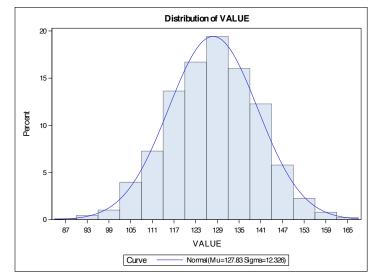
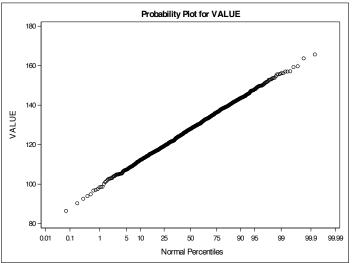
The UNIVARIATE Procedure Variable: VALUE

| Moments | | | | | |
|------------------------|------------|-------------------------|------------|--|--|
| N | 880 | Sum Weights | 880 | | |
| Mean | 127.833523 | Sum Observations | 112493.5 | | |
| Std Deviation | 12.3263345 | Variance | 151.938523 | | |
| Skewness | -0.0503064 | Kurtosis | -0.056344 | | |
| Uncorrected SS | 14513994.4 | Corrected SS | 133553.962 | | |
| Coeff Variation | 9.64248992 | Std Error Mean | 0.41552065 | | |

| Basic Statistical Measures | | | | | | |
|----------------------------|----------------------|---------------------|-----------|--|--|--|
| Loca | Location Variability | | | | | |
| Mean | 127.8335 | Std Deviation | 12.32633 | | | |
| Median | 128.0300 | Variance | 151.93852 | | | |
| Mode | 121.0400 | Range | 79.23000 | | | |
| | | Interquartile Range | 17.03500 | | | |

| Tests for Normality | | | | | |
|---------------------|------------------------------|----------|-----------|---------|--|
| Test | Test Statistic p Value | | | | |
| Shapiro-Wilk | W 0.99942 Pr < W 0 | | | | |
| Kolmogorov-Smirnov | D | 0.015657 | Pr > D | >0.1500 | |
| Cramer-von Mises | W-Sq | 0.01714 | Pr > W-Sq | >0.2500 | |
| Anderson-Darling | A-Sq | 0.105707 | Pr > A-Sq | >0.2500 | |





1. The mean and median of systolic blood pressure is 127.83 and 128.03, with standard deviation 12.33. Since mean is less than median, the distribution is likely to have a long tail to the left. The negative skewness -0.05 supports it. Range is summarized as 79.23.

Systolic blood pressure seems to follow normal distribution. We can clearly the histogram is symmetric. The quantitative test results agree. Shapiro-Wilk, Kolmogorov-Smirnov, Cramer-von Mises, and Anderson-Darling test (H0: normal distribution fits data) show p-value greater than 0.05, thus we cannot reject null hypothesis. We should assume normality for systolic blood pressure.

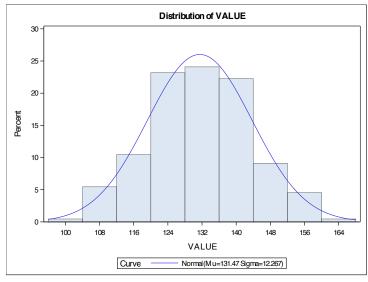
The UNIVARIATE Procedure Variable: VALUE

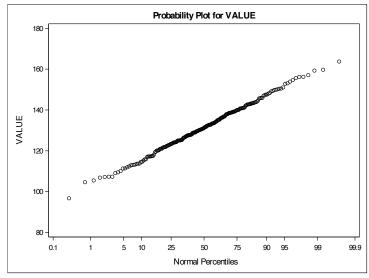
RTRTN=1

| Moments | | | | | |
|------------------------|------------|-------------------------|------------|--|--|
| N | 220 | Sum Weights | 220 | | |
| Mean | 131.468818 | Sum Observations | 28923.14 | | |
| Std Deviation | 12.2674483 | Variance | 150.490288 | | |
| Skewness | -0.0010869 | Kurtosis | -0.2313581 | | |
| Uncorrected SS | 3835448.41 | Corrected SS | 32957.3731 | | |
| Coeff Variation | 9.33107065 | Std Error Mean | 0.8270712 | | |

| Basic Statistical Measures | | | | | |
|----------------------------|----------------------|----------------------|-----------|--|--|
| Loca | Location Variability | | | | |
| Mean | 131.4688 | Std Deviation | 12.26745 | | |
| Median | 131.2050 | Variance | 150.49029 | | |
| Mode | 121.0400 | Range | 66.95000 | | |
| | | Interquartile Range | 16.53500 | | |

| Tests for Normality | | | | | | |
|---------------------|--|----------|-----------|---------|--|--|
| Test | Statistic p Value | | | | | |
| Shapiro-Wilk | W 0.99743 Pr < W 0 | | | | | |
| Kolmogorov-Smirnov | D | 0.026652 | Pr > D | >0.1500 | | |
| Cramer-von Mises | \mathbf{w} W-Sq 0.014424 Pr > W-Sq >0.2 | | >0.2500 | | | |
| Anderson-Darling | A-Sq | 0.115705 | Pr > A-Sq | >0.2500 | | |

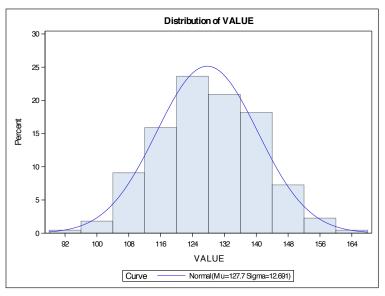


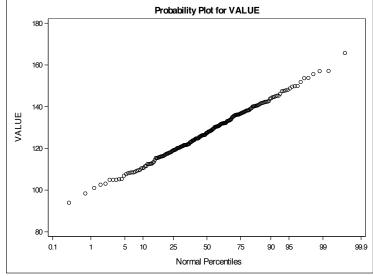


| Moments | | | | | |
|------------------------|-------------------------------|-------------------------|------------|--|--|
| N | 220 | Sum Weights | 220 | | |
| Mean | 127.699136 | Sum Observations | 28093.81 | | |
| Std Deviation | Deviation 12.6911749 Variance | | 161.065919 | | |
| Skewness | 0.07224663 | Kurtosis | -0.2093769 | | |
| Uncorrected SS | 3622828.71 | Corrected SS | 35273.4363 | | |
| Coeff Variation | 9.9383404 | Std Error Mean | 0.85563883 | | |

| Basic Statistical Measures | | | | | | |
|----------------------------|----------------------|---------------------|-----------|--|--|--|
| Loca | Location Variability | | | | | |
| Mean | 127.6991 | Std Deviation | 12.69117 | | | |
| Median | 127.4250 | Variance | 161.06592 | | | |
| Mode | 112.4600 | Range | 71.74000 | | | |
| | | Interquartile Range | 17.60000 | | | |

| Tests for Normality | | | | | |
|---------------------|--------------------------------------|----------|-----------|---------|--|
| Test | Statistic p Value | | | | |
| Shapiro-Wilk | W 0.997674 Pr < W 0 | | | | |
| Kolmogorov-Smirnov | D | 0.031239 | Pr > D | >0.1500 | |
| Cramer-von Mises | W-Sq | 0.022743 | Pr > W-Sq | >0.2500 | |
| Anderson-Darling | A-Sq | 0.142688 | Pr > A-Sq | >0.2500 | |





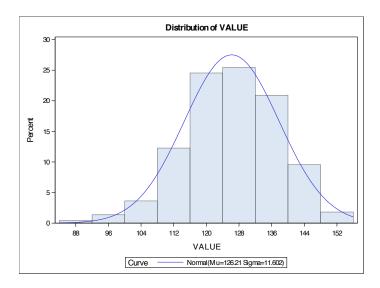
The UNIVARIATE Procedure Variable: VALUE

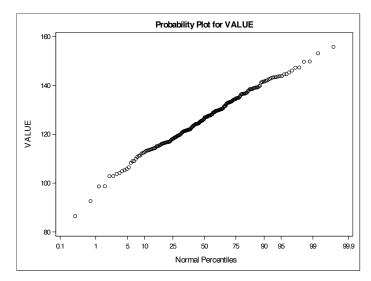
RTRTN=3

| Moments | | | | | |
|------------------------|------------|-------------------------|------------|--|--|
| N | 220 | Sum Weights | 220 | | |
| Mean | 126.213227 | Sum Observations | 27766.91 | | |
| Std Deviation | 11.60215 | Variance | 134.609884 | | |
| Skewness | -0.2289691 | Kurtosis | 0.15971785 | | |
| Uncorrected SS | 3534030.89 | Corrected SS | 29479.5646 | | |
| Coeff Variation | 9.19249925 | Std Error Mean | 0.78221679 | | |

| | Basic Statistical Measures | | | | | |
|--------|----------------------------|---------------------|-----------|--|--|--|
| Loca | Location Variability | | | | | |
| Mean | 126.2132 | Std Deviation | 11.60215 | | | |
| Median | 126.5500 | Variance | 134.60988 | | | |
| Mode | 116.2300 | Range | 69.32000 | | | |
| | | Interquartile Range | 16.38500 | | | |

| Tests for Normality | | | | | | |
|---|-------------------|----------|------------------------------|---------|--|--|
| Test | Statistic p Value | | | | | |
| Shapiro-Wilk | W | 0.993893 | 993893 Pr < W 0.50 | | | |
| Kolmogorov-Smirnov | D | 0.028123 | Pr > D | >0.1500 | | |
| Cramer-von Mises W-Sq 0.028136 Pr > W-Sq >0 | | >0.2500 | | | | |
| Anderson-Darling | A-Sq | 0.24813 | Pr > A-Sq | >0.2500 | | |





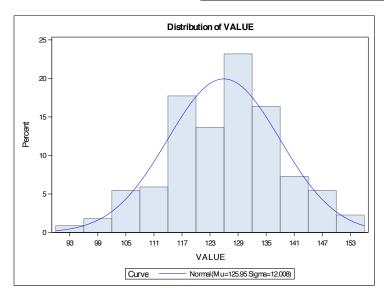
The UNIVARIATE Procedure Variable: VALUE

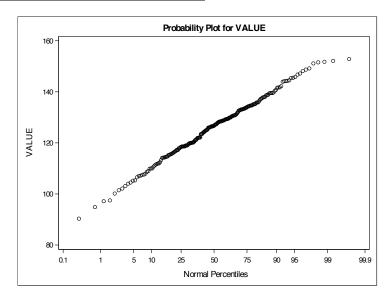
RTRTN=4

| | Moments | | | | | | |
|------------------------|------------|-------------------------|------------|--|--|--|--|
| N | 220 | Sum Weights | 220 | | | | |
| Mean | 125.952909 | Sum Observations | 27709.64 | | | | |
| Std Deviation | 12.0077179 | Variance | 144.18529 | | | | |
| Skewness | -0.1825049 | Kurtosis | -0.0691965 | | | | |
| Uncorrected SS | 3521686.35 | Corrected SS | 31576.5785 | | | | |
| Coeff Variation | 9.5334979 | Std Error Mean | 0.80956018 | | | | |

| | Basic Statistical Measures | | | | | |
|--------|----------------------------|---------------------|-----------|--|--|--|
| Loca | Location Variability | | | | | |
| Mean | 125.9529 | Std Deviation | 12.00772 | | | |
| Median | 126.7850 | Variance | 144.18529 | | | |
| Mode | 117.8500 | Range | 62.53000 | | | |
| | | Interquartile Range | 15.56500 | | | |

| Tests for Normality | | | | | |
|---------------------|-------------------|----------|-----------|---------|--|
| Test | Statistic p Value | | | | |
| Shapiro-Wilk | W | 0.99425 | Pr < W | 0.5645 | |
| Kolmogorov-Smirnov | D | 0.049239 | Pr > D | >0.1500 | |
| Cramer-von Mises | W-Sq | 0.052537 | Pr > W-Sq | >0.2500 | |
| Anderson-Darling | A-Sq | 0.283503 | Pr > A-Sq | >0.2500 | |





Now we repeat the analysis by treatment groups (RTRTN). Firstly, mean values for 1, 2, 3 and 4 are 131.47, 127.70, 126.21 and 125.95, and the median values are 131.21, 127.43, 126.55 and 126.79, respectively. 1 is likely to have larger systolic blood pressure compared to the other three groups, 2, 3, 4. Among 2, 3, 4, 2 has larger weight. The standard deviation and range for 1, 2, 3, and 4 are (12.27, 66.95), (12.69, 71.74), (11.60, 69.32) and (12.01, 62.53), respectively. It can be seen that systolic blood pressure of 2 has larger standard deviation and range.

For the skewness, systolic blood pressure of 1, 2, 3 and 4 have skewness measure as -0.001, 0.072, -0.229 and -0.183. Generally, positive measure indicates right long tail, and right-skewness.

For 1, 2, 3 and 4, all test p-values are greater than 0.05, so conclude that we do not have evidence to reject normality assumption. It is clear that histograms of 1 and 2 are symmetric. Although histograms of 3 and 4 do not have perfect symmetric shapes, they are not very bad. The observations in the QQ-plots almost follow the diagonal line. In conclusion, the distributions of systolic blood pressure for all four treatment groups are normal.

The TTEST Procedure

Variable: VALUE

| RTRTN | Method | Mean | 95% CL Mean | | Std Dev | 95% (| |
|------------|---------------|--------|----------------|-------|---------|---------|---------|
| 1 | | 131.5 | 129.8 | 133.1 | 12.2674 | 11.2183 | 13.5348 |
| 4 | | 126.0 | 124.4 | 127.5 | 12.0077 | 10.9807 | 13.2483 |
| Diff (1-2) | Pooled | 5.5159 | 3.6082 | Infty | 12.1383 | 11.3850 | 12.9992 |
| Diff (1-2) | Satterthwaite | 5.5159 | 3.6082 | Infty | | | |

| Method | Variances | DF | t Value | Pr > t |
|---------------|-----------|-------|---------|--------|
| Pooled | Equal | 438 | 4.77 | <.0001 |
| Satterthwaite | Unequal | 437.8 | 4.77 | <.0001 |

| Equality of Variances | | | | | | |
|---|-----|-----|------|--------|--|--|
| Method Num DF Den DF F Value Pr > F | | | | | | |
| Folded F | 219 | 219 | 1.04 | 0.7518 | | |

2. In Exercise 1 we found that systolic blood pressure for reference (RTRTN=1) and ABC123 80mg (RTRTN=4) be assumed as normal. Since we have normality for two groups, we perform the T-test to compare the systolic blood pressure of two groups. The "Equality of Variances" test reveals insufficient evidence of unequal variances (the Folded F statistic F'=1.04, with p=0.7518.), so we use Satterthwaite adjustment. One-sided two-sample T-test gives p-value less than 0.05, and we can conclude that ABC123 80mg significantly reduces the blood pressure compared to the reference drug.

The FREQ Procedure

| Table of RTRTN by responder | | | | | | | |
|-----------------------------|---------------|-------------|-----|--|--|--|--|
| RTRTN | 1 | responder | | | | | |
| Frequency Expected | 0 1 Tota | | | | | | |
| 1 | 184 161.75 | 36 58.25 | 220 | | | | |
| 2 | 160 161.75 | 60 58.25 | 220 | | | | |
| 3 | 153 161.75 | 67 58.25 | 220 | | | | |
| 4 | 150 161.75 | 70 58.25 | 220 | | | | |
| Total | 647 | 233 | 880 | | | | |

Statistics for Table of RTRTN by responder

| Statistic | DF | Value | Prob |
|--------------------------------|----|---------|--------|
| Chi-Square | 3 | 16.6425 | 0.0008 |
| Likelihood Ratio Chi-Square | 3 | 17.6875 | 0.0005 |
| Mantel-Haenszel Chi-Square | 1 | 13.8552 | 0.0002 |
| Phi Coefficient | | 0.1375 | |
| Contingency Coefficient | | 0.1362 | |
| Cramer's V | | 0.1375 | |

Sample Size = 880

Now we perform a hypothesis test of whether there is a significant relationship between treatment groups (RTRTN) and responder categories (responder). We find no cell presenting expected less than 5. Accordingly, we can use asymptotic tests. Both Chi-Square and Likelihood Ratio tests give p-values less than 0.05, thus we reject the null hypothesis (null: two variables are independent; alternative: there is some significant association) and conclude that there exists significant association between peanut allergy and early assumption. Note that we cannot apply Mantel-Haenszel test because treatment group is not ordered variable. Since the sample size is large, we cannot get the result of Fisher's exact test for the exact result.

The information about the magnitude of the relationship between two variables can be obtained from Phi Coefficient, Contingency Coefficient, and Cramer's V. The Phi Coefficient and Cramer's V give the same value, 0.1375, and Contingency Coefficient gives the similar magnitude 0.1362. We conclude that there's a mild association between treatment groups and responder categories. For larger dimensional tables, Cramer's V is standardized and its upper bound is 1, and therefore Cramer's V is preferred for larger dimensional tables.

The FREQ Procedure

| Table of RTRTN by responder | | | | | | |
|-----------------------------|------------|-----------|-------|--|--|--|
| RTRTN | 1 | responder | | | | |
| Frequency Expected | 0 | 1 | Total | | | |
| 1 | 184 167 | 36 53 | 220 | | | |
| 4 | 150 167 | 70 53 | 220 | | | |
| Total | 334 | 106 | 440 | | | |

Statistics for Table of RTRTN by responder

| Statistic | DF | Value | Prob |
|--------------------------------|----|---------|--------|
| Chi-Square | 1 | 14.3667 | 0.0002 |
| Likelihood Ratio Chi-Square | 1 | 14.5679 | 0.0001 |
| Continuity Adj. Chi-Square | 1 | 13.5341 | 0.0002 |
| Mantel-Haenszel Chi-Square | 1 | 14.3341 | 0.0002 |
| Phi Coefficient | | 0.1807 | |
| Contingency Coefficient | | 0.1778 | |
| Cramer's V | | 0.1807 | |

| Fisher's Exact Test | | |
|--------------------------|--------|--|
| Cell (1,1) Frequency (F) | 184 | |
| Left-sided Pr <= F | 1.0000 | |
| Right-sided Pr >= F | 0.0001 | |
| | | |
| Table Probability (P) | <.0001 | |
| Two-sided Pr <= P | 0.0002 | |

We can test if two categorical variables are significantly associated via various types of asymptotic tests. Note that asymptotic tests can be performed, because all cells have expected values greater than 5. Chi-Square and Likelihood Ration Chi-Square tests give p-value less than 0.05, thus we reject the null hypothesis (H0: two are independent), and conclude that there exists a significant association between treatment groups and responder categories. Furthermore, we cannot apply Mantel-Haenszel test because treatment group is not ordinal variable. We can always refer to Fisher's exact test for the exact result. The Fisher's test also gives p-value less than 0.05 (2-sided p-value=0.0002), thus we can make the same conclusion.

The information about the magnitude of the relationship between two variables can be obtained from Phi Coefficient, Contingency Coefficient, and Cramer's V. The Phi Coefficient and Cramer's V.

give the same value, 0.1807, and Contingency Coefficient gives the similar magnitude 0.1778. For 2x2 tables, we focus more on the Phi and Cramer's V coefficients because they are bounded between -1 and 1, and therefore are analogues of correlation coefficients. We conclude that there's a mild association between peanut allergy and early consumption. We conclude that there's a mild association between treatment groups and responder categories.

In the following table Row1 and Row2 correspond to reference and ABC123 80mg groups, respectively. The proportional difference in the responder category is -0.1545. We can test whether the difference is significant by using the confidence interval. The table provides 95% confidence limit as (-0.2331, -0.0759), and zero is not in the interval. Thus, we can conclude there are more responders in the ABC123 80mg group compared to the reference group.

| Column 1 Risk Estimates | | | | | | |
|-------------------------|-------------------------------|--------|----------------------|--------|--------------------|--------|
| | Risk | ASE | (Asympto Confiden | | (Exact Confiden | f . |
| Row 1 | 0.8364 | 0.0249 | 0.7875 | 0.8852 | 0.7807 | 0.8827 |
| Row 2 | 0.6818 | 0.0314 | 0.6203 | 0.7434 | 0.6158 | 0.7428 |
| Total | 0.7591 | 0.0204 | 0.7191 | 0.7990 | 0.7163 | 0.7983 |
| Difference | 0.1545 | 0.0401 | 0.0759 | 0.2331 | | |
| | Difference is (Row 1 - Row 2) | | | | | |

| Column 2 Risk Estimates | | | | | | | |
|-------------------------|-------------------------------|--------|----------------------|---------|--------------------|--------|--|
| | Risk | ASE | (Asympto Confiden | | (Exact Confiden | | |
| Row 1 | 0.1636 | 0.0249 | 0.1148 | 0.2125 | 0.1173 | 0.2193 | |
| Row 2 | 0.3182 | 0.0314 | 0.2566 | 0.3797 | 0.2572 | 0.3842 | |
| Total | 0.2409 | 0.0204 | 0.2010 | 0.2809 | 0.2017 | 0.2837 | |
| Difference | -0.1545 | 0.0401 | -0.2331 | -0.0759 | | | |
| | Difference is (Row 1 - Row 2) | | | | | | |

Sample Size = 440

The GLMSELECT Procedure

| | Stepwise Selection Summary | | | | | | | | |
|------|----------------------------|-------------------|----------------------|-----|---------|--------|--|--|--|
| Step | Effect Entered | Effect Removed | Number Effects In | _ , | F Value | Pr > F | | | |
| 0 | Intercept | | 1 | 1 | 0.00 | 1.0000 | | | |
| 1 | RTRTN | | 2 | 4 | 9.64 | <.0001 | | | |
| 2 | SEX | | 3 | 5 | 12.86 | 0.0004 | | | |
| 3 | SITE | | 4 | 24 | 1.73 | 0.0272 | | | |

Selection stopped because the candidate for entry has SLE > 0.05 and the candidate for removal has SLS < 0.05.

| Stop Details | | | | | |
|------------------|--------|---------------------------|---|-------------------------|-------|
| Candidate For | Effect | Candidate Significance | | Compare Significance | |
| Entry | RACE | 0.6086 | > | 0.0500 | (SLE) |
| Removal | SITE | 0.0272 | < | 0.0500 | (SLS) |

Effects: Intercept SEX RTRTN SITE

We first use stepwise selection to investigate main effects. By using GLMSELECT, only SEX, RTRTN, and SITE are selected in the model.

Dependent Variable: VALUE

| Source | D F | Type I SS | Mean Square | F Value | Pr > F |
|----------------|--------|-------------|-------------|---------|--------|
| SEX | 1 | 1937.736947 | 1937.736947 | 13.70 | 0.0002 |
| RTRTN | 3 | 4201.225734 | 1400.408578 | 9.90 | <.0001 |
| SEX*RTRTN | 3 | 162.122603 | 54.040868 | 0.38 | 0.7660 |
| SITE | 19 | 4751.550870 | 250.081625 | 1.77 | 0.0227 |
| SEX*SITE | 19 | 2164.555128 | 113.923954 | 0.81 | 0.7022 |
| RTRTN*SITE | 57 | 8585.708923 | 150.626472 | 1.06 | 0.3521 |
| SEX*RTRTN*SITE | 57 | 9885.600761 | 173.431592 | 1.23 | 0.1290 |

| Source | DF | Type III SS | Mean Square | F Value | Pr > F |
|----------------|----|-------------|-------------|---------|---------------------|
| SEX | 1 | 2127.554532 | 2127.554532 | 15.04 | 0.0001 |
| RTRTN | 3 | 3354.476431 | 1118.158810 | 7.90 | <.0001 |
| SEX*RTRTN | 3 | 256.319003 | 85.439668 | 0.60 | <mark>0.6126</mark> |
| SITE | 19 | 4631.274706 | 243.751300 | 1.72 | 0.0283 |
| SEX*SITE | 19 | 1783.048464 | 93.844656 | 0.66 | <mark>0.8564</mark> |
| RTRTN*SITE | 57 | 8153.740626 | 143.048081 | 1.01 | 0.4554 |
| SEX*RTRTN*SITE | 57 | 9885.600761 | 173.431592 | 1.23 | 0.1290 |

We then investigate whether the interaction terms are significant or not. From Type III SS, we could conclude interaction terms are not significant. Meanwhile from the plot we could also conclude there is no significant interaction. Then we focus on model with only SEX, RTRTN, and SITE as three main effects.

Dependent Variable: VALUE

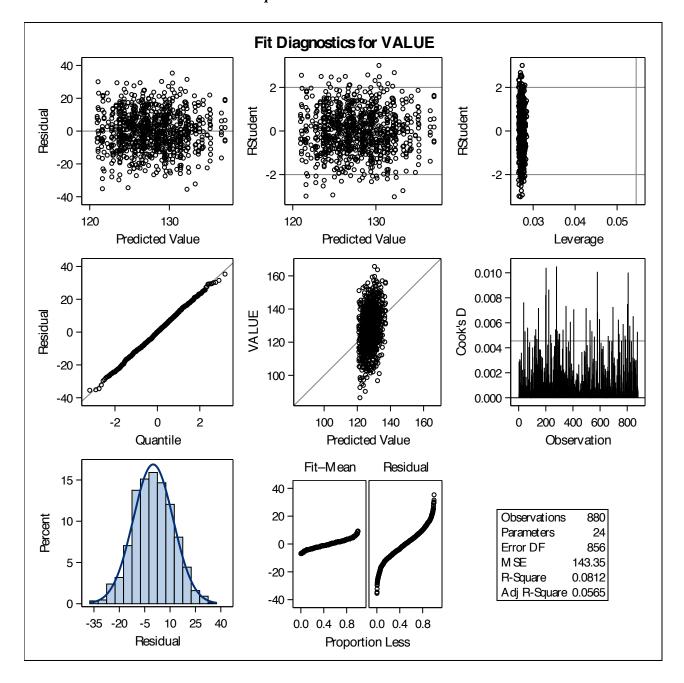
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|------------------------|-----|-------------------|-------------|---------|--------|
| Model | 23 | 10845.1411 | 471.5279 | 3.29 | <.0001 |
| Error | 856 | 122708.8210 | 143.3514 | | |
| Corrected Total | 879 | 133553.9621 | | | |

| R-Square | Coeff Var | Root MSE | VALUE Mean |
|----------|-----------|----------|------------|
| 0.081204 | 9.366045 | 11.97295 | 127.8335 |

| Source | DF | Type I SS | Mean Square | F Value | Pr > F |
|--------|----|-------------|-------------|---------|--------|
| SEX | 1 | 1937.736947 | 1937.736947 | 13.52 | 0.0003 |
| RTRTN | 3 | 4201.225734 | 1400.408578 | 9.77 | <.0001 |
| SITE | 19 | 4706.178404 | 247.693600 | 1.73 | 0.0272 |

| Source | DF | Type III SS | Mean Square | F Value | Pr > F |
|--------|----|-------------|-------------|---------|--------|
| SEX | 1 | 1601.135987 | 1601.135987 | 11.17 | 0.0009 |
| RTRTN | 3 | 4204.846218 | 1401.615406 | 9.78 | <.0001 |
| SITE | 19 | 4706.178404 | 247.693600 | 1.73 | 0.0272 |

Dependent Variable: VALUE



Then we focus on model with only SEX, RTRTN, and SITE as three main effects. The ANOVA model is significant with p-value less than .0001. The proportion of variation in blood pressure value explained by the model is 8.12%, which is R-square in the output.

The GLM Procedure Least Squares Means Adjustment for Multiple Comparisons: Tukey-Kramer

| RTRTN | VALUE LSMEAN | LSMEAN Number |
|-------|--------------|------------------|
| 1 | 131.431560 | 1 |
| 2 | 127.686717 | 2 |
| 3 | 126.374677 | 3 |
| 4 | 125.828717 | 4 |

| Least Squares Means for Effect RTRTN t for H0: LSMean(i)=LSMean(j) / Pr > t Dependent Variable: VALUE | | | | | | |
|--|--------------------|--------------------|--------------------|--------------------|--|--|
| i/j | 1 | 2 | 3 | 4 | | |
| 1 | | 3.280347 0.0059 | 4.423744 <.0001 | 4.906718 <.0001 | | |
| 2 | -3.28035 0.0059 | | 1.148132 0.6597 | 1.626877 0.3640 | | |
| 3 | -4.42374 <.0001 | -1.14813 0.6597 | | 0.476917 0.9642 | | |
| 4 | -4.90672 <.0001 | -1.62688 0.3640 | -0.47692 0.9642 | | | |

| RTRTN | VALUE LSMEAN | 95% Confidence Limits | |
|-------|--------------|--------------------------|------------|
| 1 | 131.431560 | 129.847055 | 133.016066 |
| 2 | 127.686717 | 126.102346 | 129.271088 |
| 3 | 126.374677 | 124.787489 | 127.961866 |
| 4 | 125.828717 | 124.242685 | 127.414749 |

| | Least Squares Means for Effect RTRTN | | | | | | | | | |
|---|--------------------------------------|--------------------------------|--|----------|--|--|--|--|--|--|
| i | j | Difference Between Means | Simultaneous 95% Confidence Limits for LSMean(i)-LSMean(j) | | | | | | | |
| 1 | 2 | 3.744843 | 0.806323 | 6.683364 | | | | | | |
| 1 | 3 | 5.056883 | 2.114442 | 7.999324 | | | | | | |
| 1 | 4 | 5.602844 | 2.663623 | 8.542065 | | | | | | |
| 2 | 3 | 1.312040 | -1.629469 | 4.253548 | | | | | | |
| 2 | 4 | 1.858000 | <u>-1.081719</u> | 4.797720 | | | | | | |
| 3 | 4 | 0.545961 | -2.400722 | 3.492643 | | | | | | |

The UNIVARIATE Procedure Variable: resid

| Tests for Normality | | | | | | | | | |
|---------------------|-------------------|----------|-----------|---------------------|--|--|--|--|--|
| Test | Statistic p Value | | | | | | | | |
| Shapiro-Wilk | W | 0.998765 | Pr < W | <mark>0.8165</mark> | | | | | |
| Kolmogorov-Smirnov | D | 0.020656 | Pr > D | >0.1500 | | | | | |
| Cramer-von Mises | W-Sq | 0.034131 | Pr > W-Sq | >0.2500 | | | | | |
| Anderson-Darling | A-Sq | 0.228641 | Pr > A-Sq | >0.2500 | | | | | |

Now we investigate each main effect to see where we can find the significant differences. Firstly, we rank the treatment groups based on efficacy at reducing blood pressure. For blood pressure, reference group has the largest value, the ABC123 20mg group has the second largest value, the ABC123 40mg group has the third largest value, and the ABC123 80mg group has the smallest value. Second, differences of LS means, 95% CI and p-values are highlighted. Differences between group 1 and 2, between group 1 and 3, and between group 1 and 4 are significant. Differences between group 2 and 3, between group 2 and 4, and between group 3 and 4 are insignificant. At last we test for the normality. The normality tests for residuals show p-value greater than 0.05, thus we can say that residuals are normally distributed. It implies that model assumption is valid.

The GLMSELECT Procedure

| | Stepwise Selection Summary | | | | | | | | | | |
|------|----------------------------|-------------------|----------------------|-----|---------|--------|--|--|--|--|--|
| Step | Effect Entered | Effect Removed | Number Effects In | _ , | F Value | Pr > F | | | | | |
| 0 | Intercept | | 1 | 1 | 0.00 | 1.0000 | | | | | |
| 1 | BASE | | 2 | 2 | 436.10 | <.0001 | | | | | |
| 2 | RTRTN | | 3 | 5 | 17.61 | <.0001 | | | | | |
| 3 | SEX | | 4 | 6 | 22.96 | <.0001 | | | | | |
| 4 | SITE | | 5 | 25 | 2.49 | 0.0004 | | | | | |

Selection stopped because the candidate for entry has SLE > 0.05 and the candidate for removal has SLS < 0.05.

Effects: Intercept SEX RTRTN SITE BASE

Base score, rtrtn, sex and site are retained in the final ANCOVA model after stepwise selection procedure with significance level 0.05.

The GLMSELECT Procedure Selected Model

| | Para | ameter Estir | nates | |
|-----------|------|--------------|-------------------|---------|
| Parameter | DF | Estimate | Standard Error | t Value |
| Intercept | 1 | -13.667535 | 6.620411 | -2.06 |
| SEX 1 | 1 | -2.935376 | 0.651005 | -4.51 |
| SEX 2 | 0 | 0 | | |
| RTRTN 1 | 1 | 6.622694 | 0.910344 | 7.27 |
| RTRTN 2 | 1 | 3.351580 | 0.911818 | 3.68 |
| RTRTN 3 | 1 | 1.963506 | 0.913721 | 2.15 |
| RTRTN 4 | 0 | 0 | | |
| SITE 1 | 1 | 3.959005 | 2.035122 | 1.95 |
| SITE 2 | 1 | -2.446944 | 2.038411 | -1.20 |
| SITE 3 | 1 | 0.814686 | 2.033150 | 0.40 |
| SITE 4 | 1 | -0.491596 | 2.038506 | -0.24 |
| SITE 5 | 1 | 0.380479 | 2.033020 | 0.19 |
| SITE 6 | 1 | 0.295423 | 2.034667 | 0.15 |
| SITE 7 | 1 | 1.604897 | 2.035176 | 0.79 |
| SITE 8 | 1 | 1.004447 | 2.041667 | 0.49 |
| SITE 9 | 1 | -3.815850 | 2.033261 | -1.88 |
| SITE 10 | 1 | -1.221882 | 2.037493 | -0.60 |
| SITE 11 | 1 | 2.771067 | 2.037422 | 1.36 |
| SITE 12 | 1 | -4.390241 | 2.034593 | -2.16 |
| SITE 13 | 1 | -2.017133 | 2.043674 | -0.99 |
| SITE 14 | 1 | -1.362388 | 2.034010 | -0.67 |
| SITE 15 | 1 | 1.760251 | 2.038159 | 0.86 |
| SITE 16 | 1 | -2.183887 | 2.039350 | -1.07 |
| SITE 17 | 1 | -3.675972 | 2.034477 | -1.81 |
| SITE 18 | 1 | 1.976391 | 2.044978 | 0.97 |
| SITE 19 | 1 | -0.597120 | 2.035177 | -0.29 |
| SITE 20 | 0 | 0 | | |
| BASE | 1 | 0.850936 | 0.038239 | 22.25 |

One-unit increase in the baseline score increases the final blood pressure value by 0.850936.

Dependent Variable: VALUE

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|------------------------|-----|-------------------|-------------|---------|--------|
| Model | 24 | 55850.0705 | 2327.0863 | 25.61 | <.0001 |
| Error | 855 | 77703.8916 | 90.8817 | | |
| Corrected Total | 879 | 133553.9621 | | | |

| R-Square | Coeff Var | Root MSE | VALUE Mean | |
|----------|-----------|----------|------------|--|
| 0.418184 | 7.457505 | 9.533192 | 127.8335 | |

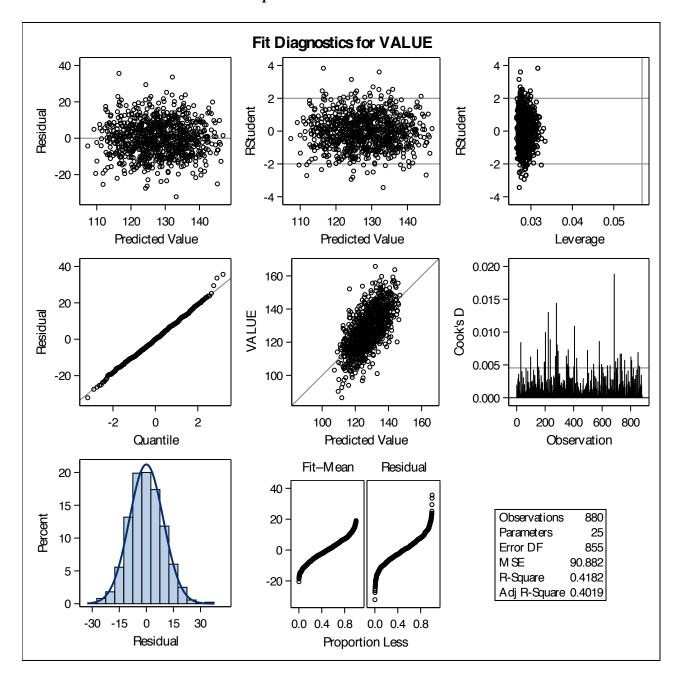
| Source DF | | Type I SS | Mean Square | F Value | Pr > F |
|-----------|----|-------------|-------------|---------|--------|
| SEX | 1 | 1937.73695 | 1937.73695 | 21.32 | <.0001 |
| RTRTN | 3 | 4201.22573 | 1400.40858 | 15.41 | <.0001 |
| SITE | 19 | 4706.17840 | 247.69360 | 2.73 | 0.0001 |
| BASE | 1 | 45004.92938 | 45004.92938 | 495.20 | <.0001 |

| Source DF | | Type III SS | Mean Square | F Value | Pr > F |
|-----------|----|-------------|-------------|---------|--------|
| SEX | 1 | 1847.71487 | 1847.71487 | 20.33 | <.0001 |
| RTRTN | 3 | 5122.02942 | 1707.34314 | 18.79 | <.0001 |
| SITE | 19 | 4292.96137 | 225.94534 | 2.49 | 0.0004 |
| BASE | 1 | 45004.92938 | 45004.92938 | 495.20 | <.0001 |

The predictors in the ANOVA model from Exercise 4 does not contain base score as in the ANCOVA model. The proportion of variation in blood pressure value explained by the ANCOVA model is 41.82%, which is much higher than the R-square in the ANOVA model from Exercise 4 (R-square=8.14%).

From the diagnostic plots below, we see all have cook's D less than 1. No observation is highly influential. The normality tests for residuals show p-value greater than 0.05, thus we can say that residuals are normally distributed. It implies that model assumption is valid.

Dependent Variable: VALUE



| Tests for Normality | | | | | | | | | |
|---------------------|-------------------|----------|-----------|---------|--|--|--|--|--|
| Test | Statistic p Value | | | ıe | | | | | |
| Shapiro-Wilk | W | 0.998249 | Pr < W | 0.5170 | | | | | |
| Kolmogorov-Smirnov | D | 0.020189 | Pr > D | >0.1500 | | | | | |
| Cramer-von Mises | W-Sq | 0.047935 | Pr > W-Sq | >0.2500 | | | | | |
| Anderson-Darling | A-Sq | 0.316642 | Pr > A-Sq | >0.2500 | | | | | |

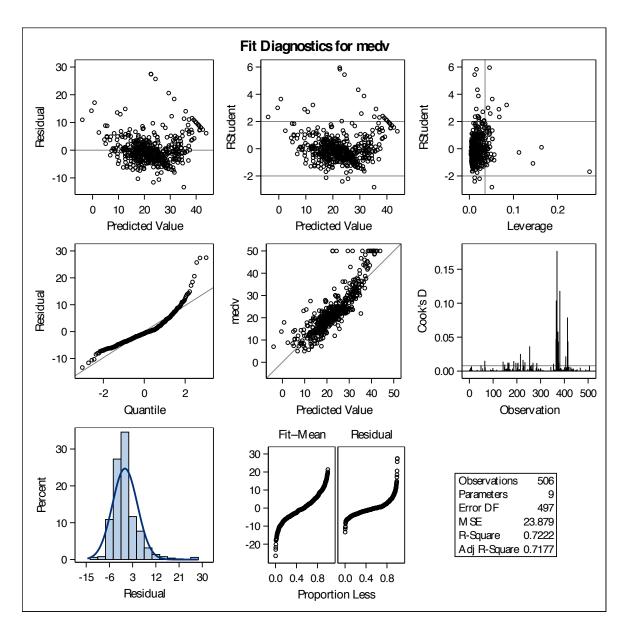
The REG Procedure Model: MODEL1 Dependent Variable: medv

| | Summary of Stepwise Selection | | | | | | | | | | |
|------|-------------------------------|---------------------|-------------------|---------------------|-------------------|---------|---------|--------|--|--|--|
| Step | Variable Entered | Variable Removed | Number Vars In | Partial R-Square | Model R-Square | C(p) | F Value | Pr > F | | | |
| 1 | <u>Istat</u> | | 1 | 0.5441 | 0.5441 | 309.376 | 601.62 | <.0001 | | | |
| 2 | rm | | 2 | 0.0944 | 0.6386 | 143.326 | 131.39 | <.0001 | | | |
| 3 | ptratio | | 3 | 0.0401 | 0.6786 | 74.0183 | 62.58 | <.0001 | | | |
| 4 | dis | | 4 | 0.0117 | 0.6903 | 55.2227 | 18.90 | <.0001 | | | |
| 5 | nox | | 5 | 0.0178 | 0.7081 | 25.5732 | 30.46 | <.0001 | | | |
| 6 | bb | | 6 | 0.0073 | 0.7154 | 14.5796 | 12.80 | 0.0004 | | | |
| 7 | <mark>zn</mark> | | 7 | 0.0042 | 0.7196 | 9.1297 | 7.43 | 0.0066 | | | |
| 8 | crim | | 8 | 0.0026 | 0.7222 | 6.5133 | 4.64 | 0.0317 | | | |

6. Based on stepwise selection, indus, age and tax are removed, and keep lstat, rm, ptratio, dis, nox, bb, zn and crim. We need to examine VIF to check multicollinearity problems. All VIFs are less than 10, thus we would not remove variables and keep all significant predictors.

| | Parameter Estimates | | | | | | | | | | |
|------------|---------------------|-----------------------------------|---------|---------|---------|-----------------------|--|--|--|--|--|
| Variable F | | Parameter Estimate Standard Error | | t Value | Pr > t | Variance Inflation | | | | | |
| Intercept | 1 | 29.54971 | 4.92700 | 6.00 | <.0001 | 0 | | | | | |
| crim | 1 | -0.06609 | 0.03068 | -2.15 | 0.0317 | 1.47310 | | | | | |
| zn | 1 | 0.04127 | 0.01357 | 3.04 | 0.0025 | 2.11847 | | | | | |
| nox | 1 | -15.21364 | 3.25900 | -4.67 | <.0001 | 3.01606 | | | | | |
| rm | 1 | 4.21741 | 0.41178 | 10.24 | <.0001 | 1.77024 | | | | | |
| dis | 1 | -1.46380 | 0.19048 | -7.68 | <.0001 | 3.40240 | | | | | |
| ptratio | 1 | -0.87583 | 0.11816 | -7.41 | <.0001 | 1.38399 | | | | | |
| bb | 1 | 0.00878 | 0.00271 | 3.24 | 0.0013 | 1.29887 | | | | | |
| lstat | 1 | -0.53163 | 0.04885 | -10.88 | <.0001 | 2.57395 | | | | | |

We need to examine VIF to check multicollinearity problems. All VIFs are less than 10, thus we would not remove variables and keep all significant predictors.



Now we need to identify any influential observations. From the diagnostic plots above, we see all have cook's D less than 1. No observation is highly influential.

The REG Procedure Model: MODEL1 Dependent Variable: medv

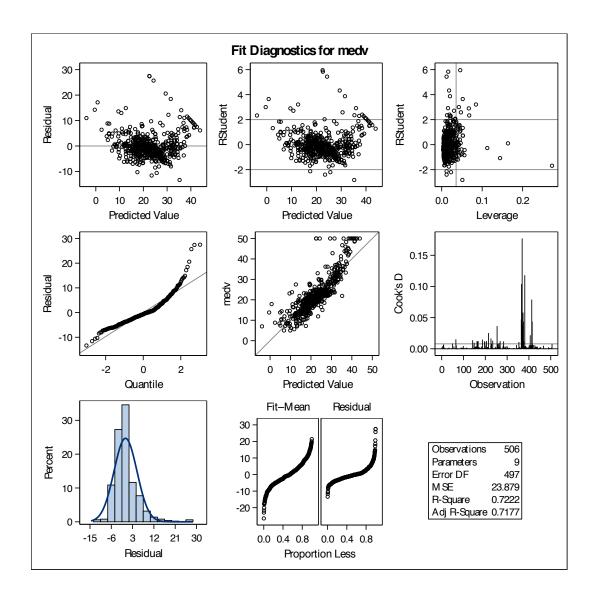
| Analysis of Variance | | | | | | | | | |
|------------------------|-----|-------------------|------------|---------|--------|--|--|--|--|
| Source | DF | Sum of Squares | | F Value | Pr > F | | | | |
| Model | 8 | 30848 | 3856.04614 | 161.48 | <.0001 | | | | |
| Error | 497 | 11868 | 23.87913 | | | | | | |
| Corrected Total | 505 | 42716 | | | | | | | |

| Root MSE | 4.88663 | R-Square | 0.7222 |
|-----------------------|----------|----------|--------|
| Dependent Mean | 22.53281 | Adj R-Sq | 0.7177 |
| Coeff Var | 21.68672 | | |

| Parameter Estimates | | | | | | | | |
|---------------------|----|-----------------------|-------------------|---------|---------|--|--|--|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t | | | |
| Intercept | 1 | 29.54971 | 4.92700 | 6.00 | <.0001 | | | |
| crim | 1 | <u>-0.06609</u> | 0.03068 | -2.15 | 0.0317 | | | |
| zn | 1 | 0.04127 | 0.01357 | 3.04 | 0.0025 | | | |
| nox | 1 | -15.21364 | 3.25900 | -4.67 | <.0001 | | | |
| rm | 1 | 4.21741 | 0.41178 | 10.24 | <.0001 | | | |
| dis | 1 | -1.46380 | 0.19048 | -7.68 | <.0001 | | | |
| ptratio | 1 | -0.87583 | 0.11816 | -7.41 | <.0001 | | | |
| bb | 1 | 0.00878 | 0.00271 | 3.24 | 0.0013 | | | |
| lstat | 1 | -0.53163 | 0.04885 | -10.88 | <.0001 | | | |

The final model (medv~crim+zn+nox+rm+dis+ptratio+bb+lstat) is statistically significant model with p-value less than 0.0001. All predictors are significant in the model. The variation explained by the model is 72.22%.

The parameter estimates are -0.06609, 0.04127, -15.21364, 4.21741, -1.46380, -0.87583, 0.00878 and -0.53163 for crim, zn, nox, rm, dis, ptratio, bb and lstat, respectively. It means that medv is expected to decrease 0.06609, 15.21364, 1.46380, 0.87583 and 0.53163 for a one-unit increase in crim, nox, dis, ptratio and lstat. Medv is expected to increase 0.04127, 4.21741 and 0.00878 for a one-unit increase inzn, rm and bb.



| Tests for Normality | | | | | | | |
|-------------------------|-----------|----------|-----------|---------|--|--|--|
| Test | Statistic | | p Value | | | | |
| Shapiro-Wilk | W | 0.886384 | Pr < W | <0.0001 | | | |
| Kolmogorov-Smirnov | D | 0.136664 | Pr > D | <0.0100 | | | |
| Cramer-von Mises | W-Sq | 2.154266 | Pr > W-Sq | <0.0050 | | | |
| Anderson-Darling | A-Sq | 12.02091 | Pr > A-Sq | <0.0050 | | | |

From diagnostic plots, we see residuals are randomly distributed around 0. The normal QQ plot illustrate that residuals do not follow the diagonal line. The histogram supports it with right skewed shape. The normality can be investigated via normality tests. All p-values are less than 0.05, thus we can conclude that residuals are not normally distributed and there is an issue on assuming normality of the residuals.