

3.

(a)

```
> aismod<-lm(Wt~Sex+Ht+SSF+Bfat, data=ais)
> summary(aismod)
```

Call:

```
lm(formula = Wt ~ Sex + Ht + SSF + Bfat, data = ais)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-13.8944	-4.7384	-0.7099	3.5957	31.6139

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	-68.693175	11.579901	-5.932	1.32e-08	***
Sex	-14.017058	2.008283	-6.980	4.41e-11	***
Ht	0.759674	0.063985	11.873	< 2e-16	***
SSF	0.199369	0.071631	2.783	0.00591	**
Bfat	0.004401	0.439623	0.010	0.99202	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.858 on 197 degrees of freedom

Multiple R-squared: 0.7623, Adjusted R-squared: 0.7574

F-statistic: 157.9 on 4 and 197 DF, p-value: < 2.2e-16

(b) least squares estimates:

Intercept: -68.693175

Sex: -14.017058

Ht: 0.759674

SSF: 0.199369

Bfat: 0.004401

(c) The “Multiple R-Squared” value: 0.7623

(d)

```
> which.max((residuals(aismod)))
```

163

163

```
> fitted(aismod)[163]
```

163

91.58611

Observation 163 has the largest residual, and its fitted value is 91.58611.

(e) According to this model, the estimated difference in weight for a male compared to a female is 14.017058.

(f) Variables that have p-values less than 0.05 are statistically significant, so sex, height and sum of skin folds are statistically significant.

(g)

```
> confint(aismod, level=0.95)
```

	2.5 %	97.5 %
(Intercept)	-91.52965492	-45.8566953
Sex	-17.97755074	-10.0565662
Ht	0.63348925	0.8858580
SSF	0.05810749	0.3406307
Bfat	-0.86257156	0.8713728

(h)

```
> newdata<-data.frame(Sex=1, Ht=170, SSF=60, Bfat=0.12)
> predict(aismod, newdata, interval = "prediction")
```

	fit	lwr	upr
1	58.39696	40.45794	76.33597

(i)

```
> aismod2<-lm(Wt~Sex+Ht, data=ais)
> anova(aismod2, aismod)
```

Analysis of Variance Table

Model 1: Wt ~ Sex + Ht
Model 2: Wt ~ Sex + Ht + SSF + Bfat

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	199	14548.6				
2	197	9266.5	2	5282	56.146	< 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Since the p-value is less than 0.05, we reject the null hypothesis. We conclude that adding sum of skin folds and percent body fat improve the model.

4.

(a)

```
> fuelmod<-lm(FuelC~Income+Pop+Tax,data=fuel2001)
> summary(fuelmod)
```

Call:

```
lm(formula = FuelC ~ Income + Pop + Tax, data = fuel2001)
```

Residuals:

Min	1Q	Median	3Q	Max
-2696785	-113067	-7653	141991	1668076

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	1.698e+06	5.820e+05	2.918	0.00539	**
Income	-3.083e+01	1.723e+01	-1.789	0.07998	.
Pop	5.638e-01	1.646e-02	34.258	< 2e-16	***
Tax	-3.373e+04	1.645e+04	-2.051	0.04587	*

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 522600 on 47 degrees of freedom

Multiple R-squared: 0.9647, Adjusted R-squared: 0.9625

F-statistic: 428.3 on 3 and 47 DF, p-value: < 2.2e-16

(b) The p-value of income is 0.07998, which is greater than 0.05, so we fail to reject H_0 .

(c) The p-value of F-test at the bottom of the output is less than 0.05, so we reject the null hypothesis.

(d)

```

> fuelmod2<-lm(FuelC~Income+Pop+Tax+Drivers,data=fuel2001)
> summary(fuelmod2)

Call:
lm(formula = FuelC ~ Income + Pop + Tax + Drivers, data = fuel2001)

Residuals:
    Min       1Q   Median       3Q      Max
-1697519 -118108  -17214   122668  1849795

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  1.231e+06  5.231e+05   2.353 0.022954 *
Income       -2.644e+01  1.512e+01  -1.749 0.086930 .
Pop           1.666e-02  1.403e-01   0.119 0.906006
Tax          -2.204e+04  1.470e+04  -1.499 0.140648
Drivers       6.496e-01  1.657e-01   3.920 0.000292 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 457400 on 46 degrees of freedom
Multiple R-squared:  0.9735,    Adjusted R-squared:  0.9712
F-statistic: 423.2 on 4 and 46 DF,  p-value: < 2.2e-16

```

(e)

```

> anova(fuelmod2, fuelmod)
Analysis of Variance Table

Model 1: FuelC ~ Income + Pop + Tax + Drivers
Model 2: FuelC ~ Income + Pop + Tax
  Res.Df    RSS Df Sum of Sq    F    Pr(>F)
1     46 9.6235e+12
2     47 1.2838e+13 -1 -3.215e+12 15.368 0.0002923 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Since the p-value is less than 0.05, we reject the null hypothesis. So $\beta_{\text{Drivers}} \neq 0$.

(f)

The p-value of Drivers in the summary of the linear model is 0.000292, which is the same as the p-value of that in the analysis of variance table.