ECE 285 – Assignment #3 CNNs and PyTorch

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As for assignment #2, we focus on classification on the MNIST Dataset but using deep Convolutional Neural Networks (CNNs) and PyTorch (instead of shallow ANNs and manual implementation).

1 Convolutional Neural Networks (CNNs)?

CNNs are specific artificial neural networks composed of *convolutional* layers, *maxpooling* operations, and *fully connected layers*.

- Convolutional layers are like typical layers except the weight matrix has a specific structure that is relevant for signals and images. They take as input N images and produce as output C images (called *feature maps* or *channels*). They are parameterized by a collection of coefficients that defines a *filter bank*. Each filter performs a weighted average of its inputs within local sliding windows of size $K \times K$ (pixels) where K is an hyperparameter (a small odd number: 3, 5, 7, 9). As for classical layers, each feature map is next processed by an activation function such as ReLU.
- Maxpooling operations reduce the dimensions of each feature map by picking the maximum value within local but non-overlapping sliding windows of size $L \times L$ (pixels) where L is another hyperparameter (usually 2). Maxpooling does not introduce new parameters to be learned.
- Fully connected layers are standard layers where the weight matrix does not have a specific structure: each of the N output units is connected to each of the M input units.

This was a very short description but CNNs will be studied more in depth during the class.

2 PyTorch?

PyTorch is a Python based scientific computing package targeted at two sets of audiences:

- a replacement for NumPy to use the power of GPUs,
- a deep learning research platform that provides maximum flexibility and speed.

For more reading please visit http://pytorch.org/tutorials/beginner/deep_learning_60min_blitz.html

3 Getting started

First of all, connect to DSMLP (ieng6 server) and start a pod with enabled GPU/CUDA capabilities

\$ launch-pytorch-gpu.sh

Next connect to your Jupyter Notebook from your web browser (go back to Assignment #1 for more details). Create a new notebook Lab3.ipynb and import

```
from __future__ import print_function
import numpy as np
import torch
```

Note that we are using PyTorch 0.3.1, which is not the most recent one (0.4.0).

For the following questions, please write your code and answers directly in your notebook. Organize your notebook with headings, markdown and code cells (following the numbering of the questions).

4 Tensors

Torch tensors are similar to NumPy ndarrays, with the addition being that they can also be used on a GPU to accelerate computing. The documentation for tensors for the current version of PyTorch we are using is available here http://pytorch.org/docs/0.3.1/tensors.html

1. Construct a 5×3 tensor and print it with the following commands

```
x = torch.Tensor(5, 3)
print(x)
```

How was x initialized? What is the type of x?

2. Construct a randomly initialized matrix:

```
y = torch.rand(5, 3)
print(y)
```

How are the random values distributed? What is the type of x? What if we use instead y = torch.randn(5, 3)?

3. Run the following

```
x = x.double()
y = y.double()
print(x)
print(y)
```

What is the type displayed when you print x and y?

4. We can also initialize directly tensors with prescribed values. Create the following two tensors:

```
x = torch.Tensor([[-0.1859],
                                       0.5236],
                              1.3970,
                   [ 2.3854,
                              0.0707,
                                       2.1970],
                   [-0.3587,
                              1.2359, 1.8951],
                   [-0.1189, -0.1376,
                                       0.4647],
                   [-1.8968,
                              2.0164,
                                       0.1092]])
y = torch.Tensor([[ 0.4838,
                              0.5822,
                                       0.2755],
                              0.4932, -0.6680],
                   [ 1.0982,
                              0.6580, -0.5819],
                   [0.7915,
                   [0.3825, -1.1822, 1.5217],
                   [0.6042, -0.2280,
                                      1.3210]])
```

What are their shape?

5. You can stack the two 2d tensors in a 3d tensor as

```
z = torch.stack((x, y))
```

What is the shape of z?

How does it compare to torch.cat((x, y), 0) and torch.cat((x, y), 1)?

6. Report the value of the element at the 5th row and 3rd column in the 2d tensor y, and try accessing the same element in the 3d tensor z.

Hint: You can use standard NumPy-like indexing on all tensors.

- 7. Similarly print all the elements corresponding to the 5th row and 3rd column in z. How many elements are there?
- 8. Adding two tensors is fairly straightforward. There are multiple syntaxes for this operation. Sum \mathbf{x} and \mathbf{y} (from question 4) as follows

```
print(x + y)
print(torch.add(x, y))
print(x.add(y))
torch.add(x, y, out=x)
print(x)
```

Check whether the above instructions are printing the same output? Are they equivalent?

9. To reshape a tensor, you can use torch.view:

```
x = torch.randn(4, 4)
y = x.view(16)
z = x.view(-1, 8)
print(x.size(), y.size(), z.size())
```

Interpret the effect of each of these instructions. What does the -1 mean?

10. Generate 2 random tensors x and y of dimensions 10×10 and 2×100 , respectively, resize them such that the instruction torch.mm(x, y) performs a row vector by matrix multiplication resulting in a row vector of dimensions 1×2 .

Go through the documentation and get familiar with other operations as well.

5 NumPy and PyTorch

Converting a Torch tensor to a NumPy array and vice versa is a breeze.

11. Run the below code snippet and report your observation

```
a = torch.ones(5)
print(a)
b = a.numpy()
print(b)
```

What are the types of a and b?

12. Let us add one to the first element of the tensor a from the previous question and report the new values of a and b.

```
a[0] += 1
print(a)
print(b)
```

Do they match? Do they share their underlying memory locations?

13. Compare the effect of each of these three instructions separately:

```
a.add_(1)
a[:] += 1
a = a.add(1)
```

For each of them, report the new values of a and b. What are the similarities and differences?

14. Let us study the reverse operation, converting NumPy arrays to a Torch tensor. Run the following code and examine the output.

```
a = np.ones(5)
b = torch.from_numpy(a)
np.add(a, 1, out=a)
print(a)
print(b)
```

All the Torch tensors on the CPU (except a CharTensor) support converting to NumPy and back.

15. Torch tensors can be moved onto GPU device's memory using the .cuda method and back to CPU device with .cpu method. Run the following script

```
x = torch.randn(5, 3)
y = torch.randn(5, 3)
if torch.cuda.is_available():
    x = x.cuda()
    y = y.cuda()
z = x + y
print(z)
if torch.cuda.is_available():
    print (z.cpu())
```

Interpret each of these instructions. Would this program produce the same result if it was run on a CPU-only architecture?

16. Run and interpret the result of the following two instructions

```
print(z.cpu().numpy())
print(z.numpy())
```

Note that moving data from CPU to GPU is slow, so try to do all the computations in GPU, and transfer the data back to CPU once all computations have been performed. Make sure your program produces the same result whether it is run on an architecture with GPU capabilities or not (you can start a pod without GPU capabilities by running launch-pytorch.sh instead). Note also that newer versions of PyTorch come with more advanced tools for manipulating GPU/CPU devices.

6 Autograd: automatic differentiation

A central package in PyTorch is the autograd package. It provides tools performing automatic differentiation for all operations based on Torch tensors. This means that the gradients of such operations will not require to be explicitly programmed. It uses a define-by-run framework that computes these gradients dynamically during runtime. This is really useful for backprop algorithm, since autograd will deduce automatically from the succession of forward operations what are the corresponding backward updates.

The class torch.autograd.Variable is the central class of the package. It wraps a Torch tensor in another class that stores a flag requires_grad. If you set its attribute .requires_grad as True, it starts to track all operations where it is involved. When you finish your computation you can call .backward() and have all the gradients computed automatically. The gradient for this tensor will be accumulated into .grad attribute of the variable that it has been wrapped into.

17. Run the following script

```
import torch.autograd as ag
x = ag.Variable(torch.ones(2, 2), requires_grad=True)
print(x)
y = x + 2
print(y)
```

What is the type of y?

18. Run the following script

```
z = y * y * 3
f = z.mean()
print(z, f)
```

Inspect the results and write the equation linking f with the four entries x_1, x_2, x_3, x_4 of x:

$$f = f(x_1, x_2, x_3, x_4)$$

19. Because the variable f contains a single scalar, we can now back-propagate the gradient of f with respect to x into the variable x as

```
f.backward() # That's it!
```

Report what the gradient $\nabla_{x} f(x) = \left(\frac{\partial f(x)}{\partial x}\right)^{T}$ is.

Hint: read the introduction to this section to recall where the gradient for tensor x is stored.

20. Based on question 18, try to figure out mathematically if autograd produces the correct answer by deriving, yourself, the partial derivatives for each x_i :

$$(\nabla_{\boldsymbol{x}} f(\boldsymbol{x}))_i = \frac{\partial f(x_1, x_2, x_3, x_4)}{\partial x_i}$$

7 MNIST Data preparation

- 21. Reuse the code from Assignment #2 to load and normalize MNIST testing and training data.
- 22. Torch expects that the input of a convolutional layer is stored in the following format

```
Batch size \times Number of input channels \times Image width \times Image height
```

The number of input channels in our case is 1 because MNIST is composed of grayscale images. It would have been 3 if the images were in RGB color. In deeper layers, the number of input channels will be the number of input feature maps. Reorganise the tensors xtrain and xtest accordingly.

Hint: Reshape them first with shape (28, 28, 1, 60000) and (28, 28, 1, 10000) respectively and then use np.moveaxis.

23. Check that your data are well reorganized by making sure that

```
import matplotlib as pyplot
MNISTtools.show(xtrain[42, 0, :, :])
```

display a digit that indeed corresponds to ltrain[42].

24. Now as studied in the previous section, we would like to convert these into autograd variable objects so that we can apply gradient propagation on them. Complete the following:

```
xtrain = COMPLETE
ltrain = COMPLETE
xtest = ag.Variable(torch.from_numpy(xtest), requires_grad=False)
```

Hint: convert them into Torch tensors before wrapping them to autograd variables.

8 Convolutional Neural Network (CNN) for MNIST classification

Neural networks can be constructed using the torch.nn package, which relies on autograd differentiation tools. This package provides an implementation of CNNs (introduced in Section 1) as follows:

- Convolutional layers can be created as nn.Conv2d(N, C, K). For input images of size $W \times H$, the output feature maps have size $[W-K+1] \times [H-K+1]$.
- In PyTorch, maxpooling is implemented like any other non-linear function (such as ReLU or softmax). For input images of size $W \times H$, the output feature maps have size $[W/L] \times [H/L]$.
- A fully connected layer can be created as nn.Linear(M, N).
- 25. Our LeNet network will be composed successively of
 - (a) a convolutional layer connecting the input image to 6 feature maps with 5×5 convolutions (K = 5) and followed by ReLU and maxpooling,

- (b) a convolutional layer connecting the 6 input channels to 16 output channels with 5×5 convolutions and followed by ReLU and maxpooling,
- (c) a fully-connected layer connecting 16 feature maps to 120 output units and followed by ReLU,
- (d) a fully-connected layer connecting 120 inputs to 84 output units and followed by ReLU,
- (e) a final linear layer connecting 84 inputs to 10 linear outputs (one for each of our digits).

Determine the size of the feature maps after each convolution and maxpooling operation. How many input units have the third layer?

26. Interpret and complete the following code initializing our LeNet network

```
import torch.nn as nn
import torch.nn.functional as F
# This is our neural networks class that inherits from nn.Module
class LeNet(nn.Module):
    # Here we define our network structure
    def __init__(self):
        super(LeNet, self).__init__()
        self.conv1 = nn.Conv2d(1, 6, 5).double()
        self.conv2 = COMPLETE
        self.fc1 = COMPLETE
        self.fc2 = nn.Linear(120, 84).double()
        self.fc3 = nn.Linear(84, 10).double()
    # Here we define one forward pass through the network
    def forward(self, x):
        x = F.max_pool2d(F.relu(self.conv1(x)), (2, 2))
        x = COMPLETE
        x = x.view(-1, self.num_flat_features(x))
        x = COMPLETE
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x
    # Determine the number of features in a batch of tensors
    def num_flat_features(self, x ):
        size = x.size()[1:]
        return np.prod(size)
net = LeNet()
print(net)
```

Note that you just have to define the forward function, and the backward function (where gradients are computed) will be automatically defined for you using autograd. You can use any of the Torch tensor operations in the forward function. For more details, please refer to https://pytorch.org/docs/master/nn.html.

27. The learnable parameters of a model are returned by net.parameters(). Run the following and interpret the results:

```
params = list(net.parameters())
for i in range(len(params)):
    print(i, params[i].size())
```

What are the parameters corresponding to indices 0 and 2? 4, 6, and 8? odd indices?

28. To run a forward pass of your initial network over your testing set, simply run:

```
yinit = net(xtest)
which is equivalent to yinit = net.forward(xtest). Run the following and interpret the result
print(100 * np.mean(ltest == yinit.data.numpy().T.argmax(axis=0)))
```

29. We will use (Mini-Batch) Stochastic Gradient Descent (SGD) with cross-entropy and momentum. Complete the following section that sets up all parameters:

```
N
          = xtrain.size()[0]
                             # Training set size
В
          = 100
                                # Minibacth size
         = COMPLETE
                               # Number of minibatches
          = 10
                                # Number of epochs
         = .001
                                # learning rate
gamma
          = .9
                                # momentum
rho
criterion = nn.CrossEntropyLoss()
optimizer = torch.optim.SGD(net.parameters(),
                            lr=COMPLETE.
                            momentum = COMPLETE)
```

For more details, refer to https://pytorch.org/docs/0.3.1/nn.html and https://pytorch.org/docs/0.3.1/optim.html. Note that PyTorch's CrossEntropyLoss is the composition of a soft-max activation with the standard cross-entropy loss.

30. We have everything ready now to train our model with SGD and backprop. Complete each part in the piece of code below

```
for epoch in range(T):
    running_loss = 0.0
    idxminibatches = np.random.permutation(NB) # shuffling
    for k in range(NB):
        i = idxminibatches[k] # index of minibatch

# Extract i-th minibatch from xtrain and ltrain
    idxsmp = COMPLETE # indices of samples for i-th minibatch
    inputs = xtrain[COMPLETE]
    labels = ltrain[COMPLETE]

# Initialize the gradients to zero
    optimizer.zero_grad()
```

Again, refer to https://pytorch.org/docs/0.3.1/nn.html and https://pytorch.org/docs/0.3.1/optim.html for more details. It may take about an hour. The loss per minibatch should decay as 2.30, 2.29, 2.27, 2.25, 2.18, 1.96, 1.44, 0.88, ... until 0.08. If it does not, you may have a bug, then you can interrupt it by pressing Esc+I+I. You may also interrupt it and move to the next question if you are impatient.

- 31. Modify your code (Q24 and 26) such that all tensors and layers are moved to GPU and rerun. Make sure your code remains CPU compatible. The learning should run in less than 20 seconds!
- 32. Re-evaluate the predictions of your trained network on the testing dataset. By how much did the accuracy improve?

9 Bonus

- 33. Play around with the learning rate, momentum, batch size and number of epochs. How do they affect loss and training?
- 34. To prevent over-fitting, implement early stopping by using 10% of the training data for validation.
- 35. Instead of printing the training loss every 100 updates, plot the graphs for training, validation and test losses with respect to the number of epochs. It's very important that you visualize these plots to get a better understanding.
- 36. Try using different optimizers learned in class. Report your observations. For more details, refer to https://pytorch.org/docs/0.3.1/optim.html.
- 37. To get even better performance, the original LeNet-5 network was trained based on data-augmentation. The training set was artificially enlarged by generating several 32×32 images that were randomly shifted and/or rescaled versions of each 28×28 image. Implement this technique and evaluate its performance.