

Laboratory 4: Postlab

Date 3/1/2022 Section 02
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Recursive Procedures (cont'd)

Now that you have enough experience with the procedure call mechanism in MIPS it is time to try something harder on your own.

A famous example of a recursive function is *Ackermann's function* $A(x, y)$:

- if $x = 0$ then $y+1$
- else if $y = 0$ then $A(x-1, 1)$
- else $A(x-1, A(x, y-1))$

Step 1

Write a program in C/C++ (named *lab4.6.c*) which:

- asks the user for two non-negative integers, x and y
- outputs the value of the Ackermann's function for those two values, $A(x, y)$

Run the program and fill out the missing parts of the following test table

Test plan for the C/C++ Ackermann's function

x	y	$A(x, y)$
0	0	1
0	2	3
1	0	2
2	3	9
2	4	11
2	5	13
2	6	15
3	1	13
3	2	29

Test plan for the C/C++ Ackermann's function

x	y	$A(x, y)$
3	3	61

Note: Do not take large values (especially for x) if you want your program to finish in a reasonable amount of time (or to finish at all). It takes 128 seconds to compute $A(3, 12)$ on an Indigo² running at 250 MHz, with 64 MB main memory, with the code compiled using the cc compiler and the -O2 flag for optimization. On the same machine $A(4, 2)$ exhausts not only the main memory space but also the 100 MB disk swap space.

Step 2

Create a program named *lab4.7.asm* which

- in 'main' prompts the user to enter two non-negative integers; store them in `$t0` and `$t1`
- check if any of the numbers entered is negative: if it is negative, then print a message saying so and prompt the user again for numbers
- call the procedure named 'Ackermann' whose parameters will be the integers read from the user, and which returns the value of the Ackermann's function for those two integers
- pass the parameters in registers
- prints a message and the value returned by 'Ackermann'

Run your program and fill out the missing spaces in the following test plan

Test plan for the MIPS assembly Ackermann's function

x	y	$A(x, y)$
0	0	1
0	2	3
1	0	2
2	3	9
2	4	11
2	5	13
2	6	15
3	1	13
3	2	29
3	3	61

Make sure you obtain the proper values when running your program.

Q 1:

How many recursive calls are made to calculate $A(2, X)$ where X is the first digit of your SSN?

$X =$	3	Recursive calls =	$2x^2 + 7x + 5 = 62$
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Q 2:

Every time a recursive call is made, the stack grows. By how many bytes per call?

8 bytes

Step 3

Return to your lab instructor copies of *lab4.6.c* and *lab4.7.asm* together with this postlab description. Ask your lab instructor whether copies of programs must be on paper (hardcopy), e-mail or both.