35: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S36: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)

and then **Set PC=677** (handles control to the new free space)

**S37: INSTEKPRIM**

should **S-PUSH** **IC** — (some offset to **ASP** to effect to the new free space)



We will write S.POP y for  $y = T2.\text{data}[-1].\text{ASP} - \text{POINTING}$ :  
 15. **PASSPARAM**  
 should S-PUSH a value that is popped off EXPSTACK  
 → i.e., it should S-PUSH EXPSTACK--ASP

12. **CALLSTATMETHOD** 671 should S-PUSH RC [handles return value from, & creates new frame]  
 and then S-PUSH EXPSTACK--ASP

171. **INFSTRUCTURE** 7 should S-PUSH FP [handles caller's FP as offset to the new frame]  
 and then Set FP to ASP-3 [makes space for caller's local variables]  
 and then Return ASP by 7 [allocates space for callee's local variables]

173. **RETURN** 4 should Set ASP to FP1 [allocates space used by return variable]  
 and then S-POP FP [removes caller's FP]  
 and then S-POP PC [sets the saved state address in PC]  
 and then Decrease ASP by 4 [allocates space used by formal parameter]

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```

13: LOADPRIMEDER
14: SAVETADDER 0
15: LOADTADDER 3
16: ADDTADDER 0
17: ADSTPTE
18: PUSHLOCADER 1
20: LOADLOCADER
22: ANDTADDER
24: WEEFLINP
25: PUSHSTADDER 0
26: SUBTADDER 5
28: MULFLINP
29: PUSHLOCADER 2
30: DIVTADDER 4
31: MODFLINP
32: PUSHLOCADER 0
33: RETTADDER
34: SAVETADDER
35: RETURN
40: STOP

```

(c) Example involving a while loop:

```

class Path {
    static int[] a = new int[10];
    public static void main (String args[])
    {
        int x = 100;
        while (x > 30)
            x = f(x, x);
    }
    static int f(int a, int n)
    {
        a[x] = a / n;
        return a[x];
    }
}

```

What would a correct solution to They? Assignment 2 translate this into?

```

SOLUTION: 0: PUSHSTADDER 0
1: PUSHFLINP 10
2: SAVETADDER
3: LOADTADDER 1
4: PUSHLOCADER 1
5: LOADLOCADER 100
6: SAVETADDER
7: LOADLOCADER 1
8: LOADPRIMEDER
9: PUSHFLINP 10
10: SAVETADDER
11: LOADTADDER 22
12: PUSHLOCADER 22
13: PUSHLOCADER 1
14: LOADLOCADER
15: PUSHPRIMEDER
16: PUSHFLINP 2
17: SAVETADDER
18: LOADTADDER
19: PUSHPRIMEDER
20: SAVETADDER 23
21: LOADTADDER 8
22: SAVETADDER
23: PUSHPRIMEDER 0
24: PUSHSTADDER 0
25: SUBTADDER 3
26: MULFLINP
27: PUSHLOCADER -3
28: PUSHLOCADER -2
29: LOADTADDER
30: SAVETADDER
31: LOADTADDER
32: SAVETADDER
33: LOADTADDER 0
34: PUSHSTADDER 0
35: PUSHFLINP 3
36: PUSHLOCADER
37: LOADTADDER
38: SAVETADDER
39: RETURN 2

```

(d) Another example involving a while loop:

```

class Hello {
    static int a[] = new int [10];
    public static void main (String args[])
    {
        a[1] = 900;
        System.out.print(a[1]);
    }
    static int getit (int a)
    {
        int t = a/5;
        while (t > 0)
            t = t / a;
        return t;
    }
}

```

What would a correct solution to They? Assignment 2 translate this into?

```

SOLUTION: 0: PUSHSTADDER 0
1: PUSHFLINP 25
2: SAVETADDER
3: LOADTADDER 0
4: PUSHLOCADER 0
5: LOADLOCADER 0
6: PUSHPRIMEDER
7: LOADPRIMEDER 5
8: ADSTPTE
9: PUSHFLINP 900
10: SAVETADDER 7
11: LOADTADDER
12: PUSHPRIMEDER
13: PUSHPRIMEDER 16
14: WEEFLINP
15: PUSHFLINP 1
16: PUSHSTADDER 1
17: PUSHLOCADER 1
18: LOADTADDER
19: PUSHLOCADER 0
20: PUSHPRIMEDER
21: LOADLOCADER
22: LOADPRIMEDER
23: PUSHLOCADER 1
24: PUSHLOCADER
25: PUSHFLINP 30
26: SAVETADDER
27: LOADTADDER 37
28: PUSHLOCADER 1
29: PUSHLOCADER 1
30: PUSHLOCADER
31: LOADLOCADER
32: PUSHLOCADER -2
33: LOADTADDER
34: DIVTADDER
35: PUSHTADDER
36: STOP 24

```

(e) The next example involves if as well as while:

```

import java.util.Scanner;
class Spring09 {
    static Scanner input = new Scanner(System.in);
    static int x;
    public static void main (String args[])
    {
        int a;
        if (input.nextInt() == 1)
            if (x < 1 + x * 20000) {
                while (x < 20000) {
                    x = x + 1;
                }
            }
        int c = a;
        System.out.print(c);
    }
}

```

What would a correct solution to They? Assignment 2 translate this into?

SOLUTION:  
Note that the local variables b and c both have a stackframe offset of 2. At the point where c is declared, b no longer exists—b's scope is exhausted at the end of the while loop. Thus stackframe offset 2 can be reallocated to c.

```

0: INITTADDER 2
1: LOADTADDER 0
2: READINT
3: LOADTADDER
4: PUSHSTADDER 0
5: SUBTADDER 20000
6: PUSHFLINP 1
7: LOADTADDER 0
8: LOADPRIMEDER
9: PUSHFLINP 20000
10: PUSHSTADDER
11: ANDTADDER
12: JND
13: JUMPFALSE 36
14: PUSHSTADDER 0
15: PUSHLOCADER
16: PUSHFLINP 20000
17: JUMPFALSE 29
18: PUSHFLINP 2
19: PUSHLOCADER
20: PUSHSTADDER 0
21: PUSHLOCADER
22: PUSHSTADDER 0
23: PUSHSTADDER 0

```



**Hints Relating to the Cases on Lines 627, 723, and 993 in ParserAndTranslator.java**

The Method `printAssignment()` (ppm on line 627)

The relevant BNF rule is `<assignment> ::= <expression> | <variable>`

(a) In the case `<variable> ::= <name>`, the code to be generated is given by  
`new NMTIMETracker();`

Assuming you correctly filled in the gap in the method `printAssignment()` in Assignment 1, if you copy just that code into the body of Assignment 2's `printAssignment()` then its call of `new NMTIMETracker()` will be redundant. You will need to remove it from `printAssignment()`. You also would need to insert a `new NMTIMETracker();` statement.

(b) In the case `<assignment> ::= <expr1> = <expr2>`, the code to be generated is given by

where `v` is the data memory address of the first and last characters of the `<expr1>` string literal that is to be printed. The `NUTIMETRACKER` is a `b` instruction can be generated by `new NUTIMETRACKER(v);` and the `PRINTB` is a `c` instruction can be generated by `new PRINTB(b);` and the `PRINTB` is a `d` instruction can be generated by `new PRINTB(d);` but how can your code find the two addresses `a` and `b`?

The solution is provided by the lexical analyzer. When `LexicalAnalyzer::nextToken()` sets the current token to `PRINTB`, it also sets the private variables `LexicalAnalyzer::startOfString` and `LexicalAnalyzer::endOfString` to the addresses of the start and end of the string. When `LexicalAnalyzer::nextToken()` is called again, the new token will be `PRINTB`, so the new address will be placed in `LexicalAnalyzer::startOfString` and `LexicalAnalyzer::endOfString` and public accessor methods that return the two addresses.

listen now

The Method `expr1()` (ppm on line 723)

The relevant BNF rule is `<expr1> ::= <expr2> | <expr2> <operator> <expr1> | <operator> <expr2> | <operator> <expr2> <operator> <expr1> | <operator> <operator> <expr2> | <operator> <operator> <operator> <expr1> | <operator> <operator> <operator> <operator> <expr1>`

The code and the `instructions` (i.e., `instructions ::= <instruction> | <instruction> <instruction> | <instruction> <instruction> <instruction> | <instruction> <instruction> <instruction> <instruction>`) have been done for you in `ParserAndTranslator.java`. Here are hints for the other cases

(a) In the case `<operator> ::= <operator> + <operator>`, the code to be generated is given by

Similarly, in the case `<operator> ::= <operator> * <operator>`, the code to be generated is given by  
`new NUTIMETRACKER(v);`

In these two cases, you will have completed the body of the method `expr1()` when doing Assignment 1, if you use that code as the body of Assignment 2's `expr1()` then in the first case the code to call `expr2()` will generate `<operator>`-code, and in the second case the reverse. In the case `<operator> ::= <operator> / <operator>`, the code to be generated is given by  
`new NUTIMETRACKER(v);`

Similarly, in the case `<operator> ::= <operator> % <operator>`, the code to be generated is given by  
`new NUTIMETRACKER(v);`

These two cases are similar to the second case of (b), except that you need to insert a `new CHARCODEGIVER()`, `a = new NUTIMETRACKER();` statement.

(c) In the case `<operator> ::= <operator> - <operator>`, the code to be generated is given by

where `v` is the data memory address of the integer literal. The instance `v` instruction can be generated by `new PRINTB(v);` with the appropriate value `v`. But how can your code find the value `v`?

The solution is provided by the lexical analyzer. When `LexicalAnalyzer::nextToken()` sets `LexicalAnalyzer::currentToken` to `PRINTB`, it also sets the private variable `LexicalAnalyzer::currentValue` to the numerical value of the `PRINTB` integer literal. `LexicalAnalyzer::currentValue` is a `b` instruction and `PRINTB` is a `c` instruction, so the `PRINTB` will be generated by `new PRINTB(b);`

In the case `<operator> ::= <operator> <operator> <operator>`, the code to be generated is given by  
`new NUTIMETRACKER(v);`

Assuming you correctly completed the body of `expr1()` when doing Assignment 1, if you use that code as the body of Assignment 2's `expr1()` then the code to be generated is given by a call of `expr1()`. You would need to insert a `new HEAPALLOCATOR();` statement.

listen now

The Method `whlLabel()` (ppm on line 993)

The relevant BNF rule is `<whlLabel> ::= while ( <expr1> ) <statement>`

and the code to be generated is given by:

```

    while ( <expr1> )
        <statement>
    ENDWHILE b
    <operator> a
    ENDWHILE b

```

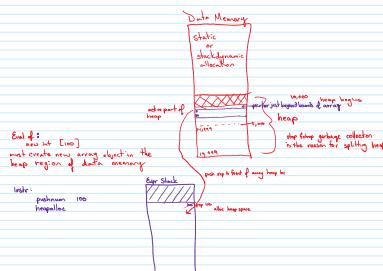
In Instruction.java, the static variable `newCodeAddress` is used to hold the code memory address of the `next` instruction. If you want to generate a local variable `val` to hold the value of `newCodeAddress`, then you will need to insert a `new LOCALSCOPE()` instruction before the `next` instruction. This will make `val` a local variable which needs to be deallocated. Then `val` will be needed as the operand `a` in the `ENDWHILE b` instruction which will label `o` to point to `label`.

When `whlLabel()` begins to generate `ENDWHILE b`, it does not know what the address `b` will be. So it has to generate a local variable `val` to hold the address of `ENDWHILE b`. `OPRANDE_NOT_YET_DEFINED` and `OPRANDE_DEFINED` are local variables which are local variables to the local variable `val`, to allow the instruction to be deallocated when `whlLabel()` is ready to fix up its operand.

```

OPRANDE_NOT_DEFINED jlabel = new OPRANDE_DEFINED(Instruction.OPRANDE_NOT_YET_DEFINED);

```



```

24: LOADR0AFTER    5
25: PUSHR0         3
26: SAVET0AFTER   -14
27: LOADT0AFTER    14
28: PUSHLOCADER   0
29: LOADLOCADER    0
30: SAVET0AFTER   -14
31: LOADR0AFTER    2
32: PUSHR0         3
33: PUSHLOCADER   2
34: SAVET0AFTER   -14
35: STOP

```

(f) Suppose `Instruction.getNextCodeAddress()` == 45 when a correct solution to T1(a) Assignment 2 begins to translate the following assembly code. What would be the address of the first instruction that they VM instructions would this method be translated into?

```

static int p(int x)
{
    int y = 3, z;
    x = x + y;
    if (x > 100) z = x * x;
    else z = x + y;
    return x - z;
}

```

SOLUTION

```

41: LDLT0AFTER    2
42: PUSHR0AFTER   3
43: PUSHR0         3
44: PUSHLOCADER   -2
45: LOADLOCADER   -2
46: LDLT0AFTER    2
47: PUSHR0         3
48: SAVET0AFTER   -14
49: LOADR0AFTER    1
50: PUSHR0         3
51: LOADR0AFTER    1
52: PUSHR0         3
53: LOADR0AFTER    1
54: SAVET0AFTER   -14
55: LOADT0AFTER    14
56: PUSHLOCADER   -2
57: LOADLOCADER   -2
58: LDLT0AFTER    10
59: LDLT0AFTER    10
60: LDLT0AFTER    10
61: PUSHSTATABER  66
62: PUSHLOCADER   -2
63: LOADLOCADER   -2
64: LDLT0AFTER    10
65: LDLT0AFTER    10
66: LDLT0AFTER    10
67: PUSHLOCADER   1
68: LOADLOCADER   -2
69: SAVET0AFTER   -14
70: PUSHSTATABER  2

```



