Dynamic Modeling for Optimal Cryptoeconomic Policies

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I   Introduction

In December 2018, the market capitalization of cryptocurrencies reached nearly 400 billion US Dollars, equivalent to 11% of M1 in the USA (Schilling & Uhlig, 2019b). As the size of blockchain and cryptocurrency networks grew, there has been increasing discussion around volatility and welfare in cryptoeconomies, and ways for the issuer of the cryptocurrency protocol to implement policies to ensure there is sustainable benefits for the network of token holders. These policies are often referred to as the protocol's "tokenomics".

As of today, most cryptoeconomic policies are static, which means the supply of tokens grows or shrinks according to a deterministic mechanism. For example, the supply of Bitcoin grows at a deterministic and decreasing rate. Many protocols cite these static policies act as an important aspect of decentralization: as the protocol pre-commits to a set of token issuance and burning policies, it reduces the requirement for trust from users in the procotol's governance. However, as demonstrated by both academic literature and recent events, the lack of response mechanisms can lead to devastating results when the cryptoeconomy faces exogenous shocks.

In many modern blockchain protocols, "staking" and "burning" are the primary coded policy rules in the underlying blockchain system. Staking is a mechanism where the user chooses to stake their token in the protocol for a period of time, after which the protocol rewards them with a staking yield that is paid out by newly minted tokens. In monetary economics terms, staking increases the total token supply by introducing new tokens into circulation, while reduces the amount of tokens in circulation due to illiquidity of the staked tokens. On the other hand, burning is a mechanism where the protocol burns (permanently destroys) some tokens from the supply, which usually comes from the transaction fees paid by users to conduct blockchain transactions.

Current staking and burning policy rules were primarily designed for the purpose of offering user incentives and/or preventing inflation from over-issuance. Most importantly, they do not respond to shock factors. My research aims to develop a model framework where staking and burning rules can be set dynamically to maximize the welfare of relevant actors in the cryptoeconomy.

This paper is organized as follows: Section II provides an overview of the established literature. Section III outlines the baseline model by Biais et al. (2020) and replicates

its solutions (3.1) and outlines the current progress of my extended model (3.2). Section IV describes the data I plan to use for calibration.

II   Literature Review

My research is related to the emerging literature on modeling cryptocurrencies and the blockchain economy. Following Yermack (2015) that argued that Bitcoin is not a currency, there was an interest in studying Bitcoin as a financial asset. Athey et al. (2016), Biais et al. (2020), Garratt and Wallace (2018), and Pagnotta (2022) studied equilibria in asset pricing models for Bitcoin. Schilling and Uhlig (2019a, 2019b) focused on the interactions between Bitcoin and the real economy, including dollar exchange rate and currency substitution. A broader set of models for Bitcoin include Bolt and Van Oordt (2020), Catalini and Gans (2020), Chiu and Koeppl (2017), Hinzen et al. (2022), and Huberman et al. (2021). For Proof-of-Stake protocols, Saleh (2019, 2021) modeled their general volatility and welfare, while Catalini et al. (2020) examined their tokenomics in the presence of an attack. A common result of the aforementioned asset pricing models is that static token supply causes all shocks are absorbed by the token price, which explains the high volatility of Bitcoin. This provides the motivation for an endogenous token supply in my model, which adds response mechanisms in terms of dynamic policy rules therefore can potentially mitigate the price effect of exogenous shocks.

Another set of literature has attempted to identify optimal policy rules for special types of tokens. Cong et al. (2021, 2022) built an asset pricing model featuring token issuance as means of platform financing and user growth leveraging network effects. Sockin and Xiong (2023a, 2023b) modeled cryptocurrencies as platform utility tokens and discussed elastic token issuance. d'Avernas et al. (2022) studied how stablecoin issuers can profit from seigniorage while maintaining the stablecoin's peg. Fernández-Villaverde et al. (2021) and Zhu and Hendry (2019) are examples of papers proposing optimal monetary policies for CBDCs. While the policy goals of utility tokens are very specific (defending peg for stablecoins/CBDCs, making profit for stablecoins/platform tokens), I adopt the general policy goal of maximizing user welfare, measured by consumption and transactional benefits.

My research is also related to the large literature on cryptocurrencies. Notable empirical researches include Liu and Tsyvinski, 2021 on the risk factors of cryptocurrencies, Makarov and Schoar, 2020 on the arbitrage spreads among different cryptocurrency markets. Griffin and Shams, 2020 studied the relationship between Tether purchases and cryptocurrency prices. Studies on the microeconomics of blockchain mechanisms include Biais et al. (2019), Budish (2018), Gans and Gandal (2019), Gans and Holden (2022), and Huberman et al. (2021).

III   Model

3.1   Baseline model

This model was proposed by Biais, Bisiere, Bouvard, Casamatta, and Menkveld in their 2020 paper in The Journal of Finance titled "Equilibrium Bitcoin Pricing". Their main

idea is that the fundamental value of cryptocurrencies comes from the stream of future transactional benefits (e.g. access to unique goods, not expropriated/taxed/constrained by government, direct internet access). The primary result is that Bitcoin price changes partly due to changes in fundamentals (net transactional benefits) but mostly due to extrinsic volatility.

The model is a two-period cryptoeconomy with overlapping generations of users. The cryptoeconomy includes three representative agents (user, validator, and hacker), three financial assets (risk-free asset, standard currency, and cryptocurrency). It features a fixed schedule money supply.

3.1.1 Users

In each period, young users receive some endowment in numeraire goods, which they spend on consumption goods and the three financial assets. They pay a fee on any cryptocurrency purchased. Old users consume all their savings from the previous period and receive transactional benefits on their cryptocurrencies. A portion of their crypto savings gets hacked. The users' budget constraints are:

$$c_t^y = e_t - s_t - (1 + \varphi_t)q_t p_t - \hat{q}_t \hat{p}_t \tag{1}$$

$$c_{t+1}^o = s_t(1 + r_t) + (1 - h_{t+1})q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1}$$
$$+ \theta_{t+1}(1 - h_{t+1})q_t p_{t+1} \tag{2}$$

e_t: endowment
s_t: quantity of risk-free assets held
$q_t, \hat{q}_t$: quantities of crypto and dollars held
$p_t, \hat{p}_t$: prices (in units of consumption goods) of crypto and dollars
h_{t+1}: portion of crypto hacked by hackers
φ_t: transaction fees involved in using crypto (exog.)[1]
θ_{t+1}: transactional benefits from using crypto (exog.) (assume $\theta_{t+1} \geq -1$)

3.1.2 Validators

Validators receive newly minted tokens as block rewards, similar to a lump-sum transfer of money. The validators' budget constraint is:

$$c_{t+1}^v = (X_{t+1} - X_t)p_{t+1} + \varphi_{t+1}q_{t+1}p_{t+1} \tag{3}$$

X_t: stock token supply
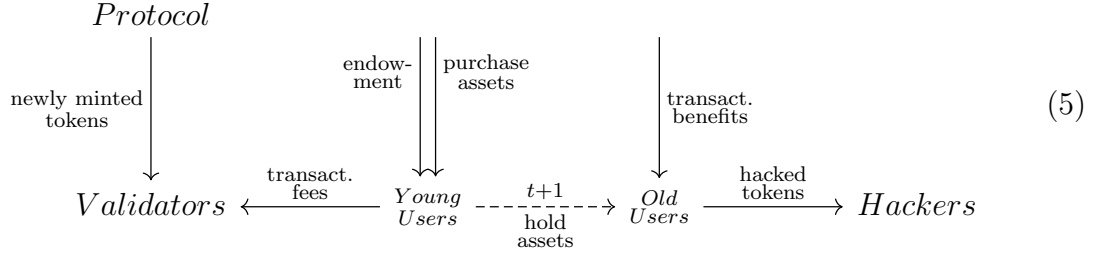$X_{t+1} - X_t$: increase in token supply (newly minted tokens)

3.1.3 Hackers

Hackers hack a portion of users' crypto. The hackers' budget constraint is:

$$c_{t+1}^h = h_{t+1}q_t p_{t+1} \tag{4}$$

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[1]The analysis remain largely unchanged if we include a transaction cost when selling crypto in period $t + 1$ as well.

I made a graph summarizing of the interaction of the agents in two periods: Figure 5.

$$Protocol$$

newly minted tokens | endowment | purchase assets | transact. benefits

$$Validators \xleftarrow{\text{transact. fees}} \begin{array}{c} Young \\ Users \end{array} \dashrightarrow[\text{hold assets}]{t+1} \begin{array}{c} Old \\ Users \end{array} \xrightarrow{\text{hacked tokens}} Hackers \qquad (5)$$

3.1.4 Solution

Here are my own steps for obtaining the pricing equations for cryptocurrency and standard currency.
The market clearing condition for the three financial assets are:

$$\text{crypto: } q_t = X_t \qquad (6)$$
$$\text{dollars: } \hat{q}_t = m \qquad (7)$$
$$\text{risk-free assets: } s_t = 0 \qquad (8)$$
$$(9)$$

Market for consumption goods also clears (by Walras's Law):

$$c_t^y + c_t^o + c_t^v + c_t^h = e_t \qquad (10)$$

A young user in period t solves:

$$\max_{s_t, q_t, \hat{q}_t} u(c_t^y) + \beta \mathbb{E}_t u(c_{t+1}^o) \qquad (11)$$

subject to user's budget constraints and $c_t^y \geq 0$

* Information set at period t includes $\{\theta_t, \varphi_t, \pi_t\}$
The Lagrangian is

$$\begin{aligned}
\mathcal{L} &= u(c_t^y) + \beta \mathbb{E}_t u(c_{t+1}^o) + \lambda c_t^y \\
&= u(e_t - s_t - (1 + \varphi_t) q_t p_t - \hat{q}_t \hat{p}_t) \\
&\quad + \beta \mathbb{E}_t \left[u(s_t(1 + r_t) + (1 - h_{t+1}) q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1} + \theta_{t+1}(1 - h_{t+1}) q_t p_{t+1}) \right] \\
&\quad + \lambda(e_t - s_t - (1 + \varphi_t) q_t p_t - \hat{q}_t \hat{p}_t) \qquad (12)
\end{aligned}$$

First-order conditions:

$$s_t : -u'(c_t^y) + \beta(1 + r_t)\mathbb{E}_t[u'(c_{t+1}^o)] = \lambda \qquad (13)$$
$$q_t : -(1 + \varphi_t) p_t u'(c_t^y) + \beta \mathbb{E}_t[u'(c_{t+1}^o)(1 - h_{t+1})(1 + \theta_{t+1}) p_{t+1}] = \lambda(1 + \varphi_t) p_t \qquad (14)$$
$$\hat{q}_t : -\hat{p}_t u'(c_t^y) + \beta \mathbb{E}_t[u'(c_{t+1}^o)\hat{p}_{t+1}] = \lambda \hat{p}_t \qquad (15)$$

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For Eqn. 14, substitute λ with LHS of Eqn. 13:

$$-(1+\varphi_t)p_t u'(c_t^y) + \beta\mathbb{E}_t[u'(c_{t+1}^o)(1-h_{t+1})(1+\theta_{t+1})p_{t+1}]$$
$$= (1+\varphi_t)p_t\{-u'(c_t^y) + \beta(1+r_t)\mathbb{E}_t[u'(c_{t+1}^o)]\} \tag{16}$$
$$\Rightarrow$$

$$\beta\mathbb{E}_t[u'(c_{t+1}^o)(1-h_{t+1})(1+\theta_{t+1})p_{t+1}]$$
$$= (1+\varphi_t)p_t\beta(1+r_t)\mathbb{E}_t[u'(c_{t+1}^o)] \tag{17}$$
$$\Rightarrow$$

$$p_t = \frac{1}{1+r_t}\frac{1}{1+\varphi_t}\mathbb{E}_t[u'(c_{t+1}^o)]^{-1}\mathbb{E}_t[u'(c_{t+1}^o)(1-h_{t+1})(1+\theta_{t+1})p_{t+1}] \tag{18}$$

Eqn. 18 is the pricing equation for cryptocurrency. Intuitively, $\frac{1}{1+r_t}$ is a discount by the interest rate, $1-h_{t+1}$ is the hack risk, $\frac{1+\theta_{t+1}}{1+\varphi_t}$ measures the net transactional benefits generating the currency's fundamental value, $\mathbb{E}_t[u'(c_{t+1}^o)]^{-1}u'(c_{t+1}^o)$ is the risk-neutral probability, and p_{t+1} is the resale value. This pricing equation provides a viewpoint that Bitcoin prices reflect both fundamentals and extrinsic factors.

We can also consider Eqn. 15, and substitute λ with LHS of Eqn. 13:

$$-\hat{p}_t u'(c_t^y) + \beta\mathbb{E}_t[u'(c_{t+1}^o)\hat{p}_{t+1}]$$
$$= \hat{p}_t\{-u'(c_t^y) + \beta(1+r_t)\mathbb{E}_t[u'(c_{t+1}^o)]\} \tag{19}$$
$$\Rightarrow$$

$$\beta\mathbb{E}_t[u'(c_{t+1}^o)\hat{p}_{t+1}]$$
$$= \hat{p}_t\beta(1+r_t)\mathbb{E}_t[u'(c_{t+1}^o)] \tag{20}$$
$$\Rightarrow$$

$$\hat{p}_t = \frac{1}{1+r_t}\mathbb{E}_t[u'(c_{t+1}^o)]^{-1}\mathbb{E}_t[u'(c_{t+1}^o)\hat{p}_{t+1}] \tag{21}$$

Eqn. 21 provides an expression for the return on dollars in the cryptoeconomy, in relation to the risk-neutral probability as well as the interest rate.
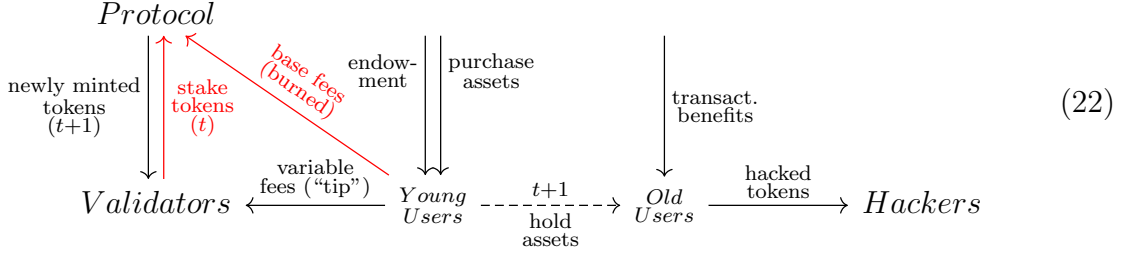
3.2 Extended model

3.2.1 Staking and burning

In my extended model, I introduce two new mechanisms:

- Two-part transaction fee with burning

- Interest-bearing staking

The protocol controls the staking yield ("interest rate") and the base transaction fee rate (burn rate). The figure below illustrates the new dynamics:

$$\text{(22)}$$

Define new variables as follows:

L_t: amount of staked tokens
δ_t: staking yield (set by protocol)
φ_t^b: base fee (set by protocol)
φ_t^v: variable fee (competitively determined by validators and users)

The new budget constraints are:

$$\text{Young users: } c_t^y = e_t - s_t - (1 + \varphi_t^b + \varphi_t^v)q_t p_t - \hat{q}_t \hat{p}_t \tag{23}$$

$$\text{Old users: } c_{t+1}^o = s_t(1 + r_t) + (1 - h_{t+1})q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1}$$
$$+ \theta_{t+1}(1 - h_{t+1})q_t p_{t+1} \tag{24}$$

$$\text{Validators: } c_{t+1}^v = (1 + \delta_t)L_t p_{t+1} + \varphi_{t+1}^v q_{t+1} p_{t+1} - L_{t+1}p_{t+1} \tag{25}$$

$$\text{Hackers: } c_{t+1}^h = h_{t+1}q_t p_{t+1} \tag{26}$$

3.2.2 Endogenous token supply

Instead of a predetermined exogenous supply of tokens, now the supply is endogenous and dependent on the staking yield and base fee rate:

$$M_{t+1} = (M_t - L_t) + L_t(1 + \delta_t) - \varphi_t^b X_t$$
$$= M_t + \delta_t L_t - \varphi_t^b X_t \tag{27}$$

M_t: total token supply
$X_t \equiv M_t - L_t$: circulating supply (Now the market clearing condition is $X_t = q_t$)

3.2.3 Validator's problem

Since the amount staked is an active choice by the validators, we now have a new optimization problem by the validators:

$$\max_{L_{t+1}} u((1 + \delta_t)L_t p_{t+1} + \varphi_{t+1}^v q_{t+1} p_{t+1} - L_{t+1}p_{t+1}) \tag{28}$$

$$\text{s.t. } q_{t+1} \leq M_{t+1} - L_{t+1}$$

This problem describes the following trade off by the validators:

$$\text{more staking at } t \Rightarrow \begin{cases} \text{more staking yield at } t + 1 \\ \text{less circulating supply} \Rightarrow \text{less transact. fees at } t \end{cases}$$

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Intuitively, the budget constraint should be binding since there should not be idle tokens in the economy: all tokens either enter the circulating supply or be staked to generate yields. Formally, we can apply Karush-Kuhn-Tucker to solve the optimization problem.

The solution to this problem, and a general equilibrium solution for the extended model, are currently work in progress.

IV Data

The model describes the relationship between a cryptocurrency's prices and its transactional benefits, transaction costs, and hacking risks. As such, I choose the Ethereum blockchain, the second largest blockchain by size today, as the main cryptoeconomy of interest. It native token Ether (ETH) is the largest utility token and second largest cryptocurrency by market capitalization.

Ether is the native token of the Ethereum protocol, which was originally founded in 2014 by Vitalik Buterin as a Proof-of-Work blockchain. In August 2021, the Ethereum blockchain implemented an upgrade referred to as Ethereum Improvement Proposal #1559 or EIP-1559. EIP-1559 introduced a two-part transaction fee mechanism with an instantly-burned "base fee" for their transactions to be included in the next block, and a "priority fee" to pay validators for faster inclusion. In September 2022, Ethereum migrated from a Proof-of-Work (PoW) to Proof-of-Stake (PoS) consensus model (commonly known as "the Merge"), mandating validator staking as the only source of new ETH tokens. Staking and burning together controls the supply of ETH on the blockchain.

4.1 Prices

The data set starts on September 16th, 2022, with the implementation of the Merge, and ends on September 31, 2023. I used time series data of daily ETH-USD prices provided by Messari[2]. For robustness checks, I follow Biais et al., 2020 to construct time series based on ETH prices denominated in five different currencies from 20 major exchanges. For non-USD denominations, I converted the prices using daily USD exchange rates data from Federal Reserve Economic Data (FRED).

4.2 Transaction fees

By design of the Ethereum blockchain, information on all historical transactions are publicly visible onchain. For each transaction, I retrieved its value and the associated base fee and priority fee through onchain data provider Dune Analytics[3]. Daily transaction volumes are computed by summing the value of all transactions in that day. Daily base fees and priority fees are computed by summing $BaseFee_i = GasUsed_i * BaseFeePerGas_j$ and $PriorityFee_i = GasUsed_i * PriorityFeePerGas_i$, respectively over each transaction i in block j produced in the day. Daily fee rates are then converted into percentages of the daily transaction volume.

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[2]https://messari.io/
[3]https://dune.com/

Admittedly, this simplified approach does not take into account self-transactions i.e. transfer of funds between different wallet addresses that belong to the same entity. Unfortunately due to the anonymity of the Ethereum blockchain, it is difficult to identify such self-transactions.

4.3   Transaction benefits

To measure the benefits of using ETH as a medium of transaction, I use a popular metric called Network Value to Transactions (NVT) ratio. The NVT ratio was originally constructed as an indicator for over- or under-priced tokens, similar to the P/E ratio for traditional equities. Intuitively, the NVT ratio measures how much an average user is willing to pay for a utility token for each unit of transaction volume denominated in that token.

4.4   Staking

Similar to transactions data, staking data has also been published in real-time on the Ethereum blockchain. I retrieved daily data on total ETH staked and ETH minted as validator rewards from open source Ethereum explorer beaconcha.in[4]. I then subtract any ETH burned as a result of slashing or other types of validator penalties from ETH minted.

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[4]https://beaconcha.in

Appendices

A Proofs

A.1 Solution for deterministic model

$$\text{Young users:} \qquad c_t^u = e_t^u - s_t - (1 + \varphi_t^b + \varphi_t^v)q_t p_t - \hat{q}_t \hat{p}_t \tag{29}$$

$$\text{Old users:} \qquad c_{t+1}^u = s_t(1 + r_t) + (1 - h_{t+1})(1 + \theta_{t+1})q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1} \tag{30}$$

$$\text{Young validators:} \qquad c_t^v = e_t^v + \varphi_t^v q_t p_t - L_t p_t \tag{31}$$

$$\text{Old validators:} \qquad c_{t+1}^v = (1 + \delta_t)L_t p_{t+1} \tag{32}$$

$$\text{Hackers:} \qquad c_{t+1}^h = h_{t+1}q_t p_{t+1} \tag{33}$$

User's problem:

$$\max_{s_t, q_t, \hat{q}_t} \quad u\left(e_t^u - s_t - (1 + \varphi_t^b + \varphi_t^v)q_t p_t - \hat{q}_t \hat{p}_t\right)$$
$$+ \beta u\left(s_t(1 + r_t) + (1 - h_{t+1})q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1}\right) \tag{34}$$

FOCs:

$$\frac{\partial}{\partial s_t} : -u'(c_t^u) + \beta(1 + r_t)u'(c_{t+1}^u) = 0 \tag{35}$$

$$\frac{\partial}{\partial q_t} : -(1 + \varphi_t^b + \varphi_t^v)p_t u'(c_t^u) + \beta(1 - h_{t+1})(1 + \theta_{t+1})p_{t+1}u'(c_{t+1}^u) = 0 \tag{36}$$

$$\frac{\partial}{\partial \hat{q}_t} : -\hat{p}_t u'(c_t^u) + \beta \hat{p}_{t+1}u'(c_{t+1}^u) = 0 \tag{37}$$

Result:

$$\Rightarrow \frac{u'(c_t^u)}{u'(c_{t+1}^u)} = \beta(1 + r_t) = \beta\frac{(1 + \theta_{t+1})(1 - h_{t+1})}{1 + \varphi_t^b + \varphi_t^v}\frac{p_{t+1}}{p_t} = \beta\frac{\hat{p}_{t+1}}{\hat{p}_t} \tag{38}$$

Validator's problem:

$$\max_{L_t} \quad u(e_t^v + \varphi_t^v q_t p_t - L_t p_t) + \beta u((1 + \delta_t)L_t p_{t+1}) \tag{39}$$

FOC:

$$-p_t u'(c_t^v) + \beta p_{t+1}(1 + \delta_t)u'(c_{t+1}^v) = 0 \tag{40}$$

Result:

$$\Rightarrow \frac{u'(c_t^v)}{u'(c_{t+1}^v)} = \beta(1 + \delta_t)\frac{p_{t+1}}{p_t} \tag{41}$$

With log utility:

$$u(c_t) = \ln c_t \Rightarrow \frac{u'(c_t)}{u'(c_{t+1})} = \frac{c_{t+1}}{c_t} \tag{42}$$

User (Solve for token demand q_t):

Combine the consumer budget equations by substituting s_t:

$$c_{t+1}^u = (1 + r_t)\left[e_t^u - c_t^u - (1 + \varphi_t^b + \varphi_t^v)q_t p_t - \hat{q}_t \hat{p}_t\right]$$
$$+ (1 + \theta_{t+1})(1 - h_{t+1})q_t p_{t+1} + \hat{q}_t \hat{p}_{t+1} \tag{43}$$

To be continued...

Validator (solve for amount staked $L_t \to$ token supply $X_t = M_t - L_t$):

$$\frac{c_{t+1}^v}{c_t^v} = \frac{(1+\delta_t)L_t p_{t+1}}{e_t^v + \varphi_t^v q_t p_t - L_t p_t} = \beta(1+\delta_t)\frac{p_{t+1}}{p_t} \tag{44}$$

$$L_t = \beta\left(\frac{e_t^v}{p_t} + \varphi_t^v q_t - L_t\right) \tag{45}$$

$$L_t = \frac{\beta}{1+\beta}\left(\frac{e_t^v}{p_t} + \varphi_t^v q_t\right) \tag{46}$$

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