

1.

a) time complexity: n^2 , space complexity: const

2 loops, each loop repeat n times

No extra memory needed

b) time complexity: n^3 , space complexity: n

3 loops, each loop repeat n times

Need n space memory for k

c) time complexity: n^2 , space complexity: const

2 loops, each loop repeat n times

Need 1 space memory for tmp

2.

a) time complexity: $\log n$, space complexity: const

first loop run $\log n$ times, second loop run i times

no extra memory needed

b) time complexity: n , space complexity: const

first loop run n times, second loop run i times

no extra memory needed

c) time complexity: $n \log n$, space complexity: const

first loop run $\log n$ times, second loop run n time

no extra memory needed

3.

	1 second	1 hour	1 month	1 century
$\log n$	10^{300000}			
\sqrt{n}	10^{12}	$1296 \cdot 10^{16}$	$6718464 \cdot 10^{18}$	
n	10^6	$36 \cdot 10^8$	$2592 \cdot 10^9$	$31556736 \cdot 10^8$
$N \log n$	62746	133378058		
N^2	1000	60000	1609968	56175382
N^3	100	1532	13736	146677

2ⁿ	19	31	41	51
N!	9	12	15	17

4.

Algorithm

Low = 0; high = length -1; mid = (high – low) / 2

Loop through array

If mid element is red, swap mid element and low element, increase mid and low by one

If mid is blue, increase mid by 1

If mid is white, swap mid element and high element, decrease high by 1