

| | |
|--------------|--------------------------------------|
| Started on | Wednesday, 4 December 2024, 10:49 AM |
| State | Finished |
| Completed on | Wednesday, 4 December 2024, 11:29 AM |
| Time taken | 40 mins 1 sec |
| Marks | 15.00/20.00 |
| Grade | 7.50 out of 10.00 (75%) |

Question 1

Complete

Mark 1.00 out of 1.00

Let f be the function satisfying $f'(x) = x\sqrt{f(x)}$ for all real numbers x , where $f(3) = 25$. Find $f''(3)$

- A. 19/2
- B. 9/2
- C. 5
- D. 53/10

Select one:

- ☐ a. D
- ☐ b. C
- ☒ c. A
- ☐ d. B

Question 2

Complete

Mark 1.00 out of 1.00

Find g if

$$g''(x) = 24x - 4$$

and

$$g(0) = g'(0) = 7.$$

Select one:

- ☐ a. None of the others
- ☒ b. $g(x) = 4x^3 - 2x^2 + 7x + 7$
- ☐ c. $g(x) = 4x^3 + 2x^2 + x + 7$
- ☐ d. $g(x) = 2x^3 - x^2 + 7x + 1$

Question **3**

Complete

Mark 1.00 out of 1.00

A ladder 25 ft long rests against a vertical wall. If the bottom of the ladder slides away from the wall at a rate of 5 ft/s, how fast is the top of the ladder sliding down the wall when the bottom of the ladder is 16 ft from the wall?

A. $4/3$ ft/sB. $9/4$ ft/s

C. 4ft/s

D. 1 ft/s

Select one:

☐ a. A☐ b. B☒ c. C☐ d. D

Question **4**

Complete

Mark 1.00 out of 1.00

For $a \neq 0$, find the limit $\lim_{x \rightarrow a} \frac{x^2 - a^2}{x^4 - a^4}$

A. 0

B. $\frac{1}{a^2}$ C. $\frac{1}{2a^2}$ D. $\frac{1}{6a^2}$

Select one:

- ☐ a. B
- ☐ b. A
- ☒ c. C
- ☐ d. D

Question **5**

Complete

Mark 0.00 out of 1.00

Suppose $g(x) = f(x) + f(-x)$, where $f(x)$ is a function defined on \mathbb{R} . Then:

Select one:

- ☐ a. g is an even function.
- ☐ b. if f is odd, then so g is.
- ☒ c. g is an odd function.
- ☐ d. None of the others

Question **6**

Complete

Mark 0.00 out of 1.00

What is $\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{\tan x}$?

A. -1

B. 0

C. 1

D. 2

Select one:

☐ a. C☒ b. B☐ c. A☐ d. D

Question 7

Complete

Mark 1.00 out of 1.00

If $\lim_{x \rightarrow 0} \frac{f(x)}{x^2} = 5$. Find the limit (if any) $\lim_{x \rightarrow 0} \frac{f(x)}{x}$

A. -5

B. 5

C. 0

D. None of the others

Select one:

☐ a. D☒ b. C☐ c. A☐ d. B

Question 8

Complete

Mark 1.00 out of 1.00

If $f(x) = \frac{4}{x-1}$ and $g(x) = 2x$, then the solution set of $f(g(x)) = g(f(x))$ is

A. $\left\{\frac{1}{3}, 2\right\}$

B. $\{3\}$

C. $\left\{\frac{1}{3}\right\}$

D. $\{2\}$

Select one:

☐ a. D☐ b. A☒ c. C☐ d. B

Question 9

Complete

Mark 0.00 out of 1.00

$$\text{Let } f(x) = \begin{cases} \frac{\sqrt{1+x^2}-1}{x^2}, & x \neq 0 \\ m, & x = 0 \end{cases}. \text{ Find the constant } m \text{ that makes } f \text{ continuous on } \mathbb{R}$$

A. 0

B. 1/2

C. 1/3

D. None of the others

Select one:

- ☐ a. D
☒ b. A
☐ c. C
☐ d. B

Question **10**

Complete

Mark 1.00 out of 1.00

A particle moves in a straight line and has acceleration given by $a(t) = 6t + 4$. Its initial velocity is $v(0) = -6$ cm/s and its initial displacement is $s(0) = 9$ cm. Find its position function $s(t)$

A. $s(t) = t^3 + 2t^2 - 6t$

B. $s(t) = t^3 + 2t^2 - 6t + 9$

C. $s(t) = t^3 + 2t^2 + 9$

D. $s(t) = s(t) = t^3 + 2t^2 + 6t + 9$

Select one:

- ☒ a. B
☐ b. C
☐ c. D
☐ d. A

Question **11**

Complete

Mark 1.00 out of 1.00

Find the most general anti-derivative of the function $f(x) = e^x - \frac{2}{\sqrt{x}}$

A. $F(x) = e^x - 2\sqrt{x} + C$

B. $F(x) = e^x - \frac{2}{x\sqrt{x}} + C$

C. $F(x) = e^x - 4\sqrt{x} + C$

D. $F(x) = e^x - \sqrt{x} + C$

Select one:

- ☐ a. A
- ☐ b. B
- ☒ c. C
- ☐ d. D

Question **12**

Complete

Mark 1.00 out of 1.00

Let f and g be differentiable functions such that $f(1) = 2$, $f'(1) = 3$, $f'(2) = -4$

$g(1) = 2$, $g'(1) = -3$, $g'(2) = 5$. If $h(x) = f(g(x))$, then $h'(1) =$

A. -9 B. -4 C. 12 D. 15

Select one:

- ☐ a. A
☐ b. D
☒ c. C
☐ d. B

Question **13**

Complete

Mark 1.00 out of 1.00

Find absolute min value of $f(x) = x^2(1-x)^3$ on $[0;2]$

A. -4 B. 0 C. -3/2 D. -2

Select one:

- ☐ a. C
☐ b. B
☒ c. A
☐ d. D

Question **14**

Complete

Mark 1.00 out of 1.00

Use Newton's Method with initial approximation $x_1 = 1$ to find x_3 , the third approximation to the root of the equation $x^3 + x - 3 = 0$. Which is the result correct to 2 decimal places?

Select one:

- ☐ a. 1.23
- ☐ b. 1.31
- ☒ c. 1.21
- ☐ d. 1.25
- ☐ e. None of the others

Newton's method for finding the root of a function $f(x) = 0$.

from x_1 , compute x_2 ,

from x_2 compute x_3 ,

from x_3 compute x_4 ,

How to compute? use the formula $x_{n+1} = x_n - f(x_n)/f'(x_n)$

Question **15**

Complete

Mark 0.00 out of 1.00

Let f be the function defined by the following:

$$f(x) = \begin{cases} \sin x, & x < 0 \\ x^2, & 0 \leq x < 1 \\ 2 - x, & 1 \leq x < 2 \\ x - 3, & 2 \leq x \end{cases}$$

For what values of x is f not continuous?

A. 2 only B. 1 only C. 0 and 2 only D. 0, 1 and 2

Select one:

- ☐ a. A
☐ b. C
☐ c. D
☒ d. B

Question **16**

Complete

Mark 1.00 out of 1.00

Let $f(x) = x^3 \sqrt{(x-2)^2}$. Find all values of c such that $f'(c) = 0$

A. 0 B. 1 C. $6/5$ D. 2

Select one:

- ☒ a. C
☐ b. A
☐ c. D
☐ d. B

Question **17**

Complete

Mark 1.00 out of 1.00

Find the x-coordinate of the points of inflection of the function $y = x^3 - 9x^2 + 17x - 11$.

Select one:

- ☐ a. 1 and -1
- ☐ b. 0
- ☒ c. 3
- ☐ d. 1

Question **18**

Complete

Mark 1.00 out of 1.00

If $3x^2 + 2xy + y^2 = 2$, then the value of dy/dx at $x = 1$ is

A. -2 B. 2 C. 0 D. Not defined

Select one:

- ☒ a. D
☐ b. B
☐ c. C
☐ d. A

Question 19

Complete

Mark 0.00 out of 1.00

Find an equation of tangent to the curve $y = \frac{\sqrt{x}}{x^2 + 1}$ at $x = 1$

A. $y = -\frac{1}{4}x + \frac{3}{4}$

B. $y = \frac{1}{4}x + \frac{1}{4}$

C. $y = x - \frac{1}{2}$

D. $y = 4x - \frac{7}{2}$

Select one:

- ☐ a. A
- ☒ b. B
- ☐ c. D
- ☐ d. C

Question **20**

Complete

Mark 1.00 out of 1.00

A particle moves in the straight line with **position function** $s(t) = t^3 - 3t^2 + 11$, find its **velocity** when $t = 3$.

Select one:

- ☐ a. 7
- ☐ b. 12
- ☐ c. 3
- ☒ d. 9

