LAB 09

Mutable Trees, Efficiency

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LOGISTICS The Control of the Control

- ANTS 🍪
 - Checkpoint 2 due today 03/21
 - The whole project due Fri 03/24
 - Submit by Thu 03/23 for one extra point!
- Lab 09 due tomorrow 03/22
- Come to OH >:)

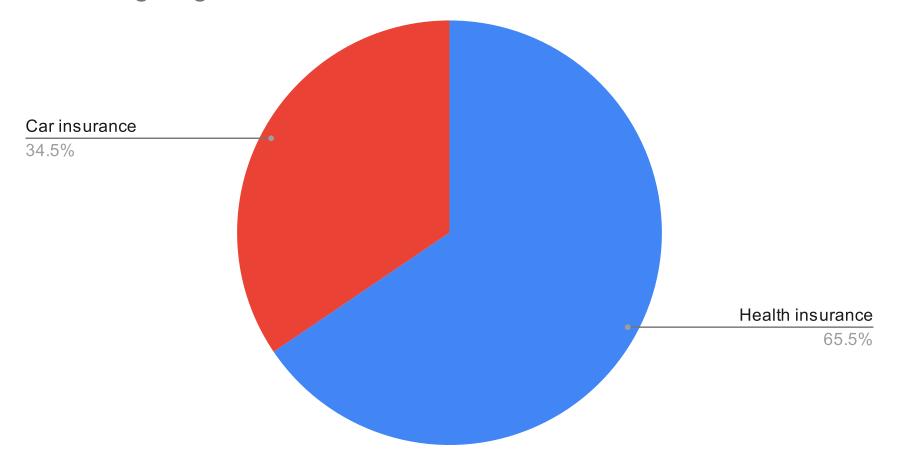
ABOUT THE 2ND MIDTERM ©

The second... what?

- Fri 4/7, 7-9 pm
- Logistics Ed post #2141
 - If you need ANY alterations (left-handed desk, remote, other accommodations due to DSP or otherwise), <u>fill out this form</u> by Mon 04/03!!
- Preparations
 - Familiarize yourself with the topics in scope
 - Attend review session (or watch recordings/slides) for more topical review - see Ed for more info
 - Do practice exams!
 - Quality > quantity
 - Post on exam threads on Ed for help
 - Walkthrough videos/guide are your friend!

FROM LAST TIME... 99

Would Lighting McQueen have car insurance or health insurance?



MUTABLE TREES



WHY MUTABLE TREES?

Recall from (functional) data abstraction...

```
def tree (label, branches=[]):
    return [label] + list(branches)

def label (tree):
    return tree[0]

def branches (tree):
    return tree[1:]

def is_leaf(tree):
    return not branches(tree)
```

- These trees are immutable
 - To modify, need to call constructor again with updated attributes - inefficient
 - Solution use OOP, since objects are mutable

MUTABLE TREES

```
>>> t = Tree(3, [Tree(2, [Tree(5)]), Tree(4)])
>>> t.label # label is now an instance attribute
3
>>> t.branches[0].label # so is branches
2
>>> t.branches[1].is_leaf() # is_leaf is a method
True
```

FUNCTIONAL DATA ABSTRACTION VS. OOP

	Functional Data Abstraction	Tree class / OOP
Constructor	tree(label, branches)	<pre>Tree(label, branches) (which calls Treeinit)</pre>
Label and branches	label(t) or branches(t)	t.label or t.branches
Mutability	immutable - cannot assign values to call expressions	mutable - can reassign label and branches
Checking if a tree is a leaf	<pre>convenience function is_leaf(t)</pre>	<pre>bound method t.is_leaf()</pre>

TREES - PROBLEM SOLVING STRATEGIES

- Pay attention to whether it's <u>mutation</u> or <u>constructing a new tree</u>
- To mutate a tree object:
 - reassign its instance attributes(t.label = ... or t.branches = ...)
 - use list mutation method (append/extend/pop/etc.) on its branches - t.branches is a <u>list</u> of trees!
- For mutation problems:
 - Which should be mutated first the root node or its branches?
 - The return value is often None
 - Sometimes the case case is implicit if we have for loop that iterates through all the branches, the loop will not be executed if t.branches is an empty list (i.e., when t is a leaf)

LAB Q1

ORDER OF GROWTH

ORDER OF GROWTH

- Order of growth (efficiency) how the runtime changes as the input size increases
 - Think of runtime as a <u>function</u> of the input size
- Input size (not the exact definition, but as a rule of thumb)
 - numeric input magnitude of the number
 - Python lists length of the list
 - linked list/trees/other recursive objects number of nodes
- Runtime (not the exact definition, but as a rule of thumb)
 - the number of operations
- Theta notation for input of size n, the runtime is denoted by $\Theta(f(n))$
 - lacksquare $\Theta(f(n))$ approximately f(n) by a constant factor

ORDER OF GROWTH - OTHER NOTES

- constant < logarithmic < linear < quadratic < exponential
- Constants are ignored
 - E.g., $\Theta(2n+3)$ is essentially $\Theta(n)$
- Only consider the term that grows fastest
 - E.g., $\Theta(n^2 + 2n + 3)$ is essentially $\Theta(n^2)$

ORDER OF GROWTH - CONSTANT

- Constant $\leftrightarrow \Theta(1)$
- Runtime does not change as the input size changes
- For example:

```
def square (x):

return x * x
```

input	function call	return value	operations
1	square(1)	1*1	1
2	square(2)	2*2	1
100	square(100)	100*100	1
n	square(n)	n*n	1

ORDER OF GROWTH - LOGARITHMIC

- Logarithmic $\leftrightarrow \Theta(\log n)$
- Often when we keep dividing the input by a constant

```
def foo (x):

while x > 0:

print('hey')

x //= 2
```

Let's say the while loop runs n times before x reaches 0.

divide x by 2 for n times before it gets to 1

$$\implies \frac{x}{2^n} = 1 \implies 2^n = x \implies n = \log_2 x$$

ORDER OF GROWTH - LINEAR

- Linear $\leftrightarrow \Theta(n)$
- ullet Often when a loop runs n times, each time doing work in constant time

```
def factorial(x):
    prod = 1
    for i in range(1, x + 1):
        prod *= i # execute x times in total
    return prod
```

input	function call	return value	operations
1	factorial(1)	1*1	1
2	factorial(2)	2*1*1	2
100	factorial(100)	100*99**1*1	100
n	factorial(n)	n*(n-1)**1*1	n

ORDER OF GROWTH - QUADRATIC

- Quadratic $\leftrightarrow \Theta(n^2)$
- ullet Often when a nested loop runs n^2 times, each time doing work in constant time

```
def bar(n):
    for a in range(n):
        for b in range(n):
            print(a, b) # print n * n times in total
```

input	function call	operations (prints)
1	bar(1)	1
2	bar(2)	4
100	bar(100)	10000
n	bar(n)	n^2

ORDER OF GROWTH - EXPONENTIAL

- Exponential $\leftrightarrow \Theta(c^n)$, where c is a constant
- Often in tree recursion

```
def rec(n):
    if n == 0:
        return 1
    else:
        return rec(n - 1) + rec(n - 1)
```

input	function call	return value	operations
1	rec(1)	2	1
2	rec(2)	4	3
10	rec(10)	1024	1023
n	rec(n)	2^n	2^n

ORDER OF GROWTH - TREE RECURSION

```
def rec(n):
    if n == 0:
        return 1
    else:
        return rec(n - 1) + rec(n - 1)
```

- Try drawing out the recursion tree diagram
- n + 1 levels
- The i^{th} level has 2^i nodes (root at level 0)
- Each node does constant work (addition)
- Total = $(1 + 2 + ... + 2^{n+1}) \cdot constant = \Theta(2^n)$

ORDER OF GROWTH - TREE RECURSION

What about this? 🤔

```
def rec(n):
    if n == 0:
        return 1
    else:
        return rec(n // 2) + rec(n // 2)
```

- Draw out the recursion tree diagram
- $\log_2 n$ levels
- The i^{th} level has 2^i nodes (root at level 0)
- Each node does constant work (addition)
- Total = $(1 + 2 + ... + 2^{\log_2 n}) \cdot constant = \Theta(n)$

ORDER OF GROWTH - NESTED LOOPS

In general, (# times the loops run) * (work done each time)

```
def factorial (n):
     # returns n! in linear time
def foo (n):
     # nested loop runs n^2 times
     for i in range(n):
          for j in range(n):
               # each time this takes theta(n) time
               print(factorial(n))
```

• foo(n) runs in $\Theta(n^3)$ time

LAB Q5

NOW IT'S YOUR TIME W

- Get started on the lab and raise your hand whenever you need help!
- Get to know your neighbors and collaborate if you'd like!
- Slides: go.cs61a.org/mingxiao-index
- Leave any anonymous feedback here: go.cs61a.org/mingxiao-anon

AND REMEMBER TO GET CHECKED OFF!

go.cs61a.org/mingxiao-att

The secret phrase is ...
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