

Question 2

a) Time complexity

$$T(1) = 1$$

$$T(n) = 3T(n/3) + n$$

$$T(n/3) = 3T(n/9) + n/3$$

$$T(n) = 3(3T(n/9) + n/3) + n = 3^2 * T(n/(3^2)) + 2n$$

$$= 3^i * T(n/(3^i)) + i*n$$

$$\Rightarrow T(n) = n + n\log_3(n)$$

$$\mathbf{O(n\log_3(n))}$$

b) 3 way has better time complexity because $\log_3 n < \log_2 n$

c) in-place merge sort algorithm

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int arr[]
```

```
int a = arr[0], int b = arr[1]
```

```
if(a < b) increase position of a by 1
```

```
else increase position of a and b by 1
```