Lecture 10: Training Neural Networks (Part 1)

Reminder: A3

Due Monday, October 14 (1 week from today!)

• Remember to <u>run the validation script</u>!

Midterm Exam

- Monday, October 21 (two weeks from today!)
- Location: Chrysler 220 (NOT HERE!)
- Format:
 - True / False, Multiple choice, short answer
 - Emphasize concepts you don't need to memorize AlexNet!
 - Closed-book
 - You can bring 1 page "cheat sheet" of handwritten notes (standard 8.5" x 11" paper)
- Alternate exam times: Fill out this form: https://forms.gle/uiMpHdg9752p27bd7
 - Conflict with EECS 551
 - SSD accommodations
 - Conference travel for Michigan

Last Time: Hardware and Software

CPU GPU TPU







Static Graphs VS **Dynamic Graphs**

PyTorch vs **TensorFlow**

Overview

1. One time setup

Activation functions, data preprocessing, weight initialization, regularization

2. Training dynamics

Learning rate schedules; large-batch training; hyperparameter optimization

3. After training

Model ensembles, transfer learning

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Model ensembles, transfer learning

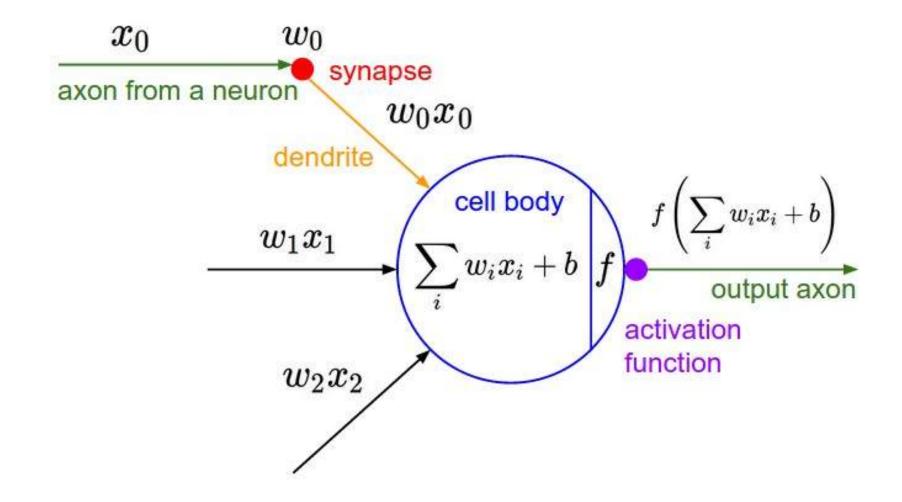
Today

Next time

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Activation Functions

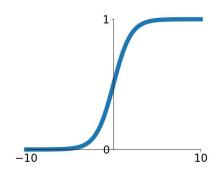
Activation Functions



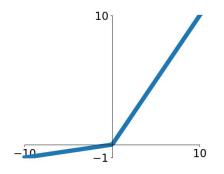
Activation Functions

Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

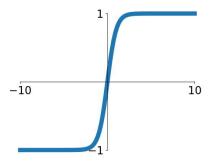


Leaky ReLU $\max(0.1x, x)$



tanh

tanh(x)

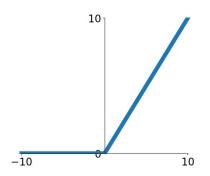


Maxout

 $\max(w_1^T x + b_1, w_2^T x + b_2)$

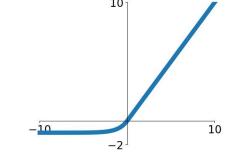
ReLU

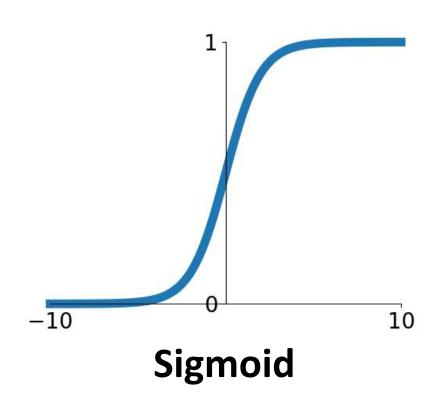
 $\max(0, x)$



ELU

$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

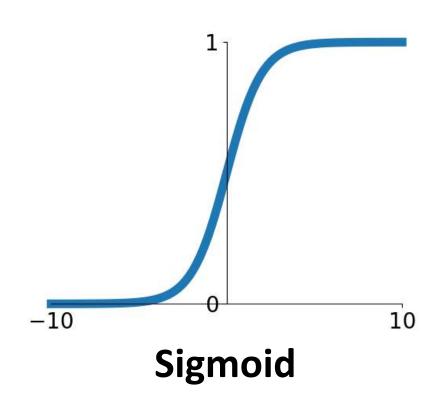




$$\sigma(x)=1/(1+e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

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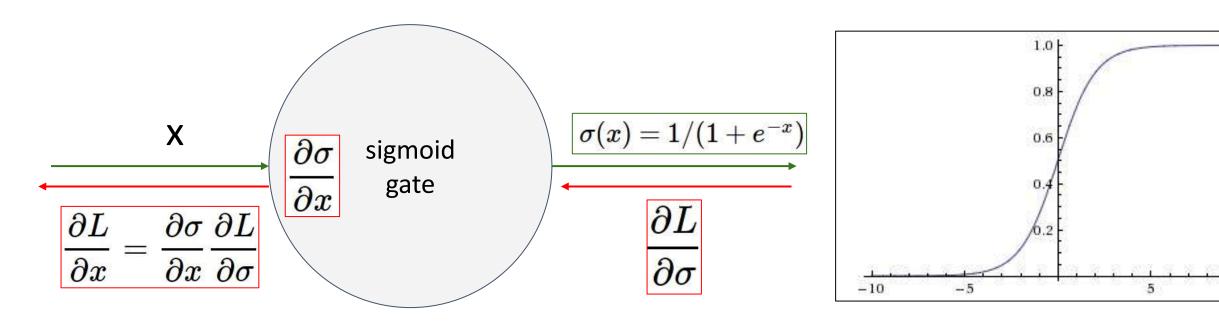
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3 problems:

Saturated neurons "kill" the gradients

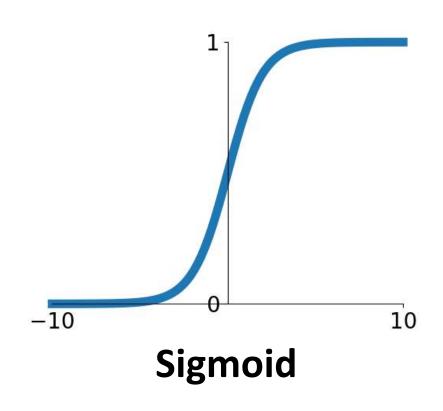
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What happens when x = -10?

What happens when x = 0?

What happens when x = 10?



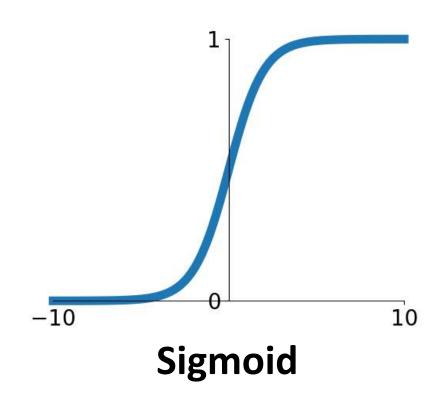
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3 problems:

1. Saturated neurons "kill" the gradients

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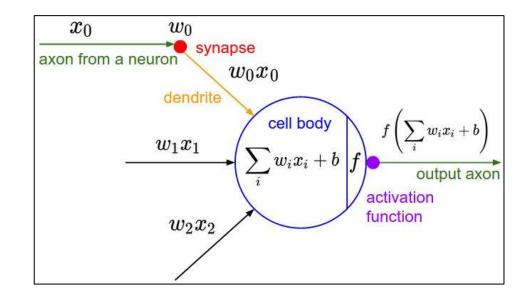
3 problems:

- 1. Saturated neurons "kill" the gradients
- Sigmoid outputs are not zero-centered

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Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b\right)$$



What can we say about the gradients on w?

Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

What can we say about the gradients on w? Always all positive or all negative :(

allowed gradient update directions

allowed gradient update directions

hypothetical optimal w vector

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Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

What can we say about the gradients on w? Always all positive or all negative :(

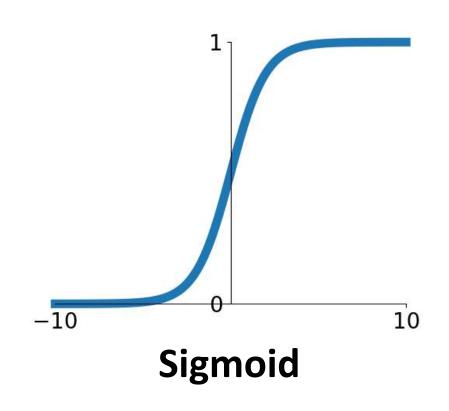
(For a single element! Minibatches help)

allowed gradient update directions

allowed gradient update directions

hypothetical optimal w vector

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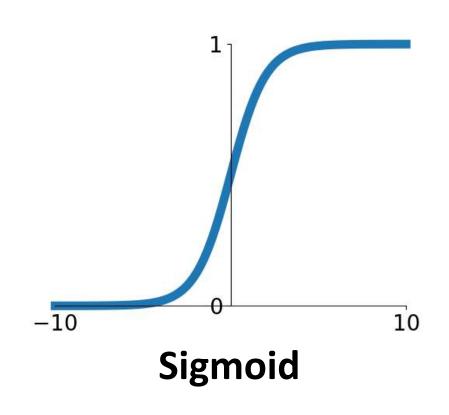
$$\sigma(x)=1/(1+e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- 1. Saturated neurons "kill" the gradients
- Sigmoid outputs are not zero-centered

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$$\sigma(x)=1/(1+e^{-x})$$

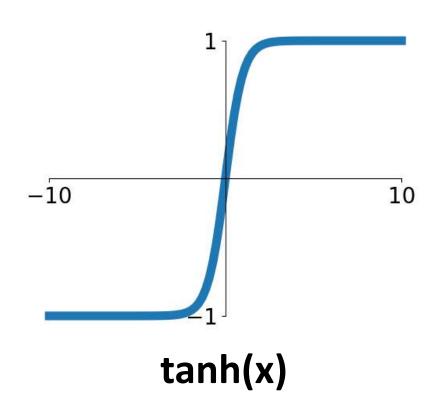
- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- 1. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered
- B. exp() is a bit compute expensive

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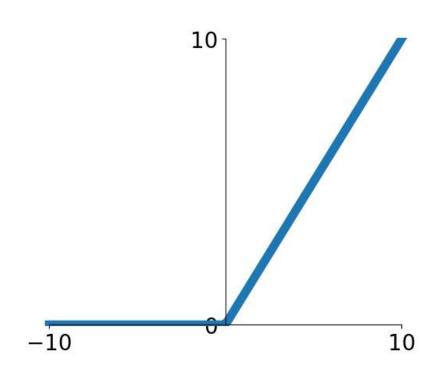
Activation Functions: Tanh



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

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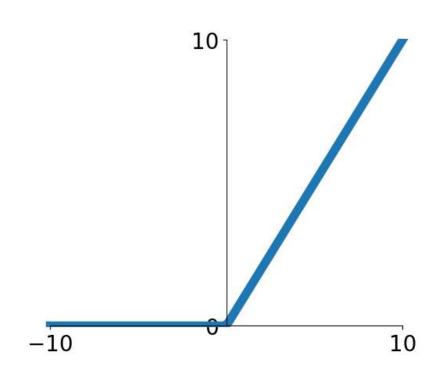
$$f(x) = max(0,x)$$



ReLU (Rectified Linear Unit)

- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

$$f(x) = max(0,x)$$

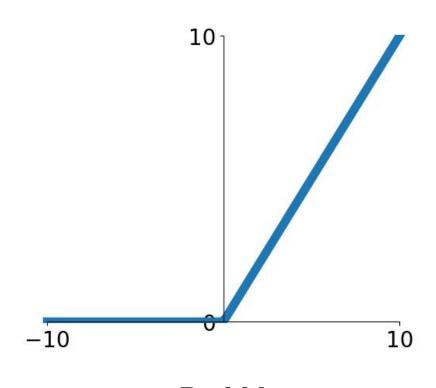


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Not zero-centered output

$$f(x) = max(0,x)$$

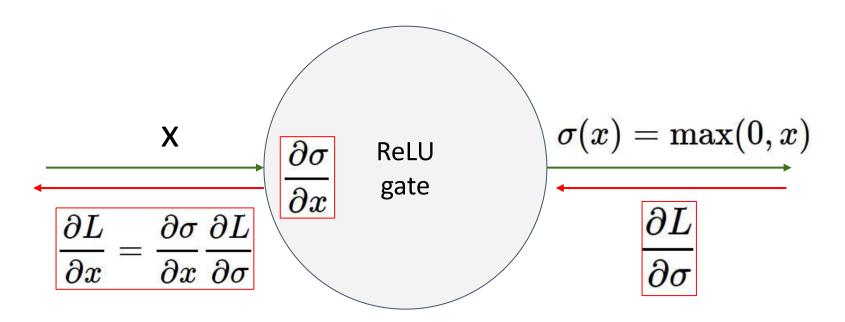


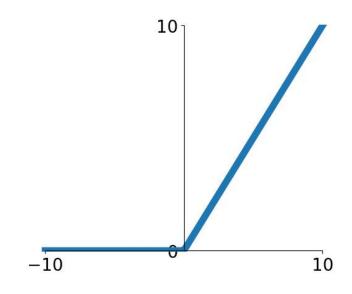
ReLU (Rectified Linear Unit)

- Does not saturate (in +region)
- Very computationally efficient
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- Not zero-centered output
- An annoyance:

hint: what is the gradient when x < 0?

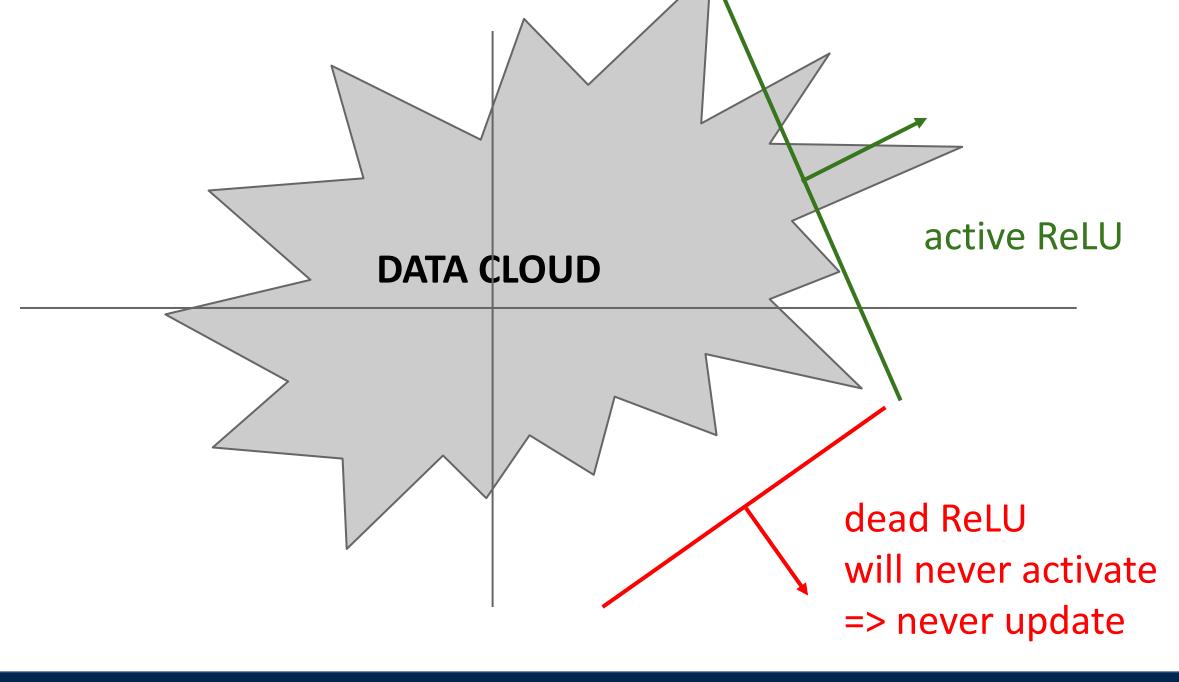




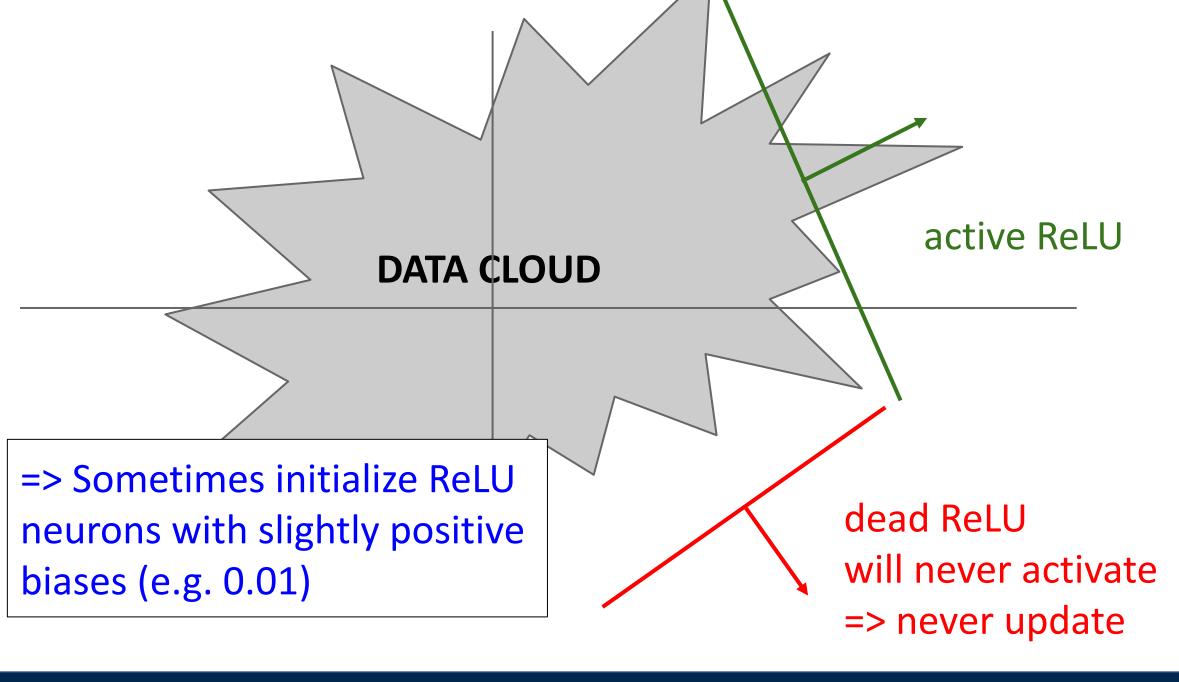
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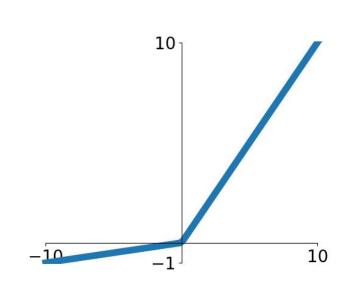


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Activation Functions: Leaky ReLU



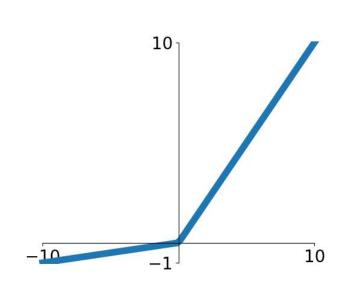
Leaky ReLU

$$f(x) = \max(0.01x, x)$$

- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

Maas et al, "Rectifier Nonlinearities Improve Neural Network Acoustic Models", ICML 2013

Activation Functions: Leaky ReLU



Leaky ReLU

$$f(x) = \max(0.01x, x)$$

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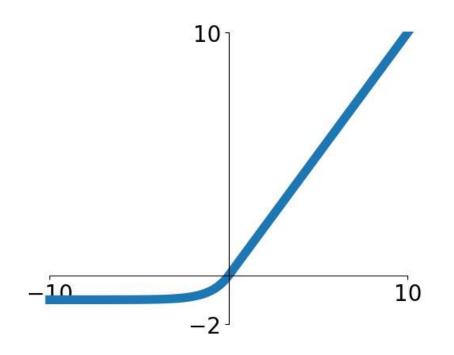
Parametric Rectifier (PReLU)

$$f(x) = \max(\alpha x, x)$$

backprop into \alpha
(parameter)

He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

Activation Functions: Exponential Linear Unit (ELU)



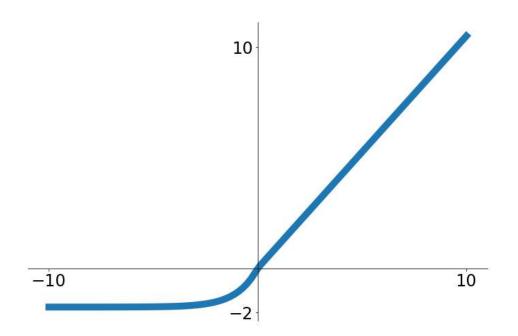
$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha \left(\exp(x) - 1 \right) & \text{if } x \le 0 \end{cases}$$
(Default alpha=1)

- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

Computation requires exp()

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Activation Functions: Scaled Exponential Linear Unit (SELU)



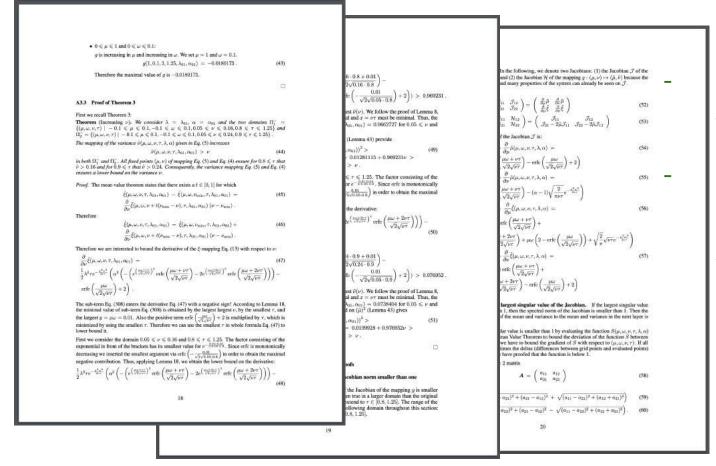
$$selu(x) = \begin{cases} \lambda x & \text{if } x < 0 \\ \lambda (\alpha e^x - \alpha) & \text{otherwise} \end{cases}$$

 $\alpha = 1.6732632423543772848170429916717$ $\lambda = 1.0507009873554804934193349852946$

- Scaled version of ELU that works better for deep networks
- "Self-Normalizing" property;
 can train deep SELU networks
 without BatchNorm

Klambauer et al, Self-Normalizing Neural Networks, ICLR 2017

Activation Functions: Scaled Exponential Linear Unit (SELU)



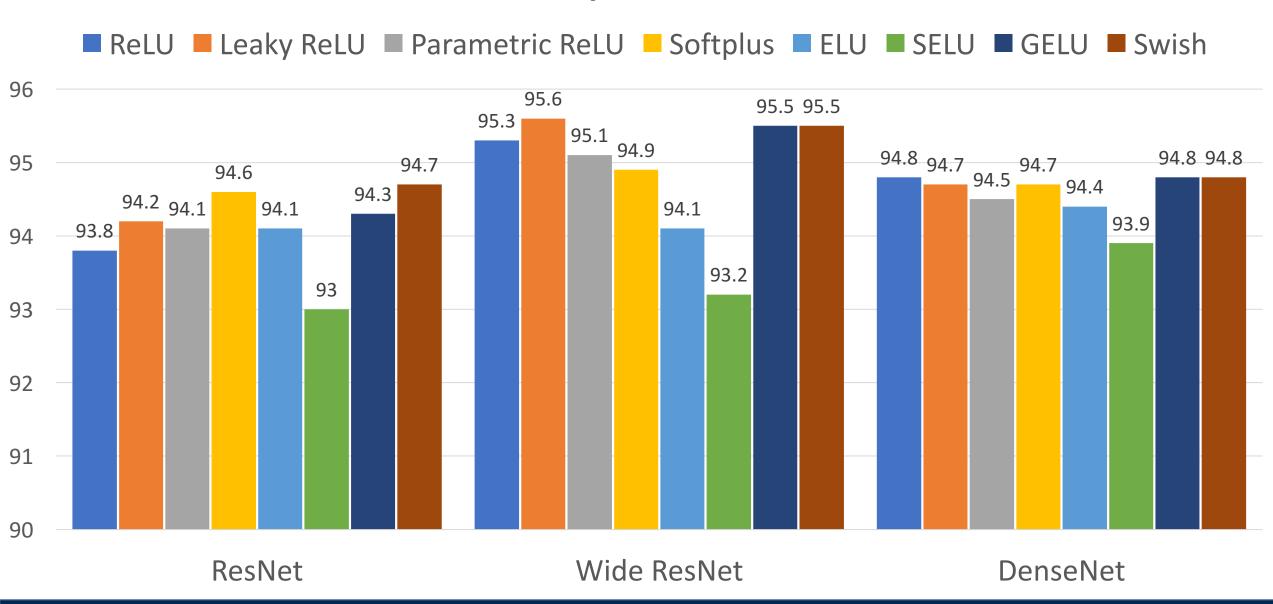
Scaled version of ELU that works better for deep networks "Self-Normalizing" property; can train deep SELU networks without BatchNorm

Derivation takes 91 pages of math in appendix...

 $\alpha = 1.6732632423543772848170429916717$ $\lambda = 1.0507009873554804934193349852946$

Klambauer et al, Self-Normalizing Neural Networks, ICLR 2017

Accuracy on CIFAR10



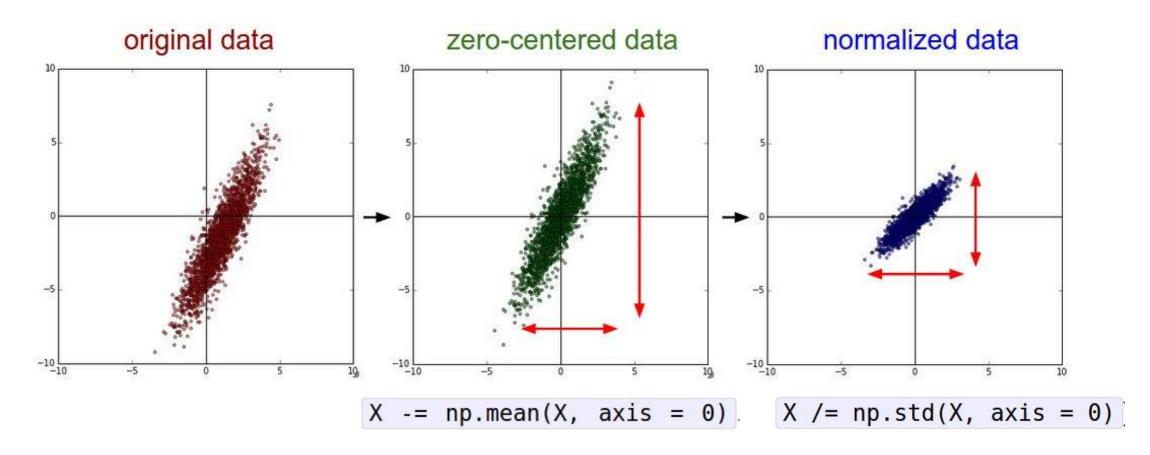
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Activation Functions: Summary

- Don't think too hard. Just use ReLU
- Try out Leaky ReLU / ELU / SELU / GELU if you need to squeeze that last 0.1%
- Don't use sigmoid or tanh

Data Preprocessing

Data Preprocessing



(Assume X [NxD] is data matrix, each example in a row)

Remember: Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

What can we say about the gradients on w? Always all positive or all negative: (this is also why you want zero-mean data!)

allowed gradient update directions

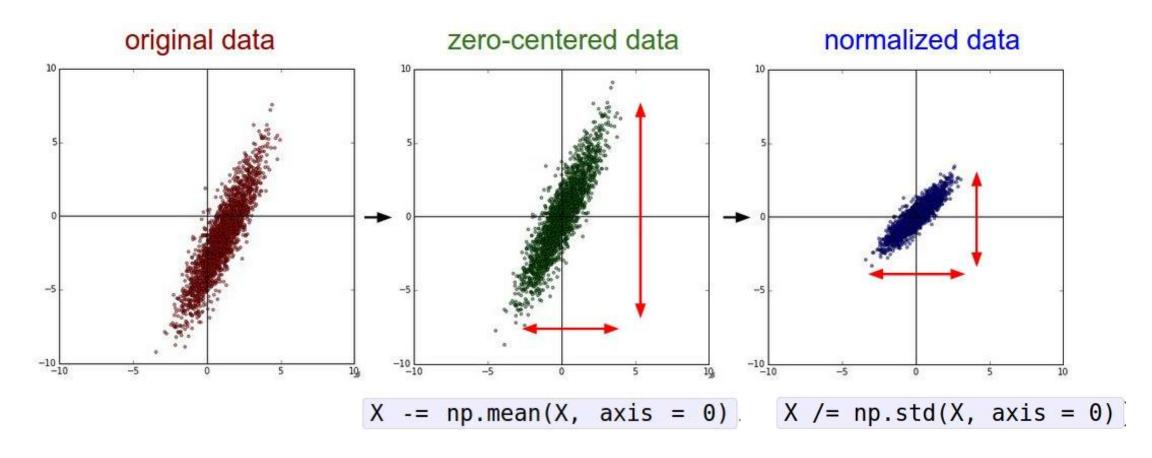
allowed gradient update directions

hypothetical optimal w

vector

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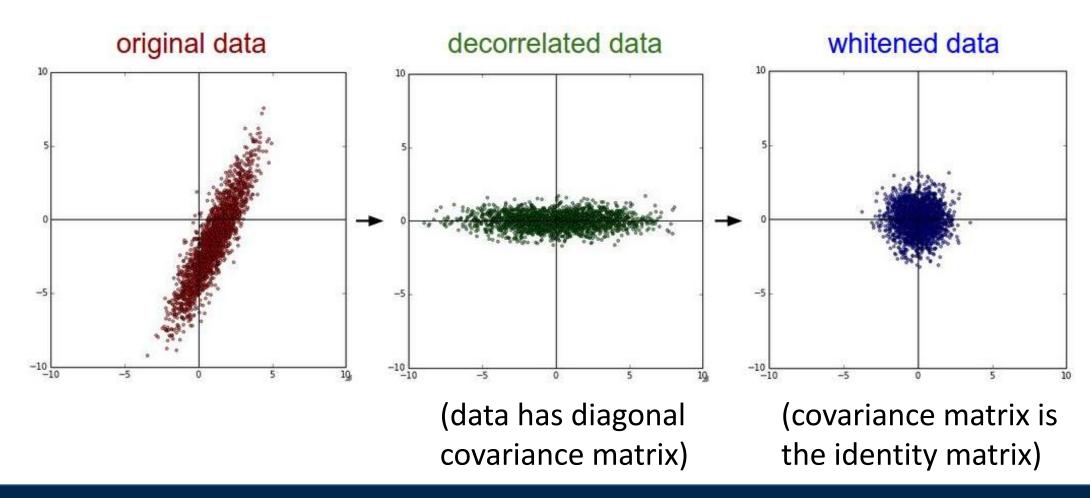
Data Preprocessing



(Assume X [NxD] is data matrix, each example in a row)

Data Preprocessing

In practice, you may also see PCA and Whitening of the data

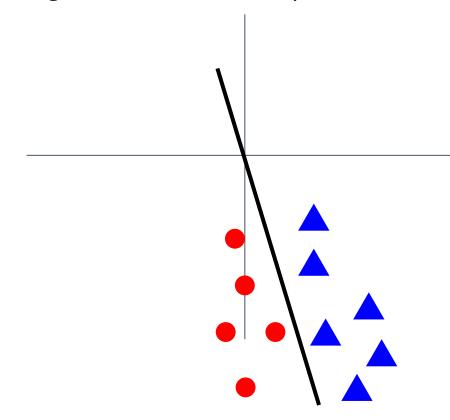


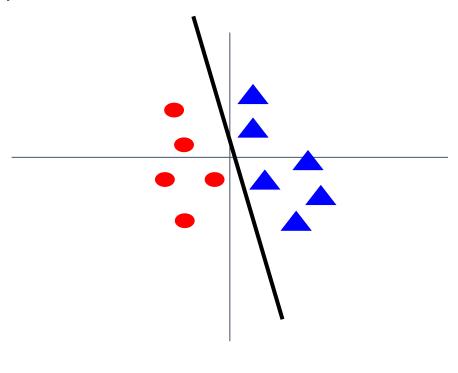
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Data Preprocessing

Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize

After normalization: less sensitive to small changes in weights; easier to optimize





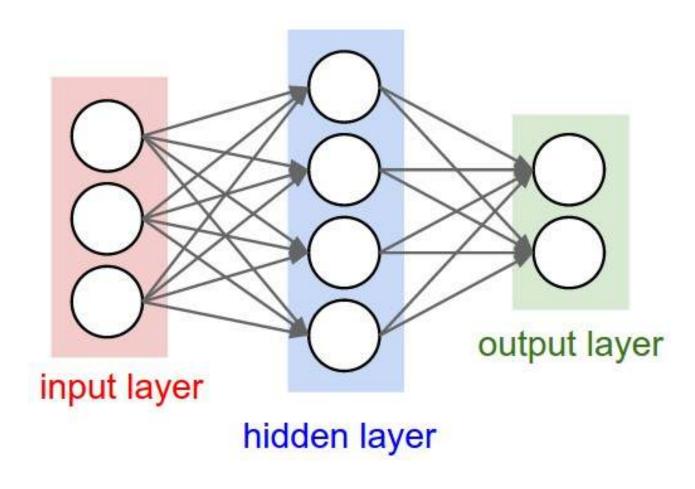
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Data Preprocessing for Images

e.g. consider CIFAR-10 example with [32,32,3] images

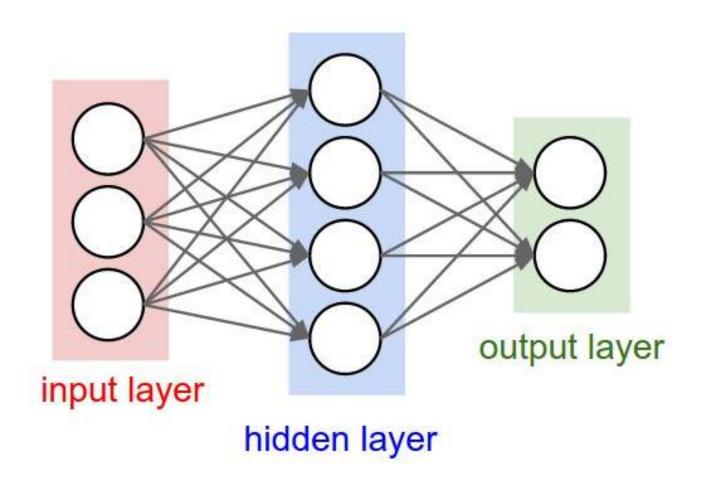
- Subtract the mean image (e.g. AlexNet)
 (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet)
 (mean along each channel = 3 numbers)
- Subtract per-channel mean and
 Divide by per-channel std (e.g. ResNet)
 (mean along each channel = 3 numbers)

Not common to do PCA or whitening



Q: What happens if we initialize all W=0, b=0?

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Q: What happens if we initialize all W=0, b=0?

A: All outputs are 0, all gradients are the same!
No "symmetry breaking"

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Next idea: **small random numbers** (Gaussian with zero mean, std=0.01)

W = 0.01 * np.random.randn(Din, Dout)

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Next idea: **small random numbers** (Gaussian with zero mean, std=0.01)

```
W = 0.01 * np.random.randn(Din, Dout)
```

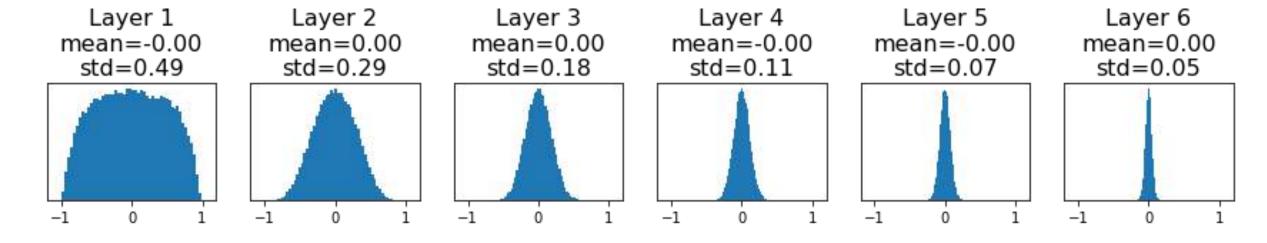
Works ~okay for small networks, but problems with deeper networks.

```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

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All activations tend to zero for deeper network layers

Q: What do the gradients dL/dW look like?



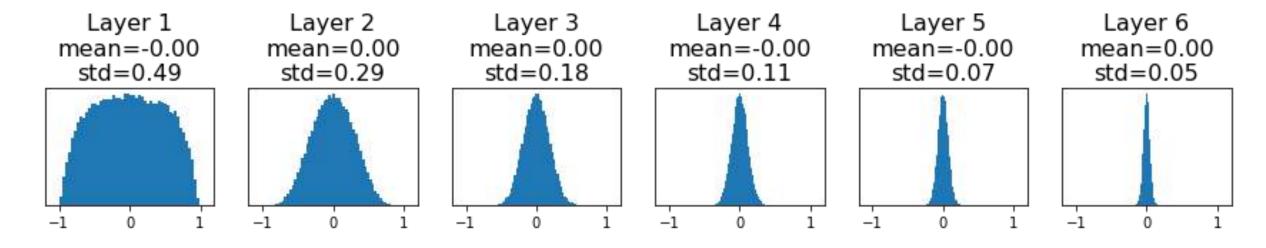
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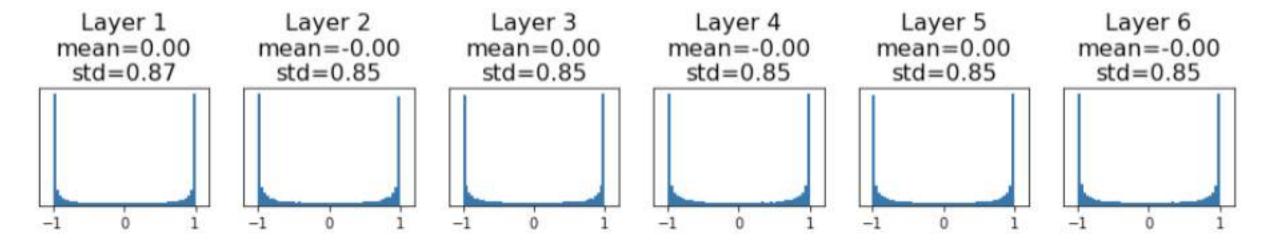
A: All zero, no learning =(



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All activations saturate

Q: What do the gradients look like?

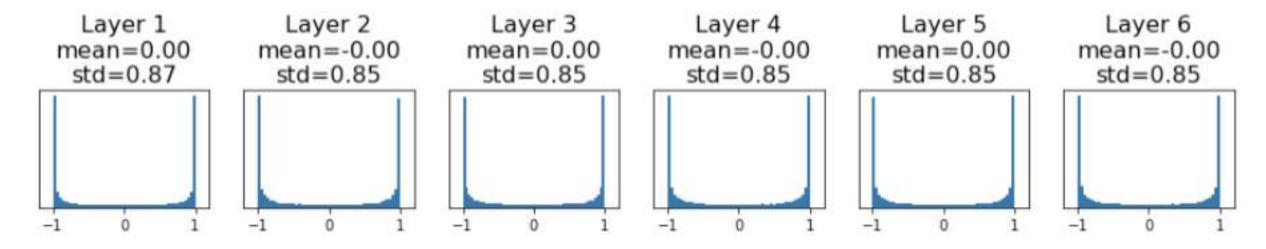


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All activations saturate

Q: What do the gradients look like?

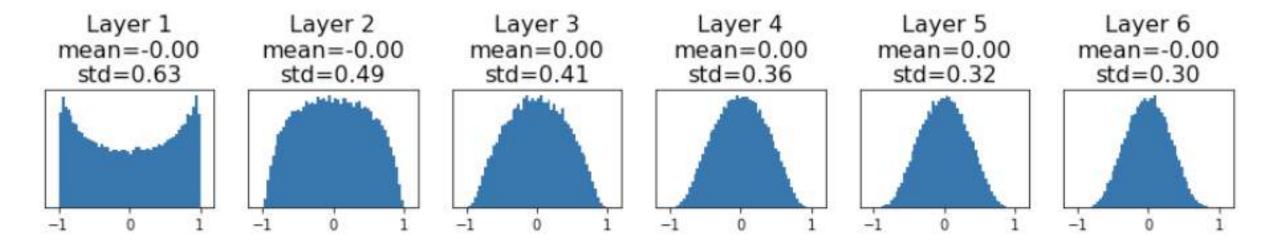
A: Local gradients all zero, no learning =(



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Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

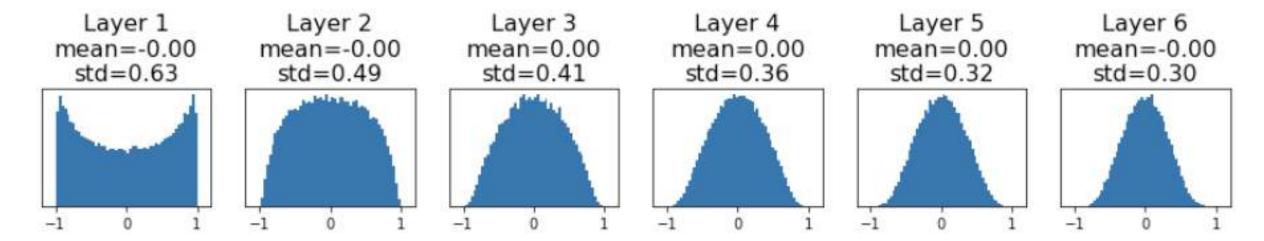
"Just right": Activations are nicely scaled for all layers!



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is kernel_size² * input_channels



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx$$

$$y_i = \sum_{j=1}^{Din} x_j w_j$$

$$Var(y_i) = Din * Var(x_i w_i)$$

[Assume x, w are iid]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

 $Var(y_i) = Din * Var(x_i w_i)$ [Assume x, w are iid] = Din * $(E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2$) [Assume x, w independent]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

 $Var(y_i) = Din * Var(x_i w_i)$ [Assume x, w are iid] = $Din * (E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2)$ [Assume x, w independent] = $Din * Var(x_i) * Var(w_i)$ [Assume x, w are zero-mean]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

 $Var(y_i) = Din * Var(x_i w_i)$ [Assume x, w are iid] = $Din * (E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2)$ [Assume x, w independent] = $Din * Var(x_i) * Var(w_i)$ [Assume x, w are zero-mean]

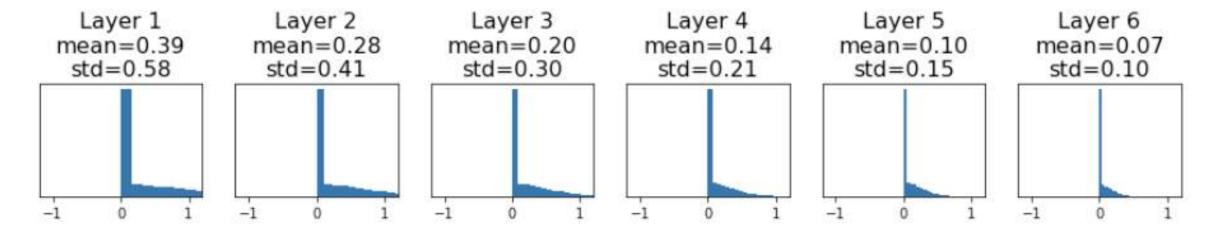
If $Var(w_i) = 1/Din then <math>Var(y_i) = Var(x_i)$

Weight Initialization: What about ReLU?

Weight Initialization: What about ReLU?

Xavier assumes zero centered activation function

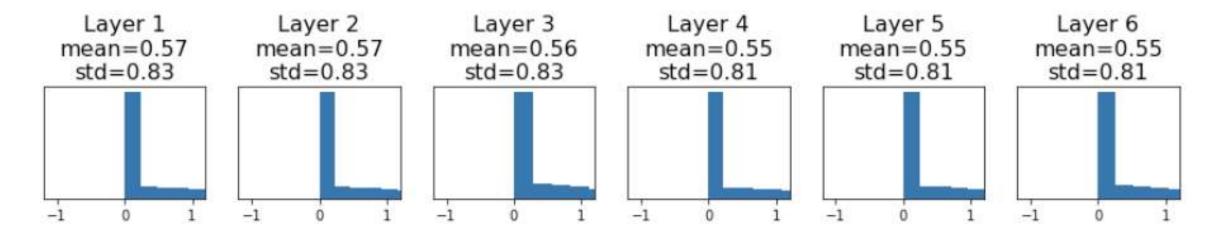
Activations collapse to zero again, no learning =(



Weight Initialization: Kaiming / MSRA Initialization

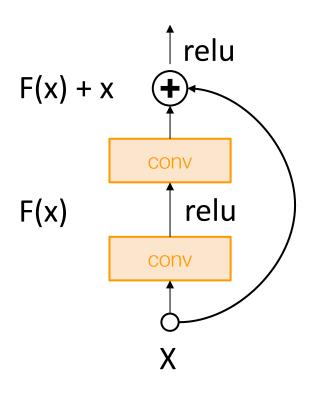
```
dims = [4096] * 7 ReLU correction: std = sqrt(2 / Din)
hs = []
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) / np.sqrt(Din)
    x = np.maximum(0, x.dot(W))
hs.append(x)
```

"Just right" – activations nicely scaled for all layers



He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

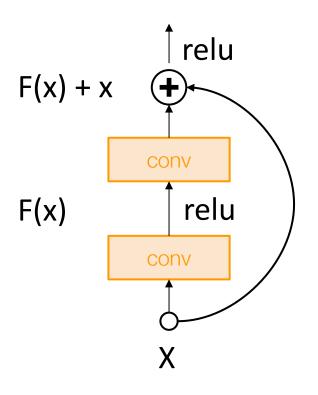
Weight Initialization: Residual Networks



Residual Block

If we initialize with MSRA: then Var(F(x)) = Var(x)But then Var(F(x) + x) > Var(x) - variance growswith each block!

Weight Initialization: Residual Networks



Residual Block

If we initialize with MSRA: then Var(F(x)) = Var(x)But then Var(F(x) + x) > Var(x) - variance growswith each block!

Solution: Initialize first conv with MSRA, initialize second conv to zero. Then Var(x + F(x)) = Var(x)

Zhang et al, "Fixup Initialization: Residual Learning Without Normalization", ICLR 2019

Proper initialization is an active area of research

Understanding the difficulty of training deep feedforward neural networks by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification by He et al., 2015

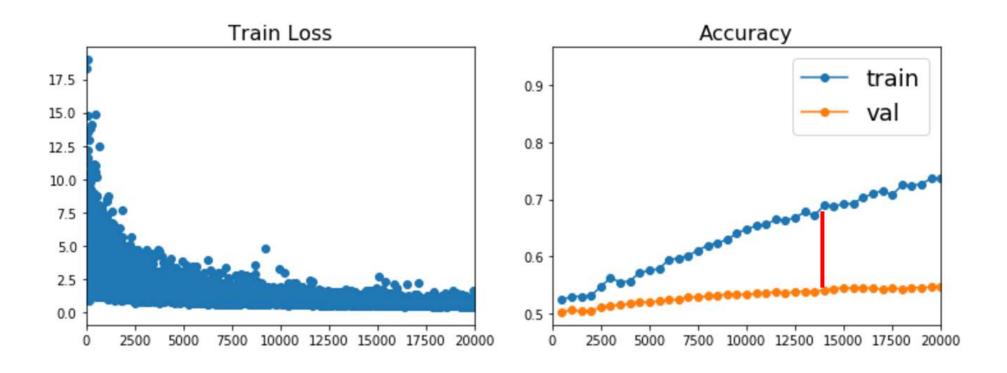
Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

All you need is a good init, Mishkin and Matas, 2015

Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019

Now your model is training ... but it overfits!



Regularization

Regularization: Add term to the loss

$$L = rac{1}{N} \sum_{i=1}^{N} \sum_{j
eq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:

L2 regularization

L1 regularization

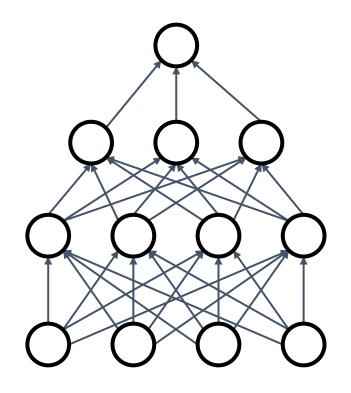
Elastic net (L1 + L2)

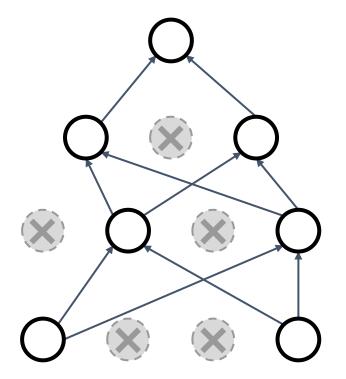
$$R(W) = \sum_k \sum_l W_{k,l}^2$$
 (Weight decay)

$$R(W) = \sum_k \sum_l |W_{k,l}|$$

$$R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$$

In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common

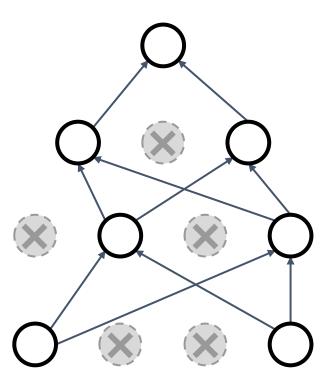


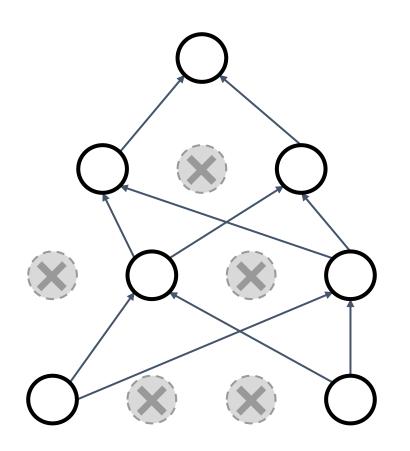


Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

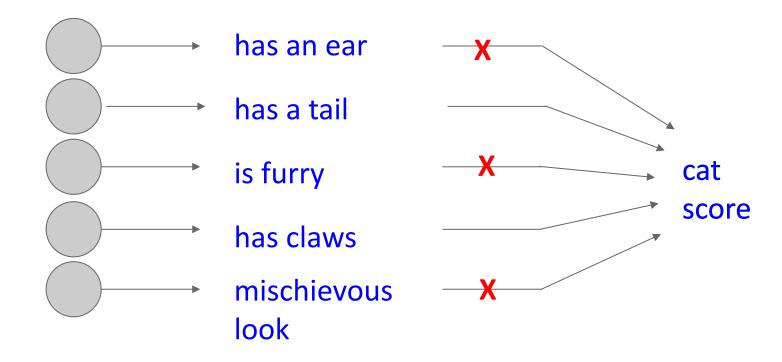
```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
```

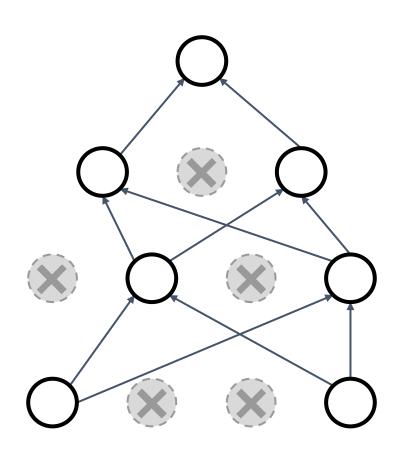
Example forward pass with a 3-layer network using dropout





Forces the network to have a redundant representation; Prevents **co-adaptation** of features





Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has $2^{4096} \sim 10^{1233}$ possible masks! Only $\sim 10^{82}$ atoms in the universe...

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Dropout: Test Time

Output Input (label) (image) $f_{\text{TM}} = f_{\text{TM}} \left(x \right)^{2} \quad \text{Random}$

mask

Dropout makes our output random!

Want to "average out" the randomness at test-time

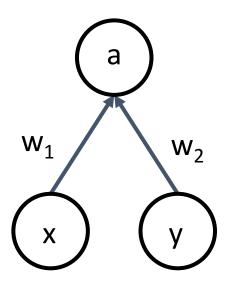
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

But this integral seems hard ...

Want to approximate the integral

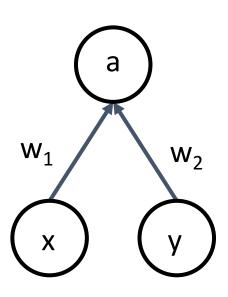
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Consider a single neuron.



Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

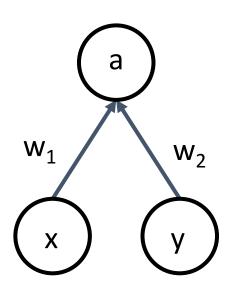


Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



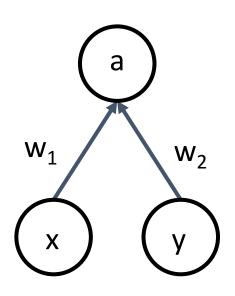
Consider a single neuron.

$$E[a] = w_1 x + w_2 y$$

$$E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y)$$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have:

During training we have:

At test time, drop nothing and **multiply** by dropout probability

$$E[a] = w_1 x + w_2 y$$

$$E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0 y) + \frac{1}{4}(0x + 0 y) + \frac{1}{4}(0x + w_2 y)$$

$$= \frac{1}{2}(w_1 x + w_2 y)$$

```
def predict(X):
    # ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: output at test time = expected output at training time

Dropout Summary

```
Vanilla Dropout: Not recommended implementation (see notes below) """
p = 0.5 # probability of keeping a unit active, higher = less dropout
def train step(X):
 """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
 H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
 out = np.dot(W3, H2) + b3
```

drop in forward pass

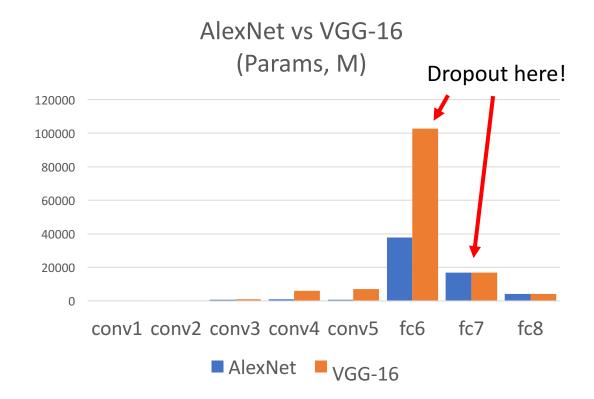
scale at test time

More common: "Inverted dropout"

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = (np.random.rand(*H1.shape) < p) / p # first dropout mask. Notice /p!
                                                                            Drop and scale
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
                                                                            during training
 U2 = (np.random.rand(*H2.shape) < p) / p # second dropout mask. Notice /p!
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
                                                                    test time is unchanged!
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) # no scaling necessary
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 out = np.dot(W3, H2) + b3
```

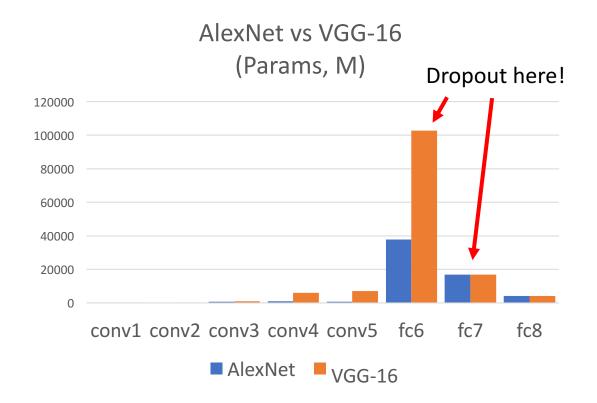
Dropout architectures

Recall AlexNet, VGG have most of their parameters in **fully-connected layers**; usually Dropout is applied there



Dropout architectures

Recall AlexNet, VGG have most of their parameters in **fully-connected layers**; usually Dropout is applied there



Later architectures (GoogLeNet, ResNet, etc) use global average pooling instead of fully-connected layers: they don't use dropout at all!

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Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Example: Batch Normalization

Training: Normalize using stats from random minibatches

Testing: Use fixed stats to normalize

Training: Add some kind of randomness

$$y = f_W(x, z)$$

For ResNet and later, often L2 and Batch Normalization are the only regularizers!

Testing: Average out randomness (sometimes approximate)

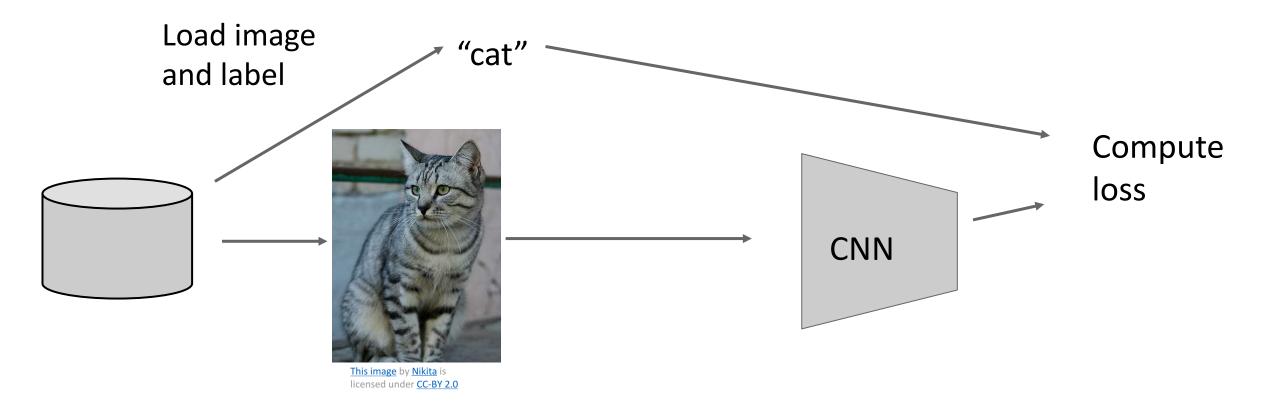
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Example: Batch Normalization

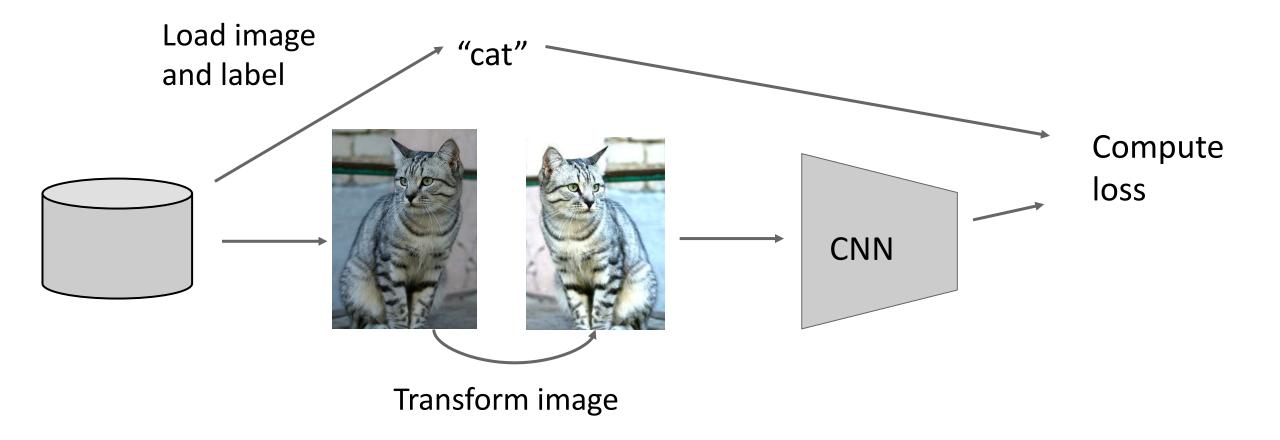
Training: Normalize using stats from random minibatches

Testing: Use fixed stats to normalize

Data Augmentation



Data Augmentation



Data Augmentation: Horizontal Flips





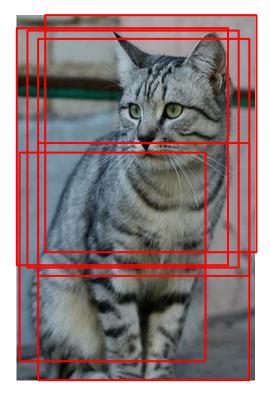


Data Augmentation: Random Crops and Scales

Training: sample random crops / scales

ResNet:

- Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



Data Augmentation: Random Crops and Scales

Training: sample random crops / scales

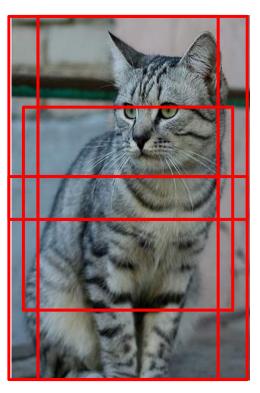
ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



ResNet:

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips



Data Augmentation: Color Jitter

Simple: Randomize contrast and brightness





More Complex:

- 1. Apply PCA to all [R, G, B] pixels in training set
- Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(Used in AlexNet, ResNet, etc)

Data Augmentation: Get creative for your problem!

Random mix/combinations of:

- translation
- rotation
- stretching
- shearing,
- lens distortions, ... (go crazy)

Training: Add some randomness

Testing: Marginalize over randomness

Examples:

Dropout

Batch Normalization

Data Augmentation

Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

Regularization: DropConnect

Training: Drop random connections between neurons (set weight=0)

Testing: Use all the connections

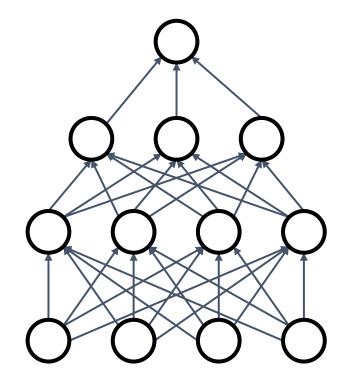
Examples:

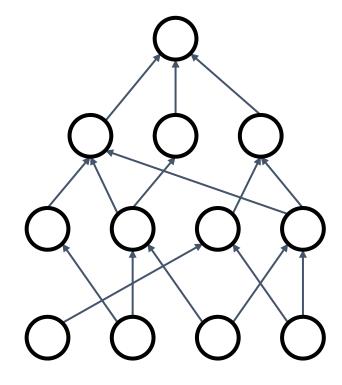
Dropout

Batch Normalization

Data Augmentation

DropConnect





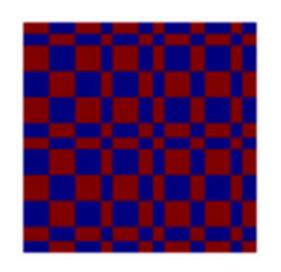
Regularization: Fractional Pooling

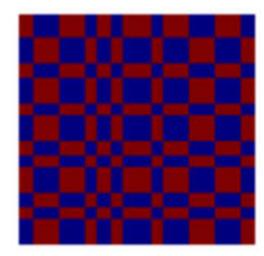
Training: Use randomized pooling regions

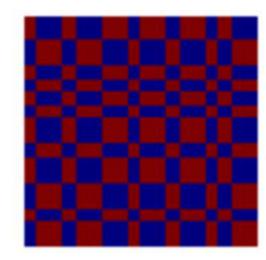
Testing: Average predictions over different samples

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling







Graham, "Fractional Max Pooling", arXiv 2014

Regularization: Stochastic Depth

Training: Skip some residual blocks in ResNet

Testing: Use the whole network

Examples:

Dropout

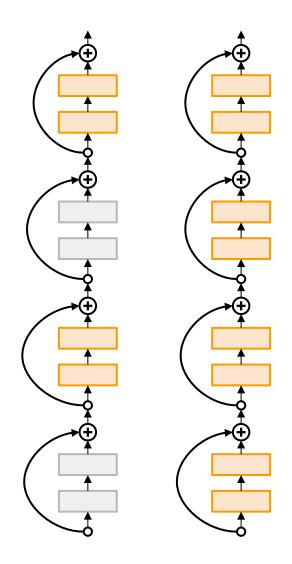
Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth



Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

Regularization: Stochastic Depth

Training: Set random images regions to 0

Testing: Use the whole image

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout









Works very well for small datasets like CIFAR, less common for large datasets like ImageNet

DeVries and Taylor, "Improved Regularization of Convolutional Neural Networks with Cutout", arXiv 2017

Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

1.0 0.8 0.6 0.4 0.2 0.0 0.2 0.4 0.6 0.8 1.0

Sample blend probability from a beta distribution Beta(a, b) with a=b≈0 so blend weights are close to 0/1

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout
Mixup







Target label: cat: 0.4 dog: 0.6

CNN

Randomly blend the pixels of pairs of training images, e.g. 40% cat, 60% dog

Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

Examples:

Dropout
Batch Normalization
Data Augmentation
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CNN

Target label: cat: 0.4 dog: 0.6

Randomly blend the pixels of pairs of training images, e.g. 40% cat, 60% dog

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Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout

Mixup

- Consider dropout for large fullyconnected layers
- Batch normalization and data augmentation almost always a good idea
- Try cutout and mixup especially for small classification datasets

Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

Summary

1. One time setup

Activation functions, data preprocessing, weight initialization, regularization

2. Training dynamics

Learning rate schedules; large-batch training; hyperparameter optimization

3. After training

Model ensembles, transfer learning

Today

Next time

Justin Johnson Lecture 10 - 100 October 7, 2019

Next time: Training Neural Networks (part 2)