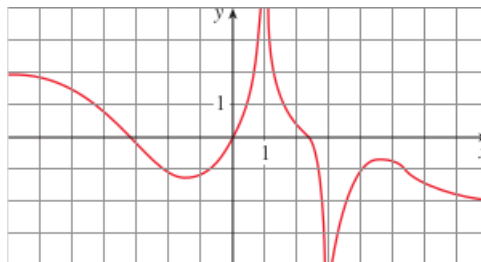


Section 3.4:

3. For the function f whose graph is given, state the following.



(a)

$$\lim_{x \rightarrow \infty} f(x) = -2$$

(b)

$$\lim_{x \rightarrow -\infty} f(x) = 2$$

(c)

$$\lim_{x \rightarrow 1} f(x) = \infty$$

(d)

$$\lim_{x \rightarrow 3} f(x) = -\infty$$

(e) The equations of the asymptotes

$$x = 1, x = 3, y = -2, y = 2$$

8. Evaluate the limit and justify each step by indicating the appropriate properties of limits.

$$\begin{aligned} & \lim_{x \rightarrow \infty} \sqrt{\frac{9x^3 + 8x - 4}{3 - 5x + x^3}} \\ &= \lim_{x \rightarrow \infty} \sqrt{\frac{x^3(9 + 8/x^2 - 4/x^3)}{x^3(3/x^3 - 5/x^2 + 1)}} \\ &= \lim_{x \rightarrow \infty} \sqrt{\frac{9 + 8/x^2 - 4/x^3}{3/x^3 - 5/x^2 + 1}} \end{aligned}$$

$$= \sqrt{\frac{9+0-0}{0-0+1}}$$

$$\boxed{= \sqrt{9} = 3}$$

11. Find the limit or show that it does not exist.

$$\lim_{t \rightarrow -\infty} \frac{3t^2 + t}{t^3 - 4t + 1}$$

$$= \lim_{t \rightarrow -\infty} \frac{t^2(3 + 1/t)}{t^3(1 - 4/t^2 + 1/t^3)}$$

$$= \lim_{t \rightarrow -\infty} \frac{(3 + 1/t)}{t(1 - 4/t^2 + 1/t^3)}$$

$$\boxed{= 0}$$

18. Find the limit or show that it does not exist.

$$\lim_{t \rightarrow \infty} \frac{t + 3}{\sqrt{2t^2 - 1}}$$

$$= \lim_{t \rightarrow \infty} \frac{t(1 + 3/t)}{t\sqrt{2 - 1/t^2}}$$

$$= \lim_{t \rightarrow \infty} \frac{1 + 3/t}{\sqrt{2 - 1/t^2}}$$

$$= \frac{1 + 0}{\sqrt{2 - 0}}$$

$$\boxed{= \frac{1}{\sqrt{2}}}$$

26. Find the limit or show that it does not exist.

$$= \lim_{x \rightarrow -\infty} (\sqrt{4x^2 + 3x} + 2x)$$

$$= \lim_{x \rightarrow -\infty} (|x|\sqrt{4 + 3/x} + 2x)$$

Because x is approaching to $-\infty$. $|x| = -x$.

$$= \lim_{x \rightarrow -\infty} (-x\sqrt{4 + 3/x} + 2x)$$

$$= \lim_{x \rightarrow -\infty} x(-\sqrt{4 + 3/x} + 2)$$

$$= -\infty(-2 + 2)$$

$$= -\infty(0)$$

$$\boxed{= 0}$$

28. Find the limit or show that it does not exist.

$$\begin{aligned} & \lim_{x \rightarrow \infty} (x - \sqrt{x}) \\ &= \lim_{x \rightarrow \infty} x(1 - 1/\sqrt{x}) \\ &= \infty(1 - 0) \\ & \boxed{= \infty} \end{aligned}$$

31. Find the limit or show that it does not exist.

$$\begin{aligned} & \lim_{x \rightarrow \infty} x \sin \frac{1}{x} \\ &= \infty \sin 0 \\ & \boxed{= 0} \end{aligned}$$

37. Find the horizontal and vertical asymptotes of each curve. You may want to use a graphing calculator (or computer) to check your work by graphing the curve and estimating the asymptotes.

$$y = \frac{2x^2 + x - 1}{x^2 + x - 2}$$

Horizontal Asymptotes:

$$\begin{aligned} & \lim_{x \rightarrow \infty} \frac{2x^2 + x - 1}{x^2 + x - 2} \\ &= \lim_{x \rightarrow \infty} \frac{x^2(2 + 1/x - 1/x^2)}{x^2(1 + 1/x - 2/x^2)} \\ &= \lim_{x \rightarrow \infty} \frac{2 + 1/x - 1/x^2}{1 + 1/x - 2/x^2} \\ & \boxed{= 2} \end{aligned}$$

$$\begin{aligned} & \lim_{x \rightarrow -\infty} \frac{2x^2 + x - 1}{x^2 + x - 2} \\ &= \lim_{x \rightarrow -\infty} \frac{x^2(2 + 1/x - 1/x^2)}{x^2(1 + 1/x - 2/x^2)} \\ &= \lim_{x \rightarrow -\infty} \frac{2 + 1/x - 1/x^2}{1 + 1/x - 2/x^2} \\ & \boxed{= 2} \end{aligned}$$

$$\boxed{y = 2}$$

Vertical Asymptotes;

$$\begin{aligned} & x^2 + x - 2 = 0 \\ & (x - 1)(x + 2) = 0 \\ & \boxed{x = 1 \text{ or } x = -2} \\ & \boxed{x = 1, x = -2} \end{aligned}$$

54. Find the limits as $x \rightarrow \infty$ and as $x \rightarrow -\infty$. Use this information, together with intercepts, to give a rough sketch of the graph as in Example 11.

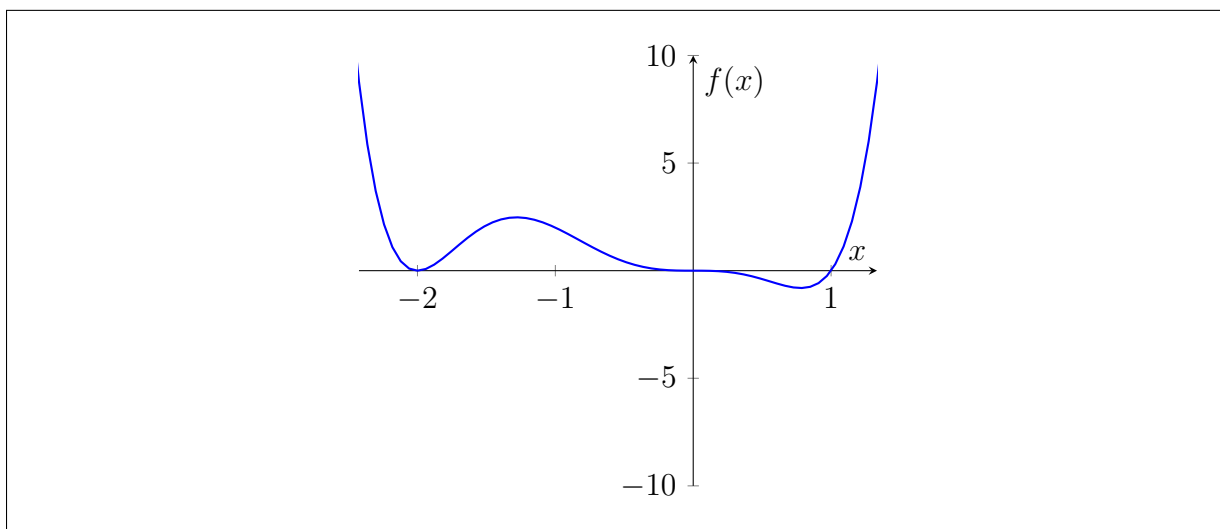
$$y = x^3(x+2)^2(x-1)$$

$$\lim_{x \rightarrow \infty} x^3(x+2)^2(x-1)$$

$$= \infty$$

$$\lim_{x \rightarrow -\infty} x^3(x+2)^2(x-1)$$

$$= \infty$$



59. Sketch the graph of a function that satisfies all of the given conditions.

Section 3.5:

5. Use the guidelines of this section to sketch the curve.

$$y = x(x - 4)^3 = x(x^3 - 3x^2 \times 4 + 3x \times 4^2 - 4^3)$$

$$y = x(x^3 - 12x^2 + 48x - 64) = x^4 - 12x^3 + 48x^2 - 64x$$

- (a) Domain: $(-\infty, \infty)$

- (b) Intercepts:

$$f(0) = 0(0 - 4)^3 = 0$$

y - intercepts are 0

$$f(x) = x(x - 4)^3 = 0$$

x - intercepts are 0 and 4

- (c) Symmetry:

$$f(-x) = (-x)^4 - 12(-x)^3 + 48(-x)^2 - 64(-x)$$

$$f(-x) = x^4 + 12x^3 + 48x^2 + 64x$$

The function is not odd nor even.

- (d) Asymptotes:

Since the function is a polynomial function. It will be defined everywhere and has no vertical asymptote.

$$\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} x^4 - 12x^3 + 48x^2 - 64x = \infty$$

$$\lim_{x \rightarrow -\infty} f(x) = \lim_{x \rightarrow -\infty} x^4 - 12x^3 + 48x^2 - 64x = \infty$$

The function also doesn't have horizontal asymptote.

- (e) Intervals of Increase or Decrease:

$$f'(x) = 4x^3 - 36x^2 + 96x - 64 = 0$$

$$x = 1 \text{ or } x = 4$$

x	$-\infty$	1	4	∞
$f'(x)$	-	0	+	0
$f(x)$		↓ -27	↑ 0	↑

The function $f(x)$ increases on the intervals $(1, 4)$ and $(4, \infty)$.

The function $f(x)$ decreases on the interval $(-\infty, 1)$.

- (f) Local Maximum and Minimum Values:

Local Minimum Values is $f(1) = -27$.

- (g) Concavity and Points of Inflection:

$$f''(x) = 12x^2 - 72x + 96 = 0$$

$$x = 2 \text{ or } x = 4$$

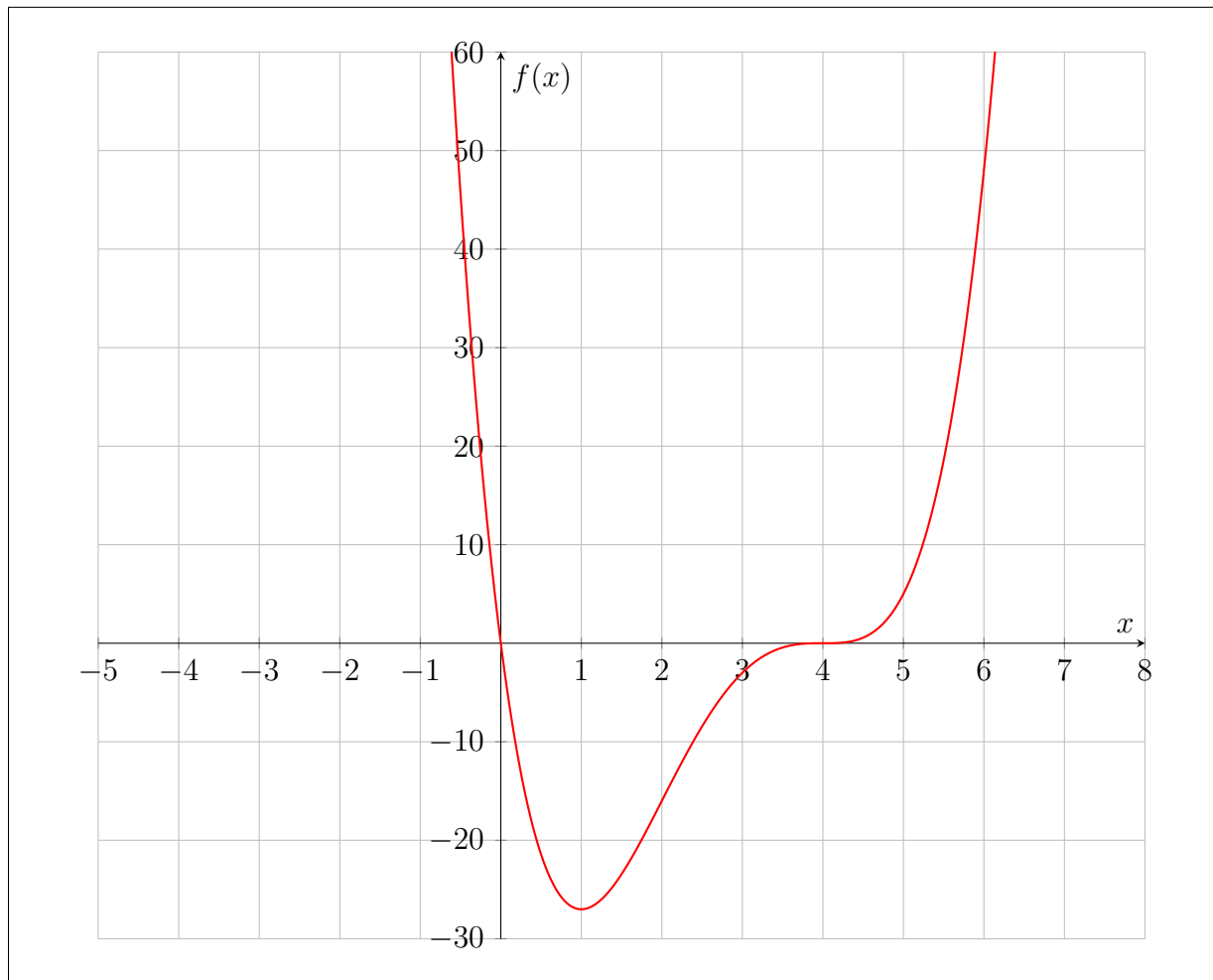
x	$-\infty$	2	4	∞
$f''(x)$	$+$	0	$-$	0
	$+$		$+$	

The function $f(x)$ is concave up on the intervals $(-\infty, 2)$ and $(4, \infty)$.

The function $f(x)$ is concave down on the intervals $(2, 4)$.

Points of Inflection are $(2, 16)$ and $(4, 0)$.

(h) Sketch the graph:



9. Use the guidelines of this section to sketch the curve.

$$y = \frac{2x + 3}{x + 2}$$

(a) Domain:

$$x + 2 \neq 0$$

$$x \neq -2$$

Hence, the domain of $f(x)$ is: $\mathbb{R} \setminus \{-2\}$

(b) Intercepts:

$$f(0) = \frac{2 \times 0 + 3}{0 + 2} = \frac{3}{2}$$

$$f(x) = \frac{2x+3}{x+2} = 0$$

$$x = -\frac{3}{2}$$

The y-intercepts of the function is $\frac{3}{2}$.

The x-intercepts of the function is $-\frac{3}{2}$.

(c) Symmetry:

$$f(-x) = \frac{2(-x)+3}{(-x)+2}$$

$$f(-x) = \frac{-2x+3}{-x+2}$$

The function is not odd nor even.

(d) Asymptotes:

$$\lim_{x \rightarrow -2^-} \frac{2x+3}{x+2} = \infty$$

$$\lim_{x \rightarrow -2^+} \frac{2x+3}{x+2} = -\infty$$

The function has a vertical asymptote $x = -2$.

$$\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} \frac{2x+3}{x+2} = \lim_{x \rightarrow \infty} \frac{x(2+3/x)}{x(1+2/x)} = \lim_{x \rightarrow \infty} \frac{2+3/x}{1+2/x} = \frac{2+0}{1+0} = 2$$

$$\lim_{x \rightarrow -\infty} f(x) = \lim_{x \rightarrow -\infty} \frac{2x+3}{x+2} = \lim_{x \rightarrow -\infty} \frac{x(2+3/x)}{x(1+2/x)} = \lim_{x \rightarrow -\infty} \frac{2+3/x}{1+2/x} = \frac{2+0}{1+0} = 2$$

The function has a horizontal asymptote $y = 2$.

(e) Intervals of Increase or Decrease:

$$f'(x) = \frac{(2x+3)'(x+2) - (x+2)'(2x+3)}{(x+2)^2}$$

$$f'(x) = \frac{2(x+2) - (2x+3)}{(x+2)^2}$$

$$f'(x) = \frac{2x+4-2x-3}{(x+2)^2}$$

$$f'(x) = \frac{1}{(x+2)^2} > 0 \quad \forall x \in (\mathbb{R} \setminus \{-2\})$$

Hence, the function always increases on the domain $\mathbb{R} \setminus \{-2\}$.

(f) Local Maximum and Minimum Values:

The function doesn't have any local maximum nor minimum.

(g) Concavity and Points of Inflection:

$$f''(x) = -\frac{[(x+2)^2]'}{(x+2)^4}$$

$$f''(x) = -\frac{2(x+2)}{(x+2)^4}$$

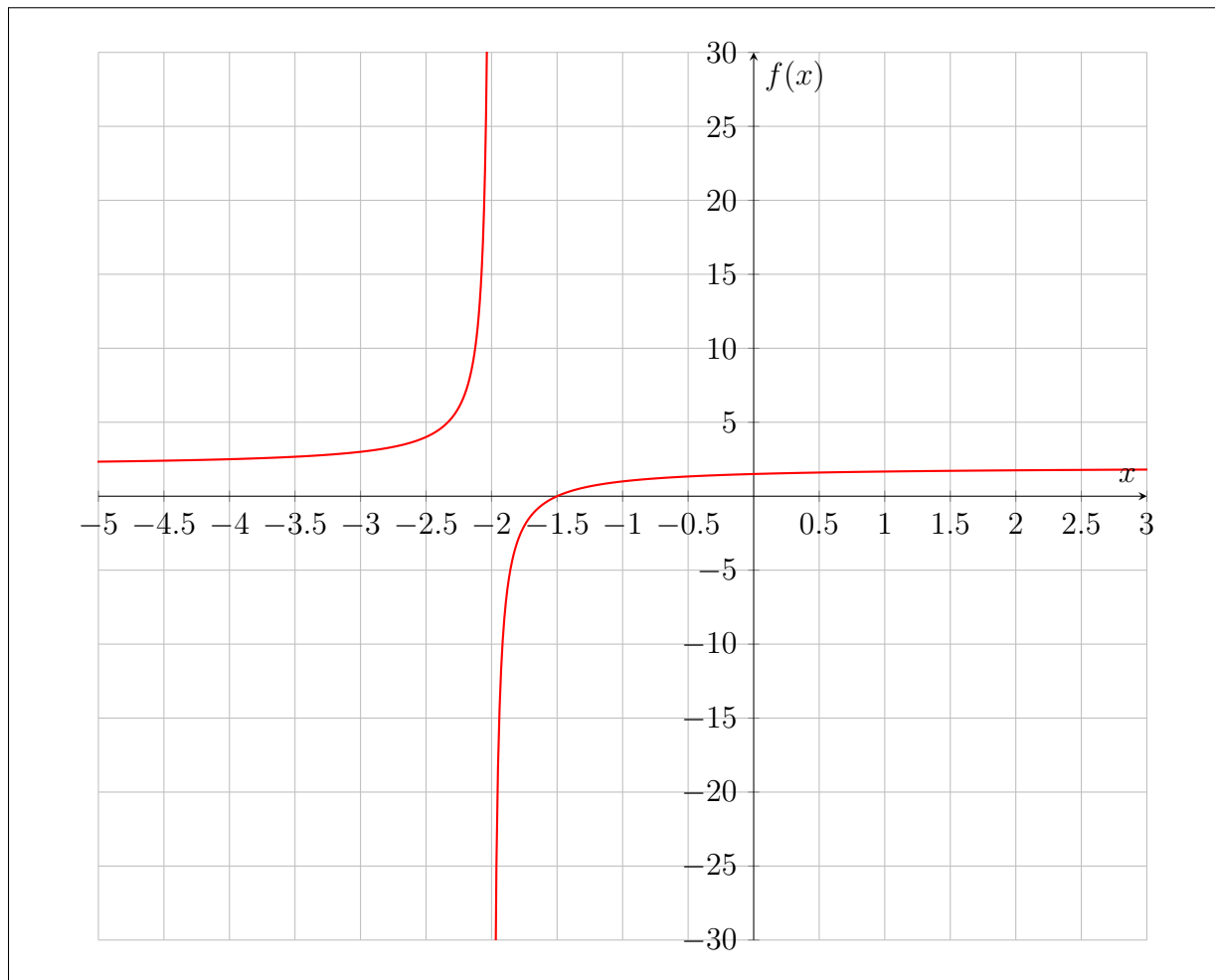
$$f''(x) = -\frac{2}{(x+2)^3}$$

x	$-\infty$	-2	∞
$f''(x)$	$+$	0	$-$

The function $f(x)$ is concave up in the interval $(-\infty, -2)$.

The function $f(x)$ is concave up in the interval $(-2, \infty)$.

(h) Sketch the graph:



21. Use the guidelines of this section to sketch the curve.

$$y = (x - 3)\sqrt{x}$$

(a) Domain:

$$x \geq 0$$

The domain of the function $f(x)$ is $[0, \infty)$.

(b) Intercepts:

$$f(0) = (0 - 3)\sqrt{0} = 0$$

$$f(x) = (x - 3)\sqrt{x} = 0$$

$$(x - 3)\sqrt{x} = 0$$

$$x = 0 \text{ or } x = 3$$

The y-intercept of the function is 0.

The x-intercepts of the function are 0 and 3.

(c) Symmetry:

Because the function has the domain $[0, \infty)$ so this function is not symmetrical.

(d) Asymptotes:

$$\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} (x - 3)\sqrt{x} = \infty$$

$$\lim_{x \rightarrow -\infty} f(x) \text{ is undefined.}$$

So the function doesn't have any horizontal nor vertical asymptote.

(e) Interval of Increase or Decrease:

$$f'(x) = (x - 3)' \sqrt{x} + (x - 3) \sqrt{x}'$$

$$f'(x) = \sqrt{x} + \frac{x - 3}{2\sqrt{x}}$$

$$f'(x) = \frac{2x + x - 3}{2\sqrt{x}}$$

$$f'(x) = \frac{3x - 3}{2\sqrt{x}} = 0$$

$$x = 1$$

x	0	1	∞	
$f'(x)$		-	0	+
$f(x)$	0	↓	-2	↑

Hence, the function f increases on the interval $(1, \infty)$.

The function f decreases on the interval $(0, 1)$.

(f) Local Maximum and Minimum Values:

The function f has local minimum at $x = 1$, $f(1) = -2$.

(g) Concavity and Inflection Point

$$f''(x) = \frac{(3x - 3)' 2\sqrt{x} - (2\sqrt{x})'(3x - 3)}{4x}$$

$$f''(x) = \frac{6\sqrt{x} - \frac{1}{\sqrt{x}}(3x - 3)}{4x}$$

$$f''(x) = \frac{6x - 3x + 3}{4x\sqrt{x}}$$

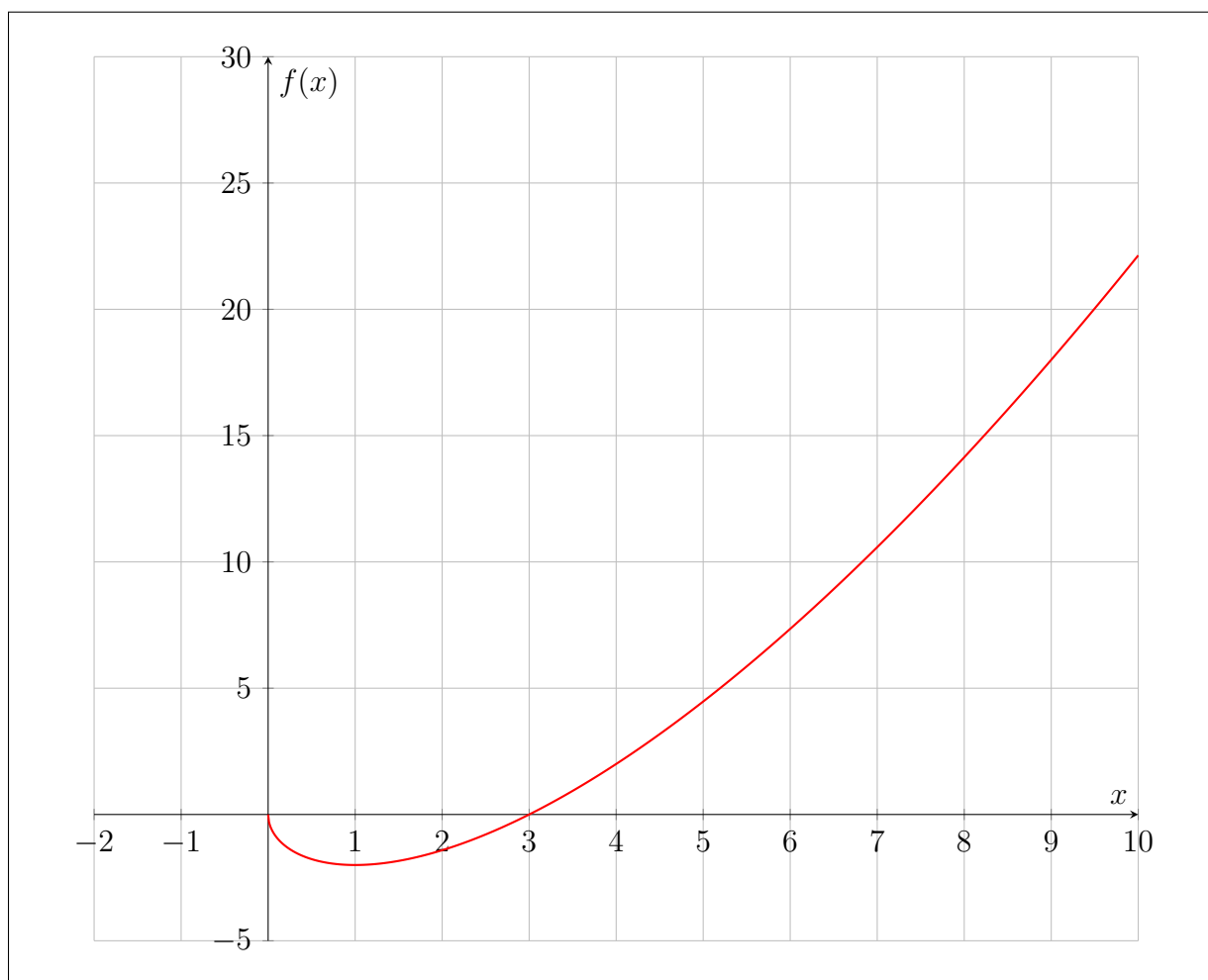
$$f''(x) = \frac{3x + 3}{4x\sqrt{x}} = 0$$

$$x = -1$$

x	$-\infty$	-1	0	∞
$f''(x)$				+

Hence, the function is concave up on the interval $(0, \infty)$

(h) Sketch the graph:



28. Use the guidelines of this section to sketch the curve.

$$y = \frac{x}{\sqrt{x^2 - 1}}$$

(a) Domain:

$$x^2 - 1 > 0$$

$$x^2 > 1$$

$$x < -1 \text{ or } x > 1$$

Hence, the domain of the function is $(-\infty, -1) \cup (1, \infty)$.

(b) Intercepts:

$$f(0) = \frac{0}{\sqrt{0^2 - 1}} \text{ is not defined}$$

$$f(x) = \frac{x}{\sqrt{x^2 - 1}} = 0$$

$$\frac{x}{\sqrt{x^2 - 1}} = 0 \text{ doesn't have any solution.}$$

Hence, there is no x nor y intercept.

(c) Symmetry:

$$f(-x) = \frac{-x}{\sqrt{(-x)^2 - 1}} = -\frac{x}{\sqrt{x^2 - 1}}$$

Hence, $f(-x) = -f(x)$. The graph is odd.

(d) Asymptotes:

$$\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^+} \frac{x}{\sqrt{x^2 - 1}} = \lim_{x \rightarrow 1^+} \frac{x}{|x|\sqrt{1 - 1/x^2}}$$

Since $x > 1$ and is positive.

$$\lim_{x \rightarrow 1^+} \frac{1}{\sqrt{1 - 1/x^2}} = \infty$$

$$\lim_{x \rightarrow -1^-} f(x) = \lim_{x \rightarrow -1^-} \frac{x}{\sqrt{x^2 - 1}} = \lim_{x \rightarrow -1^-} \frac{x}{|x|\sqrt{1 - 1/x^2}}$$

Since $x < -1$ and is negative.

$$\lim_{x \rightarrow -1^-} \frac{-1}{\sqrt{1 - 1/x^2}} = -\infty$$

$$\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} \frac{x}{\sqrt{x^2 - 1}} = \lim_{x \rightarrow \infty} \frac{1}{\sqrt{1 - 1/x^2}} = \lim_{x \rightarrow \infty} \frac{x}{|x|\sqrt{1 - 1/x^2}}$$

Since x to ∞ is positive.

$$\lim_{x \rightarrow \infty} \frac{1}{\sqrt{1 - 1/x^2}} = 1$$

$$\lim_{x \rightarrow -\infty} f(x) = \lim_{x \rightarrow -\infty} \frac{x}{\sqrt{x^2 - 1}} = \lim_{x \rightarrow -\infty} \frac{-1}{\sqrt{1 - 1/x^2}} = \lim_{x \rightarrow -\infty} \frac{x}{|x|\sqrt{1 - 1/x^2}}$$

Since x to $-\infty$ is negative.

$$\lim_{x \rightarrow -\infty} -\frac{1}{\sqrt{1 - 1/x^2}} = -1$$

Hence, the vertical asymptotes of the function are $x = -1$, $x = 1$.

The horizontal asymptotes of the function are $y = -1$, $y = 1$.

(e) Intervals of Increase or Decrease:

$$f'(x) = \frac{x'\sqrt{x^2 - 1} - (\sqrt{x^2 - 1})'x}{(x^2 - 1)}$$

$$f'(x) = \frac{\sqrt{x^2-1} - \frac{x}{\sqrt{x^2-1}}x}{(x^2-1)}$$

$$f'(x) = \frac{x^2-1-x^2}{\sqrt{x^2-1}(x^2-1)}$$

$$f'(x) = \frac{-1}{\sqrt{x^2-1}(x^2-1)} < 0 \quad \forall x \in [(-\infty, 1) \cup (1, \infty)]$$

Hence, the function decreases on its interval $(-\infty, 1) \cup (1, \infty)$.

(f) Local Maximum and Minimum Values:

The function doesn't have any maximum or minimum values since it always decreases.

(g) Concavity and Inflection Point:

$$f''(x) = -\frac{(\sqrt{x^2-1}(x^2-1))'}{(x^2-1)^3}$$

$$f''(x) = -\frac{\frac{x}{\sqrt{x^2-1}}(x^2-1) + 2x\sqrt{x^2-1}}{(x^2-1)^3}$$

$$f''(x) = -\frac{x(x^2-1) + 2x(x^2-1)}{\sqrt{x^2-1}(x^2-1)^3}$$

$$f''(x) = -\frac{x^3-x+2x^3-2x}{\sqrt{x^2-1}(x^2-1)^3}$$

$$f''(x) = -\frac{3x^3-3x}{\sqrt{x^2-1}(x^2-1)^3} = 0$$

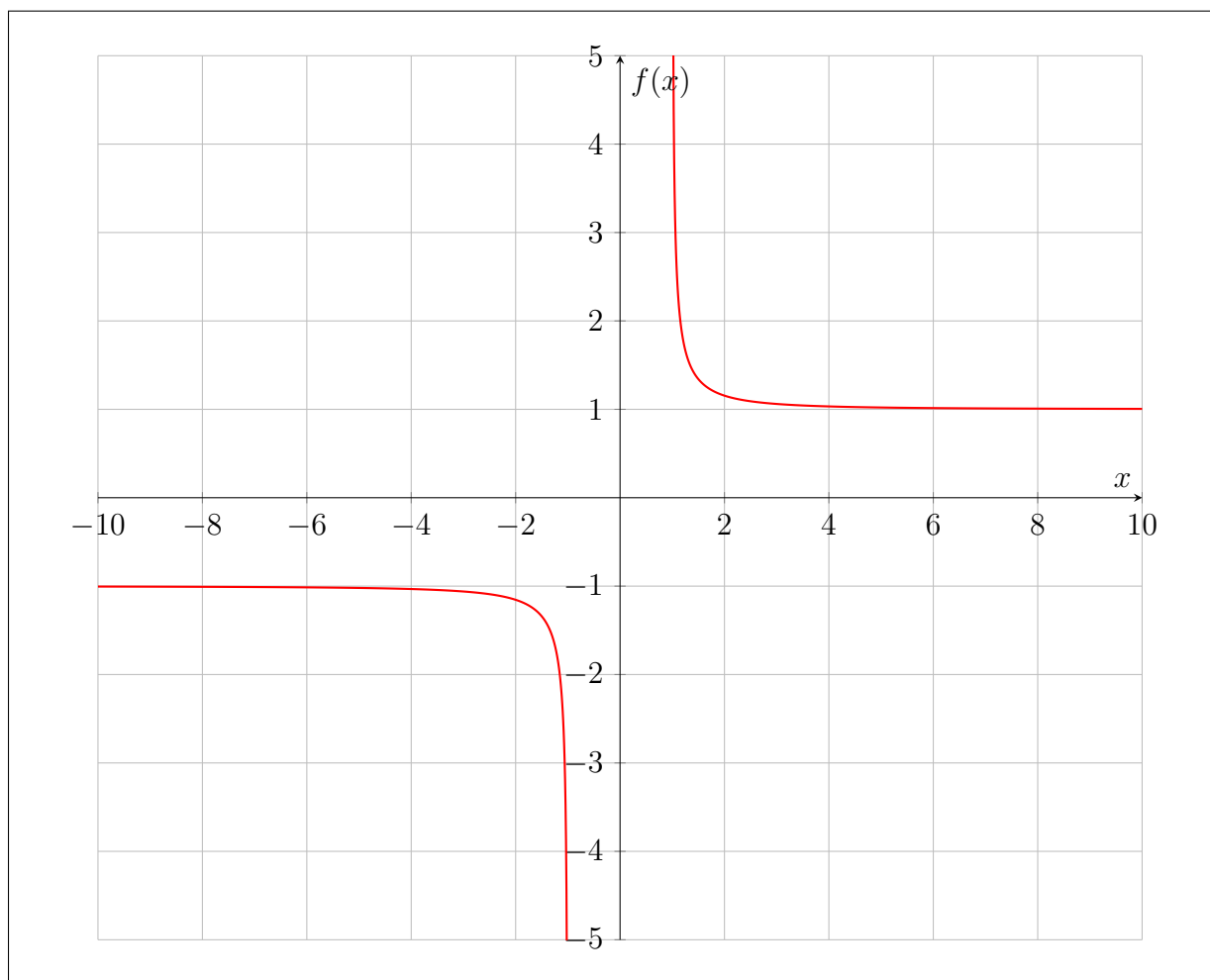
$$x = 0 \text{ or } x = \pm 1$$

x	$-\infty$	-1	0	1	∞
$f''(x)$		$-$	$ $	$ $	$+$

Hence, the function is concave up on the interval $(1, \infty)$.

The function is concave down on the interval $(-\infty, -1)$.

(h) Sketch the graph:



33. Use the guidelines of this section to sketch the curve.

$$y = \sin^3 x$$

(a) Domain:

Since this function is a trigonometric function. It will be continuous everywhere.
The domain of this function is $(-\infty, \infty)$.

(b) Intercepts:

$$f(0) = \sin^3(0) = 0$$

$$f(x) = \sin^3(x) = 0$$

$$x = n\pi \text{ with } n \text{ is a integer.}$$

The x-intercept is $n\pi$ with n is a integer.

The y-intervals is 0.

(c) Symmetry:

$$f(-x) = \sin^3(-x) = -\sin^3(x)$$

$$f(-x) = -f(x)$$

Hence, the function is odd.

(d) Asymptotes:

The function doesn't have any asymptote since it is a trigonometric function.

(e) Intervals of Increase or Decrease:

$$f'(x) = \sin^3(x)' = 3\sin^2(x)\cos(x) = 0$$

$$\sin(x) = 0 \text{ or } \cos(x) = 0$$

$$x = \frac{\pi}{2}n \text{ with } n \text{ is a integer.}$$

x	$-\infty$	\dots	0		$\pi/2$		π		$\pi 3/2$	\dots	∞
$f'(x)$		\dots	0	$+$	0	$-$	0	$+$	0	\dots	

The function repeated itself each $\frac{\pi}{2}$.

(f) Local Maximum and Minimum Values:

$$-1 \leq \sin(x) \leq 1$$

$$(-1)^3 \leq \sin^3(x) \leq (1)^3$$

$$-1 \leq \sin^3(x) \leq 1$$

Hence, the function local maximum is 1 and local minimum is -1.

(g) Concavity and Inflection Points:

$$f''(x) = 3\sin^2(x)'\cos(x) + \cos(x)'3\sin^2(x)$$

$$f''(x) = 6\sin(x)\cos^2(x) - 3\sin^3(x) = 0$$

$$6\sin(x)\cos^2(x) = 3\sin^3(x)$$

$$2 = \frac{\sin^2(x)}{\cos^2(x)}$$

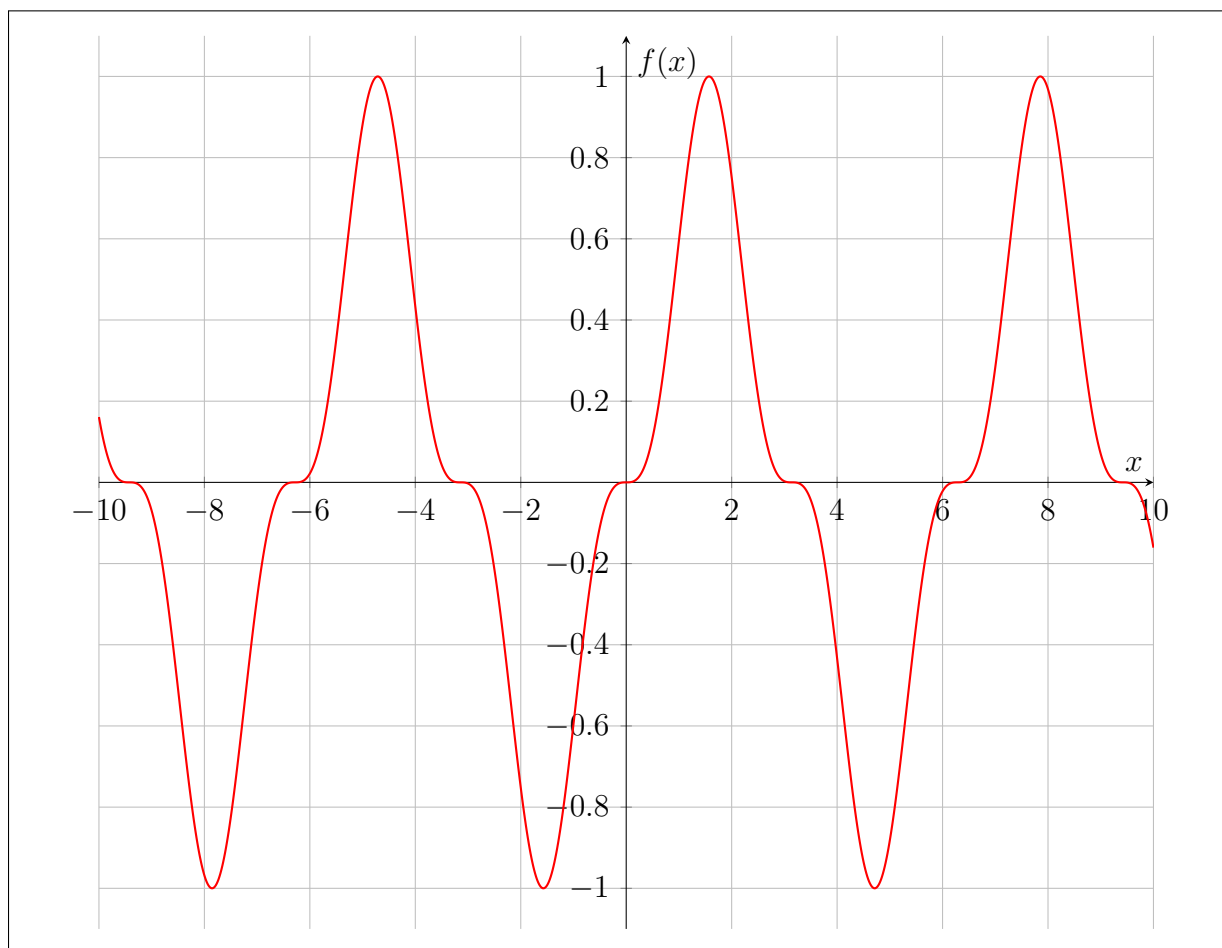
$$\tan(x) = \sqrt{2}$$

$$x = \tan^{-1}\sqrt{2} + n\pi \text{ with } n \text{ is an integer.}$$

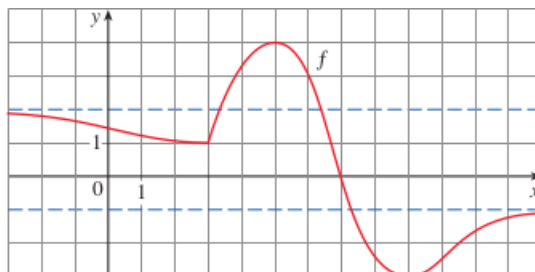
The function is concave up in $(0, \tan^{-1}\sqrt{2})$

then concave down in $(\tan^{-1}\sqrt{2}, \tan^{-1}\sqrt{2} + \pi)$ and repeats itself.

(h) Sketch the graph:



41. The graph of a function f is shown. (The dashed lines indicate horizontal asymptotes.) Find each of the following for the given function g .



$$g(x) = \sqrt{f(x)}$$

- (a) The domains of g and g' .
The domain of g is $(-\infty, 7]$.

$$g'(x) = \frac{f'(x)}{2\sqrt{f(x)}}$$

The domain of g' is $(-\infty, 3) \cup (3, 7)$.

(b) The critical numbers of g .

$$g'(x) = \frac{f'(x)}{2\sqrt{f(x)}} = 0$$

$$f'(x) = 0$$

$$x = 3 \text{ or } x = 5$$

(c) The approximate value of $g'(6)$.

$$g'(6) = \frac{f'(6)}{2\sqrt{f(6)}} \approx \frac{-2}{4} = -\frac{1}{2}$$

(d) All vertical and horizontal asymptotes of g .

$$g(x) = \sqrt{f(x)}$$

Because $f(x)$ has horizontal asymptotes $f(x) = 2$ and $f(x) = -1$. But $f(x) = -1$ is not defined for $g(x)$.

Therefore, $g(x) = \sqrt{f(x)} = \sqrt{2}$. Hence the horizontal asymptote of g is $y = \sqrt{2}$.

53. Use the guidelines of this section to sketch the curve. In guideline D , find an equation of the slant asymptote.

$$y = \frac{x^2}{x-1}$$

(a) Domain:

$$x - 1 \neq 0$$

$$x \neq 1$$

Hence the domain of the function is $(-\infty, 1) \cup (1, \infty)$.

(b) Intercepts:

$$f(0) = \frac{0^2}{0-1} = 0$$

$$f(x) = \frac{x^2}{x-1} = 0$$

$$x = 0$$

Hence, the y-intercept is 0. The x-intercept is 0.

(c) Symmetry:

$$f(-x) = \frac{(-x)^2}{-x-1} = \frac{x^2}{-x-1}$$

Hence the function is not odd nor even.

(d) Asymptotes:

$$\begin{aligned}\lim_{x \rightarrow 1^+} \frac{x^2}{x-1} &= \infty \\ \lim_{x \rightarrow 1^-} \frac{x^2}{x-1} &= -\infty \\ \lim_{x \rightarrow \infty} \frac{x^2}{x-1} &= \lim_{x \rightarrow \infty} \frac{x}{1-1/x} = \infty \\ \lim_{x \rightarrow -\infty} \frac{x^2}{x-1} &= -\infty\end{aligned}$$

Hence, the function has vertical asymptotes $x = 1$.

The slant asymptote after doing long division is $y = x + 1$.

(e) Intervals of Increase or Decrease:

$$\begin{aligned}f'(x) &= \frac{(x^2)'(x-1) - (x-1)'(x^2)}{x-1} \\ f'(x) &= \frac{2x(x-1) - (x^2)}{x-1} \\ f'(x) &= \frac{2x^2 - 2x - x^2}{x-1} \\ f'(x) &= \frac{(x^2 - 2x)}{x-1} = 0 \\ &\quad x = 0 \text{ or } x = 2 \\ \begin{array}{ccccccc} x & -\infty & 0 & 1 & 2 & \infty \\ \hline f'(x) & & - & 0 & + & || & - & 0 & + \end{array}\end{aligned}$$

Hence, the function increases on the interval $(0,1)$ and $(2,\infty)$.

The function decreases on the interval $(-\infty,0)$ and $(1,2)$.

(f) Local Maximum and Minimum Values:

Local Minimum Values:

$$\begin{aligned}f(0) &= \frac{0^2}{0-1} = 0 \\ f(2) &= \frac{2^2}{2-1} = 4\end{aligned}$$

(g) Concavity and Inflection Points:

$$\begin{aligned}f''(x) &= \frac{(x^2 - 2x)'(x-1) - (x-1)'(x^2 - 2x)}{(x-1)^2} \\ f''(x) &= \frac{(2x-2)(x-1) - (x^2 - 2x)}{(x-1)^2} \\ f''(x) &= \frac{2x^2 - 2x - 2x + 2 - x^2 + 2x}{(x-1)^2} \\ f''(x) &= \frac{x^2 - 2x + 2}{(x-1)^2} = 0\end{aligned}$$

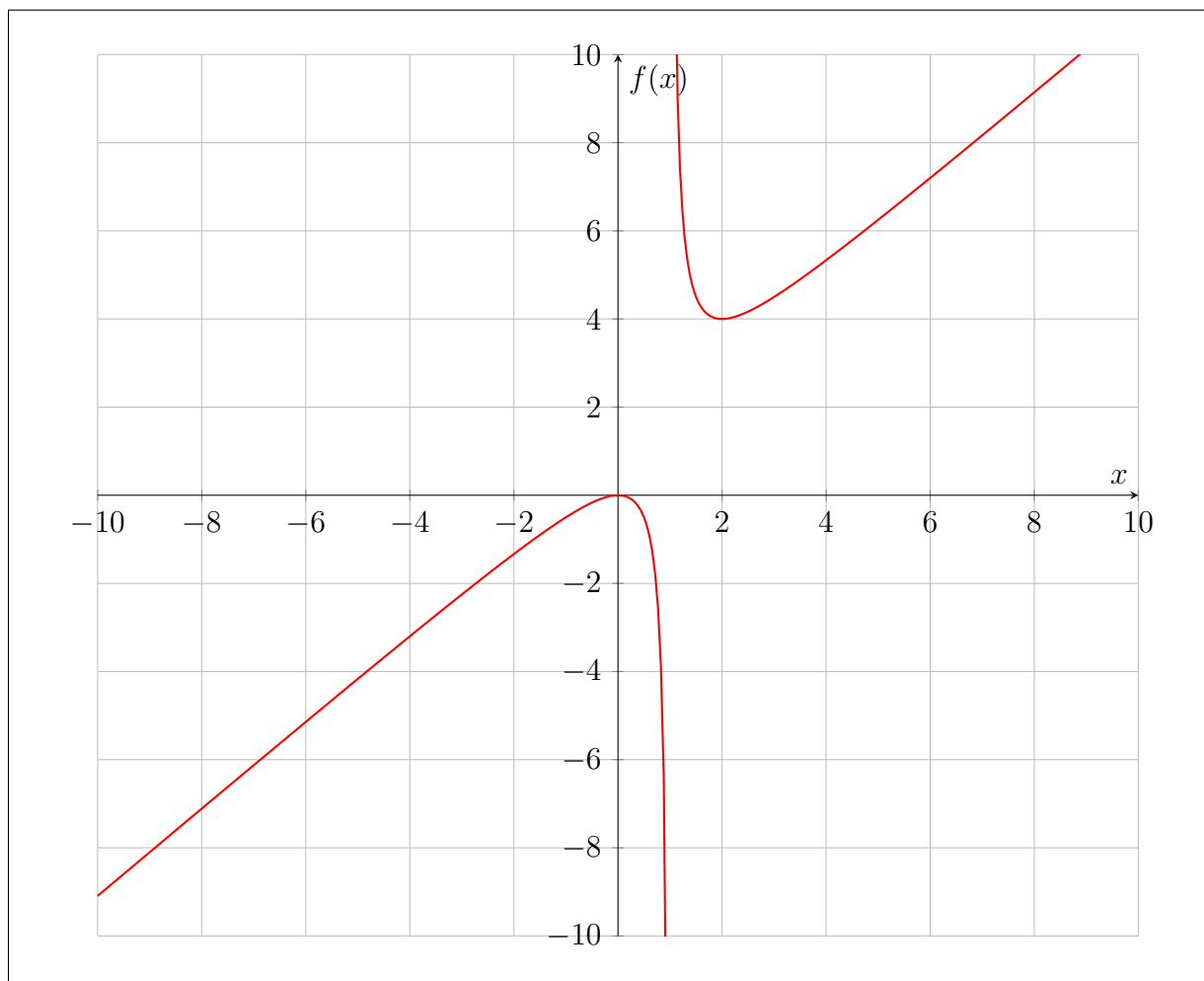
There is no solution for this function.

x	$-\infty$	1	∞
$f''(x)$	$-$	$ $	$+$

The function is concave up on the interval $(1, \infty)$.

The function is concave down on the interval $(-\infty, 1)$.

(h) Sketch the graph:



59. Show that the curve $y = \sqrt{4x^2 + 9}$ has two slant asymptotes: $y = 2x$ and $y = -2x$. Use this fact to help sketch the curve.

$$y = \sqrt{4x^2 + 9} = 2|x| + 3$$

For x very large and positive, $y \approx 2x$.

For x very large and negative, $y \approx -2x$.

Therefore, x has two slant asymptote $y = 2x$ and $y = -2x$.

