

Consider a disk with a sector size of 512 bytes, 2000 tracks per surface, 50 sectors per track, five double-sided platters, and average seek time of 10 msec. Suppose that a block size of 1024 bytes is chosen. Suppose that a file containing 100, 000 records of 100 bytes each is to be stored on such a disk and that no record is allowed to span two blocks.

1. What is the capacity of a track in bytes? What is the capacity of each surface? What is the capacity of the disk?

bytes/track= bytes/sector \times sectors/track = $512 \times 50 = 25,600$ bytes $\approx 25K$

bytes/surface= bytes/track \times tracks/surface = $25,600 \times 2000 = 51,200,000$ bytes $\approx 50,000K$

bytes/disk=bytes/surface \times surfaces/disk = $51,200,000 \times 5 \times 2 = 512,000,000$ bytes

2. How many records fit onto a block?

Block size/ Record size = $1024/100 = 10$. We can have size at most 10 records in a block.

3. How many blocks are required to store the entire file?

File size = # Record \times Record size

File size = $100,000 \times 100 = 10,000,000$ bytes

We need [File size size / block size = $10,000,000 / 1024 = 9765.625 \approx 10,000$ blocks to store

4. If the file is arranged sequentially on the disk, how many surfaces are needed

Sectors/Tracks = 50, Sector size = 512 bytes , Block size = 1024 One track has 25 blocks , One cylinder has $25 \times 5 \times 2 = 250$ blocks. One cylinder has $25 \times 5 \times 2 = 250$ blocks. We need 10,000 blocks to store this file. So , we need $10,000 / 250 = 40$ cylinders We need 10 surfaces to store the file.

5. How many records of 100 bytes each can be stored using this disk?

capacity of the disk is 512,000,000 bytes $\approx 500,000K$, which has $\approx 500,000$ blocks. Each block has 10 records.

this disk can store no more than 512,000,000 $\approx 5,000,000$ records.

On the average, the desired sector will be about half way around the circle when the heads arrive at its cylinder.

Average rotational delay is time for $\frac{1}{2}$ revolution

Example: Given a total revolution of 7200 RPM

- One rotation = $\frac{60s \times 1000}{7200} = 8.33$ ms
- Average rotational latency = 4.16 ms

Suppose a disk with an actual (formatted) capacity of 8 gigabytes (2^{33} bytes). The disk has 16 surfaces and 1024 tracks per surface. The disk rotates at 7200 rpm (rotations per minute). The average seek time is 9 ms. The block size is 8 KB.

1. What is the capacity (in bytes) of a single track?

Capacity of a single surface = $\frac{\text{Disk Capacity}}{\# \text{ Surfaces}} = \frac{8GB}{16} = \frac{2^{33}}{2^4} = 2^{29}$ bytes

Capacity of a single track = $\frac{\text{Single Surface Capacity}}{\# \text{ Tracks/Surface}} = \frac{2^{29}}{2^{10}} = 2^{19} \text{ bytes} = 0.5MB$

2. Suppose we are reading a file that occupies exactly one entire track. How long does it take to read the entire file sequentially?

$$\begin{aligned} \text{Transfer time for one track} &= \text{time for one rotation} = \frac{60s}{7200} = 8.3 \text{ ms} \\ \text{Read time} &= \text{average seek time} + \text{rotational delay} + \text{transfer time for track} \\ &= 9 + \frac{8.3}{2} + 8.3ms = 21.5ms \end{aligned}$$

Consider a hard disk with the following specifications:

- 6000 RPM
- 3.5in in diameter
- 250GB usable capacity
- 100 cylinders, numbered from 1 (innermost) to 100 (outermost).
- Takes $\tau / (1 + 100)$ milliseconds to move the heads across τ cylinders (e.g., from i to $i + \tau$).
- Block size is 32 MB.
- transfer rate is 16 GB/sec.

For this problem 1GB is 10^9 bytes, 1MB is 10^6 bytes.

(a) Based on the specifications, calculate the average rotational delay (in milliseconds) of this disk.

The average rotational delay is half of the maximum rotational delay.

$$\rightarrow \frac{1}{2} \times \frac{60s}{6000} = 5ms$$

(b) Suppose that we have just finished reading a block at track 50, and we next want to read a block at track 10. What is the total read time (time for the desired block to appear in memory)?

We will only consider seek time, rotational delay, and transfer time:

$$1 + \frac{50-10}{100} + 5 + \frac{32 \times 10^6}{16 \times 10^9} \times 10^3 = 8.4ms$$