# STA 371G Outline Fall 2017

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Office Hours: Monday & Wednesday 5:00-6:15 PM. You are welcome to come by my

office at other times.

## Wednesday, August 30

#### Topics:

- Introduction
- Probability
- Random variables

# Reading Assignments:

You are recommended to read:

Chapter 1 of OpenIntro Statistics, 3rd edition

### Wednesday, September 6

#### **Topics:**

- Probability distributions
- Mean, variance and standard deviation of a random variable

### Reading Assignments:

If you are not familiar with the topics discussed in class, you are recommended to read:

pp. 156-168, 189-195, of Data analysis and decision making, 4th edition

or

pp. 196-206, 225-231 of Data analysis and decision making, 3rd edition

You are also recommended to read:

pp. 1-14 of "1 TopicSummary\_ProbabilityConceptsAndNormalDistributions.pdf" (available in Canvas/files)

To learn more about these topics, you may further read:

Chapters 2.1, 2.2, 2.4, and 2.5 of OpenIntro Statistics, 3rd edition

## Monday, September 11

- Add a constant to a random variable
- Multiply a random variable by a constant
- Independent random variables, sum of independent random variables
- Continuous random variables
- Probability density function: area under the curve represents probability
- Standard normal distribution  $Z \sim \mathcal{N}(0,1)$
- Normal distribution  $X \sim \mathcal{N}(\mu, \sigma^2)$

#### Reading Assignments:

To get familiar with the normal distribution, you are recommended to read: pp. 211-215, 217-225 of Data analysis and decision making, 4th edition

or

pp. 247-250, 253-260 of Data analysis and decision making, 3rd edition

You are also recommended to read:

pp. 15-30 of "1TopicSummary\_ProbabilityConceptsAndNormalDistributions.pdf" (available in Canvas/files)

You may further read:

Chapters 3.1.1, 3.1.2, 3.1.4 and 3.1.5 of OpenIntro Statistics, 3rd edition

#### Wednesday, September 13

- If  $X \sim \mathcal{N}(\mu, \sigma^2)$ , then  $P(X < x) = P(\frac{X-u}{\sigma} < \frac{x-u}{\sigma}) = P(Z < \frac{x-u}{\sigma})$ .
- Standard normal calculations in Excel: NORMSDIST, or in R: pnorm (type "?pnorm" in R for help).
- Understand the meaning of the standard deviation  $\sigma$  in a normal distribution:  $P(\mu \sigma < X < \mu + \sigma) = ?$  and  $P(\mu 2\sigma < X < \mu + 2\sigma) = ?$
- Normal calculations in Excel:

NORMSDIST, NORMDIST

NORMSINV, NORMINV

or in R:

pnorm, qnorm (type "?pnorm" and "?qnorm" in R for help).

- Standardizing a normal random variable  $Z = \frac{X-\mu}{\sigma} \sim \mathcal{N}(0,1)$ Interpretation: the value of Z is the number of standard deviations that X deviates towards the left (if Z < 0) or the right (if Z > 0) of the mean.
- Plot a normal distribution in Excel and R

## Monday, September 18

- Example: Testing at ZTel, we will make an Excel spreadsheet for calculations
- Case study, Texas BBA Salary Statistics
- Expectation of a continuous random variable
- Population mean, variance, standard deviation
- Sample mean, sample variance, standard error of the sample mean
- Sampling distribution of the sample mean

### Reading Assignments:

To learn more about estimation and sampling distribution, please read:

pp. 352-353, 366-371, 374, 388-395 of Data analysis and decision making, 4th edition or

pp. 378-379, 393-398, 400-401, 422-430 of Data analysis and decision making, 3rd edition

You are also recommended to read:

"2TopicSummary\_EstimationAndSamplingDistributions.pdf" (available in Canvas/files)

For this topic, you may further read:

Chapters 4.1, 4.2, 4.4 and 5.3 of OpenIntro Statistics, 3rd edition

#### Wednesday, September 20

- Sampling distribution of the sample mean
- Confidence interval
- Simple linear regression
- Linear prediction:  $Y = b_0 + b_1 X$

### Reading Assignments:

Chapters 7.1 and 7.2 of OpenIntro Statistics, 3rd edition

pp. 531-551 of Data analysis and decision making, 4th edition or

pp. 562-584 of Data analysis and decision making, 3rd edition

# Monday, September 25

- Least squares estimation of  $b_0$  and  $b_1$
- Examples: predict house price, baseball runs per game

- Using Excel and R to do the calculation
- Excel add-in: Palisade Decision Tools (including StatTools) for Windows, StatPlus:mac LE for Mac.
- Sample mean, variance, and standard deviation
- Sample covariance, sample correlation

### Reading Assignments:

PDF "Simple Linear Regression" posted in Canvas/files

## Wednesday, September 27

- $\bullet$  Linear relationship between X and Y
- $b_0 = \bar{y} b_1 \bar{x}, b_1 = r_{xy} \times \frac{s_y}{s_x}$
- $\operatorname{mean}(e)=0$ ,  $\operatorname{Corr}(e,X)=0$ ,  $\operatorname{Corr}(e,\hat{Y})=0$ ,  $\operatorname{Corr}(\hat{Y},X)=1$
- SST, SSR, SSE
- Coefficient of determination:  $R^2 = \frac{SSR}{SST} = 1 \frac{SSE}{SST}$
- $R^2 = r_{xy}^2$  measures the proportion of variation in Y explained by X.
- Statistical model for simple linear regression
- Statistical model for simple linear regression:

$$Y = \beta_0 + \beta_1 X + \epsilon, \ \epsilon \sim \mathcal{N}(0, \sigma^2)$$
$$Y \sim \mathcal{N}(\beta_0 + \beta_1 X, \sigma^2)$$

- ullet Conditional distribution of Y given X
- 95% prediction interval of Y given X:  $\beta_0 + \beta_1 X \pm 2\sigma$

#### Reading Assignments:

- "3TopicSummary\_RegressionModelAndEstimation.pdf" (available in Canvas/files)
- "5TopicSummary\_CorrelationAndCovariance.pdf" (available in Canvas/files)
- "6TopicSummary\_ComputingAndInterpretingRSquare.pdf" (available in Canvas/files)
- "7TopicSummary\_InterpretingAndEstimatingVarianceOfEpsilon.pdf" (available in Canvas/files)

### Monday, October 2

- Conditional and marginal distributions of Y
- Interpretation of  $\epsilon$  and  $\sigma$

- The error terms  $\epsilon_i$  are independent, and identically distributed
- Least squares estimation and Gaussian maximum likelihood (optional)
- True line  $\beta_0 + \beta_1 X$  and least squares line  $b_0 + b_1 X$
- Case study: A stock's beta coefficient

# Wednesday, October 4

- Case study: Milk and Money
- Degrees of freedom
- In SLR,  $\sigma^2$  is estimated with  $s^2 = \frac{\sum_{i=1}^n e_i^2}{n-2} = \frac{SSE}{n-2}$ .
- SLR regression standard error:  $s = \sqrt{SSE/(n-2)}$
- Sampling distributions of regression parameters
- Confidence intervals of regression parameters

# Monday, October 9

- Hypothesis testing in SLR: t-statistic and p-value
- Discuss Practice Exam #1
- Common problems in homework assignments
- Topic summary for Midterm #1

### Wednesday, October 11

• Midterm Exam #1, 7:00-9:30 pm

# Monday October 16

- Multiple regression
- T-test
- Examples: Auto MPG, Baseball

#### Wednesday, October 18

• Example: Supervisor performance data

- F-test
- Understanding multiple regression
- Correlation and causation
- Multicollinearity
- Example: Number of beer and weight & height

# Monday, October 23

- Multicollinearity
- Dummy variables and interactions
- Example: Gender Discrimination in Salary at Fifth National Bank
- Case study: Orion Bus Industries—Contract Bidding Strategy

# Wednesday, October 25

- Example: MidCity House Price
- Diagnostics
- Polynomial regression

#### Reading Assignments:

Chapters 10, 11.1-11.5, and 11.8-11.11 of Data analysis and decision making, 4th edition or

Chapters 11, 12.1-12.5, and 12.8-12.11 of Data analysis and decision making, 3rd edition

"4TopicSummary\_NonlinearRelationships.pdf" (available in Canvas/files)

### Monday, October 30

- Slides 3.3 pages 25-46
- Variable interaction
- Log transformation
- Case Study, Oakland A's (A)
- Case Study, Oakland A's (B)

#### Reading Assignments:

 $"9Topic Summary\_Measuring The Quality Of The Estimate Of Beta.pdf" \ (available in Canvas/files)$ 

"10TopicSummary\_HypothesisTestingInRegression.pdf" (available in Canvas/files)

### Wednesday, November 1

- Slides 4.1, Slides 4.2 pages 1-15
- Time series: fitting a trend
- Autocorrelation
- Time series regression, Hotel Occupancy Case

### Reading Assignments:

Chapter 12 of Data analysis and decision making, 4th edition or

Chapter 13 of Data analysis and decision making, 3rd edition

## Monday, November 6

- Slides 4.2 pages 16-end, Slides 4.3 pages 1-15
- Random walk models
- Autoregressive models
- Example: Monthly stock closing prices
- Example: Daily/Monthly temperature
- Example: Monthly Boston Armed Robberies Jan.1966-Oct.1975
- Seasonal models
- Example: Fisher river daily temperatures

#### Reading Assignments:

"8TopicSummary\_ForecastingModelForSPSSSales.pdf" (available in Canvas/files)

#### Wednesday, November 8

- Slides 4.3 pages 16-end
- Example: Monthly airline passengers
- Case study: Northern Napa Valley Winery, Inc.
- Example: Monthly liquor sales

# Monday, November 13

- Slides 3.3 page 47-end, Slides 5, Slides 6.1 pages 1-3
- Outliers
- Moving averages, exponential smoothing and ARMA
- Hypothesis testing: Type I Error, Type II Error, significant level, and power
- Understanding prediction errors in linear regression
- Model selection
- Measure uncertainty with probability
- Frequency probability and subjective probability

# Wednesday, November 15

 $\bullet$  Midterm Exam #2