

Lecture 19: Generative Models, Part 1

Last Time: Videos

Many video models:

Single-frame CNN (Try this first!)

Late fusion

Early fusion

3D CNN / C3D

Two-stream networks

CNN + RNN

Convolutional RNN

Spatio-temporal self-attention

SlowFast networks (current SoTA)

Today: Generative Models, Part 1

Supervised vs Unsupervised Learning

Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a *function* to map $x \rightarrow y$

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Classification



Cat

[This image](#) is [CC0 public domain](#)

Supervised vs Unsupervised Learning

Supervised Learning

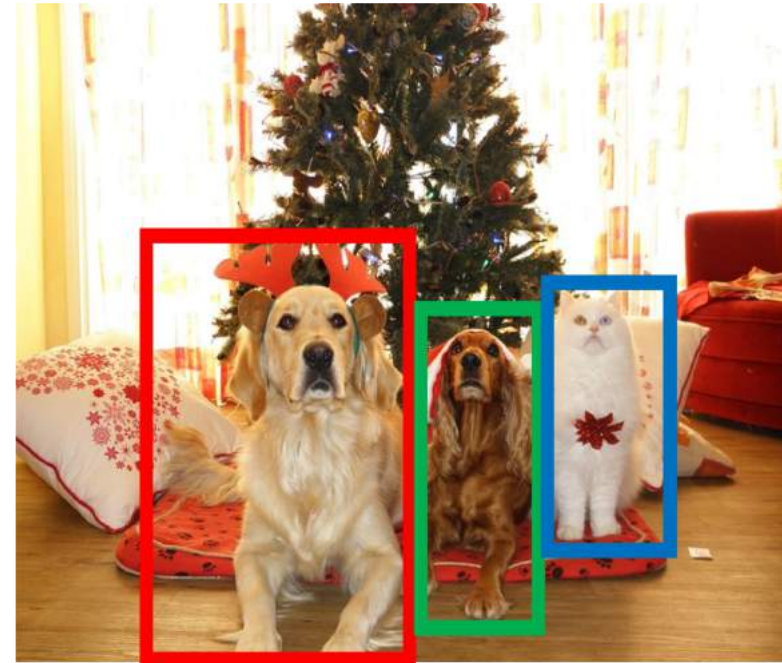
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Object Detection



DOG, DOG, CAT

[This image is CC0 public domain](#)

Supervised vs Unsupervised Learning

Supervised Learning

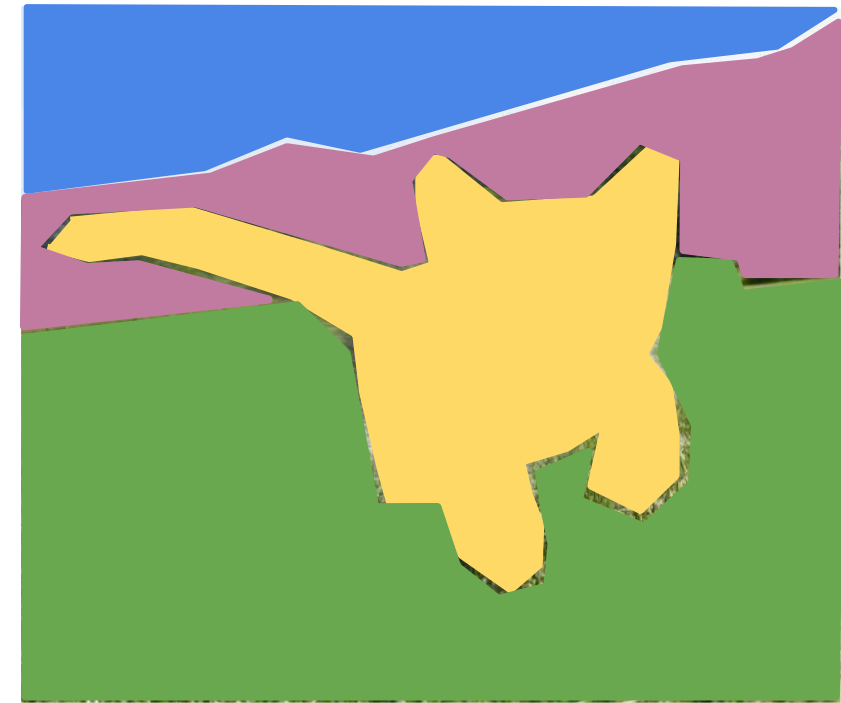
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Semantic Segmentation



GRASS, CAT, TREE, SKY

Supervised vs Unsupervised Learning

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Image captioning



A cat sitting on a suitcase on the floor

Caption generated using [neuraltalk2](#)
Image is [CC0 Public domain](#).

Supervised vs Unsupervised Learning

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Unsupervised Learning

Data: x

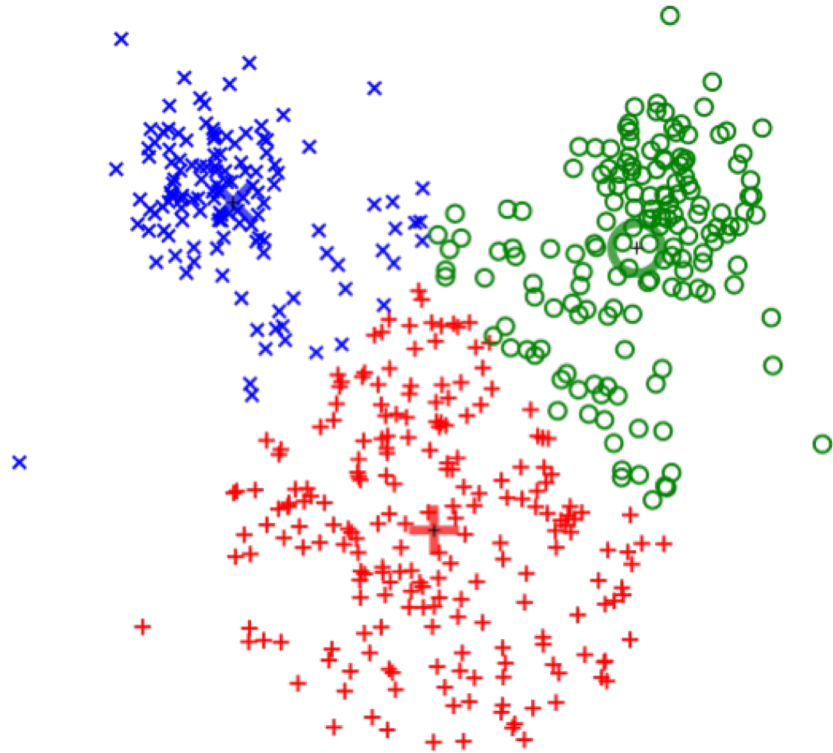
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Supervised vs Unsupervised Learning

Clustering
(e.g. K-Means)



[This image](#) is [CC0 public domain](#)

Unsupervised Learning

Data: x

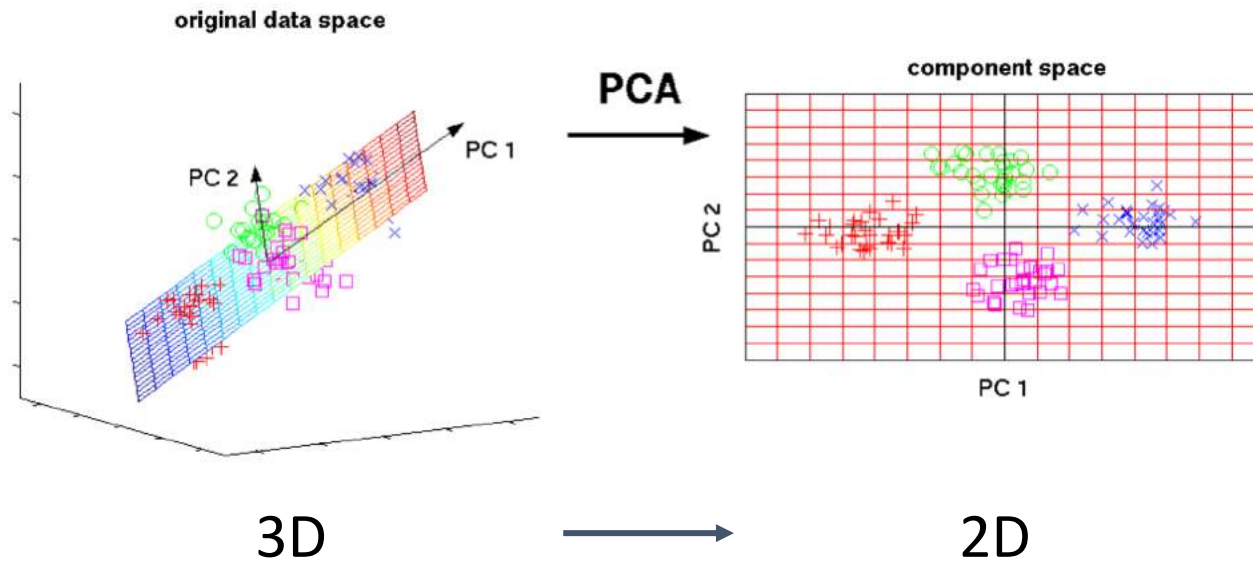
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Supervised vs Unsupervised Learning

Dimensionality Reduction (e.g. Principal Components Analysis)



[This image](#) from Matthias Scholz is [CC0 public domain](#)

Unsupervised Learning

Data: x

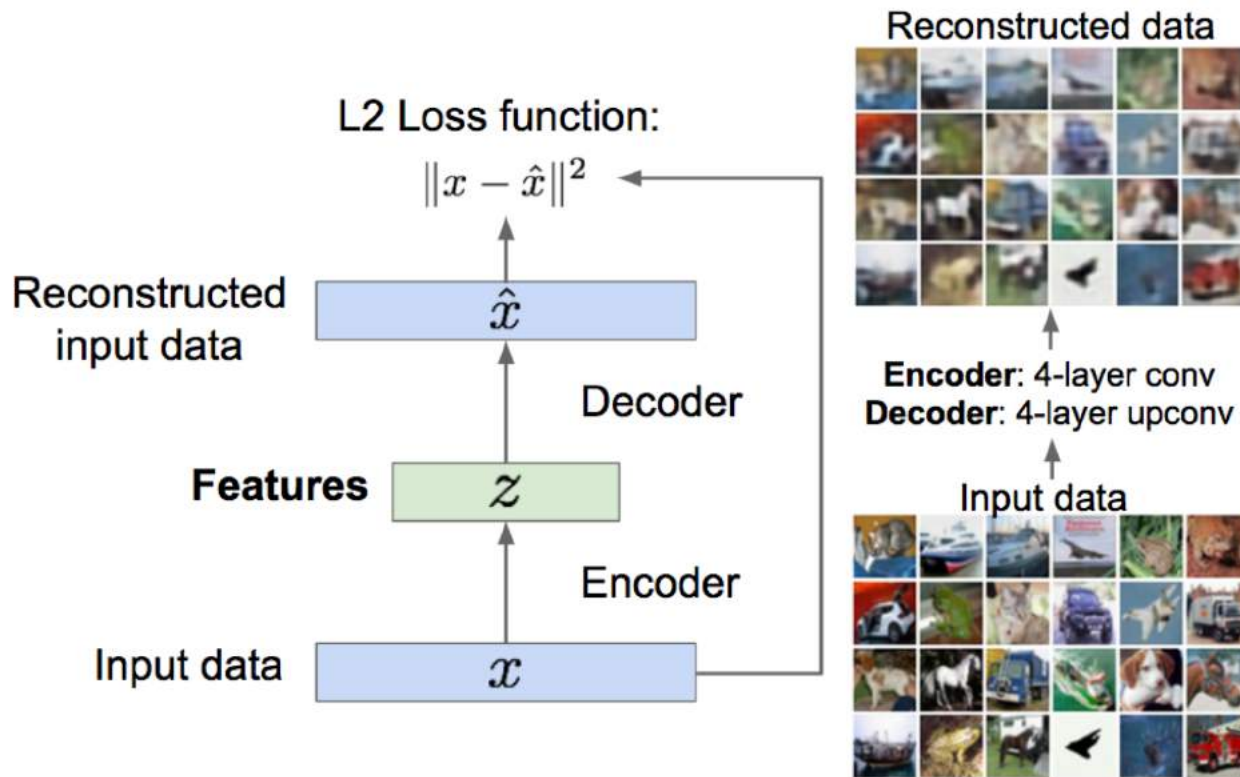
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Supervised vs Unsupervised Learning

Feature Learning
(e.g. autoencoders)



Unsupervised Learning

Data: x

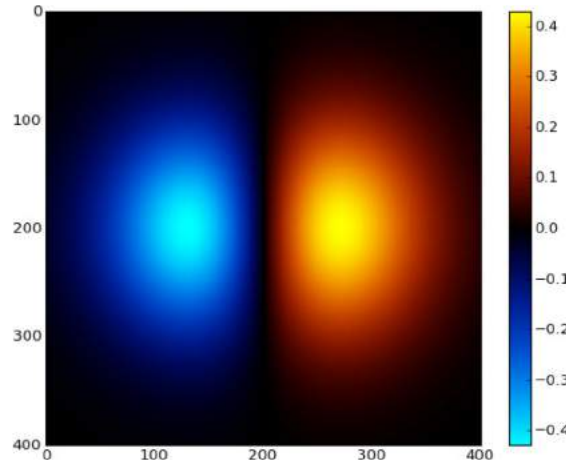
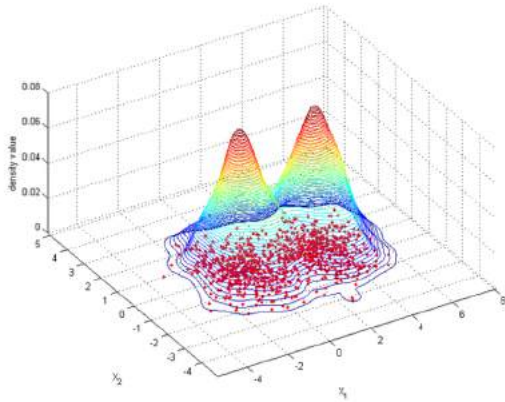
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Supervised vs Unsupervised Learning

Density Estimation



Unsupervised Learning

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Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Images [left](#) and [right](#) are [CC0 public domain](#)

Supervised vs Unsupervised Learning

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Unsupervised Learning

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Discriminative vs Generative Models

Discriminative Model:

Learn a probability distribution $p(y|x)$

Generative Model:

Learn a probability distribution $p(x)$

Conditional Generative Model: Learn $p(x|y)$

Data: x



Label: y

Cat

Discriminative vs Generative Models

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Label: y
Cat

Probability Recap:

Density Function

$p(x)$ assigns a positive number to each possible x ; higher numbers mean x is more likely

Density functions are **normalized**:

$$\int_x p(x)dx = 1$$

Different values of x **compete** for density

Discriminative vs Generative Models

Discriminative Model:

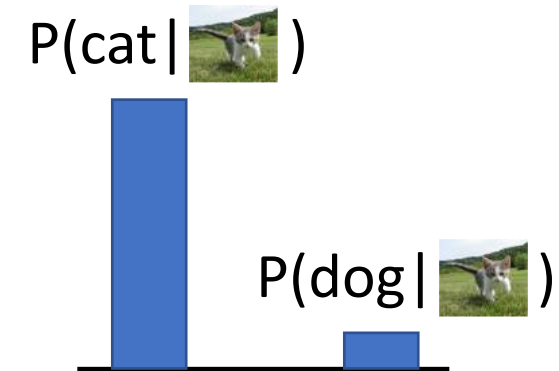
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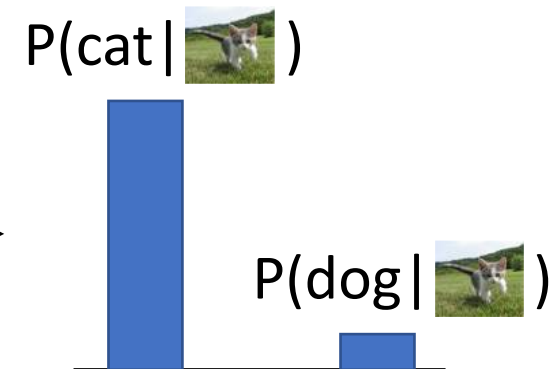
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Discriminative vs Generative Models

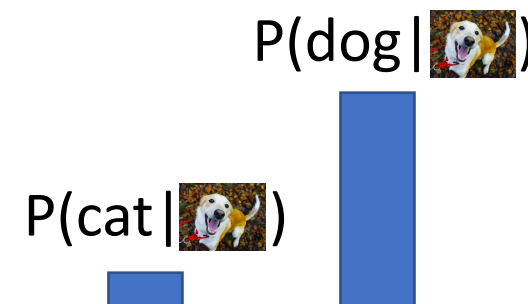
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Generative Model:

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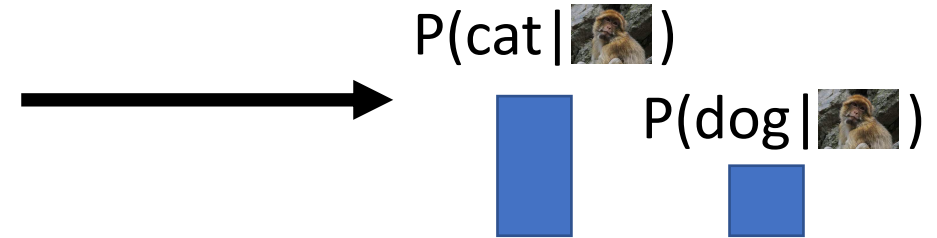
Conditional Generative Model: Learn $p(x|y)$

Discriminative model: the possible labels for each input "compete" for probability mass.
But no competition between **images**

Discriminative vs Generative Models

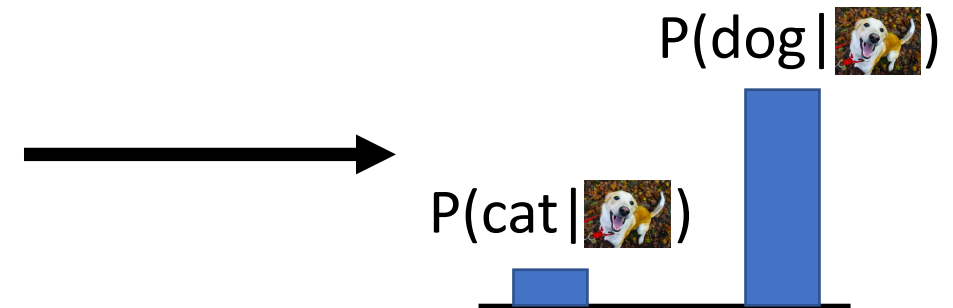
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Generative Model:

Learn a probability distribution $p(x)$



Conditional Generative Model: Learn $p(x|y)$

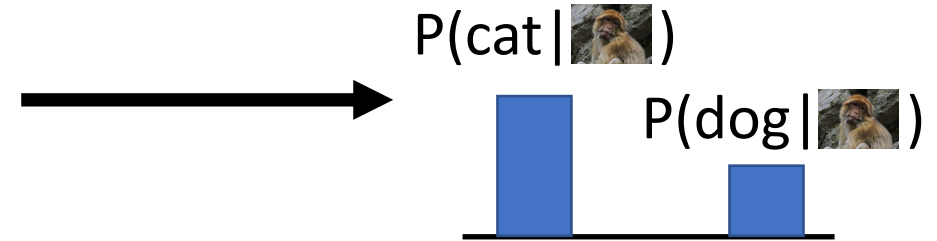
Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

[Monkey image](#) is CC0 Public Domain

Discriminative vs Generative Models

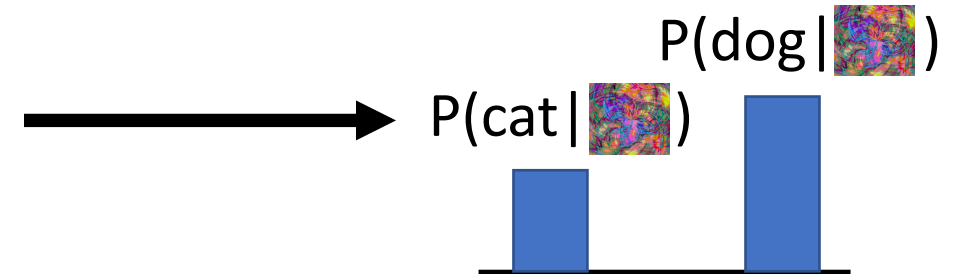
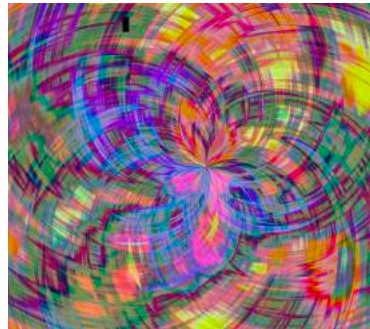
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Conditional Generative Model: Learn $p(x|y)$

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Monkey image is CC0 Public Domain
Abstract image is free to use under the [Pixabay license](#)

Discriminative vs Generative Models

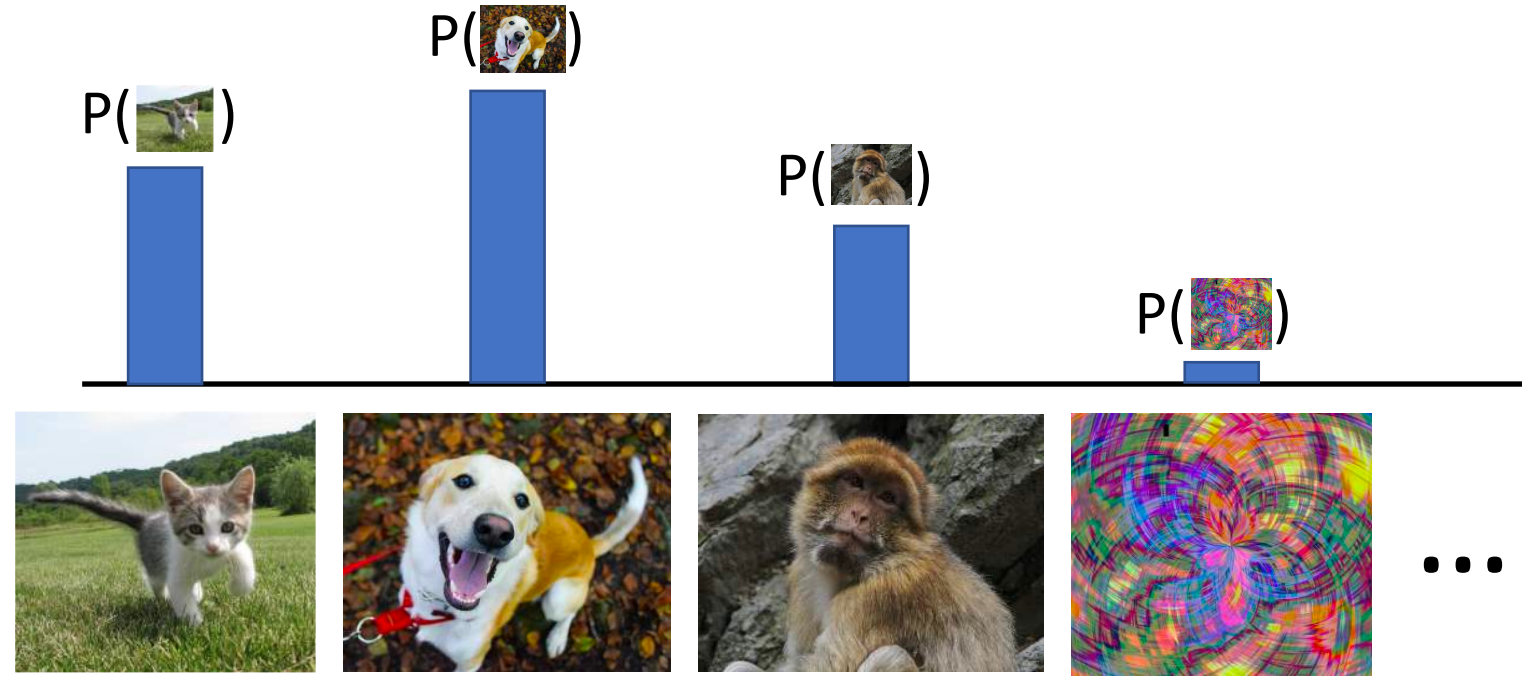
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Conditional Generative Model: Learn $p(x|y)$



Generative model: All possible images compete with each other for probability mass

Discriminative vs Generative Models

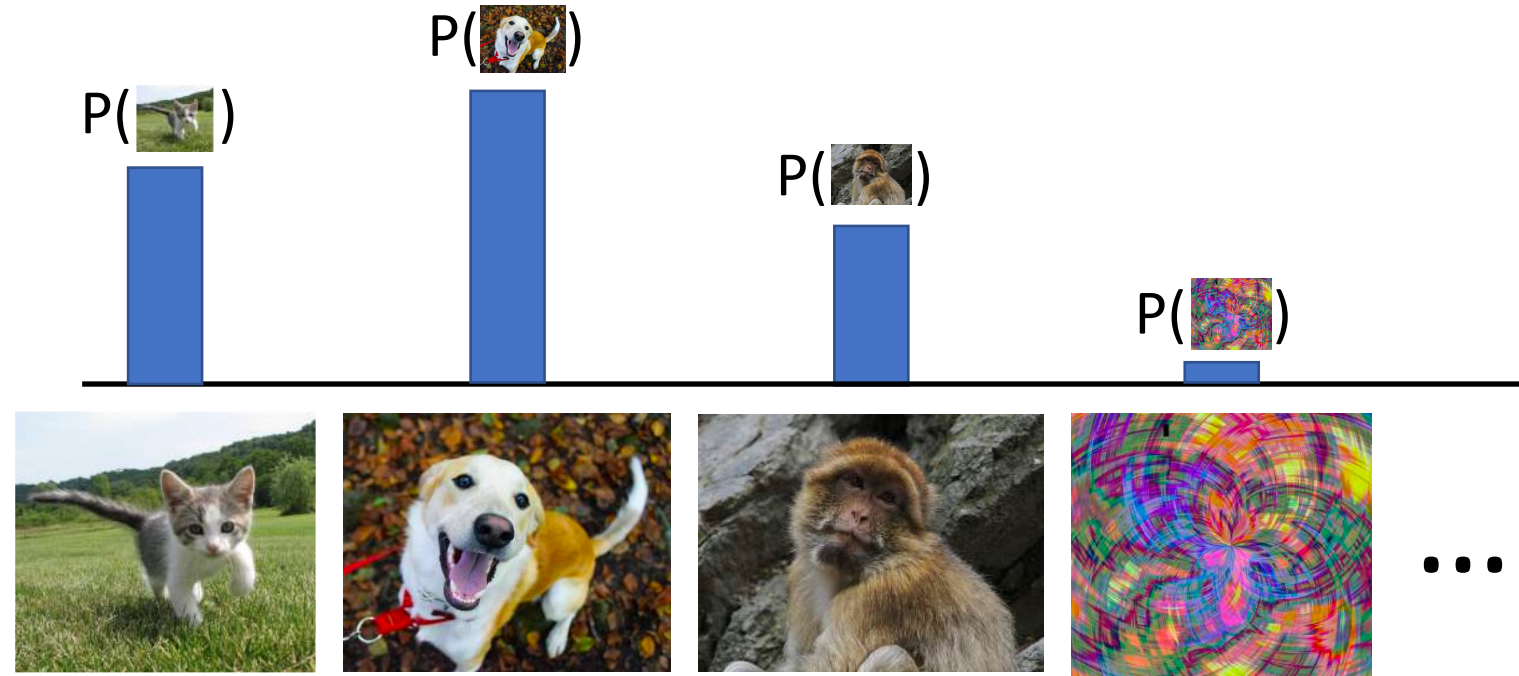
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Conditional Generative Model: Learn $p(x|y)$



Generative model: All possible images compete with each other for probability mass

Requires deep image understanding! Is a dog more likely to sit or stand? How about 3-legged dog vs 3-armed monkey?

Discriminative vs Generative Models

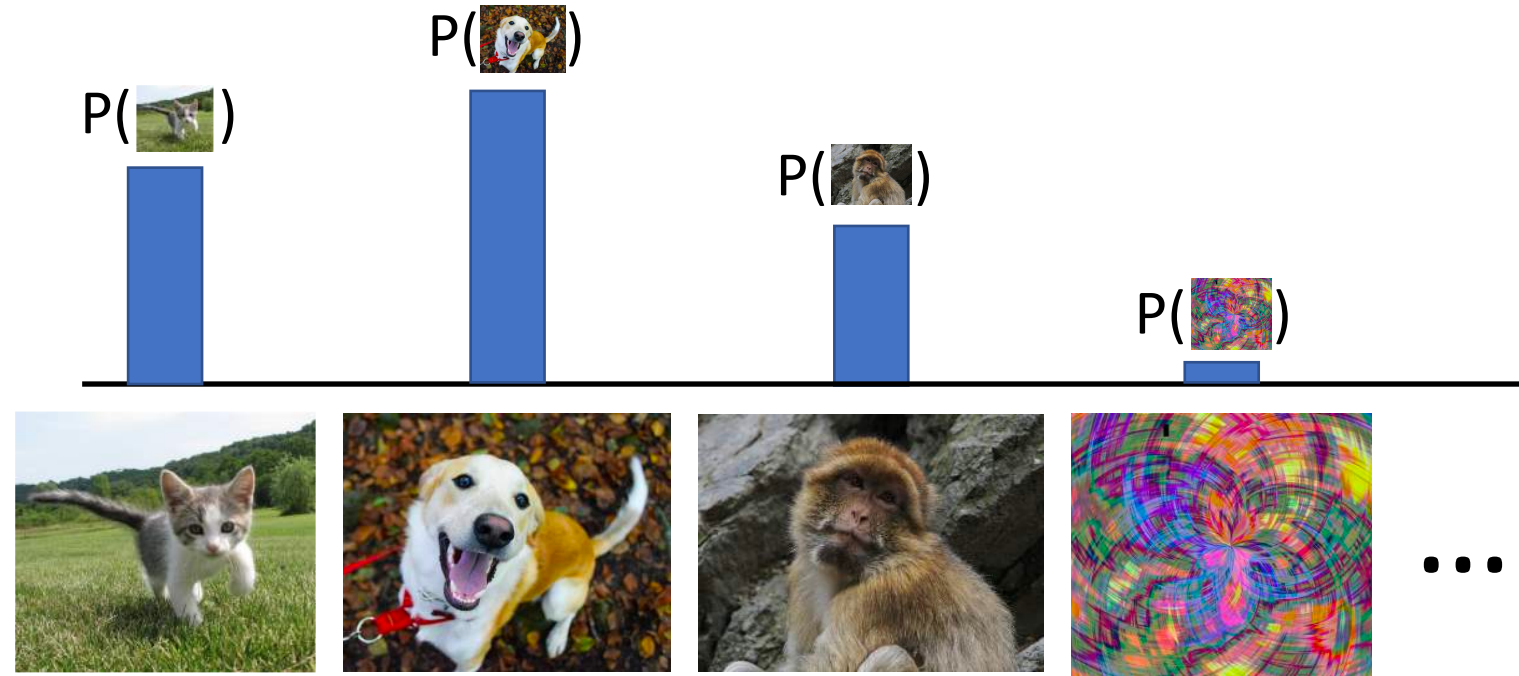
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Generative model: All possible images compete with each other for probability mass

Model can “reject” unreasonable inputs by assigning them small values

Discriminative vs Generative Models

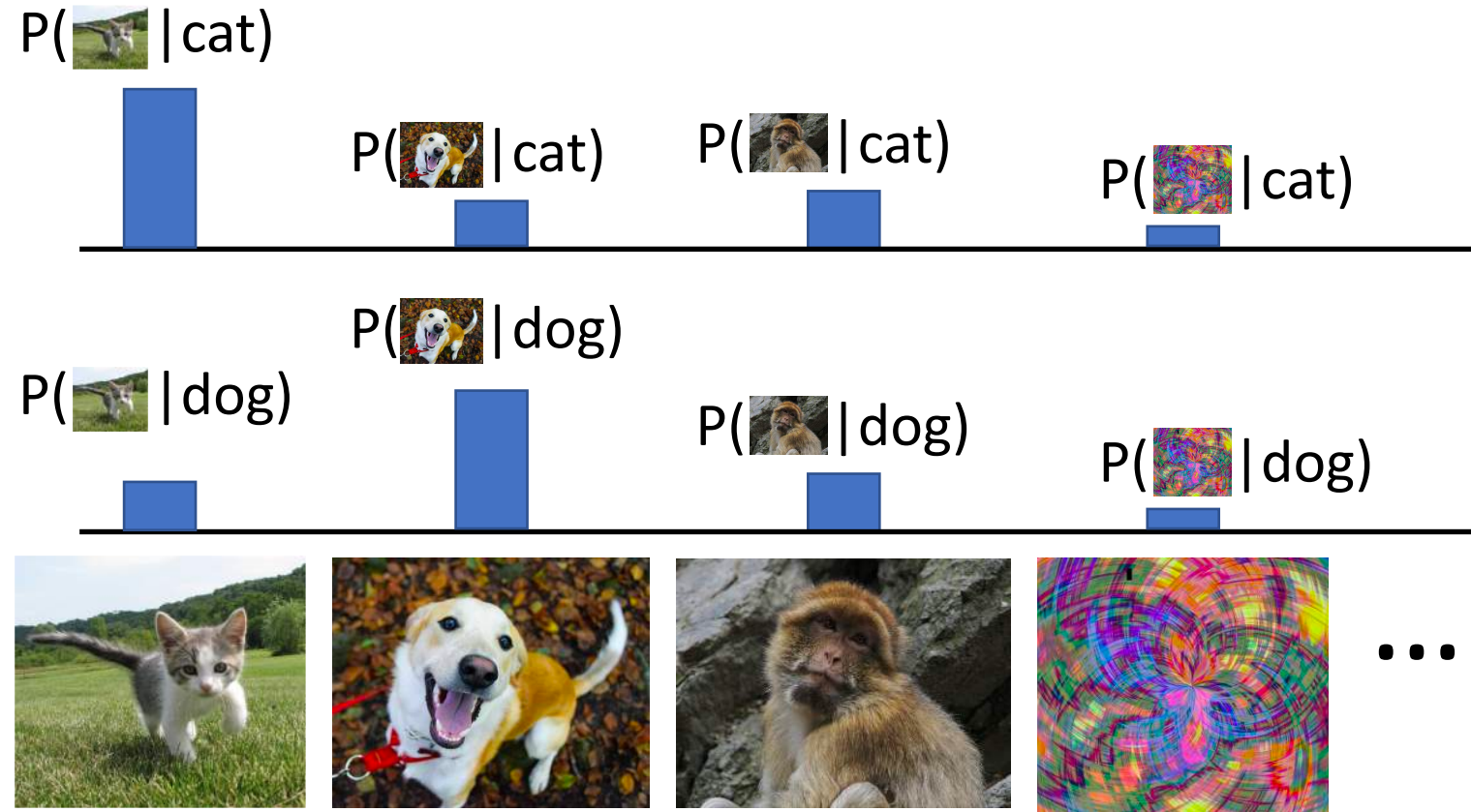
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Conditional Generative Model: Learn $p(x|y)$



Conditional Generative Model: Each possible label induces a competition among all images

Discriminative vs Generative Models

Discriminative Model:

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Generative Model:

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Conditional Generative Model: Learn $p(x|y)$

Recall **Bayes' Rule:**

$$P(x | y) = \frac{P(y | x) P(x)}{P(y)}$$

Discriminative vs Generative Models

Discriminative Model:

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Generative Model:

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Conditional Generative Model: Learn $p(x|y)$

Recall **Bayes' Rule**:

$$\underbrace{P(x|y)}_{\text{Conditional Generative Model}} = \frac{\underbrace{P(y|x)}_{\text{Discriminative Model}}}{\underbrace{P(y)}_{\text{Prior over labels}}} \underbrace{P(x)}_{\text{(Unconditional) Generative Model}}$$

We can build a conditional generative model from other components!

What can we do with a discriminative model?

Discriminative Model:

Learn a probability
distribution $p(y|x)$



Assign labels to data
Feature learning (with labels)

Generative Model:

Learn a probability
distribution $p(x)$

**Conditional Generative
Model:** Learn $p(x|y)$

What can we do with a generative model?

Discriminative Model:

Learn a probability distribution $p(y|x)$



Assign labels to data
Feature learning (with labels)

Generative Model:

Learn a probability distribution $p(x)$



Detect outliers
Feature learning (without labels)
Sample to generate new data

Conditional Generative Model: Learn $p(x|y)$

What can we do with a generative model?

Discriminative Model:

Learn a probability distribution $p(y|x)$



Assign labels to data
Feature learning (supervised)

Generative Model:

Learn a probability distribution $p(x)$



Detect outliers
Feature learning (unsupervised)
Sample to **generate** new data

Conditional Generative Model: Learn $p(x|y)$



Assign labels, while rejecting outliers!
Generate new data conditioned on input labels

Taxonomy of Generative Models

Generative models

Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Taxonomy of Generative Models

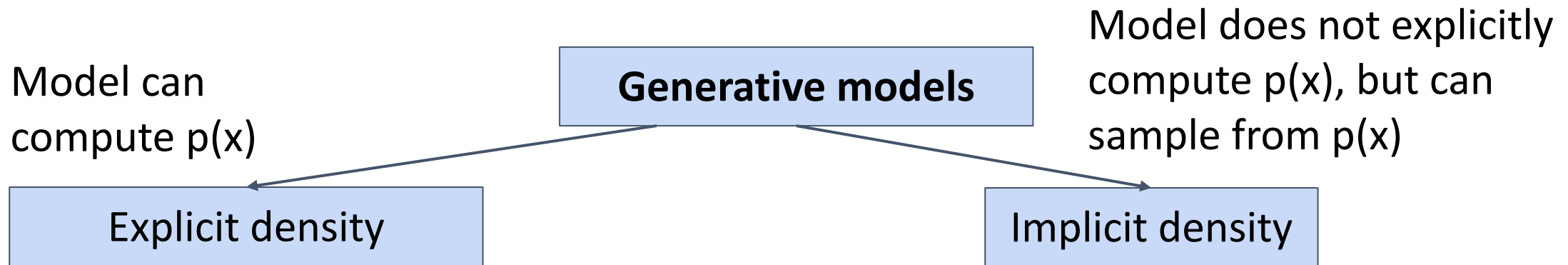


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Taxonomy of Generative Models

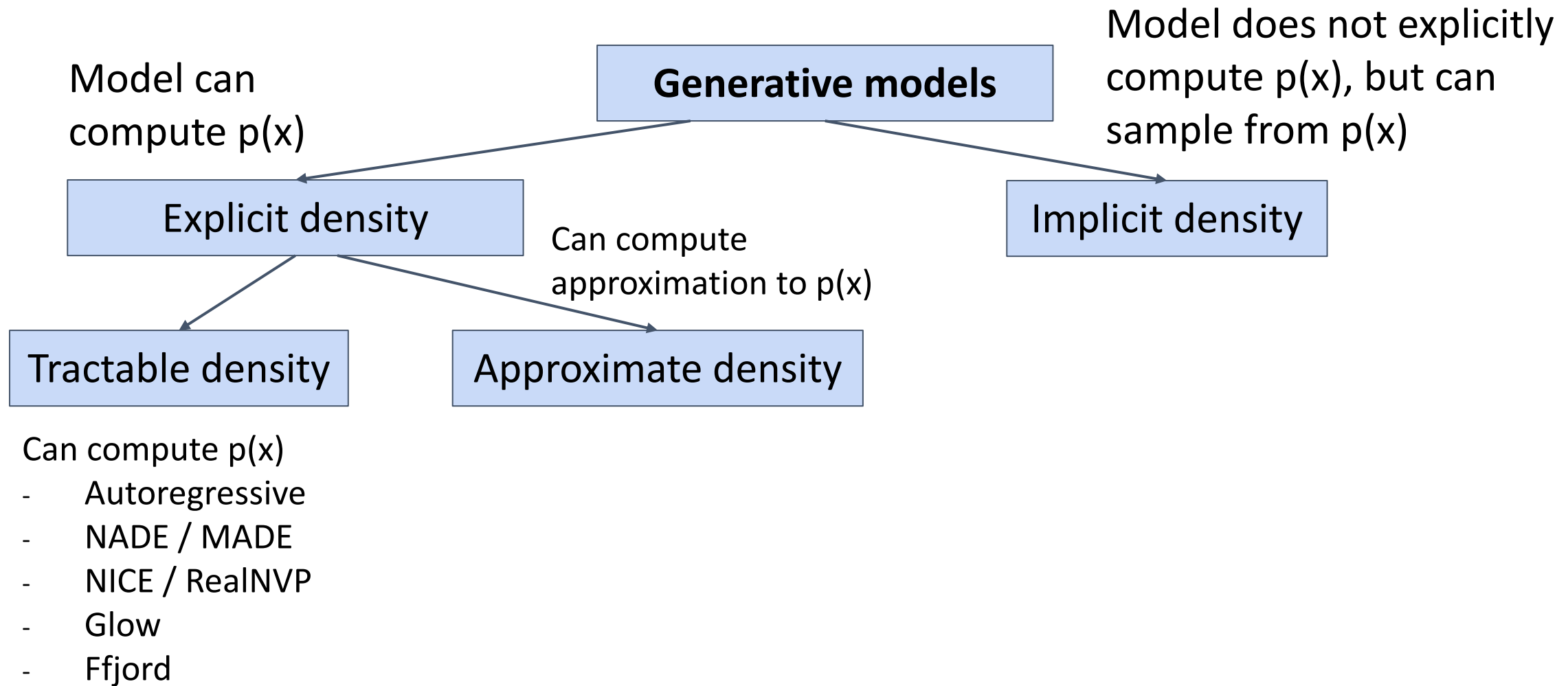


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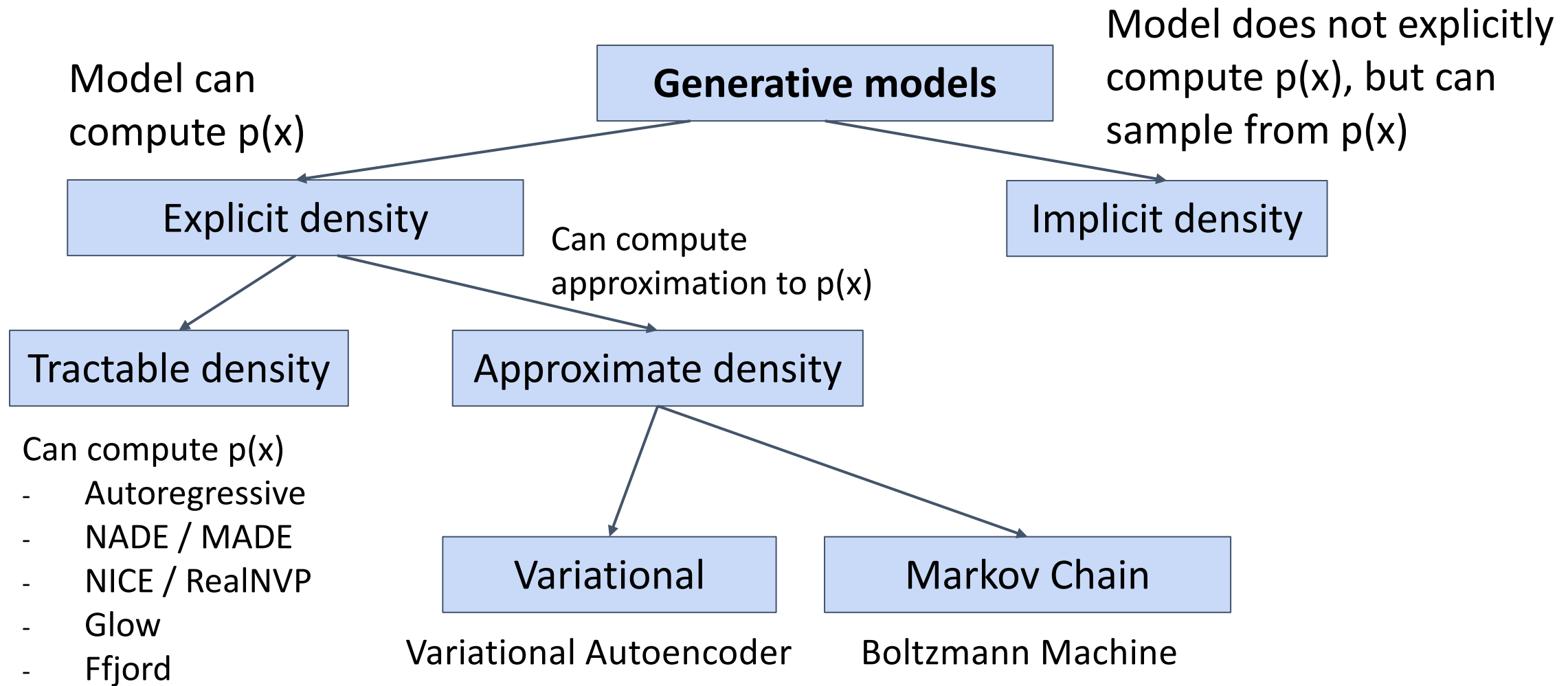


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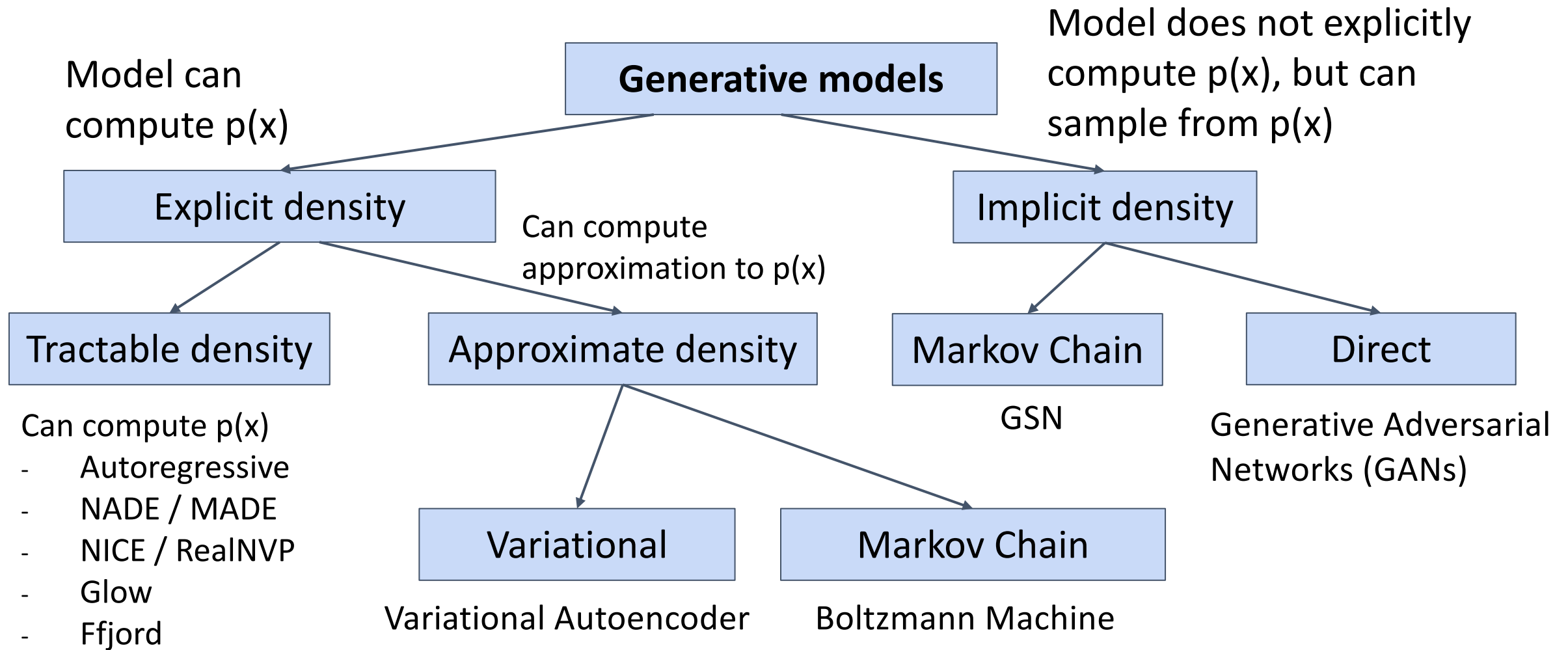


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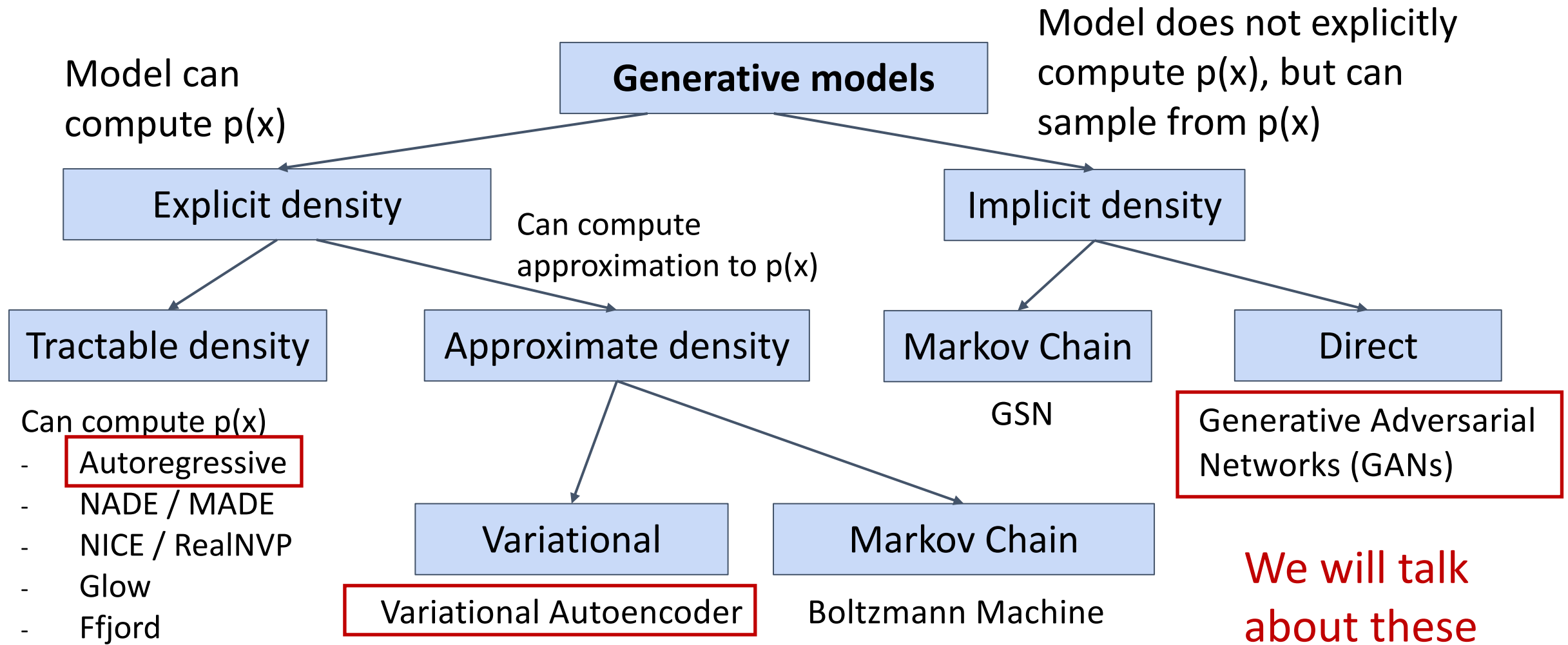


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Autoregressive models

Explicit Density Estimation

Goal: Write down an explicit function for $p(x) = f(x, W)$

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Given dataset $x^{(1)}, x^{(2)}, \dots, x^{(N)}$, train the model by solving:

$$W^* = \arg \max_W \prod_i p(x^{(i)})$$

Maximize probability of training data
(Maximum likelihood estimation)

Explicit Density Estimation

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$$= \arg \max_W \sum_i \log p(x^{(i)})$$

Log trick to exchange product for sum

Explicit Density Estimation

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Log trick to exchange product for sum

$$= \arg \max_W \sum_i \log f(x^{(i)}, W)$$

This will be our loss function!
Train with gradient descent

Explicit Density: Autoregressive Models

Goal: Write down an explicit function for $p(x) = f(x, W)$

Assume x consists of
multiple subparts:

$$x = (x_1, x_2, x_3, \dots, x_T)$$

Explicit Density: Autoregressive Models

Goal: Write down an explicit function for $p(x) = f(x, W)$

Assume x consists of multiple subparts:

$$x = (x_1, x_2, x_3, \dots, x_T)$$

Break down probability using the chain rule:

$$\begin{aligned} p(x) &= p(x_1, x_2, x_3, \dots, x_T) \\ &= p(x_1)p(x_2 | x_1)p(x_3 | x_1, x_2) \dots \end{aligned}$$

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Probability of the next subpart
given all the previous subparts

Explicit Density: Autoregressive Models

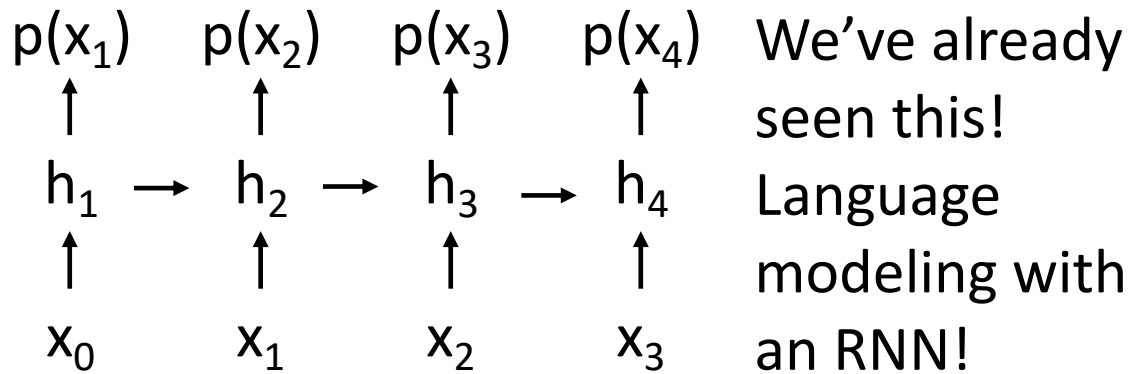
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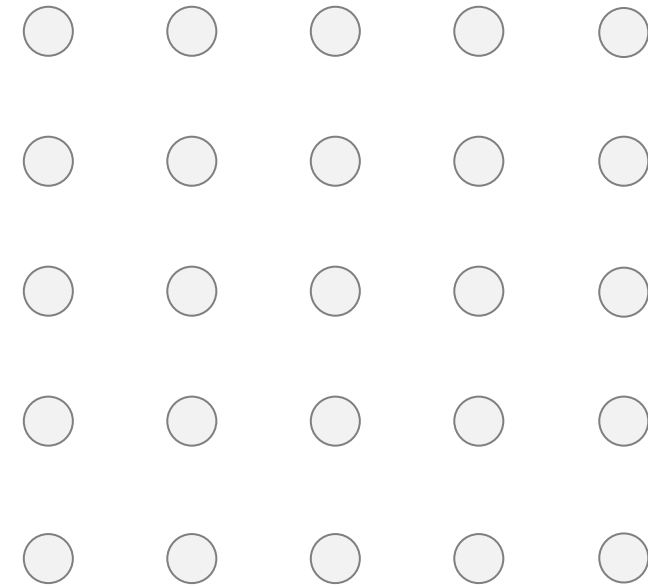
PixelRNN

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over $[0, 1, \dots, 255]$



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

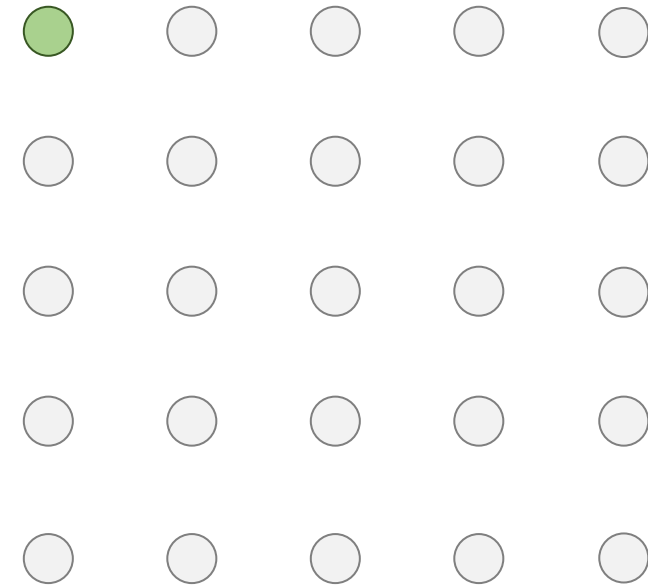
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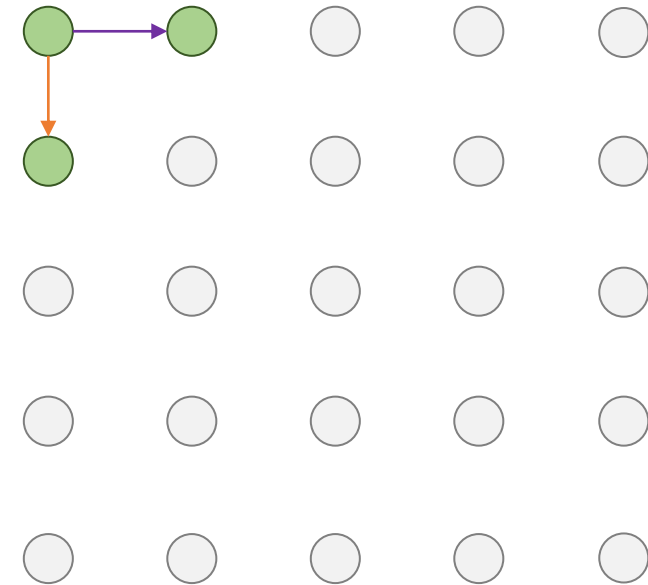
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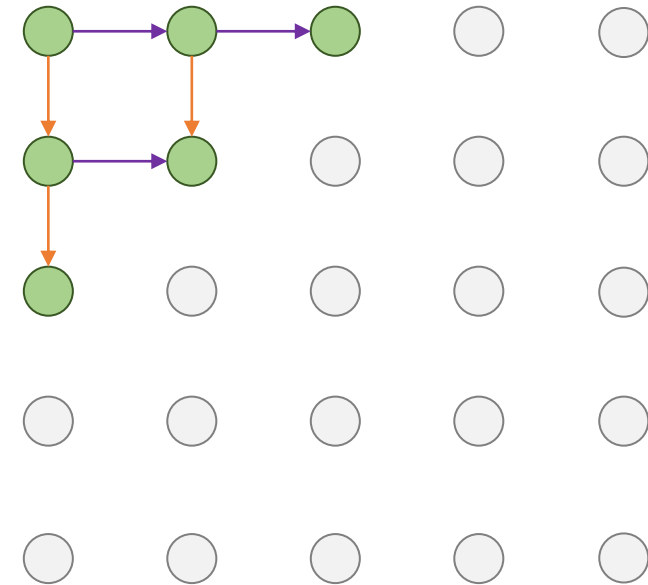
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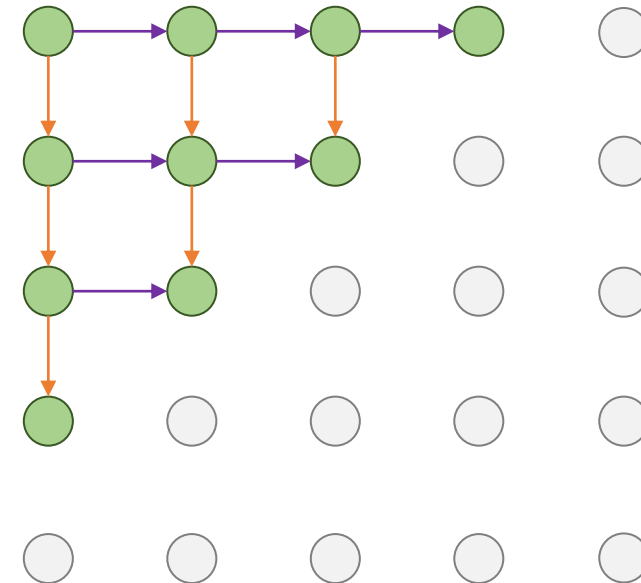
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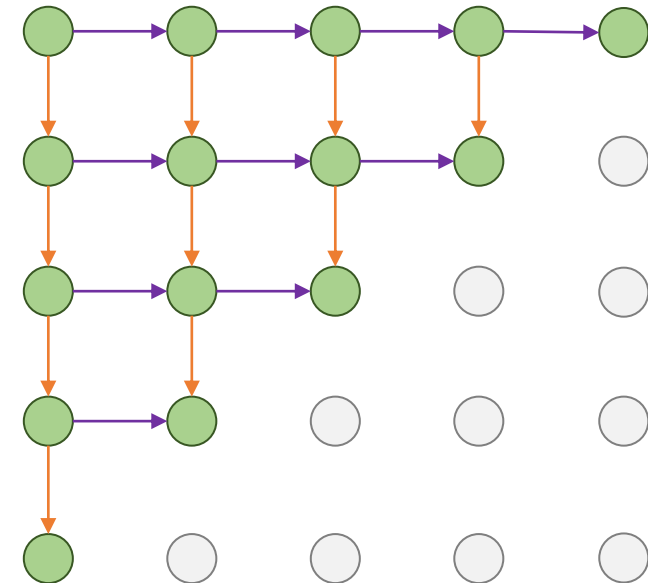
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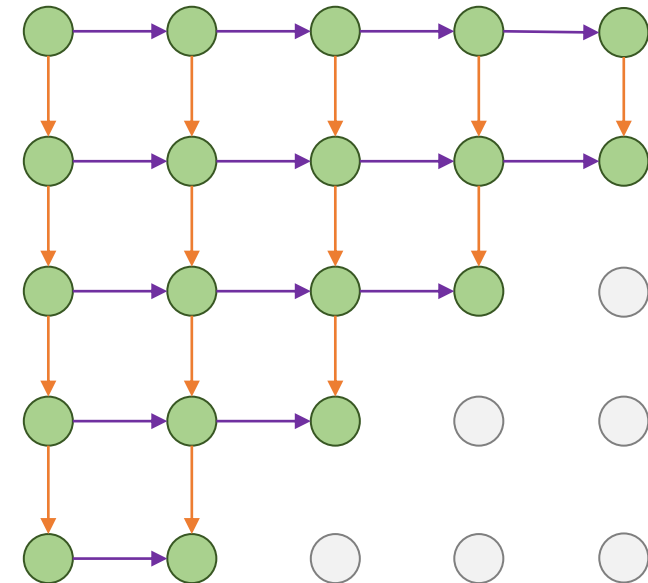
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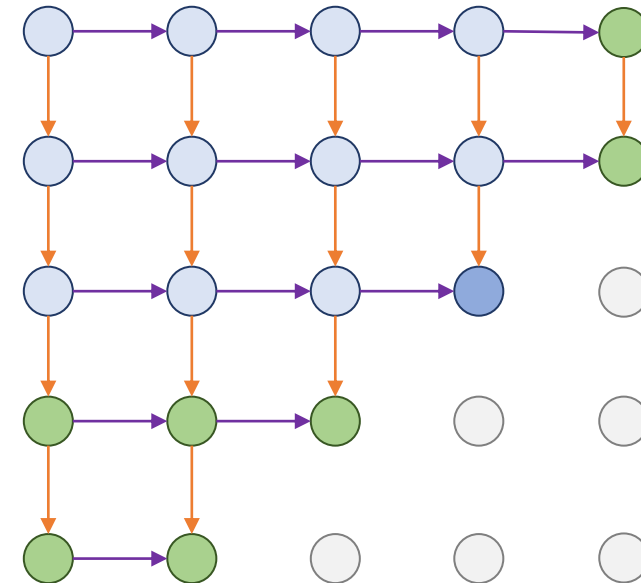
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Each pixel depends **implicitly** on all pixels above and to the left:



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

PixelRNN

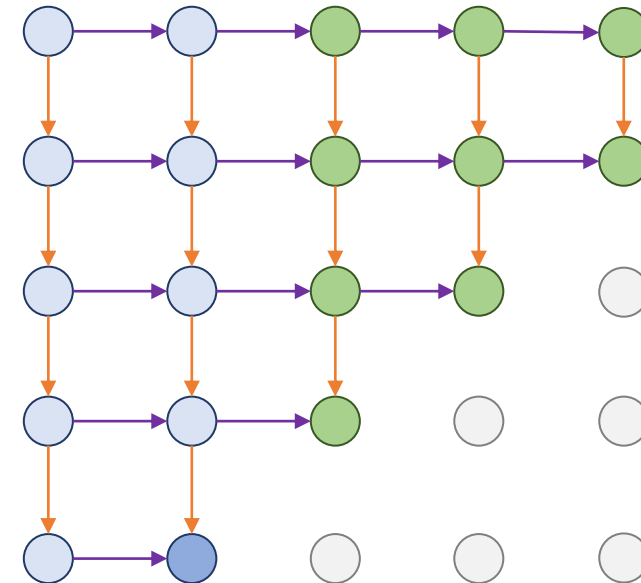
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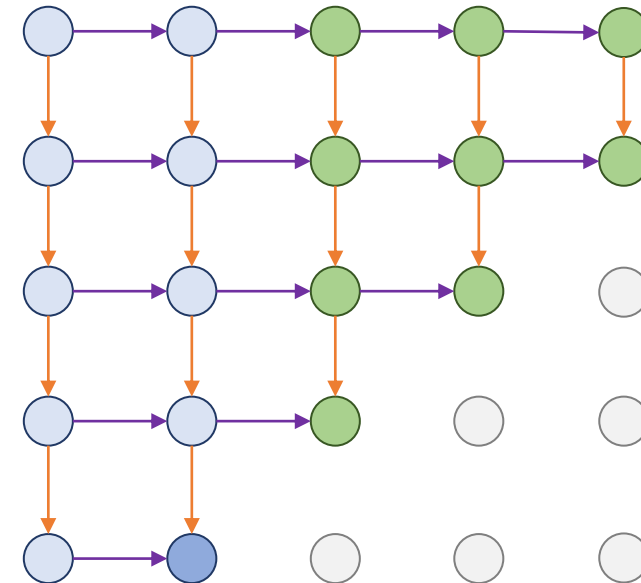
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Each pixel depends **implicitly** on all pixels above and to the left:

Problem: Very slow during both training and testing; $N \times N$ image requires $2N-1$ sequential steps

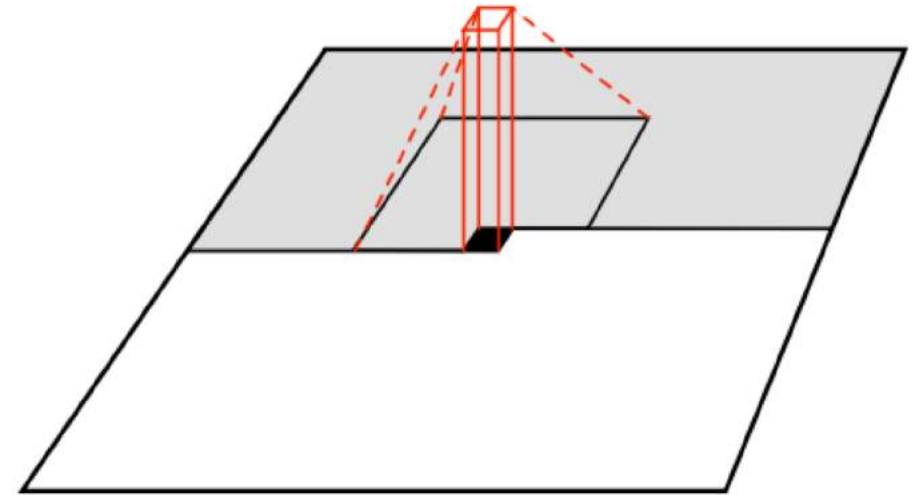


Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

PixelCNN

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region



Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

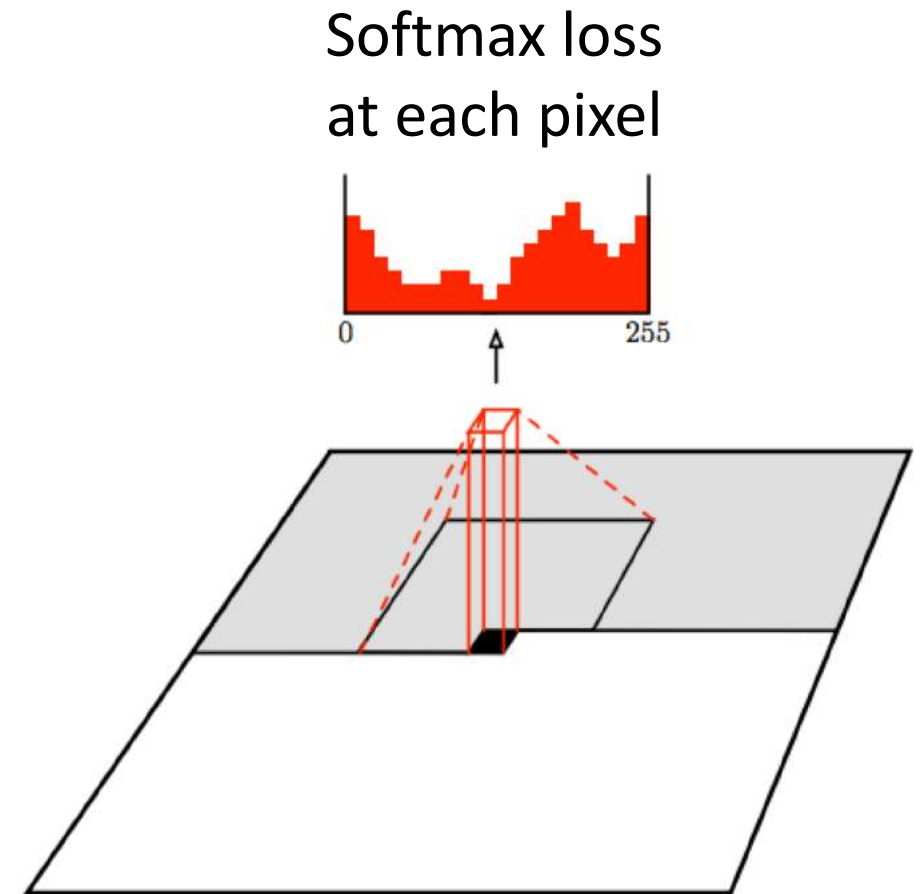
PixelCNN

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^n p(x_i | x_1, \dots, x_{i-1})$$



Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

PixelCNN

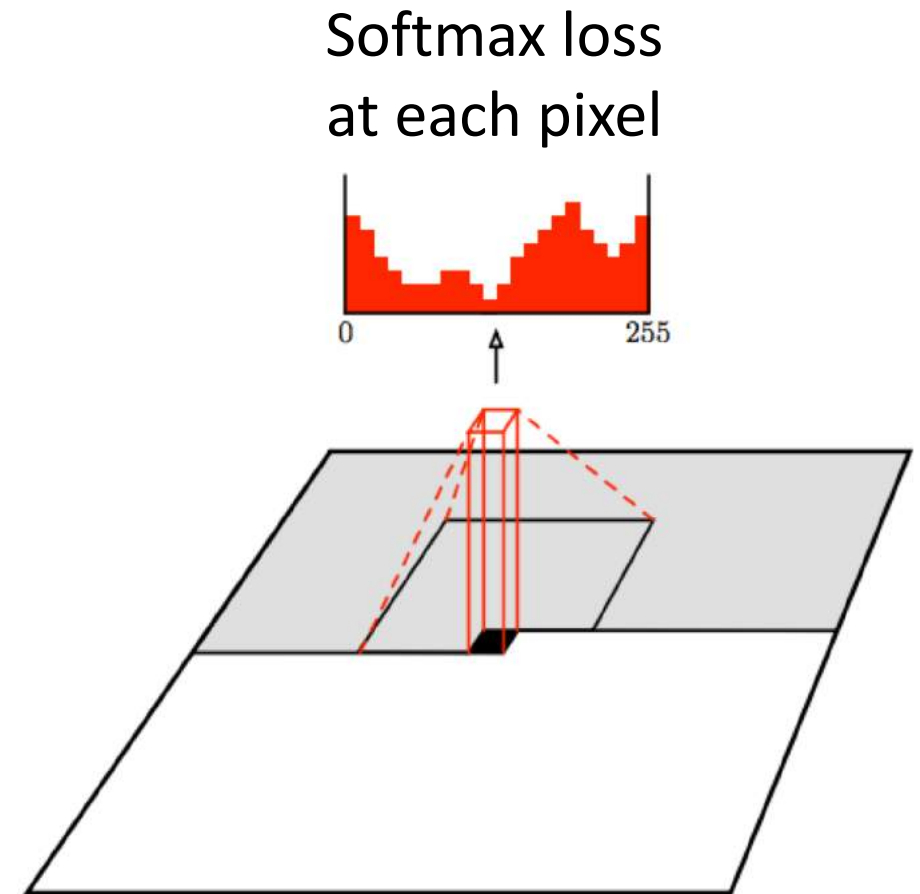
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Training: maximize likelihood of training images

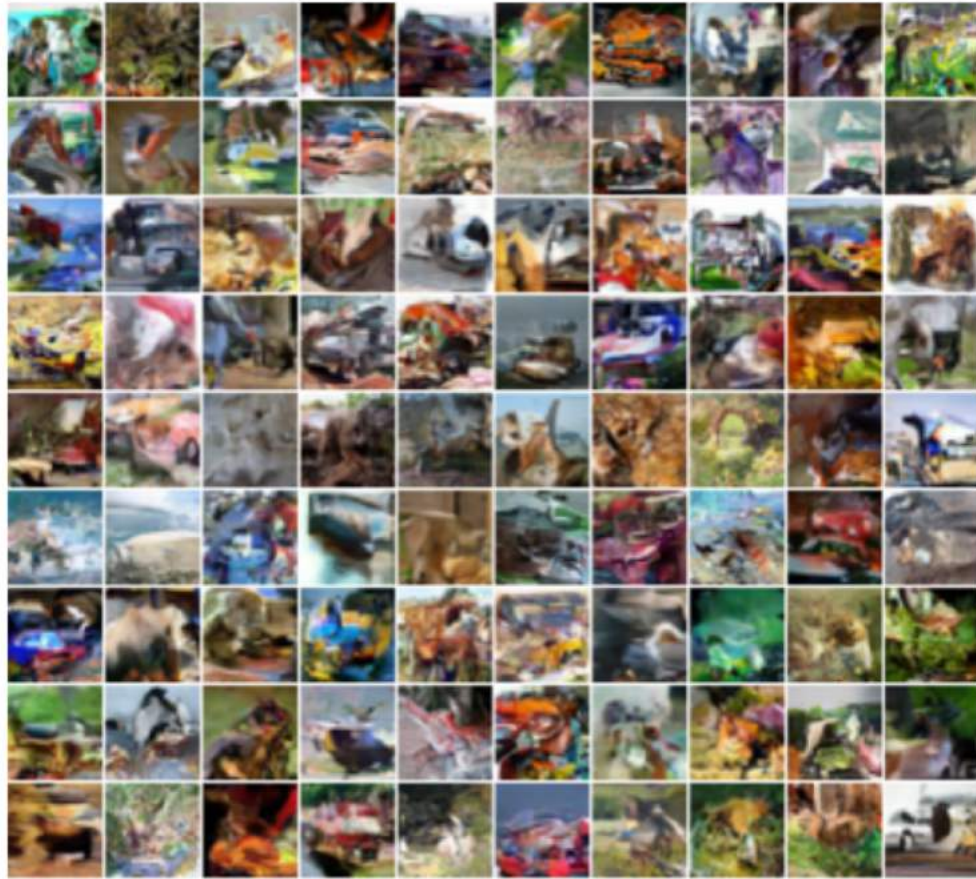
Training is faster than PixelRNN
(can parallelize convolutions since context region values known from training images)

Generation must still proceed sequentially
=> still slow

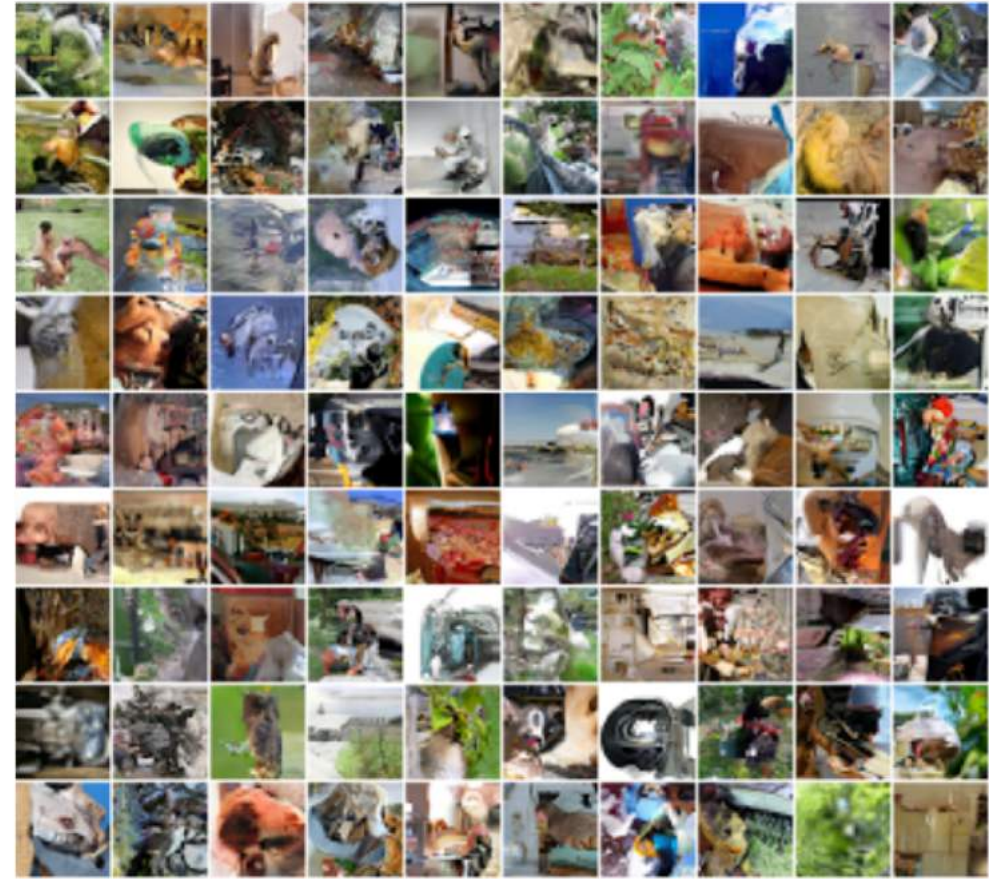


Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

PixelRNN: Generated Samples



32x32 CIFAR-10



32x32 ImageNet

Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

Autoregressive Models: PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood $p(x)$
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

- Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

Variational Autoencoders

Variational Autoencoders

PixelRNN / PixelCNN explicitly parameterizes density function with a neural network, so we can train to maximize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1}^n p_{\theta}(x_i | x_1, \dots, x_{i-1})$$

Variational Autoencoders (VAE) define an **intractable density** that we cannot explicitly compute or optimize

But we will be able to directly optimize a **lower bound** on the density

Variational Autoencoders

(Regular, non-variational) Autoencoders

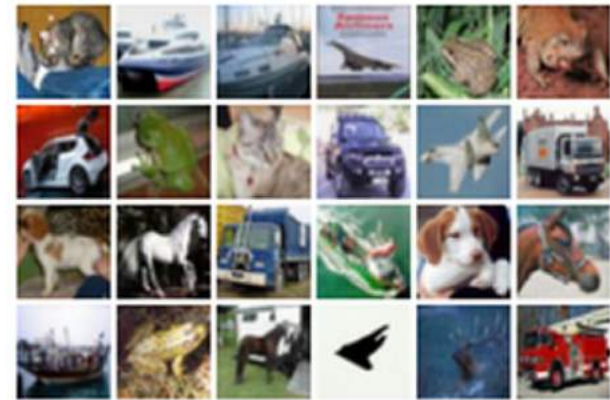
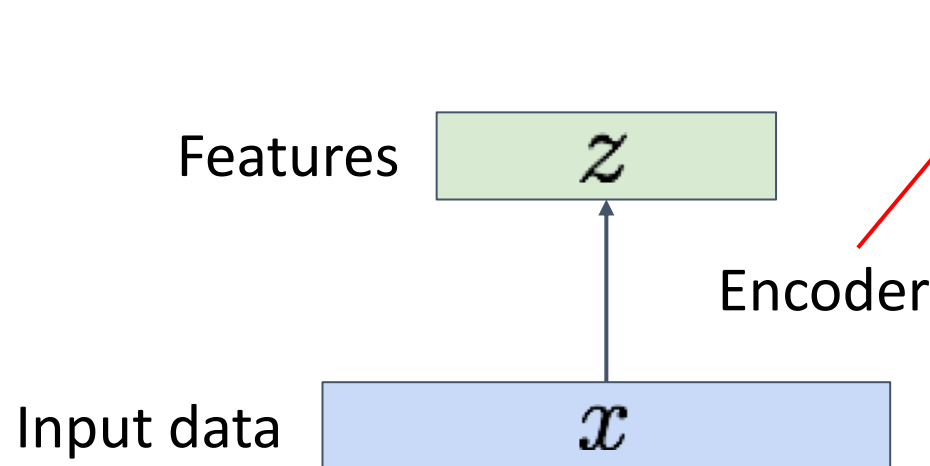
Unsupervised method for learning feature vectors from raw data x , without any labels

Features should extract useful information (maybe object identities, properties, scene type, etc) that we can use for downstream tasks

Originally: Linear + nonlinearity (sigmoid)

Later: Deep, fully-connected

Later: ReLU CNN



Input Data

(Regular, non-variational) Autoencoders

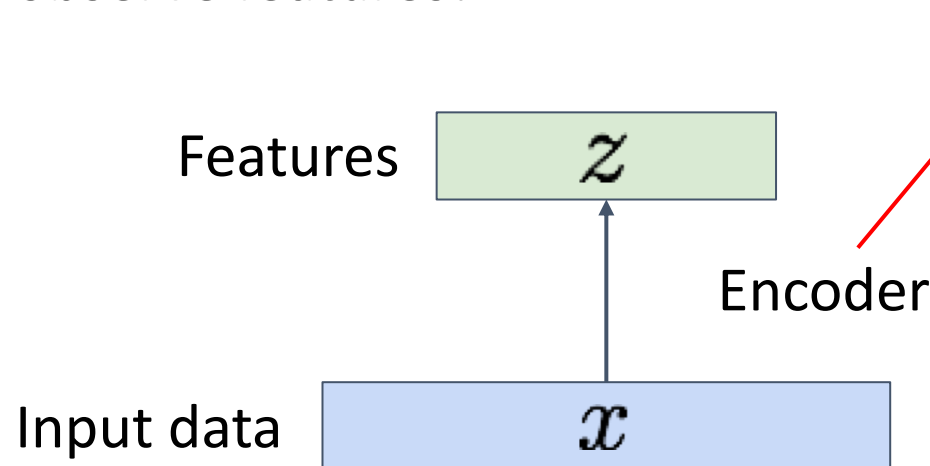
Problem: How can we learn this feature transform from raw data?

Features should extract useful information (maybe object identities, properties, scene type, etc) that we can use for downstream tasks
But we can't observe features!

Originally: Linear + nonlinearity (sigmoid)

Later: Deep, fully-connected

Later: ReLU CNN



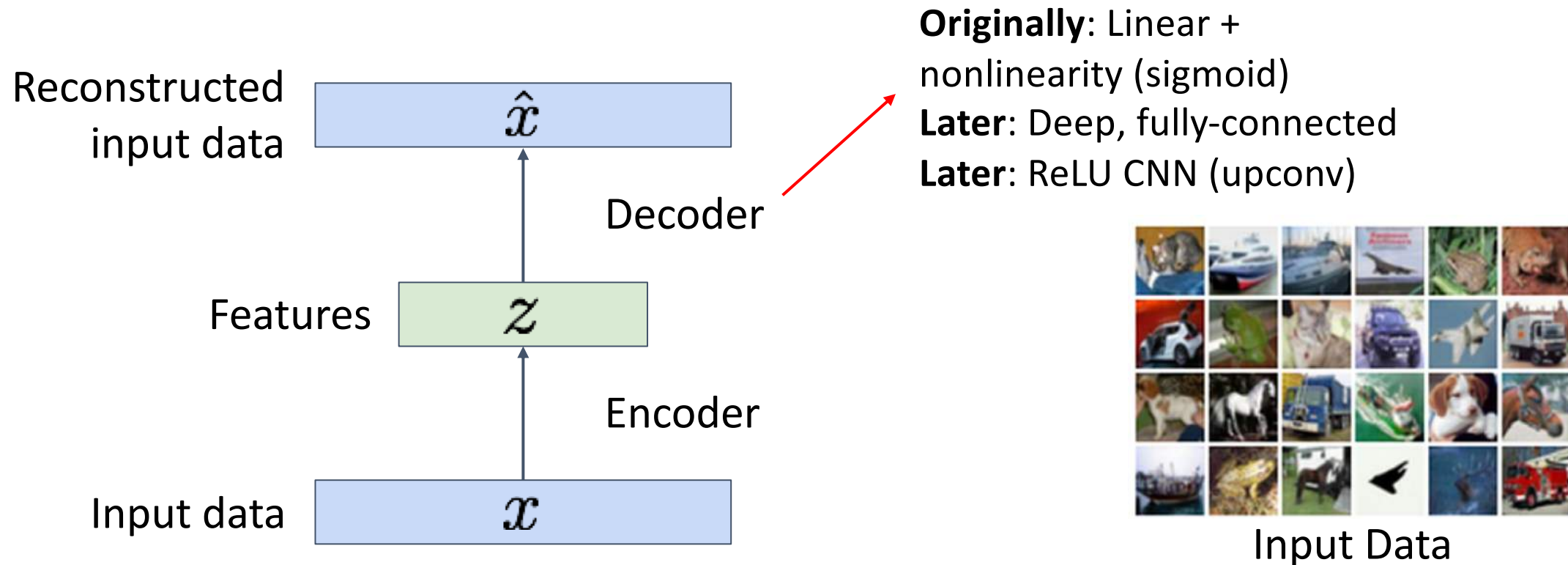
Input Data

(Regular, non-variational) Autoencoders

Problem: How can we learn this feature transform from raw data?

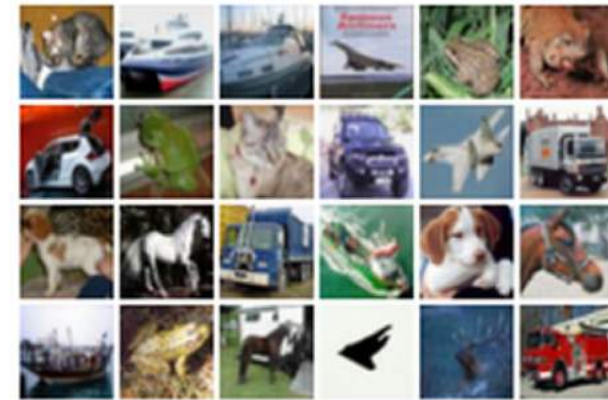
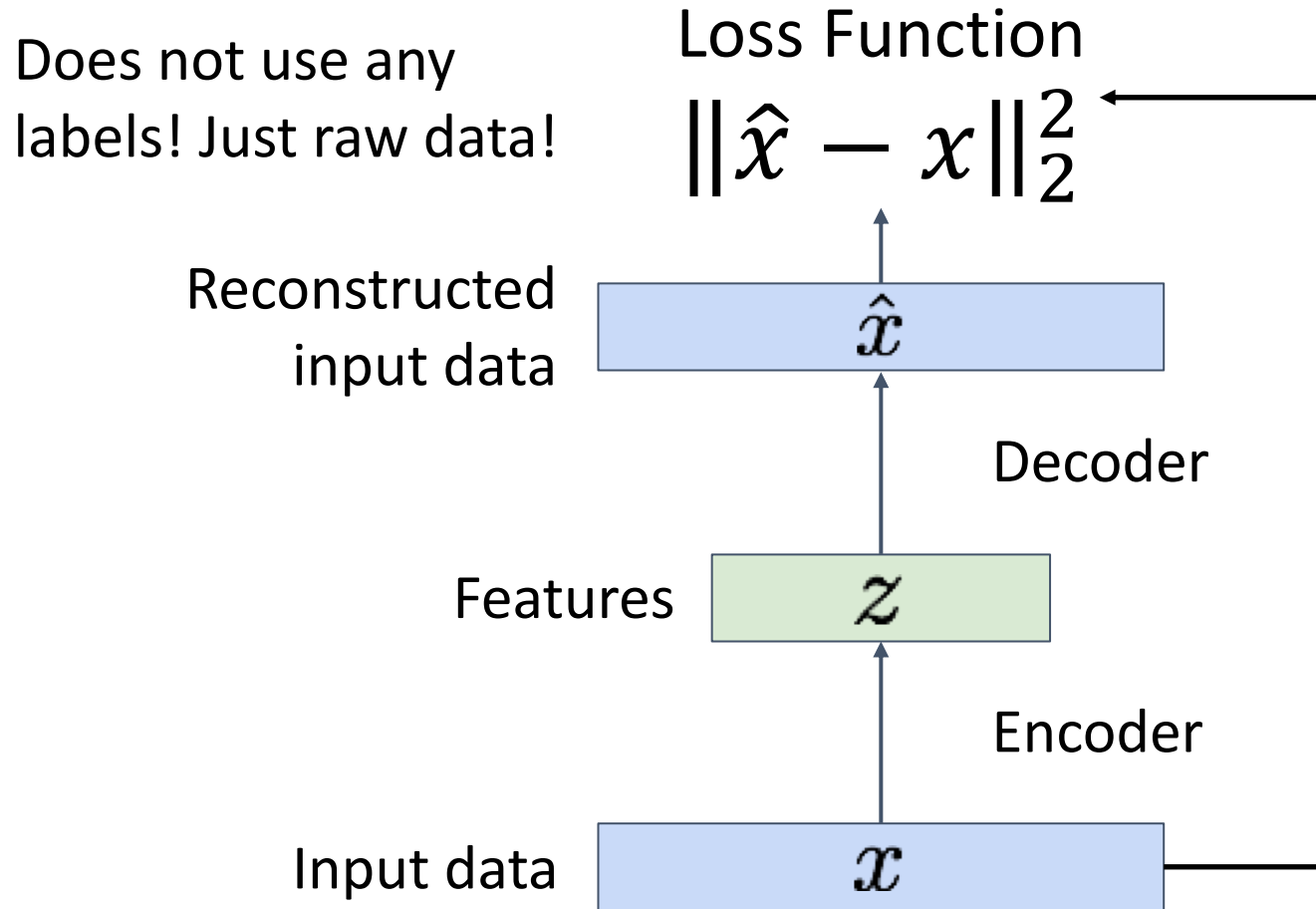
Idea: Use the features to reconstruct the input data with a **decoder**

“Autoencoding” = encoding itself



(Regular, non-variational) Autoencoders

Loss: L2 distance between input and reconstructed data.

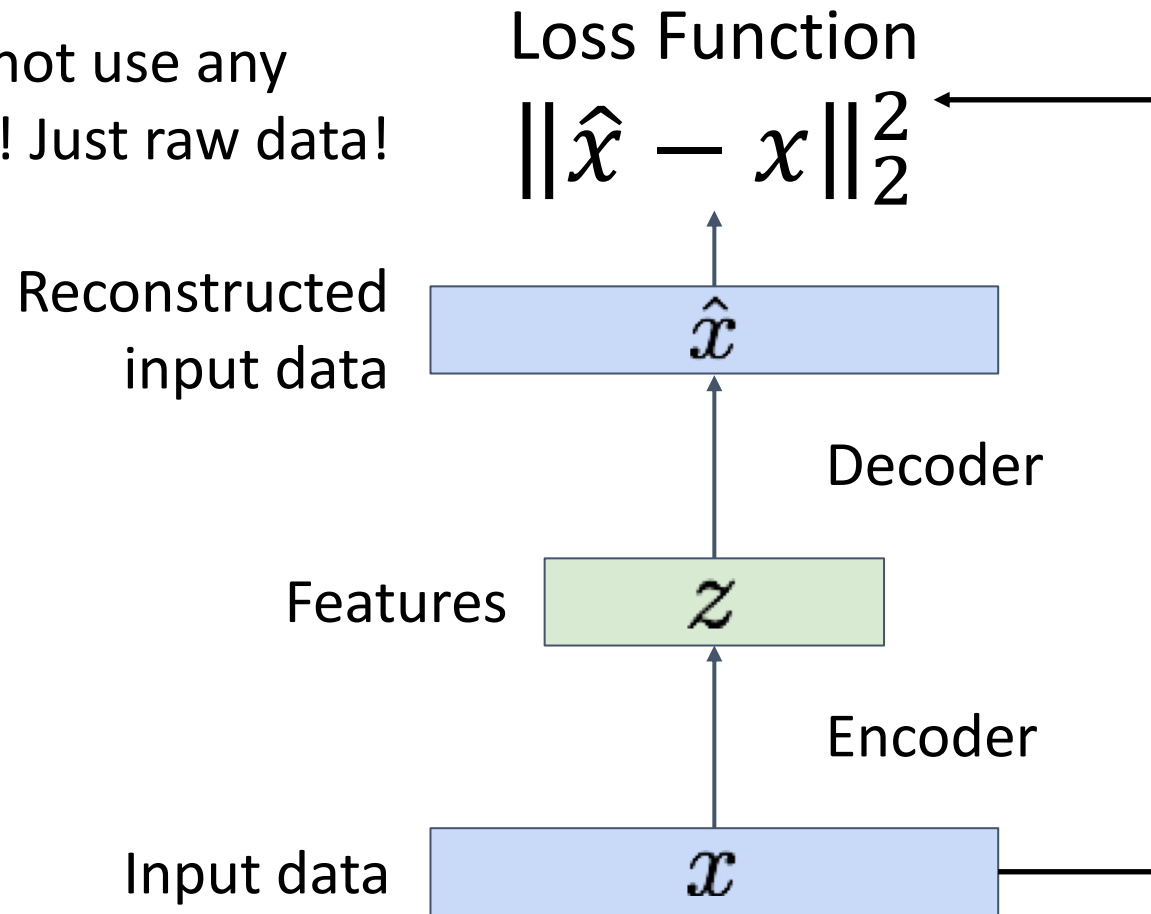


Input Data

(Regular, non-variational) Autoencoders

Loss: L2 distance between input and reconstructed data.

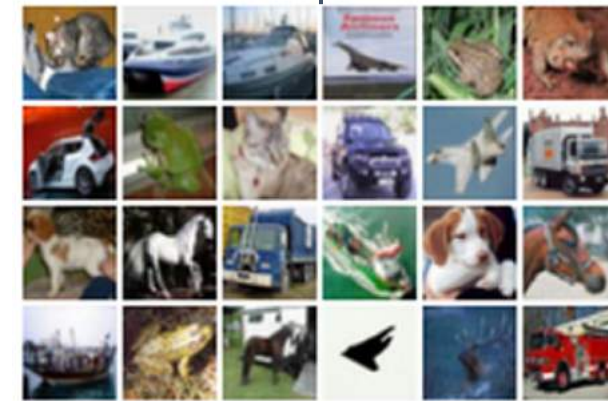
Does not use any
labels! Just raw data!



Reconstructed data



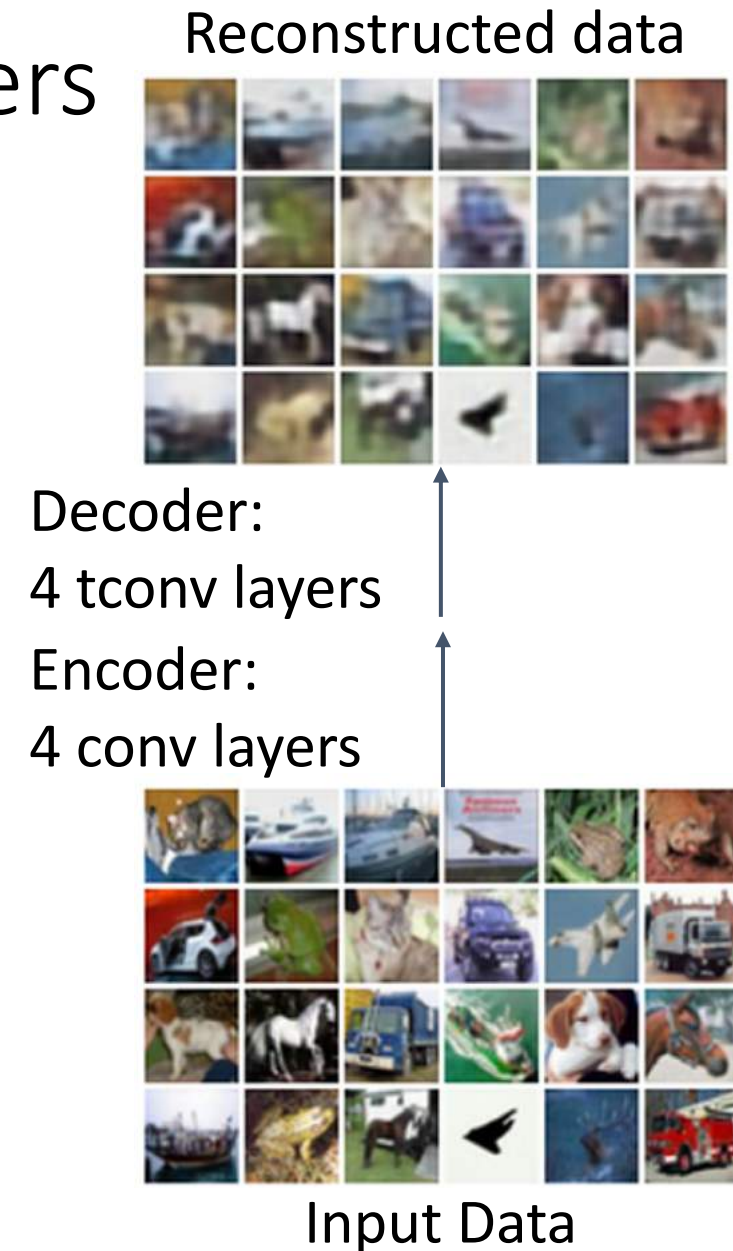
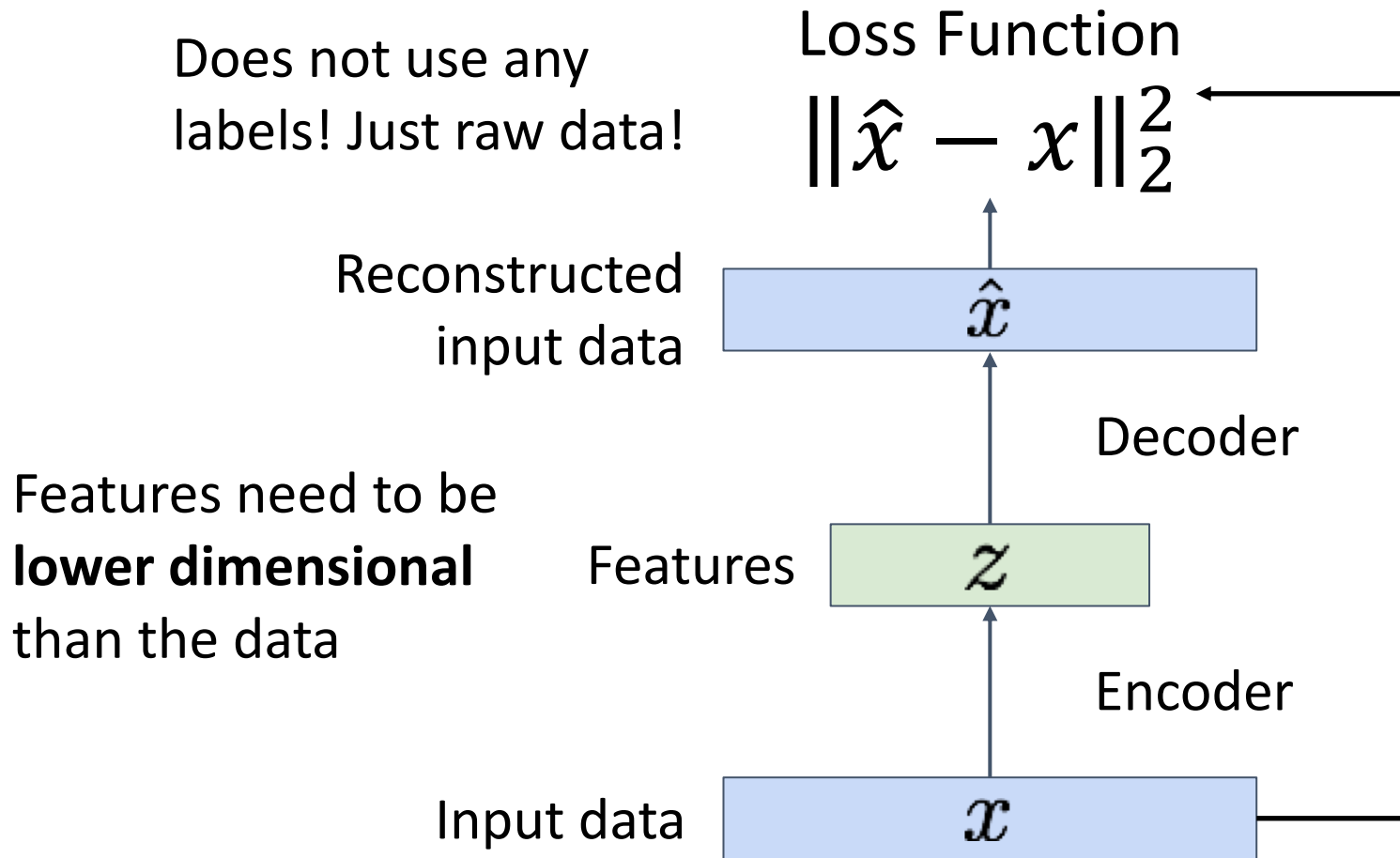
Decoder:
4 tconv layers
Encoder:
4 conv layers



Input Data

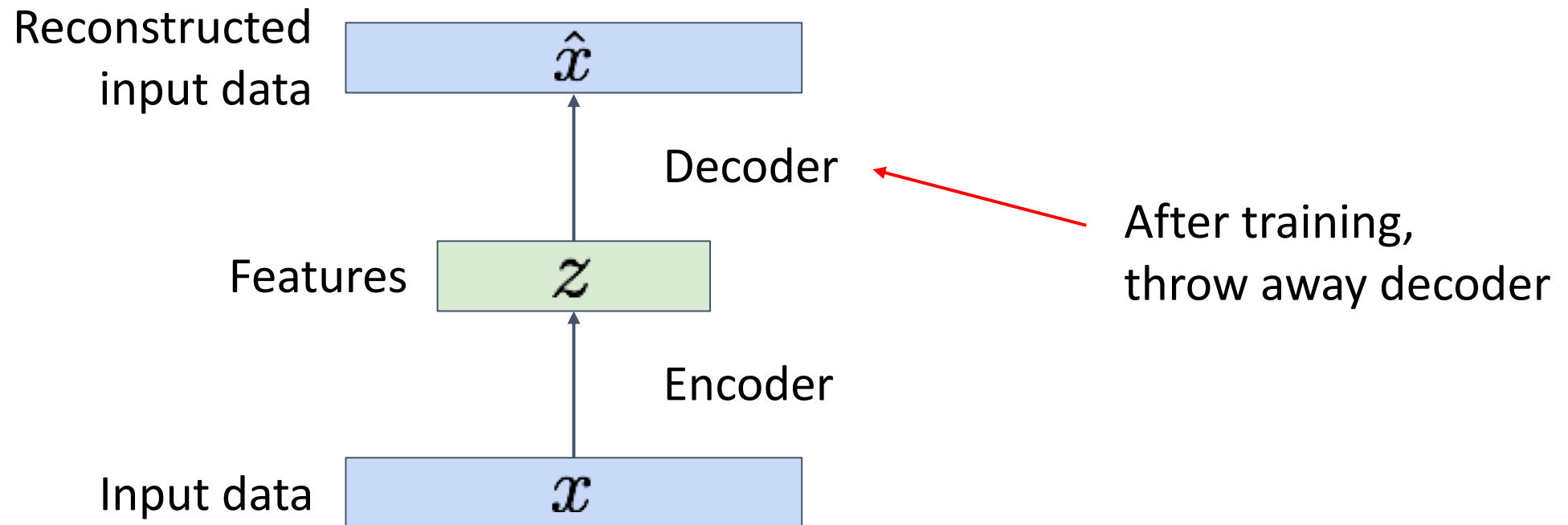
(Regular, non-variational) Autoencoders

Loss: L2 distance between input and reconstructed data.



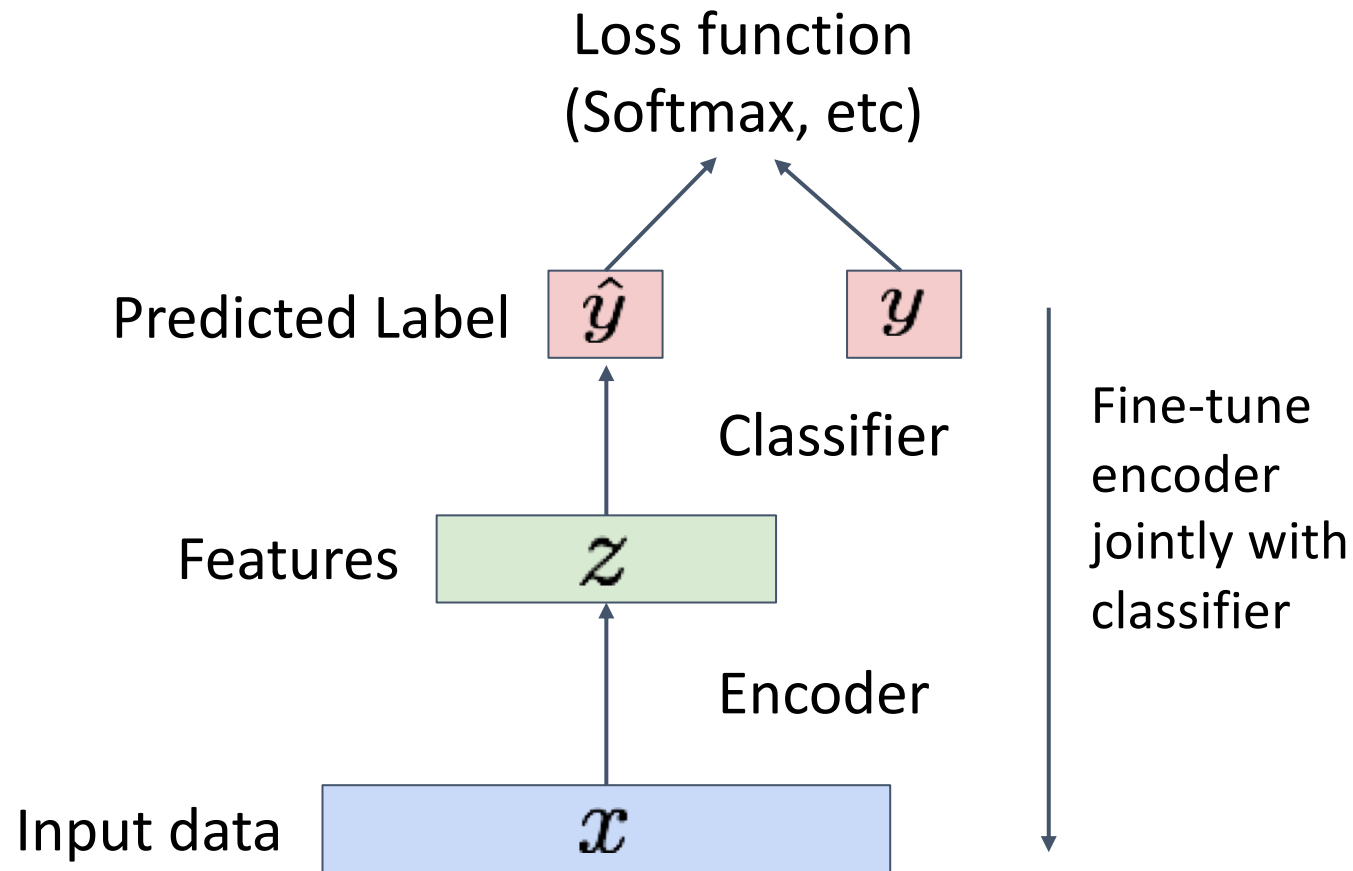
(Regular, non-variational) Autoencoders

After training, **throw away decoder** and use encoder for a downstream task



(Regular, non-variational) Autoencoders

After training, **throw away decoder** and use encoder for a downstream task



Encoder can be used to initialize a **supervised** model



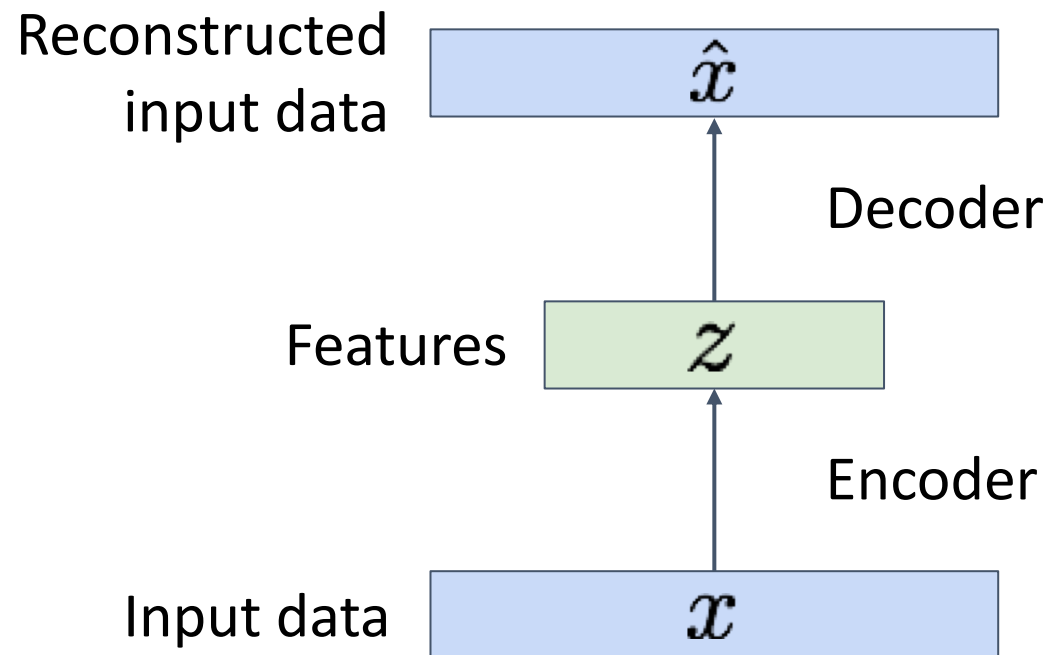
Train for final task
(sometimes with
small data)

(Regular, non-variational) Autoencoders

Autoencoders learn **latent features** for data without any labels!

Can use features to initialize a **supervised** model

Not probabilistic: No way to sample new data from learned model



Variational Autoencoders

Kingma and Welling, Auto-Encoding Variational Bayes, ICLR 2014

Variational Autoencoders

Probabilistic spin on autoencoders:

1. Learn latent features z from raw data
2. Sample from the model to generate new data

Variational Autoencoders

Probabilistic spin on autoencoders:

1. Learn latent features z from raw data
2. Sample from the model to generate new data

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from unobserved (latent) representation z

Intuition: x is an image, z is latent factors used to generate x : attributes, orientation, etc.

Variational Autoencoders

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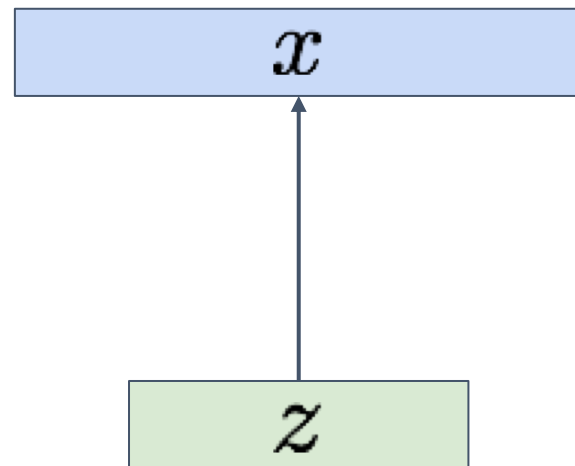
After training, sample new data like this:

Sample from
conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample z
from prior

$$p_{\theta^*}(z)$$



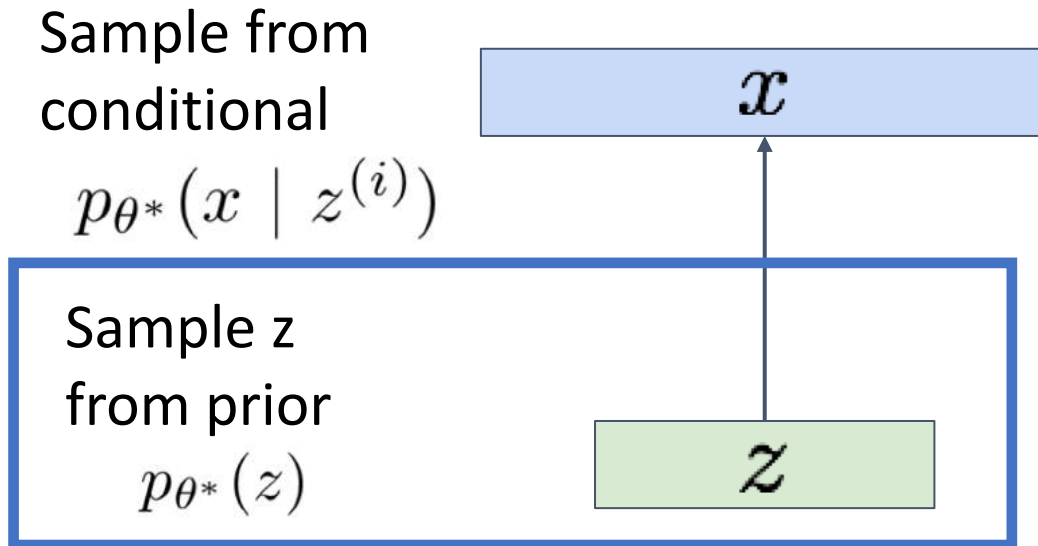
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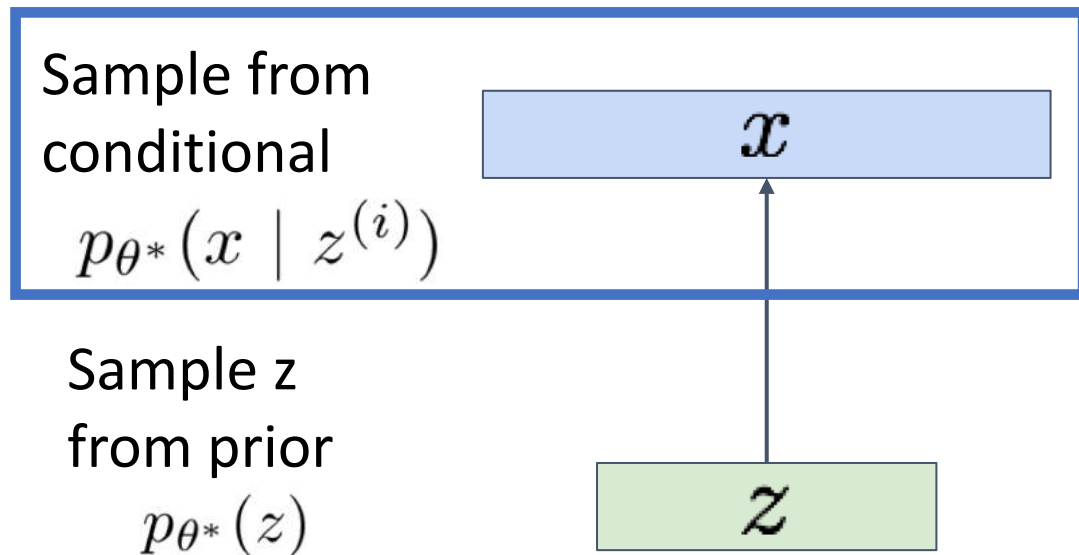
Assume simple prior $p(z)$, e.g. Gaussian

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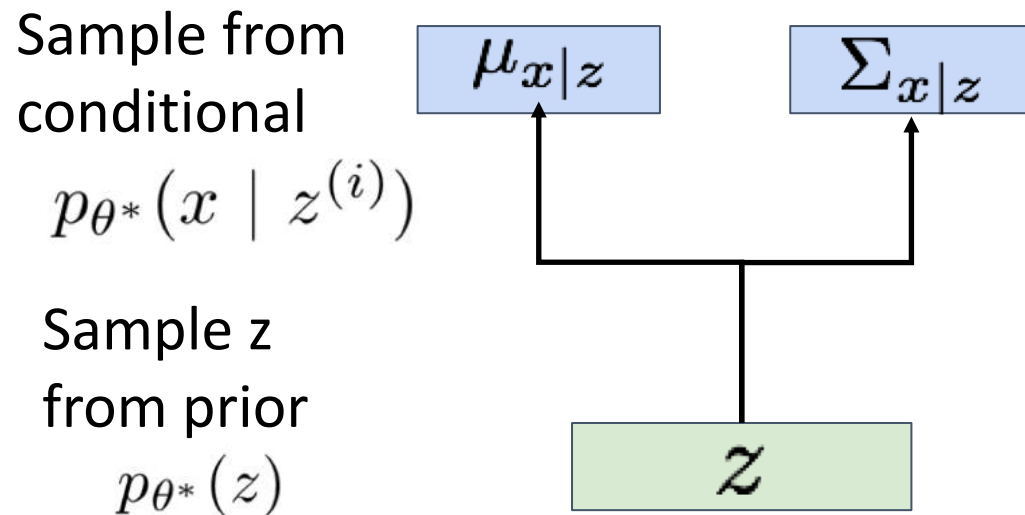
Represent $p(x|z)$ with a neural network (Similar to **decoder** from autencoder)

Variational Autoencoders

Decoder must be **probabilistic**:

Decoder inputs z , outputs mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$



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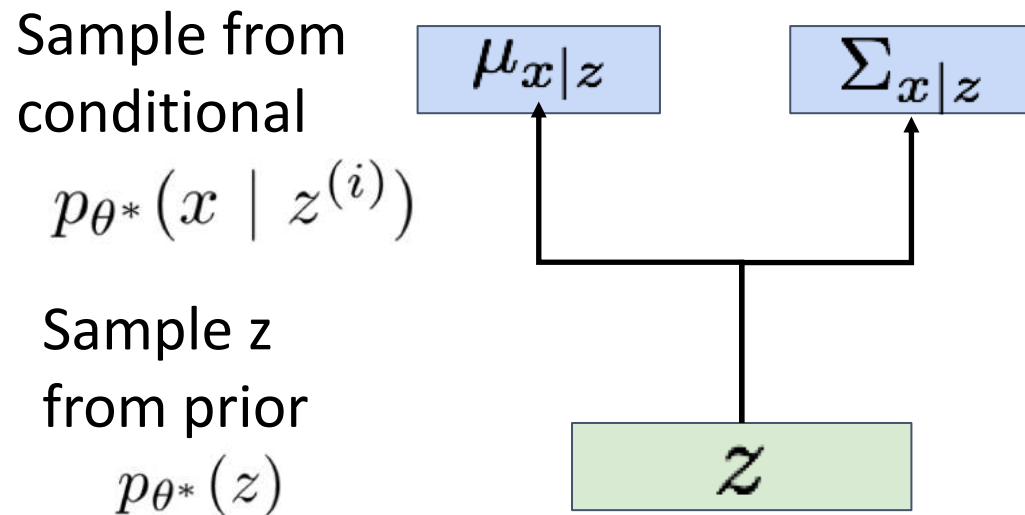
Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from unobserved (latent) representation z

How to train this model?

Basic idea: **maximize likelihood of data**

If we could observe the z for each x , then could train a *conditional generative model* $p(x|z)$



Variational Autoencoders

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Decoder inputs z , outputs mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

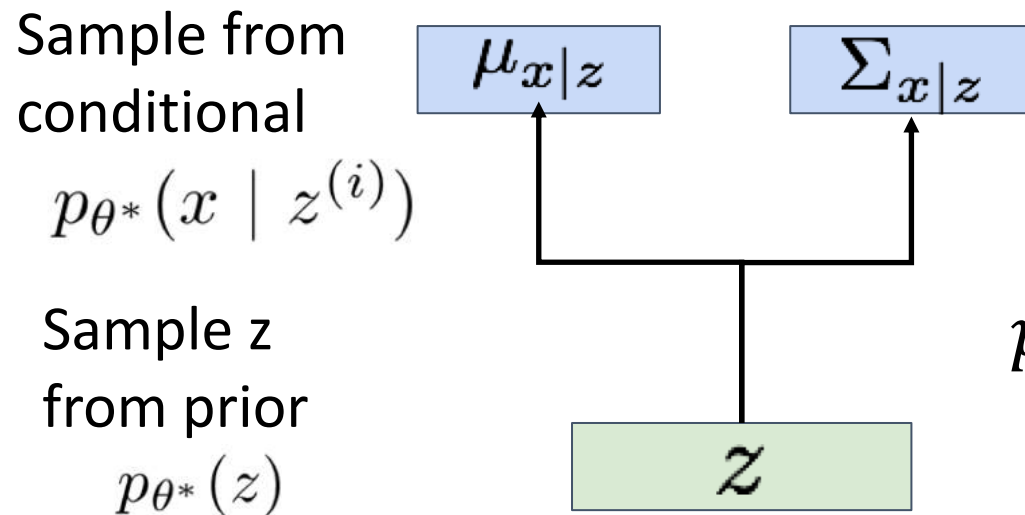
Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from unobserved (latent) representation z

How to train this model?

Basic idea: **maximize likelihood of data**

We don't observe z , so need to marginalize:

$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$$



Variational Autoencoders

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Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

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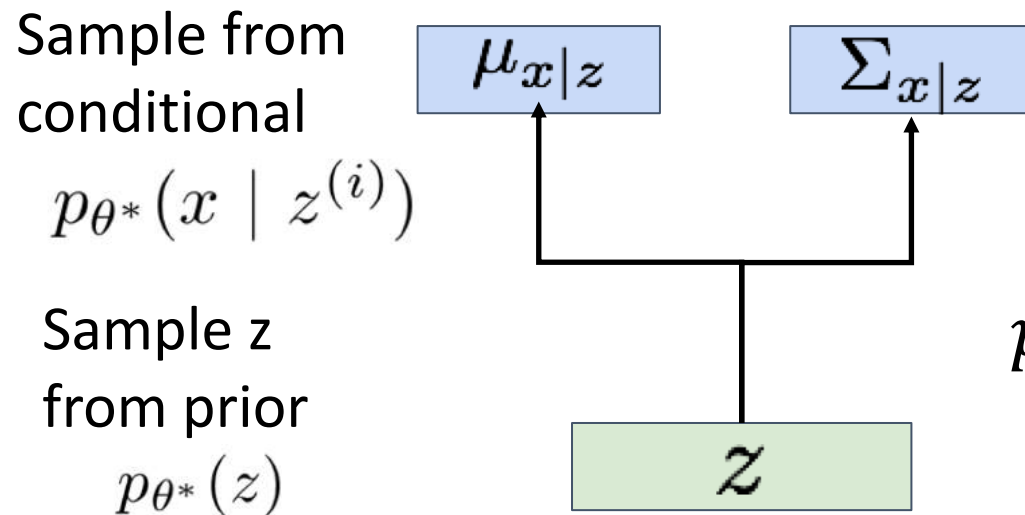
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$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int \boxed{p_{\theta}(x|z)} p_{\theta}(z) dz$$

Ok, can compute this with decoder network



Variational Autoencoders

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Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

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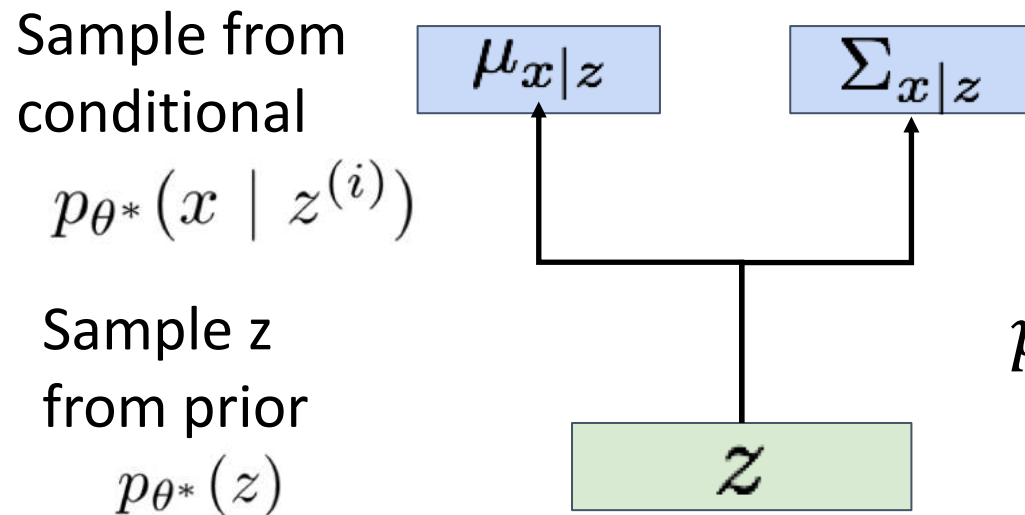
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Ok, we assumed Gaussian prior for z



Variational Autoencoders

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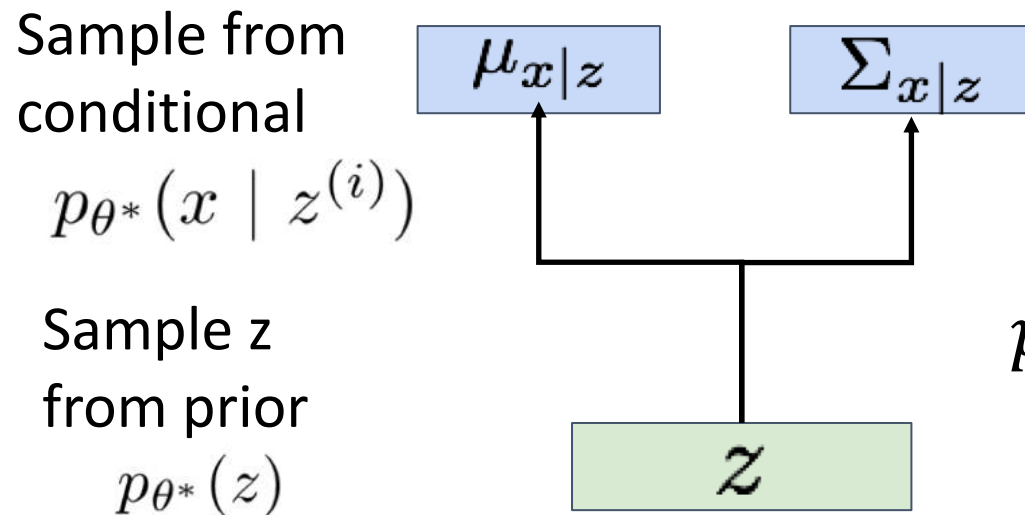
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Problem: Impossible to integrate over all z !



Variational Autoencoders

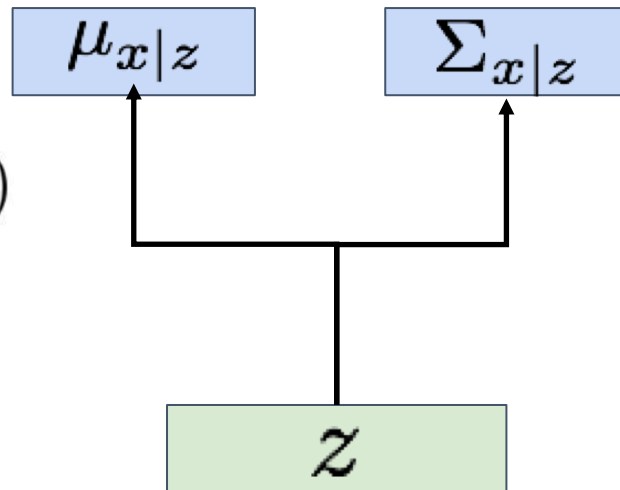
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Sample from conditional
 $p_{\theta^*}(x | z^{(i)})$

Sample z
from prior
 $p_{\theta^*}(z)$



Recall $p(x, z) = p(x | z)p(z) = p(z | x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from unobserved (latent) representation z

How to train this model?

Basic idea: **maximize likelihood of data**

Another idea: Try Bayes' Rule:

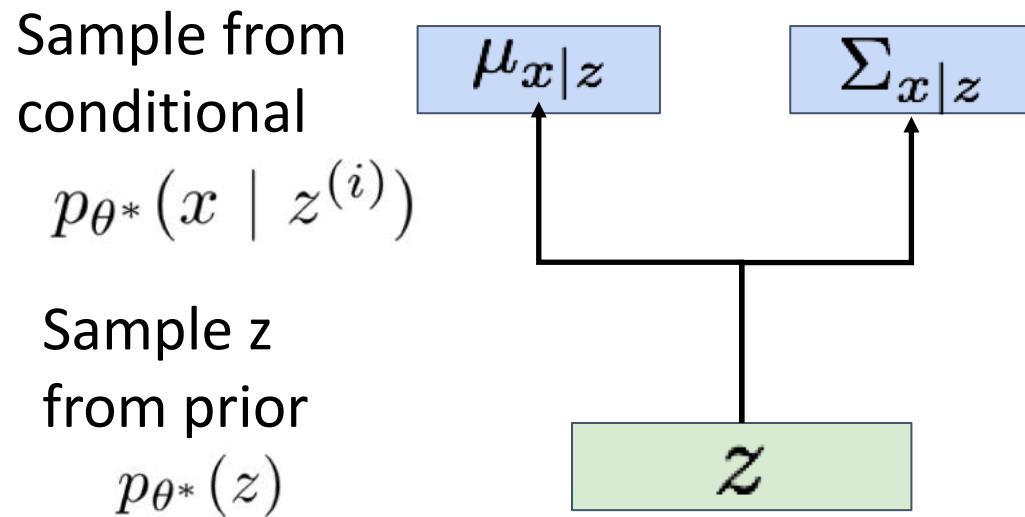
$$p_{\theta}(x) = \frac{p_{\theta}(x | z)p_{\theta}(z)}{p_{\theta}(z | x)}$$

Variational Autoencoders

Decoder must be **probabilistic**:

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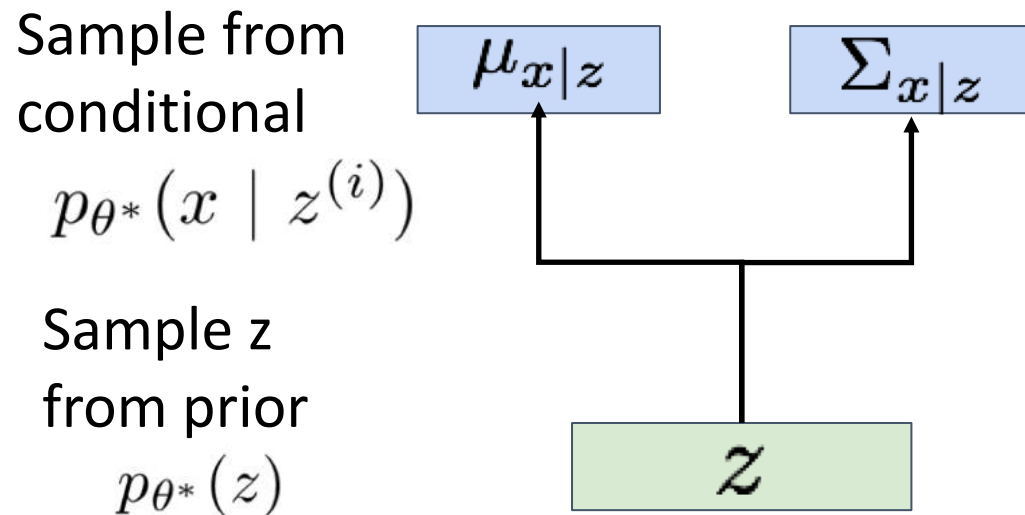
Ok, compute with decoder network

Variational Autoencoders

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Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$



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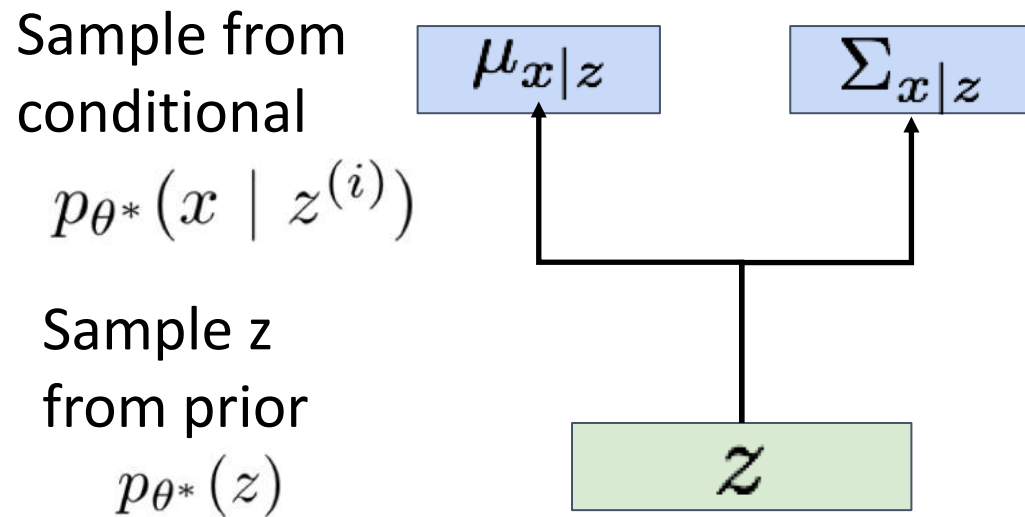
Ok, we assumed Gaussian prior

Variational Autoencoders

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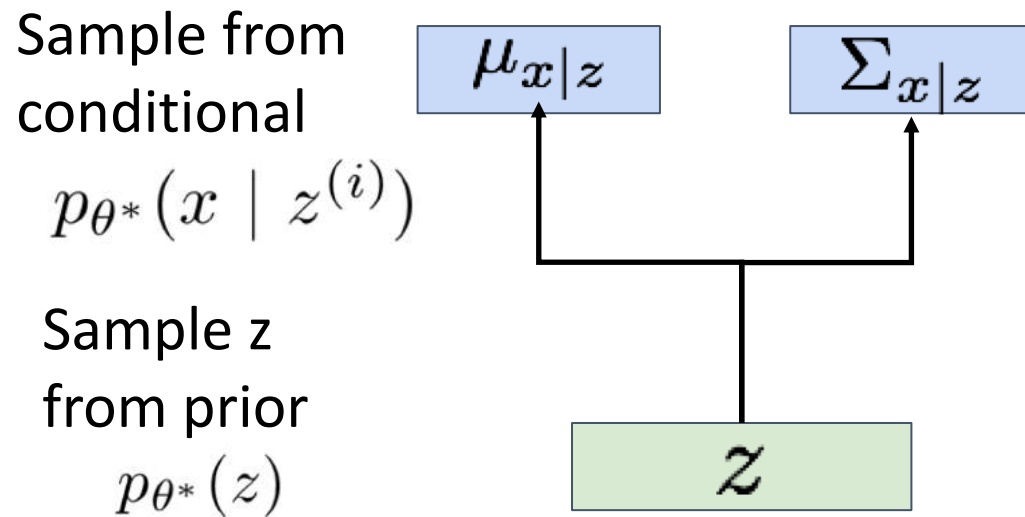
Problem: No way to compute this!

Variational Autoencoders

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Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$



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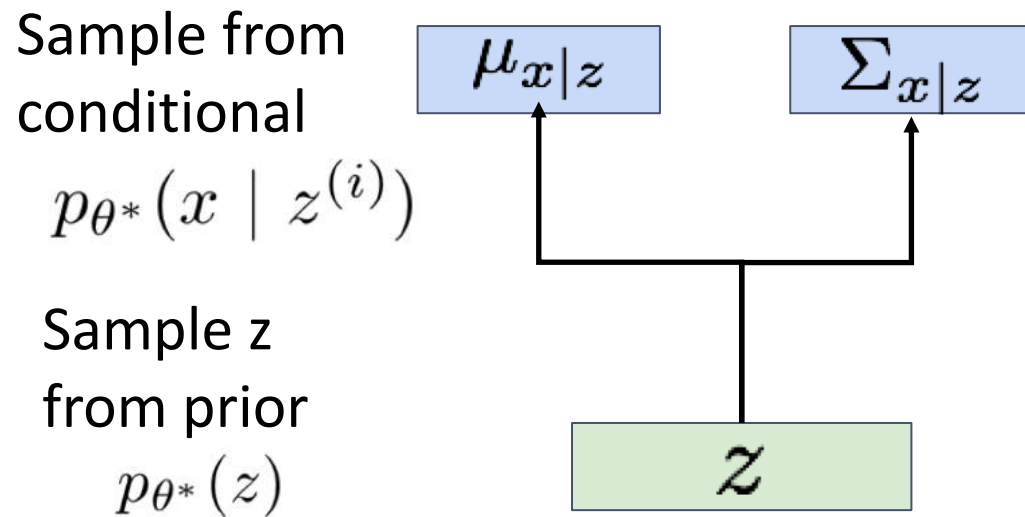
Solution: Train another network (**encoder**) that learns $q_{\phi}(z | x) \approx p_{\theta}(z | x)$

Variational Autoencoders

Decoder must be **probabilistic**:

Decoder inputs z , outputs mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\Sigma_{x|z}$



Recall $p(x, z) = p(x | z)p(z) = p(z | x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from unobserved (latent) representation z

How to train this model?

Basic idea: **maximize likelihood of data**

Another idea: Try Bayes' Rule:

$$p_{\theta}(x) = \frac{p_{\theta}(x | z)p_{\theta}(z)}{p_{\theta}(z | x)} \approx \frac{p_{\theta}(x | z)p_{\theta}(z)}{q_{\phi}(z | x)}$$

Use **encoder** to compute $q_{\phi}(z | x) \approx p_{\theta}(z | x)$

Variational Autoencoders

Decoder network inputs
latent code z , gives
distribution over data x

Encoder network inputs
data x , gives distribution
over latent codes z

If we can ensure that
 $q_\phi(z | x) \approx p_\theta(z | x)$,

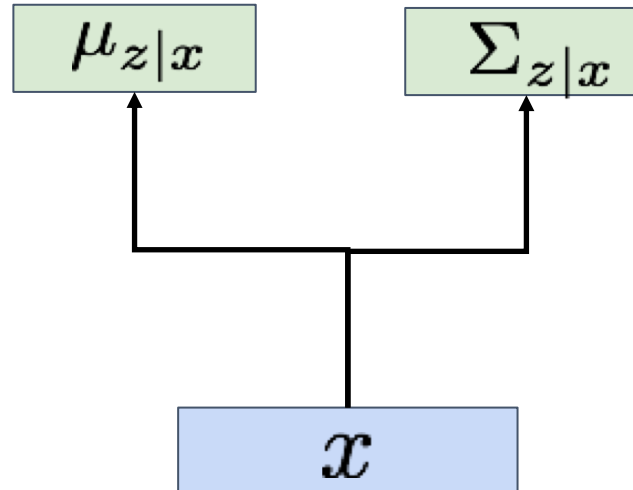
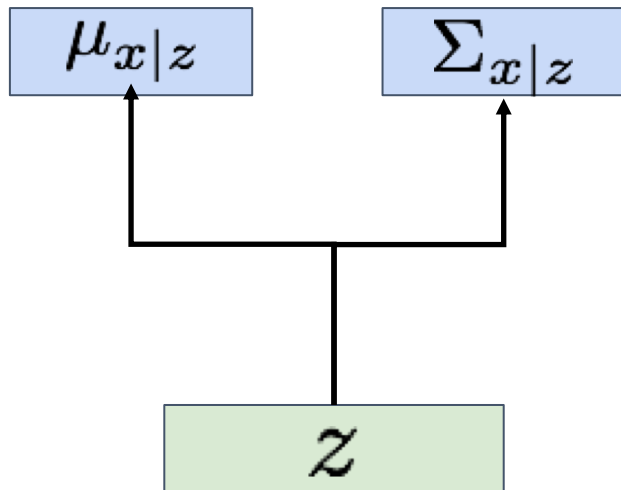
$$p_\theta(x | z) = N(\mu_{x|z}, \Sigma_{x|z})$$

$$q_\phi(z | x) = N(\mu_{z|x}, \Sigma_{z|x})$$

then we can approximate

$$p_\theta(x) \approx \frac{p_\theta(x | z)p(z)}{q_\phi(z | x)}$$

Idea: Jointly train both
encoder and decoder



Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x | z)p(z)}{p_{\theta}(z | x)}$$

Bayes' Rule

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x | z)p(z)}{p_{\theta}(z | x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

Multiply top and bottom by $q_{\phi}(z|x)$

Variational Autoencoders

$$\begin{aligned}\log p_{\theta}(x) &= \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)} \\ &= \log p_{\theta}(x|z) - \log \frac{q_{\phi}(z|x)}{p(z)} + \log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)}\end{aligned}$$

Split up using rules for logarithms

Variational Autoencoders

$$\begin{aligned}\log p_{\theta}(x) &= \log \frac{p_{\theta}(x | z)p(z)}{p_{\theta}(z | x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)} \\ &= \log p_{\theta}(x|z) - \log \frac{q_{\phi}(z|x)}{p(z)} + \log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)}\end{aligned}$$

Split up using rules for logarithms

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

$$= \log p_{\theta}(x|z) - \log \frac{q_{\phi}(z|x)}{p(z)} + \log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)}$$

$$\log p_{\theta}(x) = E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x)]$$

We can wrap in an expectation since it doesn't depend on z

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

$$= E_z[\log p_{\theta}(x|z)] - E_z \left[\log \frac{q_{\phi}(z|x)}{p(z)} \right] + E_z \left[\log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)} \right]$$

$$\log p_{\theta}(x) = E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x)]$$

We can wrap in an expectation since it doesn't depend on z

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x | z)p(z)}{p_{\theta}(z | x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

$$= E_z[\log p_{\theta}(x|z)] - E_z \left[\log \frac{q_{\phi}(z|x)}{p(z)} \right] + E_z \left[\log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)} \right]$$

$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

Data reconstruction

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x | z)p(z)}{p_{\theta}(z | x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

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$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

KL divergence between prior, and
samples from the encoder network

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

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$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

KL divergence between encoder
and posterior of decoder

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

$$= E_z[\log p_{\theta}(x|z)] - E_z \left[\log \frac{q_{\phi}(z|x)}{p(z)} \right] + E_z \left[\log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)} \right]$$

$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

KL is ≥ 0 , so dropping this term gives a **lower bound** on the data likelihood:

Variational Autoencoders

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x|z)p(z)}{p_{\theta}(z|x)} = \log \frac{p_{\theta}(x|z)p(z)q_{\phi}(z|x)}{p_{\theta}(z|x)q_{\phi}(z|x)}$$

$$= E_z[\log p_{\theta}(x|z)] - E_z \left[\log \frac{q_{\phi}(z|x)}{p(z)} \right] + E_z \left[\log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)} \right]$$

$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

$$\log p_{\theta}(x) \geq E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

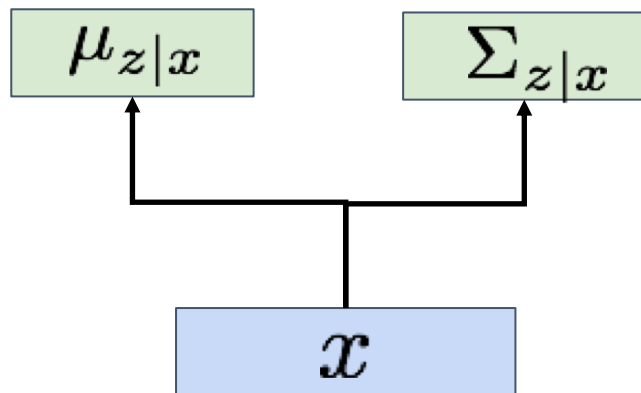
Variational Autoencoders

Jointly train **encoder** q and **decoder** p to maximize the **variational lower bound** on the data likelihood

$$\log p_{\theta}(x) \geq E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

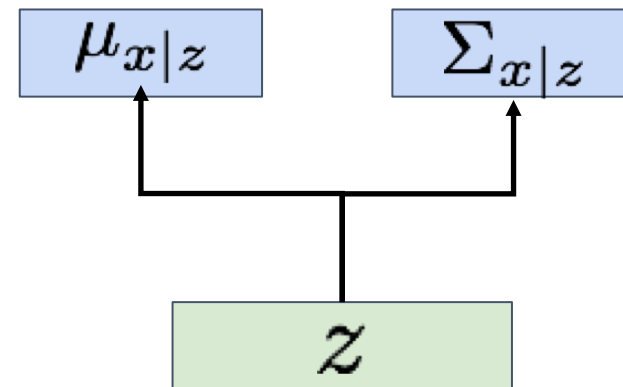
Encoder Network

$$q_{\phi}(z | x) = N(\mu_{z|x}, \Sigma_{z|x})$$



Decoder Network

$$p_{\theta}(x | z) = N(\mu_{x|z}, \Sigma_{x|z})$$



Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} (q_{\phi}(z|x), p(z))$$

Input
Data



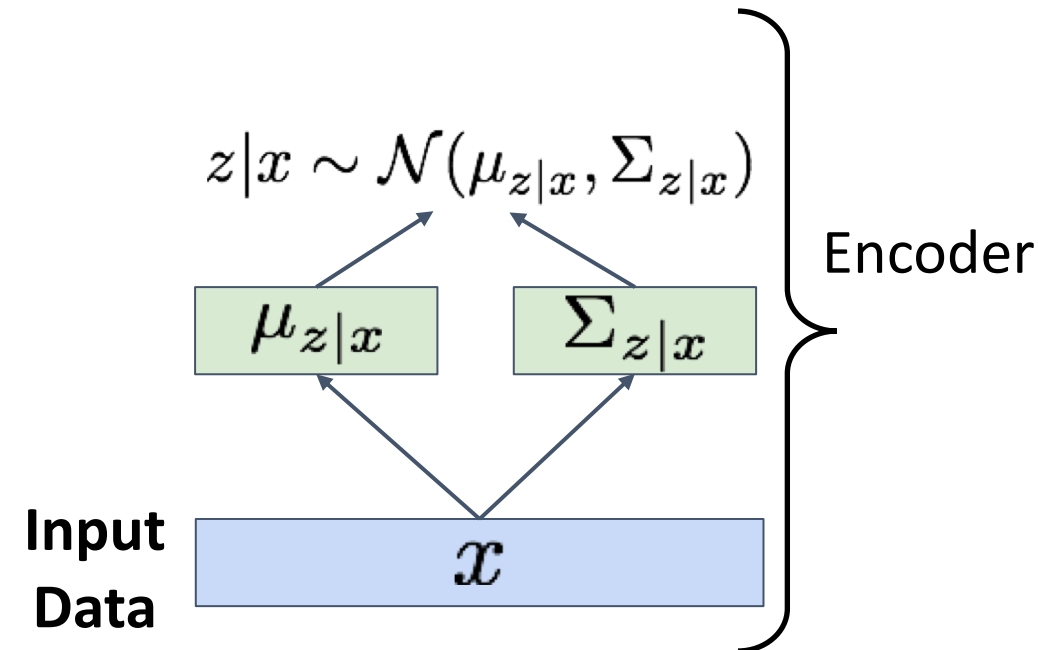
x

Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_\phi(z|x)} [\log p_\theta(x|z)] - D_{KL} (q_\phi(z|x), p(z))$$

1. Run input data through **encoder** to get a distribution over latent codes

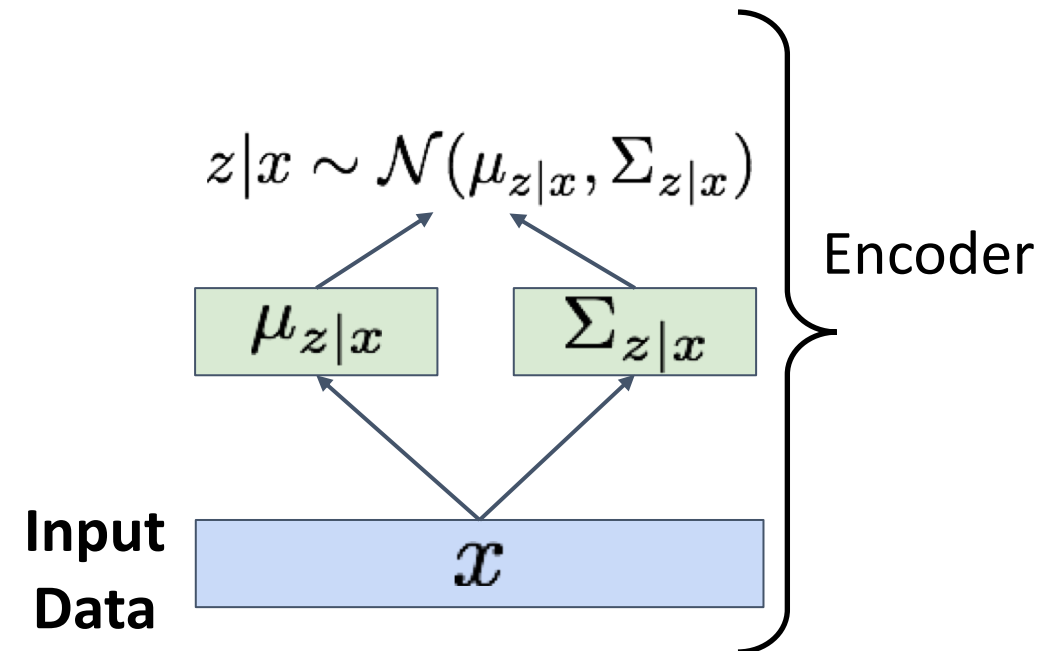


Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

1. Run input data through **encoder** to get a distribution over latent codes
2. **Encoder output should match the prior $p(z)$!**

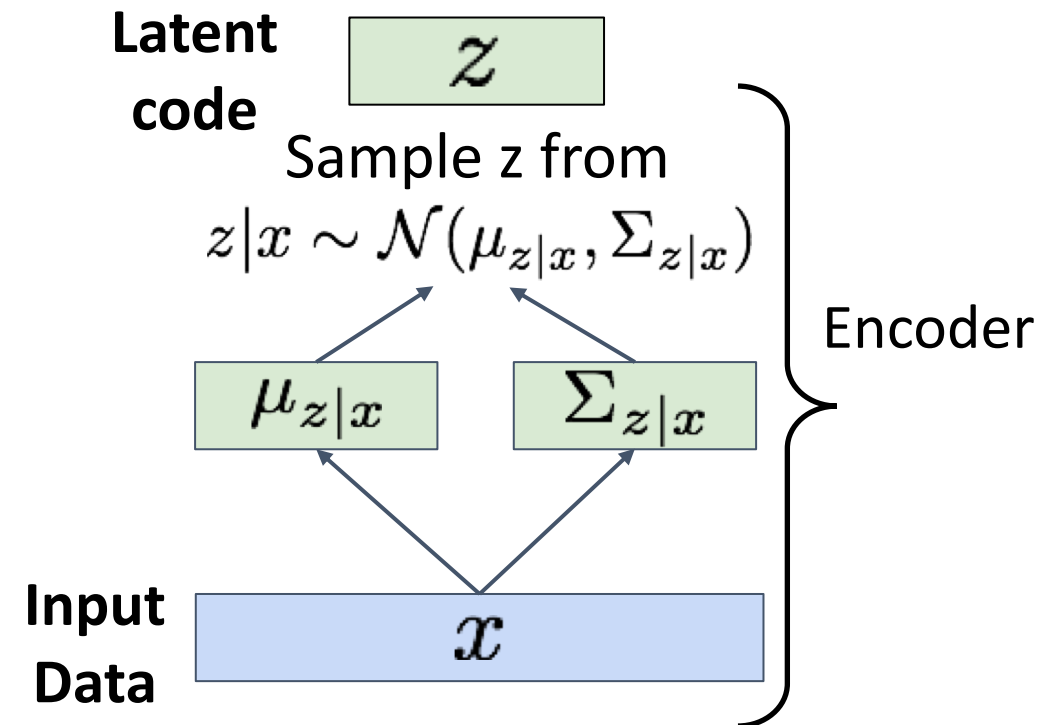


Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

1. Run input data through **encoder** to get a distribution over latent codes
2. **Encoder output should match the prior $p(z)$!**
3. Sample code z from encoder output

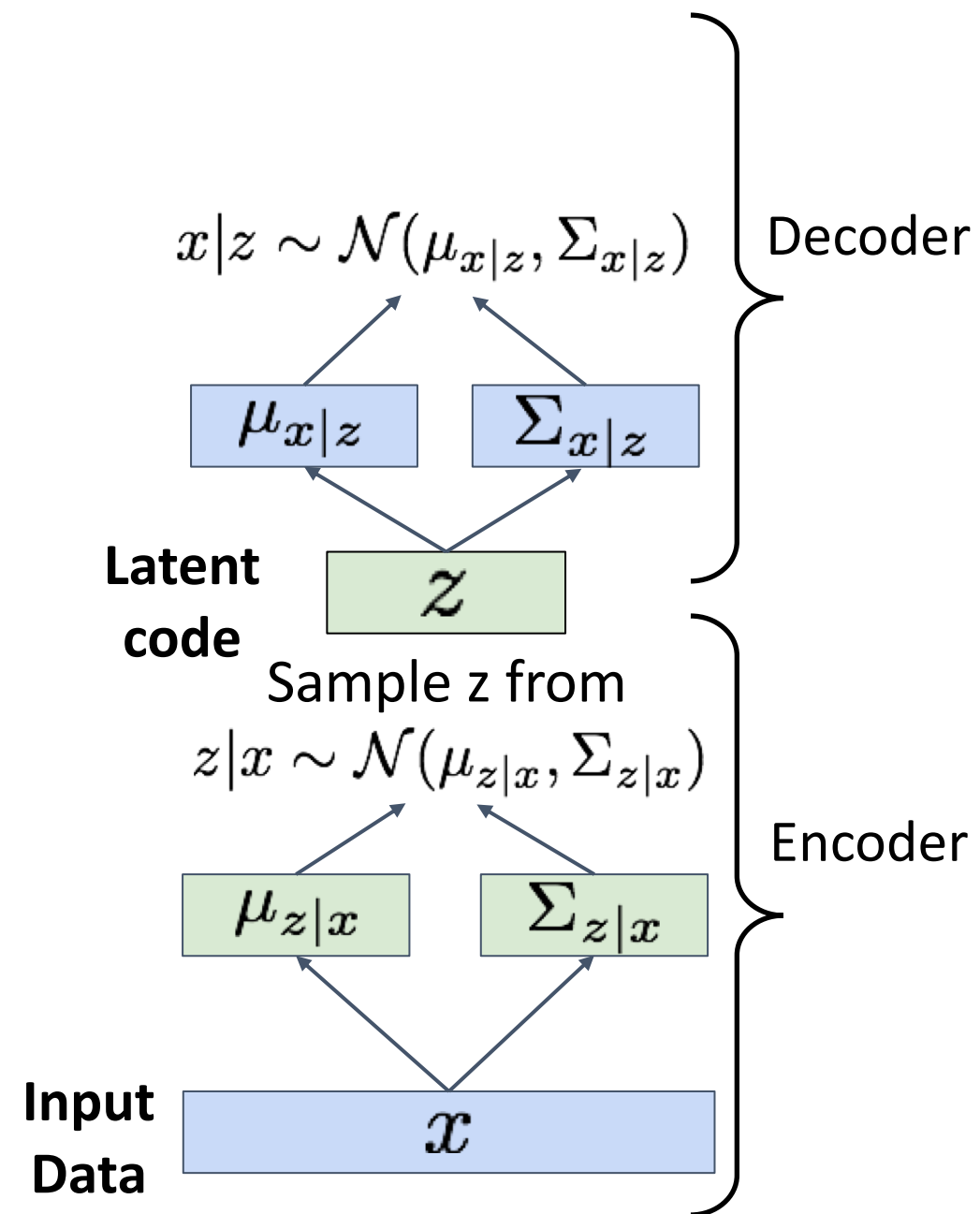


Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

1. Run input data through **encoder** to get a distribution over latent codes
2. **Encoder output should match the prior $p(z)$!**
3. Sample code z from encoder output
4. Run sampled code through **decoder** to get a distribution over data samples

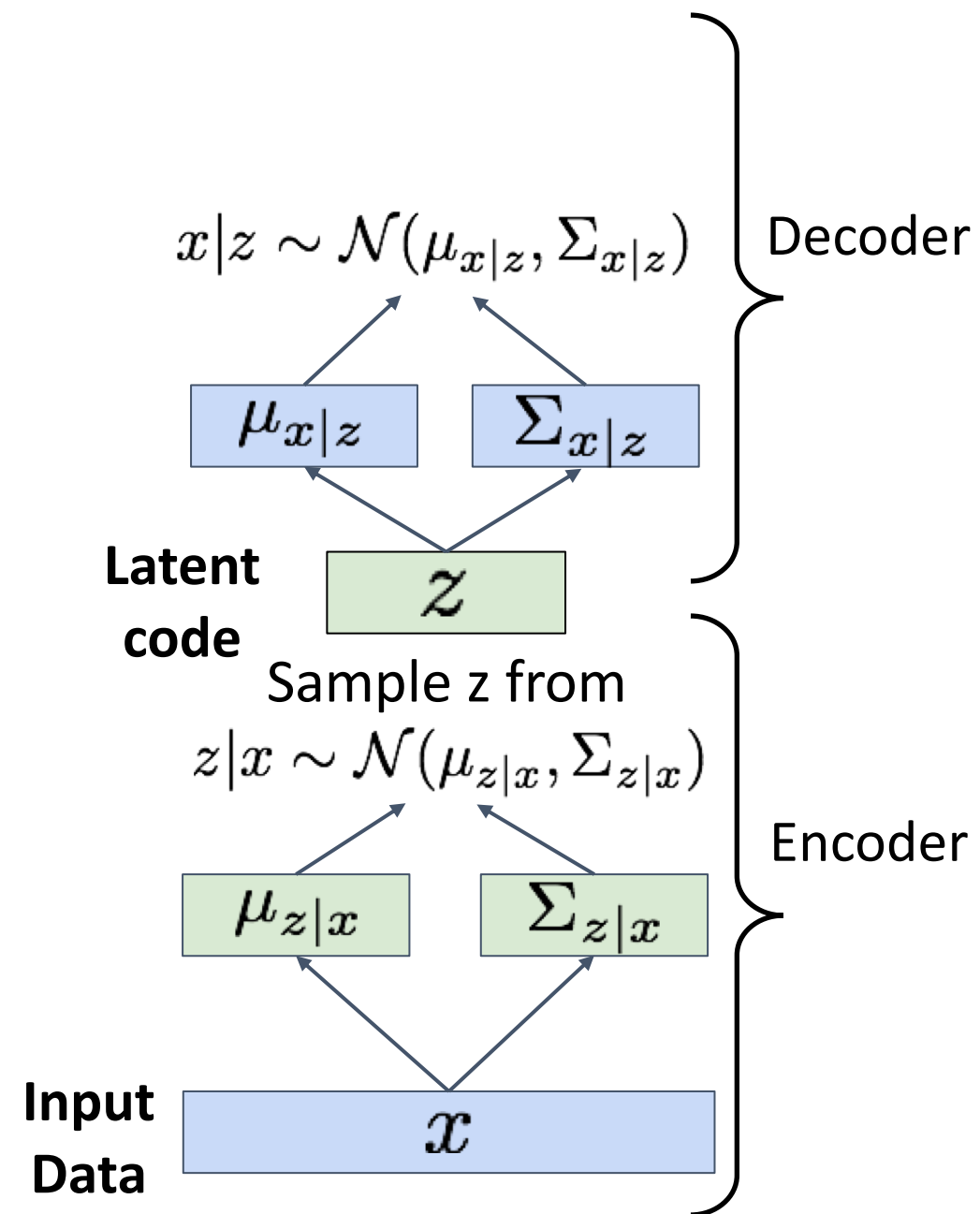


Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} (q_{\phi}(z|x), p(z))$$

1. Run input data through **encoder** to get a distribution over latent codes
2. **Encoder output should match the prior $p(z)$!**
3. Sample code z from encoder output
4. Run sampled code through **decoder** to get a distribution over data samples
5. **Original input data should be likely under the distribution output from (4)!**



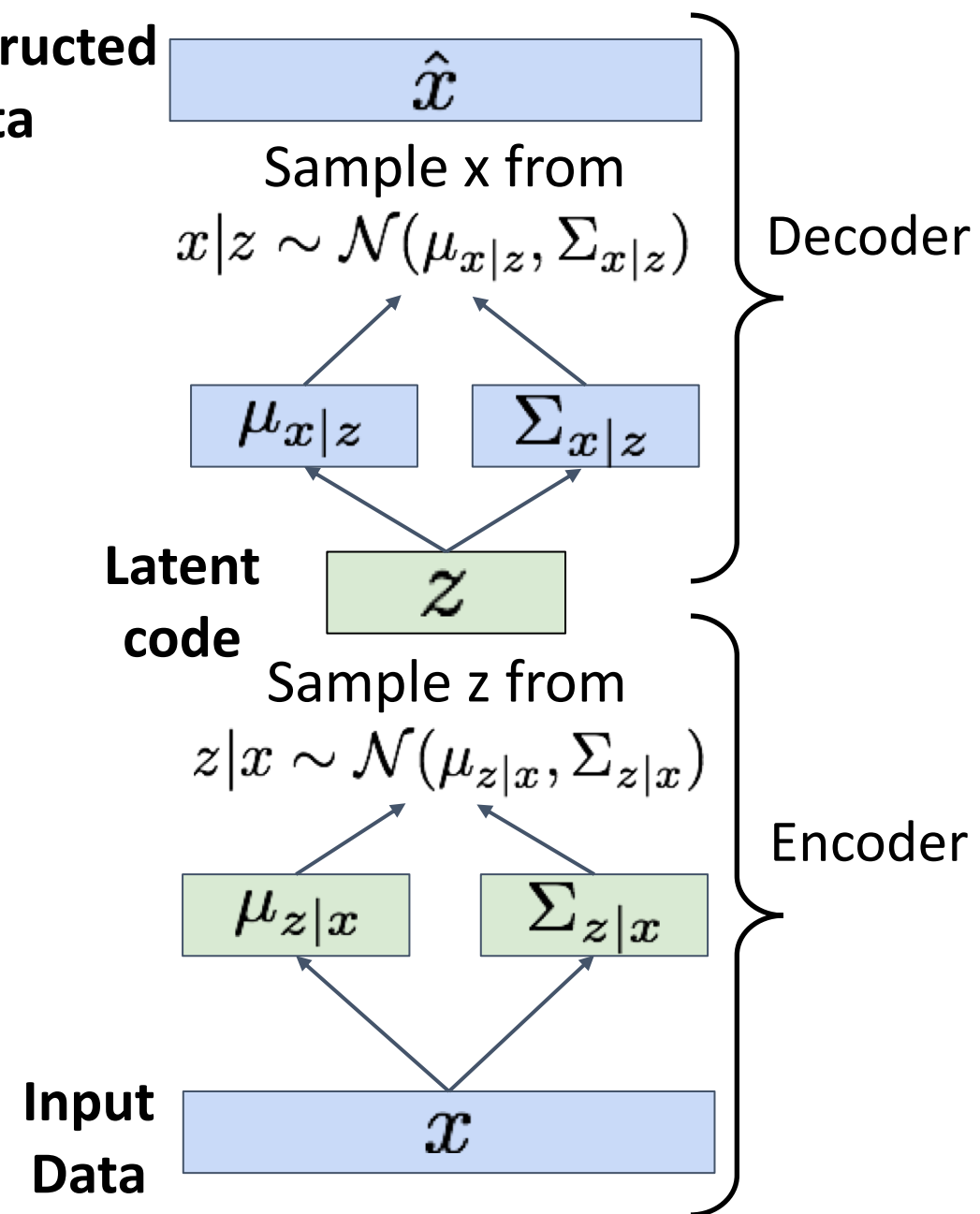
Variational Autoencoders

Train by maximizing the
variational lower bound

$$E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right)$$

1. Run input data through **encoder** to get a distribution over latent codes
2. **Encoder output should match the prior $p(z)$!**
3. Sample code z from encoder output
4. Run sampled code through **decoder** to get a distribution over data samples
5. **Original input data should be likely under the distribution output from (4)!**
6. Can sample a reconstruction from (4)

Reconstructed
data

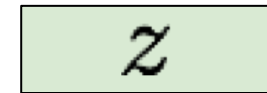


Variational Autoencoders: Generating Data

After training we can
generate new data!

1. Sample z from prior $p(z)$

**Latent
code**

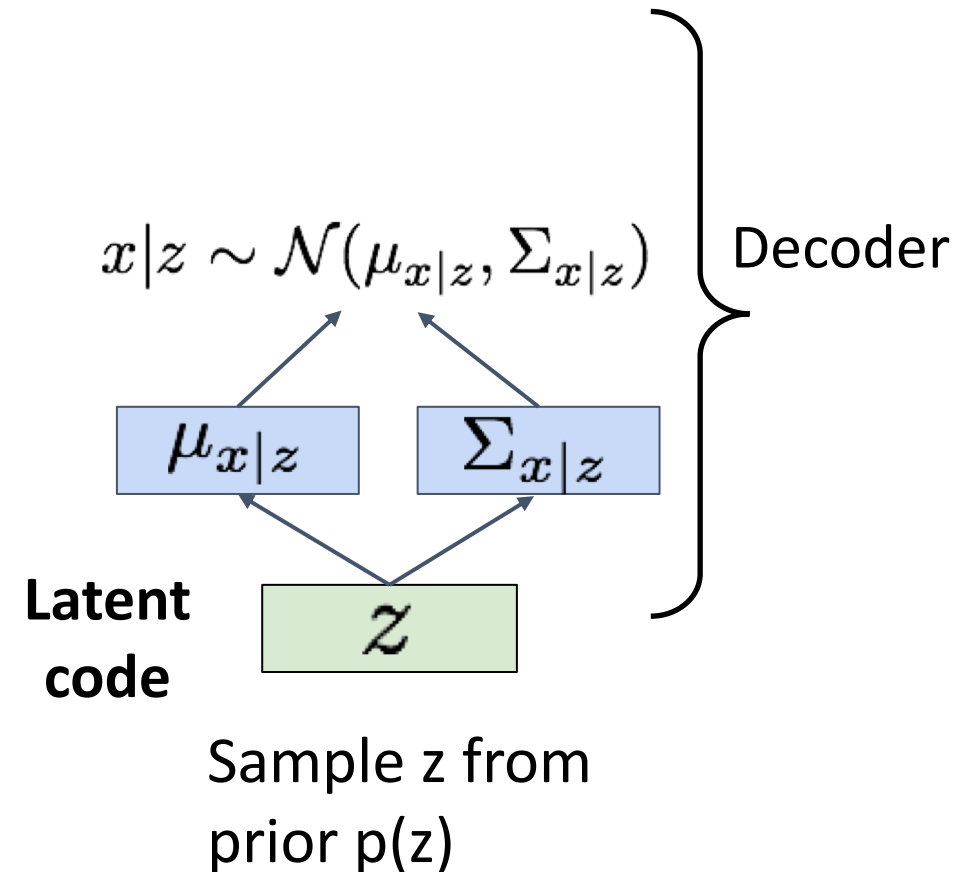


Sample z from
prior $p(z)$

Variational Autoencoders: Generating Data

After training we can
generate new data!

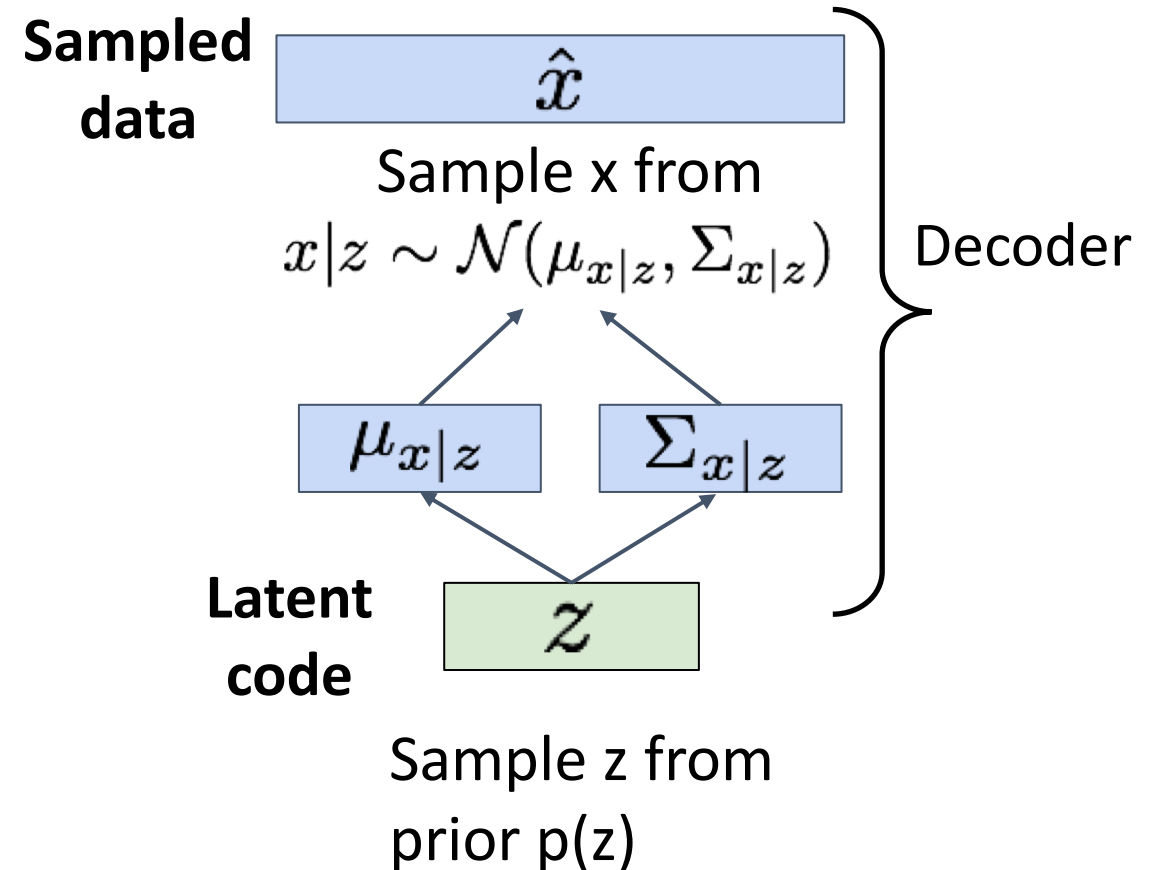
1. Sample z from prior $p(z)$
2. Run sampled z through decoder to get distribution over data x



Variational Autoencoders: Generating Data

After training we can generate new data!

1. Sample z from prior $p(z)$
2. Run sampled z through decoder to get distribution over data x
3. Sample from distribution in (2) to generate data

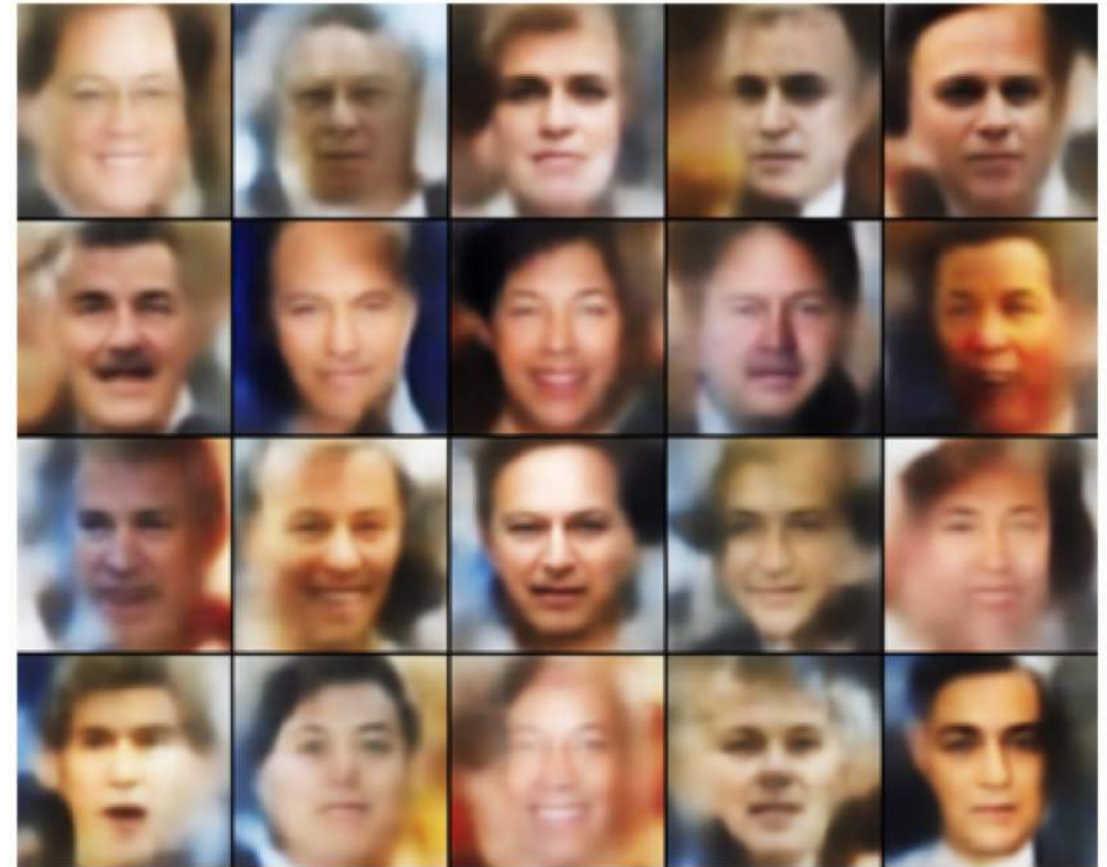


Variational Autoencoders: Generating Data

32x32 CIFAR-10



Labeled Faces in the Wild

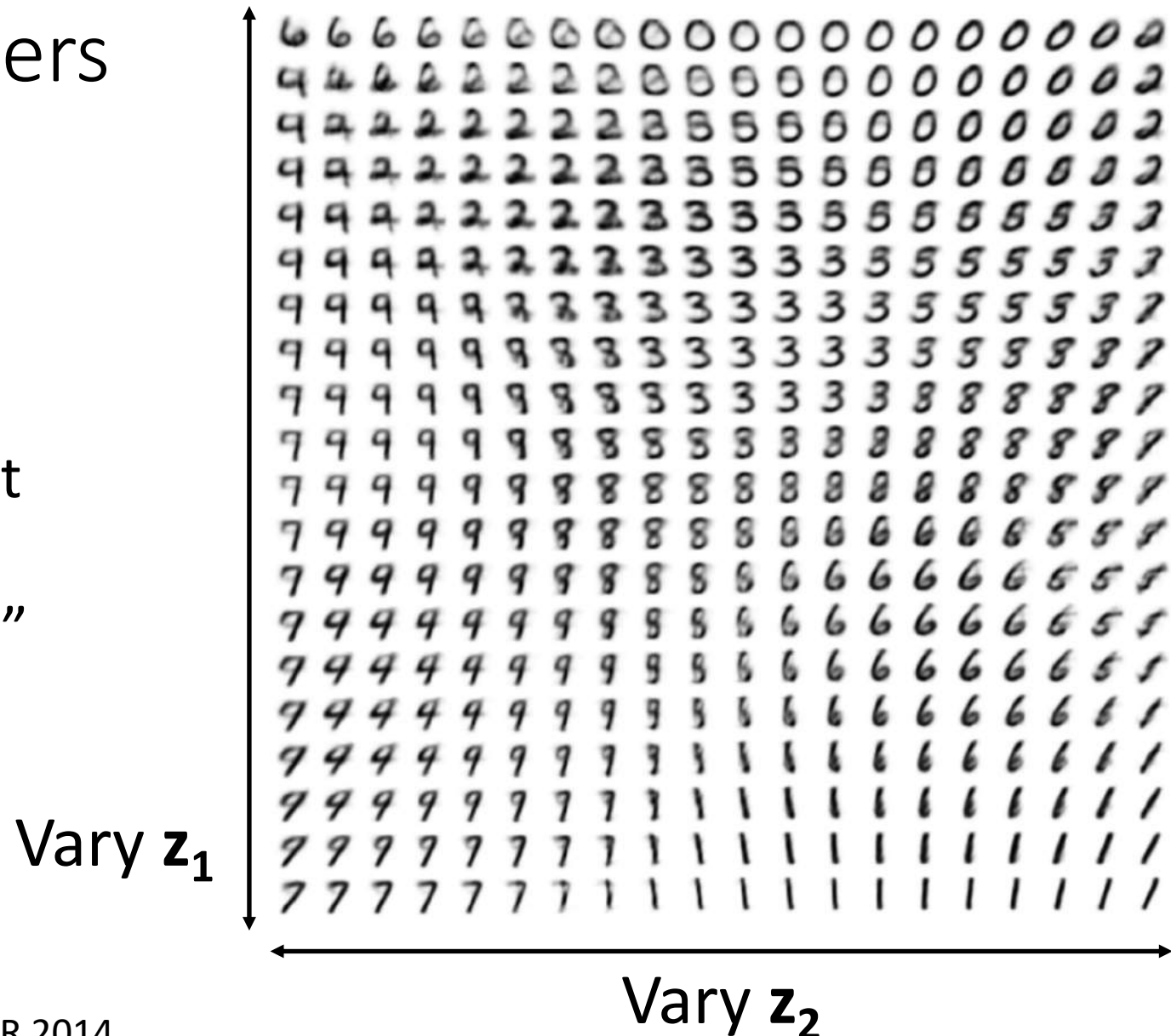


Figures from (L) Dirk Kingma et al. 2016; (R) Anders Larsen et al. 2017.

Variational Autoencoders

The diagonal prior on $p(z)$ causes dimensions of z to be independent

“Disentangling factors of variation”

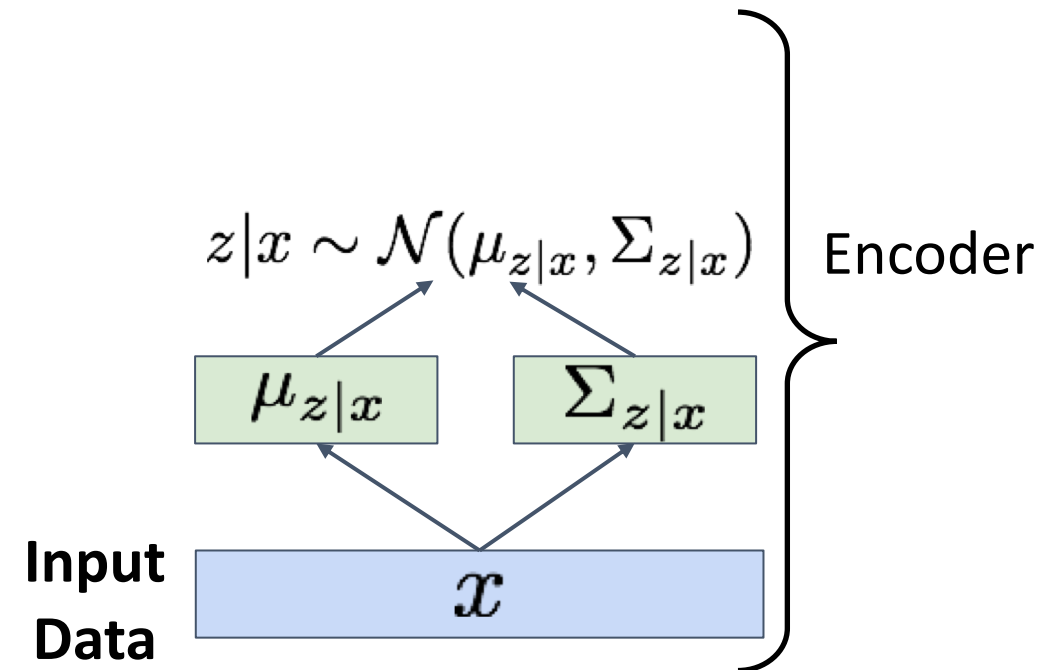


Kingma and Welling, Auto-Encoding Variational Bayes, ICLR 2014

Variational Autoencoders

After training we can **edit images**

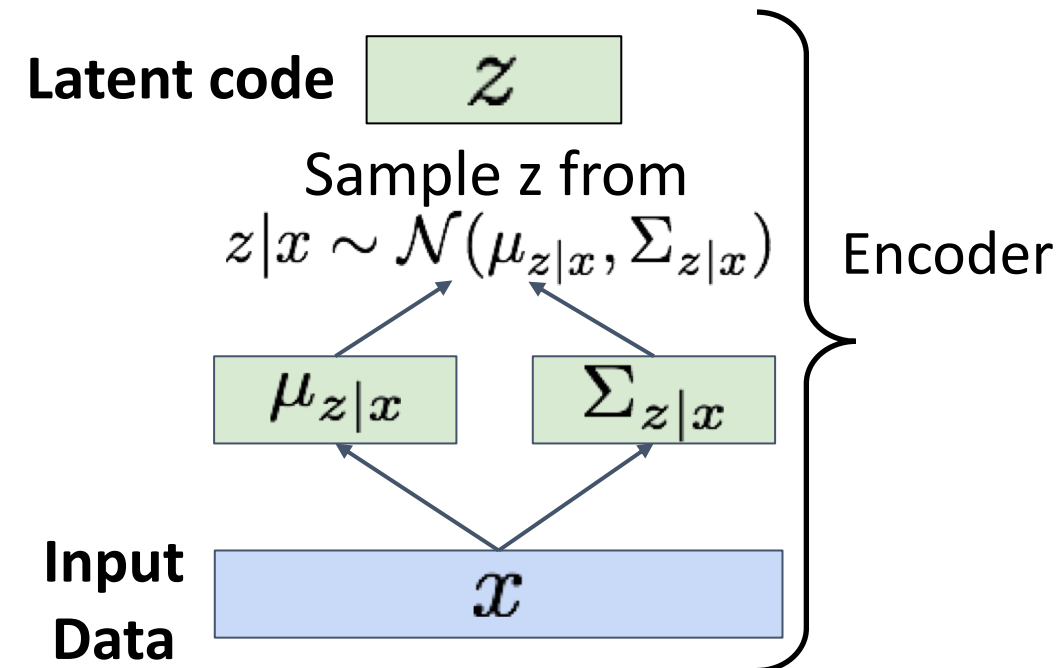
1. Run input data through **encoder** to get a distribution over latent codes



Variational Autoencoders

After training we can **edit images**

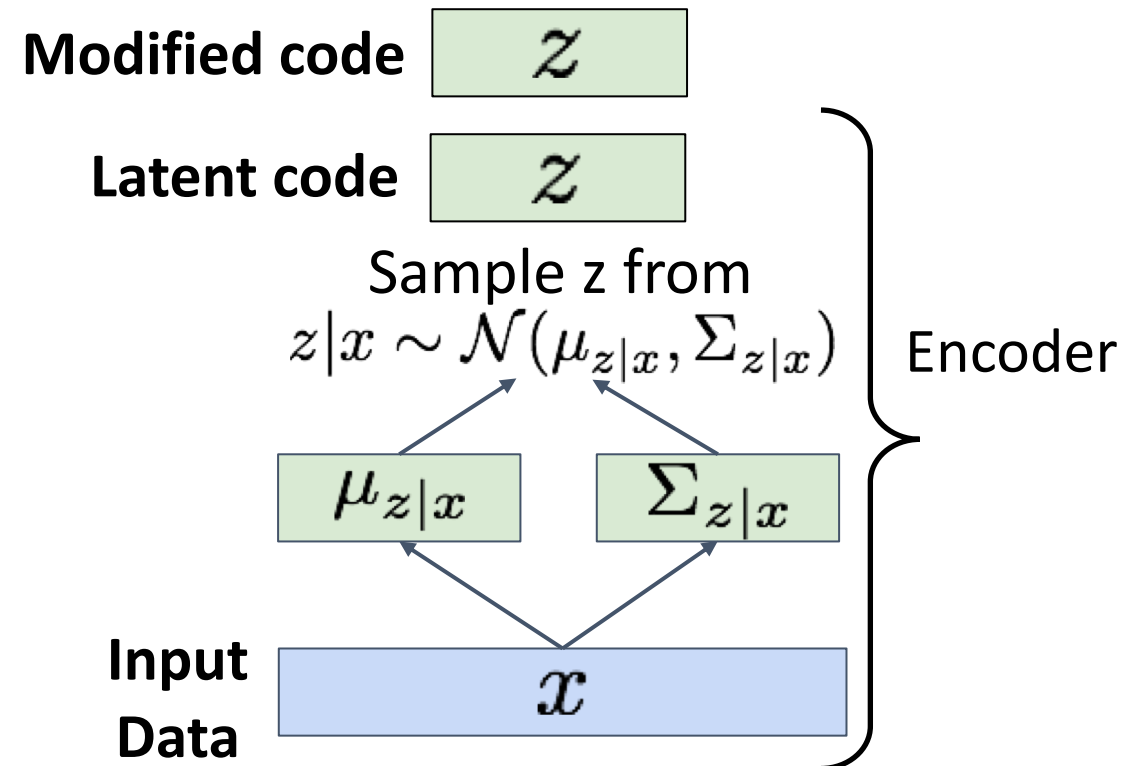
1. Run input data through **encoder** to get a distribution over latent codes
2. Sample code z from encoder output



Variational Autoencoders

After training we can **edit images**

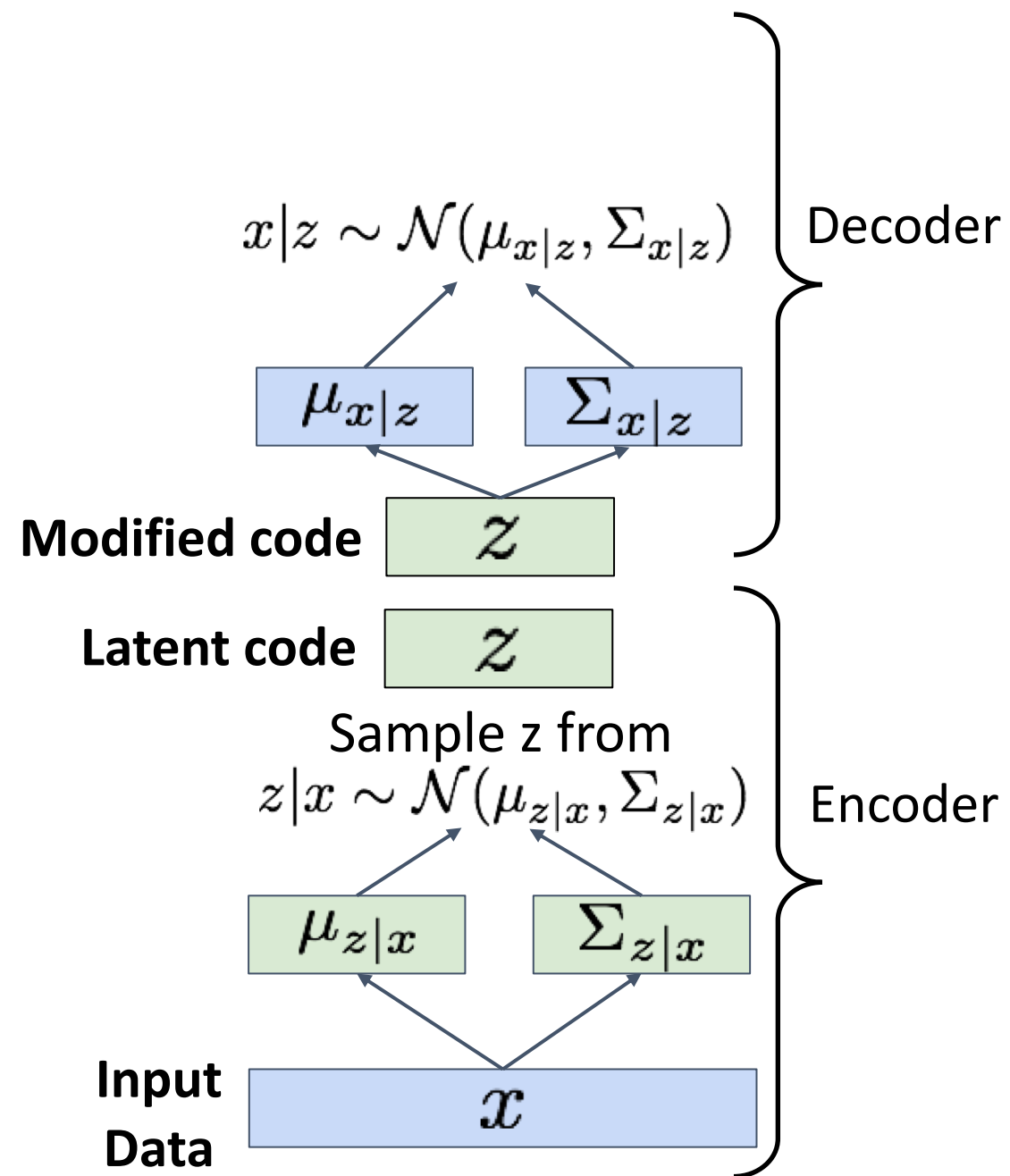
1. Run input data through **encoder** to get a distribution over latent codes
2. Sample code z from encoder output
3. Modify some dimensions of sampled code



Variational Autoencoders

After training we can **edit images**

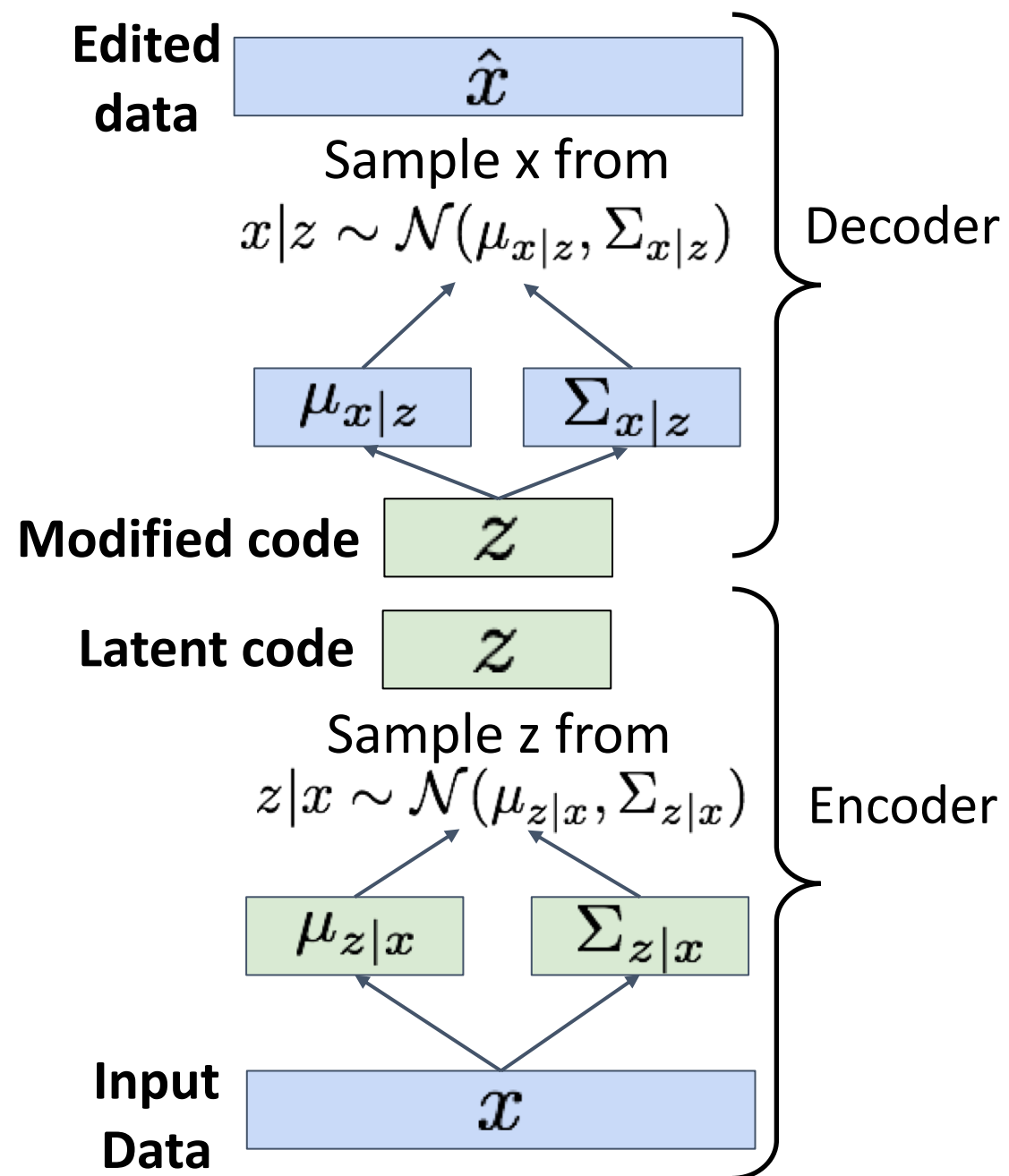
1. Run input data through **encoder** to get a distribution over latent codes
2. Sample code z from encoder output
3. Modify some dimensions of sampled code
4. Run modified z through **decoder** to get a distribution over data sample



Variational Autoencoders

After training we can **edit images**

1. Run input data through **encoder** to get a distribution over latent codes
2. Sample code z from encoder output
3. Modify some dimensions of sampled code
4. Run modified z through **decoder** to get a distribution over data samples
5. Sample new data from (4)



Variational Autoencoders

The diagonal prior on $p(z)$ causes dimensions of z to be independent

“Disentangling factors of variation”

Degree of smile

Vary z_1

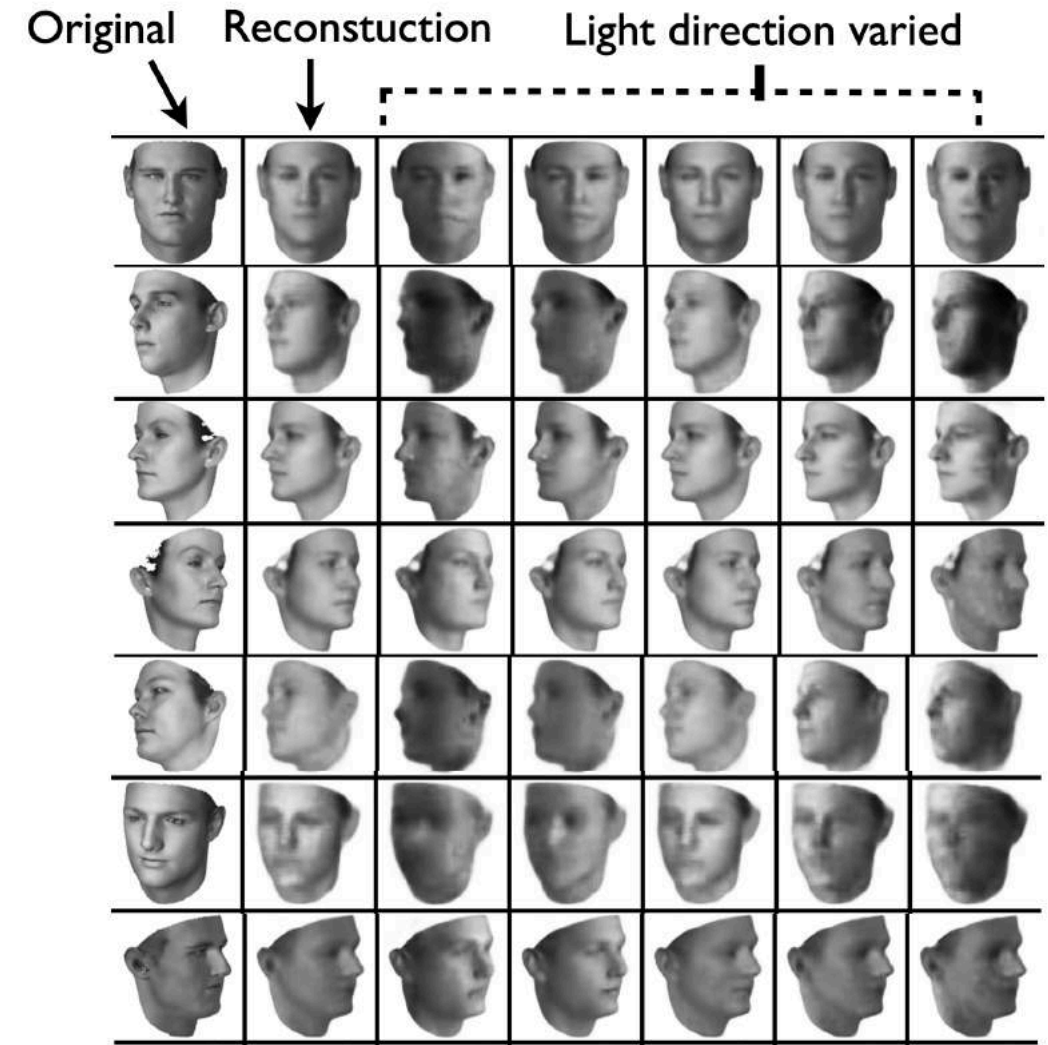
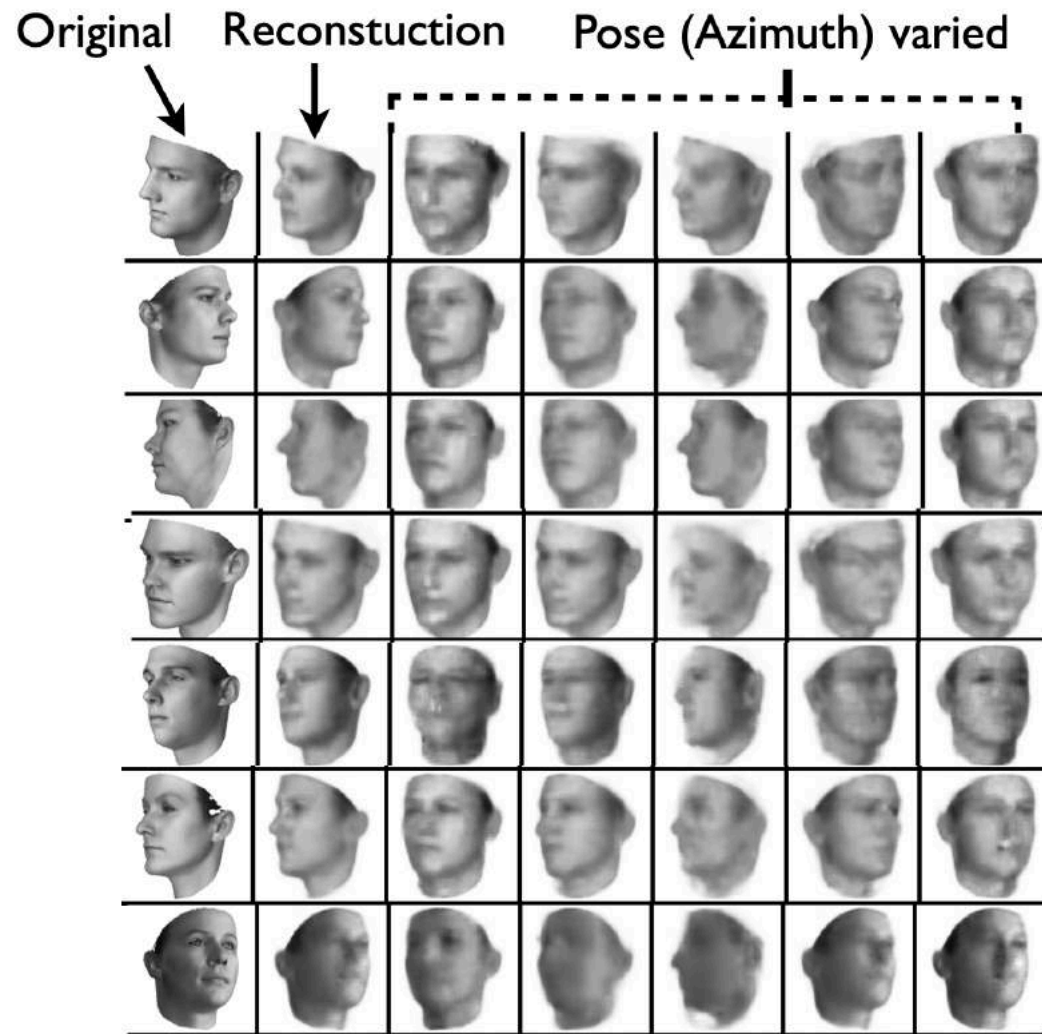
Head pose

Vary z_2



Kingma and Welling, Auto-Encoding Variational Bayes, ICLR 2014

Variational Autoencoders: Image Editing



Kulkarni et al, "Deep Convolutional Inverse Graphics Networks", NeurIPS 2014

Variational Autoencoder: Summary

Probabilistic spin to traditional autoencoders => allows generating data

Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Allows inference of $q(z|x)$, can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

- More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian, e.g., Gaussian Mixture Models (GMMs)
- Incorporating structure in latent variables, e.g., Categorical Distributions

So far: Two types of generative models

Autoregressive models

- Directly maximize $p(\text{data})$
- High-quality generated images
- Slow to generate images
- No explicit latent codes

Variational models

- Maximize lower-bound on $p(\text{data})$
- Generated images often blurry
- Very fast to generate images
- Learn rich latent codes

So far: Two types of generative models

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Variational models

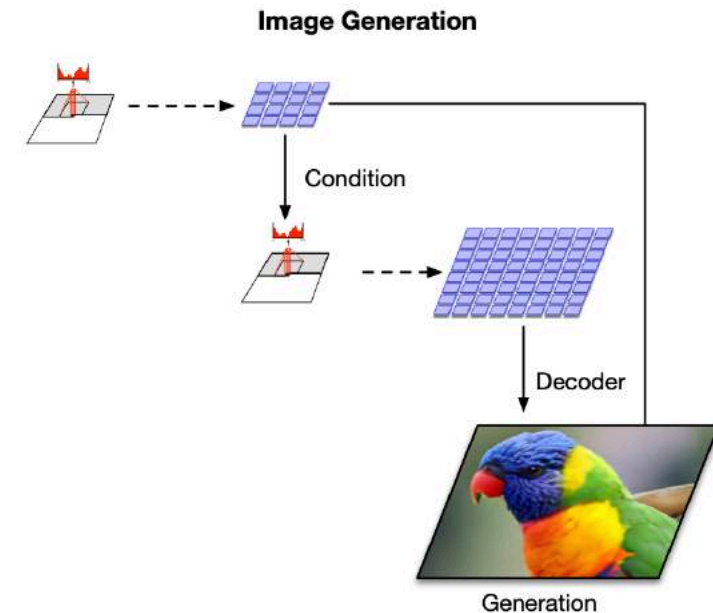
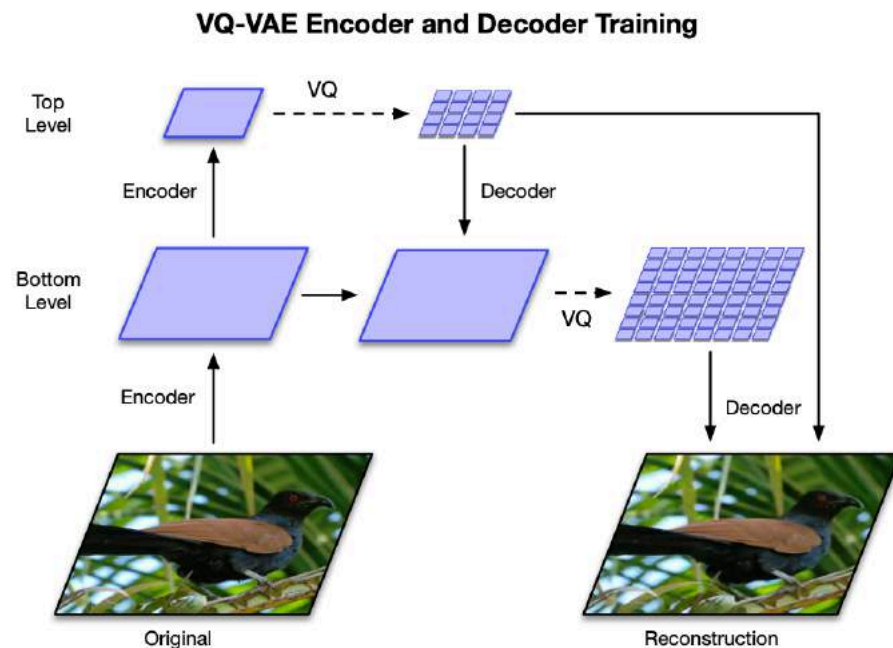
- Maximize lower-bound on $p(\text{data})$
- Generated images often blurry
- Very fast to generate images
- Learn rich latent codes

Can we combine them and get the best of both worlds?

Combining VAE + Autoregressive: Vector-Quantized Variational Autoencoder (VQ-VAE2)

Train a VAE-like model to generate multiscale grids of latent codes

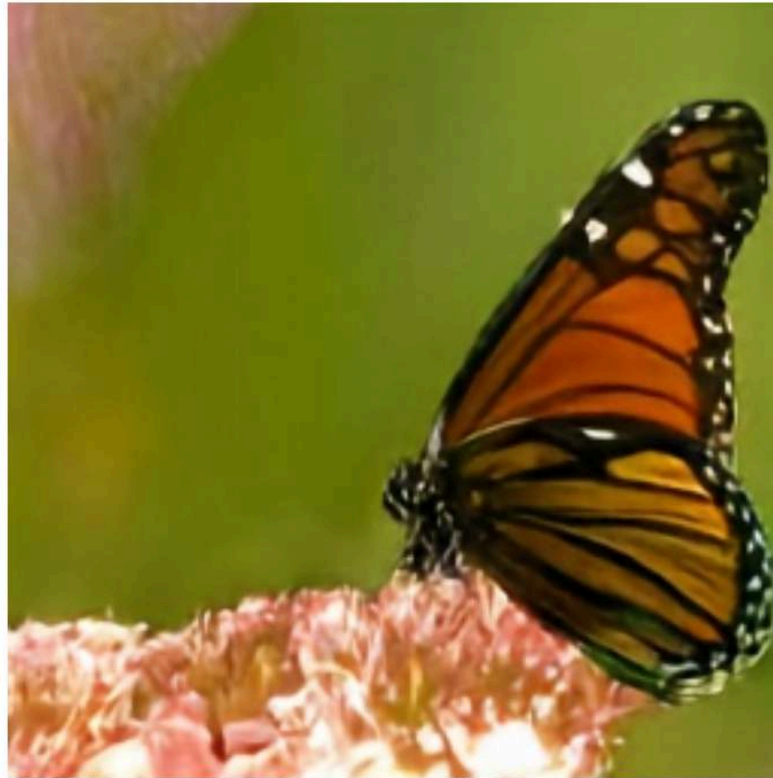
Use a multiscale PixelCNN to sample in latent code space



Razavi et al, "Generating Diverse High-Fidelity Images with VQ-VAE-2", NeurIPS 2019

Combining VAE + Autoregressive: VQ-VAE2

256 x 256 class-conditional samples, trained on ImageNet



Razavi et al, "Generating Diverse High-Fidelity Images with VQ-VAE-2", NeurIPS 2019

Combining VAE + Autoregressive: VQ-VAE2

256 x 256 class-conditional samples, trained on ImageNet



Razavi et al, "Generating Diverse High-Fidelity Images with VQ-VAE-2", NeurIPS 2019

Combining VAE + Autoregressive: VQ-VAE2

1024 x 1024 generated faces, trained on FFHQ



Razavi et al, "Generating Diverse High-Fidelity Images with VQ-VAE-2", NeurIPS 2019

Combining VAE + Autoregressive: VQ-VAE2

1024 x 1024 generated faces, trained on FFHQ



Razavi et al, "Generating Diverse High-Fidelity Images with VQ-VAE-2", NeurIPS 2019

Summary

Supervised vs Unsupervised Learning
Generative vs Discriminative models

Two classes of generative models:

Autoregressive models

- Directly maximize $p(\text{data})$
- High-quality generated images
- Slow to generate images
- No explicit latent codes

Variational models

- Maximize lower-bound on $p(\text{data})$
- Generated images often blurry
- Very fast to generate images
- Learn rich latent codes

Next Time:
Generative Models, part 2
(Generative Adversarial Networks)